

1 **Revision 1**

2 **Evaluation and application of the quartz-inclusions-in-epidote mineral**
3 **barometer**

4
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16
17 **Abstract**

18 We have examined the suitability of a quartz-inclusions-in-epidote (qtz-in-ep) mineral
19 barometer to better constrain P-T histories of epidote-bearing lithologies. Theoretical calculations
20 applying an isotropic elastic model suggest that the qtz-in-ep barometer exhibits minimal
21 temperature dependence, and thus, offers the potential to constrain growth conditions of epidote
22 in various geologic environments, including skarn deposits, epidote-bearing granitoids, and
23 metamorphic rocks.

24 To test if the applied equations of state and isotropic elastic model reasonably simulate the
25 elastic evolution of two anisotropic minerals, we measured Raman shifts of the 464 cm⁻¹ band of
26 quartz inclusions relative to that of an unencapsulated quartz standard. We calculated a quartz
27 inclusion pressure (P_{incl}^{464}) at various temperatures, and compared these values with temperature-
28 dependent P_{incl} predicted by elastic modeling ($P_{\text{incl}}^{\text{mod}}$) at elevated temperatures. Three epidote-
29 bearing samples with reasonably well-constrained P-T histories were also examined: 1) sample
30 HF14C from the Upper Schieferhuelle in the Western Tauern Window ($P_{\text{incl}}^{464} = 0.01$ GPa), 2)
31 sample LdC-31C from Lago di Cignana ($P_{\text{incl}}^{464} \approx 0.16$ GPa), and 3) sample FT1E from the Frosnitz
32 Tal in the Western Tauern region ($P_{\text{incl}}^{464} = 0.57$ GPa).

33 Entrapment pressures (P_{ent}^{464}) calculated from P_{incl}^{464} determined at various temperatures show
34 nominal differences from P_{ent} calculated from $P_{\text{incl}}^{\text{mod}}$, suggesting that for qtz-in-ep pairs, the
35 calculated P_{ent} does not significantly vary with the temperature of measurement. Furthermore, our
36 calculated P_{ent}^{464} for a sample from the Upper Schieferhuelle is in agreement with petrographic
37 context and previously-established P conditions, and the P_{ent}^{464} determined for the Frosnitz Tal
38 sample closely approximate previously reported pressures. The **Lago di Cignana sample is derived**
39 **from an epidote vein that is encased in a high-P foliation, and the** calculated P_{ent}^{464} is consistent with
40 early, low-P epidote vein formation that pre-dates high-P metamorphism, or alternatively, late vein
41 formation during exhumation, and confirms that the epidote did not form at or near peak conditions
42 (~2.0 GPa). Results of this study indicate that the qtz-in-ep barometer potentially provides another
43 tool that geoscientists can employ to better constrain P-T conditions in some epidote-bearing
44 environments, where conventional thermobarometric techniques cannot be applied.

45 Introduction

46 A fundamental goal of many geosciences studies is to constrain the pressure-temperature
47 (P-T) histories of igneous and metamorphic rocks. Many different thermobarometers have been
48 developed during the past decades to unravel complex P-T histories, and in recent years, elastic
49 thermobarometry has gained wide acceptance and applicability. Elastic thermobarometry is a
50 method that can constrain P-T conditions in a wide range of geologic environments, and records
51 conditions at which a host crystal grows and encapsulates a mineral inclusion. Because the elastic
52 properties of the inclusion and host almost always differ, upon exhumation an inclusion can
53 develop a residual pressure that is higher (or lower) than that of the surrounding host. Application
54 of elastic thermobarometers requires that changes in inclusion and host volumes from the time of
55 host growth through exhumation to Earth's surface are well constrained. When combined with
56 careful petrographic, mineralogical and petrological studies, the method can be applied to
57 constrain P-T conditions of mineral growth and fabric development, allowing deformation and
58 tectonic processes to be independently constrained. The potential applications of the technique are
59 many, yet the applicability of the technique has been limited to a few inclusion-host pairs, such as
60 apatite-in-garnet (Ashley et al. 2017; Barkoff et al. 2017, 2019), quartz-in-garnet (e.g., Enami et
61 al. 2007; Ashley et al. 2014, 2015; Kouketsu et al. 2014; Spear et al. 2014; Behr et al. 2018;
62 Bonazzi et al. 2019), zircon-in-garnet (Zhong et al. 2019), **garnet-in-diamond (Kueter et al. 2016)**,
63 **kyanite-in-diamond (Nestola et al. 2018)**, **magnesiochromite-in-diamond (Nestola et al. 2019)**,
64 **olivine-in-diamond (Izraeli et al. 1999; Nestola et al. 2011; Howell et al. 2012)**, **periclase-in-**
65 **diamond (Anzolini et al. 2019)**, and coesite-in-diamond, garnet, and zircon (Parkinson and
66 Katayama 1999; Sobolev et al. 2000). The quartz-in-garnet (qtz-in-grt) inclusion-host pair is the
67 most commonly implemented barometer because the high compressibility of quartz relative to the
68 rigid host garnet allows for retention of significant residual pressures. Additionally, the ubiquity

69 of quartz inclusions in garnet, the stability of garnet across a wide range of P-T conditions, and the
70 fact that garnet is a nearly isotropic host, makes this technique applicable to a wide range of
71 geologic environments.

72 Quartz-in-epidote (qtz-in-ep) is similarly a potentially useful barometer because: 1) the qtz-
73 in-ep barometer exhibits minimal temperature dependence (Fig. 1); 2) epidote is abundant and
74 crystallizes in a broad range of geologic settings (P-T conditions); 3) quartz is commonly found as
75 inclusions within epidote in a wide range of rock types; and 4) the thermodynamic properties of
76 quartz and epidote group minerals are reasonably well constrained (e.g., Holland et al. 1996;
77 Pawley et al. 1996; Mao et al. 2007; Gatta et al. 2011; Qin et al. 2016). The barometer is not limited
78 by sluggish kinetics and partial disequilibrium (e.g., Rubie 1998; Carlson 2002), and can help to
79 constrain P-T conditions that other thermobarometers may fail to record (e.g., fluid inclusions are
80 commonly modified or destroyed during prograde metamorphism). The qtz-in-ep barometer offers
81 the potential to constrain formation conditions in several environments for which few other
82 barometers are available, including epidote-bearing skarn deposits, epidote-bearing granitoids,
83 metamorphic rocks, epidote veins, and hydrothermally altered igneous rocks. The qtz-in-ep
84 barometer, combined with detailed field observations, examination of microstructures and
85 petrographic relationships, and independent thermobarometry, offers the possibility to
86 considerably improve our understanding of the P-T history of epidote-bearing rocks. The qtz-in-
87 ep barometer can potentially refine estimates of depths (pressures) of epidote formation in
88 metamorphic rocks and can be applied to a wide-range of bulk compositions, and the barometer
89 can also supplement existing techniques to determine formation conditions of epidote-bearing
90 granitoids and skarns.

91 This study describes the applicability of a qtz-in-ep barometer by measuring temperature
92 dependent Raman band positions of quartz, and comparing entrapment pressures calculated from
93 elastic thermobarometry with independent thermobarometry (Selverstone and Spear 1985;
94 Selverstone et al. 1992; Frezzotti et al. 2011). We follow a similar approach to that implemented
95 by Ashley et al. (2016). Elastic models have been developed for isotropic minerals and assume a
96 spherical inclusion geometry, and experiments that determine pressure-dependent Raman shifts
97 are carried out under hydrostatic conditions. For the quartz-in-epidote pair, these assumptions may
98 not be appropriate, necessitating the need for heating measurements to monitor the inclusion
99 pressure of the inclusion-host pair as temperature changes. Therefore, Raman analyses were
100 conducted at various temperatures to test the ability of the current modeling approach to predict
101 the evolution of inclusion pressure during heating of two anisotropic minerals (quartz-in-epidote).
102 We compare heating measurements and model results by two methods: 1) the Raman shift of the
103 quartz 464 cm^{-1} band was measured and used to calculate an inclusion pressure (P_{incl}^{464}) at a given
104 temperature, which we compared to P_{incl} that is predicted by elastic modeling at elevated
105 temperatures ($P_{\text{ent}}^{\text{mod}}$), and 2) entrapment pressures (P_{ent}^{464}) are calculated based on P_{incl}^{464} at elevated
106 temperature and are compared to entrapment pressures calculated from $P_{\text{ent}}^{\text{mod}}$.

107

Samples

108 Quartz inclusions in epidote from three samples with well-constrained P-T histories were
109 analyzed, and we compared our pressure estimates to the previously-determined P-T histories. The
110 samples are from three different localities that have experienced different P-T histories, and they
111 allow us to test the feasibility of implementing the qtz-in-ep barometer in metamorphic rocks that
112 have experienced different P-T paths. We also consider whether our calculated entrapment

113 pressures are reasonable and consistent with the petrographic evidence that documents the
114 formation and deformation history of the epidote hosts.

115 **Upper Schieferhuelle – HF14C**

116 Sample HF14C is a metamafic rock from the Upper Schieferhuelle (USH) in the western
117 Tauern Window, Italy, that contains a well-defined foliation defined by amphibole, epidote, quartz,
118 chlorite, and plagioclase. P-T estimates that are used here for comparison have been derived from
119 pelitic and mafic samples in the USH.

120 Reference P-T conditions of USH pelites have been estimated based on (1) mineral
121 chemistry thermobarometry, (2) Gibbs modeling of garnet zoning, and (3) fluid-inclusion
122 thermobarometry (Ferry and Spear 1978; Spear and Selverstone 1983; Selverstone and Spear
123 1985). Garnet-biotite thermometry, and garnet-plagioclase-biotite-muscovite barometry (from
124 garnet rims and matrix grain rims) give P-T estimates of $\sim 475 \pm 25$ °C and $\sim 0.5 - 0.6$ GPa. Garnet
125 core and rim modeling indicate P-T conditions of ~ 450 °C and $\sim 0.5 - 0.6$ GPa, and ~ 475 °C and
126 $\sim 0.5 - 0.6$ GPa, respectively. Garnet zoning between cores and rims indicates intermittent pressure
127 fluctuations during heating. The texturally oldest fluid inclusions in this sample indicate P-T
128 conditions of ~ 0.6 GPa and $\sim 450 - 500$ °C and may record near peak (T) conditions or the early
129 stages of USH exhumation. Younger fluid inclusions indicate near isothermal decompression after
130 the USH reached peak P-T conditions.

