1	Revision 1
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3	EXCALIBR to EXCELIBR and the Optical Orientation of Minerals: Correcting the Optical Orientation of
4	Clinoamphiboles.
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8	
9	Abstract
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11	The crystallographic orientation of $C 2/m$ amphiboles has been depicted incorrectly since the
12	standardization of amphiboles in $C 2/m$ . Texts citing the early optical work on amphiboles reference structures
13	drawn in the $I 2/m$ cell, for which the optical orientation is correct. When $C 2/m$ became the standard space group,
14	the optical orientation, (hkl), and crystallographic axes depicted in crystal form drawings were never revised. Using
15	the methods outlined by Gunter and Twamley (2001) combined X-ray and optical methods on single crystals of
16	amphiboles reveal the discrepancy between axes. In the correct orientation of a typical $C 2/m$ amphibole, the
17	physical optical orientation should have never changed from its position outlined in the Tschermak setting as shown
18	in Ford and Dana (1932), however, the crystallographic axes and (hkl) should have changed to accommodate the
19	difference between the $I 2/m$ cell and the $C 2/m$ cell. This error may perpetuate a misunderstanding between the
20	crystallographic setting and optical orientation of clinoamphiboles, which is an important relationship for
21	orientation-dependent analytical methods. Enclosed in this study is the correction of crystallographic axes for crystal
22	form drawings for $C 2/m$ amphiboles, along with an outline of methodology and updates to the spreadsheet
23	EXCELIBR. The methods applied in this study utilize relationships between crystallographic and optical vectors and
24	include an addendum to those presented by Gunter and Twamley (2001), which is applicable to arbitrary reference
25	positions on spindle stages.
26	Keywords: optical orientation, clinoamphiboles, crystallographic setting, EXCELIBR, EXCALIBR
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31	Introduction
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33	Inconsistencies in the crystallographic settings of minerals could be a source of confusion when
34	depicting crystal form drawings, such as those found in Nesse (2013), Deer et al. (2013), and Tröger and Bambauer
35	(1979). Many of the crystal depictions are based on data collected during, or even prior to the early years of X-ray
36	crystallography. Discrepancies in the optical orientation of minerals may be due one of two circumstances. The first,
37	is rearrangement of the orientations of the crystallographic axes <b>a</b> , <b>b</b> , and <b>c</b> since the original characterization of the
38	optical and crystallographic axes. This scenario is unlikely to lead to errors in the literature since the old choice of
39	axes were inherited to suit the space group of the X-ray structure solution. An example of this is with forsterite,
40	where space group is Pbnm, though if forsterite was solved under the current standards, the space group would be
41	<i>Pnma</i> , which would be the same cell as <i>Pbnm</i> , but with the definition of <b>b</b> and <b>c</b> switched. The second, is the use of
42	an entirely different lattice from the original characterization of the mineral. This scenario is far more likely to result
43	in discrepancies, particularly with monoclinic and triclinic minerals, since the original axes may have been selected
44	prior to X-ray diffraction, and there can be multiple similar lattices centered in different orientations. In the case of
45	mesolite, its structure was originally solved in $C2$ , and since the two-fold axis of monoclinic minerals must be the <b>b</b> -
46	axis, b corresponded with Y optical vector, which was also parallel to the long-axis of the form of the crystal (Deer
47	et al. 1967). Later, mesolite was solved in larger cell but of higher metric symmetry, which was in the Fdd2 space
48	group where $\mathbf{a} = X$ , $\mathbf{b} = Z$ , $\mathbf{c} = Y$ (Gunter and Ribbe 1993).
49	In the case of $C 2/m$ clinoamphiboles, originally, two crystallographic settings were used to denote the
50	symmetrical relationships between crystal faces. Though this is a correction of the optical orientation of
51	clinoamphiboles, it is important to note that the error is in the depiction of their crystallographic setting.
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53	Methods
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55	Crystallographic orientation was collected with a single crystal X-ray Diffractometer (SC-XRD) using a
56	Bruker SMART XRD system with an APEX1 detector (Bruker 2014). Diffraction data were processed and indexed

