

Supplementary material for

High-pressure phase transition and equation of state of hydrous Al-bearing silica

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Table S1. Details for the high-pressure experiments performed in this study.

| Label | Sample(s) | Culet (μm) | Pressure medium | <i>P</i> range (GPa) | Technique |
|-------|-----------|----------------------------|--------------------|-------------------------|-----------|
| DACX | Al5, Al11 | 350 | He | 0-50.13(4) | XRD |
| DAC1 | Al5 | 400 | Ne | 0-10.9(1) | Raman |
| DAC2 | Al5 | 400 | He | 0-9.4(1) | Raman |
| DAC3 | Al5 | 400 | He | 0-38.2(1) | Raman |
| DAC4 | Al11 | 250 | He | 0-44.30(3) | Raman |

Table S2. Unit-cell lattice parameters of Al5 as a function of pressure. P is calculated as the average value between pressure measured before and after XRD measurements using the ruby fluorescence shift (Shen et al. 2020), and σP is the semi-difference between the two values. Errors on the cell parameters represent one standard deviation.

| P (GPa) | σ_P (GPa) | a (Å) | σ_a (Å) | b (Å) | σ_b (Å) | c (Å) | σ_c (Å) | V (Å ³) | σ_V (Å ³) |
|--------------|---------------------|------------|-------------------|------------|-------------------|------------|-------------------|--------------------------|---------------------------------|
| 1.06 | 0.02 | 4.1940 | 0.0001 | | | 2.6714 | 0.0001 | 46.988 | 0.003 |
| 3.23 | 0.04 | 4.1813 | 0.0001 | | | 2.6679 | 0.0001 | 46.644 | 0.003 |
| 6.02 | 0.02 | 4.1667 | 0.0001 | | | 2.6634 | 0.0001 | 46.239 | 0.003 |
| 7.86 | 0.02 | 4.1573 | 0.0001 | | | 2.6603 | 0.0001 | 45.979 | 0.003 |
| 9.13 | 0.02 | 4.1515 | 0.0001 | | | 2.6580 | 0.0001 | 45.810 | 0.003 |
| 10.78 | 0.02 | 4.1440 | 0.0002 | | | 2.6554 | 0.0001 | 45.599 | 0.003 |
| 12.33 | 0.02 | 4.1374 | 0.0001 | | | 2.6524 | 0.0001 | 45.403 | 0.003 |
| 13.86 | 0.03 | 4.1311 | 0.0002 | | | 2.6498 | 0.0001 | 45.222 | 0.003 |
| 16.09 | 0.02 | 4.1309 | 0.0003 | 4.1125 | 0.0003 | 2.6459 | 0.0001 | 44.949 | 0.005 |
| 17.32 | 0.03 | 4.1275 | 0.0002 | 4.1045 | 0.0003 | 2.6438 | 0.0001 | 44.789 | 0.005 |
| 19.10 | 0.04 | 4.1237 | 0.0002 | 4.0902 | 0.0003 | 2.6413 | 0.0001 | 44.550 | 0.005 |
| 20.30 | 0.03 | 4.1187 | 0.0002 | 4.0863 | 0.0003 | 2.6392 | 0.0001 | 44.418 | 0.005 |
| 21.75 | 0.03 | 4.1173 | 0.0002 | 4.0718 | 0.0004 | 2.6368 | 0.0001 | 44.205 | 0.005 |
| 23.57 | 0.07 | 4.1135 | 0.0002 | 4.0597 | 0.0004 | 2.6338 | 0.0001 | 43.983 | 0.005 |
| 25.56 | 0.03 | 4.1094 | 0.0002 | 4.0470 | 0.0004 | 2.6305 | 0.0001 | 43.747 | 0.005 |
| 28.02 | 0.05 | 4.1040 | 0.0002 | 4.0345 | 0.0004 | 2.6259 | 0.0001 | 43.479 | 0.005 |
| 29.00 | 0.02 | 4.1019 | 0.0002 | 4.0280 | 0.0003 | 2.6245 | 0.0001 | 43.364 | 0.004 |
| 30.51 | 0.03 | 4.0985 | 0.0002 | 4.0200 | 0.0003 | 2.6212 | 0.0001 | 43.185 | 0.004 |
| 32.21 | 0.04 | 4.0946 | 0.0002 | 4.0106 | 0.0003 | 2.6178 | 0.0001 | 42.989 | 0.004 |
| 33.79 | 0.03 | 4.0910 | 0.0002 | 4.0031 | 0.0003 | 2.6149 | 0.0001 | 42.824 | 0.004 |
| 35.72 | 0.04 | 4.0865 | 0.0002 | 3.9940 | 0.0003 | 2.6114 | 0.0001 | 42.622 | 0.004 |
| 38.02 | 0.04 | 4.0821 | 0.0002 | 3.9833 | 0.0003 | 2.6071 | 0.0001 | 42.391 | 0.004 |
| 40.04 | 0.03 | 4.0780 | 0.0002 | 3.9729 | 0.0003 | 2.6036 | 0.0001 | 42.183 | 0.004 |
| 41.87 | 0.03 | 4.0751 | 0.0002 | 3.9646 | 0.0003 | 2.6001 | 0.0001 | 42.007 | 0.004 |
| 43.83 | 0.02 | 4.0714 | 0.0002 | 3.9552 | 0.0003 | 2.5968 | 0.0001 | 41.816 | 0.004 |
| 45.69 | 0.03 | 4.0680 | 0.0002 | 3.9469 | 0.0003 | 2.5938 | 0.0001 | 41.645 | 0.004 |
| 48.21 | 0.04 | 4.0650 | 0.0002 | 3.9363 | 0.0003 | 2.5889 | 0.0001 | 41.425 | 0.004 |
| 50.13 | 0.04 | 4.0610 | 0.0002 | 3.9268 | 0.0003 | 2.5856 | 0.0001 | 41.232 | 0.004 |

