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3	Formation of metasomatic tourmalinites in reduced schists during the Black Hills Orogeny,
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ABSTRACT

19 Tourmaline is a common mineral in granites and metamorphic rocks in collisional 20 orogens. This paper describes graphite-bearing, metasomatic tourmalinites in sillimanite-zone 21 schists of the Proterozoic Black Hills Orogen, South Dakota. The tourmalinites bound quartz 22 veins and beyond about 1 m grade into schists with disseminated tourmaline, and ultimately 23 tourmaline becomes only a trace, intrinsic phase in the schists. Next to the quartz veins 24 tourmaline has almost completely replaced schist minerals, including biotite, muscovite, and 25 plagioclase. The tournaline is generally anhedral and follows the original foliation direction of 26 the schist. However, tourmaline is euhedral in quartz veinlets cutting through the tourmalinites. 27 Tournaline is compositionally zoned from having about 22% to 2% of apparent Al occupancy on the Y sites. There are very good negative correlations of ^Y(Fe²⁺+Mg²⁺), ^XCa²⁺, and ^YTi⁴⁺ with 28 ^YAl³⁺, and a very good positive correlation of X-site vacancies with ^YAl³⁺. Mg# [molar 29 $Mg^{2+}/(Mg^{2+}+Fe^{2+})$] is fairly invariant at approximately 0.5, which is somewhat higher than that 30 31 in the precursor biotite. This is in contrast to tourmaline in the neighboring peraluminous Harney 32 Peak leucogranite where the range of Y site occupancy of Al is small at about 20%, but the Mg# 33 ranges from 0.12 to 0.5.

The compositional trends in the metasomatic tourmaline are dominated by the exchange $X_{\Box} + 4^{Y}Al^{3+} = {}^{X}Ca^{2+} + 3^{Y}(Fe^{2+}+Mg^{2+}) + {}^{Y}Ti^{4+}$. Mass-balance calculations suggest the metasomatizing fluid brought in H⁺ and B(OH)₃ and removed K⁺, SiO₂, and some Fe²⁺ during tourmalinization. Other elements in the tourmaline largely reflect the bulk composition of the replaced schist. The calculations show that silica in the quartz veins was locally derived, not brought in by the metasomatizing fluid. Interstitial graphite in the tourmalinites shows

40	precipitation of carbon from the methane-bearing fluid. The study demonstrates an important
41	effect of boron transfer by fluids during metamorphism and magmatism in the Earth's crust.
42	Keywords: Tourmaline, tourmalinite, metasomatism, schist, fluid, Black Hills
43	
44	INTRODUCTION
45	Relatively high abundances of boron and its common mineral host, tourmaline, are
46	frequent features of collisional granites and metapelites (Henry and Guidotti 1985; Nabelek et al.
47	1992a; Guillot and Le Fort 1995; Nabelek and Bartlett 1998; Nabelek 2019). High abundances of
48	B in metapelites stem from its incorporation into ocean floor sediments (Leeman and Sisson
49	1996). Boron may be conserved in metapelites during prograde metamorphism if it is contained
50	by tourmaline (Henry and Dutrow 1996; Wilke et al. 2002), but if instead bulk of it resides in
51	micas, some of it may be lost from rocks by aqueous fluids produced by mica-consuming
52	metamorphic reactions (Nabelek et al. 1990; Moran et al. 1992; Leeman and Sisson 1996).
53	Ultimately, when all muscovite is consumed from schists during partial melting, most B is
54	incorporated into the melts, although a portion may be retained in residual sillimanite (Grew and
55	Hinthorne 1983). An important feature of B is that it is highly mobile in aqueous fluids as is
56	evident by experiments (Pichavant 1981), frequent association of tourmaline with veins of
57	hydrothermal origin, either as a replacement mineral or a primary mineral (Slack 1996), and by
58	frequent enrichments of B in aureoles of granitic pegmatites, either within micas or in newly-
59	formed tourmaline (Shearer et al. 1984; Shearer et al. 1986; Duke 1995; Wilke et al. 2002).
60	This contribution describes a tourmalinite next to a quartz vein in a sillimanite-grade
61	schist in the aureole of the Harney Peak Granite (HPG) in the Black Hills, South Dakota, USA
62	(Figs. 1, 2). The granite, associated pegmatites, schists, and metagraywackes occur within the

