

1 **Investigation of the kieserite–szomolnokite solid solution series, (Mg,Fe)SO<sub>4</sub>·H<sub>2</sub>O, with**  
2 **relevance to Mars: a study on crystal chemistry, FTIR- (5200–400 cm<sup>-1</sup>) and Raman- (4000–**  
3 **100 cm<sup>-1</sup>) spectroscopy under ambient and Martian temperature conditions**

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5 **Revision 1**

6

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12

13 **Abstract**

14

15 The investigation of hydrous sulfate deposits and sulfate-cemented soils on the surface of  
16 Mars is one of the important topics in the recent scientific endeavor to retrieve detailed  
17 knowledge about the planetary water budget and surface weathering processes on our neighbor  
18 planet. Orbital visible/near-IR spectra of the Martian surface indicate kieserite, MgSO<sub>4</sub>·H<sub>2</sub>O, as a  
19 dominant sulfate species at lower latitudes. However, given the Fe-rich composition of the  
20 Martian surface, it is very probable that its actual composition lies at an intermediate value along  
21 the solid solution series between the kieserite and szomolnokite (FeSO<sub>4</sub>·H<sub>2</sub>O) endmembers.  
22 Despite the known existence of significant lattice parameter changes and spectral band position  
23 shifts between the two pure endmembers, no detailed crystal chemical and spectroscopic  
24 investigation along the entire kieserite–szomolnokite solid solution range has been done yet.

25           The present work proves for the first time the existence of a continuous kieserite–  
26 szomolnokite solid solution series and provides detailed insight into the changes in lattice  
27 parameters, structural details, and positions of prominent bands in FTIR- (5200–400  $\text{cm}^{-1}$ ) and  
28 Raman- (4000–100  $\text{cm}^{-1}$ ) spectra in synthetic samples as the Fe/Mg ratio progresses, at both  
29 ambient as well as Mars-relevant lower temperatures. Additionally, an UV-Vis-NIR (29000–  
30 3500  $\text{cm}^{-1}$ ) crystal field spectrum of szomolnokite is presented to elucidate the influence of  $\text{Fe}^{2+}$ -  
31 related bands on the overtone- and combination mode region.

32           The kieserite–szomolnokite solid solution series established in this work shows Vegard-  
33 type behavior, i.e., lattice parameters as well as spectral band positions change along linear  
34 trends. The presented detailed knowledge of these trends enables useful semi-quantitative  
35 estimations of the Fe/Mg ratio that can be applied to interpret Martian monohydrated sulfates in  
36 data from remote sensing missions on a global scale as well as from in-situ rover measurements.  
37 Given the knowledge of the surface temperature during spectral measurements, the established  
38 temperature behavior allows quantitative conclusions concerning the Fe/Mg ratio. Our  
39 understanding of the kieserite–szomolnokite solid solution series will be well applicable to the  
40 Mars 2020 and ExoMars 2020 rover missions that will focus on near IR (0.9 to 3.5  $\mu\text{m}$ ) and, for  
41 the first time on Mars, Raman spectroscopy.

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43 **Keywords:** Kieserite–szomolnokite solid solution, Mars mineralogy, crystal chemistry, FTIR  
44 spectroscopy, Raman spectroscopy, UV-Vis-NIR spectroscopy

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## Introduction

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51 The surprising discovery of large amounts of sulfate minerals on the Martian surface dates

52 from the late 1970s, when Viking landers carried out the first in-situ analyses of Martian soils.

53 Using X-ray fluorescence spectroscopy, the presence of diverse Mg- and Ca-dominated sulfate

54 salts was anticipated, in addition to NaCl (Keil et al. 1978; Clark and Van Hart 1981). The

55 sulfates are presumed to originate from acidic weathering of basaltic rock-forming minerals such

56 as olivine and pyroxene, which are believed to contain significant amounts of Fe (Christensen et

57 al. 2004; Schröder et al. 2004; Morrison et al. 2018). Further in-situ measurements of the soil

58 composition confirming sulfates took place at Meridiani Planum and Gusev crater using data

59 from the APXS (Alpha Particle X-ray Spectrometer), Mössbauer instrument, and the Mini-TES

60 (Miniature Thermal Emission Spectrometer) on the Opportunity and Spirit rovers (landed in

61 2004). The terrain at Meridiani Planum consists of bright, layered sediments cemented by various

62 sulfates – interpreted to be predominantly kieserite,  $\text{MgSO}_4 \cdot \text{H}_2\text{O}$ , and jarosite, perhaps also

63 minor bassanite, thenardite and some halite (Clark et al. 2005). They extend across vast regions of

64 Meridiani Planum (Christensen et al. 2004; Clark et al. 2005; Glotch et al. 2006) as well as

65 adjacent areas of Terra Meridiani (Arvidson et al. 2005). The formation of the sulfates and the

66 cementation of the sediment by them is believed to have been caused by percolating underground

67 water or sulfate-rich brines with partial contribution from overland flow or body of water

68 (Christensen et al. 2004). However, Knauth et al. (2005) suggest that the observed sedimentary

69 structures could also be ascribed to impact surges from a large nickel-iron meteorite. Papike et al.

70 (2007) note that especially kieserite, via partial Fe-, Ni-, or Co-incorporation, could be an

71 indicator for meteorite impacts as relevant processes in the formation and redistribution of

72 sulfates on Mars.

73           On a global Martian scale, WEH (Water-Equivalent Hydrogen) maps and OMEGA  
74 (Observatoire pour la Minéralogie, l'Eau, les Glaces et l'Activité) data indicate variable, low (in  
75 comparison with higher latitudes), but still significant amounts of water bound in minerals and  
76 buried water ice in the equatorial regions ranging up to 10 wt% (Feldman et al. 2004; Milliken et  
77 al. 2007), despite instability of the latter under the prevailing surface conditions. In general, the  
78 data suggest that sulfates of varying hydration state, including kieserite, probably represent the  
79 dominant water reservoir and also play a key role in the sulfur cycle at lower (<45°) and  
80 equatorial Martian latitudes. (Feldman et al. 2004; Milliken et al. 2007; Gendrin et al. 2005;  
81 Bishop et al. 2009; Karunatillake et al. 2014; Noel et al. 2015; Mangold et al. 2008; Roach et al.  
82 2010; Lichtenberg et al. 2010). OMEGA spectra confirmed surficial accumulations of hydrous  
83 sulfates (including kieserite) in various regions within Valles Marineris and elsewhere, spatially  
84 correlated with layered terrains (Gendrin et al. 2005). High-resolution CRISM (Compact  
85 Reconnaissance Imaging Spectrometer for Mars) data offer a more detailed insight into the  
86 stratigraphy of such layered sulfate deposits in Juventae Chasma (Bishop et al. 2009; Noel et al.  
87 2015) and West Candor Chasma. In the latter case, Mangold et al. (2008), considering MOLA  
88 data (Mars Orbiter Laser Altimeter), found potential indications for kieserite being the primary  
89 sulfate cementing the layered terrains, since it is dominant on steeper slopes, while higher sulfate  
90 hydrates prevail on the flatter regions where the eroded primary material accumulates and  
91 partially rehydrates. Large sulfate deposits with kieserite are known to occur in Ius Chasma  
92 (Roach et al. 2010) and Aram Chaos (Lichtenberg et al. 2010), which possibly formed by  
93 evaporation of a surface body of water.

94           Given these finds, as well as the long-term knowledge of the Martian soil containing many  
95 Fe-rich phases investigated in greater detail by Dyar and Schaefer (2004) and Dyar et al. (2013),  
96 it is very probable that the actual composition of Martian monohydrated sulfates will represent

97 various intermediate species along the binary join between kieserite and the isotypic Fe  
98 endmember szomolnokite,  $\text{FeSO}_4 \cdot \text{H}_2\text{O}$ , given their partial or complete miscibility. Despite  
99 reference data having been obtained from the kieserite and szomolnokite endmembers, showing  
100 significant shifts of the spectral features and lattice parameters (Chio et al. 2007; Lane 2007;  
101 Lane et al. 2015), no detailed investigation of the crystal chemical and spectral characteristics  
102 along the entire kieserite–szomolnokite solid solution series was done so far. However, the  
103 structural and crystal chemical evolution along the continuous kieserite–cobaltkieserite solid  
104 solution series,  $(\text{Mg},\text{Co})\text{SO}_4 \cdot \text{H}_2\text{O}$ , was recently investigated by Bechtold and Wildner (2016),  
105 indicating that complete miscibility might also be expected for the  $(\text{Mg},\text{Fe})\text{SO}_4 \cdot \text{H}_2\text{O}$  system.

106 In this paper, we present the results of detailed structural, crystal chemical, FTIR and  
107 Raman spectroscopic investigations on synthetically prepared members along the kieserite–  
108 szomolnokite binary solid solution,  $\text{Mg}_{1-x}\text{Fe}_x\text{SO}_4 \cdot \text{H}_2\text{O}$ , at ambient and lower temperatures, as  
109 relevant for Mars surface conditions, complemented by UV-Vis-NIR crystal field spectra of  $\text{Fe}^{2+}$   
110 in szomolnokite. The presented data may prove invaluable in further refining the chemical  
111 composition of Martian monohydrated sulfates based on available remote sensing data in the  
112 mid-infrared range, as well as be a fundamental dataset for interpreting future in-situ data from  
113 forthcoming Mars rovers, in particular data from the SuperCam (Wiens et al. 2017a, 2017b) and  
114 SHERLOC (Scanning Habitable Environments with Raman & Luminescence for Organics &  
115 Chemicals; Beegle et al. 2014) instruments onboard the Mars 2020 rover (NASA) and the RLS  
116 (Raman Laser Spectrometer; Rull et al. 2017; Rull 2018) and ISEM (Infrared Spectrometer for  
117 ExoMars; Dobrolenskiy et al. 2017) instruments onboard the ExoMars 2020 rover (ESA).

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## Experimental

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## 121 **Sample preparation**

122 The hydrothermal technique was used to synthesize crystalline material with a pre-adjusted  
123 Mg/Fe ratio along the kieserite–szomolnokite solid solution using Teflon-lined stainless steel  
124 autoclaves with an inner volume of  $\sim 55 \text{ cm}^3$ . Each autoclave was filled with  $\text{MgSO}_4 \cdot 7\text{H}_2\text{O}$  and  
125  $\text{FeSO}_4 \cdot 7\text{H}_2\text{O}$  amounting to 6 g in total, to obtain a specific Mg/Fe ratio in the resulting crystals;  
126  $\text{H}_2\text{SO}_4$  ( $w = 0.73$ ) was added as solvent. All reagents were of analytical grade. Initial problems  
127 regarding partial oxidation of  $\text{Fe}^{2+}$  to  $\text{Fe}^{3+}$ , leading to the formation of unwanted phases as well  
128 (e.g., rhomboclase and other  $\text{Fe}^{3+}$  or mixed  $\text{Fe}^{2+}/\text{Fe}^{3+}$  sulfates) required the use of a redox buffer.

129 In a first series of buffered synthesis runs, a foil of metallic iron (dimensions  $3 \times 10 \times 1$   
130 mm) was used, with the addition of  $25 \text{ cm}^3 \text{ H}_2\text{SO}_4$  ( $w = 0.73$ ). Despite the positive effect of the  
131 foil leading to  $(\text{Mg,Fe})\text{SO}_4 \cdot \text{H}_2\text{O}$  forming as practically the sole product, a part of the metal  
132 dissolved in the acid, causing the crystals to be significantly enriched in Fe relative to the pre-set  
133 Mg/Fe ratio. Hence, these synthesis attempts were stopped after the Mg-dominant batch runs in  
134 favor of the preferred use of 5 ml  $\text{H}_2\text{SO}_3$  ( $w = 0.06$ ) as the redox buffer instead, added along with  
135  $20 \text{ cm}^3 \text{ H}_2\text{SO}_4$  ( $w = 0.73$ ) as solvent, in all subsequent experiments for the full range of Mg/Fe  
136 ratios.

137 The filled hydrothermal autoclaves were placed into a programmable furnace and heated at  
138 a rate of  $50 \text{ }^\circ\text{C/h}$  to  $210 \text{ }^\circ\text{C}$ . Following a holding time of 24 hours to ensure complete dissolution  
139 of the contents, a cooling rate of  $3 \text{ }^\circ\text{C/h}$  down to room temperature was applied. After decantation  
140 of the acid and mechanical removal of the solids from the reaction vessel, the product was  
141 washed twice with distilled  $\text{H}_2\text{O}$ , taking advantage of the relatively slow dissolution rate of the  
142 sulfate monohydrates. Following a twofold washing process using 98% ethanol to remove  $\text{H}_2\text{O}$   
143 from the previous step, the product was dried in an oven at  $65 \text{ }^\circ\text{C}$  overnight. The resulting  
144 colorless to light beige material was stored in airtight vials. Microscopic inspection showed the

145 batches to consist predominantly of fine crystals (10–50  $\mu\text{m}$ ) and crystal aggregates, with  
146 sporadic larger individuals (up to  $\sim 300\mu\text{m}$ ), the latter revealing dipyramidal habit and  
147 pronounced sectoral or polysynthetic twinning.

148 To our surprise, the crystals, as long as they are free of residues of the parent solution, are  
149 stable in air over long time scales (years to decades; even original crystals of  $\text{FeSO}_4 \cdot \text{H}_2\text{O}$  from  
150 the syntheses of Wildner and Giester 1991 are still preserved), with only close-to-endmember  
151  $\text{MgSO}_4 \cdot \text{H}_2\text{O}$  slowly transforming to higher hydrates.

152

### 153 **Chemical analyses and powder X-ray diffraction**

154 Wet-chemical analyses were done on a part of each sample batch at the Masaryk University  
155 in Brno, Czech Republic. An amount of  $\sim 0.5$  g of ground sample material was dissolved in  
156 boiling  $\text{HNO}_3$  ( $w = 0.65$ ). Contents of Mg and Fe were both determined by atomic absorption  
157 analysis (instrument Solaar M5 - TJA solutions, measurement time 4 s per element) with an  
158 analytical error of 0.005 wt% for Mg and 0.002 wt% for Fe.

159 A further part of each sample batch was examined using powder X-ray diffraction. The  
160 material was pressed onto an Si-holder and measured on a Philips PW 3710 diffractometer  
161 (measuring interval 5– $120^\circ 2\theta$  in  $0.2^\circ$  increments, measuring time of 15 s per step). The Bruker  
162 EVA 2013 software with its database was used for the preliminary phase identification, then  
163 Rietveld refinements using the Bruker program TOPAS3 were performed to confirm expected  
164 lattice parameter shifts and the mono-phase character of the solid solutions.

165

### 166 **Single crystal X-ray diffraction**

167 Hand-picked single crystals suitable for X-ray diffraction measurements were obtained by  
168 crushing crystal aggregates and choosing fragments with homogeneous extinction under crossed

169 polars. The crystal structures of ten representatives of the  $\text{Mg}_{1-x}\text{Fe}_x\text{SO}_4\cdot\text{H}_2\text{O}$  solid solution series,  
170 including the szomolnokite endmember, were determined from single-crystal X-ray diffraction  
171 data, measured at 295 K with graphite-monochromatized  $\text{MoK}\alpha$ -radiation on a Nonius Kappa  
172 CCD diffractometer equipped with a 0.3 mm monocapillary X-ray optics collimator. Complete  
173 Ewald spheres up to  $2\theta = 80^\circ$  were each collected in several sets of  $\varphi$ - and  $\omega$ -scans with  $2^\circ$   
174 rotation per CCD frame, at a crystal to detector distance of 30 mm. The integration and correction  
175 of the intensity data, including an absorption correction by multi-frame scaling and the  
176 refinement of lattice parameters, were done with the program DENZO-SMN (Nonius 1998).

177       Temperature-dependent X-ray data collections of the kieserite and szomolnokite  
178 endmembers were performed between +40 and  $-160^\circ\text{C}$  in steps of 40 K on a Bruker ApexII  
179 diffractometer equipped with a CCD area detector and an Incoatec Microfocus Source  $\text{I}\mu\text{S}$  (30  
180 W, multilayer mirror,  $\text{Mo-K}\alpha$ ), in a dry stream of nitrogen (Cryostream 800, Oxford  
181 Cryosystems). Several sets of  $\varphi$ - and  $\omega$ -scans with  $2^\circ$  scan width were measured at a crystal-  
182 detector distance of 40 mm up to  $80^\circ 2\theta$  full sphere. Absorption was corrected by evaluation of  
183 multi-scans. For the sake of data consistency, the lattice parameters extracted from the ApexII  
184 temperature-dependent measurements were corrected in such a way that their interpolated values  
185 at  $20^\circ\text{C}$  match those obtained from the Nonius Kappa CCD room temperature measurements of  
186 the very same two endmember crystals.

187       All structure refinements were performed on  $F^2$  with SHELXL-97 (Sheldrick 2008) in the  
188 ‘traditional’ non-reduced kieserite cell setting. Scattering curves for neutral atoms were used. The  
189 Mg/Fe ratios of the particular single crystals studied were extracted as a refined variable in the  
190 respective structure refinement runs.



191 CIF data for room temperature structures included in Tables 2 and 3 (plus CIF of  
192 endmember kieserite from Bechtold and Wildner 2016) and of all temperature-dependent  
193 structure investigations have been deposited with the submission at the MSA website.