Table S3. Unit-cell lattice parameters of Al11 as a function of pressure. P is calculated as the average value between pressure measured before and after XRD measurements using the ruby fluorescence shift (Shen et al., 2020), and σP is the semi-difference between the two values. Errors on the cell parameters represent one standard deviation.

| P (GPa) | σ_P (GPa) | a (Å) | σ_a (Å) | b (Å) | σ_b (Å) | c (Å) | σ_c (Å) | V (Å ³) | σ_V (Å ³) |
|--------------|---------------------|------------|-------------------|------------|-------------------|------------|-------------------|--------------------------|---------------------------------|
| 1.06 | 0.02 | 4.2500 | 0.0002 | 4.1762 | 0.0003 | 2.6799 | 0.0001 | 47.566 | 0.004 |
| 3.23 | 0.04 | 4.2380 | 0.0002 | 4.1606 | 0.0002 | 2.6766 | 0.0001 | 47.196 | 0.004 |
| 6.02 | 0.02 | 4.2241 | 0.0002 | 4.1424 | 0.0002 | 2.6718 | 0.0001 | 46.752 | 0.004 |
| 7.86 | 0.02 | 4.2154 | 0.0002 | 4.1313 | 0.0002 | 2.6684 | 0.0001 | 46.470 | 0.004 |
| 9.13 | 0.02 | 4.2106 | 0.0002 | 4.1220 | 0.0002 | 2.6663 | 0.0001 | 46.277 | 0.004 |
| 10.78 | 0.02 | 4.2039 | 0.0002 | 4.1126 | 0.0002 | 2.6632 | 0.0001 | 46.043 | 0.003 |
| 12.33 | 0.02 | 4.1979 | 0.0002 | 4.1036 | 0.0002 | 2.6608 | 0.0001 | 45.837 | 0.004 |
| 13.86 | 0.03 | 4.1923 | 0.0002 | 4.0949 | 0.0002 | 2.6576 | 0.0001 | 45.623 | 0.003 |
| 16.09 | 0.02 | 4.1838 | 0.0002 | 4.0820 | 0.0002 | 2.6535 | 0.0001 | 45.317 | 0.003 |
| 17.32 | 0.03 | 4.1801 | 0.0002 | 4.0751 | 0.0002 | 2.6511 | 0.0001 | 45.160 | 0.004 |
| 19.10 | 0.04 | 4.1750 | 0.0002 | 4.0647 | 0.0002 | 2.6482 | 0.0001 | 44.941 | 0.003 |
| 20.30 | 0.03 | 4.1708 | 0.0002 | 4.0588 | 0.0002 | 2.6461 | 0.0001 | 44.795 | 0.003 |
| 21.75 | 0.03 | 4.1667 | 0.0002 | 4.0501 | 0.0002 | 2.6433 | 0.0001 | 44.607 | 0.004 |
| 23.57 | 0.07 | 4.1610 | 0.0002 | 4.0415 | 0.0002 | 2.6398 | 0.0001 | 44.391 | 0.003 |
| 25.56 | 0.03 | 4.1548 | 0.0002 | 4.0314 | 0.0002 | 2.6360 | 0.0001 | 44.152 | 0.003 |
| 28.02 | 0.05 | 4.1483 | 0.0002 | 4.0190 | 0.0002 | 2.6319 | 0.0001 | 43.879 | 0.003 |
| 29.00 | 0.02 | 4.1440 | 0.0002 | 4.0138 | 0.0002 | 2.6294 | 0.0001 | 43.734 | 0.004 |
| 30.51 | 0.03 | 4.1399 | 0.0002 | 4.0067 | 0.0002 | 2.6268 | 0.0001 | 43.572 | 0.003 |
| 32.21 | 0.04 | 4.1358 | 0.0002 | 3.9987 | 0.0002 | 2.6236 | 0.0001 | 43.389 | 0.003 |
| 33.79 | 0.03 | 4.1316 | 0.0002 | 3.9915 | 0.0002 | 2.6207 | 0.0001 | 43.219 | 0.003 |
| 35.72 | 0.04 | 4.1265 | 0.0002 | 3.9828 | 0.0002 | 2.6172 | 0.0001 | 43.014 | 0.003 |
| 38.02 | 0.04 | 4.1209 | 0.0002 | 3.9726 | 0.0002 | 2.6132 | 0.0001 | 42.780 | 0.003 |
| 40.04 | 0.03 | 4.1162 | 0.0002 | 3.9638 | 0.0001 | 2.6095 | 0.0001 | 42.575 | 0.003 |
| 41.87 | 0.03 | 4.1118 | 0.0002 | 3.9564 | 0.0001 | 2.6063 | 0.0001 | 42.399 | 0.003 |
| 43.83 | 0.02 | 4.1073 | 0.0002 | 3.9485 | 0.0002 | 2.6028 | 0.0001 | 42.210 | 0.003 |
| 45.69 | 0.03 | 4.1034 | 0.0002 | 3.9409 | 0.0002 | 2.5994 | 0.0001 | 42.034 | 0.003 |
| 48.21 | 0.04 | 4.098 | 0.0002 | 3.9315 | 0.0002 | 2.5949 | 0.0001 | 41.806 | 0.003 |
| 50.13 | 0.04 | 4.0938 | 0.0002 | 3.9239 | 0.0002 | 2.5916 | 0.0001 | 41.631 | 0.003 |

Table S4. Observed Raman shifts of B_{1g} (stishovite) and A_g (CaCl_2 -type phase) optic modes of Al5 (DAC1, DAC2, DAC3) as a function of pressure. Error on the peak position represent one standard deviation. P is calculated as the average value between pressure measured before and after Raman spectroscopy measurements using the ruby fluorescence shift (Shen et al. 2020), and σP is the semi-difference between the two values. Asterisks next to P values indicate measurements performed during decompression.