57 for lattice type and orientation with the Apex3 software suite. Principal optical vectors were located using the 58 spindle stage methods, along with the program EXCELIBR (Bloss 1981; Steven and Gunter 2017). The method 59 used to relate crystallographic axes collected on the SC-XRD to the coordinate system used on the polarized light 60 microscope (PLM) is outlined by Gunter and Twamley (2001). To summarize, the orientation matrix of a C 2/m cell 61 in reciprocal space is converted to the direct orientation for the **a**, **b**, and **c** axes by taking the cross-product of the 62 orthonormal reciprocal axes to the direct crystallographic axes:  $\mathbf{a} = \mathbf{b}^* \times \mathbf{c}^*$ ,  $\mathbf{b} = \mathbf{b}^*$ ,  $\mathbf{c} = \mathbf{a}^* \times \mathbf{b}^*$ . An accurate 63 orientation matrix is listed in the Apex3 software suite after integrating X-ray frames and is also written into the p4p 64 file. The cartesian coordinates for **a**, **b**, and **c** on the SC-XRD are then transformed to match their coordinates in the 65 system used on the PLM. The correct transformation of coordinates is verified with orthorhombic minerals, where 66 the optical vectors coincide with the crystallographic axes. 67 68 **EXCELIBR** 69 70 EXCELIBR is a Microsoft Excel spreadsheet that determines the orientation of the optical indicatrix of 71 crystals on a spindle stage using numerical methods, like those used in the program EXCALIBR (Steven and Gunter 72 2017). The version of EXCELIBR used in this research is designed to locate crystallographic axes and optical 73 vectors on the same crystal, using spindle stage methods and SC-XRD. The current version of EXCELIBR includes 74 new calculations to relate principle optical vectors and crystallographic axes, particularly for those of monoclinic 75 minerals (Figure 1). Previous versions of EXCALIBR and EXCELIBR output spherical coordinates, cartesian 76 coordinates, and a stereogram of the location of axes to orient principle vibration directions either North-South, or 77 East-West with lower polarizer. However, the cartesian plot depends on the readout convention of both the PLM 78 stage, and the spindle stage or whether the numbers increase clockwise, or counterclockwise. Though the readout 79 convention of the PLM stage is accommodated for in EXCALIBR and previous versions of EXCELIBR, the spindle 80 stage readout is not. This does not affect the alignment of vectors East-West or North-South, but it does affect the 81 cartesian output of where vectors lie in space. The new standard output of EXCELIBR plots vectors in direct space, 82 and outputs cartesian coordinates in direct space, which depends on whether the PLM stage readout increases 83 clockwise or counterclockwise, and if the spindle stage increases clockwise or counterclockwise when viewing 84 towards the goniometer mount surface. This feature eliminates one potential step when converting the X-ray

85	coordinate system to the PLM coordinate system, since not all spindle stage readouts increase clockwise.
86	EXCELIBR also only plots upper hemisphere vectors, so it will project any lower hemisphere vectors to the upper
87	hemisphere, and will rename axes accordingly (i.e., a lower hemisphere <b>a</b> -axis will be projected as - <b>a</b> in the upper
88	hemisphere). EXCELIBR and its supplemental guide is available in the Mineralogical Society of America's
89	Monographs page.
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91	Converting Coordinate Systems
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93	As mentioned above, the cartesian coordinates of the SC-XRD are converted to match the coordinate
94	system used on the PLM. Specifically, the cartesian basis runs in the orientation shown in Figures 2a and 2b. The
95	goniometer mount for the PLM stage is depicted in the zero position for both the spindle axis and PLM stage. At the
96	zero position, a reference notch is denoted relative to the cartesian basis and resembles the line from the spindle axis
97	to the mount pin as the long line, and direction the goniometer points at zero as the short line. This is to
98	accommodate differences in the location of the notch on the spindle stage, since the notch position may be
99	adjustable or manufactured differently among spindle stages. The goniometer mount for the SC-XRD is in the
100	mount position, which reads zero for 2 $\theta$ , $\phi$ , and $\omega$ , but with a fixed $\chi$ of 54.8°. The reference notch on the SC-XRD
101	is shown in the restored zero position on the SC-XRD relative to the cartesian basis. In this instance, after
102	superimposing the reference notches of the PLM and SC-XRD, the conversion to the basis of the PLM is $x = -z$ , $y =$
103	-y, z = -x.
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105	Methods of Locating Crystallographic Axes on a Spindle Stage
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107	In addition to locating crystallographic axes by transforming SC-XRD coordinates, crystallographic axes of
108	some monoclinic minerals may also be located using the spindle stage. For example, with monoclinic amphiboles, a
109	crystallite is commonly elongate on the line of the c-axis. However, for a randomly oriented crystal on a spindle
110	stage, it is challenging to discern when the long axis of the crystal is in the plane of the stage when viewing in the
111	PLM, and therefore, true orientation of the c-axis is challenging to find. One solution is to find any two intersecting
112	planes that do not intersect the c-axis, $(hk0)$ , $(0k0)$ , or $(h00)$ . The cross-product of any two planes that do not