194

### 195 **IR spectroscopy**

196 A part of each sample batch in powdered form and beforehand characterized by wet-  
197 chemical and powder X-ray diffraction analyses (see above) was used to conduct FTIR  
198 measurements in transmission, ATR (Attenuated Total Reflectance) and DRIFT (Diffuse  
199 Reflectance Infrared Fourier Transform) modes by means of the Bruker Tensor 27 FTIR  
200 spectrometer (Global light source, KBr beam splitter, DTGS detector). For transmission  
201 measurements, the sample material was diluted in KBr at a weight ratio of 1:300 and pressed into  
202 pellets in a vacuum press. ATR measurements were done using the mountable Bruker ATR unit  
203 by pressing the sample powder against the diamond surface. For DRIFT measurements, the  
204 powder was pressed into the sample holder of a Perkin–Elmer DRIFT unit. Finely ground MgO  
205 was used as the reflectivity standard for the background measurements. All reflectance data were  
206 corrected via the Kubelka-Munk equation implemented in the Bruker OPUS software. The full  
207 wavenumber range ( $7000\text{--}400\text{ cm}^{-1}$ ) was investigated in all analytical modes with a spectral  
208 resolution of  $4\text{ cm}^{-1}$  ( $2\text{ cm}^{-1}$  spectral sampling). Each spectrum was averaged from 50 scans to  
209 reduce noise. For the DRIFT analyses, each sample was measured in pure state, as well as diluted  
210 with KBr in a ratio of 1:20, to enhance the absorption contribution to the resulting spectrum.

211 Low-temperature FTIR transmission measurements were done using a Linkam FTIR600  
212 cooling stage equipped with KBr windows. KBr micropellets (2 mm diameter, sample dilution  
213 ratio 1:300) with the material pressed into the aperture of a steel gasket were used for these  
214 investigations. The metal gasket along with the small sample volume ensured easy handling and

215 swift thermal conductivity between the Ag-block of the cooling stage and the sample.  
216 Measurements were done in 40 K intervals ranging from 313 K (40 °C) down to 113 K (–160  
217 °C). Some additional measurements at 93 K (–180 °C) could be done occasionally.

218

### 219 **Raman spectroscopy**

220 Raman spectra were measured on a Horiba Jobin Yvon LabRam–HR spectrometer,  
221 equipped with an Olympus BX41 optical microscope. A diffraction grating with 1800  
222 grooves/mm and the 633 nm laser were used. The system is equipped with a Si-based, Peltier-  
223 cooled charge-coupled device (CCD) detector. A 100× objective (NA = 0.55) was selected for all  
224 room-temperature measurements. The wavenumber accuracy was better than 0.5 cm<sup>-1</sup>, and the  
225 spectral resolution was determined to be ~0.3 cm<sup>-1</sup>. The room-temperature Raman spectra were  
226 acquired between 100–4000 cm<sup>-1</sup> shift, using multi-window scans with a counting time of 50 s  
227 per window and repeating every scan twice to eliminate spikes.

228 Low-temperature Raman measurements were conducted using the Linkam FTIR 600  
229 cooling stage. Single crystals were placed on the Ag-block covered with a thermal conducting  
230 fluid. The use of single crystals instead of powdered material was essential, despite the inherent  
231 problems due to varying and unknown crystal orientation, as only single-crystal material allowed  
232 short-enough measuring times to prevent excessive ice buildup on the sample surface. The bulky  
233 stage necessitated the use of a long-distance 50× objective, with otherwise the same setup of the  
234 Raman instrument. The spectra were acquired in two separate spectral regions, i.e., 100–1600 and  
235 2800–4000 cm<sup>-1</sup> shift, with 5 s measuring time per window. Most acquisition temperatures match  
236 those of the FTIR low-temperature measurements to allow for direct comparison.

237

238 Band positions for both FTIR and Raman spectra were obtained by fitting the spectra in the  
239 program Peakfit (version 4.0). A Voigt-shaped band profile (i.e., a convolution of Gaussian and  
240 Lorentzian shapes) was used in both cases. Initial estimates of the number of bands and their  
241 distribution in IR and Raman spectra were based on the investigations on kieserite by previous  
242 authors (Stoilova and Lutz 1998; Lane 2007; Lane et al. 2015 for FTIR spectroscopy; and Chio et  
243 al. 2007 and citations therein for Raman spectra).

244

### 245 **UV-Vis-NIR spectroscopy and crystal field calculations**

246 An unpolarized optical absorption spectrum of a single crystal of  $\text{FeSO}_4 \cdot \text{H}_2\text{O}$  was  
247 measured at room temperature in the spectral range  $30000\text{--}3500\text{ cm}^{-1}$  on a mirror-optics  
248 microscope IRscope-II, attached to a Bruker IFS66v/S FTIR spectrometer. Appropriate  
249 combinations of light sources (Xe- or W-lamp, Globar), beam splitters (quartz, KBr) and  
250 detectors (GaP-, Si-, Ge-diodes, MCT) were used to cover the spectral range. The final spectrum  
251 is combined from four partial spectra (range in  $\text{cm}^{-1}$  / spectral resolution in  $\text{cm}^{-1}$  / averaged scans:  
252 UV:  $30000\text{--}19380$  / 40 / 1024; Vis:  $19380\text{--}9700$  / 20 / 1024; NIR:  $9700\text{--}5260$  / 10 / 768; IR:  
253  $5260\text{--}3000$  / 4 / 512), which were aligned in absorbance for perfect match, if necessary, and then  
254 converted to the linear absorption coefficient  $\alpha$ .

255 Crystal field (CF) calculations were performed in the framework of the semi-empirical  
256 Superposition Model (SM) of crystal fields using the HCFLDN2 module of the computer  
257 program package by Y.Y. Yeung (Chang et al. 1994). Due to the small number of observed  
258 crystal field levels, the power-law exponents  $t_k$  were fixed at their respective ideal electrostatic  
259 values, i.e.,  $t_4 = 5$  and  $t_2 = 3$ , and the Racah parameters were constrained to the ratio Racah C/B =  
260 4.3 given in Figgis and Hitchman (2000). The reference metal–ligand distance  $R_0$  was set to 2.13  
261 Å, the mean  $\langle \text{Fe–O} \rangle$  bond length in szomolnokite. For further details concerning the calculation

262 procedures the reader is referred to similar cases in Wildner et al. (2013) and respective  
263 references therein.

264

## 265 **Results**

266

### 267 **Sample chemistry and powder X-ray diffraction**

268 The wet chemical analyses ensured precise knowledge of the actual Mg/Fe ratio in the bulk  
269 synthesized products in their respective final state, i.e., after the purification process described in  
270 the Experimental section. In addition, they revealed systematic differences between the pre-  
271 adjusted and the actual Mg/Fe ratio in the product. The redox buffer greatly influences the extent  
272 of discrepancy between theoretical  $x_{\text{Fe}(\text{preset})}$  and experimental  $x_{\text{Fe}(\text{sample})}$  values. Whereas the  
273 crystals are usually clearly enriched in Fe when using the metallic Fe-foil as redox buffer,  
274 preferential incorporation of Fe into the monohydrated sulfate is of much lesser extent with the  
275  $\text{H}_2\text{SO}_3$  buffer in use. For the spectroscopic measurements, only batches with  $|x_{\text{Fe}(\text{sample})} - x_{\text{Fe}(\text{preset})}|$   
276  $\leq 0.06$  as listed in Table 1 and shown in Fig. 1 were used.

277 Powder X-ray diffraction measurements and Rietveld refinements revealed the various  
278 batches to consist nearly exclusively of kieserite-type  $(\text{Mg,Fe})\text{SO}_4 \cdot \text{H}_2\text{O}$  with occasional traces of  
279 hexahydrite or rhomboclase. The patterns showed no signs of Bragg peak splitting or suspicious  
280 broadening, thus confirming compositional homogeneity and the mono-phase character of the  
281 obtained monohydrate sulfate solid solutions.

282 As noted already above, the Mg/Fe ratios of the crystals hand-picked for single crystal  
283 X-ray diffraction studies were extracted as a refined variable in the structure refinements.

284

### 285 **Crystal structures**

286 The present single crystal X-ray measurements and structure refinements along the  
287 kieserite–szomolnokite solid solution series,  $\text{Mg}_{1-x}\text{Fe}_x\text{SO}_4\cdot\text{H}_2\text{O}$ , gave no indications of octahedral  
288 Mg/Fe cation ordering, domain formation or related effects. Crystal data, details of the data  
289 collections and structure refinements of four selected representatives including szomolnokite are  
290 listed in Table 2, respective final atomic coordinates and displacement parameters in Table 3.  
291 Corresponding temperature-dependent data of the endmembers kieserite and szomolnokite are  
292 compiled for two selected temperatures in Tables 4 and 5. Important crystal chemical data at  
293 ambient and temperature-dependent conditions are given in Tables 6 and 7, respectively. Details  
294 for the kieserite endmember at room temperature were recently reported by Bechtold and Wildner  
295 (2016) in their structural study of the kieserite–cobaltkieserite solid solution series, and are  
296 included in Tables 2 and 6 for convenient comparison.

297 The kieserite structure type is built from kinked chains of  $\text{O3}(\equiv\text{H}_2\text{O})$ -corner-sharing  
298  $\text{MgO}_4(\text{H}_2\text{O})_2$  octahedra, elongated along their O3–O3 axis, and nearly regular  $\text{SO}_4$  tetrahedra,  
299 intra-linking adjacent octahedra within the chains by common O2 corners. These octahedral-  
300 tetrahedral chains are aligned parallel to the *c* axis and linked to a framework structure by sharing  
301 the remaining polyhedral O1 corners as well as by moderately strong  $\text{O3}\cdots\text{O2}$  hydrogen bonds.

302 The structural behavior of the  $\text{Mg}_{1-x}\text{Fe}_x\text{SO}_4\cdot\text{H}_2\text{O}$  kieserite–szomolnokite solid solution  
303 series is illustrated in Figures 2–5. It is evident that complete miscibility exists and that the series  
304 shows Vegard-type behavior, with all lattice parameters (Fig. 2) changing in a linear way across  
305 the entire composition. The cell volume  $V$  ( $+10 \text{ \AA}^3$ ), angle  $\beta$  ( $+0.6^\circ$ ), and the lattice parameters *a*  
306 and *c* ( $+0.18$  and  $0.14 \text{ \AA}$ ) increase with Fe uptake, only the *b* axis ( $-0.08 \text{ \AA}$ ) shows an opposite  
307 trend. The clear increase of individual and average Me–O bond lengths and of the octahedral  
308 volume (Figs. 3a and 4a) comply with the larger ionic radius of  $\text{Fe}^{2+}$  compared to Mg. The  
309 comparatively moderate increase of the Me–O2 bond can be partly related with the shortening of

310 the  $b$  axis, since Me–O1, –O2 and –O3 bonds have their major vector components parallel to the  
311 crystallographic  $a$ ,  $b$  and  $c$  axis, respectively. With Fe uptake, also the octahedral distortion  
312 increases for bond lengths as well as bond angles (Figs. 3ab, Table 6), and the octahedral shape  
313 changes from a clear [4+2] coordination in kieserite towards a [2+2+2]-type coordination in  
314 szomolnokite. Also the tetrahedral SO<sub>4</sub> group slightly expands with increasing Fe content (Figs.  
315 3c, 4a), but bond length and also angular changes (Fig. 3d) hardly exceed a  $3\sigma$  limit. The  
316 medium-strength hydrogen bond O3–H···O2 lengthens only slightly (Fig. 4c), despite having its  
317 main component parallel to the strongly increasing  $a$  axis.

318 The prominent changes within the MeO<sub>6</sub> octahedron along the Mg<sub>1-x</sub>Fe<sub>x</sub>SO<sub>4</sub>·H<sub>2</sub>O solid  
319 solution are accompanied by mutual compensating polyhedral rotations and tiltings, evidenced by  
320 a significant decrease of the Me–O–S and Me–O3–Me angles shown in Fig. 4b. Hence, the tilting  
321 within the octahedral chain increases and the rather rigid SO<sub>4</sub> tetrahedron rotates by up to 2.3°  
322 (O1–O1' edge; O2–O2' edge: 2.0°) around its twofold axis (Fig. 5); combined with the strong  
323 change of the octahedral O1–Me–O3 angle this leads to a mutual shift of the polyhedral chains  
324 along the  $c$  axis, resulting in the increase of the cell angle  $\beta$  and especially of the  $a$  axis.

325 When temperature is reduced, some structural properties of the kieserite and szomolnokite  
326 endmembers seem to deviate more or less from a linear response. As expected, the cell volumes  
327 decrease, as well as  $\beta$ ,  $a$ , and  $c$ , but the  $b$  axis lengthens for both compounds (Fig. 6). Also the  
328 mean Me–O bond lengths (Fig. 7a) and octahedral volumes (Fig. 7c) decrease, mainly by  
329 reducing the longest Me–O3 bond; the only other Me–O change larger than  $3\sigma$  across the whole  
330 temperature range is a further slight shortening of shortest Fe–O2 bond; thus, for the FeO<sub>6</sub>  
331 octahedron the tendency towards a [2+2+2] coordination still increases. Most acute octahedral  
332 bond angles marginally increase (Fig. 7b), thus slightly reducing bond angle distortion at lower  
333 temperatures. If S–O bond lengths are not corrected for thermal motion, the apparent increase in

334 S–O bond lengths and tetrahedral volume upon cooling (Fig. 7cd) has to be assigned as the  
335 respective artifact. Applying a ‘simple rigid bond’ correction according to Downs et al. (1992)  
336 results (apart from a generally inherent distance increase) in a practically constant  $\langle\text{S–O}\rangle$  bond  
337 length in kieserite and a marginally decreasing one ( $\Delta_{\langle\text{S–O}\rangle} = -0.0014 \text{ \AA}$ ) in szomolnokite upon  
338 cooling along the full temperature range. The tetrahedral angles show divergent trends with  
339 temperature reduction (with maximal changes of  $0.3^\circ$ ), i.e., tending to lower distortion in  
340 kieserite compared to higher distortion in szomolnokite. The O3–H $\cdots$ O2 hydrogen bond length  
341 consistently shortens in both compounds by  $\sim 0.028 \text{ \AA}$  within the investigated 200 K range (Fig.  
342 8a). Also corresponding polyhedra-linking angles show parallel behavior in kieserite and  
343 szomolnokite (Fig. 8b): the octahedral chain angle Me–O3–Me remains constant, but Me–O–S  
344 angles get smaller by  $1.1^\circ$  (O2) and  $\sim 0.7^\circ$  (O1). The resulting rotation of the SO<sub>4</sub> tetrahedron  
345 upon cooling has the same sense as found for increasing  $x_{\text{Fe}}$  in the solid solution (compare Fig.  
346 5); between room temperature and  $-160^\circ\text{C}$  it amounts to roughly  $1.1^\circ$  for both O1–O1’ and O2–  
347 O2’ tetrahedral edges in both endmembers.

348

#### 349 **IR spectra**

350 The IR spectra of the Mg/Fe monohydrated sulfates feature several clearly discernible  
351 absorption phenomena (Fig. 9). Taking as an example the FTIR spectra measured in transmission  
352 mode, the H<sub>2</sub>O absorption region is dominated by a prominent band at  $3182\text{--}3245 \text{ cm}^{-1}$  ( $3.14\text{--}$   
353  $3.08 \mu\text{m}$ ), representing the symmetric stretching vibration  $\nu_{1(\text{H}_2\text{O})}$  of the H<sub>2</sub>O molecule. A poorly  
354 resolved broad shoulder at even higher wavenumbers ( $3367\text{--}3391 \text{ cm}^{-1}$  /  $2.97\text{--}2.95 \mu\text{m}$ )  
355 represents  $\nu_{3(\text{H}_2\text{O})}$ , the antisymmetric H<sub>2</sub>O stretching mode. The H<sub>2</sub>O bending vibration  $\nu_{2(\text{H}_2\text{O})}$   
356 occurs at  $1525\text{--}1496 \text{ cm}^{-1}$  ( $6.56\text{--}6.68 \mu\text{m}$ ). A major band group (centered around  $1150 \text{ cm}^{-1}$  /  
357  $8.70 \mu\text{m}$ ) corresponds to the antisymmetric  $\nu_{3(\text{SO}_4)}$  stretching mode of the sulfate tetrahedra and

358 the IR-forbidden symmetric stretching mode  $\nu_{1(\text{SO}_4)}$ , visible as a weak but well-defined band  
359 around  $1025 \text{ cm}^{-1}$ . A pronounced absorption phenomenon (hereafter labeled ‘Peak  $850 \text{ cm}^{-1}$ ’),  
360 considered as a potential diagnostic feature for monohydrated kieserite-group sulfates by Lane  
361 (2007), occurs in our data (Fig. 9) at  $884\text{--}831 \text{ cm}^{-1}$  ( $11.31\text{--}12.03 \mu\text{m}$ ). Lastly, a band group at  
362  $630 \text{ cm}^{-1}$  ( $15.87 \mu\text{m}$ ) is assigned to the  $\nu_{4(\text{SO}_4)}$  bending modes.

363         It should be mentioned that the absorption band shape and even position vary significantly  
364 between individual FTIR measuring modes (Fig. 9). Nevertheless, the overall spectral appearance  
365 is comparable, with the absorption of the  $\text{H}_2\text{O}$  bending vibration  $\nu_{2(\text{H}_2\text{O})}$  being enhanced in DRIFT  
366 spectra when using diluted sample material (Fig. 9). The sole exceptions as to the consistency of  
367 the spectral shapes are DRIFT measurements on pure sample material (no KBr dilution), where  
368 most intrinsic absorption phenomena at lower wavenumbers are suppressed, with strong artifacts  
369 present, such as the ‘reststrahlenband’ labeled ‘R’ in Fig. 9, a pronounced absorption at around  
370  $1300 \text{ cm}^{-1}$ . Absorptions due to  $\text{H}_2\text{O}$  modes at high wavenumbers are noisy, leading to the loss of  
371 resolution between the  $\nu_{1(\text{H}_2\text{O})}$  and  $\nu_{3(\text{H}_2\text{O})}$  bands. The spectral position of the reststrahlenband  
372 artifact, however, is also dependent on the sample composition, shifting from  $1360$  to  $1283 \text{ cm}^{-1}$   
373 ( $7.35$  to  $7.78 \mu\text{m}$ ) from kieserite to szomolnokite.

