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3 **Crystal habit (tracht) of groundmass pyroxene crystals recorded magma ascent paths**  
4 **during the 2011 Shinmoedake eruption**

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19

## Abstract

20           The morphologies and size distributions of groundmass crystals record conditions  
21 of magma ascent through volcanic conduits. Nevertheless, morphological information (such  
22 as crystal shapes) has not been incorporated into crystal size distributions (CSDs). Here, we  
23 focused on the crystal habit, especially the shape variation due to the combination of (*hk0*)  
24 faces (hereafter “tracht”) of pyroxene microlites and nano-crystals, and measured CSDs for  
25 each crystal habit (tracht) to more comprehensively characterize the crystallization kinetics.  
26 We refer to the CSDs measured for each tracht as “tracht-specific CSDs.” Pyroclasts from  
27 the 2011 eruption of Shinmoedake (Kirishima volcano group, Japan) were observed by  
28 field-emission scanning electron microscopy, electron backscatter diffraction analysis,  
29 synchrotron radiation X-ray computed nanotomography, and transmission electron  
30 microscopy. The samples contain groundmass pyroxenes of two main trachts: octagonal  
31 prisms consisting of {100}, {010}, and {110} faces and hexagonal prism lacking {100}  
32 faces. The pumice clasts formed by different eruption styles showed different trends of  
33 tracht-specific CSDs. Sub-Plinian pumice clasts were characterized by octagonal microlites  
34 (1–10  $\mu\text{m}$  wide) and numerous hexagonal nano-crystals (0.2–2  $\mu\text{m}$  wide), and a Vulcanian

35 pumice clast with the same glass composition showed the same characteristics. In contrast,  
36 Vulcanian pumice clasts with more evolved glass compositions contained mostly octagonal  
37 pyroxenes. The tracht-specific CSDs and growth zonations indicate a change from  
38 octagon-dominant to hexagon-dominant growth conditions during syneruptive ascent. We  
39 infer that the hexagonal tracht resulted from a large degree of effective undercooling due to  
40 rapid decompression in the shallow conduit. Moreover, the texture of the less-evolved  
41 Vulcanian pumice indicates that a portion of the magma erupted on the Vulcanian eruption  
42 followed almost the same ascent paths just prior to the fragmentation as those during the  
43 sub-Plinian eruptions, and thus the Vulcanian eruption may have involved the rapid ascent  
44 of deeper magma. We propose that tracht analyses of groundmass pyroxenes provide  
45 detailed information about time-evolution of magma conditions during syneruptive ascent.  
46 **Keywords:** pyroxene, crystal habit, crystal size distribution, nanolite, magma ascent

47

## Introduction

48           Degassing mechanisms within volcanic conduits involve interrelated magmatic  
49 properties and processes, and affect both the eruptive style and evolution of volcanoes  
50 (Cassidy et al. 2018). One of the most important parameters affecting the various magmatic  
51 feedbacks is magma ascent rate. The evolution of ascent rate in conduits is related to  
52 syneruptive processes such as volatile exsolution, crystallization, and rheological evolution  
53 of magmas (e.g., Gonnermann and Manga 2007; Cassidy et al. 2018; La Spina et al. 2016,  
54 2021) and thus is important for elucidating the depths where transitions in eruptive style  
55 originate and the mechanisms of those transitions. Magma ascent paths are preserved in the  
56 properties of groundmass crystals, such as their number densities and morphologies (e.g.,  
57 equant, tabular, acicular, euhedral, swallowtail, dendritic).

58           Groundmass crystallization kinetics (i.e., nucleation and growth) have been  
59 investigated both experimentally and in natural samples (e.g., Cashman 1992; Hammer and  
60 Rutherford 2002; Couch et al. 2003; Brugger and Hammer 2010a). Recent studies have  
61 focused on constraining nucleation and growth rates (Shea and Hammer 2013; Arzilli et al.  
62 2015, 2016a; Giuliani et al. 2020), nucleation events through time (Arzilli and Carroll

63 2013; Polacci et al. 2018; Le Gall et al. 2021; Arzilli et al. 2022), nucleation delay (Arzilli  
64 et al. 2020; First et al. 2020; Rusiecka et al. 2020; Rusiecka and Martel 2022), and crystal  
65 growth in real time (Polacci et al. 2018; Arzilli et al. 2019, 2022; Le Gall et al. 2021).  
66 These contributions have deepened understanding of the crystallization kinetics under  
67 disequilibrium conditions.

68         The kinetics of disequilibrium crystallization results in the various crystal textures.  
69 Crystal habits are controlled by the degree of effective undercooling ( $\Delta T_{\text{eff}}$ ) imposed from  
70 cooling and decompression-induced dehydration, and are thus important clues to  
71 investigate magma ascent and/or solidification histories via the extent of  $\Delta T_{\text{eff}}$  (e.g.,  
72 Lofgren 1974, 1980; Donaldson 1976; Hammer and Rutherford 2002; Couch et al. 2003;  
73 Castro and Dingwell 2009; Shea and Hammer 2013; Waters et al. 2015; Giuliani et al.  
74 2020; Arzilli et al. 2022). Moreover, the crystal habits have a strong influence on magma  
75 rheology and dynamics (e.g., Mueller et al. 2010; Mader et al. 2013; Le Gall et al. 2021;  
76 Arzilli et al. 2022). On the other hand, crystal number densities are also used to estimate  
77 ascent conditions, such as crystal size distributions (CSDs; Marsh 1998) and the water  
78 exsolution rate meter (Toramaru et al. 2008). In particular, the slopes of CSDs obtained

79 from pyroclasts reflect temporal changes in the balance between nucleation and growth  
80 during magmatic processes (e.g., Cashman and Marsh 1988; Marsh 1998; Armienti 2008;  
81 Mujin et al. 2017; Okumura et al. 2022a).

82 In this study, we introduce a concept of “tracht.” In contrast to the term “crystal  
83 habit,” “tracht” is a German term referring to the variation of crystal shapes due to the  
84 combination and degree of development of faces (Sunagawa 2005). Although “crystal habit”  
85 refers to the shape differences including “tracht,” this English term is generally used to  
86 specify shapes in a broader sense (cf. Franke 1989; Fig. 2.15a in Schupsky 2020). For  
87 instance, a hexagonal prism is distinguished from an octagonal prism under the concept of  
88 “tracht,” whereas the concept of “crystal habit” generally does not distinguish between  
89 these shapes and treats them as a prismatic and/or euhedral shape. Since the former concept  
90 (i.e., tracht) is not defined in English (Sunagawa 2005; Schupsky 2020), we hereafter use  
91 the term “tracht” in this study.

92 In single-step decompression experiments on hydrous dacite magma, Okumura et  
93 al. (2022b) showed that the tracht of groundmass pyroxenes changes from octagonal to  
94 hexagonal as  $\Delta T_{\text{eff}}$  increases. Since these trachts are easily classified under 2D observation,

95 CSDs can be measured for each shape. In this study, we report the CSDs of groundmass  
96 pyroxenes measured for each tracht (i.e., octagonal, heptagonal, and hexagonal; hereafter  
97 “tracht-specific CSDs”). Although there are many literatures that have focused on crystal  
98 shapes, such as crystal habits and interface-controlled versus diffusion-controlled growth  
99 textures (e.g., Lofgren 1974; Donaldson 1976; Lofgren 1980; Hammer and Rutherford  
100 2002; Shea and Hammer 2013; Giuliani et al. 2020; Arzilli et al. 2022), this study differs  
101 from the previous attempts in that it involves plane indices as crystallographic properties.  
102 The tracht-specific CSDs will push past the limits of the conventional CSD analyses by  
103 relating the growth texture to the temporal evolution of nucleation during syneruptive  
104 magma ascent, as described below.

105         The rates of crystal nucleation and growth generally escalate as the extents of  
106 decompression and resultant  $\Delta T_{\text{eff}}$  increase; the former tends to show a greater escalation  
107 than the latter (e.g., Hammer and Rutherford 2002; Couch et al. 2003; Brugger and  
108 Hammer 2010a; Mollard et al. 2012; Shea and Hammer 2013; Arzilli et al. 2016a; Mollo  
109 and Hammer 2017). In a closed magmatic system with variable rates of nucleation and  
110 growth, CSD slopes are considered to reflect the significant increase in nucleation rate



111 during magma ascent (Marsh 1998). On the other hand, the large variations in syneruptive  
112 crystal growth rates (e.g., Couch et al. 2003; Brugger and Hammer 2010b; Befus and  
113 Andrews 2018) also can affect the resultant CSD and render its interpretation difficult. For  
114 example, Okumura et al. (2022a) showed that slow crystallization (both nucleation and  
115 growth) can result in a CSD slope similar to that of rapid crystallization by using the  
116 formulas of Marsh (1998). As a measure against this, a new expression of CSDs proposed  
117 by Okumura et al. (2022a) reduces the effects of variable growth rates by adopting 3D  
118 short-axis length instead of 3D long-axis length as crystal size. This is because  
119 rock-forming minerals tend to elongate with increasing  $\Delta T_{\text{eff}}$  (e.g., Kouchi et al. 1983;  
120 Hammer and Rutherford 2002; Shea and Hammer 2013; Arzilli et al. 2022), and thus the  
121 growth rates along the long- and short-axes are probably the most and least susceptible to  
122  $\Delta T_{\text{eff}}$ , respectively. The slopes of the CSDs plotted against 3D short-axis length are  
123 controlled more strongly by nucleation rate, enabling us to investigate temporal changes in  
124 nucleation rate more reliably (Okumura et al. 2022a).

125 In contrast, it is still difficult to determine changes of growth rate during  
126 syneruptive ascent from the CSDs of pyroclasts, because magmas experience a wide range

127 of  $\Delta T_{\text{eff}}$  and thus the significant changes in nucleation rate during the ascent, as indicated by  
128 continuous decompression experiments (e.g., Brugger and Hammer 2010a; Mollard et al.  
129 2012; Befus and Andrews 2018). In such a situation, it is not possible to circumvent the  
130 overwhelming effect of the variable nucleation rate on the CSD slopes (cf. Marsh 1998),  
131 which in turn prevents the extraction of the variation in growth rate from the slopes unless  
132 parameterization analyses (Armenti 2008) are performed successfully. Since the crystal  
133 textures including CSDs and crystal habits (and probably tracts) are controlled by the  
134 interplay between nucleation and growth depending on  $\Delta T_{\text{eff}}$  (e.g., Hammer and Rutherford  
135 2002; Couch et al. 2003; Hammer 2008; Mollard et al. 2012; Shea and Hammer 2013;  
136 Mollo and Hammer 2017; Mangler et al. 2022), the temporal change of nucleation should  
137 be examined in relation to growth so as to decipher syneruptive crystallization kinetics.

138         Although the conventional CSD analyses are not suitable to investigate the  
139 temporal change of nucleation in synchronization with that of growth as mentioned above,  
140 this investigation can be possible if growth textures are incorporated into CSDs as the  
141 indicator of growth conditions such as growth rate and  $\Delta T_{\text{eff}}$ . In this context, the  
142 tract-specific CSDs are expected to provide a comprehensive view of crystallization

143 kinetics and reveal more details about temporal changes of  $\Delta T_{\text{eff}}$  and magma ascent  
144 dynamics.

145         To investigate whether the tracht-specific CSDs record syneruptive magma paths,  
146 we analyzed groundmass pyroxene crystals in pyroclasts from the 2011 eruption of  
147 Shinmoedake (Kirishima volcano group, Japan). The 2011 eruption of Shinmoedake  
148 included sub-Plinian eruptions and subsequent Vulcanian eruptions. The different magma  
149 ascent conditions in the shallow conduit during eruptions of these two styles have been  
150 investigated using groundmass plagioclase CSDs measured from scanning electron  
151 microscope (SEM) images (Mujin and Nakamura 2014; Mujin et al. 2017; Suzuki et al.  
152 2018). In addition, Okumura et al. (2022a) directly acquired 3D CSDs of groundmass  
153 pyroxenes by X-ray computed tomography and demonstrated that nucleation kinetics of  
154 pyroxenes also differed between the two styles. Therefore, the tracht-specific CSDs of  
155 groundmass pyroxenes in pumices from sub-Plinian and Vulcanian eruptions of the 2011  
156 Shinmoedake eruption should exhibit different trends.

157         In addition to their tracht-specific CSDs, the internal textures of groundmass  
158 pyroxene crystals record magmatic conditions as compositional zoning (e.g., Ubide and

159 Kamber 2018; Masotta et al. 2020). Therefore, we observed the textures within individual  
160 crystals to corroborate the magma ascent paths inferred from the CSDs. Based on the  
161 inferred crystallization kinetics of groundmass pyroxenes, we aim to better understand the  
162 conduit processes during the 2011 Shinmoedake eruption.

163

### 164 **Sample description**

165 Shinmoedake is an andesitic volcano in the Kirishima volcano group, southern  
166 Kyushu, Japan. The chronology of the 2011 Shinmoedake eruption has been well  
167 documented (e.g., Kozono et al. 2013; Nakada et al. 2013; Kato and Yamasato 2013). The  
168 main phase of the eruptive activity (26–31 January 2011) was characterized by three  
169 sub-Plinian eruptions and the subsequent extrusion of a lava dome within the crater,  
170 associated with intermittent Vulcanian eruptions. This activity was followed by repeated  
171 Vulcanian eruptions and explosive events from 1 February to 13 March 2011. Here, we  
172 examined seven pyroclasts: three gray pumice clasts from the sub-Plinian eruptions and  
173 three gray pumice clasts and one dense juvenile fragment from the Vulcanian eruptions.  
174 These samples were collected on 24 July 2011 at Takachihogawara, 3 km south of

175 Shinmoedake crater; collection details are reported in Mujin and Nakamura (2014).  
176 Although the precise eruptions that produced the Vulcanian samples have not been  
177 determined, they most likely occurred on 1 or 11 February or 13 March (Mujin et al. 2017).  
178 Nonetheless, we were able to easily distinguish the Vulcanian pumices from the sub-Plinian  
179 pumices because the former were larger than the latter.

180         The seven samples are classified into two groups according to the chemical  
181 compositions of their groundmass glasses (Mujin and Nakamura 2020): those of the three  
182 sub-Plinian pumice clasts (sP\_a, sP\_b, and sP\_c), one Vulcanian pumice clast (V-L), and  
183 the dense juvenile fragment (V-L-djf) contained <71 wt% SiO<sub>2</sub> (low-SiO<sub>2</sub> samples),  
184 whereas those of the other two Vulcanian pumice clasts (V-H\_a and V-H\_b) contained >71  
185 wt% SiO<sub>2</sub> (high-SiO<sub>2</sub> samples). Two of the pumice clasts (sP\_a and V-H\_a) and the dense  
186 juvenile fragment (V-L-djf) were previously analyzed by Okumura et al. (2022a) and Mujin  
187 et al. (2017), respectively. The dense fragment (V-L-djf) probably originated from the  
188 welding of sub-Plinian pumice at the crater, because its glass composition is similar to that  
189 of the sub-Plinian pumice (Table 1) and its degassed dense texture with nano-crystals  
190 smaller than 30 nm in diameter indicates suppressed crystal growth at high  $\Delta T_{\text{eff}}$  in the

191 dehydrated melt with low diffusivity (Mujin et al., 2017; Mujin and Nakamura 2020). The  
192 average compositions of each sample are reported in Table 1.