63 Proterozoic core of the Black Hills. The core is a classic orogenic sedimentary wedge that 64 became deformed and metamorphosed during the Proterozoic Black Hills orogeny that was a 65 consequence of the collision of the Archean Wyoming and Superior cratonic blocks. Tourmaline 66 characterizes large portions of the HPG and some pegmatites and is a common metasomatic 67 phase in the metamorphic aureoles that affect the surrounding metapelitic rocks. Although Slack 68 (1996) defined tournalinite as a metasomatized rock with more than 15% tournaline, at the 69 locality described here metasomatism was unusually intense with tourmaline effectively 70 completely replacing a quartz-mica schist. Such tourmalinites also occur at other localities in the 71 western aureole of the HPG. The tourmalinites include interstitial graphite and occur next to 72 quartz veins. 73 The focus of this contribution is on the crystal-chemistry of tourmaline as a recorder of 74 the tourmalinization process and composition of the metasomatizing fluid. Compositions of 75 tourmaline and micas reveal the solutes that were in the metasomatizing fluid and the ion-76 exchange reactions that were responsible for the tourmalinization reactions. Such fluids are 77 likely to exist in deep orogenic wedges undergoing metamorphism during continental collisions, 78 and therefore are an important part of the crustal boron cycle. 79 80 **GEOLOGIC BACKGROUND** 81 Metamorphism and magmatism in the Black Hills were previously described in several

papers (e.g., Norton and Redden 1990; Helms and Labotka 1991; Nabelek et al. 1992a, b, 2006;
Nabelek and Chen 2014). The Proterozoic core of the Black Hills was exposed by late-Mesozoic
to early-Tertiary Laramide uplift and erosion (Redden et al. 1990). Protoliths of the metamorphic
rocks were shales with variable amounts of organic components, graywackes, mafic sills, and to

86	the southeast of the HPG a sandstone (Fig. 1). Metamorphism occurred during a polyphase
87	deformational history. Evidence for the earliest metamorphism (M_1) and deformation (D_1)
88	appears to be restricted to the western margin of the terrane. They were attributed to a regional
89	thrusting related to Yavapai arc accretion from the south between 1790 and 1750 Ma (Dahl et al.
90	1999, 2005). However, metamorphism (M_2) and deformation (D_2) that dominate the structure of
91	the Proterozoic terrane are related to east-west shortening during the Black Hills Orogeny
92	beginning at c. 1750 Ma (Redden et al. 1990; Chamberlain et al. 2003; Dahl et al. 2005).
93	Late-orogenic intrusion of the HPG in the southern Black Hills superimposed contact
94	metamorphism (M_3) and associated deformation (D_3) on the regionally metamorphosed rocks.
95	Intrusion of the granite occurred at c. 1715 Ma (Redden et al. 1990). The HPG pluton and a large
96	pegmatite field are the dominant geologic features of the southern Black Hills (Norton and
97	Redden, 1990). The HPG was built-up by intrusion of many thousands of leucogranite sills and
98	dikes. Most pegmatite intrusions occur in schists and metagraywackes. In close proximity to the
99	HPG, the intrusion of magma transposed the regional S ₂ foliation in metamorphic rocks into S ₃ ,
100	which is more horizontal and generally concordant with granite sills that constructed the HPG
101	(Duke et al. 1988, 1990b). The M_2 and M_3 metamorphic events probably overlapped in time
102	(Redden and DeWitt 2008). Maximum metamorphic pressures in the aureole of the HPG were at
103	least 6 kbar but the aureole appears to have decompressed to about 3 kbar as the granite was
104	being emplaced, probably due to buoyancy (Nabelek and Chen 2014).
105	Fluids were present in the metamorphic rocks during the M ₂ and M ₃ metamorphic events.
106	Compositions of fluid inclusions in quartz veins show that reducing conditions prevailed (Huff
107	and Nabelek, 2007). During M_2 , the fluids were dominated by variable proportions of CH_4 , CO_2
108	and N ₂ . Application of the Andersen and Lindsley (1988) oxygen barometer to Mn-bearing

109 ilmenite and magnetite-ulvöspinel pairs in some garnet-grade samples suggests that fO_2 was 4.6 110 \pm 1.1 log units below the fayalite-magnetite-quartz oxygen buffer. Graphite in the schists ranges 111 from poorly ordered in the garnet zone to well-ordered within the sillimanite zone in the HPG 112 contact aureole (Huff and Nabelek 2007). Fluids in the aureole of the HPG had \sim 25% of 113 carbonic components. Well-ordered graphite commonly occurs along margins of quartz veins 114 and host rocks to the veins (Duke et al. 1990a). In the samples described here, graphite is highly 115 ordered with area ratios of "disordered/ordered" Raman peaks between 0 and 0.1, and fluid 116 inclusions in the quartz vein have >90% CH₄ (Huff and Nabelek 2007). 117 A large portion of fluids in the HPG aureole and aureoles of pegmatite intrusions was 118 magmatic. The fluids caused alkali (Na, K, Li) and B metasomatism of schists and graywackes 119 on various scales (Duke 1995; Wilke et al. 2002; Nabelek et al. 2006; Teng et al. 2006). Fluid 120 flow was probably preferentially concentrated on and near faults that bound the HPG as most 121 intense metasomatism appears to have occurred there. Moreover, tourmalinites described here 122 come from a locality that may have beneath it a portion of the Harney Peak Granite (Duke et al., 123 1990b), from which the metasomatizing fluid may have emanated. 124 The HPG in its outer portions contains abundant tourmaline. The inner portions tend to 125 have biotite instead of tourmaline as the dominant ferromagnesian mineral. Tourmaline ranges 126 from the millimeter scale in aplitic granite layers, in which it may define color banding (often 127 called "line rock"), to the decimeter scale in pegmatitic layers (Rockhold et al., 1987, Duke et al., 128 1988). In pegmatite sheets, both within the granite and the wall rocks, it is oriented almost 129 invariably with the long c-axis perpendicularly to the contacts between the sheets and intruded