| P (GPa) | σP (GPa) | ω (cm^{-1}) | $\sigma \omega$ (cm^{-1}) |
|--------------|---------------------|----------------------------------|---|
| DAC1 | | | |
| 0 | | 224.99 | 0.09 |
| 1.3 | 0.1 | 224.01 | 0.07 |
| 3.5 | 0.1 | 220.86 | 0.04 |
| 5.4 | 0.1 | 220.24 | 0.11 |
| 6.6 | 0.1 | 218.67 | 0.06 |
| 7.7 | 0.1 | 217.91 | 0.07 |
| 9.7 | 0.2 | 216.3 | 0.04 |
| 10.9 | 0.1 | 216.42 | 0.09 |
| 9.6* | 0.1 | 216.71 | 0.15 |
| 4.1* | 0.1 | 220.71 | 0.05 |
| DAC2 | | | |
| 0 | | 224.49 | 0.06 |
| 4.0 | 0.2 | 221.57 | 0.08 |
| 6.6 | 0.1 | 219.01 | 0.05 |
| 9.4 | 0.1 | 217.75 | 0.06 |
| DAC3 | | | |
| 0 | | 225.18 | 0.03 |
| 3.4 | 0.1 | 221.69 | 0.06 |
| 6.7 | 0.1 | 219.05 | 0.04 |
| 9.7 | 0.1 | 216.81 | 0.04 |
| 11.0 | 0.1 | 215.05 | 0.05 |
| 13.6 | 0.1 | 212.59 | 0.05 |
| 14.8 | 0.1 | 211.63 | 0.1 |
| 17.4 | 0.1 | 209.66 | 0.05 |
| 18.65 | 0.1 | 208.64 | 0.12 |
| 20.3 | 0.2 | 207.17 | 0.05 |
| 21.4 | 0.1 | 206.73 | 0.06 |
| 22.5 | 0.1 | 206.47 | 0.08 |
| 24.1 | 0.1 | 205.71 | 0.06 |
| 24.7 | 0.1 | 204.34 | 0.08 |
| 25.6 | 0.1 | 205.95 | 0.19 |
| 26.9 | 0.1 | 206.41 | 0.11 |
| 28.5 | 0.1 | 206.57 | 0.11 |
| 29.6 | 0.1 | 205.05 | 0.11 |
| 31.2 | 0.1 | 206.96 | 0.15 |
| 33.0 | 0.2 | 210.7 | 0.3 |

| | | | |
|-------|-----|--------|------|
| 34.9 | 0.1 | 207.86 | 0.06 |
| 36.3 | 0.2 | 212.15 | 0.06 |
| 38.2 | 0.2 | 213.92 | 0.07 |
| 26.7* | 0.2 | 206.73 | 0.08 |

Table S5. Observed Raman shifts of the A_g (CaCl_2 -type phase) optic mode of Al11 (DAC4) as a function of pressure. Error on the peak position represent one standard deviation. P is calculated as the average value between pressure measured before and after Raman spectroscopy measurements using the ruby fluorescence shift (Shen et al. 2020), and σP is the semi-difference between the two values. Asterisks next to P values indicate measurements performed during decompression.

| P (GPa) | σP (GPa) | ω (cm^{-1}) | σ_ω (cm^{-1}) |
|--------------|---------------------|----------------------------------|---|
| DAC4 | | | |
| 0 | | 226.91 | 0.03 |
| 0.14 | 0.02 | 226.39 | 0.06 |
| 0.38 | 0.02 | 225.99 | 0.05 |
| 1.45 | 0.10 | 225.44 | 0.04 |
| 2.22 | 0.03 | 225.57 | 0.04 |
| 2.79 | 0.03 | 225.53 | 0.04 |
| 3.24 | 0.02 | 225.25 | 0.03 |
| 3.48 | 0.02 | 225.84 | 0.07 |
| 3.48 | 0.02 | 226.00 | 0.05 |
| 4.23 | 0.02 | 224.64 | 0.05 |
| 5.22 | 0.02 | 224.73 | 0.03 |
| 5.65 | 0.02 | 224.66 | 0.04 |
| 6.28 | 0.02 | 224.52 | 0.04 |
| 7.10 | 0.02 | 224.29 | 0.03 |
| 7.10 | 0.02 | 223.76 | 0.03 |
| 8.16 | 0.03 | 224.10 | 0.03 |
| 8.79 | 0.02 | 224.16 | 0.03 |
| 9.43 | 0.05 | 224.05 | 0.03 |
| 15.97 | 0.03 | 223.66 | 0.03 |
| 17.17 | 0.06 | 222.91 | 0.02 |
| 24.60 | 0.10 | 225.80 | 0.05 |
| 26.87 | 0.11 | 231.18 | 0.34 |
| 28.24 | 0.07 | 235.32 | 0.31 |
| 32.17 | 0.02 | 244.46 | 0.14 |
| 36.69 | 0.07 | 250.32 | 0.21 |
| 41.65 | 0.09 | 262.70 | 0.10 |
| 44.30 | 0.03 | 265.31 | 0.14 |
| 43.74* | 0.02 | 262.56 | 0.13 |
| 42.95* | 0.02 | 262.69 | 0.09 |
| 40.44* | 0.02 | 253.05 | 0.16 |
| 35.50* | 0.03 | 249.00 | 0.09 |
| 32.9* | 0.2 | 241.32 | 0.19 |
| 25.0* | 0.5 | 225.98 | 0.08 |
| 22.2* | 0.8 | 224.55 | 0.06 |
| 20.7* | 0.5 | 224.41 | 0.05 |