193 The samples contain phenocrysts (>100  $\mu\text{m}$ ) of plagioclase, clinopyroxene (Cpx),  
194 orthopyroxene (Opx), olivine, magnetite, and ilmenite, some showing reaction rims due to  
195 mixing with a higher temperature magma (Suzuki et al. 2013; Tomiya et al. 2013). Their  
196 groundmasses are charged with crystals of plagioclase, pyroxenes, and Fe-Ti oxides (ca.  
197 0.1–10  $\mu\text{m}$  wide); those thinner than 1  $\mu\text{m}$  are referred to as nanolites, and those larger as  
198 microlites. Because most groundmass pyroxene crystals show parallel intergrowths of Opx  
199 and Cpx (Mujin et al. 2017), we treated them as a single pyroxene phase, except when  
200 analyzing internal textures.

201

## 202 **Analytical procedures**

203 The textures of groundmass pyroxenes in the pumices were analyzed with a  
204 field-emission SEM (FE-SEM). The chemical compositions of groundmass glasses in all  
205 samples were measured with a coupled energy-dispersive X-ray spectrometer (EDS). To  
206 obtain 3D aspect ratios ( $S:I:L$ , where  $S$ ,  $I$ , and  $L$  are the short, intermediate, and long axes)

207 of pyroxene crystals, which are necessary to stereologically correct the CSDs, we  
208 conducted synchrotron radiation X-ray computed nanotomography (SR-XnCT). The  
209 SR-XnCT specimens were prepared with a focused ion beam (FIB) system, and the average  
210 3D aspect ratios of groundmass pyroxenes were acquired for each pumice sample. Using  
211 these values, we calculated tracht-specific CSDs of groundmass pyroxenes in each sample.  
212 We did not calculate the CSD of the dense fragment V-L-djf because we focused on the  
213 pumice samples to investigate syneruptive ascent conditions rather than post-eruptive  
214 processes.

215         We determined the crystallographic indices of the faces of groundmass pyroxenes  
216 by combining electron backscatter diffraction (EBSD) analysis and SR-XnCT. The EBSD  
217 analysis was performed on a relatively large pyroxene microlite (~7  $\mu\text{m}$  wide) with a  
218 hexagonal cross section in V-L-djf to determine its crystallographic orientation. The crystal  
219 was then prepared as a SR-XnCT specimen with the FIB system and observed to obtain its  
220 3D outline. By combining these data, we acquired the face indices of the hexagonal crystal.

221         Moreover, we observed groundmass pyroxene crystals in three pumice samples  
222 (sP\_a, V-H\_a, and V-L) using a transmission electron microscope (TEM). Ultrathin sections

223 were prepared from the samples using FIB systems. In addition to determination of mineral  
224 phases and crystallographic orientations by selected-area electron diffraction (SAED)  
225 patterns, we investigated compositional zoning in crystals by EDS analyses in scanning  
226 TEM (STEM) mode. An overview of the analytical procedures used is shown in Figure S1  
227 in Online Resource 1.

228

## 229 **FE-SEM-EDS**

230 Quantitative compositional analyses of groundmass glasses were performed using  
231 a JEOL JSM-7001F FE-SEM coupled with an Oxford Instruments X-Max150 EDS detector  
232 and its associated analytical software *Aztec* at Kyoto University. We analyzed 50 square  
233 regions ( $\sim 1 \times 1 \mu\text{m}$ ) in each sample for 40 s each at a working distance of 10 mm, an  
234 acceleration voltage of 15 kV, and a beam current of  $\sim 0.3 \text{ nA}$ . We corrected for losses of Na  
235 and K during the measurements by calibration against analyses of larger rectangular regions  
236 ( $>400 \mu\text{m}^2$ ).

237 For textural analyses, backscattered electron (BSE) images of polished sections of  
238 the pumice samples were obtained at an acceleration voltage of 15 kV and a working



239 distance of 10 mm using the FE-SEM. Each BSE image was a rectangular area of  $127 \times 95$   
240  $\mu\text{m}^2$  with an image resolution of ca. 25 nm/pixel. To identify their trachts, magnified  
241 images of the pyroxene crystals in the analyzed areas were obtained at an acceleration  
242 voltage of 10 kV.

243

#### 244 **EBSD**

245 EBSD analysis of the large hexagonal microlite in V-L-djf was performed using a  
246 SEM equipped with a tungsten filament (FEI Quanta 200 3DS) and a HKL EBSD system  
247 with *Channel 5* software (Oxford Instruments) at Kyoto University. Using an acceleration  
248 voltage of 15 kV, a working distance of 20 mm, and the lattice parameters of diopside ( $a =$   
249  $9.75 \text{ \AA}$ ,  $b = 8.99 \text{ \AA}$ ,  $c = 5.25 \text{ \AA}$ ,  $\beta = 105.6^\circ$ ), the crystallographic orientation of the microlite  
250 was determined before SR-XnCT observation.

251

#### 252 **FIB systems**

253 For SR-XnCT observations, we extracted one or two equant specimens about 20–  
254 25  $\mu\text{m}$  wide from each sample (Table 2) using a FEI Quanta 200 3DS FIB system at Kyoto

255 University. The extracted regions were distinct from the areas of FE-SEM textural analyses.  
256 Each specimen was then mounted on a tungsten needle. A Ga<sup>+</sup> ion gun was used at an  
257 acceleration voltage of 30 kV and a beam current of 0.030–65 nA. Details of the specimen  
258 preparation for SR-XnCT are reported in Miyake et al. (2014).

259 For TEM observation, ultrathin sections about 100 nm thick were prepared using  
260 FIB systems (FEI Quanta 200 3DS and FEI Helios NanoLab G3 CX) at Kyoto University.  
261 The Ga<sup>+</sup> ion guns were used at 30 kV and 0.083–65 nA for thinning, and at 5 kV and 16 pA  
262 for final processing.

263

## 264 **SR-XnCT**

265 We acquired the 3D shapes of groundmass pyroxene crystals by SR-XnCT at  
266 beamline BL47XU of the Spring-8 synchrotron facility in Hyogo, Japan (Uesugi et al.  
267 2006; Takeuchi et al. 2009). The SR-XnCT measurements were performed in  
268 absorption-contrast mode (e.g., Cloetens et al. 1997; Mancini et al. 1998; Tsuchiyama et al.  
269 2013; Arzilli et al. 2016b) using an X-ray imaging system with a Fresnel zone plate at a  
270 single X-ray energy of 7.35 keV, providing isotropic voxel (volumetric pixel) sizes of 25–

271 78 nm on a side (Table 2) for an effective specific resolution of ~200 nm. Projection images  
272 were acquired every 0.1° during a total sample rotation of 180°, resulting in 1,800  
273 projections per specimen. The 3D CT images were reconstructed from the projection  
274 images using a convolution back-projection algorithm (Nakano et al. 2000). Details of the  
275 CT imaging procedures are reported in Matsumoto et al. (2019).

276       Except for four CT specimens (sP\_a-1, sP\_a-2, and V-H\_a-1 from Okumura et al.  
277 2022a, and V-L-djf), the CT images were denoised using iterative nonlocal means (Bruns et  
278 al. 2017) before binarization: this process reduced the effort involved in binarization by  
279 smoothing the insides of crystals without affecting the quality of the extracted 3D data.  
280 Pyroxenes were distinguishable from the other minerals on the basis of pixel values;  
281 therefore, we binarized the images with thresholds based on visual inspection, removed  
282 blurring of the binary images by erosion and dilation by 1 voxel, and extracted the 3D  
283 pyroxene crystal data using the software package *Slice* (Nakano et al. 2006). We  
284 determined the triaxial lengths  $S$ ,  $I$ , and  $L$  by ellipsoid fitting in *Slice* (e.g., Tsuchiyama et al.  
285 2011). These measurements were restricted to crystals that were entirely contained within  
286 the specimens, larger than 5 voxels wide, and readily separated from other crystals. The

287 average 3D aspect ratio of groundmass pyroxenes in each pumice sample was calculated to  
288 obtain the necessary information for determining CSDs from the BSE images (Table 2).

289           Although we analyzed six pumice samples to obtain the average 3D aspect ratios  
290 in this study, two of the pumice samples (i.e., sP\_a and V-H\_a) were already observed by  
291 SR-XnCT by Okumura et al. (2022a) (our CT specimens sP\_a-1, sP\_a-2, V-H\_a-1, and  
292 V-H\_a-2 correspond to their specimens sP\_1, sP\_2, Vul\_1, and Vul\_2, respectively). They  
293 reported 3D CSDs of groundmass pyroxenes for the samples sP\_a and V-H\_a, whereas we  
294 did not obtain 3D CSDs from the other samples. Tracht-specific CSDs could not be  
295 obtained directly from the CT data because the spatial resolution was insufficient to  
296 recognize nanolite trachts. Thus, tracht-specific CSDs were obtained from the SEM images  
297 using the 3D aspect ratios (see *Acquisition of tracht-specific CSDs*).

298

## 299 **TEM**

300           Ultrathin sections prepared from three pumice samples (sP\_a, V-H\_a, and V-L)  
301 were observed under a JEOL JEM-2100F TEM equipped with a Gatan Orius 200D CCD  
302 camera and a JEOL JET-2300T EDS detector at an acceleration voltage of 200 kV. To

303 determine mineral phases and crystallographic orientations, SAED patterns were analyzed  
304 using *DigitalMicrograph* (Gatan) and *ReciPro* (Seto and Ohtsuka 2022) software. For  
305 quantitative X-ray analyses by STEM, we used the  $\zeta$ -factor method (Watanabe and  
306 Williams 2006). To achieve the accurate electron beam current measurements required for  
307 the  $\zeta$ -factor method, appropriate calibration was performed with the CCD camera  
308 beforehand. Furthermore, we acquired annular dark-field STEM (ADF-STEM) images of  
309 pyroxene crystals perpendicular to their *c*-axes to observe their compositional zoning at  
310 higher resolution.

311

### 312 **Acquisition of tracht-specific CSDs**

313 The FE-SEM BSE images of pumice groundmasses were analyzed using *ImageJ*  
314 software to measure the examined groundmass area (i.e., groundmass crystals + glass,  
315 excluding vesicles) and the widths of the best fit ellipses to the cross sections of pyroxene  
316 crystals. The analyzed samples contained groundmass pyroxene crystals with octagonal,  
317 heptagonal, and hexagonal trachts (Fig. 1a); therefore, each pyroxene cross section was  
318 classified into one of these tracht groups based on BSE images at higher magnification.

319 Crystals were classified based on the number of faces between a pair of parallel faces  
320 (Okumura et al. 2022b). For example, the octagonal and hexagonal trachts have three and  
321 two faces, respectively, between each pair of parallel faces, whereas the heptagonal tracht  
322 has the properties of the octagonal tracht on one side of a pair of parallel faces and those of  
323 the hexagonal tracht on the other side (Fig. 1a). Crystals that were difficult to classify as  
324 belonging to a particular tracht were classified as “other”. If cross sections were incomplete  
325 (e.g., those at crystal edges or corners), we classified them based on the remaining faces if a  
326 pair of parallel faces was present for reference; otherwise, those showing no pairs of  
327 parallel faces in the plane of the BSE image were classified as “other” (Fig. 1b). When  
328 multiple crystals were attached to each other, each segment was classified in the same way  
329 (Fig. 1c). The analyzed areas and the number of crystals observed in each tracht are shown  
330 in Table 3.

331         Then, the datasets of all analyzed crystals and each tracht group were converted to  
332 a conventional CSD (i.e., including all crystal trachts) and tracht-specific CSDs,  
333 respectively, using *CSDCorrections* ver. 1.6 (Higgins 2000). *CSDCorrections* converts  
334 cross-sectional widths into 3D long-axis lengths ( $L$ ) using the 3D aspect ratio  $S:I:L$ . We

335 used the average 3D aspect ratio determined by SR-XnCT for each sample, regardless of  
336 tracht. Although *CSDCorrections* yields 3D CSDs expressed as a function of  $L$ , we  
337 expressed the CSDs as a function of  $S$  with additional corrections, because the latter is  
338 relatively insensitive to changes in crystal growth rate and thus more obviously shows  
339 changes in nucleation rate during magma ascent (Okumura et al., 2022a). We followed the  
340 correction procedure of Okumura et al. (2022a), but reduced the correction for sectioning  
341 effects in tracht-specific CSDs (see Online Resource 2), because the nature of the datasets  
342 and thus the correction assumption differed from those of Okumura et al. (2022a). The  
343 CSDs were plotted on logarithmic size intervals with five intervals per decade larger than  
344 100 nm (i.e., each interval is  $10^{0.2}$  times as large as the next smaller interval:  $10^{2.0}$ – $10^{2.2}$  nm,  
345  $10^{2.2}$ – $10^{2.4}$  nm,  $10^{2.4}$ – $10^{2.6}$  nm...).

346

## 347 **Results**

### 348 **Tracht-specific CSDs**

349 Most of groundmass pyroxenes in the pumice samples were prismatic and those in  
350 the sub-Plinian samples tended to be more elongated than those in the Vulcanian samples

351 (Table 2, Figs. S2 and S3 in Online Resource 3). Most pyroxenes exhibited hexagonal or  
352 octagonal shapes in the polished sections, and all pumice samples contained these trachts  
353 and heptagonal one (Figs. 2 and 3; Table 3). There were no obvious differences in the  
354 spatial distributions of the trachts among the samples. Figure 3 shows the groundmass  
355 pyroxene CSDs for the six pumice samples. As reported by Mujin et al. (2017), the  
356 conventional CSDs (i.e., including all crystal trachts) were concave up in all samples (black  
357 lines in Fig. 3). In addition, those of the low-SiO<sub>2</sub> samples (i.e., sP\_a–c and V-L) had  
358 steeper slopes in the size range  $S < 2 \mu\text{m}$  than those of the high-SiO<sub>2</sub> Vulcanian samples  
359 (i.e., V-H\_a and V-H\_b).

360 Figure 3 also shows tracht-specific CSDs for octagonal, heptagonal, and hexagonal  
361 cross sections. The size distributions of the trachts exhibited distinct trends, and the  
362 proportions of trachts within each sample (Table 3) depended on the type of pumice (i.e.,  
363 low-SiO<sub>2</sub> vs. high-SiO<sub>2</sub>). The low-SiO<sub>2</sub> pumice samples (sP\_a–c and V-L) were  
364 characterized by coexisting hexagonal nanolites and octagonal crystals (Fig. 3a–c, f),  
365 whereas the high-SiO<sub>2</sub> pumice samples (V-H\_a and V-H\_b) contained mostly octagonal  
366 crystals with far fewer hexagonal and heptagonal crystals (Fig. 3d, e). In both pumice types,



367 octagonal crystals spanned wide size ranges, and their slopes were relatively gentler and  
368 similar to those of the conventional CSDs in the larger size range ( $S > 2 \mu\text{m}$ ). More  
369 importantly, the size distributions of octagonal microlites were similar in all samples. In  
370 contrast, hexagonal crystals spanned narrower size ranges that were largely consistent with  
371 those at which the conventional CSDs showed steeper slopes ( $S < 2 \mu\text{m}$ ; Fig. 3a–c, f). The  
372 slopes of the hexagonal CSDs were steeper than those of the octagonal CSDs and similar to  
373 those of the conventional nanolite ( $S < 1 \mu\text{m}$ ) CSDs. The size ranges and slopes of  
374 heptagonal crystals were intermediate between those of the octagonal and hexagonal trachts,  
375 and their population densities were generally lower than those of both the octagonal and  
376 hexagonal trachts. Furthermore, the population densities of octagonal nanolites in low-SiO<sub>2</sub>  
377 samples were reduced compared to those in high-SiO<sub>2</sub> samples in response to the  
378 appearance of hexagonal nanolites.

