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4 **Plagioclase population dynamics and zoning in response to changes in temperature and**
5 **pressure**

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9

10 **Abstract**

11 Zoned plagioclase crystals are commonly interpreted as proxies for magmatic history, because
12 the mineral occurs in most silicic magmas and has compositional sensitivity to pressure,
13 temperature, and melt composition with slow internal diffusion that preserves zoning. Changes in
14 growth rates and crystal dissolution complicate quantitative relation of time to particular zoning
15 patterns. The numerical model SNGPlag uses Rhyolite MELTS to determine the equilibrium
16 phase assemblage and compositions for a user-defined magma composition, experimentally
17 determined instantaneous nucleation and growth rates, and reasonable dissolution rates to
18 examine plagioclase crystallization and population dynamics through time. SNGPlag tracks the
19 numbers, sizes, morphologies, and compositional zoning of plagioclase crystals through time in
20 response to changes in pressure, temperature, and volume or mass inputs. Results show that
21 significant fractions of time are missing from the crystal record because of effectively zero
22 growth rates, or erased through dissolution; those processes can together remove >>50% of time
23 from the crystal record. Temperature- (or pressure-) cycling alone will not produce substantial

24 compositional zoning, rather growth of complexly zoned phenocrysts requires the addition of
25 new magma. Comparison of the input pressure-temperature-time series with compositional
26 transects shows the crystal record is biased towards more recent intervals and periods of
27 decreasing temperature (i.e., neither peak temperatures nor intervals of prolonged, cool storage
28 are favored). Crystallization (or dissolution) acts to return magmas to near-equilibrium crystal
29 fractions within 100s of days.

30

31

Introduction

32 Volcanic rocks provide the only record of magmatic processes for all ancient or
33 prehistoric eruptions and at most presently active volcanoes, the exceptions being a relative
34 handful of monitored or instrumented volcanoes. The bulk chemical and isotopic compositions
35 of rock and glass provide an integrative record of fractional crystallization, magma recharge and
36 mixing, and crustal assimilation preceding eruption. Certain mineral phases tend to develop and
37 maintain compositional zoning that records changes in magmatic conditions, providing time-
38 series of magmatic processes.

39 Plagioclase is used to describe pre-eruptive magmatic processes as it is a generally
40 abundant phenocryst phase common to many volcanic systems. Numerous workers analyze
41 compositional and/or isotopic zoning together with phenocryst textures to interpret changes in
42 pressure and temperature, or magma recharge and mixing (e.g., Gerlach and Grove, 1982;
43 Anderson, 1984; Tsuchiyama, 1985; Singer et al., 1995; Davidson and Tepley, 1997; Tepley et
44 al., 1999; Tepley et al., 2000; Davidson et al., 2001; Costa et al., 2003; Browne et al., 2006;
45 Andrews et al., 2008; Costa et al., 2008; Salisbury et al., 2008; Streck et al., 2008; Waters et al.,
46 2015). U-series geochronometry has been applied to zoned crystals, typically zircons, from some

47 magmas to constrain the timescales of at least a portion of the histories recorded by individual
48 crystals (Cooper and Reid, 2003; Cooper and Kent, 2014; Budd et al., 2017). Unfortunately,
49 many crystals show evidence of dissolution, thus their records are not complete and the degree to
50 which they are incomplete is largely unknown. This observation, coupled with the variability of
51 growth rates as a function of pressure, temperature, and supersaturation (Hammer and
52 Rutherford, 2002; Mollard, et al., 2012; Befus and Andrews, 2018), complicates quantitative
53 relation of time to particular zoning patterns (Figure 1).

54 We use a numerical model of crystal nucleation, growth, and dissolution to examine how
55 crystal populations and zoning patterns record time-varying magmatic conditions. The model
56 shows that crystal dissolution is common in magmas with fluctuations in temperature and, to a
57 much lesser extent, pressure (primarily reflecting dissolved water concentration in the melt).
58 Moderate fluctuations in storage conditions can cause some dissolution, and larger excursions in
59 temperature will likely dissolve all small crystals. Consequently, populations of smaller crystals
60 most likely only record events subsequent to the most recent recharge event, whereas larger
61 crystals preserve greater fractions of the total history. Dissolution often removes substantial
62 portions of the crystal record, such that <50% of the total time may be preserved. The
63 relationship between crystal thickness and time is not constant. Because most growth is
64 accommodated during relatively short intervals of cooling following a recharge or heating event,
65 those intervals tend to be overrepresented in the crystals as compared to much longer periods
66 spent at lower temperature.

67

68

Background

69 Phenocrysts form (or dissolve) in response to thermodynamic disequilibrium, e.g.,
70 changes in pressure, temperature, oxygen fugacity, and/or composition. Supersaturation results in
71 nucleation and growth of a particular phase, whereas undersaturation results in dissolution (e.g.
72 Ghiorso and Sack, 1995; Gualda et al., 2012; Ghiorso and Gualda, 2015). Nucleation, growth,
73 and dissolution rates are controlled by the degree of disequilibrium, with high supersaturation or
74 undersaturation resulting in faster rates (Donaldson, 1985; Tsuchiyama, 1985; Hammer and
75 Rutherford, 2002; Szramek et al., 2006; Andrews and Gardner, 2010; Brugger and Hammer,
76 2010; Mollard et al., 2012; Boehnke et al., 2013; Shea and Hammer, 2013; Zhang and Xu, 2016;
77 Befus and Andrews, 2018) with the caveat that high melt viscosities, or other kinetic barriers,
78 can effectively prevent crystallization or dissolution. Both growth and dissolution act to reduce
79 disequilibrium such that crystallization or dissolution rate slows as the magma approaches
80 equilibrium. Growth and dissolution rates describe how fast a single crystal face responds, and
81 the evolution of those rates through time reflects the sum of growth or dissolution across the
82 entire crystal population (Befus and Andrews, 2018; Andrews and Befus, 2020).

83 Plagioclase feldspar is ubiquitous as a major mineral phase in arc magmas (e.g. Vance,
84 1965; Nelson and Montana, 1992; Singer et al., 1995; Davidson and Tepley, 1997; Salisbury et
85 al., 2008). The mineral is sensitive to changes in pressure, temperature, and melt composition,
86 with more calcic (anorthitic) compositions occurring in higher temperature, higher pressure
87 (particularly P_{H_2O}), and/or more mafic magmas. Numerous experimental studies exploit that
88 compositional dependence to determine pre-eruptive storage conditions (e.g. Rutherford et al.,
89 1985; Gardner et al., 1995; Martel et al., 1999; Andrews and Gardner, 2010; Sosa-Ceballos et al.,
90 2014) and develop various geothermometers and hygrometers (e.g. Housh and Luhr, 1991;
91 Putirka, 2005; Lange et al., 2009; Waters and Lange, 2015). The crystal structure of plagioclase,

92 the coupled CaAl-NaSi substitution, and the slow intracrystalline diffusion of those species
93 prevent compositional homogenization, thus compositional zoning is a proxy for the pressure-
94 temperature-compositional history of a given plagioclase. This is in contrast to minerals with no
95 major element sensitivity to those conditions, or those, like olivine, with fast internal diffusion
96 that removes most major element compositional zoning (Shea et al., 2019).

97 In general, concentrically zoned plagioclase are interpreted to record episodes of
98 increasing and decreasing temperature and/or pressure, as well as changes in magma
99 composition (e.g. Singer et al., 1995; Davidson and Tepley, 1997; Clyne, 1999; Tepley et al.,
100 1999; Tepley et al., 2000; Wallace and Bergantz, 2005; Andrews et al., 2008; Costa et al., 2008;
101 Sosa-Ceballos et al., 2014). Crystal cores record older events than the subsequently formed rims,
102 although sectioning effects biases sampled crystal populations away from cores (Wallace and
103 Bergantz, 2005; Cheng et al., 2017).

104 Plagioclase zoning patterns are often interpreted to record magma mixing or recharge
105 (e.g. Eichelberger, 1978; Tepley et al., 2000; Humphreys et al., 2006; Andrews et al., 2008;
106 Sosa-Ceballos et al., 2014). Although recharge or mixing can trigger eruption, many of those
107 events do not result in eruption. For example, both El Chichón and Popocateptl show evidence
108 for many more recharge events than eruptions (Espindola et al., 2000; Tepley et al., 2000;
109 Andrews et al., 2008; Sosa-Ceballos et al., 2014).

110 Non-euhedral growth and crystal dissolution both act to complicate simple “tree-ring”
111 interpretations of zoning. The dependence of growth texture on supersaturation (or undercooling)
112 is explored in detail by Hammer and Rutherford (2002), who demonstrate that euhedral prismatic
113 crystals only nucleate and grow under a limited set of conditions. Sieved plagioclase likely
114 records growth during water-undersaturated decompression (Nelson and Montana, 1992;

115 Humphreys et al., 2006). Kawamoto (1992) shows that some patchy zoning in plagioclase may
116 record initially skeletal habits, and Shea et al. (2019) have shown that some euhedral olivine
117 crystals form through infilling of initially skeletal growth.

118 Partial or complete dissolution will occur when a mineral is introduced to a melt in which
119 it is undersaturated (e.g., Donaldson, 1985; Tsuchiyama, 1985; Ghiorso and Sack, 1995;
120 Boehnke et al., 2013; Zhang and Xu, 2016). Dissolution thus removes portions of the crystal
121 record. Many workers have shown that dissolution surfaces are common and often repeated in
122 zoned crystals (e.g. Tepley et al., 1999; Salisbury et al., 2008; Streck et al., 2008). Unfortunately,
123 although differential dissolution between different faces can indicate the minimum amount of
124 dissolution, the absolute amount of dissolution associated with each surface is usually unknown.

125 Because crystals are the result of time-integrated nucleation, growth, and dissolution
126 processes, the compositional zoning profile of a given crystal can, in principle, be converted into
127 a timeseries if growth and dissolution rates are known or assumed. Many previous experimental
128 studies have described plagioclase nucleation and growth (e.g. Hammer and Rutherford, 2002;
129 Hammer, 2004; Couch et al., 2003; Larsen, 2005; Brugger and Hammer, 2010; Shea and
130 Hammer, 2013; Befus and Andrews, 2018), although most present time-averaged rates.
131 Plagioclase dissolution rates, in contrast, are largely undescribed in the literature, with studies by
132 Tsuchiyama (1985) showing composition-dependent rates, and Donaldson (1985) indicating that
133 dissolution is approximately twice as fast as growth.