131 P-T constraints for the mafic samples from the Upper Schieferhuelle (USH) are based on
132 a lack of glaucophane, the presence of lawsonite pseudomorphs, and the stability of Ca-amphibole,
133 albite, and chlorite throughout the history of the mafic samples, which places P-T conditions in a
134 field that has been described as the lawsonite-albite-chlorite subfacies of blueschist facies ($\sim 0.4 -$

135 0.6 GPa; Turner 1981; Selverstone and Spear 1985; Peacock 1993). Epidotes from this sample are
136 oriented parallel to foliation and suggest that growth of epidote occurred prior to, or during,
137 foliation-forming deformation (Fig. 2A) – this observation is important for comparing our results
138 with previous P-T estimates, as described in more detail below.

139 **Lago di Cignana – LdC-31C**

140 Sample LdC-31C (SESAR database; hand sample: IGSN = IECHL005C, thin section:
141 IGSN = IECHL00B2) is a felsic rock from Lago di Cignana, Italy (Selverstone and Sharp 2013),
142 a region that has experienced ultra-high-pressure metamorphism as evidenced by a diamond-
143 bearing horizon (Frezzotti et al. 2011). Temperature estimates of ~600 °C, with minimum pressure
144 estimates of 3.2 – 3.4 GPa, suggest that these samples reached the diamond stability field where
145 quartz is not stable (Groppo et al. 2009; Frezzotti et al. 2011). The foliation in the rock is defined
146 by quartz, epidote and white mica; however, epidote that we analyzed is derived from a coarse-
147 grained epidote-fuchsite vein that exhibits an irregular, undulating contact with the primary
148 foliation (Fig. 2B). The undulating boundary suggests that the epidote in the vein may have formed
149 prior to the primary foliation-forming event in the region, or during exhumation, and experienced
150 minor deformation after formation of the primary foliation.

151 **Frosnitz Tal – FT1E**

152 Sample FT1E is a metasediment from Frosnitz Tal in the Tauern Window, Austria, that
153 contains a well-defined foliation defined by quartz, epidote, white mica, omphacite, and chlorite
154 (Fig. 2C). Most published P-T conditions for the area are derived from metabasites from the
155 eclogite zone, and indicate peak metamorphic conditions of ~ 625 °C and ~1.9 – 2.5 GPa, based
156 on multiple thermobarometric techniques, e.g., Holland (1979): 650 C, 1.95 GPa; Selverstone et

157 al. (1992): 625 °C, 2.0 GPa; Kurz et al. (1998): 550 – 635 °C, 1.9 – 2.3 GPa; Hoschek (2001): 590-
158 630 °C, 1.95 – 2.24 GPa; Miller and Konzett (2003): 623 °C, 2.04 GPa; Hoschek (2007): 630 °C,
159 2.5 GPa. Slightly lower peak P-T conditions ($P \approx 2.0$ GPa, $T \approx 600$ °C) have been estimated for
160 adjacent metasediments (e.g., Spear and Franz 1986). Epidotes in the matrix are oriented parallel
161 to the primary foliation, suggesting crystallization of epidote occurred prior to, or during, the
162 primary fabric forming deformation.

163 **Analytical methods**

164 To test the suitability of using an isotropic elastic model to interpret data obtained from
165 two anisotropic phases, quartz inclusions in epidotes from three localities were analyzed by Raman
166 spectroscopy at various temperatures. For samples HF14C and FT1E, a single quartz inclusion in
167 epidote was analyzed. During heating and analysis of a quartz inclusion in sample LdC-31C, the
168 window in the heating stage cracked and the inclusion could not be heated to the final temperature;
169 a second inclusion in a different epidote crystal from this sample was selected and analyzed.
170 Samples were prepared by doubly polishing single epidote crystals that were then individually
171 loaded onto a heating stage for Raman analyses. The diameter of measured quartz inclusions
172 ranged from 10 – 15 μm , and significant care was taken to select isolated inclusions that were
173 away from recognizable fractures, cleavage or other inclusions, and at least 3 times the inclusion
174 radial distance from the host exterior (surface) to avoid relaxation of the inclusion (Campomenosi
175 et al. 2018; Mazzucchelli et al. 2018).

176 Analyses during heating were completed at Virginia Tech on a Linkam THMSG600
177 heating stage mounted onto a JY Horiba LabRam HR800 Raman spectrometer with 1800 lines/mm
178 grating. We used a 40x objective with a confocal aperture of 400 μm and a 150 μm slit width.
179 Raman spectra were centered at 360 cm^{-1} (total spectral range of $\sim 74 - 633$ cm^{-1}). All spectra were

180 collected with a 514.57 nm wavelength Ar laser, 30–45 s accumulation time, and 3 accumulations.
181 The laser interference filter was removed for all analyses, allowing us to simultaneously correct
182 measurements for drift by monitoring the position of the Ar plasma lines. For all samples, Raman
183 analyses were performed at ambient pressure and from room temperature to 600 °C in 50 °C
184 increments. The inclusions were also analyzed during subsequent cooling to test for reproducibility
185 to ensure that deformation induced during heating was elastic. All Raman spectra were temperature
186 reduced using the Bose-Einstein distribution factor to compare Raman measurements made at
187 elevated temperatures (Kuzmany 2009). After the spectra were temperature reduced, a linear
188 background correction was applied to samples LdC-31C and HF14C, and a polynomial
189 background correction was applied to sample FT1E (raw and reduced Raman spectra are provided
190 in the Supplementary Material). All Raman data was fit using PeakFit v4.12 (by Systat Software
191 Inc). A Gaussian area model was used to fit Ar plasma lines, and a Voigt Gaussian/Lorentz area
192 model was used to fit quartz and adjacent epidote bands. The 116.04 and 266.29 cm⁻¹, and 520.3
193 cm⁻¹ Ar plasma lines were used for linear drift corrections of the peak positions of quartz
194 vibrational modes near 128 cm⁻¹, 206 cm⁻¹, and 464 cm⁻¹, respectively. Peak positions of quartz
195 inclusion bands were determined relative to the peak positions of an unencapsulated Herkimer
196 quartz standard that was analyzed 5 times every day during analysis of the inclusions (Table S1).
197 The propagated errors reported in this study account for errors in peak fit statistics for the Ar
198 plasma line, quartz peaks, and instrumental uncertainty (± 0.1 cm⁻¹).

199 Based on information in the RRUFF database (Lafuente et al. 2016), the Raman spectra of
200 monoclinic epidotes shows bands in the region from $\sim 375 - 550$ cm⁻¹. Epidotes have vibrational
201 modes that exhibit strong Raman intensities at ~ 425 cm⁻¹ and 455 cm⁻¹, and lower intensity Raman
202 modes at ~ 396 cm⁻¹, ~ 443 cm⁻¹, ~ 475 cm⁻¹, ~ 490 cm⁻¹, ~ 510 cm⁻¹, and ~ 528 cm⁻¹. The absolute

203 band position and intensity varies depending on composition (Fig. 3A, 3B). Furthermore, the
204 intensity of the epidote bands varies with crystal orientation, due to the orientation-dependent
205 polarizability of mineral vibrational modes (Fig. 3A, 3B, Graves and Gardiner 1989). To account
206 for peak overlap, we deconvolved Raman bands that are between $\sim 375 - 550 \text{ cm}^{-1}$ into ~ 10 peaks
207 to simultaneously fit the quartz 464 cm^{-1} band, adjacent epidote bands (~ 8 bands), and the 520.3
208 cm^{-1} Ar plasma line (Fig. 3, all high-T peak fits are provided in the Supplementary Material). The
209 interference (overlap) of the quartz 464 cm^{-1} band with shouldering epidote bands becomes more
210 pronounced at higher T as the quartz band shifts to lower wavenumbers and mineral peaks broaden.
211 As epidote bands broadened at high temperature, some lower intensity bands became hidden, and
212 they were removed from the peak fitting procedure due to the large uncertainty associated with
213 their peak fit positions.

214 Electron probe microanalyses (EPMA) were carried out at the University of Texas at
215 Austin on a JEOL 8200 microprobe equipped with five wavelength-dispersive spectrometers.
216 Epidotes were analyzed for Na, Al, K, Mn, Ti, Mg, Si, Ca, Fe, and Cr using a $10\text{-}\mu\text{m}$ beam size,
217 10 nA beam current and 15 keV accelerating voltage. All elements were measured for 30 s on peak
218 and a mean atomic number background correction was applied. Primary standards used include:
219 synthetic anorthite glass; synthetic orthoclase; natural chromite from the Stillwater complex
220 (531M-8); synthetic enstatite; natural Amelia albite from Amelia, Virginia; and ilmenite from the
221 Ilmen Mountains, USSR (USNM96189). Analyses were monitored by analyzing Kakanui
222 hornblende as a secondary standard, using the same operating conditions as for the unknowns. All
223 iron in epidote was assumed to be ferric, and epidotes were classified according to the
224 nomenclature of Franz and Liebscher (2004). Major element compositions of epidote hosts in this

225 study and the mole fractions of epidote components (epidote and clinozoisite) are given in Table
226 S5.