374         A specific benefit of DRIFT measurements, however, is the enhanced amplitude of  
375 absorption bands assigned to  $\text{H}_2\text{O}$  combination modes in the  $4400\text{--}5200 \text{ cm}^{-1}$  ( $2.27\text{--}1.92 \mu\text{m}$ )  
376 spectral region. Three distinct bands occur at  $4688$ ,  $4845$  and  $5087 \text{ cm}^{-1}$  ( $2.13$ ,  $2.06$  and  $1.97 \mu\text{m}$ ,  
377 respectively) in endmember kieserite. When  $x_{\text{Fe}}$  increases, both peripheral bands converge closer  
378 to the central one at  $4845 \text{ cm}^{-1}$  ( $2.06 \mu\text{m}$ ), creating the misleading impression (mainly in case of  
379 poor resolution or enhanced spectral noise) of a dominant single broad band at  $4750 \text{ cm}^{-1}$  ( $2.10$   
380  $\mu\text{m}$ ) with a weaker one at  $5025 \text{ cm}^{-1}$  ( $1.99 \mu\text{m}$ ) in szomolnokite (Fig. 10ab, Table 8).



381 In agreement with the structural behavior along the (Mg,Fe)SO<sub>4</sub>·H<sub>2</sub>O solid solution series  
382 reported above, the positional changes of the IR absorption bands with increasing Fe content also  
383 show linear trends within limits of error (Fig. 11). The only exceptions to this rule are the above-  
384 mentioned H<sub>2</sub>O combination modes seen in DRIFT spectra, where a more complex trend is  
385 observed. In many cases, the changes are quite subtle, such as for the position of the SO<sub>4</sub>  
386 vibrations and that of the H<sub>2</sub>O bending mode, where the decrease in wavenumber from the  
387 kieserite to the szomolnokite endmember amounts to a mere 30 cm<sup>-1</sup> in all three measuring  
388 modes. Clearer correlation trends can be observed for the H<sub>2</sub>O stretching vibrations, where the  
389 well-resolved  $\nu_{1(\text{H}_2\text{O})}$  band changes in position from 3182 in kieserite to 3245 cm<sup>-1</sup> in  
390 szomolnokite. A somewhat smaller but still significant change can be seen for the apparent  
391 monohydrate sulfate diagnostic ‘Peak 850 cm<sup>-1</sup>’ (Lane 2007; Lane et al. 2015) that shifts in our  
392 data from 884 in kieserite to 831 cm<sup>-1</sup> with increasing  $x_{\text{Fe}}$ . No significant correlation could be  
393 observed for the  $\nu_{3(\text{H}_2\text{O})}$  band position, due to it being present as a mere shoulder of the afore-  
394 mentioned  $\nu_{1(\text{H}_2\text{O})}$  vibration, leading to significant fitting errors. The variations in the wavenumber  
395 position of relevant spectral absorption phenomena for the individual measurement modes, as  
396 well as the respective linear regression coefficients, are summarized in Table 8.

397 From the acquired temperature-dependent FTIR-spectra between +40 and -160/180 °C  
398 (Fig. 12), two behaviors are evident. Firstly, the sulfate tetrahedra behave as a rigid unit, which is  
399 reflected by the nearly stable position of all SO<sub>4</sub><sup>2-</sup> vibrational modes regardless of temperature.  
400 On the contrary, the H<sub>2</sub>O-related symmetric stretching vibration in kieserite shows a significant  
401 decrease in wavenumber by 29 cm<sup>-1</sup> (0.030 μm) from +40 °C down to -160 °C at a rate of -0.145  
402 cm<sup>-1</sup>/°C, and szomolnokite, measured down to -180 °C, shows a change of 33 cm<sup>-1</sup> (0.022 μm)  
403 with a comparable rate of -0.150 cm<sup>-1</sup>/°C. The rate of decrease appears to be constant,  
404 independent of the Mg/Fe ratio (Fig. 12). The diagnostic ‘Peak 850 cm<sup>-1</sup>’ discussed earlier shows

405 a wavenumber increase upon cooling, whereas the H<sub>2</sub>O bending vibration remains nearly  
406 unaffected by the temperature change.

407

#### 408 **Raman spectra**

409 The changes in Raman band position along the kieserite–szomolnokite solid solution are  
410 also linear as could be expected from the FTIR results (Table 9). Figure 13 graphically depicts  
411 the positional changes of prominent bands across the solid solution series in detail, and Table 9  
412 gives the respective coefficients of the linear regression between the band position and  $x_{\text{Fe}}$ .

413 The Raman spectra consist of numerous narrow bands in the 100–1600 cm<sup>-1</sup> shift region,  
414 with much better resolution compared to FTIR spectra (Fig. 9 vs. 14a). The most prominent band  
415 is the symmetric stretching vibration  $\nu_{1(\text{SO}_4)}$  of the sulfate tetrahedron with Raman shift at 1042  
416 cm<sup>-1</sup> for kieserite and 1018 cm<sup>-1</sup> for szomolnokite. Several relevant spectral features occur at  
417 lower shift values, and the most prominent are located at ~270, ~430 and a doublet at ~620 cm<sup>-1</sup>.  
418 Weak bands in the spectral range 1100–1600 cm<sup>-1</sup> are assigned to the split  $\nu_{3(\text{SO}_4)}$  vibrations  
419 (Stoilova and Lutz 1998; Chio et al. 2007), with the exception of the broader H<sub>2</sub>O bending mode  
420 at 1500 cm<sup>-1</sup>. Stretching vibrations of the H<sub>2</sub>O molecule occur in the expected region, i.e., the  
421  $\nu_{1(\text{H}_2\text{O})}$  band is located at 3179 up to 3247 cm<sup>-1</sup> with increasing  $x_{\text{Fe}}$  (Fig. 14b), whereas the  
422 antisymmetric  $\nu_{3(\text{H}_2\text{O})}$  mode is again present as its shoulder, analogous to the FTIR spectra.

423 It should be mentioned that despite the sample being in finely powdered form, the effect of  
424 varying (and unknown) crystallite orientation, influencing the relative amplitude of the Raman  
425 bands, is clearly visible. This is attributed to the small scattering volume excited by the laser spot  
426 in comparison with the much higher (and thus orientation-averaging) sample volume measured  
427 by IR spectroscopic techniques (in the order of mm<sup>3</sup>, depending on the specific measuring mode).  
428 Fortunately, only band amplitudes are affected, while their positions remain the same.

429 Low-temperature Raman measurements have also been conducted. As expected, a  
430 significant composition-independent systematic shift of the band position with temperature is  
431 seen for the  $\nu_{1(\text{H}_2\text{O})}$  band, which decreases in wavenumber shift by about  $30 \text{ cm}^{-1}$  across the full  
432 temperature range, and represents the strongest change among all examined bands. The  $\nu_{3(\text{H}_2\text{O})}$   
433 band is again poorly resolved, thus impeding any precise fit. The very good band resolution and  
434 low FWHM of the  $\text{SO}_4$  vibrational bands in Raman spectra allow accurate examination of even  
435 their subtle positional changes, which are not so apparent in IR spectra (Table 9). In general, their  
436 wavenumber change with temperature never exceeds  $10 \text{ cm}^{-1}$  within the examined temperature  
437 range (Table 9). A systematic increase in wavenumber shift is observed at low temperature for  
438 the lowest-energetic bands, representing octahedral stretching modes according to Chio et al.  
439 (2007). For all observed bands, the rates at which the band positions change with temperature  
440 remain constant across the examined temperature range, allowing one to determine a mean shift  
441 per  $1 \text{ }^\circ\text{C}$  for the individual bands, included in Table 9.

442

#### 443 **UV-Vis-NIR spectroscopy and crystal field calculations**

444 The optical absorption spectrum of szomolnokite is shown in Fig. 15. Two prominent  
445 crystal field absorption bands centered around  $7650$  and  $10640 \text{ cm}^{-1}$  are attributed to transitions  
446 from the  ${}^5\text{T}_{2g}$  ground state with parental  ${}^5\text{D}$  term to the spin-allowed  ${}^5\text{E}_g(\text{D})$  level of octahedral  
447  $\text{Fe}^{2+}$ , which is split into two non-degenerate states in non-cubic crystal fields (i.e., in a pseudo-  
448 tetragonal approach  ${}^5\text{A}_{1g}$  and  ${}^5\text{B}_{1g}$ ). A sharp peak at  $6565 \text{ cm}^{-1}$  within the low-energy wing of the  
449 first crystal field band represents the first overtone of the O–H stretching mode. All other spectral  
450 features observed between  $19800$  to  $25900 \text{ cm}^{-1}$  (see inset in Fig. 15) are very weak and can be  
451 attributed to spin-forbidden crystal field transitions of  $\text{Fe}^{2+}$  derived from excited triplet terms,  
452 very probably  ${}^3\text{T}_{1g}(\text{H})$ ,  ${}^3\text{T}_{2g}(\text{G})$ ,  ${}^3\text{E}_g(\text{H})$ ,  ${}^3\text{T}_{1g}(\text{G})$  and  ${}^3\text{T}_{2g}(\text{F}_2)$ , in sequence of increasing energy

453 (labels for cubic symmetry). The background increase in absorption towards the UV is most  
454 likely related to the LMCT transition (ligand–metal charge transfer) of trace contents of  $\text{Fe}^{3+}$ ,  
455 causing the light beige hue of szomolnokite. The crystal field (CF) calculations, either based on a  
456 full superposition model (SM) calculation in the actual triclinic polyhedral symmetry, or on a  
457 pseudotetragonal approach assuming a [4+2]-elongated octahedron and employing classical CF  
458 parameters, both yield basically comparable and reasonable results, summarized in Table 10.  
459 They also match well with respective results for cobaltkieserite (Wildner 1996), showing the  
460 comparability of crystal fields in transition metal kieserite-group compounds. Apart from similar  
461 field strengths  $Dq_{\text{cub}}$  and Racah parameters, even the tetragonal distortion parameter  $Dt$ ,  
462 expressing the polyhedral elongation of the  $\text{H}_2\text{O}\text{--Me--OH}_2$  axis, is similarly underestimated due  
463 to the higher field strength of  $\text{H}_2\text{O}$  molecules compared to oxygen ligands of the  $\text{SO}_4$  groups.

464

465

## Discussion

466

### Crystal structural evolution and crystal chemistry

468 In view of previous single-crystal structure investigations of endmember kieserite  
469 (Bechtold and Wildner 2016; earlier Hawthorne et al. 1987) and szomolnokite (Wildner and  
470 Giester 1991), the solid solution series presented here behaves as expected: in particular, all  
471 lattice parameters and crystal chemical data exhibit Vegard-type behavior within the limits of  
472 error, i.e., they show linear changes with Mg/Fe ratio. The extent of those changes along the solid  
473 solution allows, amongst others, to infer the Mg/Fe ratio in  $\text{Mg}_{1-x}\text{Fe}_x\text{SO}_4\cdot\text{H}_2\text{O}$  samples of  
474 unknown composition from X-ray data. Furthermore, this work also constitutes an important  
475 basis for any further theoretical calculations of interest, as well as the possibility to easily  
476 determine the values of thermodynamic parameters for any member of the solid solution. This is

477 enabled because the Vegard-type behavior indicates one-site ideal mixing of both endmembers  
478 (Powell and Holland 1993). Enthalpy, entropy, molar volume, as well as heat capacity and  
479 thermal expansion can be determined by the linear combination of these parameters for both  
480 endmembers in their respective formula ratio in the sample (van Hinsberg et al. 2005a,b).

481 As expected from a crystal chemical point of view, the replacement of the smaller Mg  
482 cation ( $r_{\text{Mg}} = 0.720 \text{ \AA}$ ) by the larger  $\text{Fe}^{2+}$  ( $r_{\text{Fe}^{2+}} = 0.780 \text{ \AA}$ ; all radii from Shannon 1976) leads to a  
483 corresponding increase of average and individual Me–O bond lengths, of the respective  
484 octahedral volume, and hence also of the unit-cell volume (Figs. 2b, 3a and 4a). However, a more  
485 detailed analysis is advisable, since this is not the case for the kieserite-cobaltkieserite solid  
486 solution series,  $\text{Mg}_{1-x}\text{Co}_x\text{SO}_4 \cdot \text{H}_2\text{O}$ , recently studied by Bechtold and Wildner (2016). There, the  
487 replacement of the smaller Mg by the larger  $\text{Co}^{2+}$  ( $r_{\text{Co}^{2+}} = 0.745 \text{ \AA}$ ) leads to an increase of  
488 average and individual Me–O bond lengths and of the octahedral volume, but surprisingly at the  
489 same time the cell volume is reduced. Apart from Bechtold and Wildner (2016) (and earlier  
490 Wildner and Giester 1991 and Giester and Wildner 1992) for kieserite-type compounds, a  
491 comparable aberrant behavior has been explicitly noted and documented for blödite-type  
492 compounds  $\text{Na}_2\text{Me}^{2+}(\text{SO}_4)_2 \cdot 4\text{H}_2\text{O}$  (Stoilova and Wildner 2004) or for Tutton's salts  
493  $\text{K}_2\text{Me}^{2+}(\text{SO}_4)_2(\text{SO}_4)_2 \cdot 6\text{H}_2\text{O}$  (Bosi et al. 2009). Bechtold and Wildner (2016) attribute this  
494 mismatch to the absence of (for Mg) and the presence of (for  $\text{Co}^{2+}$ )  $3d$  orbitals, the latter  
495 imposing anisotropy of the electron density around transition metal (TM) cations. This anisotropy  
496 affects the position of the bond critical point  $\mathbf{r}_c$  along the Me–O bond path and the electron  
497 density  $\rho(\mathbf{r}_c)$  at this point (cf. e.g., Bader 1998). For Mg–O bonds,  $\mathbf{r}_c$  lies comparatively closer to  
498 Mg with lower  $\rho(\mathbf{r}_c)$  than for  $3d\text{TM}$ –O bonds, thus in turn also affecting the electron density at  
499 the oxygen ligands and hence the second coordination sphere: S–O bond lengths (slightly)  
500 increase with Co- and in the present case Fe-uptake (Fig. 3c); however, the second coordination

501 sphere ‘contracts’ due to increased interpolyhedral folding as evidenced by reduction of the Me–  
502 O–S and Me–O–Me angles shown in Fig. 4b (also see respective discussion, Figures and  
503 references in Bechtold and Wildner 2016). These aspects are also directly related to significant  
504 differences in the total, as well as Me<sup>2+</sup>-cation polarizabilities  $\alpha$  in kieserite compared to the  
505 3dTM kieserite-group compounds, as recently discussed by Gagné et al. (2018) for various  
506 structure types comprising Mg- and 3dTM-representatives. All the arguments discussed for Co<sup>2+</sup>  
507 also hold for Fe<sup>2+</sup> compared to Mg, but due to the clearly higher difference in ionic radii, no eye-  
508 catching volume mismatch is found for the present kieserite–szomolnokite solid solution series.

509         Nonetheless, szomolnokite (and Fe-rich representatives in general) also deviates in some  
510 aspects from the otherwise uniform properties of kieserite and the 3dTM-kieserite-group sulfates,  
511 especially concerning the tendency towards a [2+2+2]-coordination in the octahedral unit,  
512 compared to clear [4+2] geometries in the kieserite-group monohydrate sulfates of Mg, Mn, Ni,  
513 Co and Zn (see Fig. 2 in Wildner and Giester 1991). Hence we may suppose that a moderately  
514 elongated octahedral [4+2]-environment complies well with packing requirements of the kieserite  
515 structure type (note that a strong elongation imposed e.g., by Jahn-Teller affected Cu<sup>2+</sup> is not  
516 accepted, leading to symmetry reduction; Giester 1988). The deviation observed for szomolnokite  
517 might be attributed to the uneven *d*-electron distribution of high-spin 3d<sup>6</sup>-configured Fe<sup>2+</sup>, with  
518 one excess (i.e., paired) electron in the triply degenerate *t<sub>2g</sub>* set of the 3d orbitals. Other  
519 representatives have either no (for Mg), symmetrically (for Mn<sup>2+</sup>, Ni<sup>2+</sup>) or fully occupied (for  
520 Zn<sup>2+</sup>) 3d orbitals, or two excess (paired) electrons in the *t<sub>2g</sub>* orbital set (as for Co<sup>2+</sup>). In the latter  
521 case, an appropriately elongated [4+2] Jahn-Teller distortion is in theory expected, neglecting any  
522 thermodynamic considerations (in practice, respective static effects are not statistically detectable  
523 in room temperature crystal structures; Wildner 1992). However, in case of 3d<sup>6</sup>-configured  
524 Fe<sup>2+</sup>, a compressed octahedral [2+4] Jahn-Teller distortion is theoretically predicted, thus

525 suggesting the specific uneven *d*-electron distribution as probable explanation for the particular  
526 deviation of the octahedral distortion in szomolnokite (but there seem to exist no systematic  
527 studies seeking to generally verify a respective static effect for Fe<sup>2+</sup>).