134 Previous researchers apply numerical models to understand and interpret plagioclase
135 zoning patterns, with many of these efforts focused on small amplitude and short length scale
136 oscillatory zoning. Haase et al. (1980) use a composition-dependent growth rate to show that
137 oscillatory zoning can develop over a wide range of parameter space. L'Heureux and Fowler

138 (1994) show that disequilibrium at the crystal-melt interface drives crystallization, and
139 oscillatory zoning can develop depending on the partition of material into the crystal and the
140 relative growth and diffusion rates. Gorokhova et al. (2013) present a model of plagioclase rim
141 growth during decompression that reproduces compositional zoning observed in samples from
142 Bezymianny. Notably, none of those studies address crystal dissolution, the evolution of
143 populations through time, nor timescales substantially in excess of 10s of days.

144

145 **Numerical Model of Plagioclase Nucleation, Growth, and Dissolution**

146 We examine plagioclase crystallization and dissolution within an initially 1 m³ model
147 volume using a modified version of the program SNGPlag (Andrews and Befus, 2020); the new
148 version allows for longer model runs, time-variant temperature and pressure, and crystal
149 dissolution. We briefly describe the original SNGPlag model, before describing the
150 modifications. Following Befus and Andrews (2018) and Andrews and Befus (2020),
151 “supersaturation” describes the disequilibrium of the system, rather than “undercooling,” as the
152 former can be readily calculated or measured. Note that in this formulation, a negative
153 supersaturation (“undersaturation”) refers to a system with an excess of crystals, i.e. a system in
154 which crystals should dissolve.

155

156 ***SNGPlag Model***

157 Supersaturation Nucleation and Growth of Plagioclase (SNGPlag) is an iterative
158 numerical model that predicts plagioclase sizes and abundances as a function of magma
159 composition, temperature, and decompression path (Andrews and Befus, 2020). At each time, t_i ,
160 SNGPlag evaluates the supersaturation, $\Delta\phi$, as the difference between the plagioclase volume

161 fraction, ϕ , at the previous time step and the equilibrium plagioclase volume fraction, ϕ_{eqb} , as
162 predicted by MELTS (Gualda et al, 2012; Ghiorso and Gualda, 2015) at the specified time-
163 dependent pressure and temperature, $P(t_i)$ and $T(t_i)$. Plagioclase volume fractions ϕ and ϕ_{eqb} are
164 considered on a vesicle-free basis. Nucleation and growth rates, $I(t_i)$ and $J(t_i)$, are defined for the
165 time step as functions of $\Delta\phi$ (Befus and Andrews, 2018). SNGPlag considers the crystals to be
166 rectangular prisms; at each time step, the axes grow by the amount $F \times J(t_i) \times \Delta t$, where F is a factor
167 between 0 and 1 describing the ratio of the axis length to the c-axis length, and Δt is the time step
168 duration. Growth only occurs on crystals or nuclei that exist in the previous step t_{i-1} . Nuclei are
169 added to the model volume in the amount $I(t_i) \times \Delta t$. SNGPlag accounts for volumetric
170 interferences between crystals through an analytical expression that prevents two crystals from
171 occupying the same volume (Andrews and Befus, 2020); potential local variations in
172 crystallization or dissolution rates arising from chemical gradients are not examined. Although
173 growth of real crystals in magmas does not usually result in rectangular prisms, analysis and
174 modeling of realistic textures (swallow tail, hopper, skeletal, etc.; Hammer and Rutherford,
175 2002) for $>10^9$ crystals is not feasible.

176

177 ***3.2 Modifications to SNGPlag***

178 The new version of SNGPlag allows for variable P-T conditions and longer run times,
179 permitting the study of magmatic processes in the reservoir prior to decompression and eruption.
180 Temperature can follow a prescribed path simulating isothermal (or near isothermal) conditions
181 punctuated by a series of heating or recharge events. Similarly, the system can be isobaric or
182 show fluctuations in pressure as might result from eruption of a portion of the reservoir (Segall,

183 2016) or from circulation of a parcel of magma through higher and lower pressure regions
184 (Anderson, 1984).

185 Crystals often reside within magmas for hundreds or thousands of years (e.g. Tepley et
186 al., 1999; Tepley et al., 2000; Cooper and Reid, 2003; Andrews et al., 2008; Cooper and Kent,
187 2014; Sosa-Ceballos et al., 2014; Budd et al., 2017), but nucleation and growth processes can
188 have timescales of seconds to days (e.g. Gerlach and Grove, 1982; Hammer and Rutherford,
189 2002; Befus and Andrews, 2018; Andrews and Befus, 2020). The previous version of SNGPlag
190 cannot cover that dynamic range (~8 orders of magnitude). The new version addresses this
191 challenge by calculating changes to the crystal population at fine temporal resolution (600 s), but
192 only recording those changes twice per day (Figure 2). Supplementary Material 1 describes the
193 equations that reduce the temporary population of 120 classes generated at 600 s intervals, each
194 with its own a-, b-, and c- axis dimensions and N_v , into a single characteristic class for each 12
195 hour period.

196 The c-axis growth rates used in SNGPlag are from Befus and Andrews (2018). The
197 relative growth rates (J_x) of the a- and b-axes are not constant fractions of the c-axis rate, but
198 instead vary linearly with $\Delta\phi$, from equant or isotropic at $\Delta\phi = 0$, to highly anisotropic at high
199 supersaturations:

$$J_x = (1 + \Delta\phi m_x) J_c$$

200 Eq. 1

201 where the subscript x denotes the a- or b-axis, and m_x describes deviation from equant growth;
202 note that the c-axis growth rate does not vary linearly with $\Delta\phi$. The parameter m_x is assumed to
203 be -3 for a and -2 for b; although no systematic examination of m_x as a function of $\Delta\phi$ has been
204 made, experimental studies show that crystal morphologies are more elongate at high degrees of

205 disequilibrium (e.g. Hammer and Rutherford, 2002; Szramek et al., 2006) and the chosen m_x
206 values produce reasonable crystal shapes. We use the expression

$$S n_i = \frac{\sum N_i (L_{ai}^2 + L_{bi}^2 + L_{ci}^2)^{1/3}}{\sum N_i}$$

207 Eq. 2

208 to obtain the characteristic crystal size S_n at each time i . The anorthite content (An) at time i is
209 determined using MELTS as a function of pressure and temperature, resulting in a-, b-, and c-
210 axis growth patterns and compositions within each crystal.

211 Crystal dissolution is an important and frequent process within many magmatic systems
212 (Tepley et al., 1999; Tepley et al., 2000; Andrews et al., 2008; Salisbury et al., 2008; Streck et
213 al., 2008; Sosa-Ceballos et al., 2014). The stable composition of plagioclase varies with pressure
214 and temperature (e.g. Rutherford et al. 1985; Putirka, 2005; Lange et al., 2009; Andrews and
215 Gardner, 2010; Sosa-Ceballos et al., 2014; Waters and Lange, 2015; Waters et al., 2015), such
216 that unless the system becomes superliquidus with respect to plagioclase, only certain
217 compositions will dissolve (Tsuchiyama, 1985). We assume that dissolution rate is a function of
218 undersaturation ($\Delta\phi < 0$), thus dissolution is faster in highly undersaturated systems. The
219 dissolution rate follows the same functional form as the c-axis growth rate, but with a two-fold
220 increase in magnitude; e.g., if $\Delta\phi = 0.1$ results in a growth rate of $\sim 0.2 \mu\text{m/h}$, then $\Delta\phi = -0.1$ results
221 in a dissolution rate of $\sim 0.4 \mu\text{m/h}$. Experimental work by Tsuchiyama (1985) and Donaldson
222 (1985) suggests this assumption of faster dissolution rates as compared to growth rates is
223 reasonable. Recent papers combining experimental measurements of diffusion and zircon
224 saturation (Boehnke et al., 2013; Zhang and Xu, 2016) show that zircon dissolution rate rapidly
225 increases as the zircon liquidus is exceeded; applying their general findings to plagioclase, the

226 dissolution rates of unstable plagioclase compositions should increase with the magnitude of
227 undersaturation. We assume dissolution rates are isotropic. Finally, to account for the potential
228 stability of relatively higher An compositions of plagioclase (Tsuchiyama, 1985), SNGPlag only
229 dissolves plagioclase with An less than the equilibrium value calculated by MELTS for the
230 pressure and temperature at that time step.

231 Together, the $\Delta\phi$ -dependent anisotropic growth rates and $\Delta\phi$ - and An-dependent
232 dissolution rates allow SNGPlag to grow complexly zoned crystals. A P-T trajectory resulting in
233 increasing $\Delta\phi$ and decreasing An produces a concentrically zoned crystal with a higher An core
234 and lower An rim. If that crystal undergoes a dissolution event followed by renewed
235 crystallization, the concentric zoning will be truncated with greater fractions of the a- and b-axes
236 dissolved compared to the c-axis (Figure 3). Repeated episodes of dissolution and crystallization
237 can produce crystals with oscillatory zoning in the c-axis and effectively monotonic zoning in the
238 a- and/or b-axes (Figure 3).

239 The modified model allows a change in system volume during recharge events. As
240 temperature increases, volume can increase by a specified fraction of crystal-free melt with an
241 identical bulk composition as the original magma, decreasing total crystallinity. For example, an
242 increase of 0.1 decreases crystallinity by a factor of ~ 0.09 ($=1/(1+0.1)$).

243 SNGPlag assumes that the other crystal phases are in instant equilibrium. The model does
244 not account for changes in melt composition through time. Although tracking compositional
245 changes during crystallization is trivial, calculating those changes during dissolution of
246 compositionally zoned anisotropic crystals is not feasible.