227 **Calculation procedures**

228 **Calculation of inclusion pressures**

229 Raman shifts of the quartz (inclusion) 464 cm^{-1} band ($\omega_{\text{incl}}^{464}$) at a given temperature were
230 determined relative to the Raman shift of the 464 cm^{-1} band of a Herkimer quartz crystal ($\omega_{\text{std}}^{464}$)
231 measured at 0.1 MPa and the same temperature ($\Delta\omega_{\text{shift}}^{464} = \omega_{\text{incl}}^{464} - \omega_{\text{std}}^{464}$; Table 2). This allowed us
232 to correct for temperature-induced strain on the quartz inclusions, and to monitor stress-induced
233 strains (Murri et al. 2018, 2019). For sample HF14C (low-P inclusion), we calculate $\Delta\omega_{\text{shift}}^{464}$ of
234 inclusions relative to the Herkimer quartz standard using a polynomial equation that describes the
235 $\omega_{\text{std}}^{464}$ of a Herkimer quartz analyzed at 0.1 MPa and the measurement temperature. The $\omega_{\text{std}}^{464}$ -
236 temperature relationship is linear over most of the temperature range, but deviates from linearity
237 near the quartz α - β transition (Fig. 4, Table S2, Ashley et al., 2016). The temperature of the quartz
238 α - β transition occurs at $\sim 573^\circ\text{C}$ at 0.1 MPa, and increases by about $0.25^\circ\text{C}/\text{MPa}$. Thus, the higher
239 P_{incl} samples (FT1E and LdC-31C) do not approach the quartz α - β transition during heating to
240 600°C , and we calculated $\Delta\omega_{\text{shift}}^{464}$ using a linear extrapolation to the polynomial equation (Fig. 4,
241 Tables S3, S4). Quartz inclusions in epidote record a smaller change in wavenumber of the 464
242 cm^{-1} Raman band during heating relative to Herkimer quartz at ambient pressure, because the
243 inclusion pressure increases during heating. The increase in $\Delta\omega_{\text{shift}}^{464}$ reflects the effect of pressure
244 on encapsulated quartz (inclusions) during heating, due to its higher thermal expansivity relative
245 to epidote. The hydrostatic calibration of Schmidt and Ziemann (2000) was used to calculate P_{incl}^{464}
246 from $\Delta\omega_{\text{shift}}^{464}$ at elevated T.

247 Recent studies report conflicting results concerning the accuracy of entrapment pressures
248 that are calculated from Raman shifts of the quartz 464 cm⁻¹ band with increasing pressure
249 assuming hydrostatic calibrations (P_{incl}^{464} , Thomas and Spear 2018; Bonazzi et al. 2019). Some
250 experiments that synthesize garnets with quartz inclusions show that P_{incl}^{464} provides accurate garnet
251 growth pressures (Thomas and Spear 2018). Results from other experiments show that sometimes
252 P_{incl}^{464} can accurately replicate experimental conditions (2.5 GPa experiments), but that in other cases
253 (3.0 GPa experiments), use of the 464 cm⁻¹ band underestimates experimental P_{ent} , and the use of
254 quartz strains ($P_{\text{incl}}^{\text{strains}}$) better replicates experimental conditions (± 0.2 GPa; Bonazzi et al. 2019).
255 To assess the extent of anisotropy that quartz inclusions retain in an anisotropic host (epidote), we
256 calculate $P_{\text{incl}}^{\text{strains}}$ to account for quartz anisotropy, and compare it to P_{incl} calculated from hydrostatic
257 calibrations (Fig. 5, Tables S2, S3). Calculating quartz strains requires that Raman shifts of at least
258 2 quartz vibrational modes can be measured. For samples HF14C and LdC-31C, we measured the
259 quartz 128, 206 and 464 cm⁻¹ band positions at ambient temperature. Strains were determined from
260 the Raman shifts of quartz 128 cm⁻¹, 206 cm⁻¹ and 464 cm⁻¹ bands by using Strainman (Murri et
261 al. 2018, 2019; Angel et al. 2019), and they were then converted to a mean stress [$P_{\text{incl}}^{\text{strains}} = (2\sigma_1 +$
262 $\sigma_3)/3$] using the matrix relationship $\sigma_i = c_{ij}\epsilon_j$, where σ_i , c_{ij} , and ϵ_j , are the stress, elastic modulus,
263 and strain matrices, respectively. We used the α -quartz trigonal symmetry constraints of Nye
264 (1985) and quartz elastic constants of Wang et al. (2015). For sample FT1E, only the quartz 464
265 cm⁻¹ band was fit at ambient temperature because the 128 and 206 cm⁻¹ bands exhibited low
266 intensities or had significant overlap with epidote peaks.

267 **Calculation of entrapment conditions**

268 Entrapment pressures (P_{ent}) and modeled inclusion pressures (P_{incl}^{mod}) were calculated by
269 implementing the Guiraud and Powell (2006) 1-D elastic model, with an updated exact solution
270 described by Angel et al. (2017b), following the equation:

$$271 \quad \left[\left(\frac{V_{P_{meas}, T_{meas}}}{V_{P_{ent}, T_{ent}}} \right)_{incl} - \left(\frac{V_{P_{meas}, T_{meas}}}{V_{P_{ent}, T_{ent}}} \right)_{host} \right] \left(\frac{V_{P_{ent}, T_{ent}}}{V_{P_{foot}, T_{meas}}} \right)_{incl} - \frac{3}{4G_{host}} (P_{incl} - P_{ext}) = 0$$

272 Where $(V_{P_{meas}, T_{meas}}/V_{P_{ent}, T_{ent}})_{incl}$ and $(V_{P_{meas}, T_{meas}}/V_{P_{ent}, T_{ent}})_{host}$ are the molar volume ratios
273 of the entrapped inclusion and the host at measurement conditions ($V_{P_{meas}, T_{meas}}$), and at entrapment
274 conditions ($V_{P_{ent}, T_{ent}}$), respectively. $(V_{P_{ent}, T_{ent}}/V_{P_{foot}, T_{meas}})_{incl}$ is the inclusion molar volume ratio at
275 entrapment conditions, and at a measurement temperature and a pressure along an isomeke defined
276 by the entrapment conditions ($V_{P_{foot}}$, see Angel et al. 2017b). G_{host} , P_{incl} , and P_{ext} are the shear
277 modulus of the host, the inclusion pressure at measurement conditions, and the pressure of the host
278 (0.1 MPa) at ambient T, respectively. P_{incl}^{mod} and P_{ent} were calculated using an internal MATLAB
279 script that allows for ideal mixing of solid-solutions; see Table S6 for a comparison of entrapment
280 pressures calculated using EoSFit-Pinc (Angel et al. 2017b). Modeled P_{incl} (P_{incl}^{mod}), i.e., the
281 evolution of P_{incl} that is predicted by elastic modeling, is calculated by determining a residual
282 quartz inclusion pressure (P_{incl}^{464}) at ambient T from Raman measurements, calculating an
283 entrapment pressure (P_{ent}^{464}) from P_{incl}^{464} (and an assumed entrapment temperature), and subsequently
284 back-calculating P_{incl}^{mod} at elevated T from the determined entrapment pressure (constant).
285 Therefore, the modeled P_{ent} does not depend on the T of the Raman measurement. The increase of
286 P_{incl}^{mod} reflects the increase in pressure that an inclusion would have to record at elevated T to predict
287 the same P_{ent} . Entrapment pressures calculated from Raman measurements of quartz inclusions at
288 elevated T (P_{ent}^{464}) use P_{incl}^{464} determined from quartz at various temperatures during heating of the

289 sample, the T during heating measurements, and an assumed entrapment T (see Figure S1 for a
290 schematic illustration of the calculation method).

291 Molar volumes (V) of quartz were calculated using the quartz parameters of Angel et al.
292 (2017a), and following their curved boundary model approach. Thermodynamic properties of
293 epidote and clinozoisite were derived from the experimental P-T-V data of Gatta et al. (2011), and
294 Qin et al. 2016 Pawley et al. (1996), respectively. P-T-V data were fit using EoSFit7c (Angel et
295 al. 2014). Epidote and clinozoisite data were fit with the modified Tait Equation of State (EoS)
296 and **thermal pressure term** (Fig. S2). The clinozoisite thermodynamic properties are less well
297 constrained, because the P-T-V data are derived from two experimental sources that used different
298 epidote crystals (bulk modulus from Qin et al. 2016, $X_{ep} = 0.39$; thermal expansivity from Pawley
299 et al. 1996, $X_{ep} = 0.02$); therefore, the thermodynamic properties calculated using data from two
300 different sources may have a larger uncertainty. The clinozoisite P-V data of Qin et al. (2016) were
301 used because it shows smaller errors, and to the best of our knowledge, no updated T-V data exist
302 for clinozoisite. For zoisite, we use the reference bulk modulus and thermal expansivity given in
303 Holland and Powell (2011), and the Tait EoS and thermal pressure term (Table 2). Shear moduli
304 for epidote, clinozoisite, and zoisite were calculated by implementing the aggregate Poisson's ratio
305 of 0.26 from Mao et al. (2007) and the determined bulk moduli (Table 2). The shear modulus for
306 an isotropic material is given by:

307
$$G = \frac{3K(1 - 2\nu)}{2(1 + \nu)}$$

308 where G is the shear modulus, K is the bulk modulus, and ν is the Poisson ratio. This relationship
309 predicts a shear modulus for epidote of 65.1 GPa, calculated from the Gatta et al. (2011) bulk
310 modulus (Table 2); the calculated value closely approximates experimentally determined values

311 (e.g., 61.2 GPa, Ryzhova et al. 1966). We are not aware of experimental shear modulus data for
312 clinozoisite; therefore, to maintain internal consistency we calculate shear moduli using our
313 regressed bulk moduli and equation 2; the calculated shear moduli are given in Table 2. The small
314 difference between experimentally-derived and calculated shear moduli have a **minimal** effect on
315 P_{ent} . The molar volume and shear modulus of epidote and clinozoisite solid-solution compositions
316 **were** calculated assuming ideal (linear) mixing. A comparison of epidote V- X_{ep} (mol fraction of
317 epidote) that is based on the compilation of Franz and Liebscher (2004) shows that linear mixing
318 of molar volumes is an appropriate approximation (Fig. S3). Elastic modeling suggests that X_{ep}
319 has a greater influence on calculated entrapment pressures when epidote preserves quartz with
320 higher P_{incl} (Fig. 1D).