379

### 380 **Crystallographic analyses of groundmass pyroxenes**

381 Figure 4 shows the 3D morphology and crystallographic axes of the large  
382 hexagonal pyroxene microlite in the dense fragment (V-L-djf). The hexagonal prism was

383 elongated along its *c*-axis, consisted of {010} and {110} prismatic faces, and was truncated  
384 by a rough surface lacking any facet or distinct crystallographic index (the other end was  
385 polished away). Although the detail of this truncated surface was limited by the effective  
386 spatial resolution of the SR-XnCT images (~200 nm), we assume that the growth rate of  
387 this rough surface must have been larger than those of the relatively flat {010} and {110}  
388 surfaces to produce such an elongated crystal.

389         Figures 5–8 summarize our TEM observations of pyroxene nanolites and  
390 microlites in samples sP\_a, V-H\_a, and V-L. The above combinations of prismatic faces  
391 were confirmed in other groundmass pyroxenes by TEM analyses (Figs. 5–7). Octagonal  
392 crystals had an additional pair of {100} faces (Figs. 7, 8), and heptagons lacked {100}  
393 faces on one side. Cross-sectional shapes similarly corresponded to these combinations of  
394 plane indices in all samples observed.

395         Almost all crystals observed by TEM showed epitaxial parallel growth of Opx  
396 (*Pbca*) and Cpx composed of augite (Aug; *C2/c*) and pigeonite (Pgt; *P2<sub>1</sub>/c*), as reported by  
397 Sharp et al. (1996) and Mujin et al. (2017). Figure 5 shows a typical texture observed in a  
398 pyroxene nanolite in sP\_a. The SAED patterns (Fig. 5f–h) show that a pair of Cpx domains

399 epitaxially attached to the (100) and ( $\bar{1}00$ ) surfaces of Opx. In some crystals, the two  
400 epitaxial Cpx domains were in a twin relationship (Fig. 5f, h). The SAED patterns of Cpx  
401 domains sometimes showed weak reflections of  $P2_1/c$  in addition to those of  $C2/c$  (i.e., the  
402  $hkl$  reflections of “ $h + k = \text{even}$ ”; Fig. 5f, h), indicating that Aug and Pgt exist both as fine  
403 exsolution lamellae (Fig. 5) and as distinct domains (Fig. 6). Rarely, distinct domains of Pgt  
404 and Aug formed parallel growth textures without Opx (Fig. 6).

405         As shown in the ADF-STEM images and compositional maps perpendicular to the  
406  $c$ -axis (Figs. 5a–d, 6a–d, 7, and 8a–d), most of the observed groundmass pyroxenes showed  
407 compositional growth zoning with low-Mg# ( $=\text{Mg}/(\text{Mg} + \text{Fe})$ ) rims. The low-Mg# rims  
408 were approximately 10–300 nm wide. In the low-SiO<sub>2</sub> samples (sP\_a and V-L), this zoning  
409 was common and was characterized by a distinct boundary between the core and rim.  
410 Moreover, this sharp rim tended to be enriched in Al and Ti, especially in low-Ca pyroxene  
411 phases (Figs. 5c, 6c, and 7c, g; quantitative data are reported in Online Resource 4). The  
412 zoning boundaries showed euhedral shapes. In most crystals, the zoning boundary was the  
413 same shape as their external tracht (Figs. 5 and 7); however, a few hexagonal crystals  
414 exhibited internal octagonal zoning boundaries (Fig. 6), indicating the extinction of {100}

415 faces during growth. In contrast, pyroxenes in the high-SiO<sub>2</sub> sample (V-H\_a) tended to have  
416 more diffuse rims (Fig. 8a–d), and in some crystals, especially nanolites, the low-Mg# rim  
417 was not discernible (Fig. 8e–h). Additionally, when low-Mg# rims were present in the  
418 high-SiO<sub>2</sub> sample, no obvious enrichment of Al and Ti was observed, in contrast to those in  
419 the low-SiO<sub>2</sub> samples (Fig. 8c, g).

420

## 421 **Discussion**

### 422 **Interpretation of tracht-specific CSDs**

423 The observed groundmass pyroxene textures differ between the low-SiO<sub>2</sub> and  
424 high-SiO<sub>2</sub> pumices, as summarized in Figure 9. Before investigating the syneruptive  
425 magma ascent paths, we first derive crystallization histories from the tracht-specific CSDs  
426 (Fig. 3).

427 The size ranges and population densities of groundmass pyroxene crystals differed  
428 according to their crystal tracht. Pyroxene microlites in all samples and most nanolites in  
429 the high-SiO<sub>2</sub> samples were characterized by the octagonal tracht (Fig. 3). In contrast, the  
430 hexagonal tracht dominated nanolites in the low-SiO<sub>2</sub> samples (Fig. 3a–c, f). Moreover, the

431 population densities of the hexagonal nanolites exceeded those of octagonal crystals in the  
432 low-SiO<sub>2</sub> samples, and the CSD slopes of nanolites and hexagonal crystals were steeper  
433 than those of microlites and octagonal ones. This means that the production of the  
434 hexagonal tracht was accompanied by an accelerated increase in pyroxene nucleation rate,  
435 suggesting a high degree of effective undercooling ( $\Delta T_{\text{eff}}$ , i.e., including cooling and the  
436 contribution from decompression-induced dehydration; e.g., Armienti et al. 1994; Marsh  
437 1998; Okumura et al. 2022a). Indeed, the hexagonal tracht is reproduced at  $\Delta T_{\text{eff}} > 100$  °C  
438 in the decompression experiment of a dacitic magma (Okumura et al. 2022b; discussed in  
439 the following subsection).

440           It is difficult to exclude the possibility that the hexagonal and octagonal crystals  
441 originated from different magma batches based solely on the tracht-specific CSDs (Fig. 3).  
442 However, given the lack of any obvious difference in the spatial distributions of the  
443 different trachts among samples, it is plausible that a single magma batch underwent  
444 successive crystallization conditions. This interpretation is consistent with the hexagonal  
445 crystals showing internal octagonal zoning boundaries in the low-SiO<sub>2</sub> sample (Fig. 6).

446           In the case of the low-SiO<sub>2</sub> samples, and given this crystallization sequence in a

447 single magma batch, the tracht-specific CSDs indicate that the octagonal tracht was favored  
448 during an early crystallization stage at depth, and that the crystallizing conditions then  
449 changed into those favoring the hexagonal tracht as the magma ascended into the shallow  
450 conduit (Fig. 3a–c, f). In this case, we assume that the larger microlites retained their  
451 octagonal tracht during shallow crystallization because, compared to nanolites, a  
452 larger-volume overgrowth is required to change their tracht to hexagonal. In contrast, some  
453 hexagonal pyroxenes, especially those 1–2  $\mu\text{m}$  wide, must have originally been octagonal,  
454 as suggested by the distributions of heptagonal crystals (i.e., the transitional tracht between  
455 octagonal and hexagonal; Fig. 3) and the presence of hexagonal crystals with internal  
456 octagonal growth zoning (Fig. 6). Therefore, we note that the tracht-specific CSDs describe  
457 the final texture after quenching and could be strictly different from the nucleation history  
458 of each tracht.

459 In contrast to the low-SiO<sub>2</sub> samples, which are assumed to have experienced  
460 increasing  $\Delta T_{\text{eff}}$ , the crystallization kinetics of the high-SiO<sub>2</sub> samples can be similar to that  
461 of single-step decompression/cooling experiments because the magma stagnated in the  
462 conduit prior to the Vulcanian eruptions (Suzuki et al. 2018). Arzilli et al. (2022) performed

463 *in situ* 4D (3D + time) observation of cooling-induced crystallization in a hydrous  
464 trachybasaltic magma. After they imposed cooling in a single step, several nucleation  
465 events occurred through time; moreover, the time-evolutions of growth rate and the  
466 resultant sizes of the crystals were similar regardless of their nucleation timing. Since  
467 crystals can reach similar sizes while held at a certain  $\Delta T_{\text{eff}}$  (Arzilli et al. 2022), the peak  
468 positions of the CSDs for the high-SiO<sub>2</sub> samples at slightly larger sizes (Fig. 3d, e;  
469 Okumura et al. 2022a) can be attributed to the quasi-single-step decompression path. Given  
470 the tracht-specific CSDs (Fig. 3d, e), the magma of the high-SiO<sub>2</sub> samples was held at the  
471 condition favoring the octagonal tracht through the crystallization history.

472         From the above, in the following subsections, we discuss the groundmass  
473 crystallization histories in two stages: early and late stages when microlites and nanolites  
474 nucleated in the deep and shallow parts of the volcanic conduit, respectively. The early  
475 stage for all samples and the late stage for the high-SiO<sub>2</sub> samples were octagon-dominant,  
476 whereas only the late stage for the low-SiO<sub>2</sub> samples was hexagon-dominant.

477

478 **Factors controlling the tracht of groundmass pyroxenes**

479           The tracht change of groundmass pyroxene crystals in hydrous dacite magma was  
480 previously investigated via single-step decompression experiments by Okumura et al.  
481 (2022b). Although they did not mention the plane indices of crystals, they found that the  
482 dominant groundmass pyroxene tracht changed from octagonal to hexagonal as the final  
483 pressure decreased and that pyroxenes in differentiated melts within 10  $\mu\text{m}$  of plagioclase  
484 crystals were more likely to be hexagonal. They suggested that the pyroxene tracht was  
485 related to  $\Delta T_{\text{eff}}$ : increasing  $\Delta T_{\text{eff}}$  with decreasing final pressure and melt evolution due to  
486 plagioclase crystallization (Mujin et al. 2017) caused the tracht change from octagonal to  
487 hexagonal. The value of  $\Delta T_{\text{eff}}$  for each experiment was estimated from the liquidus  
488 determined experimentally by Sekine et al. (1979), and their results showed that the tracht  
489 change occurred at  $\Delta T_{\text{eff}} = 90\text{--}110$  °C. Based on this correlation, the existence of hexagonal  
490 nanolites indicates that the late stage of pyroxene crystallization in the low- $\text{SiO}_2$  samples  
491 proceeded under high  $\Delta T_{\text{eff}}$ , consistent with their high nucleation rates (Fig. 3) and  
492 elongated shapes (Table 2). Although the experienced  $\Delta T_{\text{eff}}$  might be higher than the  
493 threshold value determined by the experiments of dacitic magma (Okumura et al.



494 2022b;  $\Delta T_{\text{eff}} \sim 100$  °C), the threshold  $\Delta T_{\text{eff}}$  can be different in the andesitic magma of the  
495 Shinmoedake volcano because the melt composition and chemical diffusivity probably  
496 affect growth mechanisms and resultant crystal textures (e.g., Lofgren 1974; Sunagawa  
497 1981; Hammer 2008; Mollo and Hammer 2017). For example, Cpx crystals are governed  
498 by interface-controlled growth at  $\Delta T_{\text{eff}} < 112$  °C in a hydrous basaltic-andesite magma  
499 (Shea and Hammer 2013), whereas they exhibit diffusion-controlled growth texture at  $\Delta T_{\text{eff}}$   
500  $\geq 30$  °C in hydrous basaltic magmas (Moschini et al. 2021; Arzilli et al. 2022). Given the  
501 difference in threshold  $\Delta T_{\text{eff}}$  for the growth mechanisms, the threshold for the tracht change  
502 might similarly depend on melt compositions. Therefore, further experiments using  
503 andesitic magma are required to estimate the accurate value of  $\Delta T_{\text{eff}}$  during the ascent.

504           Moreover, we confirmed that the octagonal tracht comprises {100}, {010}, and  
505 {110} prismatic faces and that the change to the hexagonal one by losing {100} faces (Figs.  
506 4–8). These results indicate that the relative growth rates of {100} faces become faster than  
507 those of other prismatic faces under high  $\Delta T_{\text{eff}}$  until the faces disappear. On the other hand,  
508 relationships between the degree of cooling-induced undercooling,  $\Delta T$ , and relative growth  
509 rate for different faces of Cpx were previously investigated by Kouchi et al. (1983). They

510 conducted cooling-induced crystallization experiments in the system  $\text{CaMgSi}_2\text{O}_6$ –  
511  $\text{CaTiAl}_2\text{O}_6$ . In the  $\Delta T$  range where Cpx crystals had smooth surfaces, their results showed  
512 that the order of the growth rates of Cpx faces was  $(110) < (010) < (100) < (\bar{1}11)$  and that  
513 the differences between the growth rates increased with increasing  $\Delta T$ . On the other hand,  
514 the crystallization kinetics likely differ between their melt of Cpx composition and a  
515 multi-component magmatic system in general (Sunagawa 1981, 2005), and the difference  
516 should be more significant than that between different magmas mentioned above.  
517 Nevertheless, we assume that their results except the quantitative values of  $\Delta T$  are  
518 qualitatively applicable to crystallization during the 2011 Shinmoedake eruption because  
519 the growth mechanism, i.e., interface-controlled growth, is essentially the same in both  
520 systems, as suggested by the smooth prismatic faces of the pyroxene crystals studied  
521 herein.

522         During interface-controlled growth, the key process limiting the growth rate is not  
523 mass transfer through the melt towards the crystal surface, but the attachment of growth  
524 components on the surface (Hammer 2008). The attachment energy  $E_{\text{att}}$  strongly affects the  
525 relative growth rates of different crystallographic faces and thus the resultant crystal tracht

526 (e.g., Hartman and Perdok 1955a, b; Hartman and Bennema 1980; Duan et al. 2010).  $E_{\text{att}}$  on  
527 faces  $\{hkl\}$  is defined as the bond energy released per structural unit when a growth unit  
528 (i.e., a layer of crystal on the  $\{hkl\}$  face) attaches to the crystal surface. In general,  
529 crystallographic faces with higher  $E_{\text{att}}$  have faster relative growth rates and thus lower  
530 morphological importance (e.g., Hartman and Perdok 1955a, b; Hartman and Bennema  
531 1980; Liu and Bennema 1996). Van Panhuys-Sigler and Hartman (1981) calculated  $E_{\text{att}}$  for  
532 Cpx crystal faces based on periodic bond chain theory (Hartman and Perdok 1955a) and  
533 found that  $E_{\text{att}}$  for different faces follows the order  $(110) < (010) < (100) < (\bar{1}11)$ , consistent  
534 with the growth rates determined experimentally by Kouchi et al (1983). Their calculations  
535 also showed that, assuming that the relative growth rate is proportional to  $E_{\text{att}}$ , the growth  
536 form of augite is the hexagonal tracht with  $\{010\}$  and  $\{110\}$  prismatic faces.