130 rocks. Tourmaline's orientation within the intrusive sheets follows the probable direction of heat

131 loss from the crystallizing sheets.

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133 **ANALYTICAL TECHNIQUE AND DATA REDUCTION** 134 Tourmaline, biotite, and muscovite in tourmalinites were analyzed for major elements by 135 a JEOL JXA-8200 electron microprobe at Washington University, St. Louis, Missouri. The 136 operating conditions were 15 keV accelerating voltage, 25 nA specimen current, 5-10 µm beam 137 diameter, and 11 mm working distance. The Mean Atomic Number correction method of 138 Donovan et al. (2016) was used to calculate wt.% of oxides in the minerals. For tourmaline, Si, 139 Ti, Al, Fe, Mn, Mg, Zn, Ca, Na, and K were sought, but Zn was below the detection limit and 140 K₂O was always <0.02 wt.%. F was analyzed in only a subset of tourmaline. 141 Atomic site assignments in tourmaline, given its formula $XY_3Z_6(T_6O_{18})(BO_3)_3V_3W_3$ 142 followed the scheme recommended by Henry et al. (2011). Thirty-one oxygens per formula unit 143 were assumed. The weight percents of H₂O and B₂O₃ were iteratively adjusted to obtain 3 B 144 atoms and 15 other cations in Y+Z+T sites. Vacancies can exist on the X sites. The V and W sites are filled by either OH^- , F^- , or O^{2-} , but here for simplicity, it is assumed that F^- and O^{2-} 145 146 occur only on the W sites. Given the reducing conditions of the environment in which the 147 tourmalinites formed, all Fe was assumed to be ferric. Compositions of tourmaline with minimum and maximum amounts of apparent ^YAl³⁺ in each sample are given in Table 1. Site 148 assignments for biotite and muscovite were calculated by assuming 12 O^{2-} anions and two H⁺ 149 150 cations. All mineral analyses are given in Supplementary Material. 151 152 **PETROGRAPHY OF TOURMALINITE**

153 Tourmalinites described here replaced schists and occur next to quartz veins. This style of 154 occurrence differs from tourmalinites that occur as breccia tourmaline-quartz veins at relatively

155	low-pressure localities (e.g., Dini et al. 2008) or gold-bearing tourmaline-quartz veins (e.g.,
156	Olivo and Williams-Jones 2002). Samples 195-1, 195-3A, B, and 195-5 represent the
157	metasomatic progression from nearly wholly replaced schist to one with only disseminated
158	tourmaline. Sample 195-3A is a 7 mm thick quartz-tourmaline vein that cuts through sample
159	195-3B. In samples 195-1 and 195-3B, interstices between tourmaline grains are mostly filled
160	with graphite (Fig. 3a, c). There are occasional interstitial quartz grains, but most quartz occurs
161	as rounded, anhedral inclusions within tourmaline. Tourmaline within 195-3A is euhedral (Fig.
162	3b). A few grains of pyrrhotite occur in 195-3B. Foliated muscovite, biotite, and quartz dominate
163	sample 195-5, and graphite is much less abundant in it than in the other samples. Plagioclase and
164	minor ilmenite also occur in the sample. Tourmaline is generally euhedral (Fig. 3d).
165	Petrography of samples 195-1 and 195-3B shows apparent alignment of tourmaline
166	grains that corresponds with the local foliation direction in unmetasomatized schist (Fig. 3c). It is
167	unclear whether the tourmaline foliation is due to compression of the tourmaline itself, or
168	whether the tourmaline merely mimics the foliation direction of replaced micas. Tourmaline
169	within 195-3A (quartz vein) and 195-5 appears to be randomly oriented (Fig. 3b, d). The random
170	orientation of tourmaline in sample 195-5 suggests that the bulk of its crystals grew after the
171	development of foliation. Because intrusion of the HPG and pegmatites was the last major event
172	of the Black Hills Orogeny, and some minerals, particularly staurolite, in the aureole of the HPG
173	overgrew the D_3 foliation, the metasomatism at location 195 appears to have been related to the
174	late-orogenic magmatism in the region.
175	Zoning of tourmaline in sample 195-5 is not apparent by either petrography and back-
176	scatter electron (BSE) imaging. On the other hand, zoning of tourmaline is revealed by both

techniques in samples 195-1, 195-3A, and 195-3B. In BSE images, most tourmaline grains in