Table S6. Fractional atomic coordinates of oxygen and symmetry breaking mode $\Gamma 2+$ as a function of pressure. P is calculated as the average value between pressure measured before and after XRD measurements, and σP is the semi-difference between the two values. Errors on the fractional atomic coordinates represent one standard deviation.

| P | σP | $x(\text{O})$ | $\sigma_{x(\text{O})}$ | $y(\text{O})$ | $\sigma_{y(\text{O})}$ | $\Gamma 2+$ |
|-------|------------|---------------|------------------------|---------------|------------------------|-------------|
| 1.06 | 0.02 | 0.3059 | 0.0003 | | | 0 |
| 3.23 | 0.04 | 0.3056 | 0.0003 | | | 0 |
| 6.02 | 0.02 | 0.3053 | 0.0003 | | | 0 |
| 7.86 | 0.02 | 0.3052 | 0.0002 | | | 0 |
| 9.13 | 0.02 | 0.3051 | 0.0003 | | | 0 |
| 10.78 | 0.02 | 0.3052 | 0.0002 | | | 0 |
| 12.33 | 0.02 | 0.3054 | 0.0002 | | | 0 |
| 13.86 | 0.03 | 0.3054 | 0.0002 | | | 0 |
| 16.09 | 0.02 | 0.3056 | 0.0003 | 0.6977 | 0.0006 | 0.0192 |
| 19.10 | 0.04 | 0.3081 | 0.0004 | 0.7007 | 0.0004 | 0.0215 |
| 21.75 | 0.03 | 0.3091 | 0.0005 | 0.6999 | 0.0011 | 0.0522 |
| 25.56 | 0.03 | 0.3111 | 0.0003 | 0.7034 | 0.0007 | 0.0839 |
| 28.02 | 0.05 | 0.3115 | 0.0004 | 0.7049 | 0.0008 | 0.0947 |
| 29.00 | 0.02 | 0.3122 | 0.0004 | 0.7045 | 0.0008 | 0.0963 |
| 30.51 | 0.03 | 0.3126 | 0.0003 | 0.7161 | 0.0007 | 0.1078 |
| 32.21 | 0.04 | 0.3125 | 0.0009 | 0.7055 | 0.0021 | 0.1019 |
| 33.79 | 0.03 | 0.3137 | 0.0004 | 0.7079 | 0.0007 | 0.1242 |
| 35.72 | 0.04 | 0.3142 | 0.0003 | 0.7085 | 0.0006 | 0.1303 |
| 38.02 | 0.04 | 0.3149 | 0.0003 | 0.7094 | 0.0006 | 0.1393 |
| 40.04 | 0.03 | 0.3158 | 0.0003 | 0.7104 | 0.0006 | 0.1506 |
| 41.87 | 0.03 | 0.3162 | 0.0002 | 0.7116 | 0.0005 | 0.159 |
| 43.83 | 0.02 | 0.3168 | 0.0003 | 0.7118 | 0.0006 | 0.1634 |
| 45.69 | 0.03 | 0.3171 | 0.0003 | 0.7135 | 0.0007 | 0.174 |
| 48.21 | 0.04 | 0.3184 | 0.0003 | 0.7145 | 0.0007 | 0.1875 |
| 50.13 | 0.04 | 0.3187 | 0.0003 | 0.7150 | 0.0006 | 0.1918 |