528

## 529 **IR, Raman and crystal field spectra**

530 **IR spectra at ambient conditions.** The linear Vegard-type behavior observed in the  
531 structural data of the Mg<sub>1-x</sub>Fe<sub>x</sub>SO<sub>4</sub>·H<sub>2</sub>O solid solution series (Figs. 2–4) is also reflected in the  
532 results of FTIR and Raman spectroscopic measurements. With wavenumber units in use, one can  
533 recognize a linear change of the position of IR spectral bands across the kieserite–szomolnokite  
534 series (Fig. 11, Table 8). Evidently, the wavenumber of the prominent symmetric stretching  
535 vibration  $\nu_{1(\text{H}_2\text{O})}$  of the H<sub>2</sub>O molecule increases with Fe content. This is in agreement with the  
536 structural data (Fig 4c, Table 6), where the O3···O2 donor–acceptor hydrogen bond length  
537 increases with  $x_{\text{Fe}}$ , expectably leading to the observed band behavior (e.g., Libowitzky 1999).  
538 Likewise, a similar blue-shift of the antisymmetric stretching mode  $\nu_{3(\text{H}_2\text{O})}$  would also be  
539 expected. However, since the band overlaps significantly with the prominent  $\nu_{1(\text{H}_2\text{O})}$  absorption,  
540 the trend is obscured due to reduced fitting accuracy. The H<sub>2</sub>O bending mode  $\nu_{2(\text{H}_2\text{O})}$  decreases  
541 slightly but constantly in position with increasing  $x_{\text{Fe}}$ , which might be correlated with the  
542 widening of the acceptor–donor–acceptor angle O2···O3···O2 from kieserite to szomolnokite  
543 (136.7–140.5°). Both the symmetric  $\nu_{1(\text{SO}_4)}$  vibration and the three bands assigned to the split  
544  $\nu_{3(\text{SO}_4)}$  mode (Chio et al. 2007; Lane 2007) decrease in wavenumber with increasing  $x_{\text{Fe}}$ , in accord  
545 with the observed slight relaxation of the SO<sub>4</sub><sup>2-</sup> tetrahedron towards szomolnokite (Figs. 3c, 4a,  
546 Table 6). Of the latter three bands, only the major one is depicted and its position followed in Fig.  
547 11 and Table 8, since the peripheral bands present as shoulders are not traceable reliably. Similar  
548 to  $\nu_{1(\text{H}_2\text{O})}$ , the prominent ‘Peak 850 cm<sup>-1</sup>’ absorption band deemed as diagnostic by Lane (2007)

549 and Lane et al. (2015) could also be used to infer the Mg/Fe ratio, since it shows a rather  
550 pronounced wavenumber decrease towards Fe-rich compositions (i.e.,  $831\text{ cm}^{-1}$  in szomolnokite).  
551 A group of bands at  $\sim 630\text{ cm}^{-1}$ , assigned by Lane et al. (2015) to the  $\nu_{4(\text{SO}_4)}$  vibration, cannot  
552 easily be exploited for cosmochemical considerations, as the spectral region not only consists of  
553 numerous bands with varying FWHM, but also does not prove to be clearly discernible from the  
554 signals of other sulfates and even silicates. Furthermore, the Martian atmosphere is dominated by  
555  $\text{CO}_2$  that has a strong band centered at  $\sim 667\text{ cm}^{-1}$ , potentially obscuring bands within the wings of  
556 the  $\text{CO}_2$  band ( $\sim 529$  to  $794\text{ cm}^{-1}$ ; e.g., Christensen et al. 2000). Therefore, the IR spectral region  
557 between  $700$  and  $300\text{ cm}^{-1}$  ( $14.3$ – $27.0\text{ }\mu\text{m}$ ) was not studied in further detail.

558 Contrary, the  $4400$ – $5200\text{ cm}^{-1}$  ( $2.27$ – $1.92\text{ }\mu\text{m}$ ) spectral region, where absorptions  
559 associated with combination modes of the  $\text{H}_2\text{O}$  stretching and bending modes occur, is  
560 considered by many authors to be an important spectral feature in reflectance spectra from Mars  
561 orbiters, allowing not only to discern kieserite from other sulfate hydrates, in which the  
562 prominent bands occur at higher wavenumbers (Mangold et al. 2008; Noel et al. 2015), but also  
563 to roughly infer its Fe content (Cloutis et al. 2006; Bishop et al. 2009; Liu et al. 2016). The  $\text{H}_2\text{O}$   
564 combination modes are most apparent in DRIFT spectra of pure undiluted sample material. The  
565 kieserite endmember shows a typical set of three bands at  $\sim 4700$ ,  $4850$  and  $5090\text{ cm}^{-1}$  ( $2.13$ ,  $2.06$ ,  
566  $1.96\text{ }\mu\text{m}$ ) (Fig. 10ab, Table 8). A comparison between the kieserite and szomolnokite endmember  
567 patterns (Bishop et al. 2009) has led many of the above-mentioned authors to infer the presence  
568 of a single dominant absorption band ( $2.09\text{ }\mu\text{m}$ ) with a shoulder in szomolnokite, instead of the  
569 clearly visible triplet observed in kieserite. As can be seen in Fig. 10a, all three bands occur in  
570 szomolnokite as well, with the peripheral bands ‘converged’ in their position closer to the central  
571 one. Given their broad FWHM, the three bands, shifted close together in szomolnokite, create the  
572 misleading impression of a broad peak (central band) with a single shoulder (highest-energetic



573 peak) with the center at a higher wavenumber than the strongest of the three individual bands  
574 discernible in endmember kieserite, which corresponds to the lowest-energetic peak in the triplet  
575 (Fig. 10a, Table 8). A more detailed analysis of the behavior of the triplet with increasing  $x_{\text{Fe}}$   
576 revealed a non-linear relation of the band position with the Mg/Fe ratio at higher Fe contents.  
577 This discrepancy may, however, be attributed to the presence of a weak yet broad band caused by  
578  $\text{Fe}^{2+}$  crystal field transitions (Fig. 15), which partly alters the background even in the  $\text{H}_2\text{O}$   
579 combination mode region due to its large FWHM (Jamieson et al., 2014). Together with the  $\text{H}_2\text{O}$ -  
580 related combination bands being very weak even when measuring undiluted sample material in  
581 DRIFT mode, a fitting error is introduced, which, to our opinion, accounts for the non-linearity of  
582 the observed trends when higher amounts of  $\text{Fe}^{2+}$  are present (Fig. 10b, Table 8).

583 As noted above, the wavenumber of any particular absorption in the IR spectrum also  
584 changes in relation to the measuring technique (Table 8). As an example, the  $\nu_{1(\text{H}_2\text{O})}$  band occurs  
585 at  $3182\text{ cm}^{-1}$  in endmember kieserite measured in transmission mode, whereas the corresponding  
586 feature is centered at  $3165\text{ cm}^{-1}$  in ATR mode and as high as  $3203\text{ cm}^{-1}$  using the DRIFT  
587 technique on the very same sample (3.14, 3.16 and 3.12  $\mu\text{m}$ , respectively). The shift in band  
588 position is to be attributed to the known change in refractive index close to a spectral absorption,  
589 dependent on the ratio of the reflection and transmission components constituting the final  
590 spectral signal. Besides, DRIFT spectra of undiluted sample material show significant artifacts  
591 (reststrahlenband, etc.) instead of the expected sulfate vibrations between  $1300$  and  $370\text{ cm}^{-1}$   
592 ( $7.69$  and  $27.02\text{ }\mu\text{m}$ ). A sample dilution of 1:20 in an IR-transparent material (KBr) already leads  
593 to a spectral shape very close to the result of proper transmission measurements, with enhanced  
594 amplitudes of weaker bands, such as  $\nu_{2(\text{H}_2\text{O})}$  and the  $\text{H}_2\text{O}$  combination modes.

595 All these factors have implications for measurements on Mars, where IR spectra reflected  
596 by ‘fluffy’ kieserite aggregates (more transmission) would somewhat differ in shape and band

597 position from signals acquired on compact kieserite masses or crusts due to the different  
598 reflection/transmission ratio of the particular material. Disregard of these issues could be  
599 misleading in the assessment of the properties and composition of the measured monohydrate  
600 sulfate. Contrary, the grain size seems to have little effect on the band *position* in IR reflectance  
601 spectra (Jamieson et al. 2014; Pitman et al. 2014).

602 With this in mind, promising spectral features for a semi-quantitative assessment of the  
603 chemistry of kieserite-group solid solutions from orbiter spectra should be the absorption bands  
604 with a pronounced regression slope in relation to  $x_{\text{Fe}}$ . In addition to the H<sub>2</sub>O combination mode  
605 region centered at  $\sim 4900 \text{ cm}^{-1}$  ( $2.04 \text{ }\mu\text{m}$ ), a promising candidate would seem to be the  $\nu_{1(\text{H}_2\text{O})}$   
606 band, showing a wavenumber change towards higher values by  $\sim 60 \text{ cm}^{-1}$  ( $0.06 \text{ }\mu\text{m}$ ) from kieserite  
607 to szomolnokite (Fig. 11). While  $\nu_{2(\text{H}_2\text{O})}$  and the sulfate modes all show smaller positional  
608 changes with respect to sample chemistry, the ‘Peak  $850 \text{ cm}^{-1}$ ’ ( $11.8 \text{ }\mu\text{m}$ ), deemed as diagnostic  
609 for monohydrated sulfates by previous authors (Lane et al., 2015), appears to be promising as  
610 well due to a comparatively large shift in wavenumber of roughly  $50 \text{ cm}^{-1}$  ( $0.72 \text{ }\mu\text{m}$ ).

611 When expressing positions and shifts of the spectral bands (e.g., as done just above), a  
612 ‘technical’ issue immediately becomes apparent. The choice of spectral units, i.e., wavenumber in  
613  $\text{cm}^{-1}$  vs. wavelength in  $\mu\text{m}$ , significantly influences the shape of the spectral envelope and the  
614 apparent extent of changes in the position of absorption features. Whereas the difference in the  
615 wavenumber position of the H<sub>2</sub>O symmetric stretching mode  $\nu_{1(\text{H}_2\text{O})}$  and the ‘Peak  $850 \text{ cm}^{-1}$ ’ band  
616 amounts to a comparable shift of  $60$  and  $50 \text{ cm}^{-1}$ , respectively, the same values expressed in  
617 wavelength as spectral unit amount to  $0.06$  and  $0.72 \text{ }\mu\text{m}$ , respectively, setting both values apart  
618 by an entire order of magnitude. While wavelength units are more commonly used in the Vis-  
619 NIR research of the cosmochemical community, wavenumber units were chosen for this work  
620 because it better suits our aim of comparing the structural and spectroscopic behavior of the

621 kieserite–szomolnokite solid solution series. Unlike wavelength, wavenumber units are directly  
622 proportional to the frequency and thus to the energy of the observed phonons, allowing for a  
623 meaningful comparison with structural data. Furthermore, IR spectra represented in wavenumber  
624 units facilitate band fitting using Voigt profiles, as the absorption bands appear symmetrical,  
625 unlike the situation with wavelength units (especially  $> 4 \mu\text{m}$ ). In this way, we were able to  
626 amply demonstrate the linear Vegard-type dependency of vibrational bands on the interatomic  
627 distances and polyhedral size along the entire kieserite–szomolnokite solid solution and the  
628 consistency of single-crystal X-ray and spectral results. Furthermore, the direct comparison of  
629 related vibrational features between Raman and IR spectra is simplified. The corresponding  
630 wavelengths  $\lambda$  (in  $\mu\text{m}$ ) can be easily obtained according to the formula  $\lambda(\mu\text{m}) = 10000/\nu(\text{cm}^{-1})$ .

631

632 **Temperature dependence of IR spectra.** Temperature-related spectral changes (Fig. 12)  
633 are important to consider, especially for interpreting extraterrestrial data, e.g., from Mars, where  
634 the average temperature spans from  $+20$  to  $-120$  °C (Witzke et al. 2007) and reaches values as  
635 low as 5 K elsewhere. Considering that the two bands showing the strongest change with  
636 increasing Fe content ( $\nu_{1(\text{H}_2\text{O})}$  and ‘Peak  $850 \text{ cm}^{-1}$ ’) are also those showing the greatest variation  
637 in position with temperature (Fig. 12), the range of error in the assessment of  $x_{\text{Fe}}$  from a single  
638 band can be up to  $\pm 0.25$  without the approximate knowledge of temperature. The same,  
639 considering the temperature sensitivity of the fundamental  $\text{H}_2\text{O}$  bands, will apply to their  
640 combination modes in the  $\sim 4900 \text{ cm}^{-1}$  region (Fig. 10ab), which, according to the results for  
641 kieserite of Jamieson et al. (2014), split further apart with decreasing temperature. This behavior  
642 is in contrast to the ‘merging’ of the three bands from kieserite to szomolnokite into a seemingly  
643 single broad absorption at higher wavenumbers. In contrast to  $\nu_{1(\text{H}_2\text{O})}$ , the  $\text{H}_2\text{O}$  bending vibration  
644 hardly changes with temperature, obviously related to the small change of the acceptor–donor–

645 acceptor angle O2···O3···O2 (~1.6°), compared to the significant influence of the Mg/Fe ratio  
646 (~4°)

647 As to the sulfate bands, the splitting of  $\nu_{3(\text{SO}_4)}$  into three components and the low amplitude  
648 of the  $\nu_{1(\text{SO}_4)}$  symmetric stretching vibration are the effects that hamper precise fitting and  
649 estimation of  $x_{\text{Fe}}$ , not temperature, towards which they are rather insensitive.

650

651 **Raman spectra at ambient conditions.** Raman spectra acquired across the solid solution  
652 also exhibit systematic band shifts with variable  $x_{\text{Fe}}$  (Figs. 13 and 14, Table 9), and corresponding  
653 vibrational modes show the same behavior in IR and Raman spectra. However, the better band  
654 resolution due to narrower FWHMs and fewer band overlaps in Raman spectra allow for a more  
655 precise refinement of the subtle changes in position and splitting of the diverse  $\text{SO}_4$  modes, as  
656 well as a more accurate characterization of octahedral modes with changing Mg/Fe ratio.

657 The increase in hydrogen bond length with increasing  $x_{\text{Fe}}$  leads to the expected increase in  
658 the wavenumber of the  $\text{H}_2\text{O}$  symmetric stretching vibration from 3179 to 3247  $\text{cm}^{-1}$  shift (3.14–  
659 3.08  $\mu\text{m}$ ). The nearly perfect match between the positions observed in the IR transmission spectra  
660 and the Raman data underline the consistency of both data sets.

661 The change in position of the  $\nu_{1(\text{SO}_4)}$  vibration from 1042 to 1018  $\text{cm}^{-1}$  between kieserite and  
662 szomolnokite, respectively, also parallels its behavior in the IR spectra, where it was present,  
663 albeit weak (e.g., Fig. 11; Lane 2007). On the contrary, it represents the strongest feature in the  
664 Raman spectra of the kieserite–szomolnokite solid solutions, making it the optimum candidate to  
665 infer the Mg/Fe ratio, more so given its stable position at lower temperatures (see below). Also  
666 the three well-resolved bands assigned to the split antisymmetric  $\nu_{3(\text{SO}_4)}$  vibration offer a more  
667 accurate insight into the behavior of the sulfate tetrahedron, in that the spectral position of all  
668 three modes tends to decrease with increasing  $x_{\text{Fe}}$ , as noted before for other methods. The same

669 holds true for the wavenumber decrease of the other modes of the  $\text{SO}_4$  group (Fig. 13, Table 9),  
670 in accord with its slight relaxation upon Fe uptake revealed by the single-crystal diffraction data  
671 (Fig. 3cd, Table 6). The bands observed in the  $100\text{--}250\text{ cm}^{-1}$  shift region feature a component at  
672  $\sim 220\text{ cm}^{-1}$  assigned by Chio et al. (2007) to a vibration involving the translation along the Fe–  
673  $\text{H}_2\text{O}$  bond. However, its spectral position remains nearly unchanged regardless of the Mg/Fe ratio  
674 (Fig. 13, Table 9), which challenges this assignment, given the variation in octahedral bond  
675 lengths across the solid solution (Table 6). A significant positional decrease was observed for the  
676 lowest mode at  $\sim 130\text{ cm}^{-1}$ , changing from  $137$  to  $112\text{ cm}^{-1}$  from kieserite to szomolnokite. While  
677 we are unable to ascertain the exact character of this vibration, its significant change with the  
678 Mg/Fe ratio makes it another viable band to infer on the chemistry of kieserite-group minerals  
679 from vibrational spectra.

680

681 **Temperature dependence of Raman spectra.** Band shifts in low-temperature Raman  
682 spectra show similar behavior to that of the corresponding vibrational modes observed in the IR  
683 spectra (Table 9). Better band resolution compared to IR spectra allows, however, to accurately  
684 track even the subtle positional changes of sulfate-related peaks. The highest-energy peak of the  
685 split  $\nu_{3(\text{SO}_4)}$  mode at  $\sim 1200\text{ cm}^{-1}$  increases, while the lowest-energy  $\nu_{3(\text{SO}_4)}$  peak at  $\sim 1100\text{ cm}^{-1}$   
686 decreases in position (Table 9). This increase of spectroscopic distortion may be correlated with  
687 the slight increase in geometric tetrahedral distortion at reduced temperatures (compare  
688 respective distortion parameters in Tables 6 and 7).