321 **Results and Discussion**

322 **Raman analyses at ambient conditions**

323 We compare P_{incl}^{464} of samples HF14C and LdC-31C with P_{incl} calculated from hydrostatic
324 calibrations of Raman shifts of the 128 cm^{-1} (P_{incl}^{128}) and 206 cm^{-1} (P_{incl}^{206}) quartz bands with pressure
325 (Schmidt and Ziemann, 2000), and with strains ($P_{\text{incl}}^{\text{strains}}$). If we assume a $P_{\text{incl}}^{\text{strains}}$ error (1σ) that is
326 equal to the error of P_{incl}^{464} , P_{incl} calculated from both approaches are within error (1σ , Fig. 5, Tables
327 S2, S3). We note that the $P_{\text{incl}}^{\text{strains}}$ error is a minimum uncertainty, because the errors associated with
328 peak fitting for the quartz 128 cm^{-1} and 206 cm^{-1} bands are significant (Tables S2, S3).

329 P_{incl} estimates for sample HF14C resulting from hydrostatic calibrations of Raman shifts of
330 quartz 128, 206, and 464 cm^{-1} bands are statistically identical (within error, 1σ): $P_{\text{incl}}^{128} = 29 \pm 37$
331 MPa, $P_{\text{incl}}^{206} = 27 \pm 23$ MPa, and $P_{\text{incl}}^{464} = 15 \pm 26$ MPa (1σ , Fig. 5, Table S2). $P_{\text{incl}}^{\text{strains}}$ (48 MPa) indicates
332 a slightly higher P_{incl} than that predicted from hydrostatic calibrations; however, the similar

333 inclusion pressures calculated from hydrostatic calibrations and strains suggest that this quartz
334 inclusion retains nominal strain anisotropy. Quartz inclusions from sample LdC-31C retain
335 residual pressures of: $P_{\text{incl}}^{128} = 90 \pm 31$ MPa, $P_{\text{incl}}^{206} = 125 \pm 77$ MPa, $P_{\text{incl}}^{464} = 144 \pm 23$ MPa (inclusion
336 1, 1σ) and $P_{\text{incl}}^{128} = 157 \pm 32$ MPa, $P_{\text{incl}}^{206} = 140 \pm 21$ MPa, $P_{\text{incl}}^{464} = 175 \pm 24$ MPa (inclusion 2, 1σ).
337 $P_{\text{incl}}^{\text{strains}}$ for both inclusions are slightly higher than predicted by the hydrostatic calibrations: $P_{\text{incl}}^{\text{strains}}$
338 = 183 MPa (inclusion 1) and $P_{\text{incl}}^{\text{strains}} = 191$ MPa (inclusion 2) (Fig. 5, Table S3). LdC-31C inclusion
339 1 seems to record the largest anisotropy, as shown by the difference in inclusion pressures from
340 hydrostatic calibrations. However, P_{incl}^{464} is within error of $P_{\text{incl}}^{\text{strains}}$ for all inclusions in samples
341 HF14C and LdC-31C. The difference in P_{incl} calculated from P_{incl}^{464} and from strains results in a
342 difference of < 0.07 GPa in the final calculated entrapment pressure (Tables S2, S3).

343 We can further quantify the anisotropy of the α -quartz inclusions with trigonal symmetry
344 ($\varepsilon_1 = \varepsilon_2$) by comparing strains that were determined from shifts of Raman band positions and the
345 phonon-mode Grüneisen tensor, using the equation:

$$346 \quad \Delta\varepsilon = \frac{\varepsilon_1 + \varepsilon_2}{2} - \varepsilon_3$$

347 The difference in strains ($\Delta\varepsilon$) suggests that the HF14C quartz inclusion ($\Delta\varepsilon = -0.0017$, Table S2)
348 records anisotropy similar to LdC-31C inclusion 2 (inclusion 1: $\Delta\varepsilon = -0.0034$, inclusion 2: $\Delta\varepsilon = -$
349 0.0013 , Table S3). LdC-31C inclusion 1 records the largest anisotropy, but the limitations of using
350 an isotropic elastic model and current EoS to predict the pressure evolution of this inclusion ($P_{\text{incl}}^{\text{mod}}$)
351 showing greater anisotropy can only be evaluated up to 200 °C because the heating measurement
352 was aborted when the window in the heating stage cracked (Fig. 4).

353 **Raman analyses at elevated temperature**

354 All quartz inclusions exhibited a shift of the 464 cm^{-1} band position to lower wavenumbers
355 with increasing temperature, but encapsulated inclusions exhibit less of a shift compared to Raman
356 bands of the Herkimer quartz standard analyzed at 0.1 MPa and the measurement temperature (Fig.
357 4). At elevated temperatures, we encountered difficulties in separating the quartz 464 cm^{-1} band
358 and epidote shoulder bands due to their convergence that results from the T-dependence of Raman
359 shifts and broadening of both the quartz and epidote bands with increasing temperature. The
360 convergence of quartz and epidote bands caused a significant increase in peak fit errors, resulting
361 in greater uncertainties associated with $\Delta\omega$, P_{incl}^{464} , and P_{ent}^{464} values at elevated T (Fig. 4, 6, 7). At all
362 temperatures, P_{incl}^{464} calculated from Raman measurements during heating and cooling are within
363 error (1σ), and P_{incl}^{464} errors (1σ) exceed the difference between $P_{\text{incl}}^{\text{mod}}$ (modeled) and P_{incl}^{464} ; above
364 $250\text{ }^{\circ}\text{C}$, peak fitting errors increase significantly (Fig. 6, 7B). The increase in peak fit uncertainty
365 makes it challenging to determine with confidence if the elastic model and associated EoS
366 reproduce P_{incl}^{464} at elevated temperatures.

367 Samples HF14C and LdC-31C displayed the largest increase in P_{incl}^{464} during heating. The
368 P_{incl}^{464} for sample HF14C is sufficiently low such that the quartz inclusion approaches the α - β
369 transition during heating to $600\text{ }^{\circ}\text{C}$, and hence records a large increase in P_{incl}^{464} . P_{incl}^{464} calculated from
370 measurements at elevated temperatures underestimated $P_{\text{incl}}^{\text{mod}}$ significantly at low to moderate
371 temperatures; however, the general trend of $P_{\text{incl}}^{\text{mod}}$ is matched by P_{incl}^{464} at high temperatures (Fig. 6).
372 Sample LdC-31C retains quartz inclusions with a higher P_{incl}^{464} such that during heating the α - β
373 transition temperature is significantly higher than $600\text{ }^{\circ}\text{C}$ and the trend is not influenced by the α -
374 β transition. Nonetheless, quartz inclusion (# 2) records the largest increase in P_{incl}^{464} that also
375 matches the trend of $P_{\text{incl}}^{\text{mod}}$. P_{incl}^{464} calculated from LdC-31C inclusion 1 is within error of $P_{\text{incl}}^{\text{mod}}$ up to

376 the final measurement temperature at 200 °C. Sample FT1E exhibits the smallest increase in P_{incl}^{464}
377 during heating, and P_{incl}^{464} calculated at super-ambient temperatures significantly underestimates
378 $P_{\text{incl}}^{\text{mod}}$ (Fig. 6). However, all P_{incl}^{464} values are within error (1σ) of $P_{\text{incl}}^{\text{mod}}$, owing to the high uncertainty
379 associated with peak fits of sample FT1E. The lower P_{incl}^{464} values obtained during heating likely
380 reflect an overestimation of $P_{\text{incl}}^{\text{mod}}$ by the elastic model and associated EoS, quartz anisotropy,
381 measurement and peak fitting errors, or some combination of all of these factors; therefore, we do
382 not use data from this inclusion to assess the reliability of the elastic model and EoS. It is possible
383 that the quartz inclusion from sample FT1E records more anisotropic strain, or that the least
384 thermally expansive axis of quartz is oriented parallel to the *c*-axis of epidote (maximum thermal
385 expansivity), and therefore records a nominal pressure increase. Nonetheless, based on P_{incl}^{464}
386 calculated from the lower temperature measurements of samples HF14C, LdC-31C, and FT1E (\leq
387 250 °C), our results suggest that application of the current equations of state, with an isotropic
388 elastic model, satisfactorily simulates the evolution of P_{incl} with increasing temperature for
389 anisotropic minerals (quartz and epidote).

390 **Evaluation of calculated entrapment pressures at elevated temperatures**

391 To evaluate the applicability of the elastic model and EoS for estimating entrapment
392 pressures of quartz inclusions in epidote, we calculate entrapment pressures (P_{ent}^{464}) from P_{incl}^{464}
393 derived at elevated temperatures (Fig. 7). Low P_{incl}^{464} sample HF14C showed the largest variation in
394 calculated entrapment pressures, and measurements result in lower entrapment pressures relative
395 to theoretical estimates at low temperatures. However, large uncertainties are associated with peak
396 fits from sample HF14C due to the overlap of the quartz 464 cm^{-1} band with epidote shoulder
397 bands, making peak deconvolution less robust. Likewise, sample FT1E exhibited a general

398 decrease in P_{ent}^{464} with increasing T, but the quartz 464 cm^{-1} band exhibited a strong overlap with
399 neighboring epidote bands at ambient and increasing T (Fig. 3F). Owing to these large
400 uncertainties, it is challenging to use HF14C and FT1E data to evaluate whether entrapment
401 pressure calculations require a thermal correction. We limit P_{ent}^{464} to $T \leq 250$ °C, a temperature at
402 which most errors in P_{incl}^{464} are < 0.1 GPa (Fig. 7A), to evaluate the need for a correction to P_{ent}
403 calculated at elevated T. For these measurements, entrapment pressures calculated from P_{incl}^{464} of
404 heated inclusions exhibit only small differences compared to entrapment pressures calculated from
405 $P_{\text{ent}}^{\text{mod}}$. Most inclusions exhibit a decrease in absolute P_{ent}^{464} with increasing T, but all P_{ent}^{464} values
406 remain within error (1σ) of modeled P_{ent} . We can also evaluate the difference between the mean
407 P_{ent}^{464} of all Raman analyses of a single inclusion and $P_{\text{ent}}^{\text{mod}}$. We evaluate the weighted mean of
408 Raman analyses of our analyzed inclusions by assigning a weight (ω_i) to each calculated P_{ent}^{464} that
409 considers measurement uncertainty:

$$410 \quad \omega_i = 1/\sigma_i^2$$

411 where σ_i is the 1σ error of each P_{ent}^{464} calculation (Tables S2, S3, S4). For samples HF14C, LdC-
412 31C, and FT1E, we calculate P_{ent}^{464} weighted means of 0.41 GPa, 0.79 GPa and 0.86 GPa, and 1.67
413 GPa, respectively. These values slightly underestimate, but closely approximate, calculated $P_{\text{ent}}^{\text{mod}}$
414 values of 0.49 GPa, 0.82 and 0.87 GPa, and 1.75 GPa, respectively. These observations suggest
415 that the errors introduced by associated EoS, an isotropic elastic model, and Grüneisen tensor
416 components are minimal, and that the calculated entrapment pressure is not a function of the
417 temperature at which the sample is analyzed (Fig. 7).