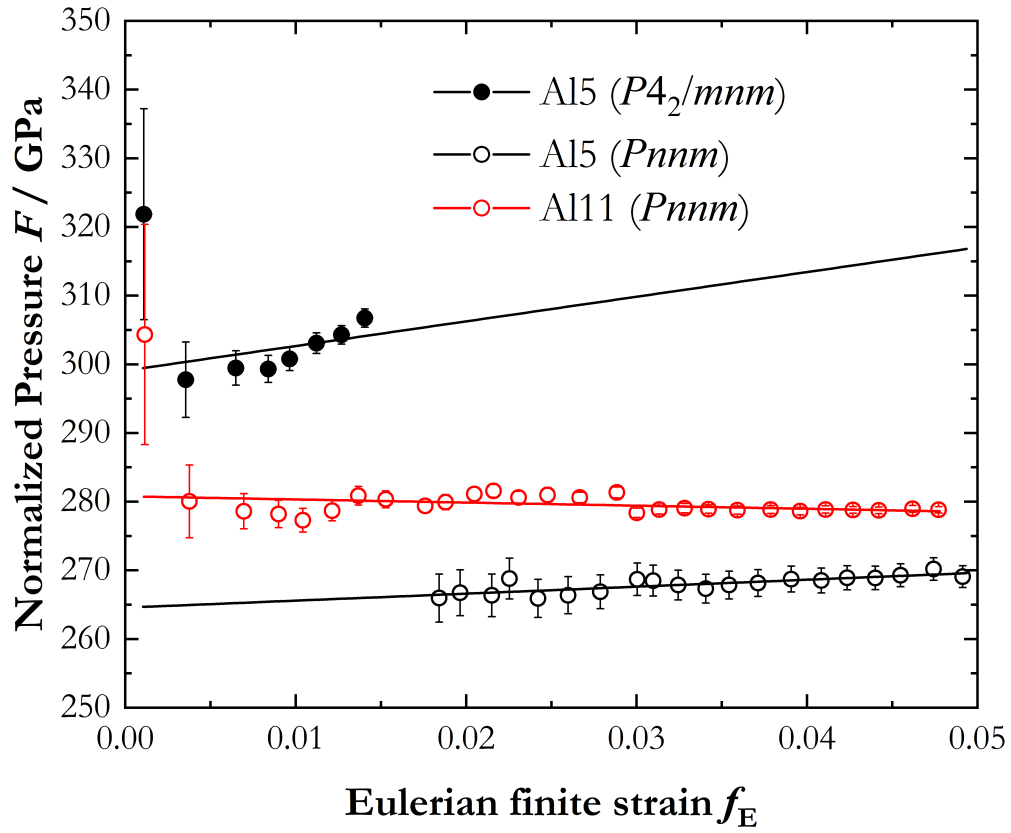


Figure S1. f_E - F plot of the EOSs of Al5 ($P4_2/mnm$ and $Pnnm$) and Al11 ($Pnnm$). The normalized pressure F was calculated as $F = P/[3f_E (2f_E + 1)^{5/2}]$, where $f_E = [(V_0/V)^{2/3} - 1]/2$ is the Eulerian finite strain. Note that K'_{T0} of tetragonal Al5 was fixed to 4.8 in the fitting procedure (see main text for details).