178 195-1 and 195-3 have fairly bright, broad cores that trend outward toward even brighter zones 179 (Fig. 4a). The shapes of the brighter zones are not well defined. The rims of the grains are gray. 180 In sample 195-3A, the zoning is more pronounced and the shape of zoning is consistent with the 181 euhedral crystal shapes. The cores are gray but become brighter outward. The rims of the grains 182 are again gray. The brightness of the zones correlates mostly with Fe concentration. There is no 183 obvious evidence for detrital grains in any of the tourmaline images. Petrographically in plain 184 light, the most intense zoning of tourmaline appears in 195-3A where it ranges from green in 185 cores to brown outward toward rims (Fig. 3b). However, the very rims have less intense brown 186 color.

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COMPOSITIONAL ZONING IN TOURMALINE

189 Chemical variations in the metasomatic tournaline are best considered in view of the 190 formula $XY_3Z_6(T_6O_{18})(BO_3)_3V_3W$. In the stoichiometric schorl end-member, the X site is filled with Na^+ , the Y sites are filled with Fe^{2+} , the Z sites are filled with Al^{3+} , the T sites are filled 191 with Si^{4+} , the V sites are filled with OH⁻ or O²⁻, and the W site is filled with OH⁻, O²⁻, or F⁻ 192 (Henry et al. 2011). In the dravite end-member, the Y sites are filled with Mg^{2+} instead of Fe²⁺. 193 When Al³⁺ partially occupies the Y sites, it is frequently assumed that its charge is balanced by 194 195 Li⁺ also in the Y sites, which makes up the elbaite component. Although Li was not measured in 196 the metasomatic tourmaline, analysis of schorl-dravite tourmaline in high-Li pegmatites shows 197 that Li concentrations are only up to ~ 1000 ppm by weight (Maloney et al. 2008). Published data 198 suggests that there is only a limited solubility of the elbaite component in dravite-bearing 199 tourmaline, such that there appears to exist a complete solution only between dravite-poor

200 tourmaline and elbaite (Henry and Guidotti 1985; Jolliff et al. 1986; Henry and Dutrow 1992,

201 1996; Keller et al. 1999).

202 The metasomatic tournaline in the Black Hills has sub-equal proportions of schorl and dravite components with up to 22% Al^{3+} in the Y site (Fig 5a). The highest Mg^{2+}/Fe^{2+} is in 203 tourmaline 195-5, probably due to the preferential partitioning of Mg over Fe into tourmaline 204 relative to biotite (Henry and Guidotti, 1985). The Mg²⁺/Fe²⁺ ratios in the metasomatic 205 206 tourmaline are on the high end of the tourmaline composition trend in the HPG (Fig. 5a), but the HPG tourmaline (Supplementary Material) does not trend toward zero ^YAl³⁺. There is no 207 correlation of Mg^{2+}/Fe^{2+} with ${}^{Y}Al^{3+}$ in the metasomatic tourmaline. The Mg# of all metasomatic 208 209 tourmaline is higher than that of biotite in sample 195-5 and in most analyzed metapelites in the 210 Black Hills (Fig. 5b). The correspondence of major element biotite compositions in 195-5 with 211 compositions of biotite in other metapelites shows that its composition was not affected by 212 metasomatism to any significant extent.

The metasomatic tourmaline shows remarkably good negative correlations of $^{\rm Y}({\rm Fe}^{2+}+$ 213 Mg^{2+}), ^XCa²⁺, and ^YTi⁴⁺ with ^YAl³⁺ (Fig. 6a, b; Table 2). There is also a very good positive 214 correlation of X-site vacancies with ^YAl³⁺. Tourmaline within 195-3A (thin quartz vein) occupies 215 the whole compositional trend from ${}^{Y}Al^{3+} = 0.07$ to 0.66, which is also exhibited by optical and 216 217 BSE zoning (Figs. 3, 4). Only portions of the trend are occupied by tourmaline in the other 218 samples, which is also reflected in less pronounced optical and BSE zoning. The tight negative correlation of ${}^{Y}(Fe^{2+}+Mg^{2+})$ with ${}^{Y}Al^{3+}$ is largely driven by Fe^{2+} as the correlation of Mg^{2+} with 219 ^YAl³⁺ is weak (Fig. 6b, Table 2). There are no significant correlations of Na⁺ and O²⁻ with ^YAl³⁺ 220 (Fig. 6c). There is only very minor apparent substitution of Al^{3+} in the T sites (Table 1; 221

Supplementary Material), on average 0.08 atoms per formula unite (apfu) that is ignored in thesubstitution relationships below.