537         From the above evidence, among the important prismatic faces of Cpx,  $\{100\}$   
538 faces are the most likely to disappear because of the crystallographic structure, and an  
539 increase in  $\Delta T_{\text{eff}}$  further promotes their disappearance. Given the order of  $E_{\text{att}}$  for different  
540 faces, an additional increase in  $\Delta T_{\text{eff}}$  may also make  $\{010\}$  faces disappear, resulting in a  
541 parallelogrammatic tracht composed of  $\{110\}$  faces as observed in pumice from the 1914

542 Plinian eruption of the Sakurajima volcano (Okumura et al. 2022b).

543           This same mechanism depending on  $\Delta T_{\text{eff}}$  and the order of  $E_{\text{att}}$  for different faces  
544 can explain why the groundmass pyroxenes in the sub-Plinian samples are more elongated  
545 than those in the Vulcanian ones (Table 2). There are two factors that can increase  $\Delta T_{\text{eff}}$ :  
546 magma ascent rate and melt evolution by crystallization. It is plausible that the magma  
547 ascent rate was faster during the sub-Plinian than the Vulcanian eruptions because textural  
548 analyses of pyroclasts and geophysical observations indicate that the magma stagnated in  
549 the conduit prior to the Vulcanian eruptions (Suzuki et al. 2018). The rapid ascent during  
550 the sub-Plinian eruptions should have involved large  $\Delta T_{\text{eff}}$  due to decompression-induced  
551 dehydration and possibly cooling. Therefore, late crystallization in the low-SiO<sub>2</sub> samples  
552 (i.e., the sub-Plinian pumices and one Vulcanian pumice) should have occurred under the  
553 largest  $\Delta T_{\text{eff}}$  during the 2011 eruptive activity; hence the occurrence of the hexagonal tracht  
554 in those samples (Fig. 3).

555           In contrast, plagioclase crystallization causes melt evolution and may increase the  
556 degree of supersaturation for pyroxene in the melt (Mujin et al. 2017). In the case of the  
557 2011 Shinmoedake eruption, the whole-rock compositions (SiO<sub>2</sub> = 57.3–58.4 wt%; Suzuki

558 et al. 2013) and the bulk groundmass compositions excluding phenocrysts ( $\text{SiO}_2 = 62\text{--}65$   
559 wt%; Mujin and Nakamura 2020) of the brown-gray pumices were similar regardless of the  
560 pumice type. Therefore, the difference in glass composition (low- $\text{SiO}_2$  vs. high- $\text{SiO}_2$ ) is due  
561 to crystallization differentiation from the initial melt (i.e., the bulk groundmass) during the  
562 ascent (Mujin and Nakamura 2020). The degrees of plagioclase crystallization and melt  
563 evolution were highest in the late crystallization stage of the high- $\text{SiO}_2$  samples, followed  
564 in order by the late stage of the low- $\text{SiO}_2$  samples and the early stages of both samples  
565 (Mujin and Nakamura 2014, 2020; Suzuki et al. 2018). Therefore, in terms of melt  
566 evolution, nanolites in the high- $\text{SiO}_2$  samples are the most likely to be hexagonal. However,  
567 our results show that only the late crystallization of the low- $\text{SiO}_2$  samples was  
568 hexagon-dominant (Fig. 3). Accordingly, we conclude that melt evolution is not the main  
569 factor that caused the tracht change. Therefore, in the case of the 2011 Shinmoedake  
570 eruption, the tracht change resulted from the high  $\Delta T_{\text{eff}}$  associated with rapid magma ascent  
571 through the shallow conduit.

572

573 **Crystallization conditions and the timing of growth zoning**

574 Growth zoning records the ascent paths of individual crystals after their nucleation.  
575 In general, normal Mg# zoning could reflect evolution of the melt, cooling (e.g., Lindsley  
576 1983; Lofgren et al. 2006; Putirka 2008), and/or reduced oxygen fugacity (Hammer 2006),  
577 which can result from sulfur degassing during decompression (e.g., Burgisser and Scaillet  
578 2007; Blundy et al. 2008; Okumura et al. 2021). In addition, the enrichment of pyroxene in  
579 Al indicates rapid growth (e.g., Dymek and Gromet 1984; Mollo et al. 2013; Masotta et al.  
580 2020). In our low-SiO<sub>2</sub> samples, the groundmass pyroxene crystals had low-Mg# and  
581 Al-rich rims with distinct boundaries (Figs. 5–7), indicating their rapid growth after an  
582 abrupt change in the surrounding conditions. In other words, their sharp rims formed during  
583 rapid ascent through the shallowest and possibly cold part of the conduit, perhaps in a  
584 gas-pyroclast flow after magma fragmentation (see the next paragraph, Fig. 10). In contrast,  
585 the gradual Mg# zoning without any associated Al enrichment in the high-SiO<sub>2</sub> samples  
586 (Fig. 8) indicates slow ascent or stagnation. These inferences are consistent with our above  
587 interpretation of the tracht-specific CSDs.

588 The time scale for the formation of the sharply zoned rims in the low-SiO<sub>2</sub> samples

589 can be estimated based on the growth rate of pyroxene. Although data on pyroxene growth  
590 rates in dacitic to rhyolitic melts are lacking, pyroxene growth rates on the order of  $10^{-7}$ –  
591  $10^{-5}$  mm/s (time averages over the experimental durations) have been reported from several  
592 crystallization experiments in andesitic (Shea and Hammer 2013) and trachybasaltic melts  
593 (Pontesilli et al. 2019; Masotta et al. 2020). Moreover, *in-situ* observations of pyroxene  
594 crystallization in trachybasalt revealed that the instantaneous growth rate of pyroxene can  
595 reach  $1 \times 10^{-4}$  mm/s (Arzilli et al. 2019, 2022; Le Gall et al. 2021). Assuming that the  
596 instantaneous growth rate is slower in andesitic-dacitic melt than in trachybasaltic melt,  
597 with a maximum value of  $1 \times 10^{-5}$  mm/s, a 100 nm thick rim should form in 10 s. For  
598 comparison, the duration between magma fragmentation and quenching (or vitrification)  
599 can be estimated as follows. Numerical simulations (Suzuki and Koyaguchi 2013, 2015)  
600 indicate that high temperatures in the eruption column can be maintained to up to a few  
601 kilometers above the fragmentation level, corresponding to flight times of a few tens of  
602 seconds at the sound velocity of the gas-pyroclast mixture (e.g., 134 m/s; Suzuki and  
603 Koyaguchi 2013). In cold air (0 °C), a spherical pumice clast 1 cm in diameter would  
604 quench from an initial temperature of 950 °C (Suzuki et al. 2013; Tomiya et al. 2013) by

605 conductive cooling within 10 s at a thermal diffusivity of  $3.2 \times 10^{-7} \text{ m}^2/\text{s}$  (Bagdassarov and  
606 Dingwell 1994). Therefore, it could take several tens of seconds for a pumice clast to  
607 quench in an eruption plume, which is comparable to the minimum timescale of the rim  
608 formation. Further investigation of pyroxene growth rates in dacitic and rhyolitic melts are  
609 required to verify whether the sharply zoned rims observed herein formed after magma  
610 fragmentation.

611 Finally, we note that the change from octagon-dominant to hexagon-dominant  
612 conditions preceded the formation of the low-Mg# rims (Fig. 10) because most hexagonal  
613 crystals had hexagonal zoning boundaries (Fig. 5). Therefore, the tracht change probably  
614 resulted from the ascent condition prior to fragmentation (Fig. 10).

615

## 616 **Implications**

617 Based on the pyroxene trachts, we interpret the magma ascent paths during the  
618 2011 Shinmoedake eruption (Fig. 10). The tracht and size distributions of the pyroxene  
619 microlites (i.e.,  $>1 \mu\text{m}$  wide) are almost the same in all samples (Fig. 3), indicating that the  
620 ascent conditions deeper in the conduit were identical for both the sub-Plinian and



621 Vulcanian eruptions. Consistently, the CSDs of plagioclase microlites (Mujin and  
622 Nakamura 2014; Mujin et al. 2017; Suzuki et al. 2018) were almost the same, regardless of  
623 eruptive style.

624 In the shallow conduit, the magma ascent conditions diverged according to  
625 eruption style: the tracht-specific CSDs of the low-SiO<sub>2</sub> samples (Fig. 3a–c, f) clearly  
626 demonstrate differences in the crystallization kinetics (i.e., nucleation and growth) of  
627 nanolites and microlites. The magma accelerated in the shallow conduit during the  
628 sub-Plinian eruptions, increasing  $\Delta T_{\text{eff}}$  enough to produce hexagonal nanolites before  
629 magma fragmentation. Their sharply zoned low-Mg# rims then formed in the shallowest  
630 part of the conduit or during cooling within the plume. In contrast, the magma ascended  
631 slowly or stagnated in the shallow conduit prior to Vulcanian eruptions, where the relatively  
632 slow growth of pyroxene resulted in gradually zoned rims, when present. This prolonged  
633 crystallization period maintained  $\Delta T_{\text{eff}}$  within octagon-dominant conditions, and the final  
634 rapid ascent accompanied by the fragmentation produced a small number of hexagonal  
635 nanolites.

636 In addition, the CSDs of the low-SiO<sub>2</sub> Vulcanian pumice (V-L; Fig. 3f) are similar

637 to those of the sub-Plinian pumice (Fig. 3a–c), indicating that a portion of the magma  
638 erupted during the Vulcanian eruption followed almost the same ascent paths just prior to  
639 the fragmentation as those during the sub-Plinian eruptions (Fig. 10). Similarly, Matsumoto  
640 and Geshi (2021) reported the co-existence of vesicular low-SiO<sub>2</sub> particles and poorly  
641 vesiculated high-SiO<sub>2</sub> particles in ash collected during the 2018 eruption of Shinmoedake,  
642 which was accompanied by lava effusion and frequent small explosions. They attributed  
643 these different textures to the simultaneous eruption of magmas with different  
644 decompression paths: (1) rapid ascent from deeper parts of the conduit and (2) slow ascent  
645 or stagnation in the shallow conduit. Therefore, the rapid ascent of deeper magma may not  
646 be exclusive to sub-Plinian eruptions at Shinmoedake, but may also be involved in the  
647 Vulcanian eruptions.

648         Our observations have demonstrated the applicability of pyroxene tracht analyses  
649 to the investigation of magma ascent paths in the conduit. The tracht-specific CSDs  
650 recorded the acceleration of magma batches in the shallow conduit, and associated growth  
651 zoning recorded the conditions in the surrounding magma. In addition, the tracht analyses  
652 can be applicable even to glassy pyroclasts with few groundmass crystals resulting from

653 considerably fast ascent. Therefore, pyroxene tracht is expected to be a clue to elucidate  
654 magma dynamics in shallow conduits and those on short time scales just prior to eruptions.  
655 Experiments reproducing the observed tracht-specific CSDs and growth zonations of  
656 groundmass pyroxene crystals will provide information on time-evolution of magma  
657 conditions (e.g., temperature, pressure,  $\Delta T_{\text{eff}}$ ) during syneruptive ascent. This approach is  
658 probably applicable even to glassy pyroclasts produced by explosive eruptions and will  
659 elucidate the mechanisms controlling eruptive style during syneruptive ascent in shallow  
660 conduits.

661

662

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672 **References**

673 Armienti, P. (2008) Decryption of Igneous Rock Textures: Crystal Size Distribution Tools.

674 *Reviews in Mineralogy and Geochemistry*, 69, 623–649.

675 <https://doi.org/10.2138/rmg.2008.69.16>

676 Armienti, P., Pareschi, M.T., Innocenti, F., and Pompilio, M. (1994) Effects of magma

677 storage and ascent on the kinetics of crystal growth. *Contributions to Mineralogy*

678 and *Petrology*, 115, 402–414. <https://doi.org/10.1007/BF00320974>

679 Arzilli, F., and Carroll, M.R. (2013) Crystallization kinetics of alkali feldspars in cooling

680 and decompression-induced crystallization experiments in trachytic melt.

681 *Contributions to Mineralogy and Petrology*, 166, 1011–1027.

682 <https://doi.org/10.1007/s00410-013-0906-1>

683 Arzilli, F., Agostini, C., Landi, P., Fortunati, A., Mancini, L., and Carroll, M.R. (2015)

684 Plagioclase nucleation and growth kinetics in a hydrous basaltic melt by

- 685           decompression experiments. *Contributions to Mineralogy and Petrology*, 170, 55.
- 686           <https://doi.org/10.1007/s00410-015-1205-9>
- 687    Arzilli, F., Piochi, M., Mormone, A., Agostini, C., and Carroll, M.R. (2016a) Constraining
- 688           pre-eruptive magma conditions and unrest timescales during the Monte Nuovo
- 689           eruption (1538 AD; Campi Flegrei, Southern Italy): integrating textural and CSD
- 690           results from experimental and natural trachy-phonolites. *Bulletin of Volcanology*,
- 691           78, 72. <https://doi.org/10.1007/s00445-016-1062-z>
- 692    Arzilli, F., Polacci, M., Landi, P., Giordano, D., Baker, D.R., and Mancini, L. (2016b) A
- 693           novel protocol for resolving feldspar crystals in synchrotron X-ray
- 694           microtomographic images of crystallized natural magmas and synthetic analogs.
- 695           *American Mineralogist*, 101, 2301–2311. <https://doi.org/10.2138/am-2016-5788>
- 696    Arzilli, F., La Spina, G., Burton, M.R., Polacci, M., Le Gall, N., Hartley, M.E., Di Genova,
- 697           D., Cai, B., Vo, N.T., Bamber, E.C., and others. (2019) Magma fragmentation in
- 698           highly explosive basaltic eruptions induced by rapid crystallization. *Nature*
- 699           *Geoscience*, 12, 1023–1028. <https://doi.org/10.1038/s41561-019-0468-6>
- 700    Arzilli, F., Stabile, P., Fabbrizio, A., Landi, P., Scaillet, B., Paris, E., and Carroll, M.R.