247 We use the nucleation and growth rates presented in Befus and Andrews (2018) as these
248 are the only published instantaneous rates. All other published values are presented as time-

249 averaged rates, generally as functions of initial undercooling (Hammer and Rutherford, 2002;
250 Couch et al., 2003; Larsen, 2005; Brugger and Hammer, 2010; Shea and Hammer, 2013). Use of
251 time-averaged rates in an instantaneous model results in either impossibly large crystals and high
252 crystallinities (applied to model durations of years or centuries such rates produce m-scale
253 crystals in mm-scale volumes of magma), or implausibly low crystallinities (when converted to
254 time-variant rates). The Results section presents the effects of variation in nucleation, growth and
255 dissolution rates on model outputs.

256 The terms “antecryst,” “phenocryst,” and “microlite” follow the definitions used in
257 Andrews and Befus (2020). The initial antecryst volume does not affect the system equilibrium,
258 although subsequent crystallization on antecrysts will affect equilibrium. Phenocrysts are crystals
259 present at the start of the run whose initial volume contributes towards equilibrium. Microlites
260 are defined as those crystals that nucleate and grow during the course of the simulation.

261

262

Model results

263 We present three suites of model runs using an El Chichón trachyandesite bulk
264 composition (Macias et al., 2003; Andrews et al., 2008; Table 1). First, we examine the system
265 response to step-like changes in temperature to establish timescales over which a magma returns
266 to equilibrium during 2-year model runs. These simulations act as simplified perturbation
267 analyses of a more complex natural system and are discussed in the context of model sensitivity
268 to nucleation, growth, and dissolution rates. Second, we consider 2-year simulations with
269 repeated heating-cooling or decompression-pressurization cycles to understand how crystal
270 populations survive intervals of crystallization and dissolution. Finally, we parameterize model

271 results and extend a simplified version of the model to a ~5300-year interval to study what
272 fractions of magmatic history are preserved within a single crystal.

273

274 *Timescales of equilibration and model sensitivity*

275 Model runs with step-like changes in temperature rapidly increase the disequilibrium
276 magnitude ($|\Delta\phi|$) and show how quickly the magma returns to or approaches equilibrium. After
277 an initial dwell time of 182.5 days (0.5 years) at T_o , temperature changes to T_f over 1 day, and
278 then holds at T_f for the remainder of the 2-year run; simulations with $T_f > T_o$ record negative
279 values of $\Delta\phi$, resulting in dissolution, whereas runs with $T_f < T_o$ show positive excursions in $\Delta\phi$,
280 and thus crystal nucleation and growth. These runs have no volume addition.

281 Figure 4A shows variation in $\Delta\phi$ with respect to time, and thus how quickly the systems
282 equilibrate. The rate at which $|\Delta\phi|$ decreases is proportional to $|\Delta\phi|$. Because the experimentally
283 determined nucleation and growth rates are very low for $\Delta\phi < 0.04$, reduction of $|\Delta\phi|$ to $\ll 0.04$
284 occurs slowly, with an asymptotic approach to $\Delta\phi = 0$. Larger initial excursions in $\Delta\phi$ require
285 longer recovery times. Although the instantaneous dissolution rate is at least twice as fast as the
286 growth rate for undersaturation and supersaturations with the same magnitude, system
287 equilibration rates differ by less than a factor of 2, likely because dissolution acts on a decreasing
288 number of crystals with decreasing size, whereas growth acts on an increasing number of ever
289 larger crystals.

290 To examine SNGPlag sensitivity to nucleation, growth, and dissolution rates, we vary the
291 magnitudes of those rates from 25 times less (i.e. roughly comparable to rates from Hammer and
292 Rutherford, 2002) to 5 times greater, while maintaining the same functional form as in Befus and
293 Andrews (2018). Figure 4B shows that slower rates, varied individually or jointly, result in

294 slower equilibration. Faster rates result in faster equilibration, with the decrease in response time
295 approximately proportional to the increase in rate. Changes in nucleation and growth rate both
296 affect crystallization responses during intervals of supersaturation. Not surprisingly, the
297 dissolution response during heating is most sensitive to changes in dissolution rate, with minor
298 sensitivity to nucleation rate, as nucleation affects the initial crystal population.

299 Nucleation, growth, and dissolution rates also affect the fidelity with which individual
300 crystals record magmatic history. Supplementary Material 2 shows zoning pattern sensitivity to
301 variation in those rates from 25 times less to 10 times greater than those from Befus and
302 Andrews (2018). Elevated growth rates produce large crystals recording large time fractions
303 (>70% in the test scenario) when nucleation rate is low, with changes in dissolution rate only
304 causing minor differences in the crystal record. High nucleation rates result in low recorded time
305 fractions (~10%) even at high growth rates. The recorded time fraction varies inversely with
306 covariation in nucleation, growth, and dissolution rates such that for elevated or nominal values,
307 the crystals record ~10% of the scenario, but preserved time fraction increases to ~18 and ~37%
308 as the rates decrease to 0.1 and 0.04 times the nominal values, respectively. Low growth rates
309 produce small crystals; complete dissolution of such crystals is common during heating or
310 recharge events except when nucleation and dissolution rates are both reduced.

311 The time series for different magnitude heating or cooling events collapse onto single
312 dissolution or crystallization trajectories. Time series with lower $|\Delta\phi|$ can be overlain onto the
313 highest $|\Delta\phi|$ series by introducing a lag in the time indices of the lower $|\Delta\phi|$ series. Crystallinity
314 (expressed as $\Delta\phi$) does not vary exponentially with time nor follow a “half-life” return to
315 equilibrium, but instead $|\Delta\phi|$ decreases approximately linearly as a function of $|\Delta\phi|$ in log-log
316 space. These patterns indicate that the maximum disequilibrium experienced by a system

317 controls the time over which that system approaches equilibrium, and that $\Delta\phi$ can predict the
318 instantaneous rate of system crystallization or dissolution when the nucleation, growth, and
319 dissolution rates are known. Although this predicted response is not as precise as the full model,
320 it can inform longer duration models of crystallization.

321

322 *Repeated oscillations in temperature and/or pressure*

323 *Thermal cycling*

324 We examine repeated cycles of magma heating and cooling, conceptually analogous to
325 the thermal effects of recharge on a host magma. We begin with an initial temperature T_o then
326 increase temperature to T_f , before returning to T_o . The T-t series follows a Gaussian path
327 described by the error function; heating of the magma in this scenario occurs ~3 times more
328 rapidly than cooling such that a 60-day total duration heating event achieves a maximum
329 temperature after 15 days. We present four runs, each with three heating events. The initial
330 equilibrium crystal fraction plagioclase for all scenarios is 0.413, and the runs begin with
331 $\phi_{\text{plag}}=0.207$ comprising equal fractions of 200, 150, 100, and 75 μm cubic crystals.
332 Supplementary Material 3 describes presentation of 3D crystal shapes.

333 Figure 5 shows results from a 2-year model run at $T_o=800$ °C with 60-day 100°C heating
334 events with no volume addition, occurring at 6, 12, and 18 months. During each event,
335 crystallinity decreases during heating and increases during cooling. The crystal population
336 changes through the model run, with maximum numbers present immediately before initiation of
337 each recharge event (and at the end of the run), and minimum numbers present during high
338 temperature intervals. Most of the crystals that form do not survive subsequent recharge events,
339 the population always comprises a small number of phenocrysts and a small subset of early-

340 nucleated crystals, with a subordinate number that nucleate and dissolve until the final thermal
341 maximum is achieved (Figure 5c and 5d). As a consequence, the characteristic crystal
342 dimensions (Figure 5e) are dominated by the early-formed crystals with only minor excursions
343 reflecting the nucleation and dissolution of new crystals; the crystal size S_n , however, shows step
344 changes as crystals nucleate and dissolve. The characteristic shape for all crystals (Figure 5f)
345 gradually elongates through time, reflecting effectively isotropic dissolution followed by non-
346 isotropic (e.g., $c > b > a$ axis) growth; the shape of newly grown crystals is more elongate and
347 oscillates over the same range through each cycle.

348 Figure 6 shows a run with identical conditions as presented in Figure 5, but with volume
349 addition of 0.25 during each heating event. The additional volume decreases the plagioclase
350 volume fraction during heating, reducing undersaturation magnitude. The slower dissolution
351 rates and reduced total amount of dissolution allow survival of more crystals, with nearly all
352 crystals nucleated prior to the first heating event, and a portion of those nucleated after the first
353 thermal maximum, surviving to the end of the model run (Figure 6c). The preservation of a more
354 diverse crystal population also damps the step-like variations in S_n (Figure 6e). Characteristic
355 crystal shapes lengthen with time (Figure 6f).

356 Crystal dissolution during and growth following heating events are inversely and directly
357 proportional to volume fraction input, respectively (Figure 7). Volume addition makes zones
358 larger, and reduces their subsequent dissolution. Increased volume during heating events also
359 affects crystal compositional zoning. Figure 8 shows a-, b-, and c-axis transects of An and the
360 times that are recorded by a crystal nucleated at day 1 for the scenarios shown in Figure 5 and 6.
361 Although the c-axis profiles for both crystals show 3 peaks in An, the scenario with volume
362 addition preserves 2 peaks in the a- and b-axes. Volume addition preserves the a- and b-axis

363 zones grown following the first heating event – a fraction of crystal completely dissolved during
364 the scenario with no volume addition.

365 Not all recharge events should be the same temperature, nor affect all regions of the host
366 magma with the same magnitude and duration of temperature excursion, therefore we conduct 2-
367 year model runs with 120-day recharge events of increasing and decreasing thermal magnitudes
368 (Figure 9). For these simulations, volume addition during each recharge event is 0.1. In systems
369 with increasing temperatures, no crystals nucleated following one recharge event survive the
370 next recharge event. In contrast, the run with decreasing magnitude heating events preserves a
371 large number of crystals; all crystals formed above 200°C during cooling following the first
372 thermal maximum survive until the end of the run, as do all formed above 150°C during cooling
373 following the second thermal maximum. The characteristic sizes and shapes evolve differently
374 for the two scenarios. In the increasing series, Sn evolves strong peaks during the heating events,
375 reflecting dissolution of all but the largest crystals, whereas in the decreasing series Sn remains
376 low after the first event because some small crystals survive each heating event. Similarly, the
377 increasing series shows more variation in characteristic shape and finishes with slightly more
378 elongate morphology.