Intercepts of regressions (Table 2) and consideration of errors on the intercepts, suggest that if the tourmaline compositions extended to ${}^{Y}Al^{3+} = 0$, the substitution relative to a

226 stoichiometric dravite-schorl solution would be:

227
$$2^{X}Na^{+} + {}^{Y}(Fe^{2+}+Mg^{2+}) + 2 OH^{-} \rightarrow {}^{X}Ca^{2+} + {}^{X}\Box + {}^{Y}Ti^{4+} + 2 O^{2-} (1)$$

At the high end of the ^YAl³⁺ spectrum, at approximately ^YAl³⁺ = 0.66 where both Ca²⁺ and Ti⁴⁺

229 have zero concentrations, the substitution relative to a stoichiometric dravite-schorl solution is:

230
$${}^{X}Na^{+} + 2{}^{Y}(Fe^{2+}+Mg^{2+}) + OH^{-} \rightarrow {}^{X}\Box + 2{}^{Y}Al^{3+} + O^{2-}$$
 (2)

231 Both of these substitutions require deprotonation on the W site and existence of vacancies on the

232 X site. These two substitutions produce theoretical tourmaline compositions that describe the

ends of the compositional trend (Table 3). Thus, along the trend of decreasing ${}^{Y}Al^{3+}$ the

234 substitution is:

235
$$0.03^{X}Na^{+} + 0.66^{Y}Al^{3+} + 0.15^{X}\Box + 0.03 \text{ OH}^{-} =$$

236 $0.18 {}^{x}Ca^{2+} + 0.48 {}^{y}(Fe^{2+}+Mg^{2+}) + 0.18 {}^{y}Ti^{4+} + 0.03 O^{2-}$ (3)

Because the participation of Na⁺, OH⁻, and O²⁻ in the substitution is minor and none of them shows a significant correlation with ${}^{Y}Al^{3+}$, the substitution is dominated by:

239
$$4^{Y}Al^{3+} + {}^{X}\Box = {}^{X}Ca^{2+} + 3^{Y}(Fe^{2+}+Mg^{2+}) + {}^{Y}Ti^{4+}.$$
 (4)

This substitution effectively represents zoning from green to brown color seen in plain light in
195-3A (Fig. 3b) and from dark to bright portions of the metasomatic tourmaline in BSE images
(Fig. 4).

243

245

DISCUSSION

246 Tourmaline-producing reactions

247 Zoning in tourmaline within the tourmalinities in the aureole of the HPG, from cores with elevated ^YAl³⁺ toward rims with less ^YAl³⁺ but higher ^YFe²⁺ and ^YTi⁴⁺ concentrations, suggests 248 249 that the replacement of muscovite occurred preferentially over the replacement of biotite during 250 early stages of metasomatism. This is not surprising because of the peraluminous compositions of both tourmaline and muscovite. On the other hand, the nearly 1:1 correlation of ^YTi⁴⁺ and 251 252 $^{\rm X}$ Ca²⁺ substitution in tourmaline is surprising. Such a correlation has also been noted in 253 metasomatic tournaline on the island of Elba, Italy (Dini et al. 2008) and at various localities on 254 the margins of the Leinster Granite, Ireland (Gallaher and Kennan 1992). The correlation 255 between the two elements exists in spite of the probability that in the tourmaline studied here, most Ti⁴⁺ came from biotite in the unmetasomatized schists, whereas Ca²⁺ probably came from 256 257 plagioclase. The correlation can be explained by preferential partitioning of both elements into tourmaline over the metasomatizing fluid. Experiments have shown that above 500°C, Ca^{2+} is 258 259 partitioned preferentially into tourmaline over a Cl-bearing fluid (von Goerne and Franz 2000; von Goerne et al. 2011). The average Ca# [molar Ca²⁺/(Na⁺+Ca²⁺)] of 0.22 ratio in the low-Al 260 261 metasomatic tourmaline corresponds closely to the average Ca# of 0.20 in plagioclase in Black 262 Hills schists (unpublished data), and in all likelihood the composition of plagioclase in the 263 metasomatized schist. A correspondence of the Ca# between coexisting tournaline and plagioclase has been noted by von Goerne et al. (2011). The solubility of Ti⁴⁺ in hydrothermal 264 265 fluids is generally low, usually only tens to hundreds of ppm when saturated with rutile (Manning et al. 2008). Instead, Ti⁴⁺ usually prefers to partition into minerals, including silicates. 266