113 intersect the c-axis will intersect along a vector that is parallel to the c-axis, and in the case of tremolite-114 ferroactinolite amphiboles, the optic normal is the orthogonal vector to the optic axial plane which is parallel to 115 (010), so indexing any (hk0) or (0k0) results in the solution of **c** in EXCELIBR (Figure 3). In the example from 116 Figure 3, the c-axis is parallel with the (hk0), even though it is tilted down out of the plane of the stage. After 117 indexing the (hk0) from Figures 3 and 4a, the cross product of the coordinates of the optic normal and the orientation 118 of the (hk0) results in the calculated orientation that will align the c-axis East-West and in the plane of the stage 119 (Figure 4b). Calculations for the method outlined above are contained within the program EXCELIBR (Steven and 120 Gunter 2017).

After locating the c-axis, EXCELIBR will solve for the **b**-axis by taking the cross-product of c and each of the principle vibration directions. With monoclinic minerals, two of the cross-products will be the same orientation and thus will be the **b**-axis. In the case of tremolite-ferroactinolite amphiboles,  $Z \times c = X \times c$ , and therefore,

124 b = Y.

125 The remaining axis to find is **a**, and, admittedly, the **a**-axis of clinoamphiboles cannot be directly located 126 with the spindle stage methods, since there is no plane of reference in a crystallite for the **a**-axis. However, since the 127 **a**-axis also lies in the orthogonal plane to **b**, the **c**-axis can be rotated by the common  $\beta$  angle of amphiboles of 128 104.7° along the optic axial plane. Then, the problem is that the rotation direction is unknown. At this point, the 129 method would then rely on crystal form drawings for where the **a**-axis should be relative the optical vectors and the 130 **b** and **c**-axes. In the published crystal form drawings of amphiboles in the tremolite-ferroactinolite series, the **a**-axis 131 is  $\sim 104.7^{\circ}$  from c and normal to b rotated towards Z, as is depicted in Figure 5. When rotated in this way, the **a**-axis 132 of the C 2/m XRD orientation does not align with the spindle stage orientation solution. However, when rotated the 133 opposite direction, shown in Figure 6, the a-axis closely coincides with the SC-XRD orientation solution, which is 134 what is given for the spindle stage orientation solutions for actinolite samples given in Table 1. The probable 135 explanation for this inconsistency, is that the crystallographic setting depicted in crystal form drawings of 136 clinoamphiboles, have drawn the crystallographic axes and (hkl) in the I 2/m setting, despite listing C 2/m as the 137 space group. This would mean that Tschermak's setting is parallel to the I 2/m setting which is closely related to the 138 axes used for C 2/c pyroxenes (Figures 5 and 7). 139 The results of this method are compared to the X-ray orientation for **a**, **b**, and **c** with a residual angle to

140 demonstrate the efficacy of the method. For the clinopyroxene samples, the same method was applied to locate the a