418 **Comparison of calculated entrapment pressures to previously reported P-T histories**

419 To assess if the quartz-in-epidote barometer provides reasonable estimates of the pressure
420 of epidote growth, we compare our results to previously determined P-T conditions for our
421 samples.

422 **Upper Schieferhuelle – Sample HF14C**

423 Sample HF14C preserves foliation parallel epidotes that appear to have crystallized pre-or-syn-
424 kinematic to fabric-forming deformation (Fig. 2A). Development of the dominant foliation (S1)
425 observed in the mafic sample is proposed to have occurred early in the metamorphic history of the
426 USH. This foliation was overprinted by static lawsonite growth in the mafic samples, and at least
427 some of the epidote is associated with subsequent breakdown of lawsonite. A subsequent shear
428 foliation subparallel to S1 is evident in the pelites, but not in the mafic rocks at the sample localities
429 (Selverstone 1985). Garnet growth in pelites occurred after lawsonite breakdown, and rotated
430 garnets indicate that they formed during development of the subparallel shear foliation (S1,
431 Selverstone 1985). Epidote inclusions are found within garnets that formed near peak T. It is thus
432 likely that matrix epidote analyzed in the mafic sample formed early, before USH rocks reach peak
433 T. The epidote analyzed from this sample encapsulates a quartz inclusion with a residual $P_{\text{incl}}^{464} = 15$
434 ± 26 (1 σ) MPa, or $P_{\text{incl}}^{\text{strains}} = 48$ MPa. Assuming an entrapment temperature of 475 °C (below peak
435 T of ~ 500 °C), we estimate entrapment pressures of 0.49 ± 0.10 (2 σ) GPa from P_{incl}^{464} and 0.55 GPa
436 from $P_{\text{incl}}^{\text{strains}}$ (Fig. 7A, Table S2). These P-T estimates likely reflect epidote growth conditions prior
437 to reaching peak T conditions, and our results are consistent with petrographic observations and
438 previously established P-T constraints; these previous P-T constraints are derived from a range of
439 thermobarometry approaches that give consistent results related to the P-T evolution of these
440 samples (cation thermobarometry, Gibbs garnet modeling, and fluid inclusion thermobarometry;
441 Selverstone and Spear 1985). It is possible that overstepping of reaction boundaries occurred

442 during formation of epidotes, but the agreement of our results with petrographic constraints and
443 independent thermobarometry suggest that overstepping did not significantly affect the P-T
444 estimates obtained here.

445 **Lago di Cignana – Sample LdC-31C**

446 Quartz inclusions 1 and 2 from sample LdC-31C retain residual pressures of $P_{\text{incl}}^{464} = 143 \pm 23$ (1 σ)
447 MPa and $P_{\text{incl}}^{464} = 175 \pm 24$ (1 σ) MPa, or $P_{\text{incl}}^{\text{strains}} = 183$ MPa and $P_{\text{incl}}^{\text{strains}} = 191$ MPa, respectively.
448 Assuming an entrapment temperature of 550 °C, we calculate an entrapment pressure of ~ 0.8 - 0.9
449 ± 0.08 (2 σ) GPa (Fig. 7A, Table S3). This estimate is much lower than the reported peak
450 metamorphic conditions of ~ 600 °C and 3.2 – 3.4 GPa (within the diamond-bearing horizon at
451 Lago di Cignana; Frezzotti et al. 2011). However, the presence of quartz inclusions in epidote is
452 clear evidence that the qtz-in-ep entrapment pressures do not record peak pressure conditions,
453 where coesite is stable. Our calculated entrapment pressures, and field and petrographic
454 relationships of epidote-fuchsite veins encased in the high-P foliation, suggests that epidote growth
455 represents an early vein formation stage that predates HP/LT metamorphism in the Lago Di
456 Cignana region or, alternatively, that the late epidote vein formed during exhumation and
457 experienced only minor deformation (Fig. 2B). Our P-T estimates for sample LdC-31C are also
458 consistent with retrograde metamorphic conditions that have been suggested by van der Klauw et
459 al. (1997) (T = 550 - 500 °C, P \approx 1.8 GPa; T = 350 – 450 °C, P \approx 0.35 – 0.55 GPa); however, our
460 samples show no evidence for extensive retrogression as represented by the preservation of HP
461 assemblages. It is most likely that the epidote vein formed during exhumation and after leaving
462 the coesite-stable field. If the epidote veins formed along the prograde path and before reaching
463 peak conditions, the epidotes would have encapsulated quartz and would traverse through the
464 coesite-stable field at peak conditions and then return to the quartz-stable region during

465 exhumation. The preservation of quartz inclusions in these epidotes would require kinetic barriers
466 to prevent formation of coesite at peak conditions or, conversely, mass conversion of coesite back
467 to quartz along the retrograde path. While this scenario is possible, it is more likely that the epidote
468 formed late, during exhumation and while P-T conditions were in the quartz stable field.

469 **Frosnitz Tal – Sample FT1E**

470 Epidotes in sample FT1E are aligned parallel to the primary foliation, suggesting pre-to syn-
471 tectonic crystallization of epidote (Fig. 2C). The quartz inclusion analyzed from sample FT1E
472 retains a residual inclusion pressure of $P_{\text{incl}}^{464} = 573 \pm 30$ (1 σ) MPa. Assuming an entrapment
473 temperature of 625 °C, our results suggest a formation pressure of 1.75 ± 0.12 (2 σ) GPa (Fig. 7A).
474 Our predicted pressure is slightly lower than previous peak P-T estimates for the Frosnitz Tal
475 eclogite zone in the Tauern Window ($T \approx 600$ °C, $P \approx 1.9 - 2.5$ GPa) (e.g., Spear and Franz 1986;
476 Selverstone et al. 1992). Epidote growth conditions are further constrained by petrographic
477 observations. Banded eclogites from the Frosnitz Tal contain epidote-zoisite pairs in apparent
478 textural equilibrium, suggesting a transformation loop at ~ 2.0 GPa, 625 °C (Selverstone et al.
479 1992). Pseudosection models of banded eclogites from Eisse (Tauern Window eclogite zone)
480 predict growth of matrix zoisite during exhumation at P-T conditions below ~ 1.9 GPa and ~ 625
481 °C (Hoschek 2007); however, pseudosections based on samples that have different bulk rock
482 compositions should be compared with caution.

483 **Corrections to the thermal component of the elastic model**

484 The agreement between P_{incl}^{464} (measured) and $P_{\text{incl}}^{\text{mod}}$ (P_{incl} predicted by elastic modeling) at
485 $T \leq 250$ °C tentatively suggests that entrapment pressures calculated from the quartz-in-epidote
486 barometer do not require a temperature-dependent correction; i.e., an empirical correction to

487 entrapment pressures (based on the estimated entrapment temperature) that accounts for elastic
488 modeling or EoS errors, is not required. We note that at $T > 250$ °C, it is more difficult to evaluate
489 the current elastic modeling approach and associated EoS, and our interpretation is limited by
490 errors associated with fitting of the quartz 464 cm^{-1} band at elevated T . Our interpretation is
491 consistent with results from the apatite-in-garnet barometer that conclude that a temperature
492 correction is not needed for apatite inclusion pressure measurements conducted at ambient
493 temperature and that are subsequently used to calculate entrapment pressures at higher
494 temperatures (Ashley et al. 2017). In comparison, previous work suggests that a temperature
495 correction is required for the qtz-in-grt barometer when the Raman 464 cm^{-1} band is used for
496 inclusion P determination (Ashley et al. 2016). These somewhat contradictory results (i.e., no
497 observed offset in measured and modeled inclusion P at elevated temperatures) are problematic,
498 given that quartz is the common inclusion phase between the qtz-in-grt and qtz-in-ep barometers.
499 P_{incl} estimates based on different quartz inclusion bands and strains are similar in this study and
500 hence, the P_{incl}^{464} and $P_{\text{incl}}^{\text{mod}}$ are similar, but significant disparities in pressures obtained from the
501 different bands are observed for quartz in garnet, suggesting significant anisotropy (Bonazzi et al.
502 2019). Perhaps the lower bulk modulus of epidote results in a smaller stress anisotropy for the
503 quartz inclusion that is not detectable with current methods. Additionally, because quartz and
504 epidote typically (re)crystallize along a schistosity during fabric development, it may be that the
505 orientation of the quartz inclusion relative to the epidote host leads to a bulk stress tensor that
506 optimally characterizes the inclusion P for the system, and in this case, the mutual orientation of
507 quartz inclusions in epidote minimizes quartz anisotropy due to the anisotropic expansion of
508 epidote during heating (Gatta et al. 2011). Furthermore, the quartz inclusion in sample FT1E may
509 record the largest anisotropy and the deviation of absolute values of P_{ent}^{464} from modeled P_{ent} may

510 be real, but we cannot fully evaluate the extent of anisotropy preserved by this quartz inclusion.
511 Regardless of the mechanism, our results lead to the following conclusions: 1) inclusion pressures
512 calculated from the hydrostatic calibration of the quartz 464 cm^{-1} Raman band shifts (not valid for
513 high anisotropic strain), yield nearly constant entrapment pressures (within uncertainty),
514 independent of the temperature at which the inclusion is analyzed; and 2) allowing for errors
515 introduced by modeling of entrapment pressures, our results suggest that the 1D-isotropic model
516 is appropriate for modeling the elastic behavior of these two anisotropic phases, and no further
517 correction is required for calculation of final entrapment pressures.