267 Figure 5b shows that tourmaline has a higher Mg/Fe ratio than the replaced biotite, which 268 implies that some Fe was lost into the metasomatizing fluid or incorporated into pyrrhotite. 269 Dissolution of a significant amount of Fe in the metasomatizing fluid has probably occurred 270 given the very low-fO₂ conditions in the system. Fe loss to the fluids is suggested by low-Fe rims 271 on most tourmaline grains (Fig. 4). 272 Two ion-exchange reactions can be written, one for the initial growth of tourmaline that 273 preferentially replaced muscovite (Reaction 5) and one for the latter growth that that involved a 274 progressively increasing amount of reactant biotite (Reaction 6): $1.36 \text{ Bt} + 1.54 \text{ Ms} + 3.00 \text{ B(OH)}_3 + 0.31 \text{ Na}^+_{ag} + 3.90 \text{ H}^+_{ag} \rightarrow$ 275 $Tur(^{Y}Al^{3+} = 0.66) + 0.17 Ilm + 2.46 SiO_{2,aq} + 7.53 H_{2}O + 0.88 Fe^{2+}_{aq} + 2.44 K^{+}_{aq}$ (5) 276 277 $1.47 \text{ Bt} + 0.92 \text{ Ms} + 0.85 \text{ Pl}(\text{An}_{20}) + 3.00 \text{ B}(\text{OH})_3 + 3.85 \text{ H}^+_{aq} \rightarrow$ $Tur({}^{Y}Al^{3+} = 0.1) + 0.02 Ilm + 3.22 SiO_{2 aq} + 6.99 H_{2}O + 0.78 Fe^{2+}_{aq} + 2.04 K^{+}_{aq} + 0.26 Na^{+}_{aq}.$ (6) 278 279 Mineral compositions that were used to compute these reactions are given in Table 4. Tourmaline compositions corresponding to those at ${}^{Y}Al^{3+} = 0.1$ and 0.66 as given by the ends of 280 281 regressed compositional zoning (Fig. 6; Table 2). Biotite and muscovite compositions are 282 averages in sample 195-5. Ilmenite is added as a possible source or sink for Ti^{4+} . The reactions show the addition of $B(OH)_3$ and H^+ by the fluid and dissolution of Fe^{2+} . 283 284 K^+ , and an aqueous SiO₂ species. The reactions imply that the main quartz vein (Fig. 2) and thin 285 quartz veinlets within the tourmalinites (Fig. 3b) are products of the metasomatic reaction, not 286 the cause of it. The SiO₂ is deemed to have been an aqueous species so it could accumulate to 287 make the veins. The apparent dissolution of quartz from the schist during tourmalinization, as is 288 evident by occurrences of round quartz inclusions in tourmaline, suggests that there was a 289 chemical potential gradient of Si between the schist and the metasomatizing fluid into which the

290 Si must have transferred and where quartz has ultimately precipitated. Cl⁻ was probably the dominant anion in the fluid to which Na^+ , K^+ , H^+ , and Fe^{2+} were bonded. F^- was probably a 291 292 minor component as it does not exceed 0.1 apfu in the tourmaline. In biotite in sample 195-5, F⁻ 293 concentration is <0.07 apfu, which is somewhat less than the average amount in biotite in other 294 schists in the Black Hills (Supplementary Material). Reaction 6 shows that there was a sufficient amount of Ti⁴⁺ in biotite to explain the amount in the low-Al tourmaline as ilmenite appears as a 295 296 product of the reaction. Na⁺ as a reactant is needed to balance reaction 5, but is a product in reaction 6, in which Na⁺ is coming from plagioclase. Nevertheless, the small amount of Na⁺ 297 298 involved is consistent with the precursor plagioclase largely controlling the Ca# of the low-Al 299 tourmaline. It is thus apparent that the tourmalinite largely reflects the bulk composition of the replaced schist, except for lost K^+ and some Si^{4+} , Fe^{2+} , and H_2O . 300

301

302 Graphite and methane

Graphite occurs in interstices of the tourmalinites. The graphite apparently precipitated 303 304 from the CH₄-bearing fluid that is evident in microthermometric and Raman spectroscopic 305 analyses of fluid inclusions in the main quartz vein (Huff and Nabelek 2007). A combination of 306 CH₄ and H₂O is predicted to dominate a fluid at the very reduced fO₂ conditions indicated by Fe-307 Ti oxides in the schists (Nabelek et al., 2006) and will cause precipitation of graphite (Ohmoto 308 and Kerrick 1977). Well-ordered graphite is seen not only in the tourmalinites described here, 309 but also in other quartz veins in the high-grade metamorphic rocks of the Black Hills (Duke et al. 310 1990a). Thus, along with components that were needed to replace silicate minerals by 311 tourmaline, the metasomatizing fluid must have contained abundant CH₄ to cause precipitation 312 of the graphite.