141	and <b>c</b> -axes which matches the x-ray orientation. For the orthopyroxene sample, the <b>a</b> , <b>b</b> , and <b>c</b> -axes coincide with
142	the optical vectors, so the crystallographic axes on the spindle stage were directly located by the optical solution.
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144	Crystal Form
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146	Since the discrepancy in clinoamphiboles is in the crystal axes, nothing changes in the crystal form of
147	amphiboles, however, the labeling of some of the ( <i>hkl</i> ) is different. In a typical clinoamphibole, the crystal form is a
148	prism terminated by a clinodome, which is formed by the r faces Figure 8. Note that the setting of axes for
149	clinopyroxene and clinoamphibole in Figure 8 are drawn parallel and are both labelled in their respective Tschermak
150	settings. In the Tschermak setting, the r faces are (011) and p face is (-101) (Ford and Dana 1932). In the alternate
151	setting, the r face is (-111) and the p face is (001) (Ford and Dana 1932). Experimentally, a growth crystal of a
152	tremolite was selected to verify the crystal faces with the SC-XRD, and the clinodome was found to be terminated
153	by (-111) and (-1-11) shown in Figure 9.
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155	Discussion
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157	The combined use of the spindle stage methods, and SC-XRD used in conjunction with EXCELIBR allow
158	for an unambiguous determination of the location of optical vectors, and crystallographic vectors for a particular
159	lattice setting. These methods may be used to check the crystallographic settings of minerals, and orient crystals for
160	orientation-dependent analytical methods. The spindle stage methods outlined in the research offer a convenient way
161	of locating optical vectors and reference axes based on crystal morphology, which also establishes handedness for
162	the reference axes of monoclinic crystals. The discrepancy in the crystallographic axes of monoclinic amphiboles,
163	likely stems from the adoption of the $I 2/m$ lattice setting.
164	The choice of axes for monoclinic amphiboles dates back to the work of Tschermak in the late 1800s,
165	before X-ray crystallography (Tschermak 1897). Tschermak's setting is one of two crystallographic settings used in
166	the early years of crystallography for amphiboles and is perhaps the easiest setting to visualize with the common
167	crystal form of amphiboles, shown in Figure 8. However, Ford and Dana (1932) noted that some authors used an
168	alternate setting where the p crystal face is marked as (001) rather than (-101) in the Tschermak setting (Ford and

169 Dana 1932). In the Tschermak setting, clinopyroxenes and clinoamphiboles are indexed so that their crystal axes and 170 crystal faces coincide. Later, Warren (1929) published the first X-ray structure solution for a monoclinic amphibole, 171 which was for tremolite. The structure was solved in the I 2/m space group with an acute  $\beta$  angle, which was used so 172 that the crystallographic axes, relative to the structure, would coincide with the crystallographic axes of diopside, 173 also with an acute  $\beta$  angle, solved in C 2/c (Warren and Bragg 1928). The choice of axes for C 2/c pyroxenes is 174 depicted in Figure 8, which is the setting parallel to those used by Tschermak, and besides a 180° rotation of the **b** 175 and a-axes, the obtuse  $\beta$  setting, the axes as used by Warren and Bragg has not changed for C 2/c pyroxenes since 176 (Warren and Bragg 1928). 177 One discrepancy of the setting of clinoamphiboles, is in Strunz (1966), where the lattice of clinoamphibole 178 is stated to be C 2/m, yet the Tschermak setting is adopted. As stated above, relative to their structures, the C 2/c179 lattice setting of clinopyroxenes is parallel to the I 2/m lattice of clinoamphiboles, which coincides with the 180 Tschermak setting. Whittaker and Zussman (1961) had discussed the relationship between the I 2/m of 181 clinoamphibole, and the C 2/c of clinopyroxene, as well as the confusion surrounding the choice of axes for 182 clinoamphibole since both lattices setting share similar cell parameters. Figure 10 depicts the relationship between 183 the I and C monoclinic lattice settings as described by Whittaker and Zussman. Despite this, several authors adopted 184 the Tschermak setting, presuming the axes were parallel to the axes of the C 2/m lattice setting. Since about 1961, 185 clinoamphiboles have all been solved in C 2/m, which currently used as the standard centered monoclinic lattice. 186 Inconsistencies in crystallographic settings in reference literature are a demonstrable source of confusion if 187 Bravais lattice is not listed with the set of axes depicted. With accurate reference material, the methods listed above 188 allows a user to obtain the full crystallographic orientation of a C 2/m amphibole just by knowing orientation of the 189 c-axis and optical vectors. These relationships are helpful when orienting a large number of crystals for analytical 190 methods that depend on orientation, which is particularly useful if SC-XRD is not available. 191 Beyond the clinoamphiboles, inconsistencies in settings may still exist in depictions of other minerals. 192 Mesolite would have benefitted from investigating the optical setting as a possible crystallographic setting, since 193 principle optical vectors work as a reliable set of reference vectors for a crystal, though their orientation may depend 194 on composition in monoclinic and triclinic crystals. In contrast, the optical setting for scolecite deviates from any 195 translational lattice with orthogonal axes, and therefore the optical setting informs that the crystal system must be 196 monoclinic or triclinic. In one crystallographic setting, scolecite is nearly face-centered orthorhombic, belonging to