379

380 *Pressure cycling*

381 Pressure within a magma reservoir may drop during eruption (e.g. Anderson, 1984;
382 DeGruyter and Huber, 2014; Segall, 2016; Townsend et al., 2019). The decompression
383 magnitude and the timescale over which pressure returns to its initial value are functions of
384 numerous factors including magma and host rock compressibility and the ratio of erupted to
385 reservoir volume (Huppert and Woods, 2002; DeGruyter and Huber, 2014; Segall, 2016;

386 Townsend et al., 2019). We consider comparatively rapid decompression events as generated by
387 eruptions that are followed by more gradual return to the initial pressure. The P-t path follows
388 the same functional form as the recharge events, with the minimum pressure achieved at 25% of
389 the total cycle duration. During each decompression-pressurization cycle, no volume is added to
390 the system. Note that a decompression event is equivalent to a cooling event within SNGPlag, as
391 both result in an initial increase then decrease in $\Delta\phi$.

392 Figure 10 shows the P-t path for a sequence of three decompressions from 100 to 50 MPa
393 at 800 °C with event durations of 120 days. These decompressions are of larger magnitude than
394 might be expected during most natural eruptive cycles, but have $|\Delta\phi|$ roughly comparable to
395 cooling from 800 to ~750°C; smaller, more geologically plausible decompressions manifest
396 virtually no crystallization record in SNGPlag. Pressure cycling begins with a positive change in
397 $\Delta\phi$, resulting in nucleation and growth. The system remains plagioclase-supersaturated during
398 repressurization ($\Delta\phi$ remains positive), thus although nucleation and growth rates decrease, the
399 system never dissolves crystals. This lack of dissolution results from pressure cycles with
400 durations comparable to or less than the timescales required for equilibration, and decompression
401 inducing small amplitude changes in $\Delta\phi$ ($< \sim 0.03$). Larger magnitude or longer duration pressure
402 cycles might result in dissolution during the later stages of repressurization.

403

404 *Modelling longer run durations*

405 The previously discussed runs had 2-year durations, with one 10-year simulation used to
406 examine how systems approach equilibrium over a longer time. Magmatic processes, however,
407 often occur over much longer intervals, and individual crystals can reside in magmas for
408 thousands of years (Cooper and Reid, 2003; Andrews et al., 2008; Cooper and Kent, 2014; Sosa-

409 Ceballos et al., 2014; Budd et al., 2017). We use the equilibration timescales determined above
410 to develop a simplified model of plagioclase $\Delta\phi$ as a function of P-T-t path. That $\Delta\phi$ timeseries
411 allows calculation of the growth, dissolution, and compositional history of a single crystal over a
412 geologically interesting interval. We describe that simplified model, validate it against a 5-year
413 run of SNGPlag to ensure that it can recover results of the full model, and then use it to examine
414 a hypothetical ~5300-year P-T-t series.

415 At a constant equilibrium crystallinity ϕ_{EQB} , the rate at which $\Delta\phi$ changes ($\Delta\phi/dt$)
416 describes the crystallization rate of that system. The equilibration timeseries discussed previously
417 and displayed in Figure 4 show $\Delta\phi/dt$ is proportional to $\Delta\phi$. If plagioclase crystallinity (ϕ) is
418 known, then $\Delta\phi$ can be calculated as $\Delta\phi = \phi_{EQB} - \phi$, which can determine $\Delta\phi/dt$ at that time. That
419 rate describes the amount of crystallization (or dissolution) during the next time step. At that new
420 time t_i , the difference between ϕ and ϕ_{EQB} determines $\Delta\phi$, and the model thus proceeds
421 iteratively, as shown in the expression:

$$\phi_i = \phi_{i-1} + \left(\frac{\Delta\phi}{dt} \right)_{i-1} \Delta t$$

422 Eq. 3

423 Although this approach may accumulate uncertainty, the timescales required for equilibration are
424 100s of days, thus intervals spent at constant conditions for more than one year prevent forward
425 propagation of those errors.

426 We compare this approximation to a 5-year run of SNGPlag. The runs have a series of
427 convolved temperature and pressure changes (Figure 11), allowing examination of plagioclase
428 population dynamics over a range of temperature, pressure, and time scales. Comparison of $\Delta\phi$

429 between the full and simplified runs shows good agreement (Figure 11) indicating the
430 parameterized version can recover results of the full model.

431 We now consider a magma over ~5300 years with a randomly generated recharge and
432 eruption history. Series of recharge events occur every 200 years (Figure 12). Each series can
433 last from 10-100 years, with up to 5 events per decade. Those events have 50-150 °C
434 magnitudes, durations of 0.25-10 years, volume fraction additions of 0-0.5, and can be
435 superimposed upon one another. Each recharge series can also have an eruption, i.e. an interval
436 of 10-25 MPa decompression over up to 7 days, with the system returning to its initial pressure
437 (100 MPa) over 0.25-10 years. The initial pressure is at the lower bound of likely storage
438 pressures for the Chichón trachyandesite (Macias et al., 2003) or other intermediate arc magmas,
439 but is chosen because allows for a larger thermal range of plagioclase stability and composition
440 than higher pressures. Runs at higher pressures show a systematic decrease in the fraction of time
441 preserved in crystals as the same temperature excursions induce greater magnitude $|\Delta\phi|$ and
442 potentially more time spent at or above the plagioclase liquidus. The modeled interval contains a
443 total of 454 recharge events and 12 decompressions or eruptions occurring in 26 groups. These
444 values do not mimic any specific volcano or series of eruptions, but rather examine a
445 geologically reasonable family of recharge and eruption scenarios (Andrews and Manga, 2014;
446 Cooper and Kent, 2014; Sosa-Ceballos et al., 2014; Segall, 2016).

447 Figure 13 shows the final compositional zoning profile for the P-T-t series.
448 Supplementary Material 4 shows an animation of the compositionally zoned crystal, illustrating
449 growth, dissolution, and compositional profiles through time. In runs with zero or low volume
450 additions during heating events, the system repeatedly crystallizes and dissolves variations of the
451 same zone, thus no net growth occurs (Supplementary Material 5). Each heating-cooling episode

452 results in possible dissolution followed by crystallization of initially higher An plagioclase
453 followed by decreasing An plagioclase. Moving outward from the core, approximately 20
454 distinct An peaks with step-like increases of >10 mol.% are preserved in the record. This number
455 is lower than the >400 total recharge events in the temperature timeseries (Figure 12). The lower
456 number of recorded events is expected as some of the recharge events are superimposed on one
457 another, resulting in effectively singular events, and because dissolution removes portions of the
458 crystal record. In addition, the crystal completely dissolves twice during the first 2000 years
459 (Figure 13).

460 The ~5300-year magmatic history is not uniformly sampled by the crystal (Figure 13).
461 The more complete zoning patterns preserved in the c- versus a- and b-axes show that large
462 fractions of the crystal record are missing. Not only are intervals of dissolution missing from the
463 crystal, but its record is dominated by intervals of high supersaturation during which faster
464 growth occurs. This has the effect of undersampling higher- and lower-temperature intervals
465 (those with the highest and lowest An compositions). A histogram of An composition indicates
466 that the range of P-T conditions recorded by the crystal approximates the range of conditions
467 experienced by the magma, but its distribution is not proportional to the time spent at those
468 conditions (Figure 13).

469

470

Discussion

471 SNGPlag predicts how plagioclase populations evolve in response to changes in
472 temperature and pressure. Heating or pressurization result in dissolution, whereas cooling or
473 decompression result in nucleation and growth. More anorthitic plagioclase forms at elevated
474 temperature and pressures, thus an individual recharge event is likely recorded as a step-like

475 increase in An, followed by a more gradual decline. Because SNGPlag conditions dissolution on
476 An, a high-An zone can shield inboard regions from dissolution. The net results of these
477 processes are that smaller, more albitic plagioclase dissolve more easily than larger plagioclase
478 with more anorthitic zones, and that high temperature excursions often dissolve crystals (or
479 zones) formed during preceding cooler intervals including recharge events of smaller thermal
480 magnitude.

481 Large crystals survive for longer intervals and effectively grow at the expense of smaller
482 crystals. This process is not Ostwald ripening, but the interplay of outward growth and inward
483 dissolution rates of crystal faces. Growth and dissolution have units of distance per time, as these
484 processes occur through the incremental addition or removal of atoms from crystal faces;
485 defining these rates with units of volume (or volume fraction) per time presupposes a crystal
486 number density and size distribution. The same growth rate applied to large and small crystals
487 crystallizes much more material onto the former, more rapidly reducing supersaturation and
488 retarding additional crystallization. Larger crystals are more likely to contain high-An zones that
489 shield albitic interiors. Consequently, smaller crystals completely dissolve more readily than
490 large crystals, and repeated dissolution-crystallization cycles can increase the size of surviving
491 crystals.

492

493 *Net growth requires mass addition*

494 If the modeled system has no additions of mass (or volume), then those crystals (or
495 zones) formed during the initial crystallization event and/or some final temperature decrease are
496 most likely to be preserved; crystals formed during earlier, lower temperature intervals will be
497 dissolved. Oscillatory zoning with compositional range >10 mol.% An (and perhaps less) is

498 unlikely to form only through cycling of temperature and/or pressure, but also requires mass
499 addition.

500 The addition of mass to the system during recharge events has the effect of reducing total
501 crystallinity, thereby reducing the undersaturation magnitude . Although dissolution can still
502 occur during an episode of heating, reduction of system crystallinity allows the magma to
503 crystallize a larger final fraction than initially dissolved (i.e., 9 vol.% dissolves, but 10 vol.%
504 crystallizes). Without mass addition, the same zones repeatedly grow and dissolve, thus
505 oscillatory or complex zoning cannot develop.