- 701 (2020) Crystallization kinetics of alkali feldspar in peralkaline rhyolitic melts:  
702 implications for Pantelleria volcano. *Frontiers in Earth Science*, 8, 177.  
703 <https://doi.org/10.3389/feart.2020.00177>
- 704 Arzilli, F., Polacci, M., La Spina, G., Le Gall, N., Llewellyn, E.W., Brooker, R.A.,  
705 Torres-Orozco, R., Di Genova, D., Neave, D.A., Hartley, M.E., and others. (2022)  
706 Dendritic crystallization in hydrous basaltic magmas controls magma mobility  
707 within the Earth's crust. *Nature Communications*, 13, 3354.  
708 <https://doi.org/10.1038/s41467-022-30890-8>
- 709 Bagdassarov, N., and Dingwell, D. (1994) Thermal properties of vesicular rhyolite. *Journal*  
710 *of Volcanology and Geothermal Research*, 60, 179–191.  
711 [https://doi.org/10.1016/0377-0273\(94\)90067-1](https://doi.org/10.1016/0377-0273(94)90067-1)
- 712 Befus, K.S., and Andrews, B.J. (2018) Crystal nucleation and growth produced by  
713 continuous decompression of Pinatubo magma. *Contributions to Mineralogy and*  
714 *Petrology*, 173, 92. <https://doi.org/10.1007/s00410-018-1519-5>
- 715 Blundy, J., Cashman, K.V., and Berlo, K. (2008) Evolving magma storage conditions  
716 beneath Mount St. Helens inferred from chemical variations in melt inclusions

- 717 from the 1980–1986 and current (2004–2006) eruptions. In D.R. Sherrod, W.E.  
718 Scott, and P.H. Stauffer, Ed., *A Volcano Rekindled: The Renewed Eruption of*  
719 *Mount St. Helens, 2004-2006*, p. 755–790. U.S. Geological Survey, Washington.  
720 <https://doi.org/10.3133/pp175033>
- 721 Brugger, C.R., and Hammer, J.E. (2010a) Crystallization kinetics in continuous  
722 decompression experiments: implications for interpreting natural magma ascent  
723 processes. *Journal of Petrology*, 51, 1941–1965.  
724 <https://doi.org/10.1093/petrology/egq044>
- 725 Brugger, C.R., and Hammer, J.E. (2010b) Crystal size distribution analysis of plagioclase in  
726 experimentally decompressed hydrous rhyodacite magma. *Earth and Planetary*  
727 *Science Letters*, 300, 246–254. <https://doi.org/10.1016/j.epsl.2010.09.046>
- 728 Bruns, S., Stipp, S.L.S., and Sørensen, H.O. (2017) Looking for the signal: A guide to  
729 iterative noise and artefact removal in X-ray tomographic reconstructions of  
730 porous geomaterials. *Advances in water resources*, 105, 96–107.  
731 <https://doi.org/10.1016/j.advwatres.2017.04.020>
- 732 Burgisser, A., and Scaillet, B. (2007) Redox evolution of a degassing magma rising to the

- 733 surface. *Nature*, 445, 194–197. <https://doi.org/10.1038/nature05509>
- 734 Cashman, K.V. (1992) Groundmass crystallization of Mount St. Helens dacite, 1980–1986:  
735 a tool for interpreting shallow magmatic processes. *Contributions to Mineralogy*  
736 and *Petrology*, 109, 431–449. <https://doi.org/10.1007/BF00306547>
- 737 Cashman, K.V., and Marsh, B.D. (1988) Crystal size distribution (CSD) in rocks and the  
738 kinetics and dynamics of crystallization II: Makaopuhi lava lake. *Contributions to*  
739 *Mineralogy and Petrology*, 99, 292–305. <https://doi.org/10.1007/BF00375363>
- 740 Cassidy, M., Manga, M., Cashman, K., and Bachmann, O. (2018) Controls on  
741 explosive-effusive volcanic eruption styles. *Nature communications*, 9, 2839.  
742 <https://doi.org/10.1038/s41467-018-05293-3>
- 743 Castro, J.M., and Dingwell, D.B. (2009) Rapid ascent of rhyolitic magma at Chaitén  
744 volcano, Chile. *Nature*, 461, 780–783. <https://doi.org/10.1038/nature08458>
- 745 Cloetens, P., Pateyron-Salomé, M., Buffiere, J.Y., Peix, G., Baruchel, J., Peyrin, F., and  
746 Schlenker, M. (1997). Observation of microstructure and damage in materials by  
747 phase sensitive radiography and tomography. *Journal of Applied Physics*, 81,  
748 5878–5886. <https://doi.org/10.1063/1.364374>



- 749 Couch, S., Sparks, R.S.J., and Carroll, M.R. (2003) The kinetics of degassing-induced  
750 crystallization at Soufriere Hills Volcano, Montserrat. *Journal of Petrology*, 44,  
751 1477–1502. <https://doi.org/10.1093/petrology/44.8.1477>
- 752 Donaldson, C.H. (1976) An experimental investigation of olivine morphology.  
753 *Contributions to Mineralogy and Petrology*, 57, 187–213.  
754 <https://doi.org/10.1007/BF00405225>
- 755 Duan, X., Wei, C., Liu, Y., and Pei, C. (2010) A molecular dynamics simulation of solvent  
756 effects on the crystal morphology of HMX. *Journal of Hazardous Materials*, 174,  
757 175–180. <https://doi.org/10.1016/j.jhazmat.2009.09.033>
- 758 Dymek, R.F., and Gromet, L.P. (1984) Nature and origin of orthopyroxene megacrysts from  
759 the St-Urbain anorthosite massif, Quebec. *The Canadian Mineralogist*, 22, 297–  
760 326.
- 761 First, E.C., Leonhardi, T.C., and Hammer, J.E. (2020) Effects of superheating magnitude on  
762 olivine growth. *Contributions to Mineralogy and Petrology*, 175, 13.  
763 <https://doi.org/10.1007/s00410-019-1638-7>
- 764 Franke, W.A. (1989) Tracht and habit of synthetic minerals grown under hydrothermal

- 765 conditions. *European Journal of Mineralogy*, 1, 557–566.
- 766 Giuliani, L., Iezzi, G., Vetere, F., Behrens, H., Mollo, S., Cauti, F., Ventura, G., and Scarlato,  
767 P. (2020) Evolution of textures, crystal size distributions and growth rates of  
768 plagioclase, clinopyroxene and spinel crystallized at variable cooling rates from a  
769 mid-ocean ridge basaltic melt. *Earth-Science Reviews*, 204, 103165.  
770 <https://doi.org/10.1016/j.earscirev.2020.103165>
- 771 Gonnermann, H.M., and Manga, M. (2007) The fluid mechanics inside a volcano. *Annual*  
772 *Review of Fluid Mechanics*, 39, 321–356.  
773 <https://doi.org/10.1146/annurev.fluid.39.050905.110207>
- 774 Hammer, J.E. (2006) Influence of  $fO_2$  and cooling rate on the kinetics and energetics of  
775 Fe-rich basalt crystallization. *Earth and Planetary Science Letters*, 248, 618–637.  
776 <https://doi.org/10.1016/j.epsl.2006.04.022>
- 777 Hammer, J.E. (2008) Experimental studies of the kinetics and energetics of magma  
778 crystallization. In K.D. Putirka and F.J. Tepley III, Eds., *Minerals, Inclusions and*  
779 *Volcanic Processes*, 69, p. 9–60. *Reviews in Mineralogy and Geochemistry*,  
780 Mineralogical Society of America, Chantilly, Virginia.

- 781 <https://doi.org/10.2138/rmg.2008.69.2>
- 782 Hammer, J.E., and Rutherford, M.J. (2002) An experimental study of the kinetics of  
783 decompression-induced crystallization in silicic melt. Journal of Geophysical  
784 Research, 107, 1–23. <https://doi.org/10.1029/2001JB000281>
- 785 Hartman, P., and Bennema, P. (1980) The attachment energy as a habit controlling factor: I.  
786 Theoretical considerations. Journal of Crystal Growth, 49, 145–156.  
787 [https://doi.org/10.1016/0022-0248\(80\)90075-5](https://doi.org/10.1016/0022-0248(80)90075-5)
- 788 Hartman, P., and Perdok, W.G. (1955a) On the relations between structure and morphology  
789 of crystals. I. Acta Crystallographica, 8, 49–52.  
790 <https://doi.org/10.1107/S0365110X55000121>
- 791 Hartman, P., and Perdok, W.G. (1955b) On the relations between structure and morphology  
792 of crystals. II. Acta Crystallographica, 8, 521–524.  
793 <https://doi.org/10.1107/S0365110X55001679>
- 794 Higgins, M.D. (2000) Measurement of crystal size distributions. American Mineralogist, 85,  
795 1105–1116. <https://doi.org/10.2138/am-2000-8-901>
- 796 Kato, K., and Yamasato, H. (2013) The 2011 eruptive activity of Shinmoedake volcano,

- 797 Kirishimayama, Kyushu, Japan—overview of activity and volcanic alert level of  
798 the Japan meteorological agency—. *Earth, Planets and Space*, 65, 489–504.  
799 <https://doi.org/10.5047/eps.2013.05.009>
- 800 Kouchi, A., Sugawara, Y., Kashima, K., and Sunagawa, I. (1983) Laboratory growth of  
801 sector zoned clinopyroxenes in the system  $\text{CaMgSi}_2\text{O}_6\text{--CaTiAl}_2\text{O}_6$ . *Contributions*  
802 *to Mineralogy and Petrology*, 83, 177–184. <https://doi.org/10.1007/BF00373091>
- 803 Kozono, T., Ueda, H., Ozawa, T., Koyaguchi, T., Fujita, E., Tomiya, A., and Suzuki, Y.J.  
804 (2013) Magma discharge variations during the 2011 eruptions of Shinmoe-dake  
805 volcano, Japan, revealed by geodetic and satellite observations. *Bulletin of*  
806 *volcanology*, 75, 695. <https://doi.org/10.1007/s00445-013-0695-4>
- 807 La Spina, G., Burton, M., and Arzilli, F. (2016) Role of syn-eruptive plagioclase  
808 disequilibrium crystallization in basaltic magma ascent dynamics. *Nature*  
809 *communications*, 7, 13402. <https://doi.org/10.1038/ncomms13402>
- 810 La Spina, G., Arzilli, F., Llewellyn, E.W., Burton, M.R., Clarke, A.B., Vitturi, M.D.M.,  
811 Polacci, M., Hartley, M.E., Di Genova, D., and Mader, H.M. (2021) Explosivity of  
812 basaltic lava fountains is controlled by magma rheology, ascent rate and

- 813           outgassing. *Earth and Planetary Science Letters*, 553, 116658.
- 814           <https://doi.org/10.1016/j.epsl.2020.116658>
- 815    Le Gall, N., Arzilli, F., La Spina, G., Polacci, M., Cai, B., Hartley, M.E., Vo, N.T., Atwood,  
816           R.C., Di Genova, D., Nonni, S., and others. (2021) In situ quantification of  
817           crystallisation kinetics of plagioclase and clinopyroxene in basaltic magma:  
818           Implications for lava flow. *Earth and Planetary Science Letters*, 568, 117016.
- 819           <https://doi.org/10.1016/j.epsl.2021.117016>
- 820    Lindsley, D.H. (1983) Pyroxene thermometry. *American Mineralogist*, 68, 477–493.
- 821    Liu, X.Y., and Bennema, P. (1996) Theoretical consideration of the growth morphology of  
822           crystals. *Physical Review B*, 53, 2314–2325.
- 823           <https://doi.org/10.1103/PhysRevB.53.2314>
- 824    Lofgren, G. (1974) An experimental study of plagioclase crystal morphology; isothermal  
825           crystallization. *American Journal of Science*, 274, 243–273.
- 826    Lofgren, G (1980) Experimental studies on the dynamic crystallization of silicate melts. In  
827           R.B. Hargraves, Ed., *Physics of magmatic processes*, p. 487–551. Princeton  
828           University Press, Princeton.

- 829 Lofgren, G.E., Huss, G.R., and Wasserburg, G.J. (2006) An experimental study of  
830 trace-element partitioning between Ti-Al-clinopyroxene and melt: Equilibrium and  
831 kinetic effects including sector zoning. *American Mineralogist*, 91, 1596–1606.  
832 <https://doi.org/10.2138/am.2006.2108>
- 833 Mader, H.M., Llewellyn, E.W., and Mueller, S.P. (2013) The rheology of two-phase  
834 magmas: A review and analysis. *Journal of Volcanology and geothermal Research*,  
835 257, 135–158. <https://doi.org/10.1016/j.jvolgeores.2013.02.014>
- 836 Mancini, L., Reinier, E., Cloetens, P., Gastaldi, J., Härtwig, J., Schlenker, M., and Baruchel,  
837 J. (1998) Investigation of structural defects and inhomogeneities in Al-Pd-Mn  
838 icosahedral quasicrystals by combined synchrotron X-ray topography and phase  
839 radiography. *Philosophical Magazine A*, 78, 1175–1194.  
840 <https://doi.org/10.1080/01418619808239982>
- 841 Mangler, M.F., Humphreys, M., Wadsworth, F.B., Iveson, A.A., and Higgins, M.D. (2022)  
842 Variation of plagioclase shape with size in intermediate magmas: a window into  
843 incipient plagioclase crystallisation. *Contributions to Mineralogy and Petrology*,  
844 177, 64. <https://doi.org/10.1007/s00410-022-01922-9>

- 845 Marsh, B.D. (1998) On the interpretation of crystal size distributions in magmatic  
846 systems. *Journal of Petrology*, 39, 553–599.  
847 <https://doi.org/10.1093/petroj/39.4.553>
- 848 Masotta, M., Pontesilli, A., Mollo, S., Armienti, P., Ubide, T., Nazzari, M., and Scarlato, P.  
849 (2020) The role of undercooling during clinopyroxene growth in trachybasaltic  
850 magmas: Insights on magma decompression and cooling at Mt. Etna volcano.  
851 *Geochimica et Cosmochimica Acta*, 268, 258–276.  
852 <https://doi.org/10.1016/j.gca.2019.10.009>
- 853 Matsumoto, K., and Geshi, N. (2021) Shallow crystallization of eruptive magma inferred  
854 from volcanic ash microtextures: a case study of the 2018 eruption of  
855 Shinmoedake volcano, Japan. *Bulletin of Volcanology*, 83, 31.  
856 <https://doi.org/10.1007/s00445-021-01451-6>
- 857 Matsumoto, M., Tsuchiyama, A., Nakato, A., Matsuno, J., Miyake, A., Kataoka, A., Ito, M.,  
858 Tomioka, N., Kodama, Y., Uesugi, K., Takeuchi, A., Nakano, T., and Vaccaro, E.  
859 (2019) Discovery of fossil asteroidal ice in primitive meteorite Acfer 094. *Science*  
860 *Advances*, 5, eaax5078. <https://doi.org/10.1126/sciadv.aax5078>

- 861 Miyake, A., Matsuno, J., and Toh, S. (2014) Sample preparation toward seamless 3D  
862 imaging technique from micrometer to nanometer scale. *Microscopy*, 63, i24–i25.  
863 <https://doi.org/10.1093/jmicro/dfu055>
- 864 Mollard, E., Martel, C., and Bourdier, J.L. (2012) Decompression-induced crystallization in  
865 hydrated silica-rich melts: empirical models of experimental plagioclase  
866 nucleation and growth kinetics. *Journal of Petrology*, 53, 1743–1766.
- 867 Mollo, S., and Hammer, J.E. (2017) Dynamic crystallization in magmas. In W. Heinrich  
868 and R. Abart, Eds., *Mineral reaction kinetics: Microstructures, textures, chemical  
869 and isotopic signatures*, 16, p. 373–418. European Mineralogical Union Notes in  
870 Mineralogy, European Mineralogical Union and Mineralogical Society of Great  
871 Britain and Ireland. <https://doi.org/10.1180/EMU-notes.16.12>
- 872 Mollo, S., Blundy, J.D., Iezzi, G., Scarlato, P., and Langone, A. (2013) The partitioning of  
873 trace elements between clinopyroxene and trachybasaltic melt during rapid cooling  
874 and crystal growth. *Contributions to Mineralogy and Petrology*, 166, 1633–1654.  
875 <https://doi.org/10.1007/s00410-013-0946-6>
- 876 Moschini, P., Mollo, S., Gaeta, M., Fanara, S., Nazzari, M., Petrone, C.M., and Scarlato, P.