197	the nonstandard monoclinic F1d1 lattice. When processing SC-XRD data from scolecite, the crystal would appear to
198	be face-centered orthorhombic until scaling the data, where large discrepancies in supposed symmetrically
199	equivalent intensity maxima arise. Additionally, when relating the orientation of the principle optical vectors to the
200	axes to the pseudo-orthorhombic cell, it is clear that the <b>b</b> -axis corresponds with the Z optical vector (Figure 11c),
201	while the X and Y optical vectors don't correspond with the other axes of the lattice, suggesting a monoclinic lattice.
202	Further, for crystallographers solving scolecite in the Cc space group, the correct C monoclinic lattice must be
203	centered for the best refinement results, since multiple C-centered monoclinic lattices can be centered to a crystal
204	that is nearly face-centered orthorhombic (Figure 11).
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206	Implications
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208	The methods listed above were compiled for projects involving orientation-dependent spectroscopic
209	methods, though they are also useful for rectifying inconsistencies in crystallographic settings in compilation
210	reference material. The relationship between the principal optical vectors and crystallographic axes are extremely
211	important for orientation-dependent spectroscopic methods, since anisotropic absorption behavior of light may be, in
212	part, analogous to anisotropic behavior of other wavelengths of electromagnetic radiation, such as visible light (Dyar
213	et al. 2002). For example, an X-ray absorption spectrum will depend on several variables including, bond
214	characteristics and chemical speciation, but importantly, will depend on the orientation of the vibration path of the
215	photon source through an anisotropic crystal. Therefore, in empirical studies of XANES spectra of mineral series, an
216	effort must be made to compare like-orientations. Anisotropic diffusion of halogens in apatite during Electron Probe
217	Microanalysis (EPMA) is a known source of analytical error in halogen count rate per beam exposure time (Stormer
218	et al. 1993). This can be partially mitigated by preparing oriented mounts such that the polished surface runs parallel
219	to the (100) plane of apatite, rather than the (001) plane, where there is more variation in count rate per beam
220	exposure time. The optical and crystallographic orientation of minerals mounted on a spindle stage allows a user to
221	prepare oriented grains or grain mounts of crystals for spectroscopic analysis. The updated version of EXCELIBR
222	includes calculations for relating crystallographic and principle optical vectors of crystals from single crystal X-ray
223	data and extinction data, which can be used for characterizing new minerals, or for minerals where the relationship
224	between the optic indicatrix and crystallographic vectors is unknown.

225	Acknowledgements
226	We are grateful for support from NASA grant 80NSSC19K1008 and NSF grants EAR-1754261 and EAR-
227	1754268.
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273	Figure Captions
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275	Figure 1: EXCELIBR tab for locating optical vectors and crystallographic axes of monoclinic minerals. The output
276	is for actinolite1, and includes the inputs in blue, and the output location of crystallographic axes using spindle stage
277	methods, optical orientation, and transformed X-ray orientation. The cartesian coordinates and plot are given in real
278	space so that the coordinate system of a SC-XRD can be directly converted to the microscope coordinate system.
279	
280	Figure 2: (a) Cartesian coordinate basis used on a SC-XRD. This example is of a fixed $\chi$ goniometer, and reference
281	notch is drawn in the restored zero position for the diffractometer. The reference notch resembles the line from the $\phi$
282	axis to the mount pin as the long line, and direction the goniometer points as the short line in the restored zero
283	position. (b) The goniometer mount for the microscope stage depicted at the zero position for the spindle axis and
284	microscope stage. The reference notch is positioned relative to the cartesian basis and resembles the line from the
285	spindle axis to the mount pin as the long line, and direction the goniometer points at zero as the short line.
286	
287	Figure 3: Representation of the clinoamphibole actinolite1 mounted on a spindle stage. For actinolite, the
288	intersection of the optic axial plane, and an ( <i>hk</i> 0) forms a vector parallel to the <b>c</b> -axis. Indexing any two intersecting
289	( $hk0$ ), ( $0k0$ ), or ( $h00$ ) may be used to locate <b>c</b> , for example, the (110) cleavage planes.
290	
291	Figure 4: (a) Microscopic view of actinolite1 of the position in Figure 3. An ( <i>hk</i> 0), (0 <i>k</i> 0), or ( <i>h</i> 00) is indexed by
292	aligning the <b>c</b> -axis with the N-S crosshair even if it is plunging into the plane of the microscope stage. ( <b>b</b> ) The
293	calculated position of the c-axis aligned E-W and in the plane of the microscope stage after taking the cross product
294	of an $(hk0)$ and the coordinates of the optic normal, which is equivalent to $(0k0)$ for actinolite.
295	
296	<b>Figure 5:</b> A stereogram, crystal structure, and crystal form of the <i>I</i> 2/ <i>m</i> setting of a clinoamphibole. The stereogram
297	and crystal form drawing depict (hkl), crystallographic axes, and optical vectors. Optical vectors are drawn in an
298	orientation similar to that of a typical tremolite. The internal crystal structure (solution from Warren, 1929) is drawn
299	viewing down the <b>b</b> -axis using the CrystalMaker software and, relative to their structures, is oriented in line with the
300	clinopyroxene structure in Figure 7.