506 This required mass addition does not mean that the total magma reservoir increases in
507 volume by, e.g., 10%, only that the volume interacting with the crystal(s) of interest increases.
508 The new mass need not be directly from the recharging magma, but could be remobilized host
509 magma. This further highlights how two crystals might record the same event differently
510 (Andrews et al., 2008; Sosa-Ceballos et al., 2014): a crystal near enough to the recharging
511 magma to encounter the added mass would partly dissolve before growing a larger new zone and
512 increasing in size, whereas a more distal crystal might dissolve before growing a roughly
513 equivalent new zone resulting in no change in crystal size. Analysis of trace element or isotopic
514 zoning, in tandem with An zoning, can identify whether the added mass is remobilized from the
515 host or is new magma entering the system (Tepley et al., 1999; Tepley et al., 2000; Andrews et
516 al., 2008).

517

518 *Application to natural systems*

519 This paper does not precisely model a specific natural system. Although the presented
520 simulations use El Chichón trachyandesite compositions, the Chichón magma system has

521 processes and characteristics beyond consideration of this model. Further, SNGPlag assumes
522 dissolution rates and axis-dependent growth rates that are reasonable but not experimentally
523 verified for Chichón. Despite those simplifications, the model offers insights into natural magma
524 dynamics, and the parameterized model can be applied to an arbitrary magma composition by
525 using MELTS to determine the plagioclase volume fraction and composition as functions of
526 pressure and temperature.

527 First, because plagioclase growth and dissolution rates are very low at small $|\Delta\phi|$, growth
528 and dissolution are not sensitive to small changes in pressure, temperature, or composition.
529 Whereas large excursions in disequilibrium will return to $|\Delta\phi| < 0.05$ in 100s of days, reduction in
530 $|\Delta\phi|$ to < 0.02 requires times in excess of 150 years; even if that second timescale is too long, the
531 pattern of asymptotic equilibration holds, and magmas should show limited response to small
532 changes in $\Delta\phi$. Crystallization (or dissolution) will maintain equilibrium, or a state near
533 equilibrium, with any changes in intensive parameters occurring over timescales > 100 s of days.

534 Second, dissolution and changing growth rates result in the absence of substantial
535 amounts of time from most crystal records. It is not unreasonable for 50% of a crystal to form
536 during 10% of its history, and 75% of its total history to be removed by dissolution. This
537 observation is similar to the “cold storage” hypothesis of Cooper and Kent (2014), where
538 magmas spend substantial fractions of time in a cool, rheologically locked, uneruptible state, but
539 with the extension that many intervals are entirely removed from individual crystals. Our results
540 show that the plagioclase record is biased against high-temperature intervals, although more
541 limited information describing high-temperature thermal state may be preserved by diffusion
542 profiles within crystals, such as duration and magnitude of heating. Future work, involving a
543 large number of model runs with P-T-t paths informed by other petrologic observations and

544 numerical models (e.g. Andrews et al., 2008; DeGruyter and Huber, 2014; Sosa-Ceballos et al.,
545 2014; Townsend et al., 2019) could quantify bias in the crystal record as a function of recharge
546 volumes, and recharge and eruption frequencies.

547 Third, the c-axis preserves a more complete record than other crystallographic axes. This
548 is true because the faster growing axis stretches zoning patterns compared to the a- and b-axes,
549 and also because dissolution completely removes zones from faces normal to the a- and b-axes.
550 Previous workers have noted that the c-axis provides the best opportunity to correlate crystals
551 (e.g., Wallace and Bergantz, 2002, 2004, 2005), but observational artifacts and magmatic
552 processes complicate correlation (Wallace and Bergantz, 2005; Andrews et al., 2008; Cheng et
553 al., 2017). Robust correlations likely require analysis of large numbers of crystals from the
554 outside in, and matching both the shape and magnitude of zones because they record separate
555 aspects of magmatic history: the change in An provides an indication of the absolute change in
556 temperature (or melt composition), whereas the shape of a zone records $\Delta\phi$ through time.

557

558

Implications

559 SNGPlag suggests the plagioclase record is biased against higher and lower An
560 compositions and towards more recent time intervals. Although the plagioclase compositional
561 range reflects the pressure-temperature-composition range experienced by the magma, the
562 fraction of high- to low-An zones does not record the relative time spent at those conditions.
563 Further, the smallest crystals likely only record time since the most recent dissolution event.

564 Substantial intervals of time are not recorded by phenocrysts. Depending upon the
565 amount of mass addition that occurs in close proximity to a crystal during recharge or heating

566 events, dissolution can erase and slow growth rates can compress large fractions of a crystal's
567 history. Together those processes can remove more than 50% of time from a crystal record.

568 Complex compositional zoning in plagioclase requires mass addition as well as heating.
569 Significant heating with little or no mass addition results in substantial dissolution and
570 obliteration of the crystal record. The common occurrence of complex compositional zoning
571 indicates that most heating events experienced by individual crystals, or at least those preserved
572 in crystals, are accompanied by new melt.

573 Mixed crystal populations are ubiquitous in arc andesites and dacites. The compositional
574 range in any crystal records the pressure-temperature-composition-time (P-T-X-t) conditions that
575 crystal experienced; but that history may not be representative of the magma in general.

576 Obtaining a unified P-T-X-t history of a magma requires reconciling disparate records of many
577 crystals. The complexity in resolving those histories should indicate the timescales and length
578 scales of magmatic processes: large, prolonged events affecting the entire magma body should be
579 recorded more uniformly than small events only recorded by crystals in close physical proximity
580 to the disturbance.

581 Plagioclase populations approach equilibrium with magma intensive parameters over
582 timescales of 100s of days, thus those populations effectively maintain textural (and
583 compositional) equilibrium during processes operating over timescales longer than a year (e.g.,
584 gradual heating or cooling). The lag between the onset of some rapid process and the
585 crystallization response of the magma(s) is thus shorter than 100s of days. Consequently, the
586 interval during which neither a hot intruding magma nor cool host magma are sufficiently
587 crystallized to be rheologically locked is on the order of months, thus fluid mixing of
588 compositionally and/or thermally distinct magmas must occur over similar timescales.

589

590

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763 **Plagioclase population dynamics and zoning in response to changes in temperature and**
764 **pressure**

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769 For submission to **American Mineralogist**

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771 Figures:

772 Figure 1. A) BSE image of El Chichón Unit E sample CHI9516 (1465-1520 yBP) plagioclase

773 with line indicating core-to-rim transect. Age from Espindola et al. (2000). B) Core-to-

774 rim transect illustrating variation in An.

775 Figure 2. Schematic of SNGPlag crystal nucleation, growth, and dissolution. At each time t_i , N_i

776 crystals can nucleate. Over the subsequent time step, those nuclei and all existing crystals

777 grow (or dissolve) depending on supersaturation $\Delta\phi$. To balance long model durations

778 with computational limitations, temporary populations of newly nucleated crystals are

779 tracked (light gray) at high temporal resolution, and then synthesized into a single crystal

780 class (dark gray) with characteristic size and number density N calculated every 120 time

781 steps. Those “through-going” classes continue to grow (or dissolve) throughout the rest

782 of the run. Dissolution can eliminate crystals from the temporary and through-going

783 populations.

784 Figure 3. Schematic of crystal growth-dissolution cycles, with higher An zones shown in lighter

785 gray. Crystals grow at axis-specific rates proportional to supersaturation $\Delta\phi$, with $c \rightarrow b$ -

786 >a-axis rates, resulting in elongate or tabular crystals. Dissolution is assumed to occur at
787 the same rates for all axes, but dissolution along a particular axis stops when a zone of
788 stable An is intersected. Repeated dissolution-growth cycles result in zoned crystals, with
789 some zones dissolved from some or all crystal faces..

790 Figure 4. A) Variation in supersaturation $\Delta\phi$ with time for rapid heating from $T_o=800$ °C and
791 cooling from $T_o=900$ or 1000 °C. The cooling paths ($\Delta T=100, 150,$ and 200 °C) follow
792 essentially identical decreases in $\Delta\phi$. The heating paths show similar functional forms,
793 but are offset by the differences between their initial $\Delta\phi$. B) Changes in the magnitudes of
794 nucleation (I) and growth or dissolution rates (J) affect how quickly a magma returns to
795 equilibrium. The rate at which a system returns to equilibrium is proportional to both I
796 and J during crystallization, but mostly dependent upon J during dissolution.

797 Figure 5. 2-year SNGPlag run with no volume addition at $P=100$ MPa. A) Temperature-time
798 series. B) Equilibrium ($\phi_{EQBplag}$) and calculated (ϕ_{plag}) plagioclase crystal fractions and
799 supersaturation ($\Delta\phi$). C) Survival diagram indicating crystal nucleation and residence
800 time in the magma. D) Plagioclase number density N_v . E) Characteristic crystal size S_n
801 and lengths L_a, L_b, L_c . F) Characteristic crystal shape for all crystals (“All”) at each time
802 and only those nucleated during the model run (“New”). The upper line indicates the ratio
803 of b- to c-axis length, and the lower line a- to c-axis length; the two lines together thus
804 describe how equant, tabular, or elongate the crystals are. Supplementary Material 3
805 describes this method of plotting shape.

806 Figure 6. 2-year SNGPlag run with 0.25 volume fraction addition during each heating event. A)
807 Temperature-time series. B) Equilibrium ($\phi_{EQBplag}$) and calculated (ϕ_{plag}) plagioclase
808 crystal fractions and supersaturation ($\Delta\phi$). C) Survival diagram. D) Plagioclase number

809 density N_v . E) Characteristic crystal size S_n and lengths L_a , L_b , L_c . F) Characteristic
810 shape for all crystals at each time (“All”) and only those nucleated during the model run
811 (“New”).

812 Figure 7. Effects of different volume additions V_{input} during otherwise identical SNGPlag runs
813 with three 60-day 150 °C heating events from $T_o=750$ °C. With $V_{input}=0$, only the peak
814 A_n values from the first two events survive. As V_{input} increases, the three recharge events
815 become more distinct in the crystal record. At $V_{input}>0.25$, some crystallization from
816 between the recharge events is preserved. The double-peaked structure in the zoning
817 patterns results from MELTS calculating non-monotonic variation in A_n between 750
818 and 800 °C at 100 MPa.