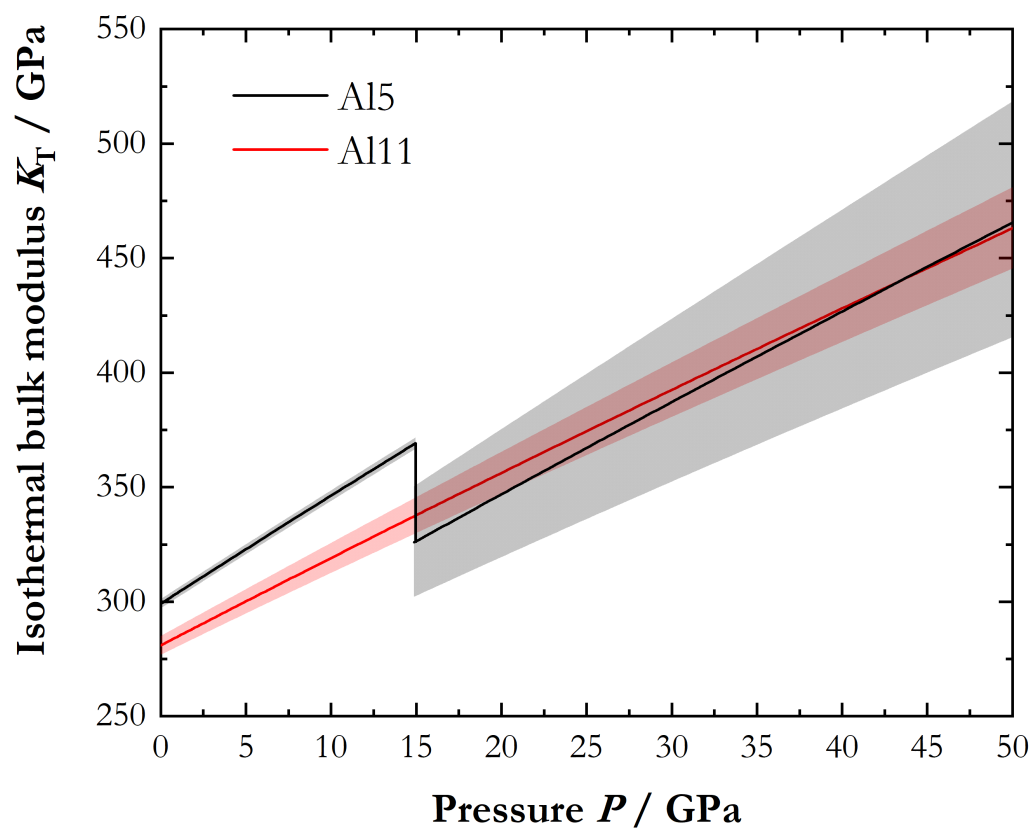


Figure S2. Pressure evolution of the isothermal bulk modulus K_T of Al5 (black) and Al11 (red) samples investigated in this study. At about 16 GPa, a phase transition from tetragonal to orthorhombic occurs in Al5 and causes a drop in K_T . Shaded area represent propagated uncertainties.