518 **Quartz-in-epidote barometry limitations**

519 A major limitation of the quartz-in-epidote barometer is related to the convergence of the
520 464 cm^{-1} Raman band of quartz (and other quartz bands) and the epidote shoulder bands as
521 temperature is increased, causing peak overlap and requiring deconvolution to fit the quartz band.
522 However, robust peak fits can be applied to most standard Raman measurements made at ambient
523 T, wherein the peak overlap is less significant because the separation between the quartz 464 cm^{-1}
524 band and epidote shoulder bands is larger. Elastic thermobarometry requires robust determination
525 of positions of multiple bands to calculate strains and to account for anisotropy (Murri et al. 2018,
526 2019; Angel et al. 2019); however, epidotes contain many bands that overlap with quartz bands,
527 especially those near 128 cm^{-1} , 206 cm^{-1} , and 464 cm^{-1} . To minimize uncertainties associated with
528 fitting quartz peaks, sufficiently high quartz inclusion Raman intensities may be achieved by
529 rotating samples to analyze quartz inclusions in different orientations. **Different epidote and quartz**
530 **bands will reach maximum intensities at different orientations due to the orientation-dependent**
531 **polarizability of mineral vibrational modes (Raman band positions will not change), but an**
532 **orientation that makes the quartz Raman bands dominant can minimize peak fitting uncertainties.**

533 Additionally, the Raman spectra of epidotes may be subtracted from the convolved Raman spectra
534 of quartz and epidote to obtain a pure quartz Raman spectrum, but this would require careful
535 evaluation. Choosing samples from high-P rocks that preserve quartz with high residual P_{incl} , may
536 also limit overlap of quartz bands (e.g., 464 cm^{-1}) with high intensity epidote bands near $\sim 425 \text{ cm}^{-1}$
537 and 455 cm^{-1} . For high-T/low-P samples, convergence of the 464 cm^{-1} quartz band may not allow
538 separation of the quartz and epidote bands via deconvolution, perhaps limiting application of qtz-
539 in-ep barometry to epidote crystals that have entrapped quartz under moderate to high pressure
540 conditions. Further analyses using epidotes from magmatic systems or skarns that have well
541 constrained P-T histories might help better understand the limitations of the technique.

542 We emphasize that our approach does not allow us to fully evaluate the reliability of the
543 calculated entrapment pressures because we cannot demonstrate that reactions that produce epidote
544 were not significantly overstepped. **The importance of overstepping will depend on the relationship**
545 **of the qtz-in-ep isomekes and the slope (dP/dT) of the epidote-in reaction line. Because qtz-in-ep**
546 **isomekes are nearly flat, if the epidote-in reaction line is flat ($dP/dT = 0$) or vertical ($dT/dP = 0$),**
547 **the effect of T is minimal. Between these extremes overstepping may become important, and will**
548 **depend on the relative slopes of the qtz-in-ep isomekes and reaction line, and the P-T path of the**
549 **rock.** Furthermore, we cannot unambiguously determine if the final P_{ent}^{464} of sample FT1E is
550 affected by quartz anisotropy; therefore, we advise that the uncertainties that we report for the
551 entrapment pressures below be applied with caution. In spite of these concerns, the relatively good
552 correlation between pressure determined here and P-T estimates and petrographic, field, and
553 petrologic studies of the same areas provides confidence that the qtz-in-ep barometer provides
554 reasonable pressure estimates in some cases. Future recommended studies would include
555 comparing qtz-in-ep pressure estimates with additional samples that have good field, petrographic,

556 and independent thermobarometry constraints, with modeled reactions that include both epidote
557 and quartz as product phases, and/or synthesis experiments of quartz inclusions in epidote (e.g.,
558 Thomas and Spear, 2018; Bonazzi et al., 2019).

559 **Final comments and implications**

560 This work highlights the potential of the qtz-in-ep barometer to constrain formation
561 conditions of epidote, and also highlights some of the obstacles and uncertainties associated with
562 implementing this barometer. The qtz-in-ep barometer was evaluated for moderate to high-P
563 metamorphic rocks, but can potentially be applied to understand formation conditions of other
564 geologic processes that include epidote-bearing skarn formation, epidote growth in ore deposits,
565 epidote-bearing granitoid rocks, hydrothermal alteration of oceanic crust, and growth conditions
566 of epidote in metamorphic rocks from convergent margins. Although entrapment pressures
567 calculated from the qtz-in-ep barometer are in general consistent with previous estimates for the
568 samples studied, further work is needed to document the accuracy and reliability of entrapment
569 pressures (e.g., synthesis experiments, or detailed petrographic studies that integrate reaction
570 modeling). Nevertheless, qtz-in-ep entrapment pressures of samples from the Frosnitz Tal eclogite
571 zone in the Tauern Window and the Upper Schieferhuelle in the Western Tauern are in general
572 agreement with previously-established P-T conditions. Qtz-in-ep entrapment pressures of samples
573 from Lago di Cignana indicate vein epidote crystallization below maximum pressure conditions
574 of the area (diamond stability field). The presence of quartz inclusions suggests that the qtz-in-ep
575 barometer records P-T conditions that are not in the diamond stability field, due to the lack of
576 coesite, and highlights how field and petrographic observations can be combined with the
577 barometer to better constrain cryptic stages of P-T histories. Furthermore, results of our analyses
578 at various temperatures suggest that a temperature-dependent entrapment pressure correction is

579 not required, contrary to what has been noted for the qtz-in-grt barometer. Therefore, this work
580 suggests that Raman measurements of quartz inclusions in epidote taken at ambient conditions can
581 be used to calculate high-temperature entrapment pressures without applying temperature
582 corrections (for quartz inclusions preserving near isotropic strains). Our results further highlight
583 the importance of integrating data from mineral geobarometers with field and petrographic
584 observations that document the relative timing of various mineral formation and deformation
585 events to constraint P-T conditions associated with development of distinct structural and textural
586 fabrics.

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598 **Figure Captions**

599 **Figure 1.** (a) Schematic illustration of the evolution of a host phase (e.g., epidote) and an inclusion
600 (e.g., quartz) during exhumation, and the residual pressure (P_{incl}) retained by a quartz inclusion at
601 ambient T (modified from Guiraud and Powell 2006; Befus et al. 2018). Models of the P-T
602 dependence of P_{incl} for quartz in (b) epidote, (c) clinozoisite, and (d) zoisite. Models vary over the
603 range of $P_{\text{incl}} = -0.2$ GPa to 0.8 GPa (0.1 GPa intervals) and from 400 °C – 800 °C. Models show
604 that P_{incl} is nominally affected by the assumed entrapment temperature. Dependence of entrapment
605 pressure (e) and temperature (f) on the mol fraction (X_{ep}) of Al-Fe monoclinic epidote at T = 500
606 °C and P = 1 GPa, respectively. At low P_{incl} , the composition of epidote minimally affects the final
607 entrapment pressure or temperature. At higher P_{incl} , the final entrapment pressure and temperature
608 are more dependent on X_{ep} . Regions in grey denote conditions at which P_{incl} is below 0 GPa,
609 wherein quartz preserves a tensile stress.

610 **Figure 2.** Photomicrographs of thin sections showing the petrographic relationships of epidotes
611 analyzed in this study. (a) HF14C: foliation parallel epidote grains suggest that epidote likely grew
612 prior to or during deformation associated with formation of the primary foliation. (b) LdC-31C:
613 analyzed epidotes are from a vein that has an irregular, undulating contact with the primary
614 foliation. The petrographic relations suggest that epidote crystallized prior to formation of the
615 HP/LT foliation, or during exhumation. This fabric and the presence of quartz inclusions and lack
616 of coesite suggests that the epidotes record formation pressures below high-pressure conditions
617 where coesite is stable. (c) FT1E: epidote grains aligned parallel to foliation, suggesting that
618 crystallization occurred prior to, or during, the formation of the primary foliation.

619 **Figure 3.** Raman spectra of epidotes (a) R060284 ($X_{\text{ep}} = 0.30$) and (b) R050131 ($X_{\text{ep}} = 0.76$) from
620 the RRUFF database, and Raman spectra of all samples at ambient conditions and their associated

621 peaks after fitting. (a, b) Raman spectra of epidotes are shown in two epidote orientations (red and
622 blue lines) over the wavenumber region 380-540 cm^{-1} . (c, d, e, f) Shown in circles are the Raman
623 spectra, the dashed blue line is the fit to the Raman spectra, and solid lines indicate the peaks used
624 to fit the quartz 464 cm^{-1} band (red), epidote bands (grey), and the 520.3 cm^{-1} Ar-plasma line
625 (blue).

626 **Figure 4.** Raman shifts of the quartz (inclusion) 464 cm^{-1} band for the three samples measured
627 during heating measurements. All samples display a decrease in wavenumber with increasing
628 temperature. Relative to the position of the 464 cm^{-1} band of Herkimer quartz measured at ambient
629 pressure, all inclusions exhibit a smaller change in the Raman shift of the quartz 464 cm^{-1} band
630 due to an increase in inclusion pressure with increasing temperature. The solid black line is derived
631 from the reference polynomial equation for the change in Raman shift of Herkimer quartz at 0.1
632 MPa and analysis T (Ashley et al. 2016). The dashed line is the linear extrapolation of the
633 polynomial equation used to correct Raman shifts from samples LdC-31C and FT-1E relative to
634 Herkimer quartz at measurement conditions. Error bars are propagated errors from instrument
635 uncertainty, and errors associated with fitting quartz 464 cm^{-1} bands and the Ar plasma line.
636 Symbols represent the following samples: FT1E (yellow diamond), LdC-31C inclusion 1 (grey
637 circle), LdC-31C inclusion 2 (red circle) HF14C (blue square). White (open) symbols represent
638 measurements made during cooling.