819 Figure 8. Modeled compositional zoning and time intervals recorded by crystals nucleated at $t=1$
820 day for the scenarios shown in Figures 6 and 7. Model runs with $V_{input}=0$ record very
821 little zoning in the a- and b-axes (panels A-D), whereas those with $V_{input}=0.25$ show well
822 developed zones and virtually no missing time intervals. The c-axis shows zoning in both
823 scenarios, although the zones are highly compressed (E) and have substantial time
824 missing for the $V_{input}=0$ condition (F).

825 Figure 9. SNGPlag results for increasing (“Inc.”) or decreasing (“Dec.”) magnitude heating
826 sequences. A) Temperature-time series. B) Supersaturation $\Delta\phi$. C) Survival diagram. D)
827 Plagioclase number density N_v . E) Characteristic crystal size (S_n) and c-axis length (L_c).
828 F) Characteristic shape for crystals nucleated during the two runs. In all panels, the heavy
829 line represents the increasing series and the thin line the decreasing series.

830 Figure 10. 2-year SNGPlag run at 800 °C. A) Pressure-time series. B) Equilibrium ($\phi_{EQBplag}$) and
831 calculated (ϕ_{plag}) plagioclase crystal fractions and supersaturation ($\Delta\phi$). C) Survival
832 diagram. D) Plagioclase number density N_v .

833 Figure 11. A) 5-year temperature-time series used in full and parameterized SNGPlag run. B)
834 Comparison of $\Delta\phi$ for the two runs. Because $\Delta\phi$ controls crystallization and dissolution
835 rates, good agreement between $\Delta\phi$ for the runs shows the parameterized run accurately
836 reproduces the full run crystallization record .

837 Figure 12. A) Temperature and B) pressure series for the 5269-year run. The run comprises 454
838 heating events and 12 decompressions or eruptions in 26 groups.

839 Figure 13. A) C-axis core-to-rim transects during 5269-year time series, and pseudo-back-
840 scattered electron sections through the growing crystal. B) Histogram showing
841 cumulative thickness as a function of composition for the final (5269-year) crystal (bin
842 size of 0.01 An). C) Input and recorded (crystallized) conditions shown as histogram of
843 time. D) Ratio of recorded to input time as a function of pressure-temperature conditions
844 (and thus An).

845

846

847 Table 1. Whole rock composition (in anhydrous wt.%) of El Chichón trachyandesite used as
848 input for MELTS and SNGPlag. Analysis from Macias et al. (2003) and Andrews et al., (2008).

849	SiO ₂	TiO ₂	Al ₂ O ₃	FeO	MnO	MgO	CaO	Na ₂ O	K ₂ O	P ₂ O ₅	Total	fO ₂ (log ₁₀)
850	56.28	0.74	19.34	6.52	0.19	2.47	7.57	2.48	3.92	0.36	99.87	NNO+2.3

851

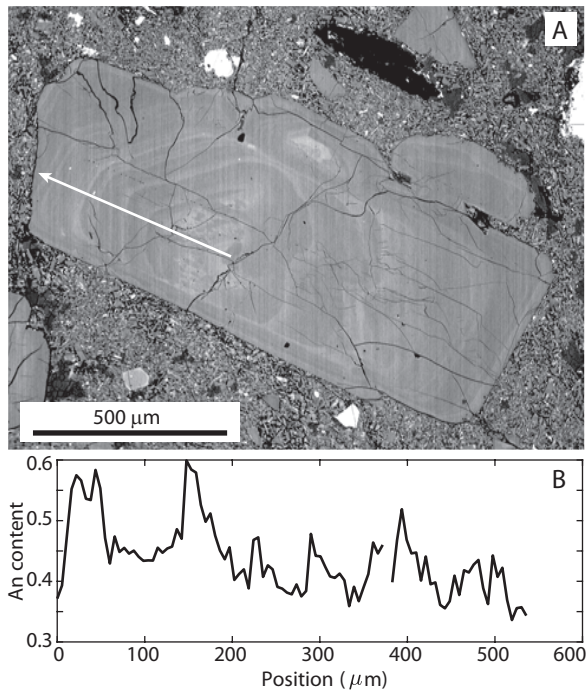


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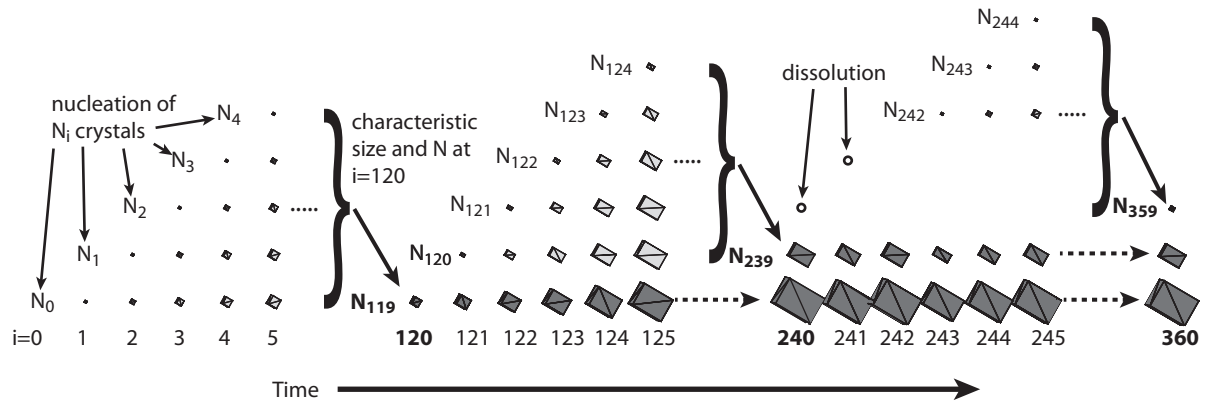


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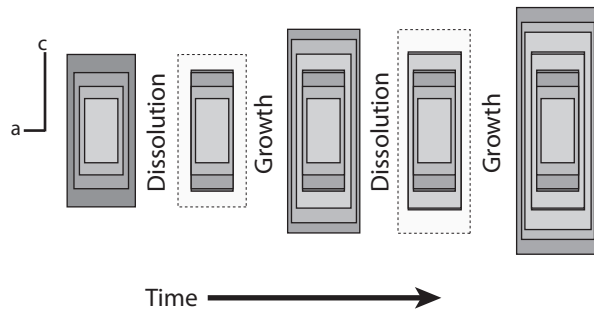


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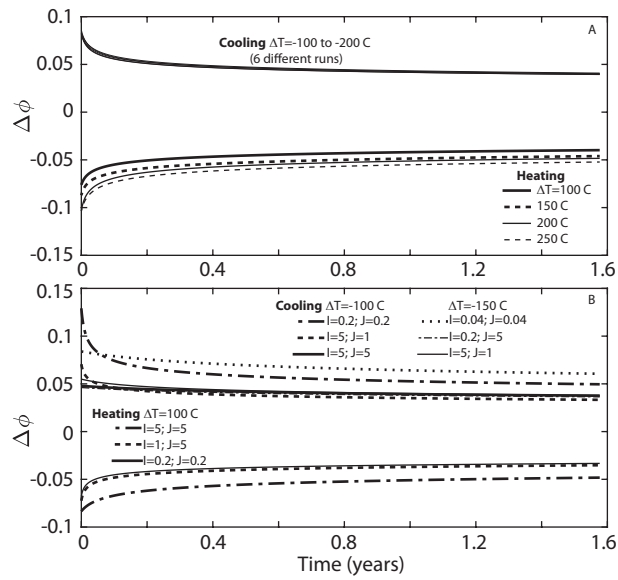