313

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IMPLICATIONS

315	The tourmalinites described here and abundant metasomatic tourmaline in the aureoles of
316	the Harney Peak Granite and pegmatites in the Black Hills (Shearer et al. 1984, 1986; Duke
317	1995) demonstrate a high mobility of boron through metamorphic rocks in collisional orogens. In
318	the case presented here, the activity of boron in the fluid was sufficiently high to cause an
319	effectively complete replacement of muscovite, biotite, quartz, and feldspar in schists. Because
320	oceanic sediments that are protoliths to orogenic schists commonly contain organic components,
321	the metamorphic environment was highly reducing. Thus, methane is likely to accompany boron
322	in the fluid and ultimately cause precipitation of graphite along with tourmaline. In a way,
323	tourmalinites in collisional orogens are reflections of the end of a boron cycle that beings with
324	absorption of boron from seawater into clays on the ocean floor, continues with its incorporation
325	into partial melts that mark the limit of metamorphism of oceanic sediments, and ends with
326	expulsion of boron from the crystallizing melts back into the metamorphic aureoles of plutons.
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475	FIGURE CAPTIONS
476	Figure 1: Map showing the location of station 195 in the western aureole of the Harney Peak
477	Granite (HPG). Thin solid lines are formation boundaries and thick solid lines are recognized
478	faults. Thick dashed lines are isograds. Metamorphic zones are Grt = garnet, St = staurolite, Sil =
479	sillimanite, and 2^{nd} Sil = second sillimanite where partial melting has occurred.
480	
481	Figure 2: An image showing a quartz vein that is bounded by tourmalinite. A schist into which
482	the tourmalinite grades is not shown in this image.
483	
484	Figure 3: Thin-section images of (a) 195-1, (b) 195-3A, (c) 195-3B, and (d) 195-5. All images
485	are in plain light and each field of view is 1 mm. (a) and (c) show tourmaline and graphite and
486	some remnant anhedral quartz (white spots). (b) shows tourmaline within a 7 mm thick quartz
487	vein cutting through 195-3B. (d) shows a biotite-muscovite schist with randomly-oriented
488	tourmaline.
489	
490	Figure 4: Back-scatter electron images of (a) sample 195-1 and (b) 195-3A. Each scale-bar
491	represents 100 μ m. Grey areas in tourmaline contain relatively low Fe/Al ratios. The ratio
492	increases with brightness. Interstitial black patches are graphite. Quartz, also black, occurs as
493	rounded inclusions in tourmaline.
494	
495	Figure 5: (a) Relative occupancies of Al^{3+} , Fe^{2+} , and Mg^{2+} on tourmaline's Y sites in
496	tourmalinite and HPG. Compositions of tourmaline in the HPG are given in Supplementary
497	Material. (b) Average molar proportions of Al ₂ O ₃ , FeO, and MgO in individual grains of

498	tourmaline in samples 195-1, 195-3A, 195-3B, and 195-5, in biotite and muscovite in 195-5, and
499	in biotite in other Black Hills schists (Nabelek and Bartlett, 2000; compositions given in
500	Supplementary Material).
501	
502	Figure 6: Variations of selected ions and X-site vacancies with ^Y Al ³⁺ in metasomatic tourmaline.
503	Lines through data are linear regressions given in Table 2. Fe^{2+} contributes more than Mg^{2+} to a
504	tight combined correlation of ${}^{Y}(Fe^{2+}+Mg^{2+})$ with ${}^{Y}Al^{3+}$. Na ⁺ and O ²⁻ do not show significant
505	correlations with ^Y Al ³⁺ .
506	