639 **Figure 5.** Comparison of P_{incl} calculated from the hydrostatic calibration of Raman shifts of quartz
640 128 cm^{-1} , 206 cm^{-1} , and 464 cm^{-1} bands, and P_{incl} calculated from strains. Yellow circles, red
641 squares, and blue diamonds are the $P_{\text{incl}}^{\text{strains}}$ vs. P_{incl}^{464} , P_{incl}^{206} vs. P_{incl}^{464} , and P_{incl}^{128} vs. P_{incl}^{464} values,
642 respectively. P_{incl} for sample LdC-31C (inclusion 2) is calculated at 23.7 °C and 23.8 °C. The

643 dashed line shows where P_{incl} calculated from different bands and strains would have the same
644 values (1:1 line).

645 **Figure 6.** Inclusion pressures (P_{incl}^{464}) calculated from Raman analyses conducted during heating
646 (symbols), compared to the P_{incl} evolution predicted by elastic modeling ($P_{\text{incl}}^{\text{mod}}$). The dashed lines
647 represent $P_{\text{incl}}^{\text{mod}} - P_{\text{incl}}^{464}$ errors (1σ) show the increase in error with increasing temperature. The error
648 exceeds the difference between P_{incl}^{464} and $P_{\text{incl}}^{\text{mod}}$. Symbols represent the following samples: FT1E
649 (yellow diamond), LdC-31C inclusion 1 (grey circle), LdC-31C inclusion 2 (red circle) HF14C
650 (blue square). White (open) symbols are the measurements made during cooling.

651 **Figure 7. (a)** Entrapment pressures calculated from P_{incl}^{464} determined from Raman shifts of quartz
652 inclusions during heating (relative to a quartz crystal at 0.1 MPa and measurement T), and
653 comparison with model estimates of the temperature-dependence of entrapment pressure (solid
654 lines). Transparent colored lines bound errors of entrapment pressure estimates ($\pm 2\sigma$). **(b)**
655 Reference P-T conditions for samples FT1E and HF14C (grey boxes) and our estimated qtz-in-ep
656 barometry entrapment pressures are shown for comparison. See text for discussion of the reference
657 P-T conditions. Symbols represent the following samples: FT1E (yellow diamond), LdC-31C
658 inclusion 1 (grey circle), LdC-31C inclusion 2 (red circle) HF14C (blue square). White (open)
659 symbols represent measurements made during cooling.

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- 838

Table 1. Abbreviations used in this manuscript

Abbreviation	Definition
$\omega_{\text{std}}^{464}$	Wavenumber position of the quartz 464 cm^{-1} band of a standard at a measurement T
$\omega_{\text{incl}}^{464}$	Wavenumber position of the quartz 464 cm^{-1} band of an inclusion at a measurement T
$\Delta\omega_{\text{shift}}^{464}$	$\Delta\omega_{\text{shift}}^{464} = \omega_{\text{incl}}^{464} - \omega_{\text{std}}^{464}$
P_{incl}^{128}	Inclusion pressure calculated from the hydrostatic calibration of the quartz 128 cm^{-1} band
P_{incl}^{206}	Inclusion pressure calculated from the hydrostatic calibration of the quartz 206 cm^{-1} band
P_{incl}^{464}	Inclusion pressure calculated from the hydrostatic calibration of the quartz 464 cm^{-1} band
$P_{\text{incl}}^{\text{strains}}$	Inclusion pressure calculated from strains
$P_{\text{incl}}^{\text{mod}}$	Inclusion pressure predicted by elastic modeling (Fig. S1B)
P_{ent}^{464}	Entrapment pressure calculated from P_{incl}^{464}
HF14C	Sample from Upper Schieferhuelle
LdC-31C	Samples from Lago di Cignana
FT1E	Sample from Frosnitz Tal

Table 2. Thermodynamic and Physical Properties of Clinozoisite, Epidote, and Zoisite

Phase	V_0 ($\text{cm}^3 \text{mol}^{-1}$)	α_0 (10^5K^{-1})	κ_0 (GPa)	κ_0'	κ_0'' $\kappa_0'' = -\kappa_0'/\kappa_0$	S_0 ($\text{J mol}^{-1} \text{K}^{-1}$)	θ_E K
Clinozoisite	138.1(4)‡	2.24(6)*	147(2)‡	4.0‡	-0.0027	301 [■]	528.58
Epidote	138.06(9)†	2.25(3)†	115(2)†	6.7(5)†	-0.0058	315 [■]	512.38
Zoisite	135.80**	3.12**	104.4**	4.00**	-0.0038	298 [■]	532.19

All thermodynamic properties are given at standard state: 0.1 MPa, 298 K.

Einstein temperature (θ_E) is calculated from $\theta_E = 10636/(S_0/n_i + 6.44)$, where n_i is the number of ato

Reference P-V-T data from which thermodynamic properties are calculated:

‡Qin et. al, 2016 ($X_{\text{Ep}} = 0.39$), data fit with the Tait 2nd-order EoS.

*Pawley et. al, 1996 ($X_{\text{Ep}} = 0.02$), data fit with the Tait 2nd-order EoS and thermal pressure.

†Gatta et al., 2011 ($X_{\text{Ep}} = 0.74$), data fit with the Tait 3rd-order EoS and thermal pressure.

**Holland and Powell, 2011, Tait 2nd-order EoS and thermal pressure.

References from which thermodynamic and physical properties are derived:

■Holland and Powell, 2011.

ˆMao et al., 2007.

v (poisson ratio)	G (GPa)
0.26*	84.0
0.26*	65.7
0.26*	59.7

ms in epidote or zoisite (22).