Figure 4

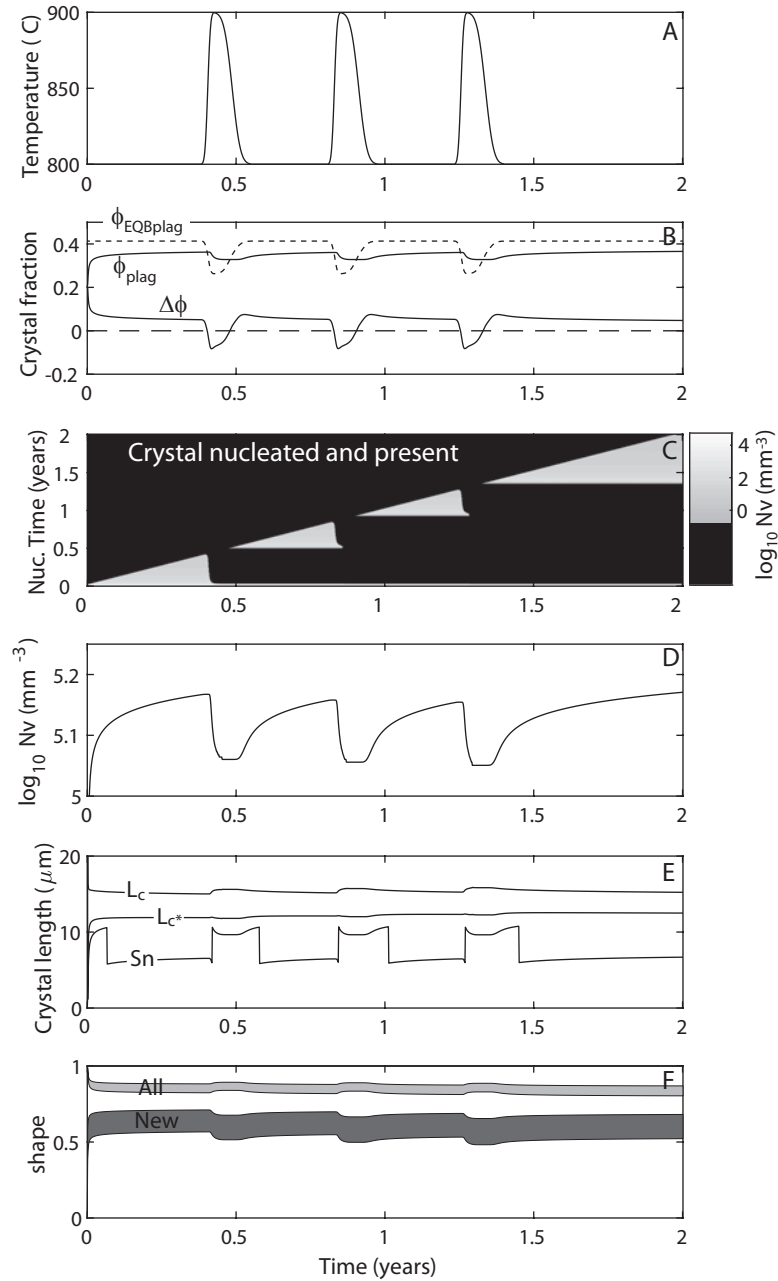


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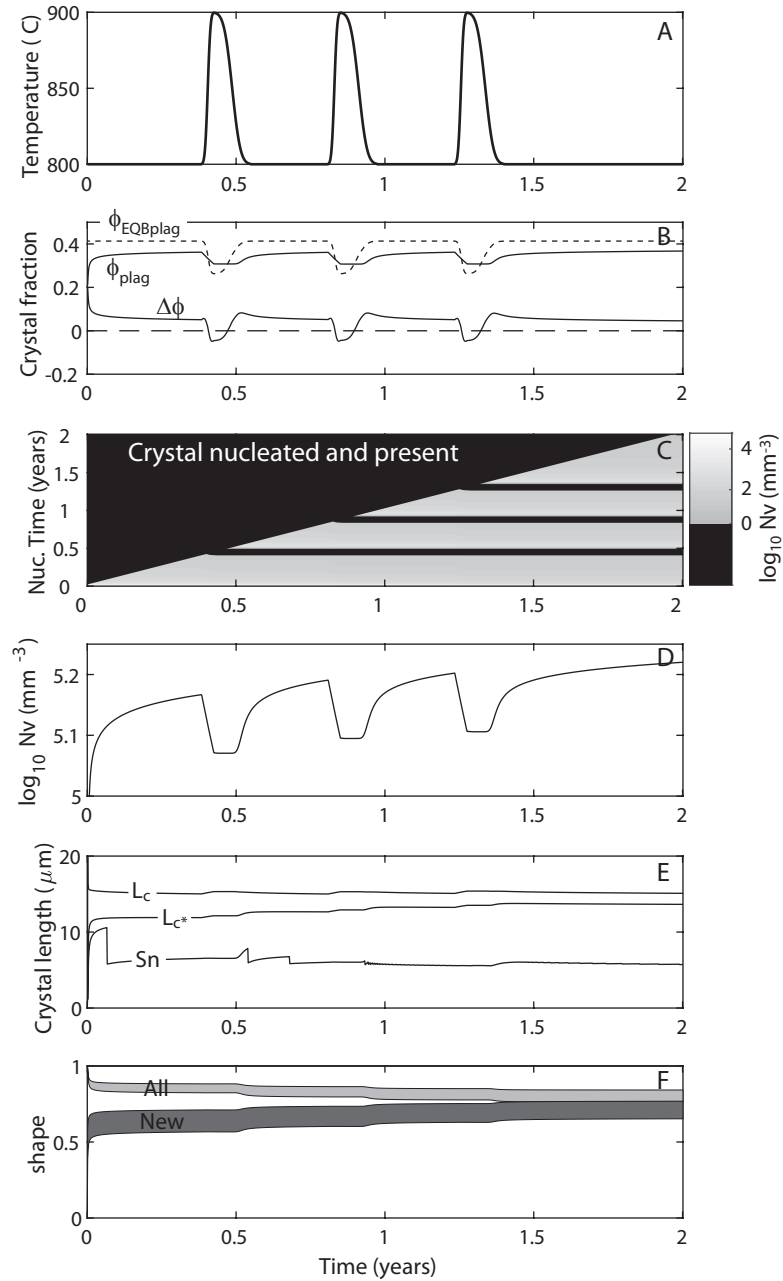


Figure 6

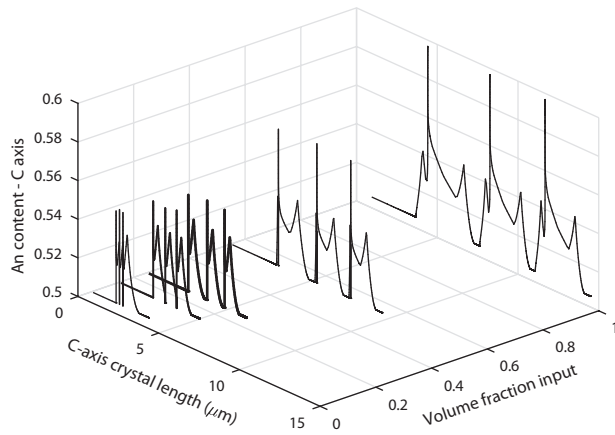


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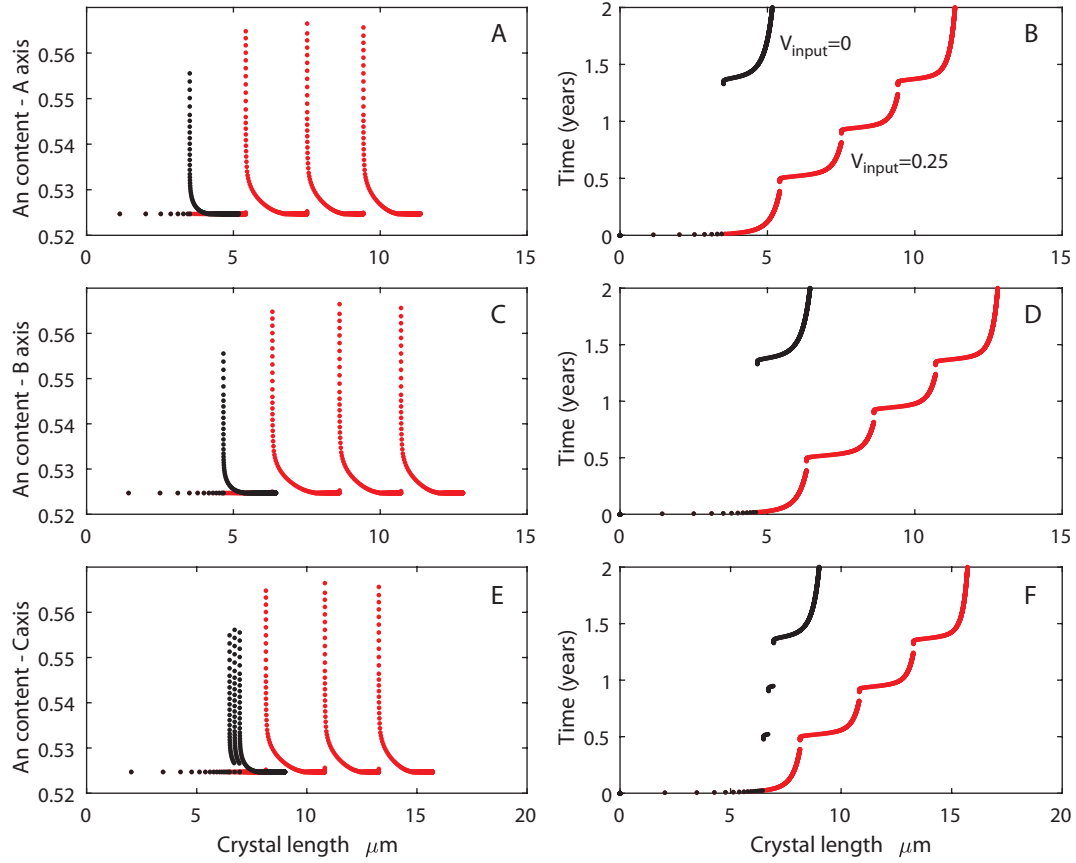