689 The vibrational mode at  $\sim 220\text{ cm}^{-1}$  shift shows a notable increase in wavenumber at low  
690 temperature. This behavior, together with its position at  $\sim 220\text{ cm}^{-1}$ , implies a possibility that the  
691 diagnostic ‘Peak  $850\text{ cm}^{-1}$ ’ absorption feature in the *IR spectra* (Lane et al. 2015), is actually a  
692 combination of this mode and the  $\nu_{4(\text{SO}_4)}$  mode at  $\sim 630\text{ cm}^{-1}$ , which decreases in wavenumber

693 from kieserite to szomolnokite. This would lead to the expected wavenumber decrease of the  
694 resulting IR absorption at  $\sim 850\text{ cm}^{-1}$  from kieserite to szomolnokite, as would be dictated by the  
695 trends seen for both  $\nu_{4(\text{SO}_4)}$  components (Fig. 13). The absence of this band in the Raman spectra  
696 supports this theory, since such phenomena are suppressed in Raman spectroscopy to a great  
697 extent due to the different underlying physical process of spectrum formation (IR absorption  
698 versus inelastic scattering). The splitting of the  $\nu_{4(\text{SO}_4)}$  vibration into two bands may also account  
699 for the slight asymmetry observed for the ‘Peak  $850\text{ cm}^{-1}$ ’ IR band (Fig. 13, Table 9).

700

701 **Use of vibrational spectra to infer the composition of Martian kieserite.** Linear trends,  
702 observed for changes in structural parameters of  $(\text{Mg,Fe})\text{SO}_4\cdot\text{H}_2\text{O}$  (Figs. 2-4), as well as in the  
703 position of IR bands (when expressed in wavenumbers) and in Raman spectra, clearly correlate  
704 with the Mg/Fe ratio (Figs. 11, 13). Aside from documenting in detail the behavior of kieserite-  
705 group compounds throughout the Mg/Fe solid solution series, the linearity of the data also allows  
706 its use as a standard in evaluating IR spectra acquired during orbiter missions as well as Raman  
707 measurements, which will be conducted during future rover missions to Mars.

708 In general, the evaluation of OMEGA (0.35 to  $5.2\ \mu\text{m}$ ) and CRISM (0.362 to  $3.92\ \mu\text{m}$ )  
709 measurements in the VNIR-SWIR spectral range (visible/near to shortwave infrared) leading to  
710 the assessment of the mineral phases present on the planet’s surface and their composition,  
711 follows the ‘spectral unmixing’ approach, requiring reference endmember spectra (Cloutis et al.  
712 2006; Combe et al. 2008; Mangold et al. 2008; Bishop et al. 2009; Lichtenberg et al. 2010; Roach  
713 et al. 2010; Noel et al. 2015; Liu et al. 2016). In brief, using the reference endmember spectra, the  
714 spectral signal from orbiter measurements is fitted by least-squares techniques, after its correction  
715 for the instrumental function (CRISM smile, etc.), atmospheric scattering and incidence angle,  
716 using detailed knowledge of Mars topography simultaneously verified by MOLA (Mars Orbital

717 Laser Altimeter). While to date, only pure endmember kieserite and szomolnokite spectra were  
718 used for this assessment, the detection of linear trends across the entire kieserite–szomolnokite  
719 solid solution presented in this work allows us to derive reference spectra for kieserite–  
720 szomolnokite solid solution minerals of intermediate composition and, in theory, to then obtain  
721 additional information on the chemistry (i.e., Mg/Fe ratio) of the unknown  $(\text{Mg,Fe})\text{SO}_4 \cdot \text{H}_2\text{O}$   
722 kieserite-group mineral at hand, with semi-quantitative results.

723         However, additional sources of error arise from the use of different correction datasets  
724 preceding the actual spectral unmixing procedure. Different versions of the atmospheric  
725 correction model used in the evaluation of CRISM spectra may lead to significant changes in the  
726 form of the resulting spectrum, even causing errors in the discrimination between kieserite and  
727 szomolnokite endmembers in the same region of interest. Such a case can be seen comparing the  
728 work of Bishop et al. (2009) to that of Noel et al. (2015), when the latter authors dismissed the  
729 presence of Fe-rich kieserite or endmember szomolnokite in Juventae Chasma using a newer  
730 parameter set. We nevertheless believe, that at least a semi-quantitative impression as to the  
731 Mg/Fe ratio in kieserite-group minerals in a studied region can be obtained from IR spectra, as  
732 long as comparable correction routines are used.

733         As already outlined above, the knowledge of surface temperatures (at least approximate  
734 values) during remote measurements facilitates quantitative comparisons, but otherwise ~~only~~  
735 useful semi-quantitative information (better than  $x_{\text{Fe}} \pm 0.25$ ) may be extracted, especially when  
736 combining several spectral features. The attempt to use sulfate-related bands for such  
737 considerations is hampered by their wavenumber position being largely insensitive to  
738 temperature changes in IR spectra (Fig. 12). Given the limited resolution of orbiter spectra up to  
739 date, this will likely prevent any exact observation of the subtle band position changes due to  
740 enhanced noise.

741 A much more promising situation is to be expected considering the higher resolution and  
742 low FWHM of Raman bands, which aids in ascertaining their position changes from kieserite to  
743 szomolnokite with higher precision. The superior spectral resolution even allows efficient use of  
744 the sulfate-related bands, such as the prominent  $\nu_1(\text{SO}_4)$  band (Fig. 14), to infer the Mg/Fe content,  
745 with the benefit of their nearly perfect insensitivity to temperature changes. Despite the lack of  
746 surface Raman data at the moment, forthcoming rover missions (in particular ExoMars 2020 and  
747 Mars 2020) include Raman on-board instruments. Besides, Mars rovers are and will be equipped  
748 with thermometers, providing the precise temperature during measurement.

749 This work considers the behavior of kieserite and szomolnokite, as we know it from Earth,  
750 i.e., crystallizing in the above described  $C2/c$  structure type. However, a second ‘polymorph’ of  
751  $\text{MgSO}_4 \cdot \text{H}_2\text{O}$  has been postulated in literature to be present as a stable phase instead of or along  
752 with ‘classic’ kieserite on Mars. This phase has been obtained during dehydration-rehydration  
753 studies at Mars-relevant conditions by Wang et al. (2009, 2011) and is often labeled LH-kieserite  
754 (LH for ‘low humidity’); Jamieson et al. (2014) obtained this ‘polymorph’ by dehydrating  
755 kieserite at 250 °C for one week. The resulting phase shows minor spectral differences compared  
756 to ‘classic’ kieserite, with a slightly different position of the  $\text{H}_2\text{O}$  combination modes in the 4900  
757  $\text{cm}^{-1}$  (2.04  $\mu\text{m}$ ) region. We are currently working on a paper elucidating the actual character and  
758 spectroscopic properties of this second kieserite ‘polymorph’ in detail.

759

760 **Crystal field spectra.** The main purpose of presenting an optical crystal field (CF)  
761 spectrum of szomolnokite in the present context is to provide an impression on the possible  
762 influence of the spin-allowed  ${}^5\text{T}_{2g}(\text{D}) \rightarrow {}^5\text{E}_g(\text{D})$  crystal field transition of octahedral  $\text{Fe}^{2+}$  on  
763 remote or in-situ NIR spectra from orbiter and rover missions. Figure 15 shows that the cubic  
764  ${}^5\text{E}_g(\text{D})$  state splits into two levels in the low-symmetry field of szomolnokite and that the lower



765 energy  ${}^5A_{1g}$  split level (tetragonal label) centered at  $7650\text{ cm}^{-1}$  ( $1.31\text{ }\mu\text{m}$ ) may influence  
766 overtones and combinations modes in the NIR spectra from  $\sim 5350\text{ cm}^{-1}$  ( $1.87\text{ }\mu\text{m}$ ) onwards. In  
767 particular, the first overtone of the  $\text{H}_2\text{O}$  stretching mode is located at  $6565\text{ cm}^{-1}$  within the low-  
768 energy wing of  ${}^5A_{1g}$ , also perceivable in the VNIR DRIFT spectra of szomolnokite acquired by  
769 Pitman et al. (2014). Concerning CF states, up to now only the higher-energetic and more intense  
770  ${}^5B_{1g}$  split level at  $10640\text{ cm}^{-1}$  ( $0.94\text{ }\mu\text{m}$ ) was attributed to szomolnokite (at  $0.9\text{--}0.95\text{ }\mu\text{m}$ ) and  
771 discussed (Cloutis et al. 2006; Bishop et al. 2009; Jamieson et al. 2014; Pitman et al. 2014). It  
772 was argued that the latter Fe-related absorption ( $\sim 0.95\text{ }\mu\text{m}$ ) is commonly observed in spectra of  
773 Martian sulfate salts and thus may not uniquely identify szomolnokite, since it could also be  
774 produced by even minor amounts of particles of a separate Fe-bearing dust phase covering sulfate  
775 rocks (Bishop et al. 2009). However, the  ${}^5A_{1g}$  split level at  $7640\text{ cm}^{-1}$  ( $1.31\text{ }\mu\text{m}$ ) was not  
776 considered so far as diagnostic for szomolnokite, in spite of the fact that it is present, albeit weak,  
777 also in the comparative laboratory spectra of szomolnokite by Bishop et al. (2009). Furthermore,  
778 in the usual wavelength presentation, this band is broadened compared to the stronger  ${}^5B_{1g}$  band  
779 and thus even less noticeable. Admittedly, in Fe-bearing monohydrated sulfate, i.e., in diluted  
780 szomolnokite, the electronic  ${}^5A_{1g}$  band will be most likely too weak to be extracted from orbiter  
781 spectra, but we propose to regard it as highly diagnostic for szomolnokite in data of future rover  
782 missions. Moreover, since the energies of the  ${}^5E_g(\text{D})$  split levels at  $7650$  and  $10640\text{ cm}^{-1}$  are very  
783 closely reproduced by the CF calculations at  $7713$  and  $10549\text{ cm}^{-1}$ , respectively (full triclinic SM  
784 calculation, Table 10), the influence of temperature as well as of the Mg/Fe ratio in solid  
785 solutions can be efficiently predicted from our presented single crystal structure data: for  
786 example, a temperature reduction to  $-160\text{ }^\circ\text{C}$  hardly changes the calculated energy of  ${}^5B_{1g}$  ( $10539$   
787  $\text{cm}^{-1}$ ) but predicts a moderate shift of  ${}^5A_{1g}$  by  $\sim 100\text{ cm}^{-1}$  to  $7815\text{ cm}^{-1}$ ; contrary, stronger band

788 shifts are predicted with changing Mg/Fe ratio: for the structure with  $\text{Mg}_{0.55}\text{Fe}_{0.45}$  (Tables 2,3,6)  
789 respective energies of 11034 and 8249  $\text{cm}^{-1}$  are calculated for ambient conditions.

790

791

### Implications

792

793 The verification of the existence of a continuous solid solution series between kieserite and  
794 szomolnokite suggests that respective intermediate compositions are expected to occur in Fe-rich  
795 environments. The presented data can generally assist in the identification of kieserite,  
796 szomolnokite and their solid solutions, not only on Mars, despite the attention given to this  
797 planet. The linear character of the observed spectral and structural trends at room temperature and  
798 the knowledge of their changes upon cooling provides a solid starting basis to draw conclusions  
799 about the composition of this important Martian sulfate based on absorption band positions in IR  
800 and Raman spectra. Even in the case of a semi-quantitative approach (no knowledge of  
801 temperature), zoning of Fe contents in Martian kieserite-containing sediments can be monitored.  
802 The presented data are especially relevant in view of the shortly forthcoming rover missions Mars  
803 2020 (NASA) and ExoMars 2020 (ESA) allowing in-situ vibrational spectroscopic  
804 measurements, including, for the first time on Mars, Raman investigations.

805 Chemical zoning of kieserite-group minerals from past spectral results may also be  
806 determined. Promising candidates for such a re-evaluation are, as representative examples, the  
807 spatially resolved CRISM spectra acquired across the rather large Ius Chasma and Juventae  
808 Chasma sulfate deposits or Aram Chaos.

809

810

811

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821

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1007

## 1008 **Figure captions**

1009

1010 **Figure 1.** Deviations between actual Fe content of the  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4) \cdot \text{H}_2\text{O}$  solid solution samples  
1011  $x_{\text{Fe}(\text{sample})}$  as determined by the wet chemical analyses and the pre-adjusted Mg/Fe ratio in the  
1012 hydrothermal batch  $x_{\text{Fe}(\text{preset})}$ . Errors are equal or smaller than the symbol size. Note that batches  
1013 exceeding the shown range of deviation (i.e., mainly Mg-dominant batch runs with metallic Fe-  
1014 foil as redox buffer yielding significantly Fe-enriched samples) were not used for the  
1015 spectroscopic measurements.

1016

1017 **Figure 2.** Variation of the lattice parameters (a)  $a$ ,  $b$ ,  $c$  and (b)  $\beta$  and  $V$  along the  
1018  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4) \cdot \text{H}_2\text{O}$  solid solution series with linear regression lines. Errors are equal or smaller  
1019 than the symbol size. The data for endmember kieserite are taken from Bechtold and Wildner  
1020 (2016). Previous data for the Fe endmember (Wildner and Giester 1991) are shown (without  
1021 errors) as dotted diamond symbols.

1022

1023 **Figure 3.** Polyhedral geometries along the  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid solution series with linear  
1024 regression lines, (a) octahedral Me–O bond lengths and (b) O–Me–O angles, (c) tetrahedral S–O  
1025 bond lengths and (d) O–S–O angles. If not indicated, errors are equal or smaller than the symbol  
1026 size. The data for endmember kieserite are taken from Bechtold and Wildner (2016). Previous  
1027 data for the Fe endmember (Wildner and Giester 1991) are shown (without errors) as dotted  
1028 diamond symbols.

1029

1030 **Figure 4.** (a) Polyhedral volumes, (b) Me–O–S and Me–O–Me angles and (c) hydrogen bond  
1031 lengths along the  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid solution series with linear regression lines. For (a),  
1032 note the strongly different scales for the tetrahedral and octahedral volumes. If not indicated,  
1033 errors are equal or smaller than the symbol size. The data for endmember kieserite are taken from  
1034 Bechtold and Wildner (2016). Previous data for the Fe endmember (Wildner and Giester 1991)  
1035 are shown (without errors) as dotted diamond symbols.

1036

1037 **Figure 5.** Overlay of crystal structure fragments of kieserite,  $\text{MgSO}_4\cdot\text{H}_2\text{O}$  (full lines), in front of  
1038 szomolnokite,  $\text{FeSO}_4\cdot\text{H}_2\text{O}$  (dashed lines), centred at the S atom ( $0,y,1/4$ ), in a projection along the  
1039 negative *b*-axis.  $\text{MgO}_6$  octahedra are shown in grey,  $\text{FeO}_6$  octahedra below in green,  $\text{SO}_4$   
1040 tetrahedra in yellow, and the water molecules as cyan spheres. Dotted arrows indicate major  
1041 rotational and translational changes along the  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid solution series as  
1042 discussed in the text. Cell axes plots are scaled to 50%. Structural data for endmember kieserite  
1043 are taken from Bechtold and Wildner (2016).

1044

1045 **Figure 6.** Variation of the lattice parameters (a) *a*, *b*, *c* and (b)  $\beta$  and *V* for kieserite (‘Mg’, light  
1046 grey circle symbols) and szomolnokite (‘Fe’, dark grey diamond symbols) within the investigated

1047 temperature range, with second-order regression lines. Errors are equal or smaller than the  
1048 symbol size.

1049

1050 **Figure 7.** Variation of the polyhedral geometries **(a)** octahedral Me–O bond lengths and **(b)** O–  
1051 Me–O angles, **(c)** polyhedral volumes, and **(d)** tetrahedral S–O bond lengths (uncorrected for  
1052 thermal motion, see text) for kieserite (‘Mg’, light grey circle symbols) and szomolnokite (‘Fe’,  
1053 dark grey diamond symbols) within the investigated temperature range, with second- or third  
1054 order regression lines. Third-order regressions are very probably not significant, but are used to  
1055 guide the eye. For **(c)**, note the somewhat different scales for the tetrahedral and octahedral  
1056 volumes. If not indicated, errors are equal or smaller than the symbol size.

1057

1058 **Figure 8.** Variation of **(a)** hydrogen bond lengths and **(b)** Me–O–S/Me angles for kieserite (‘Mg’,  
1059 light grey circle symbols) and szomolnokite (‘Fe’, dark grey diamond symbols) within the  
1060 investigated temperature range, with second-order regression lines. If not indicated, errors are  
1061 equal or smaller than the symbol size.

1062

1063 **Figure 9.** FTIR spectra of the kieserite and szomolnokite endmembers, Mg/Fe(SO<sub>4</sub>)·H<sub>2</sub>O, in each  
1064 measuring mode. In addition to band position changes between the endmembers, note the  
1065 differences in band positions and shapes between the measuring modes.

1066

1067 **Figure 10.** Spectral region with three diagnostic H<sub>2</sub>O combination modes, **(a)** observed in DRIFT  
1068 measurements on undiluted sample material, **(b)** detailed plot of band position change for the  
1069 examined bands across the kieserite–szomolnokite solid solution series. Errors equal or smaller  
1070 than the symbol size are not plotted.

1071

1072 **Figure 11.** Dependence of the positions of relevant FTIR absorption features (transmission  
1073 measurements) of  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid solutions on the Fe content at room temperature  
1074 (RT). The scatter in data points of the  $\nu_{3(\text{H}_2\text{O})}$  vibration is caused by the significant overlap with  
1075 the  $\nu_{1(\text{H}_2\text{O})}$  vibration. Errors equal or smaller than the symbol size are not plotted.

1076

1077 **Figure 12.** Dependence of the FTIR absorption band positions of  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid  
1078 solutions on temperature, as seen in transmission mode. The two most promising candidate bands  
1079 for the determination of  $x_{\text{Fe}}$  based on FTIR spectra are shown by rectangular symbols.

1080

1081 **Figure 13.** Dependence of the Raman band positions of  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid solutions on  
1082 increasing Fe content  $x_{\text{Fe}}$  at room temperature. Errors are equal or smaller than the symbol size.

1083

1084 **Figure 14.** Raman spectra of the kieserite and szomolnokite endmembers,  $\text{Mg/Fe}(\text{SO}_4)\cdot\text{H}_2\text{O}$ , at  
1085 room temperature.