301	<b>Figure 6:</b> A stereogram crystal structure and crystal form of a $C 2/m$ amphibole in the tremolite ferroactinolite
202	Tighte 6. A stereogram, crystal structure, and crystal form of a C 2/m ampinoole in the tremone remote the
302	series. The stereogram and crystal form drawing depict ( <i>hkl</i> ), crystallographic axes, and optical vectors. Optical
303	vectors are drawn in an orientation similar to that of a typical tremolite. The internal crystal structure (solution from
304	Cameron and Gibbs 1973) is drawn viewing down the <b>b</b> -axis using the CrystalMaker software, and, relative to their
305	structures, is oriented in line with the clinopyroxene structure in Figure 7.
306	
307	Figure 7: A stereogram, crystal structure, and crystal form of C 2/c pyroxenes. Optical vectors are drawn in an
308	orientation similar to that of a typical diopside. The stereogram and crystal form drawing depict (hkl),
309	crystallographic axes, and optical vectors. The internal structure (solution from Mottana et al. 1979) was drawn in
310	CrystalMaker, and, relative to their structures, is oriented in line with the clinoamphiboles from Figures 5 and 6.
311	
312	Figure 8: The common crystal form of clinopyroxene with faces labeled in lettering form, axes and Miller indices
313	denoted using the C monoclinic lattice (left) and clinoamphibole with faces labeled in lettering form, axes and
314	Miller indices denoting faces in the Tschermak I monoclinic lattice setting (right).
315	
316	Figure 9: Image of a portion of a growth crystal of tremolite. Crystal faces are indexed in the Apex3 software after
317	collecting the unit cell. The full growth crystal was cleaved in half on (110) for experimental purposes. The crystal is
318	a tremolite sample from Gouverneur talc mine, New York, and corresponds to the sample name actinolite2 in Table
319	1. Outside of the (110) cleavage face in the back, the crystal is bounded by growth faces and clinodome is
320	terminated by (1-1-1) and (11-1).
321	
322	Figure 10: Depiction of the relationship between the centering of the C monoclinic lattice in bold, and the I
323	monoclinic lattice shaded in grey with axes denoted by subscripts for the C and I lattice settings, modified after
324	Whittaker and Zussman (1961).
325	
326	Figure 11: Stereograms depicting the orientation solution for a scolecite crystal in a) the F1d1 lattice b) an incorrect
327	monoclinic C lattice centering where no optical vector corresponds with a crystallographic axis and c) the correct Cc
328	lattice where $b = Z$