Figure 8

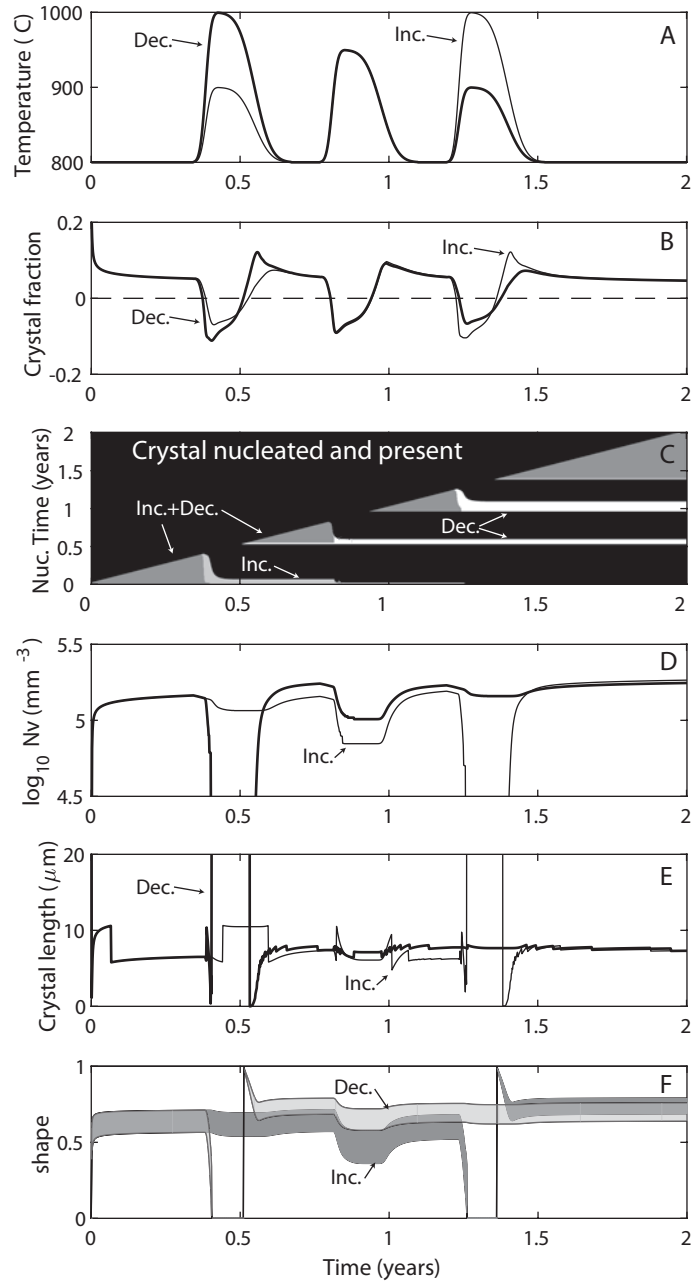


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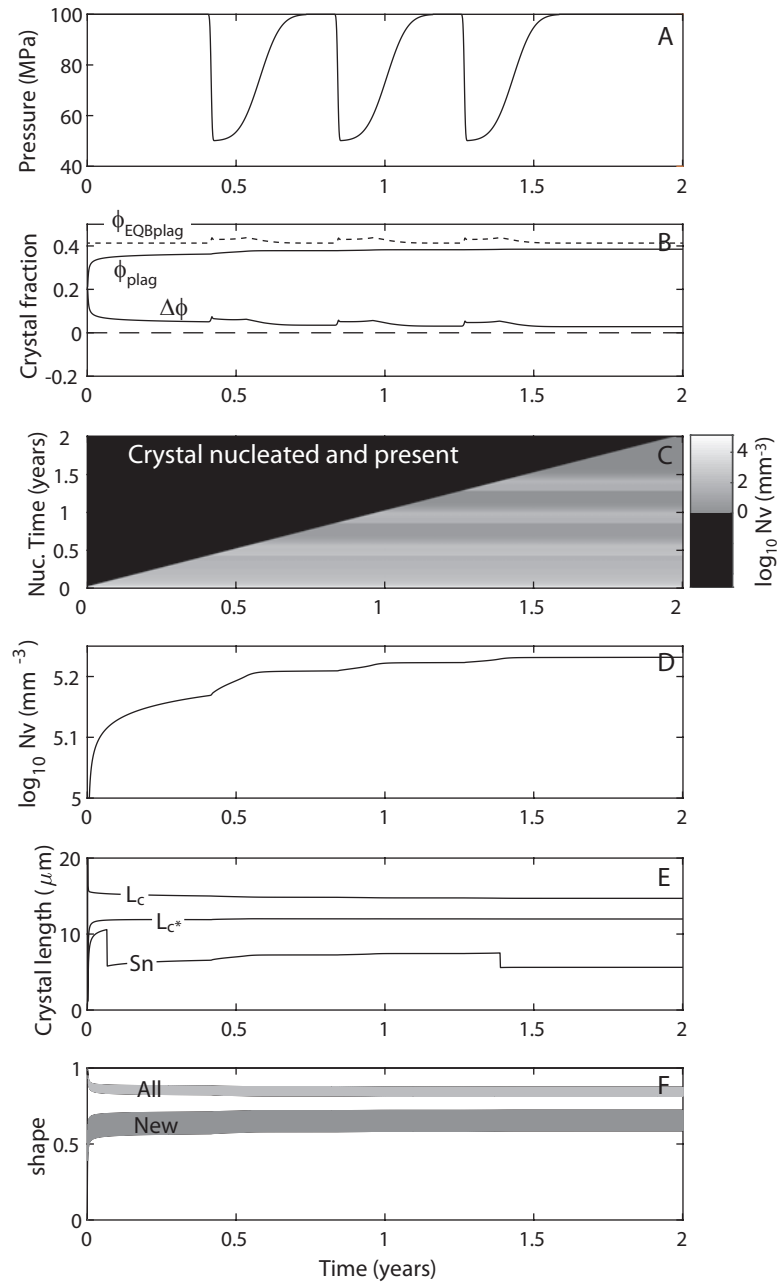


Figure 10

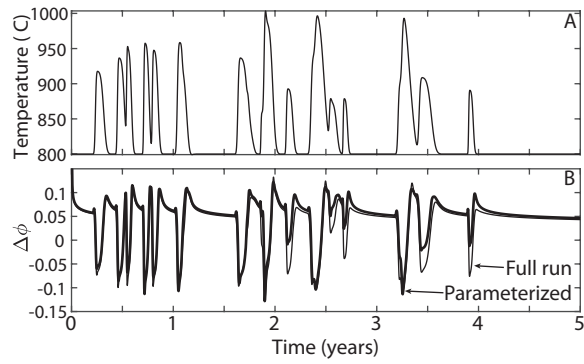


Figure 11

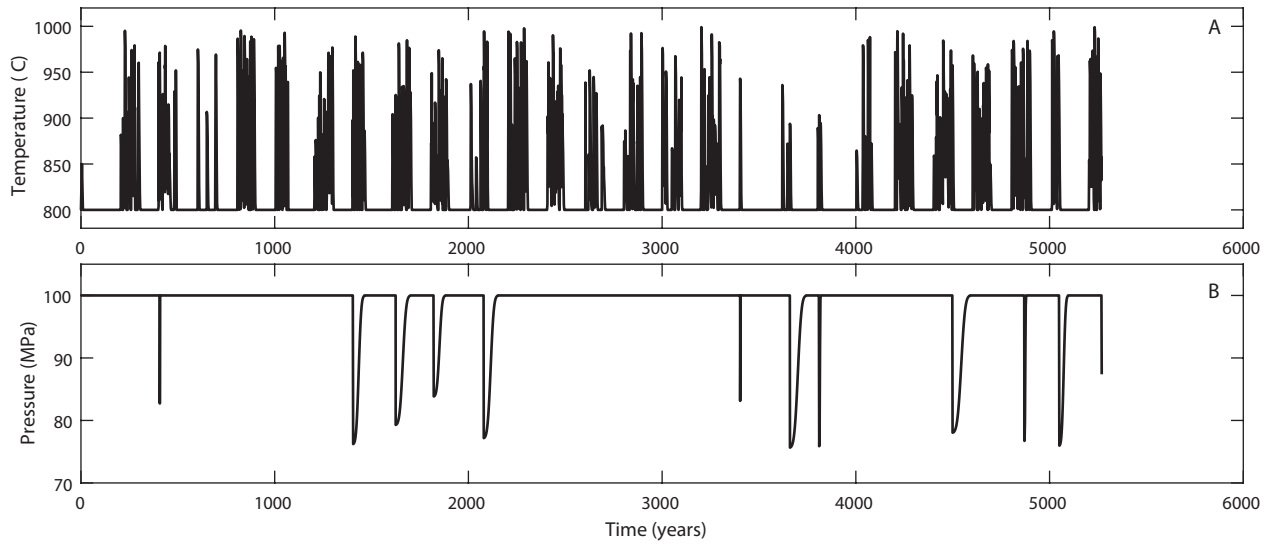


Figure 12

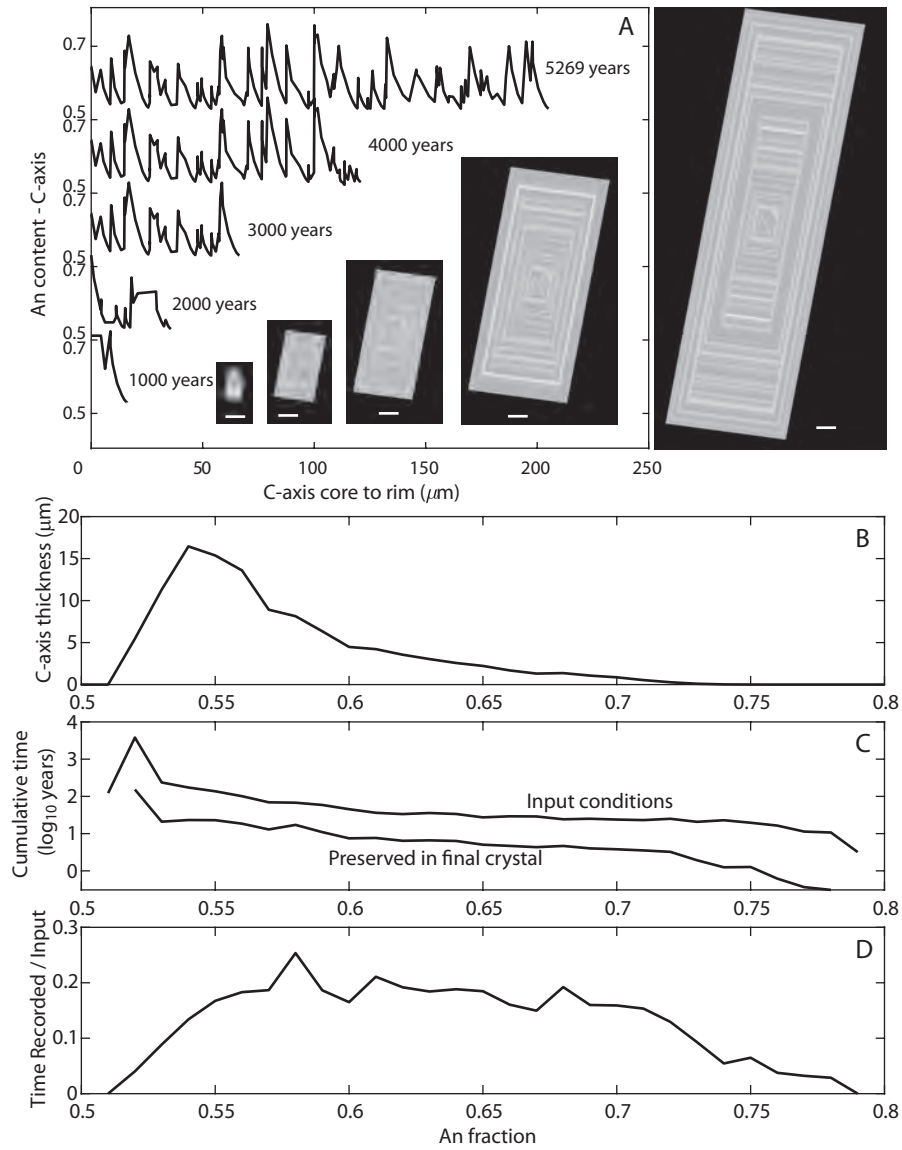


Figure 13