- 877 (2021) Parameterization of clinopyroxene growth kinetics via crystal size  
878 distribution (CSD) analysis: Insights into the temporal scales of magma dynamics  
879 at Mt. Etna volcano. *Lithos*, 396–397, 106225.  
880 <https://doi.org/10.1016/j.lithos.2021.106225>
- 881 Mueller, S., Llewellyn, E.W., and Mader, H.M. (2010) The rheology of suspensions of solid  
882 particles. *Proceedings of the Royal Society A: Mathematical, Physical and*  
883 *Engineering Sciences*, 466, 1201–1228. <https://doi.org/10.1098/rspa.2009.0445>
- 884 Mujin, M., and Nakamura, M. (2014) A nanolite record of eruption style transition.  
885 *Geology*, 42, 661–614. <https://doi.org/10.1130/G35553.1>
- 886 Mujin, M., and Nakamura, M. (2020) Late-stage groundmass differentiation as a record of  
887 magma stagnation, fragmentation, and rewelding. *Bulletin of Volcanology*, 82, 48.  
888 <https://doi.org/10.1007/s00445-020-01389-1>
- 889 Mujin, M., Nakamura, M., and Miyake, A. (2017) Eruption style and crystal size  
890 distributions: Crystallization of groundmass nanolites in the 2011 Shinmoedake  
891 eruption. *American Mineralogist*, 102, 2367–2380.  
892 <https://doi.org/10.2138/am-2017-6052CCBYNCND>

- 893 Nakada, S., Nagai, M., Kaneko, T., Suzuki, Y., and Maeno, F. (2013) The outline of the  
894 2011 eruption at Shinmoe-dake (Kirishima), Japan. *Earth, planets and space*, 65,  
895 475–488. <https://doi.org/10.5047/eps.2013.03.016>
- 896 Nakano, T., Nakashima, Y., Nakamura, K., and Ikeda, S. (2000) Observation and analysis  
897 of internal structure of rock using X-ray CT. *Journal of Geological Society of*  
898 *Japan*, 106, 363–378 (in Japanese). <https://doi.org/10.5575/geosoc.106.363>
- 899 Nakano, T., Tsuchiyama, A., Uesugi, K., Uesugi, M., and Shinohara, K. (2006) "Slice"  
900 -Softwares for basic 3-D analysis-. Available: <http://www-bl20.spring8.or.jp/slice/>.  
901 Japan Synchrotron Radiation Research Institute (JASRI), Hyogo.
- 902 Okumura, S., Ishibashi, H., Itoh, S., Suzumura, A., Furukawa, Y., Miwa, T., and Kagi, H.  
903 (2021) Decompression experiments for sulfur-bearing hydrous rhyolite magma:  
904 Redox evolution during magma decompression. *American Mineralogist*, 106, 216–  
905 225. <https://doi.org/10.2138/am-2020-7535>
- 906 Okumura, S.H., Mujin, M., Tsuchiyama, A., and Miyake, A. (2022a) 3D crystal size  
907 distributions of pyroxene nanolites from nano X-ray computed tomography:  
908 Improved correction of crystal size distributions from CSDCorrections for magma

- 909 ascent dynamics in conduits. *American Mineralogist*, 107, 1766–1778.
- 910 <https://doi.org/10.2138/am-2022-8039>
- 911 Okumura, S.H., Okumura, S., and Miyake, A. (2022b) Tract change of groundmass
- 912 pyroxene crystals in decompression experiments. *Journal of Mineralogical and*
- 913 *Petrological Sciences*, 117, 211219. <https://doi.org/10.2465/jmps.211219>
- 914 Polacci, M., Arzilli, F., La Spina, G., Le Gall, N., Cai, B., Hartley, M.E., Di Genova, D., Vo,
- 915 N.T., Nonni, S., Atwood, R.C. and others. (2018) Crystallisation in basaltic
- 916 magmas revealed via *in situ* 4D synchrotron X-ray microtomography. *Scientific*
- 917 *Reports*, 8, 8377. <https://doi.org/10.1038/s41598-018-26644-6>
- 918 Pontesilli, A., Masotta, M., Nazzari, M., Mollo, S., Armienti, P., Scarlato, P., and Brenna, M.
- 919 (2019) Crystallization kinetics of clinopyroxene and titanomagnetite growing from
- 920 a trachybasaltic melt: New insights from isothermal time-series
- 921 experiments. *Chemical Geology*, 510, 113–129.
- 922 <https://doi.org/10.1016/j.chemgeo.2019.02.015>
- 923 Putirka, K.D. (2008) Thermometers and barometers for volcanic systems. *Reviews in*
- 924 *Mineralogy and Geochemistry*, 69, 61–120. <https://doi.org/10.2138/rmg.2008.69.3>

- 925 Rusiecka, M.K., and Martel, C. (2022) Nucleation delay in water-saturated rhyolite during  
926 decompression in shallow volcanic systems and its implications for ascent  
927 dynamics. *Bulletin of Volcanology*, 84, 61.  
928 <https://doi.org/10.1007/s00445-022-01569-1>
- 929 Rusiecka, M.K., Bilodeau, M., and Baker, D.R. (2020) Quantification of nucleation delay  
930 in magmatic systems: experimental and theoretical approach. *Contributions to*  
931 *Mineralogy and Petrology*, 175, 47. <https://doi.org/10.1007/s00410-020-01682-4>
- 932 Schupsky, J.P. (2020) Crystallisation of oxidic gasifier slags. Doctoral dissertation, Fakultät  
933 für Maschinenwesen, Rheinisch-Westfälische Technische Hochschule Aachen,  
934 Aachen. DOI:10.18154/RWTH-2020-10033
- 935 Sekine, T., Katsura, T., and Aramaki, S. (1979) Water saturated phase relations of some  
936 andesites with application to the estimation of the initial temperature and water  
937 pressure at the time of eruption. *Geochimica et Cosmochimica Acta*, 43, 1367–  
938 1376.
- 939 Seto, Y., and Ohtsuka, M. (2022) *ReciPro*: free and open-source multipurpose  
940 crystallographic software integrating a crystal model database and viewer,

- 941 diffraction and microscopy simulators, and diffraction data analysis tools. Journal  
942 of Applied Crystallography, 55, 397–410.  
943 <https://doi.org/10.1107/S1600576722000139>
- 944 Shea, T., and Hammer, J.E. (2013) Kinetics of cooling- and decompression-induced  
945 crystallization in hydrous mafic-intermediate magmas. Journal of Volcanology and  
946 Geothermal research, 260, 127–145.  
947 <https://doi.org/10.1016/j.jvolgeores.2013.04.018>
- 948 Sunagawa, I. (1981) Characteristics of crystal growth in nature as seen from the  
949 morphology of mineral crystals. Bulletin de Minéralogie, 104, 81–87.  
950 <https://doi.org/10.3406/bulmi.1981.7438>
- 951 Sunagawa, I. (2005) Crystals: Growth, Morphology, and Perfection, 295 p. Cambridge  
952 University Press, New York.
- 953 Suzuki, Y., Yasuda, A., Hokanishi, N., Kaneko, T., Nakada, S., and Fujii, T. (2013)  
954 Syneruptive deep magma transfer and shallow magma remobilization during the  
955 2011 eruption of Shinmoe-dake, Japan—Constraints from melt inclusions and  
956 phase equilibria experiments. Journal of Volcanology and Geothermal Research,

- 957 257, 184–204. <https://doi.org/10.1016/j.jvolgeores.2013.03.017>
- 958 Suzuki, Y., Maeno, F., Nagai, M., Shibutani, H., Shimizu, S., and Nakada, S. (2018)
- 959 Conduit processes during the climactic phase of the Shinmoe-dake 2011 eruption
- 960 (Japan): Insights into intermittent explosive activity and transition in eruption style
- 961 of andesitic magma. *Journal of Volcanology and Geothermal Research*, 358, 87–
- 962 104. <https://doi.org/10.1016/j.jvolgeores.2018.02.008>
- 963 Suzuki, Y.J., and Koyaguchi, T. (2013) 3D numerical simulation of volcanic eruption
- 964 clouds during the 2011 Shinmoe-dake eruptions. *Earth, Planets and Space*, 65,
- 965 581–589. <https://doi.org/10.5047/eps.2013.03.009>
- 966 Suzuki, Y.J., and Koyaguchi, T. (2015) Effects of wind on entrainment efficiency in
- 967 volcanic plumes. *Journal of Geophysical Research: Solid Earth*, 120, 6122–6140.
- 968 <https://doi.org/10.1002/2015JB012208>
- 969 Takeuchi, A., Uesugi, K., and Suzuki, Y. (2009) Zernike phase-contrast x-ray microscope
- 970 with pseudo-Kohler illumination generated by sectorized (polygon) condenser plate.
- 971 *Journal of Physics: Conference Series*, 186, 012020.
- 972 <https://doi.org/10.1088/1742-6596/186/1/012020>

- 973 Tomiya, A., Miyagi, I., Saito, G., and Geshi, N. (2013) Short time scales of magma-mixing  
974 processes prior to the 2011 eruption of Shinmoedake volcano, Kirishima volcanic  
975 group, Japan. *Bulletin of Volcanology*, 75, 750.  
976 <https://doi.org/10.1007/s00445-013-0750-1>
- 977 Toramaru, A., Noguchi, S., Oyoshihara, S., and Tsune, A. (2008) MND(microlite number  
978 density) water exsolution rate meter. *Journal of Volcanology and Geothermal*  
979 *Research*, 175, 156–167. <https://doi.org/10.1016/j.jvolgeores.2008.03.035>
- 980 Tsuchiyama, A., Uesugi, M., Matsushima, T., Michikami, T., Kadono, T., Nakamura, T.,  
981 Uesugi, K., Nakano, T., Sandford, S.A., Noguchi, R., and others. (2011)  
982 Three-dimensional structure of Hayabusa samples: origin and evolution of Itokawa  
983 regolith. *Science*, 333, 1125–1128. <https://doi.org/10.1126/science.1207807>
- 984 Tsuchiyama, A., Nakano, T., Uesugi, K., Uesugi, M., Takeuchi, A., Suzuki, Y., Noguchi, R.,  
985 Matsumoto, T., Matsuno, J., Nagano, T., and others. (2013) Analytical dual-energy  
986 microtomography: A new method for obtaining three-dimensional phase images  
987 and its application to Hayabusa samples. *Geochimica et Cosmochimica Acta*, 116,  
988 5–16. <https://doi.org/10.1016/j.gca.2012.11.036>

- 989 Ubide, T., and Kamber, B.S. (2018) Volcanic crystals as time capsules of eruption  
990 history. *Nature Communications*, 9, 326.  
991 <https://doi.org/10.1038/s41467-017-02274-w>
- 992 Uesugi, K., Takeuchi, A., and Suzuki, Y. (2006) Development of micro-tomography system  
993 with Fresnel zone plate optics at SPring-8. In U. Bonse, Ed., *Proceedings of SPIE*  
994 *OPTICS + PHOTONICS*, 6318, 63181F. International Society for Optics and  
995 Photonics, Bellingham, Washington. <https://doi.org/10.1117/12.679822>
- 996 Van Panhuys-Sigler, M., and Hartman, P. (1981) Morphologie théorique de certains  
997 pyroxenes déduite de la structure cristalline. *Bulletin de Minéralogie*, 104, 95–106  
998 (in French). <https://doi.org/10.3406/bulmi.1981.7441>
- 999 Watanabe, M., and Williams, D.B. (2006) The quantitative analysis of thin specimens: a  
1000 review of progress from the Cliff-Lorimer to the new  $\zeta$ -factor methods. *Journal of*  
1001 *microscopy*, 221, 89–109. <https://doi.org/10.1111/j.1365-2818.2006.01549.x>
- 1002 Waters, L.E., Andrews, B.J., and Lange, R.A. (2015) Rapid crystallization of plagioclase  
1003 phenocrysts in silicic melts during fluid-saturated ascent: phase equilibrium and  
1004 decompression experiments. *Journal of Petrology*, 56, 981–1006.



1005                    <https://doi.org/10.1093/petrology/egv025>

1006

1007

### Figure captions

1008 **Figure 1.** Classification of crystal trachts. (a) Cross sections of groundmass pyroxene  
1009 crystals were classified based on the number of faces between a given pair of parallel faces  
1010 (indicated by yellow circles). (b) Incomplete shapes were classified similarly if a pair of  
1011 parallel faces was present. (c) Individual segments of attached crystals were classified in a  
1012 similar manner.

1013

1014 **Figure 2.** Backscattered electron (BSE) images of groundmass pyroxenes in (a) sub-Plinian  
1015 pumice sP\_a and (b) high-SiO<sub>2</sub> Vulcanian pumice V-H\_a from the 2011 Shinmoedake  
1016 eruption. These images were obtained by FE-SEM at an acceleration voltage of 10 kV. The  
1017 tracht of each pyroxene crystal (i.e., octagonal, heptagonal, or hexagonal) is indicated by  
1018 colored symbols (blue square, red diamond, and yellow triangle, respectively).  
1019 Abbreviations: Pl, plagioclase; Px, pyroxene.

1020

1021 **Figure 3.** Tracht-specific CSDs of groundmass pyroxenes in the pumice samples. The  
1022 conventional CSDs (i.e., including all trachts) are plotted in black for comparison. The size

1023 range shown is from 0.10 to 6.31  $\mu\text{m}$  in width (short-axis length). Open symbols with  
1024 dashed lines represent data in size intervals where fewer than three crystals could be  
1025 counted. **(a–c)** Sub-Plinian pumices; **(d, e)** high-SiO<sub>2</sub> Vulcanian pumices; **(f)** low-SiO<sub>2</sub>  
1026 Vulcanian pumice.

1027

1028 **Figure 4.** 3D shape and plane indices of a relatively large hexagonal pyroxene microlite  
1029 from the dense juvenile fragment V-L-djf. **(a)** The CT image and **(b)** 3D reconstruction  
1030 acquired by SR-XnCT are shown with the crystallographic orientation as determined by  
1031 EBSD analysis. The crystallographic indices of the prismatic faces are also noted in **(b)**.  
1032 The lower end of the crystal corresponds to the polished sample surface.

1033

1034 **Figure 5.** Representative internal texture of groundmass pyroxenes in the sub-Plinian  
1035 pumice sP\_a. The results of TEM analyses for a hexagonal nanolite in the sub-Plinian  
1036 pumice sP\_a are shown. **(a)** An ADF-STEM image and **(b–d)** Ca, Al, and Mg# (=Mg/(Mg  
1037 + Fe) in mol) compositional maps, respectively, were obtained along the [001] zone axis.  
1038 **(e)** A bright-field (BF) TEM image and **(f–h)** the SAED patterns of each domain were

1039 obtained at another orientation. The medium gray shape around the pyroxene in (e) is the  
1040 bright-field background, not an overgrowth. The two Cpx domains (f, h) have a twin  
1041 relationship. Quantitative compositional data are reported in Supplementary Table S1.  
1042 Abbreviations: Opx, orthopyroxene; Cpx, clinopyroxene.

1043

1044 **Figure 6.** Internal texture of a hexagonal pyroxene microlite in the sub-Plinian pumice sP\_a.  
1045 (a) An ADF-STEM image and (b–d) Ca, Al, and Mg# compositional maps, respectively,  
1046 were obtained along the [001] zone axis, indicating the extinction of {100} faces during  
1047 growth. (e) A schematic view of the zoning boundaries. The dashed lines represent the  
1048 phase boundaries. (f) The SAED pattern of the Pgt domain at the center was obtained along  
1049 the  $[0\bar{1}2]$  zone axis. This crystallographic orientation is common in the crystal.  
1050 Abbreviations: Pgt, pigeonite; Aug, augite.