	195-1 min. ^Y Al	195-1 max. ^Y AI	195-3A min. ^Y Al	195-3A max. ^Y Al	195-3B min. ^Y Al	195-3B max. ^Y Al	195-5 min. ^Y Al	195-5 max. ^Y Al
				Oxides				
SiO ₂	34.71	35.19	34.26	32.51	35.10	35.29	35.40	35.37
TiO ₂	1.03	0.92	1.47	0.20	0.96	0.33	0.83	0.53
AI_2O_3	30.94	32.14	30.18	34.11	31.35	33.59	32.02	32.88
FeO	9.29	8.28	10.77	8.30	9.75	7.81	7.90	7.43
MnO	0.05	0.03	0.05	0.04	0.05	0.04	0.02	0.03
MgO	5.31	5.26	4.52	4.40	5.48	5.22	5.63	5.58
CaO	0.75	0.37	0.90	0.13	0.80	0.20	0.34	0.30
Na ₂ O	2.03	2.04	1.73	1.78	1.98	2.05	2.04	2.08
K ₂ O	0.02	0.01	0.03	0.01	0.03	0.01	0.01	0.02
F ^c	-	-	-	_	0.09	_	-	_
$B_2O_3^{b}$	10.16	10.26	10.05	10.01	10.33	10.37	10.29	10.32
H ₂ O ^b	3.22	3.20	3.20	3.48	3.33	3.31	3.24	3.23
O=F	-	-	-	_	0.04	_	_	_
Total	97.50	97.71	97.17	94.97	99.23	98.23	97.72	97.77
			Site	occupanci	es			
B ^a	3.000	3.000	3.000	3.000	3.000	3.000	3.000	3.000
™Si	5.939	5.961	5.925	5.645	5.906	5.917	5.982	5.956
^T AI	0.061	0.039	0.075	0.355	0.094	0.083	0.018	0.044
^z Al	6.000	6.000	6.000	6.000	6.000	6.000	6.000	6.000
YAI	0.178	0.378	0.079	0.624	0.123	0.554	0.359	0.484
^Y Ti	0.132	0.117	0.191	0.026	0.122	0.042	0.105	0.067
^Y Fe	1.330	1.174	1.558	1.205	1.372	1.095	1.116	1.046
^Y Mn	0.007	0.005	0.008	0.006	0.008	0.006	0.003	0.004
^Y Mg	1.353	1.327	1.164	1.137	1.375	1.304	1.417	1.399
^x Ca	0.137	0.067	0.167	0.024	0.144	0.035	0.062	0.053
^x Na	0.672	0.670	0.581	0.599	0.647	0.667	0.669	0.680
×К	0.004	0.002	0.007	0.002	0.006	0.003	0.001	0.005
^x vacancy	0.187	0.261	0.245	0.375	0.203	0.295	0.267	0.262
^v OH	3	3	3	3	3	3	3	3
^w он	0.670	0.621	0.691	1.000	0.737	0.705	0.654	0.634
^w F ^c	_	_	_	-	0.048	_	_	_
мО	0.330	0.379	0.309	0.000	0.215	0.295	0.346	0.366

TABLE 1. Compositions of tourmaline with minimum and maximum ^YAl in each sample

^a Assumed occupancy.

^b Calculated by assuming 3 boron atoms and 15 Y+Z+T cations.

^c Fluorine was analyzed in only a subset of samples (see Supplementary Materials).

Element or vacancies	regression	R^2
Fe + Mg	–0.77 × ^Y AI + 2.82	0.92
Fe	–0.65× ^Y AI + 1.49	0.55
Mg	–0.12 × ^Y AI + 1.33	0.04
Ti	–0.24 × ^Y AI + 0.17	0.74
Са	–0.31 × ^Y AI + 0.20	0.87
Na	–0.04 × ^Y AI + 0.66	0.02
Vacancies X	0.36 × ^Y AI + 0.13	0.70

 TABLE 2. Regressions of element occupancies with ^YAI

TABLE 3. Tourmaline compositions(apfu) used in computing substitution 3

(upiu) usee	in computing	
Element	Tourmaline	Tourmaline
	$(^{Y}AI = 0.0)$	(^Y AI = 0.66)
[⊤] Si	6.00	6.00
^T AI	0.00	0.00
^z Al	6.00	6.00
YAI	0.00	0.66
^Y (Fe+Mg)	2.82	2.34
^Y Ti	0.18	0.00
^x Ca	0.18	0.00
^x Na	0.64	0.67
^x vacancy	0.18	0.33
^w OH	0.64	0.67
МО	0.36	0.33

Element	Tourmaline (^Y Al = 0.1)	Tourmaline (^Y AI = 0.66)	Biotite	Muscovite
Si	5.922 ^a	5.922 ^a	2.688	3.054
Ti	0.146	0	0.105	0.015
AI	6.178	6.738	1.737	2.831
Fe	1.425	1.061	1.466	0.071
Mg	1.318	1.251	0.865	0.046
Ca	0.169	0	0	0
Na	0.650 ^a	0.650 ^a	0.039	0.187
K	0	0	0.877	0.809
В	3.000	3.000	0.000	0.000
Н	3.660 ^a	3.660 ^a	2.000	2.000
0	31.000	31.000	12.000	12.000

 TABLE 4. Mineral compositions (apfu) used in reactions 5 and 6

^a Because there is no significant correlation of these cations with ^YAI in tourmaline, average concentrations were used to calculate reactions.