Figure 1

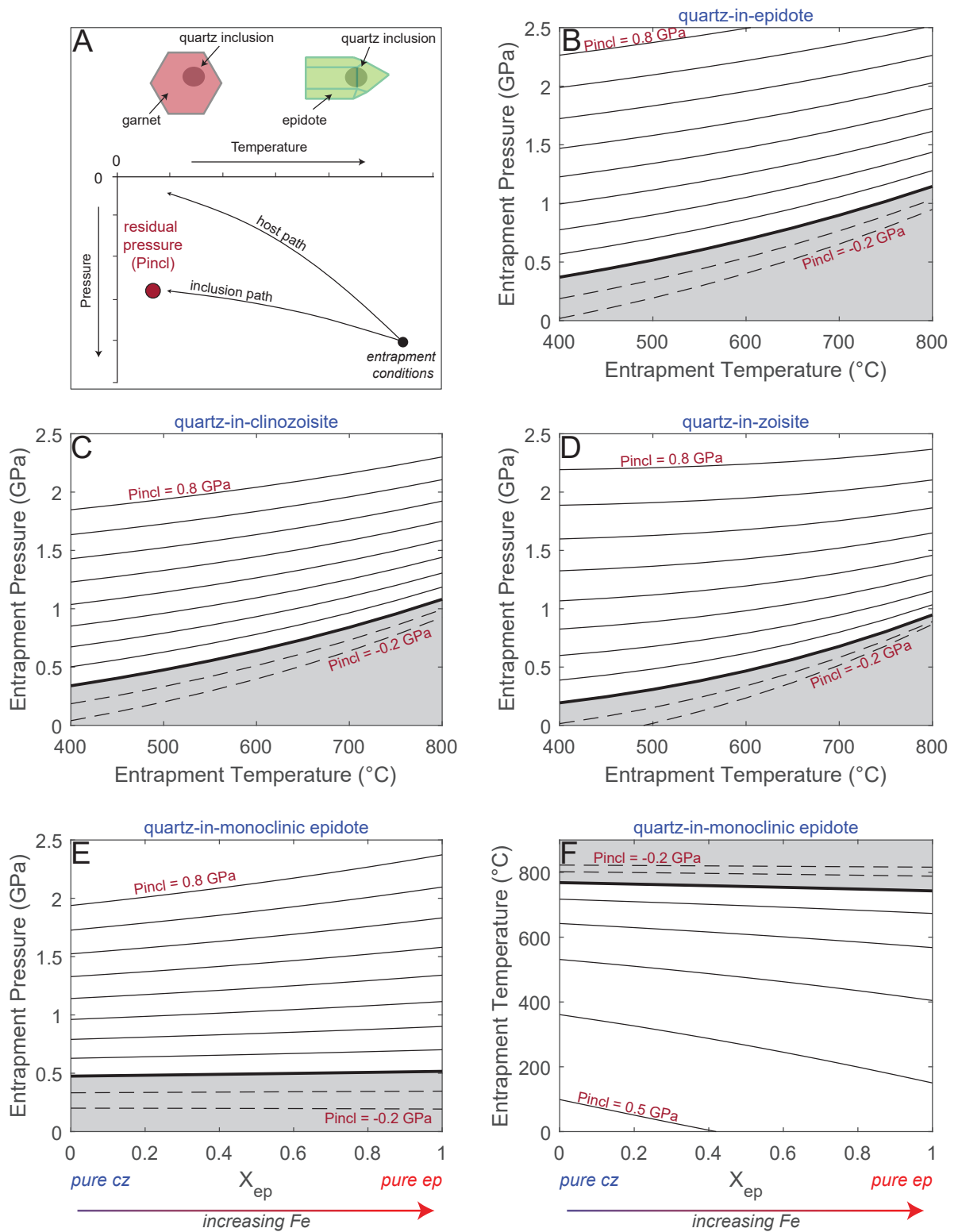


Figure 2

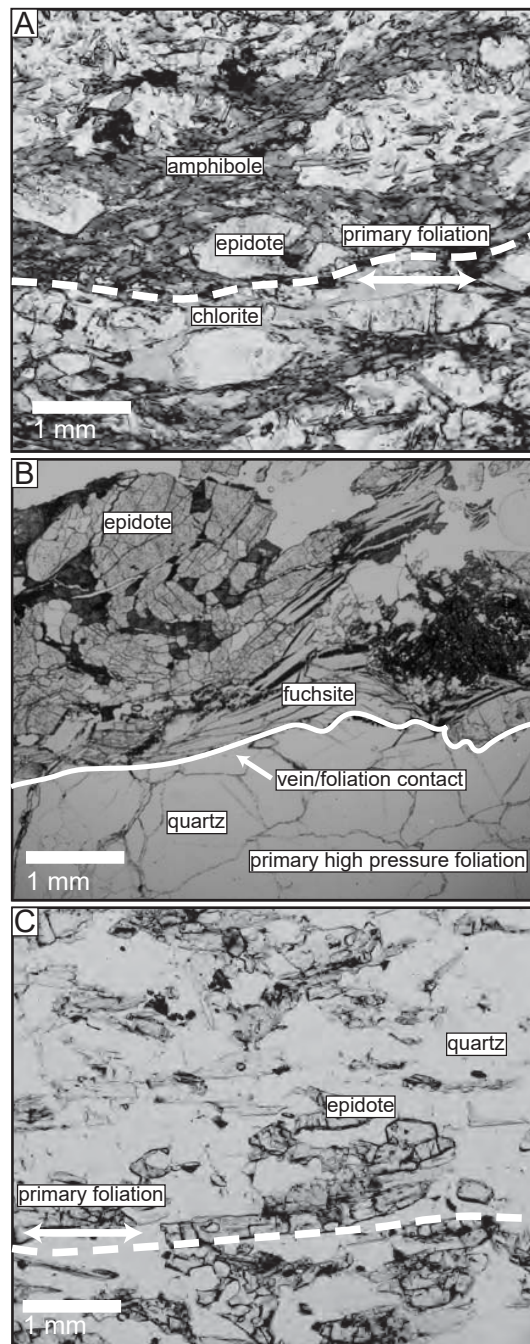


Figure 3

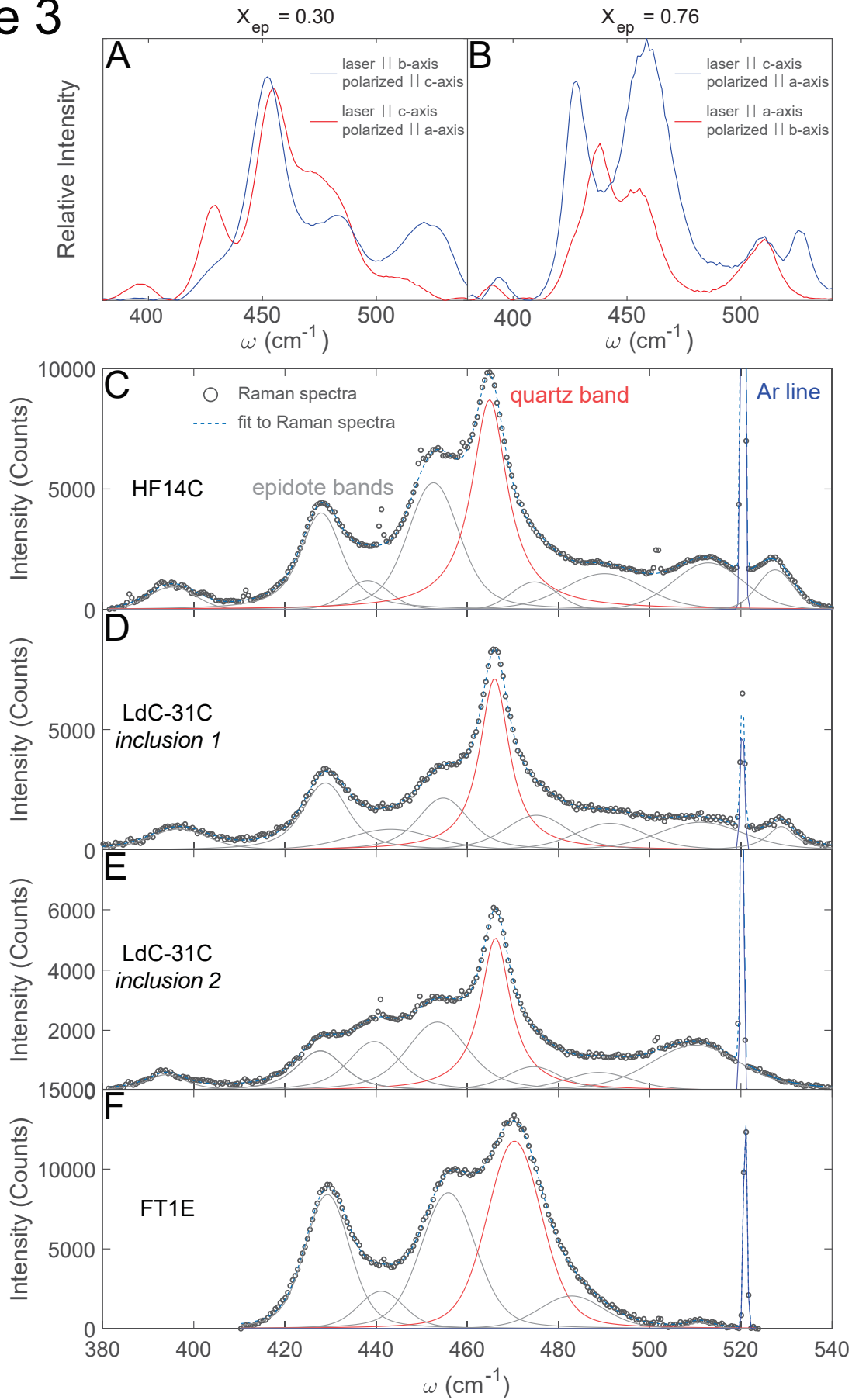


Figure 4

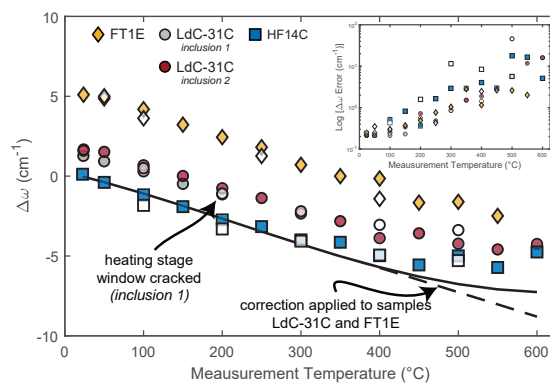


Figure 5

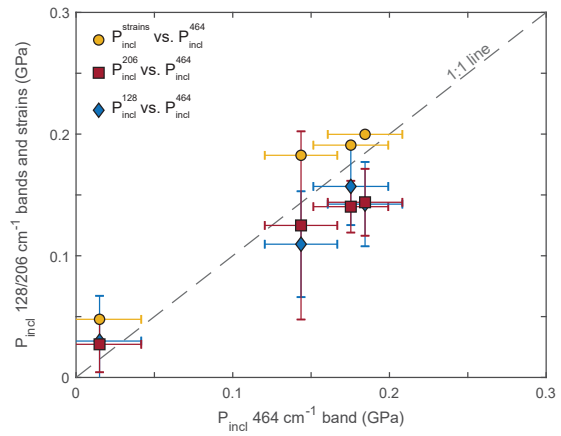


Figure 6

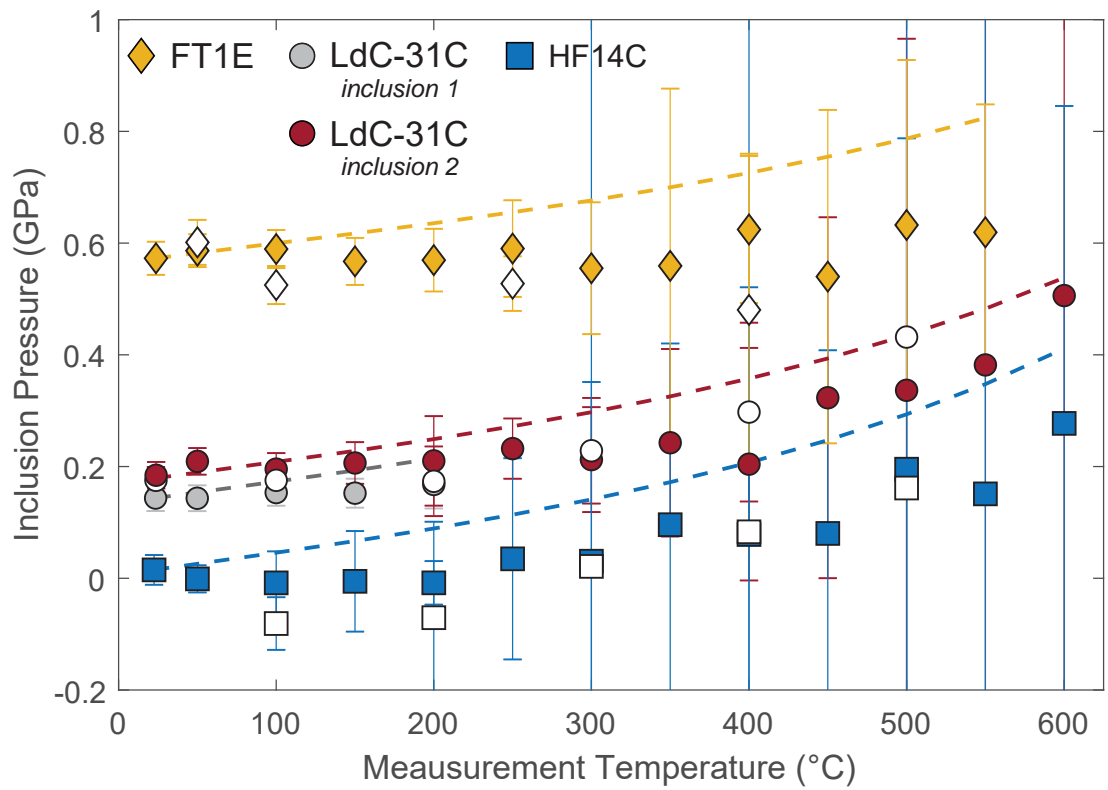


Figure 7