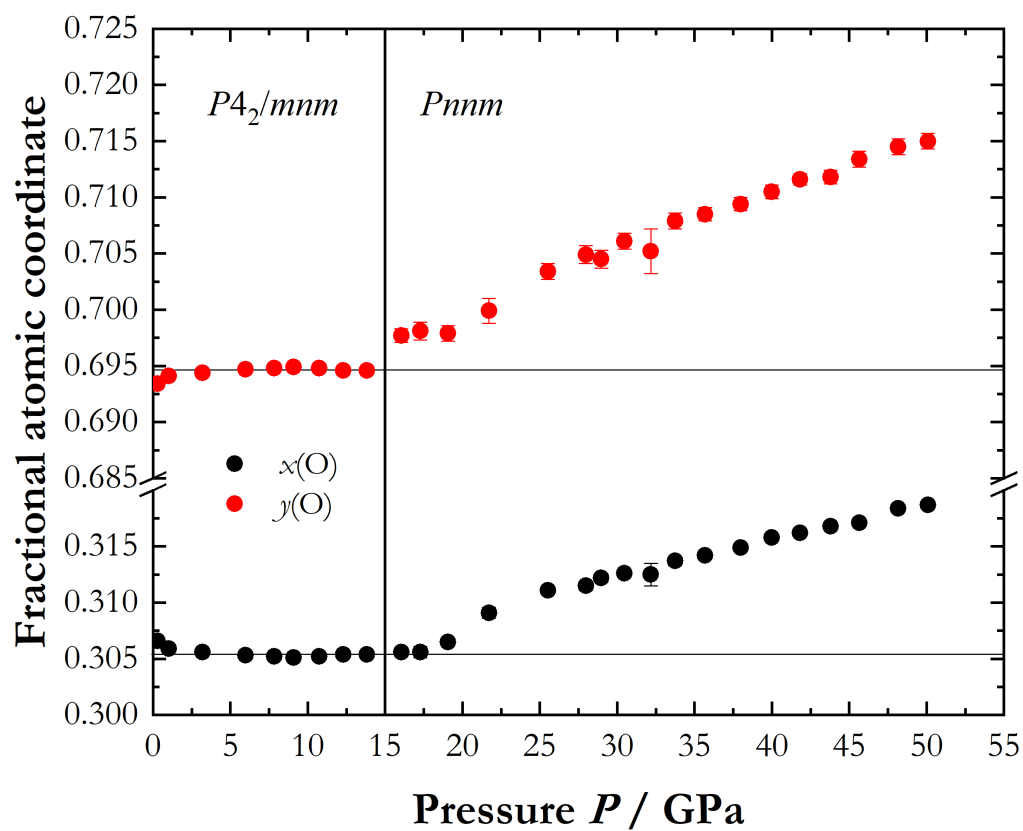


Figure S3. Fractional x and y coordinates of O in the tetragonal ($P4_2/mnm$) and orthorhombic ($Pnnm$) phases of Al_5 as a function of pressure. Horizontal lines represent values of $x(\text{O})$ and $y(\text{O}) = 1 - x(\text{O})$ assumed for the tetragonal phase in the stability field of the orthorhombic phase, which are required in the symmetry-mode decomposition analysis.