1086

1087 **Figure 15.** UV-Vis-NIR absorption spectrum of szomolnokite in the range from 28800–3500  
1088  $\text{cm}^{-1}$  with observed (bold line marks) and calculated energy levels (thin line marks) and  
1089 respective assignments for cubic symmetry, in case of spin-allowed  ${}^5\text{E}_g(\text{D})$  also with tetragonal  
1090 labels. Calculated singlet states are not shown. The inset shows the background-subtracted and  
1091 intensity-enhanced region between 27000–18000  $\text{cm}^{-1}$ .

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1098 **Tables**

1099

1100 **Table 1.** Composition of the spectroscopically studied samples as determined by wet chemical  
1101 analyses. The analytical error is 0.005 wt% for Mg and 0.002 wt% for Fe. Deviations of the  
1102 actual sample Fe content  $x_{\text{Fe}(\text{sample})}$  from the preset Mg/Fe ratio in the batch  $x_{\text{Fe}(\text{preset})}$  are also  
1103 given. The Mg/Fe ratios of individual hand-picked crystals for single crystal X-ray diffraction  
1104 studies were extracted as variable parameter in the respective structure refinement runs.

1105

Sample ID	Mg (wt%)	Fe (wt%)	$x_{\text{Fe}(\text{sample})}$	$x_{\text{Fe}(\text{preset})}$	$x_{\text{Fe}(\text{sample})} - x_{\text{Fe}(\text{preset})}$
Fe10c	15.77	3.73	0.093	0.100	-0.006
Fe15c	13.84	6.54	0.170	0.150	0.020
Fe20c	13.05	7.53	0.200	0.200	0.000
Fe30c	11.87	9.68	0.261	0.300	-0.038
Fe40c	9.85	12.78	0.360	0.400	-0.039
Fe5Sa	15.81	3.89	0.096	0.050	0.046
Fe10Sa	14.21	5.42	0.142	0.100	0.042
Fe15Sa	12.77	7.63	0.206	0.150	0.056
Fe25Sa	11.05	10.25	0.287	0.250	0.037
Fe45Sa	7.68	15.84	0.473	0.450	0.023
Fe65Sa	4.67	20.78	0.659	0.650	0.009
Fe85Sa	2.36	23.04	0.868	0.850	0.018
Fe0Sb	16.76	0.05	0.000	0.000	0.000
Fe20Sa	11.87	8.81	0.244	0.200	0.044
Fe30Sa	9.85	12.22	0.350	0.300	0.050
Fe35Sa	8.82	14.17	0.411	0.350	0.061
Fe40Sa	8.10	14.36	0.435	0.400	0.035
Fe50Sa	6.41	17.99	0.549	0.500	0.049
Fe60Sa	5.14	19.87	0.627	0.600	0.027
Fe70Sa	3.85	22.03	0.713	0.700	0.013
Fe75Sa	3.28	22.65	0.750	0.750	0.000
Fe80Sa	2.36	23.04	0.809	0.800	0.009
Fe90Sa	0.92	24.71	0.920	0.900	0.020
Fe95Sa	0.69	27.19	0.945	0.950	-0.004
Fe100Sa	0.01	27.5	0.999	1.000	0.000
Fe5Sc	15.89	3.64	0.090	0.050	0.040
Fe80Sc	3.34	22.93	0.749	0.800	-0.050
Fe85Sc	2.49	23.96	0.807	0.850	-0.042
Fe0Sc	17.59	0	0	0	0

1106 **Table 2.** Crystal data and details of room-temperature X-ray data collections and structure  
 1107 refinements for selected representatives of the  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid solution series. Common  
 1108 data: monoclinic, space group  $C2/c$  (no. 15),  $Z = 4$ . Data for the kieserite endmember are taken  
 1109 from Bechtold and Wildner (2016).  
 1110

$\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$	$\text{Mg}_{1.00}\text{Fe}_{0.00}$	$\text{Mg}_{0.86}\text{Fe}_{0.14}$	$\text{Mg}_{0.55}\text{Fe}_{0.45}$	$\text{Mg}_{0.25}\text{Fe}_{0.75}$	$\text{Mg}_{0.00}\text{Fe}_{1.00}$
$x_{\text{Fe}}$	0.0	0.138(2)	0.450(2)	0.752(3)	1.0
$a$ (Å)	6.910(1)	6.938(1)	6.989(1)	7.042(1)	7.086(1)
$b$ (Å)	7.634(2)	7.621(1)	7.601(1)	7.579(2)	7.555(1)
$c$ (Å)	7.643(2)	7.663(1)	7.710(1)	7.753(2)	7.780(1)
$\beta$ (°)	118.00(1)	118.14(1)	118.30(1)	118.49(1)	118.61(1)
$V$ (Å <sup>3</sup> )	356.00(14)	357.32(8)	360.63(8)	363.65(14)	365.63(8)
$\mu$ (mm <sup>-1</sup> )	0.97	1.48	2.61	3.70	4.58
$D_{\text{calc}}$ (gcm <sup>-3</sup> )	2.582	2.653	2.810	2.961	3.087
Exposure time (s)/frame	140	150	25	70	40
CCD frames processed	508	526	503	514	511
Frame scale factors $_{\text{max, min}}$	1.11, 0.89	1.12, 0.91	1.16, 0.81	1.17, 0.76	1.09, 0.77
Total number of intensity data	12919	14115	13849	14055	12661
Total number of reflections	8865	8935	8613	8615	8875
Intensity data for unit cell	5101	7219	7420	7418	5362
Number of hkl's	3995	4178	4203	4211	4255
Unique hkl's	1089	1100	1110	1126	1133
$R_i$ (%)	3.20	2.77	2.37	3.09	2.65
$F_o > 4\sigma(F_o)$	937	985	1026	1027	1111
Variables	39	42	42	42	40
wR2 [for all $F_o^2$ ] (%)	6.17	5.75	5.72	5.98	4.12
weighting parameters a, b <sup>a</sup>	0.028, 0.20	0.027, 0.27	0.028, 0.20	0.030, 0.32	0.018, 0.27
R1 [for $F_o > 4\sigma(F_o)$ ] (%)	2.27	2.23	2.20	2.39	1.56
R1 [for all $F_o$ ] (%)	2.94	2.73	2.53	2.82	1.60
Goodness of fit	1.109	1.062	1.151	1.073	1.065
Extinction coefficient	0	0.004(2)	0.009(2)	0.009(2)	0.260(5)
$\Delta\rho_{\text{max, min}}$ (e <sup>-</sup> Å <sup>-3</sup> )	0.47, -0.51	0.59, -0.43	0.95, -0.45	1.02, -0.49	0.77, -0.62

1111 <sup>a</sup>  $w = 1 / [\sigma^2(F_o^2) + (a \times P)^2 + b \times P]$ ;  $P = \{[\text{max of } (0 \text{ or } F_o^2)] + 2F_c^2\} / 3$ .

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1116 **Table 3.** Structure parameters at room temperature for selected representatives of the  
 1117  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid solution series.  $U_{ij}$  are given in  $\text{pm}^2$ . Wyckoff positions: Mg/Fe on 4b  
 1118 (sym  $\bar{1}$ ): 0,  $\frac{1}{2}$ , 0 etc.; S and O3 on 4e (sym 2): 0,  $y$ ,  $\frac{1}{4}$  etc.,  $U_{23}=U_{12}=0$ ; O1, O2 and H on 8f (sym  
 1119 1):  $x, y, z$  etc. Respective data for endmember kieserite are given in Bechtold and Wildner (2016).

$\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$	$\text{Mg}_{0.86}\text{Fe}_{0.14}$	$\text{Mg}_{0.55}\text{Fe}_{0.45}$	$\text{Mg}_{0.25}\text{Fe}_{0.75}$	$\text{Mg}_{0.00}\text{Fe}_{1.00}$	
Mg/Fe	$x_{\text{Fe}}$	0.138(2)	0.450(2)	0.752(3)	1.0
	$U_{11}$	81(1)	86(1)	90(1)	81(1)
	$U_{22}$	93(2)	97(1)	101(1)	93(1)
	$U_{33}$	88(1)	100(1)	99(1)	91(1)
	$U_{23}$	6(1)	7(1)	8(1)	9(1)
	$U_{13}$	35(1)	39(1)	41(1)	38(1)
	$U_{12}$	-4(1)	-3(1)	-2(1)	-1(1)
	$U_{\text{eq}}$	90(1)	96(1)	98(1)	90(1)
S	$y$	0.15459(3)	0.15413(3)	0.15362(4)	0.15329(3)
	$U_{11}$	63(1)	67(1)	70(1)	57(1)
	$U_{22}$	78(1)	81(1)	84(1)	73(1)
	$U_{33}$	89(1)	101(1)	100(1)	91(1)
	$U_{13}$	30(1)	34(1)	36(1)	31(1)
	$U_{\text{eq}}$	79(1)	86(1)	87(1)	75(1)
O1	$x$	0.17509(10)	0.17307(10)	0.17096(12)	0.16934(9)
	$y$	0.04446( 9)	0.04384( 9)	0.04312(12)	0.04258(9)
	$z$	0.39481(10)	0.39605(10)	0.39722(12)	0.39810(9)
	$U_{11}$	94(2)	105(2)	107(3)	91(2)
	$U_{22}$	162(3)	174(3)	179(3)	170(2)
	$U_{33}$	161(3)	178(3)	182(3)	177(2)
	$U_{23}$	70(2)	74(2)	79(3)	80(2)
	$U_{13}$	39(2)	47(2)	50(2)	51(2)
	$U_{12}$	41(2)	46(2)	47(2)	44(2)
	$U_{\text{eq}}$	148(1)	160(1)	164(1)	151(1)
O2	$x$	0.09221(10)	0.09347(10)	0.09476(12)	0.09619(9)
	$y$	0.26771( 8)	0.26779( 8)	0.26783(10)	0.26810(7)
	$z$	0.15040(10)	0.15273(10)	0.15504(12)	0.15713(8)
	$U_{11}$	135(2)	141(2)	145(3)	128(2)
	$U_{22}$	119(2)	130(2)	132(3)	122(2)
	$U_{33}$	173(2)	190(3)	190(3)	177(2)
	$U_{23}$	53(2)	53(2)	53(2)	53(2)
	$U_{13}$	95(2)	101(2)	103(2)	94(2)
	$U_{12}$	14(2)	16(2)	14(2)	15(2)
	$U_{\text{eq}}$	133(1)	144(1)	146(1)	134(1)
O3	$y$	0.63647(12)	0.63940(12)	0.64236(15)	0.64477(10)
	$U_{11}$	117(3)	122(3)	130(4)	125(3)
	$U_{22}$	134(3)	139(3)	149(4)	131(3)
	$U_{33}$	118(3)	133(3)	132(4)	116(3)
	$U_{13}$	58(3)	63(3)	62(3)	62(2)
	$U_{\text{eq}}$	122(1)	131(1)	137(2)	122(1)
H	$x$	0.097(3)	0.094(3)	0.102(3)	0.099(3)
	$y$	0.698(2)	0.704(3)	0.710(3)	0.717(3)
	$z$	0.285(3)	0.287(3)	0.290(3)	0.294(3)
	$U_{\text{iso}}$	323(47)	355(50)	372(60)	354(46)



1120 **Table 4.** Crystal data and details of selected temperature-dependent X-ray data collections and  
 1121 structure refinements for kieserite and szomolnokite endmembers, Mg/Fe(SO<sub>4</sub>)·H<sub>2</sub>O. Common  
 1122 data: monoclinic, space group *C2/c* (no. 15), *Z* = 4; Exposure time/frame 20 s; 40 variables.  
 1123 Respective room-temperature data for kieserite (Bechtold and Wildner 2016) and szomolnokite  
 1124 are given in Table 1.  
 1125

Mg/Fe(SO <sub>4</sub> )·H <sub>2</sub> O	Mg <sub>1.00</sub>	Mg <sub>1.00</sub>	Fe <sub>1.00</sub>	Fe <sub>1.00</sub>
<i>T</i> (°C)	−80	−160	−80	−160
<i>a</i> (Å) <sup>a</sup>	6.882(1)	6.865(1)	7.058(1)	7.040(1)
<i>b</i> (Å) <sup>a</sup>	7.653(1)	7.668(1)	7.566(1)	7.576(1)
<i>c</i> (Å) <sup>a</sup>	7.617(1)	7.606(1)	7.758(1)	7.745(1)
<i>β</i> (°) <sup>a</sup>	117.88(1)	117.79(1)	118.45(1)	118.37(1)
<i>V</i> (Å <sup>3</sup> )	354.60(9)	354.18(9)	364.23(9)	363.48(9)
<i>μ</i> (mm <sup>−1</sup> )	0.97	0.97	4.60	4.61
<i>D</i> <sub>calc</sub> (gcm <sup>−3</sup> )	2.592	2.595	3.099	3.105
CCD frames processed	748	748	766	766
Transmission factors <sub>max, min</sub>	0.69, 0.75	0.69, 0.75	0.57, 0.75	0.58, 0.75
Total number of reflections	10428	10307	10851	10783
Intensity data for unit cell	6649	7061	8498	8607
Unique hkl's	1098	1097	1131	1128
<i>R</i> <sub><i>i</i></sub> (%)	1.96	1.84	2.60	2.30
<i>F</i> <sub>o</sub> > 4σ( <i>F</i> <sub>o</sub> )	1047	1054	1112	1118
wR2 [for all <i>F</i> <sub>o</sub> <sup>2</sup> ] (%)	4.48	4.26	3.38	3.22
weighting parameters <i>a</i> , <i>b</i> <sup>b</sup>	0.020, 0.18	0.018, 0.21	0.015, 0.20	0.013, 0.24
R1 [for <i>F</i> <sub>o</sub> > 4σ( <i>F</i> <sub>o</sub> )] (%)	1.56	1.48	1.28	1.27
R1 [for all <i>F</i> <sub>o</sub> ] (%)	1.67	1.56	1.31	1.29
Goodness of fit	1.202	1.207	1.168	1.193
Extinction coefficient	0.004(2)	0.006(2)	0.033(1)	0.042(1)
Δρ <sub>max, min</sub> (e <sup>−</sup> Å <sup>−3</sup> )	0.49, −0.37	0.46, −0.40	0.49, −0.52	0.68, −0.44

1126 <sup>a</sup> lattice parameters are corrected to comply with data from Nonius Kappa CCD room temperature  
 1127 measurements of the very same two crystals (see Experimental section).

1128 <sup>b</sup>  $w = 1 / [\sigma^2(F_o^2) + (a \times P)^2 + b \times P]$ ;  $P = \{[\max \text{ of } (0 \text{ or } F_o^2)] + 2F_c^2\} / 3$ .

1129

1130 **Table 5.** Selected temperature-dependent structure parameters for kieserite and szomolnokite,  
 1131 Mg/Fe(SO<sub>4</sub>)·H<sub>2</sub>O.  $U_{ij}$  are given in pm<sup>2</sup>. Wyckoff positions: Mg/Fe on 4*b* (sym  $\bar{1}$ ): 0, 1/2, 0 etc.;  
 1132 S and O3 on 4*e* (sym 2): 0, *y*, 1/4 etc.,  $U_{23}=U_{12}=0$ ; O1, O2 and H on 8*f* (sym 1): *x*, *y*, *z* etc.  
 1133 Respective room-temperature data for kieserite are given in Bechtold and Wildner (2016), those  
 1134 for szomolnokite in Table 2.

Mg/Fe(SO <sub>4</sub> )·H <sub>2</sub> O		Mg <sub>1.00</sub> (-80 °C)	Mg <sub>1.00</sub> (-160 °C)	Fe <sub>1.00</sub> (-80 °C)	Fe <sub>1.00</sub> (-160 °C)
Mg/Fe	$U_{11}$	49(1)	39(1)	53(1)	36(1)
	$U_{22}$	60(1)	45(1)	57(1)	38(1)
	$U_{33}$	57(1)	43(1)	63(1)	42(1)
	$U_{23}$	2(1)	1(1)	6(1)	5(1)
	$U_{13}$	22(1)	17(1)	27(1)	18(1)
	$U_{12}$	-3(1)	-2(1)	-0(1)	0(1)
	$U_{eq}$	57(1)	43(1)	58(1)	39(1)
S	<i>y</i>	0.15635(2)	0.15710(2)	0.15447(2)	0.15512(2)
	$U_{11}$	35(1)	27(1)	38(1)	28(1)
	$U_{22}$	46(1)	34(1)	46(1)	33(1)
	$U_{33}$	54(1)	38(1)	65(1)	44(1)
	$U_{13}$	18(1)	13(1)	23(1)	16(1)
	$U_{eq}$	46(1)	34(1)	51(1)	35(1)
O1	<i>x</i>	0.17541(7)	0.17522(7)	0.16874(7)	0.16853(7)
	<i>y</i>	0.04664(6)	0.04770(6)	0.04405(7)	0.04497(6)
	<i>z</i>	0.39602(7)	0.39686(6)	0.39968(7)	0.40047(7)
	$U_{11}$	58(2)	42(1)	63(2)	46(1)
	$U_{22}$	102(2)	73(2)	111(2)	77(2)
	$U_{33}$	102(2)	70(1)	120(2)	79(2)
	$U_{23}$	44(1)	29(1)	54(1)	35(1)
	$U_{13}$	28(1)	19(1)	35(1)	23(1)
	$U_{12}$	27(1)	19(1)	30(1)	21(1)
$U_{eq}$	91(1)	65(1)	102(1)	70(1)	
O2	<i>x</i>	0.09440(7)	0.09574(7)	0.09854(7)	0.09991(7)
	<i>y</i>	0.26900(6)	0.26975(5)	0.26941(6)	0.27015(6)
	<i>z</i>	0.15044(7)	0.15109(6)	0.15838(7)	0.15910(6)
	$U_{11}$	81(2)	59(2)	83(2)	61(2)
	$U_{22}$	76(2)	57(1)	80(2)	56(2)
	$U_{33}$	108(2)	75(1)	122(2)	83(2)
	$U_{23}$	32(1)	21(1)	34(1)	22(1)
	$U_{13}$	59(1)	42(1)	63(1)	45(1)
	$U_{12}$	6(1)	2(1)	7(1)	3(1)
$U_{eq}$	82(1)	60(1)	89(1)	62(1)	
O3	<i>y</i>	0.63431(8)	0.63384(8)	0.64418(9)	0.64381(8)
	$U_{11}$	70(2)	51(2)	84(2)	60(2)
	$U_{22}$	83(2)	62(2)	88(2)	64(2)
	$U_{33}$	75(2)	59(2)	87(2)	64(2)
	$U_{13}$	34(2)	26(2)	44(2)	32(2)
	$U_{eq}$	76(1)	57(1)	85(1)	62(1)
H	<i>x</i>	0.104(2)	0.106(2)	0.108(2)	0.109(2)
	<i>y</i>	0.700(2)	0.699(2)	0.716(2)	0.712(2)
	<i>z</i>	0.291(2)	0.290(2)	0.294(2)	0.292(2)
	$U_{iso}$	222(33)	128(31)	283(37)	208(34)

1135 **Table 6.** Survey of crystal chemical data at room temperature for selected representatives of the  
 1136  $\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$  solid solution series: bond lengths (Å) and angles (°), polyhedral volumes  
 1137 (Å<sup>3</sup>), bond strengths (without H atoms; calculated according to Brese and O’Keeffe 1991), and  
 1138 polyhedral distortion parameters (Brown and Shannon 1973; Robinson et al. 1971; Griffen and  
 1139 Ribbe 1979). Data for the kieserite endmember are taken from Bechtold and Wildner (2016).