# **329** Tables and Figures

- **Table 1:** Tables of the converted XRD coordinates and the spindle stage coordinates of an orthopyroxene,
- 332 clinopyroxene, and five clinoamphiboles. The spindle stage coordinates for the **a**-axis and **c**-axis of the monoclinic
- 333 minerals are located using the method outlined in the text, and the difference in the coordinates are given as an angle
- 334 on the right. The consistency in the orientations demonstrate the efficacy of relating crystallographic vectors
- between the spindle stage methods and X-ray orientation solution. Discrepancies for clinopyroxenes tend to be
- 336 larger due to its high dispersion, which influences extinction measurements and ultimately the orientation
- determined from the optical solution.
- 338

orthopyroxene1										
	X-ray Orio	entation			Spindle St	age Orienta	tion	discrep	ancy (de	grees)
	-a	-b	-c		-a	-b	-с	-a	-b	-с
Х	-0.2099	0.4383	0.8740	х	-0.2091	0.4437	0.8714	1.0	1.1	0.8
У	0.0580	0.8979	-0.4364	У	0.0402	0.8943	-0.4457			
Z	0.9760	0.0408	0.2139	Z	0.9771	0.0581	0.2048			

clinopyroxene1										
	X-ray Ori	entation			Spindle St	age Orienta	tion	discrep	ancy (de	grees)
	-a	b	-c		-a	b	-с	-a	b	-с
х	0.6061	0.0780	-0.9311	х	0.5911	0.0027	-0.9413	2.4	4.4	4.4
У	-0.4386	0.8630	-0.1159	у	-0.4126	0.8603	-0.1700			
Z	0.6635	0.4992	0.3459	Z	0.6931	0.5098	0.2918			

clinopyroxene2										
	X-ray Orio	entation			Spindle St	age Orienta	tion	discrep	ancy (de	grees)
	а	-b	-c		а	-b	-с	а	-b	-c
х	-0.1807	-0.1462	-0.9841	х	-0.1776	-0.1833	-0.9777	3.4	3.7	2.5
У	-0.2228	0.9693	-0.1629	У	-0.2801	0.9513	-0.2028			
Z	0.9580	0.1978	0.0707	Z	0.9434	0.2480	0.0550			
_				_						

actinolite1										
	X-ray Orie	entation			Spindle St	age Orienta	tion	discrep	ancy (de	grees)
	-a	b	-c		-a	b	-c	-a	b	-с
х	-0.2999	-0.52	0.85	х	-0.3138	-0.5290	0.8427	2.4	2.8	1.1
У	0.95358	-0.19	-0	У	0.9471	-0.2324	-0.0268			
Z	0.02756	0.83	0.53	Z	0.0670	0.8162	0.5378			

	X-ray Orientation				Spindle Stage Orientation				discrepancy (degrees)		
	-a	-b	с		-a	-b	с	-a	-b	c	
Х	0.6448	-0.3191	0.8367	х	0.6906	-0.3266	0.7994	3.9	0.8	4.1	
У	0.7260	-0.0287	-0.4778	У	0.6781	-0.0178	-0.5386				
Z	0.2392	0.9473	0.2674	z	0.2514	0.9450	0.2661				

actinolite3										
	X-ray Orientation				Spindle St	discrepancy (degrees)				
	-a	b	-c		-a	b	-c	-a	b	-c
Х	0.2868	-0.2866	0.8108	х	0.3024	-0.3085	0.7947	0.9	1.5	1.8
У	0.9572	0.0469	-0.5201	У	0.9524	0.0607	-0.5320			
Z	0.0390	0.9569	0.2684	Z	0.0374	0.9493	0.2923			

actinolite4										
	X-ray Orientation				Spindle St	discrepancy (degrees)				
	-a	-b	-c		-a	-b	-c	-a	-b	-с
Х	-0.1205	-0.3085	-0.9433	х	-0.1356	-0.2947	0.9494	2.6	2.3	1.6
У	-0.6550	0.7389	-0.3189	У	-0.6848	0.7180	0.2952			
Z	0.7459	0.5990	0.0925	Z	0.7160	0.6306	0.1076			

actinolite5

	X-ray Orientation				Spindle Stage Orientation				discrepancy (degrees)		
	-a	b	-c		-a	b	-c	-a	b	-с	
х	-0.4598	-0.4326	0.8667	х	-0.4735	-0.4444	0.8557	0.9	1.5	1.2	
у	0.2620	-0.9005	-0.4021	У	0.2552	-0.8956	-0.4173				
Z	0.8485	0.0436	0.2953	Z	0.8430	0.0215	0.3060				



