1051

1052 **Figure 7.** Internal texture of (a–d) a microlite and (e–h) a nanolite in the low-SiO<sub>2</sub>  
1053 Vulcanian pumice V-L. (a, e) The ADF-STEM images and (b–d, f–h) Ca, Al, and Mg#  
1054 compositional maps, respectively, were obtained along the [001] zone axes. As shown in (a,

1055 e), the two crystals have growth zonations of the same tracht as their external forms. The  
1056 Cpx domains have a twin relationship in the microlite whereas those in the nanolite have  
1057 the same crystallographic orientation. Abbreviations: Pgt, pigeonite; Opx, orthopyroxene;  
1058 Cpx, clinopyroxene.

1059

1060 **Figure 8.** Internal texture of (a–d) a microlite and (e–h) a nanolite in the high-SiO<sub>2</sub>  
1061 Vulcanian pumice V-H\_a. (a, e) The ADF-STEM images and (b–d, f–h) Ca, Al, and Mg#  
1062 compositional maps, respectively, were obtained along the [001] zone axes. Cpx domains in  
1063 both crystals show twin relationships. Abbreviations: Pgt, pigeonite; Opx, orthopyroxene;  
1064 Cpx, clinopyroxene.

1065

1066 **Figure 9.** Schematic illustration of the observed textures of groundmass pyroxenes. The  
1067 typical textures of groundmass pyroxenes in (a) the low-SiO<sub>2</sub> and (b) the high-SiO<sub>2</sub>  
1068 pumices are shown with their tracht-specific CSDs and internal textures. The tracht-specific  
1069 CSDs of samples (a) sP\_a and (b) V-H\_a are provided as representative of each type of  
1070 pumice. The inserted illustrations of pyroxene crystals show typical zoning patterns (blue:

1071 low-Mg# rim) at the parts of the CSDs indicated by the arrows.

1072

1073 **Figure 10.** Schematic illustration of pyroxene crystallization kinetics and magma ascent  
1074 paths during the 2011 Shinmoedake eruption. **(a)** Pressure–time paths and **(b)**  $\Delta T_{\text{eff}}$ –time  
1075 paths of the magmas that formed the low-SiO<sub>2</sub> and high-SiO<sub>2</sub> pumices are shown in orange  
1076 and blue, respectively. The time evolution of the pyroxene texture is also shown in **(a)**. The  
1077 low-Mg# rims formed in the shallowest part of the conduit (blue shaded area in **(a)**). The  
1078 vertical dashed line indicates the time when  $\Delta T_{\text{eff}}$  exceeded the threshold between  
1079 octagon-dominant and hexagon-dominant conditions (gray horizontal line in **(b)**) preceding  
1080 the formation of the low-Mg# rims. The possible timings of magma fragmentation events  
1081 are indicated by stars.

1082

Table 1. Average chemical compositions of groundmass glasses (wt%).

	Sub-Plinian			Vulcanian			
	sP_a <sup>a</sup>	sP_b	sP_c	V-H_a <sup>a</sup>	V-H_b	V-L	V-L-djf
SiO <sub>2</sub>	67.33 (41)	66.64 (27)	67.80 (35)	71.69 (21)	72.35 (29)	66.83 (45)	67.52 (61)
TiO <sub>2</sub>	0.88 (5)	1.00 (4)	0.90 (5)	0.73 (4)	0.70 (4)	0.94 (6)	0.84 (8)
Al <sub>2</sub> O <sub>3</sub>	14.15 (26)	14.06 (21)	14.06 (16)	12.66 (9)	12.52 (18)	14.09 (23)	14.36 (20)
FeO	5.75 (25)	6.41 (16)	5.63 (19)	4.24 (13)	3.95 (13)	6.23 (30)	5.43 (45)
MnO	0.11 (5)	0.11 (5)	0.11 (4)	0.10 (4)	0.03 (5)	0.12 (5)	0.11 (4)
MgO	1.13 (8)	1.15 (9)	0.98 (5)	0.64 (3)	0.58 (6)	1.14 (11)	1.06 (10)
CaO	3.92 (19)	4.08 (10)	3.67 (13)	2.56 (9)	2.35 (11)	3.99 (15)	3.92 (19)
Na <sub>2</sub> O	3.38 (10)	3.30 (10)	3.35 (8)	3.28 (12)	3.42 (9)	3.33 (9)	3.35 (8)
K <sub>2</sub> O	3.24 (8)	3.12 (6)	3.37 (6)	3.93 (4)	3.98 (7)	3.22 (8)	3.29 (11)
P <sub>2</sub> O <sub>5</sub>	0.11 (5)	0.13 (5)	0.13 (4)	0.16 (4)	0.11 (8)	0.12 (4)	0.12 (4)
Total	100	100	100	100	100	100	100

NOTES: Each sample was analyzed in 50 distinct regions.

Values in parentheses are standard deviations.

Oxide concentrations were recalculated to total 100% by cation balance.

<sup>a</sup> Data from Okumura et al. (2022a) are corrected for losses of Na and K during the measurements.

Table 2. Conditions and results of SR-XnCT analyses.

Eruptive style	CT specimen	Voxel size (nm)	Number of crystals analyzed <sup>a</sup>	Average 3D aspect ratio		
				<i>S</i>	<i>I</i> <sup>b</sup>	<i>L</i> <sup>b</sup>
sub-Plinian	sP_a-1	40.00	74	1.0	1.4 <sup>c</sup> (6)	9.4 <sup>c</sup> (56)
	sP_a-2	24.70	103			
	sP_b	77.80	123	1.0	1.4 (3)	8.7 (46)
	sP_c	77.80	151	1.0	1.3 (2)	8.4 (44)
Vulcanian	V-H_a-1	33.86	47	1.0	1.3 <sup>c</sup> (4)	5.1 <sup>c</sup> (39)
	V-H_a-2	34.70	86			
	V-H_b	77.80	95	1.0	1.3 (4)	5.6 (40)
	V-L	77.80	163	1.0	1.4 (3)	6.5 (42)
	V-L-djf	34.70	1			

<sup>a</sup> Crystals smaller than 5 pixels in the shortest dimension *S* were excluded.

<sup>b</sup> Values in parentheses are standard deviations.

<sup>c</sup> Values averaged from two CT specimens; data from Okumura et al. (2022a).



Table 3. Parameters used in *CSDCorrections*.

Eruptive style	Sample	Number of regions	Analyzed area (excluding vesicles)		Number of crystal cross sections				3D aspect ratio	Roundness	Size scale length (Bins per decade <sup>c</sup> )
			( $\mu\text{m}^2$ )	(vesicle%) <sup>b</sup>	All	Octagon	Heptagon	Hexagon			
sub-Plinian	sP_a	1 <sup>a</sup>	20,077	57.3	793	83	34	385	1:1.4:9.4	0.8	5
	sP_b	2	15,291	37.2	1,037	167	59	399	1:1.4:8.7		
	sP_c	2	15,566	35.9	728	43	27	305	1:1.3:8.4		
Vulcanian	V-H_a	1 <sup>a</sup>	19,791	54.5	381	171	9	10	1:1.3:5.1		
	V-H_b	3	14,268	60.9	319	142	8	5	1:1.3:5.6		
	V-L	2	12,533	48.5	645	115	36	242	1:1.4:6.5		

<sup>a</sup> A single larger region comprising multiple BSE images (Okumura et al. 2022a).

<sup>b</sup> The percentage of vesicles in the analyzed rectangle area.

<sup>c</sup> Logarithmic base-10 size scale.

Figure 1

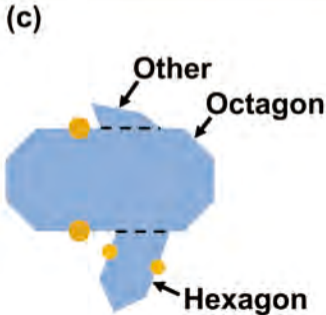


Figure 2

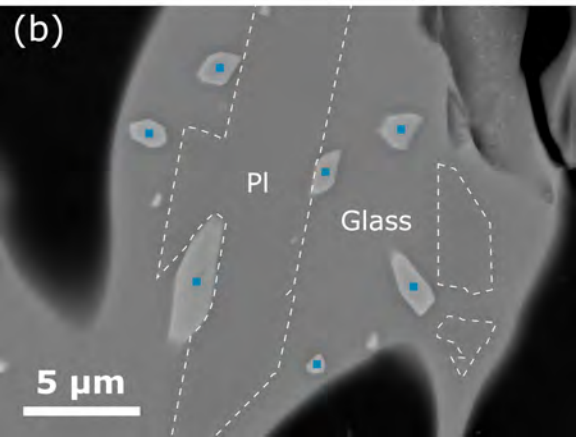
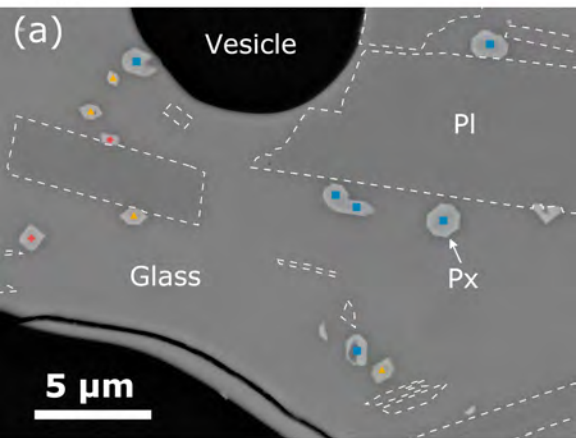


Figure 3

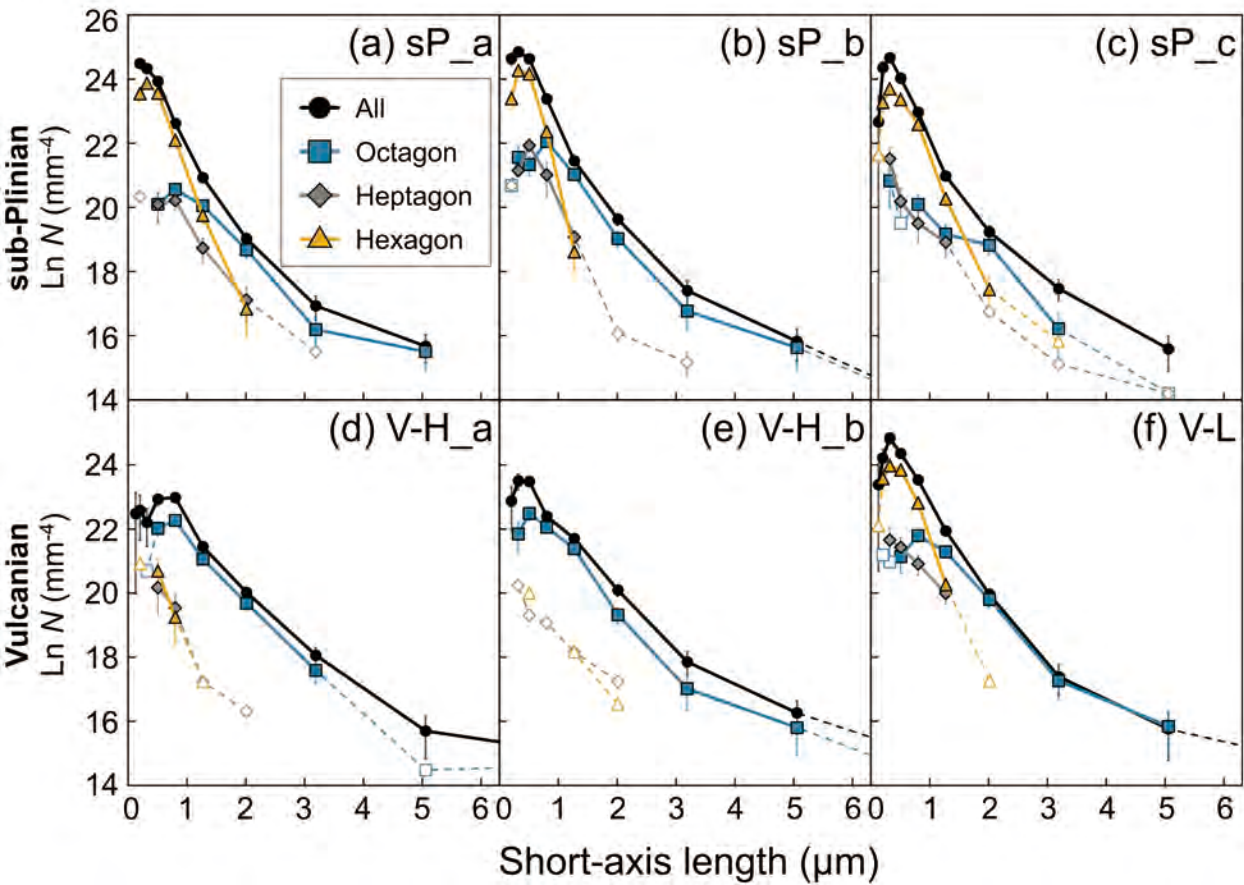


Figure 4

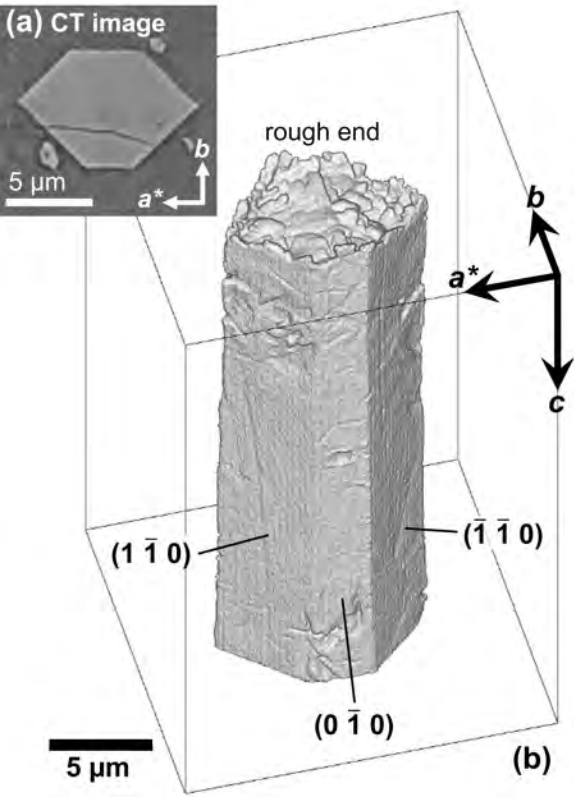


Figure 5

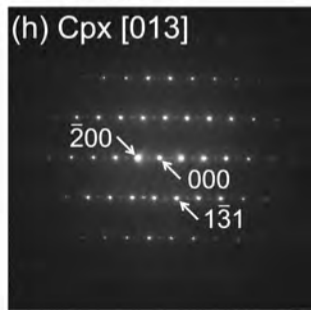
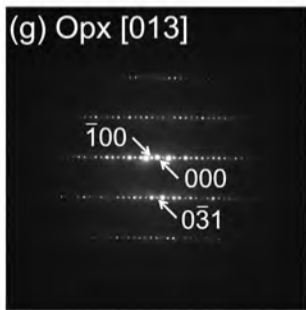
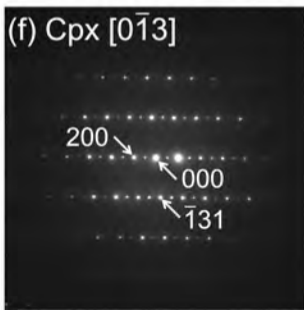
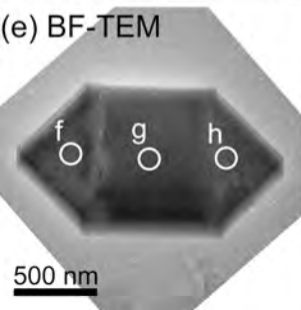
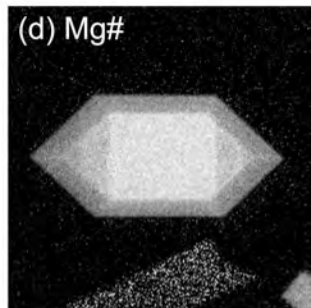
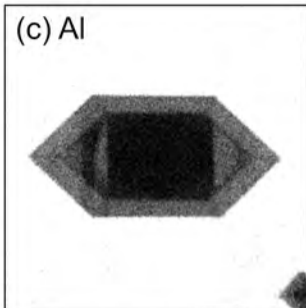
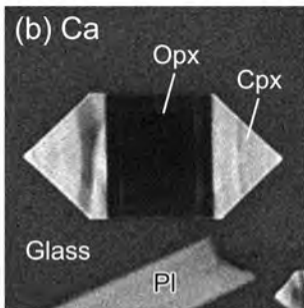
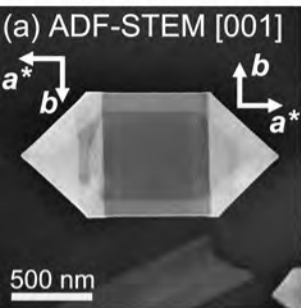