$\text{Mg}_{1-x}\text{Fe}_x(\text{SO}_4)\cdot\text{H}_2\text{O}$	$\text{Mg}_{1.00}\text{Fe}_{0.00}$	$\text{Mg}_{0.86}\text{Fe}_{0.14}$	$\text{Mg}_{0.55}\text{Fe}_{0.45}$	$\text{Mg}_{0.25}\text{Fe}_{0.75}$	$\text{Mg}_{0.00}\text{Fe}_{1.00}$
$x_{\text{Fe}}$	0.0	0.138(2)	0.450(2)	0.752(3)	1.0
Me–O1 (2×)	2.0216(7)	2.0327(7)	2.0585(7)	2.0854(8)	2.1079(6)
Me–O2 (2×)	2.0414(7)	2.0436(6)	2.0493(6)	2.0545(8)	2.0567(6)
Me–O3 (2×)	2.1714(6)	2.1800(5)	2.1996(5)	2.2183(7)	2.2314(4)
<Me–O>	2.0782	2.0854	2.1025	2.1194	2.1320
$\Delta_{\text{oct}}\times 10^3$	1.023	1.033	1.070	1.124	1.183
$\Sigma$ v.u. (Me)	2.15	2.14	2.12	2.10	2.09
O1–Me–O2 (2×) <sup>a</sup>	85.91(3)	85.82(3)	85.59(3)	85.36(3)	85.08(3)
O1–Me–O3 (2×) <sup>a</sup>	88.50(2)	88.19(2)	87.59(2)	86.96(2)	86.48(2)
O2–Me–O3 (2×) <sup>a</sup>	87.20(3)	87.28(3)	87.49(3)	87.67(4)	87.84(3)
$\sigma_{\text{oct}}^2$	9.75	10.24	11.48	13.16	15.00
$V_{\text{oct}}$	11.901(10)	12.024(8)	12.314(8)	12.604(11)	12.820(8)
S–O1 (2×)	1.4639(7)	1.4629(6)	1.4636(6)	1.4638(8)	1.4638(6)
S–O2 (2×)	1.4817(7)	1.4818(6)	1.4833(6)	1.4849(8)	1.4868(5)
<S–O>	1.4728	1.4724	1.4735	1.4743	1.4753
BLDP $\times 10^3$	6.98	7.41	7.72	8.28	9.00
$\Sigma$ v.u. (S)	6.02	6.03	6.01	6.00	5.98
O1–S–O1’	109.94(6)	109.98(6)	110.11(6)	110.20(8)	110.31(6)
O1–S–O2 (2×)	108.59(4)	108.59(4)	108.73(4)	108.85(4)	108.79(3)
O1–S–O2’(2×)	110.41(4)	110.42(4)	110.24(4)	110.11(5)	110.15(4)
O2–S–O2’	108.89(6)	108.84(5)	108.76(5)	108.70(7)	108.62(5)
$\sigma_{\text{tetr}}^2$	0.77	0.80	0.64	0.54	0.66
$V_{\text{tetr}}$	1.639(2)	1.638(2)	1.641(2)	1.644(3)	1.648(2)
Me–O1–S	140.38(4)	139.93(4)	138.77(4)	137.58(5)	136.70(4)
Me–O2–S	134.31(4)	134.28(4)	134.06(4)	133.78(5)	133.41(3)
Me–O3–Me	123.27(5)	123.01(4)	122.40(4)	121.80(5)	121.31(4)
$\Sigma$ v.u. (O1)	1.95	1.95	1.93	1.92	1.91
$\Sigma$ v.u. (O2)	1.86	1.86	1.86	1.87	1.87
$\Sigma$ v.u. (O3)	0.55	0.54	0.53	0.53	0.52
O3···O2	2.7449(8)	2.7478(8)	2.7507(8)	2.7541(9)	2.7565(7)
O3–H	0.81(2)	0.76(2)	0.76(2)	0.82(2)	0.82(2)
O2···H	2.01(2)	2.04(2)	2.06(2)	2.01(2)	2.04(2)
O3–H···O2	151(2)	155(2)	150(2)	151(2)	145(2)

1140 <sup>a</sup> plus corresponding obtuse angles.

1141 **Table 7.** Survey of selected temperature-dependent crystal chemical data for kieserite and  
 1142 szomolnokite, Mg/Fe(SO<sub>4</sub>)·H<sub>2</sub>O: bond lengths (Å) and angles (°), polyhedral volumes (Å<sup>3</sup>), bond  
 1143 strengths (without H atoms; calculated according to Brese and O’Keeffe 1991), and polyhedral  
 1144 distortion parameters (Brown and Shannon 1973; Robinson et al. 1971; Griffen and Ribbe 1979).  
 1145 Respective room-temperature data for kieserite (Bechtold and Wildner 2016) and szomolnokite  
 1146 are given in Table 6.

Mg/Fe(SO <sub>4</sub> )·H <sub>2</sub> O	Mg <sub>1.00</sub>	Mg <sub>1.00</sub>	Fe <sub>1.00</sub>	Fe <sub>1.00</sub>
<i>T</i> (°C)	−80	−160	−80	−160
Me–O1 (2×)	2.0222(5)	2.0222(5)	2.1093(6)	2.1088(5)
Me–O2 (2×)	2.0407(5)	2.0410(5)	2.0551(5)	2.0546(5)
Me–O3 (2×)	2.1640(4)	2.1607(4)	2.2252(4)	2.2217(4)
<Me–O>	2.0756	2.0746	2.1299	2.1284
Δ <sub>oct</sub> ×10 <sup>3</sup>	0.919	0.874	1.110	1.070
Σ v.u. (Me)	2.16	2.17	2.10	2.10
O1–Me–O2 (2×) <sup>a</sup>	85.97(2)	86.03(2)	85.05(2)	85.04(2)
O1–Me–O3 (2×) <sup>a</sup>	88.51(2)	88.56(1)	86.49(2)	86.54(2)
O2–Me–O3 (2×) <sup>a</sup>	87.23(2)	87.27(2)	87.95(2)	88.01(2)
σ <sub>oct</sub> <sup>2</sup>	9.50	9.20	14.92	14.74
<i>V</i> <sub>oct</sub>	11.861(6)	11.845(6)	12.783(7)	12.758(6)
S–O1 (2×)	1.4640(5)	1.4647(5)	1.4652(5)	1.4657(5)
S–O2 (2×)	1.4837(5)	1.4849(4)	1.4887(5)	1.4901(5)
<S–O>	1.4739	1.4748	1.4770	1.4779
BLDP×10 <sup>3</sup>	7.72	7.91	9.19	9.53
Σ v.u. (S)	6.00	5.99	5.96	5.94
O1–S–O1’	110.01(4)	110.12(4)	110.47(4)	110.59(4)
O1–S–O2 (2×)	108.61(3)	108.63(2)	108.86(3)	108.85(3)
O1–S–O2’(2×)	110.33(3)	110.30(3)	110.06(3)	110.05(3)
O2–S–O2’	108.94(4)	108.85(4)	108.52(4)	108.42(4)
σ <sub>tetr</sub> <sup>2</sup>	0.71	0.72	0.69	0.76
<i>V</i> <sub>tetr</sub>	1.643(1)	1.646(1)	1.653(1)	1.656(1)
Me–O1–S	140.00(3)	139.84(3)	136.22(3)	136.04(3)
Me–O2–S	133.63(3)	133.32(3)	132.79(3)	132.45(3)
Me–O3–Me	123.28(3)	123.28(3)	121.28(3)	121.27(3)
Σ v.u. (O1)	1.95	1.95	1.96	1.95
Σ v.u. (O2)	1.86	1.85	1.80	1.80
Σ v.u. (O3)	0.56	0.57	0.53	0.54
O3···O2	2.7292(6)	2.7216(5)	2.7409(6)	2.7316(6)
O3–H	0.81(1)	0.82(1)	0.87(2)	0.85(2)
O2···H	1.98(1)	1.96(1)	1.97(2)	1.95(2)
O3–H···O2	154(1)	156(1)	149(2)	152(1)

1147 <sup>a</sup> plus corresponding obtuse angles.

1148 **Table 8.** Wavenumber positions of relevant absorption features in FTIR spectra in each  
 1149 measuring mode for the kieserite and szomolnokite endmembers, Mg/Fe(SO<sub>4</sub>)·H<sub>2</sub>O at room  
 1150 temperature. Linear regression coefficients of the correlations between wavenumber and Fe  
 1151 content ( $x_{\text{Fe}}$ ) are listed. Positions of weak yet important bands observed in the region of H<sub>2</sub>O  
 1152 combination modes are given in the scope of DRIFT measurements on undiluted sample material.

<b>Transmission (1:300 sample dilution in KBr)</b>				
<b>Vibration</b>	<b>Wavenumber position (cm<sup>-1</sup>)</b>		<b>Linear regression coefficients<sup>a</sup></b>	
	Kieserite	Szomolnokite	<b>a</b>	<b>b</b>
Peak 850 cm <sup>-1</sup>	884(1)	831(2)	-57.5(1)	887.8(8)
ν <sub>1</sub> (SO <sub>4</sub> )	1043(1)	1015(1)	-29.6(1)	1040(1)
ν <sub>3</sub> (SO <sub>4</sub> ) <sub>main</sub>	1165(1)	1133(1)	-27.8(1)	1162.1(8)
ν <sub>2</sub> (H <sub>2</sub> O)	1525(4)	1496(2)	-32.1(1)	1528.9(8)
ν <sub>1</sub> (H <sub>2</sub> O)	3182(4)	3245(4)	67.2(3)	3188(2)
ν <sub>3</sub> (H <sub>2</sub> O)	3367(12)	3391(10)	1.3(1)	3388(5)
<b>Attenuated Total Reflectance (ATR)</b>				
<b>Vibration</b>	<b>Wavenumber position (cm<sup>-1</sup>)</b>		<b>Linear regression coefficients<sup>a</sup></b>	
	Kieserite	Szomolnokite	<b>a</b>	<b>b</b>
Peak 850 cm <sup>-1</sup>	866(3)	810(1)	-54.7(2)	861(1)
ν <sub>2</sub> (H <sub>2</sub> O)	1520(1)	1491(2)	-30.57(7)	1522.2(4)
ν <sub>1</sub> (H <sub>2</sub> O)	3165(4)	3217(5)	57.5(3)	3157(2)
ν <sub>3</sub> (H <sub>2</sub> O)	3345(8)	3340(10)	0.8(7)	3342(4)
<b>Diffuse Reflectance (1:20 sample dilution in KBr)</b>				
<b>Vibration</b>	<b>Wavenumber position (cm<sup>-1</sup>)</b>		<b>Linear regression coefficients<sup>a</sup></b>	
	Kieserite	Szomolnokite	<b>a</b>	<b>b</b>
Peak 850 cm <sup>-1</sup>	886(3)	839(1)	-57.2(2)	895.4(1)
ν <sub>1</sub> (SO <sub>4</sub> )	1044(2)	1018(1)	-27.6(1)	1042(1)
ν <sub>3</sub> (SO <sub>4</sub> ) <sub>center</sub>	1172(3)	1139(2)	-21.3(2)	1158(2)
ν <sub>2</sub> (H <sub>2</sub> O)	1523(1)	1494(1)	-29.38(6)	1523(4)
ν <sub>1</sub> (H <sub>2</sub> O)	3180(2)	3249(5)	70.8(2)	3180(1)
ν <sub>3</sub> (H <sub>2</sub> O)	3365(13)	3383(21)	1.7(6)	3359(3)
<b>Diffuse Reflectance (undiluted samples)</b>				
<b>Vibration</b>	<b>Wavenumber position (cm<sup>-1</sup>)</b>		<b>Linear regression coefficients<sup>a</sup></b>	
	Kieserite	Szomolnokite	<b>a</b>	<b>b</b>
Peak 600 cm <sup>-1</sup>	690(1)	678(1)	-11.6(1)	688.5(7)
Reststrahlenband	1316(6)	1283(5)	-30.1(2)	1312(1)
ν <sub>2</sub> (H <sub>2</sub> O)	1526(3)	1496(2)	-30.7(3)	1528(2)
ν <sub>1</sub> (H <sub>2</sub> O)	3203(20)	3304(9)	88.8(1)	3209(5)
ν <sub>3</sub> (H <sub>2</sub> O)	3412(23)	3431(9)	2.3(1)	3405(6)
Peak 4700 cm <sup>-1</sup>	4688(4)	4749(5)	---	---
Peak 4850 cm <sup>-1</sup>	4845(3)	4854(6)	---	---
Peak 5090 cm <sup>-1</sup>	5087(10)	5021(11)	---	---

1153 <sup>a</sup>Linear regression equation  $y = \mathbf{a}(x_{\text{Fe}}) + \mathbf{b}$ , where  $y$  denotes the wavenumber position of the vibration mode.

1154 **Table 9.** Wavenumber shift positions of relevant bands in Raman spectra for the kieserite and  
 1155 szomolnokite endmembers, Mg/Fe(SO<sub>4</sub>)·H<sub>2</sub>O. Linear regression coefficients of the correlations  
 1156 between band position and the Fe content ( $x_{\text{Fe}}$ ) are listed. Additionally, changes in the band  
 1157 position with decreasing temperature are given for all relevant Raman bands.  
 1158

Peak assignment	Raman shift position at RT (cm <sup>-1</sup> )		Linear regression coefficients <sup>a</sup>		Band shift with temperature decrease (×10 <sup>-2</sup> cm <sup>-1</sup> / °C)
	Kieserite	Szomolnokite	a	b	
Lattice modes	125.3(1)	112.4(4)	-10.7(6)	123.7(3)	4.66
$\nu_{\text{transl Fe-H}_2\text{O}}$	219.2(1)	218.0(1)	-0.4(5)	219.2(3)	3.43
$\nu_2(\text{SO}_4)_1$	432.2(1)	422.8(1)	-9.4(3)	432.2(2)	-1.95
$\nu_2(\text{SO}_4)_2$	502.1(1)	493.8(1)	-7.2(3)	501.2(2)	-1.61
$\nu_4(\text{SO}_4)_1$	628.7(4)	616.6(2)	-11.78(4)	628.1(2)	0.85
$\nu_4(\text{SO}_4)_2$	633.8(2)	623(1)	-10.1(5)	633.0(3)	-0.55
$\nu_1(\text{SO}_4)$	1041.8(1)	1017.6(1)	-24.9(1)	1040.9(6)	-0.47
$\nu_3(\text{SO}_4)_1$	1101.6(1)	1071.0(5)	-28.7(1)	1101.2(8)	-1.82
$\nu_3(\text{SO}_4)_2$	1118.9(1)	1090.4(7)	-29.1(1)	1121(1)	-0.51
$\nu_3(\text{SO}_4)_3$	1216.7(1)	1195.0(1)	-22.0(9)	1215(5)	2.22
$\nu_2(\text{H}_2\text{O})$	1508.3(1)	1477.6(1)	-27.1(3)	1501(2)	2.22
$\nu_1(\text{H}_2\text{O})$	3178(2)	3247(5)	53.0(6)	3189(4)	-16.57
$\nu_3(\text{H}_2\text{O})$	3388(4)	3368(12)	-9(1)	3372(6)	15.25

1159 <sup>a</sup> Linear regression equation  $y = \mathbf{a}(x_{\text{Fe}}) + \mathbf{b}$ , where  $y$  denotes the Raman shift position.  
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1174 **Table 10.** Summary of results from classical crystal field (CF) and superposition model (SM)  
1175 calculations for Fe<sup>2+</sup> in szomolnokite, based on observed transitions energies as indicated in Fig.  
1176 15. Fixed SM parameters are  $R_0=2.13 \text{ \AA}$ ,  $t_4=5$ ,  $t_2=3$ . All given values are in  $\text{cm}^{-1}$  except the ratio  
1177 C/B (fixed at 4.3) and the nephelauxetic ratio  $\beta$ . Racah B<sub>0</sub> and C/B are taken from Figgis and  
1178 Hitchman (2000).