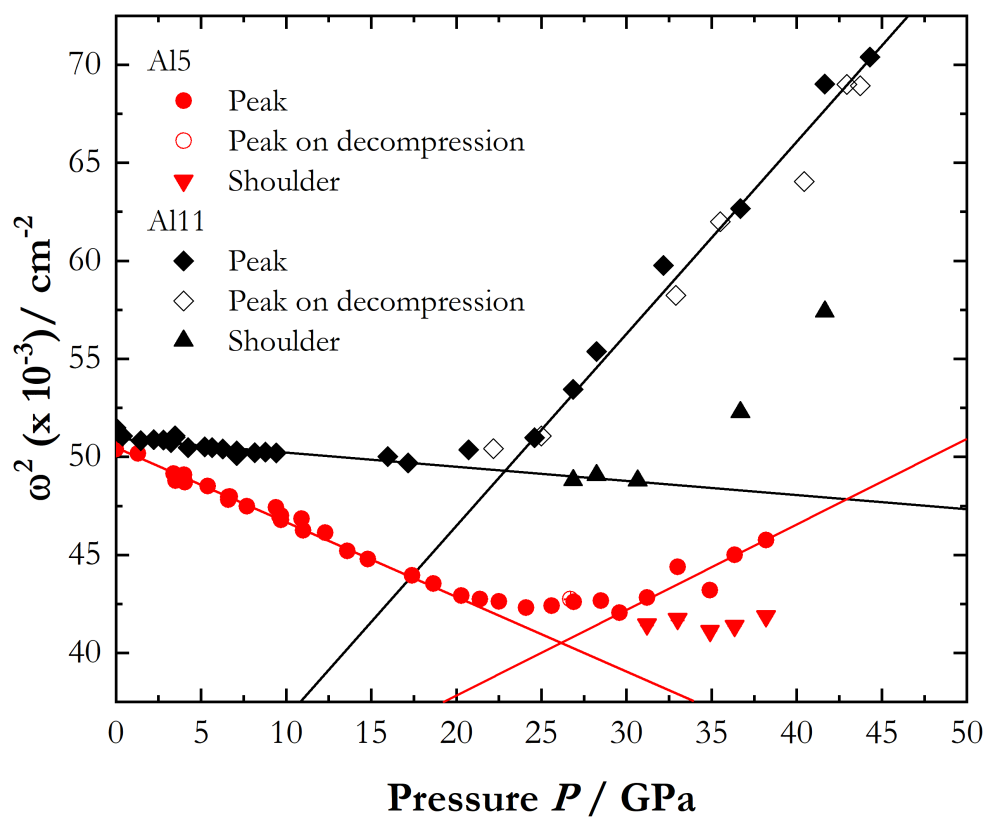


Figure S4. Pressure evolution of Raman bands and their shoulders in Al5 and Al11. Empty symbols represent points collected upon decompression. The shoulder at lower wavenumber represented by black (Al11) and red (Al5) triangles is less intense and tend to disappear as pressure increases.