Figure 6

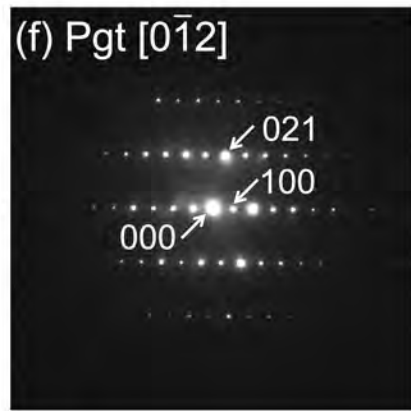
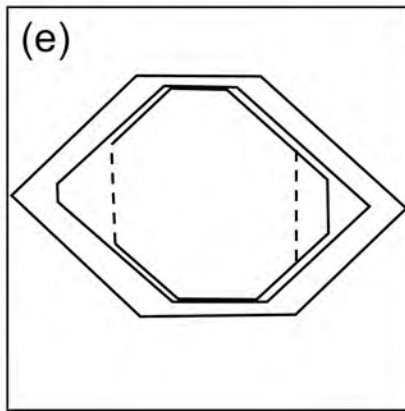
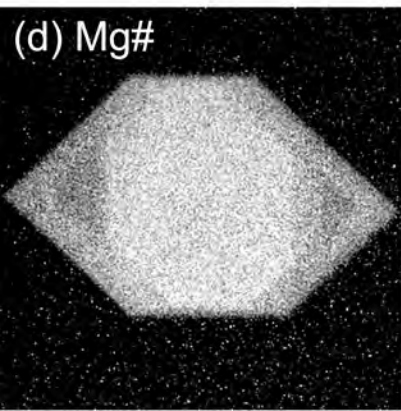
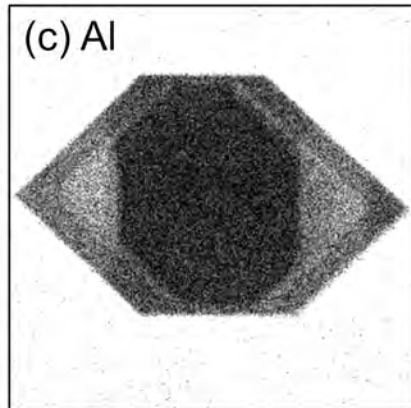
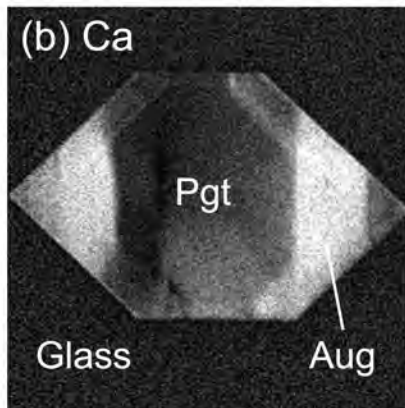
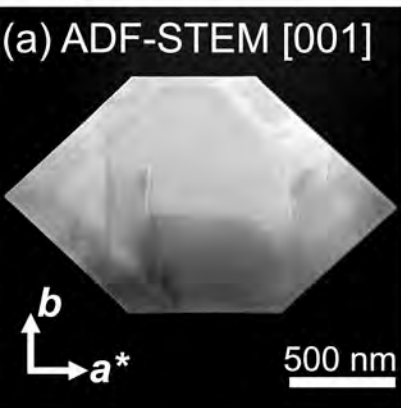


Figure 7

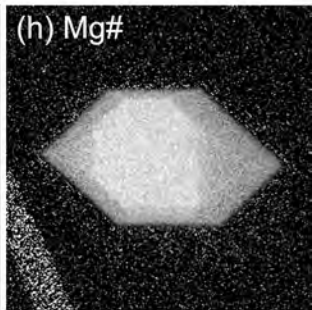
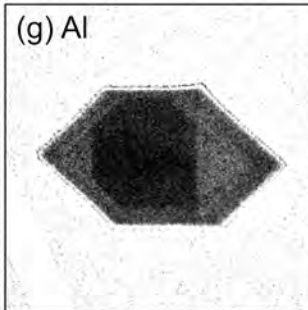
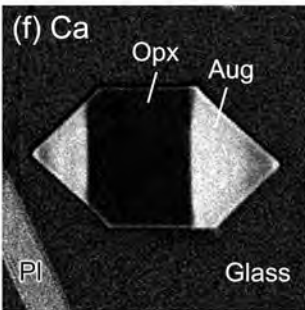
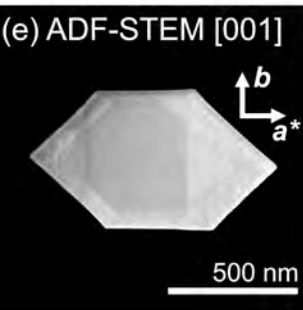
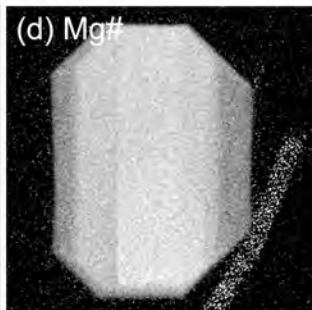
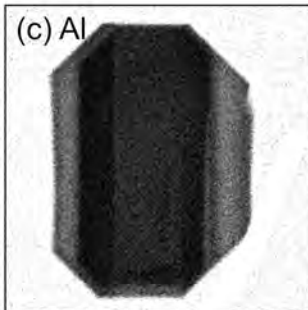
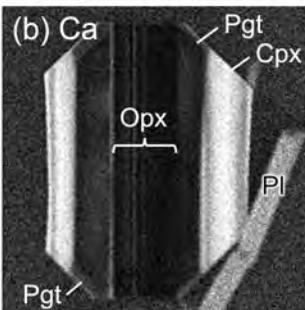
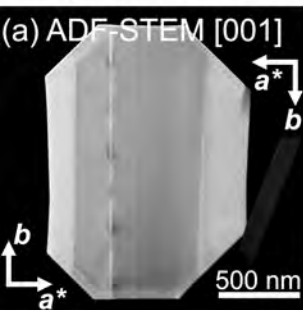




Figure 8

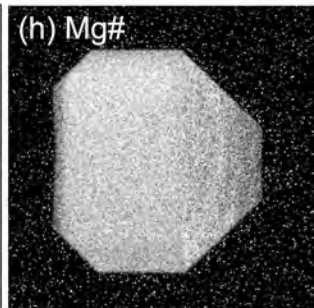
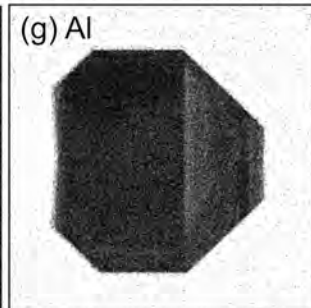
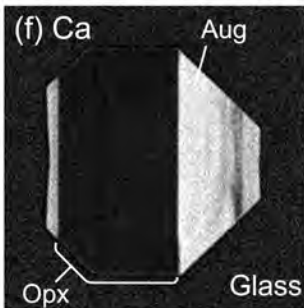
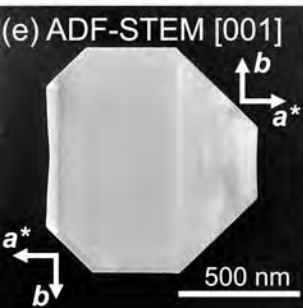
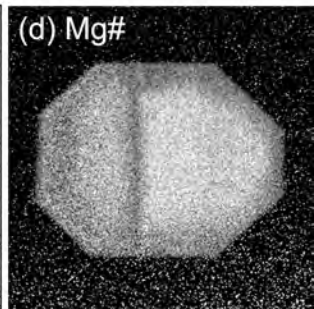
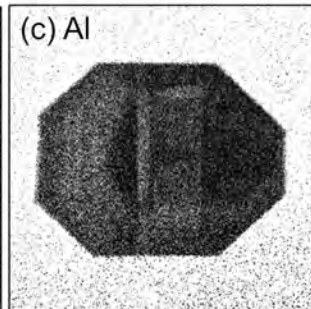
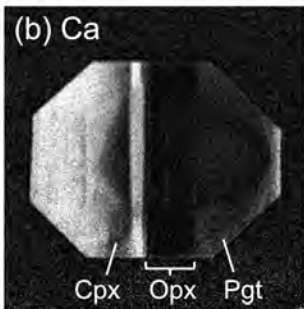
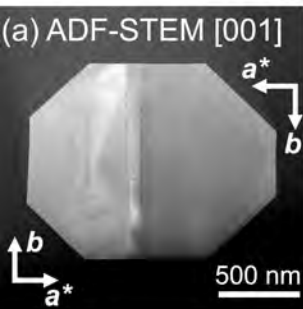


Figure 9

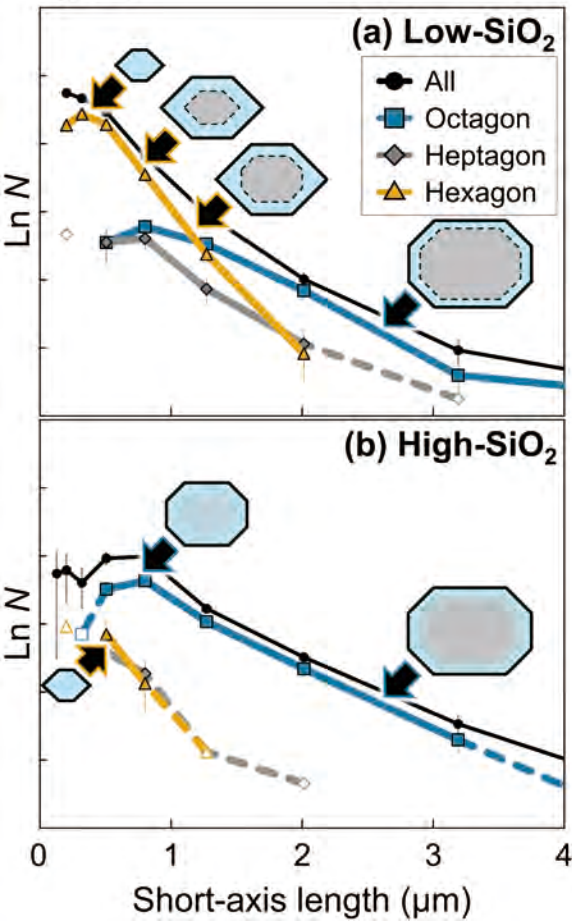
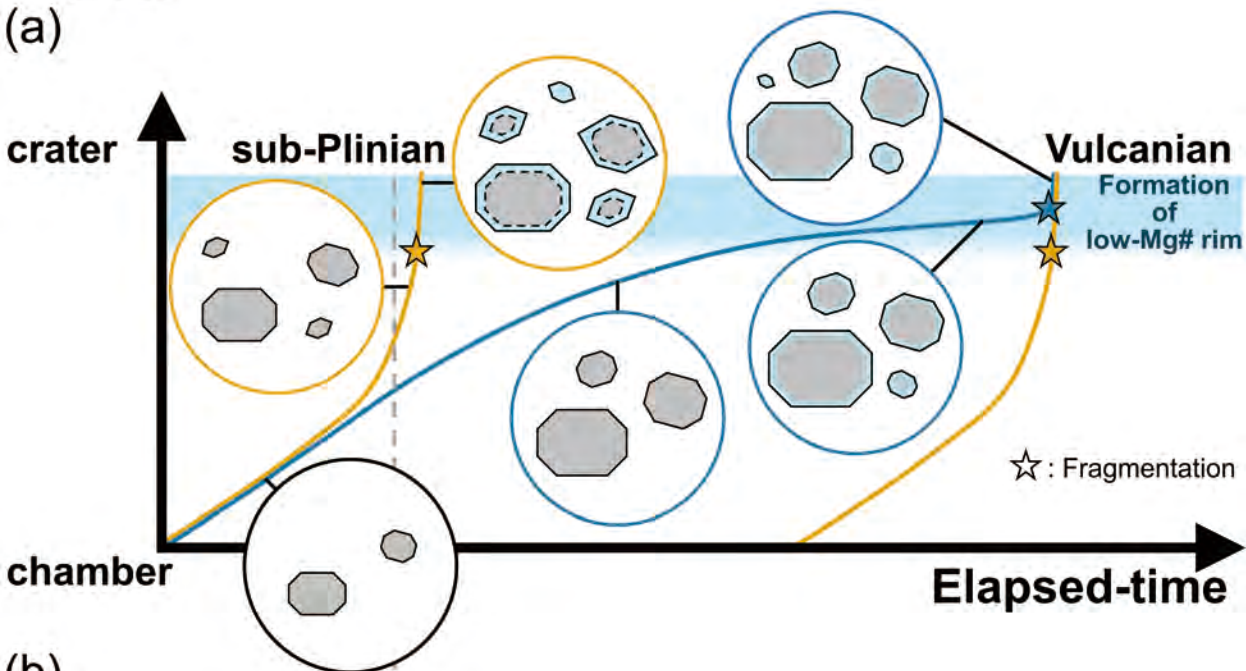


Figure 10

(a)



(b)