1179

Szomolnokite	SM (triclinic)	'classical' CF (tetragonal)
Dq <sub>cub</sub>	—	855
Dq <sub>eq</sub>	—	878
Dt	—	40
Ds	—	660
Racah B (C/B=4.3)	835	840
$\beta$ (B <sub>0</sub> =897 $\text{cm}^{-1}$ )	0.93	0.94
Dq <sub>cub</sub> (from s <sub>4</sub> )	826	855
$\bar{B}_4$	4920	—
$\bar{B}_2$	8900	—
s <sub>4</sub>	7573	7838
s <sub>2</sub>	2319	2066

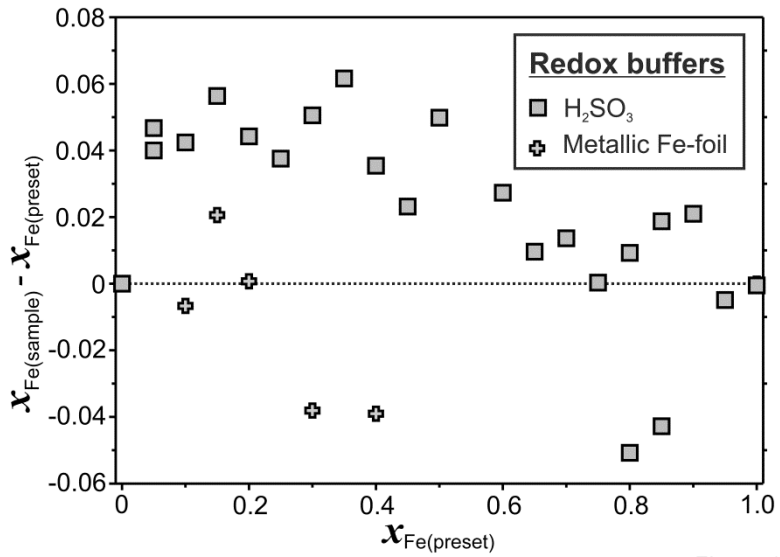
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1182 **Figures**

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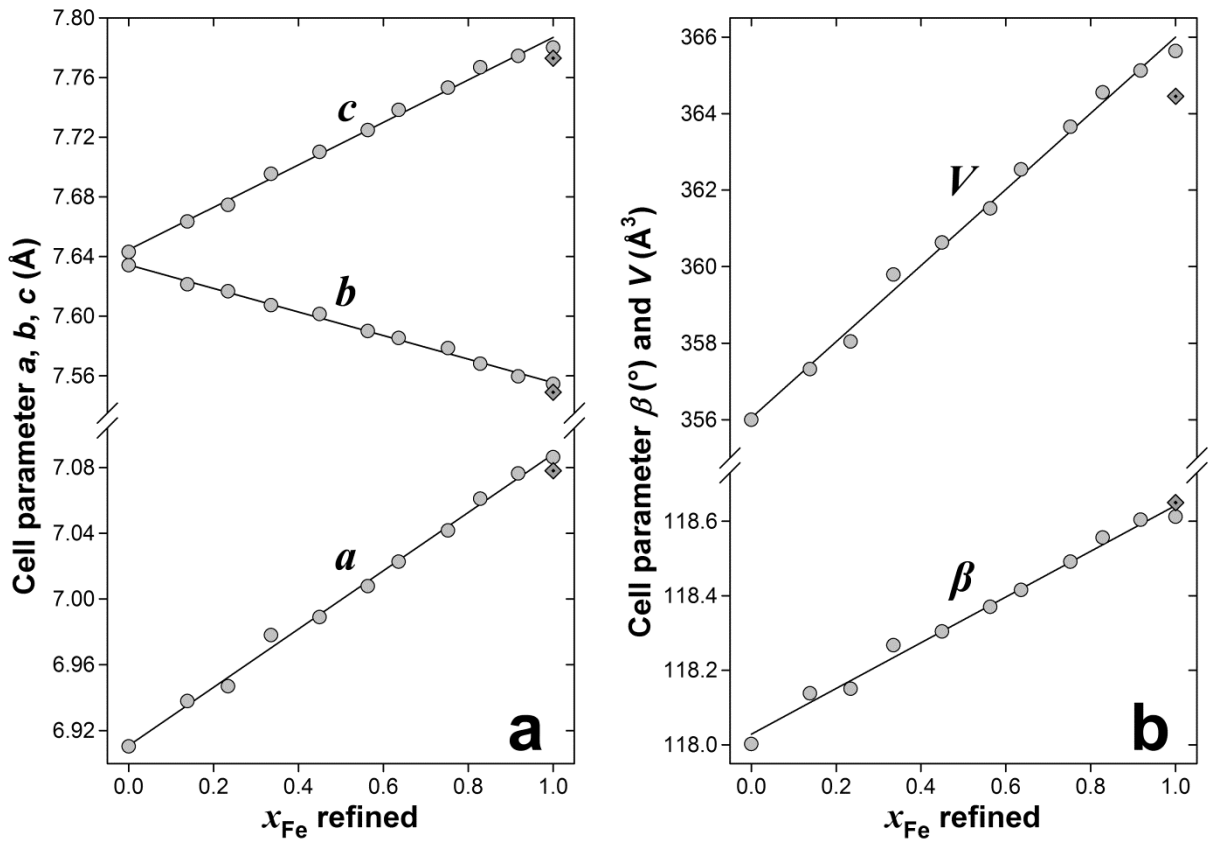
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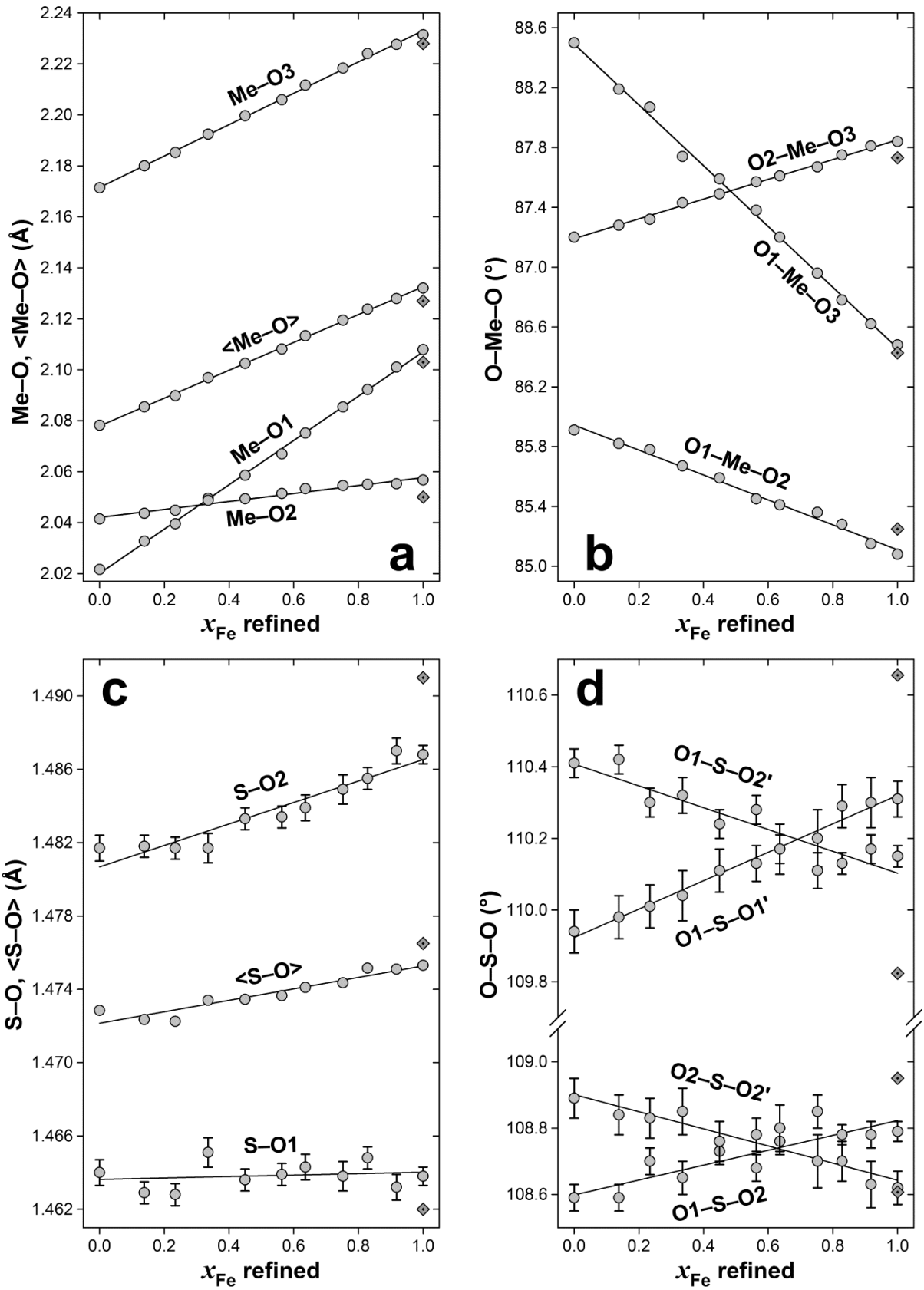


Figure 3

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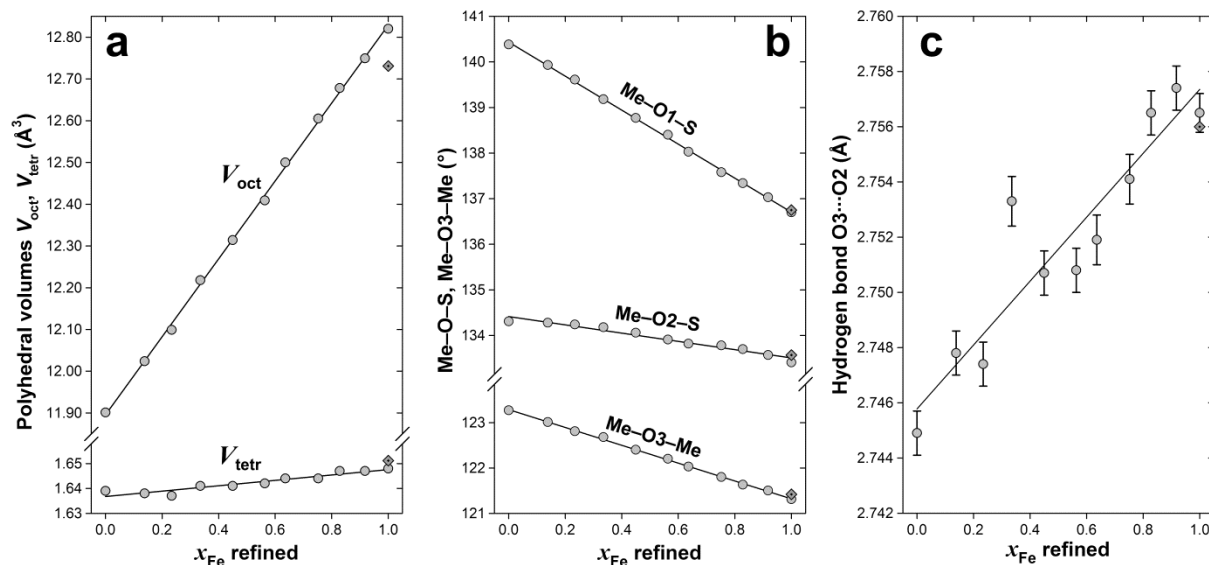


Figure 4

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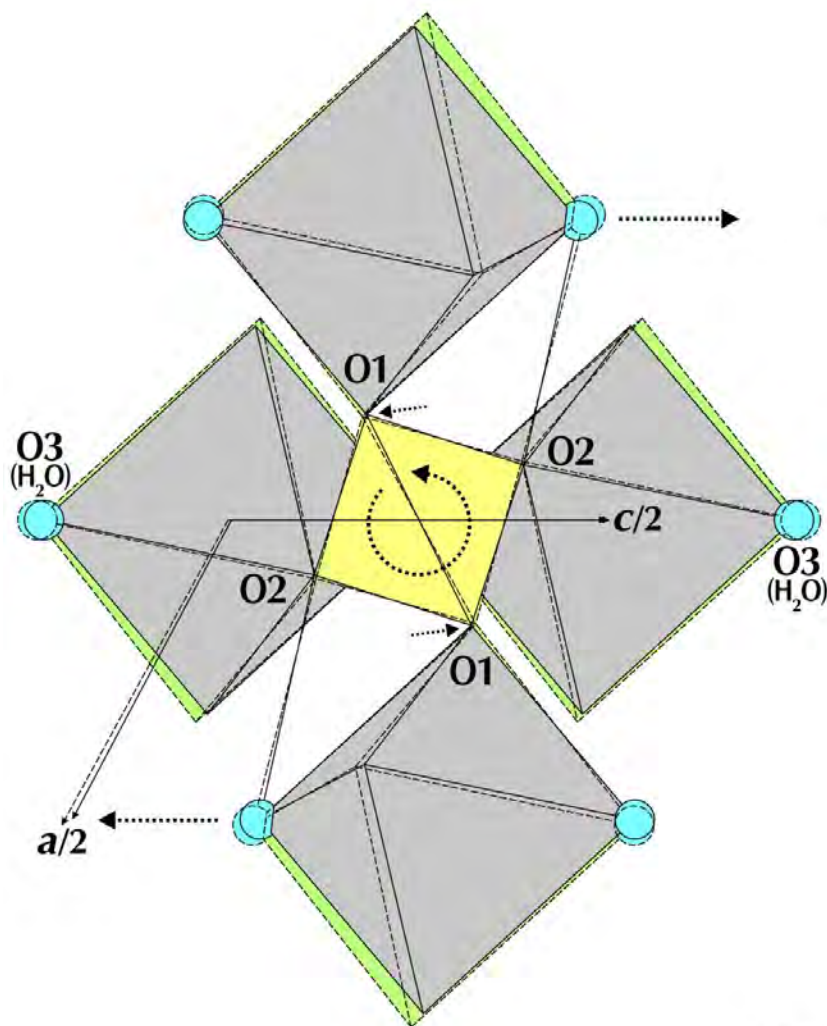


Figure 5

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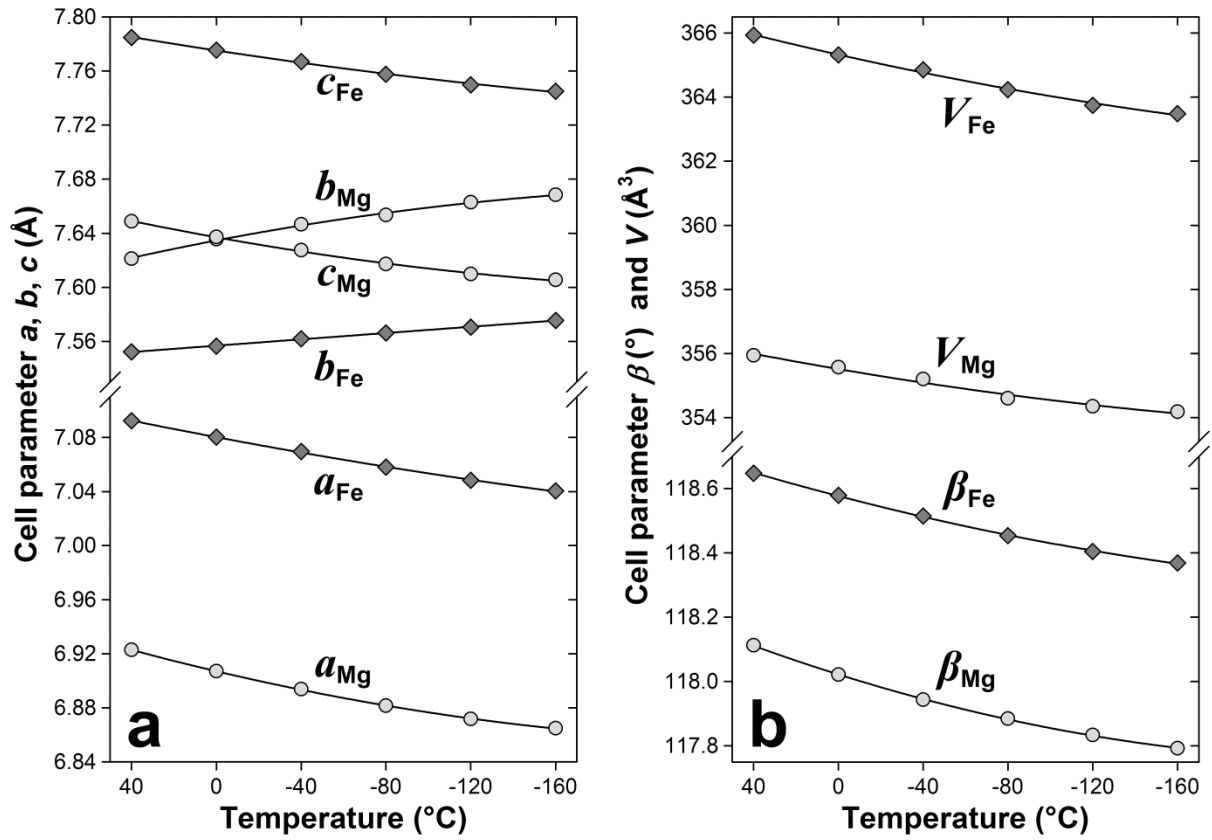


Figure 6

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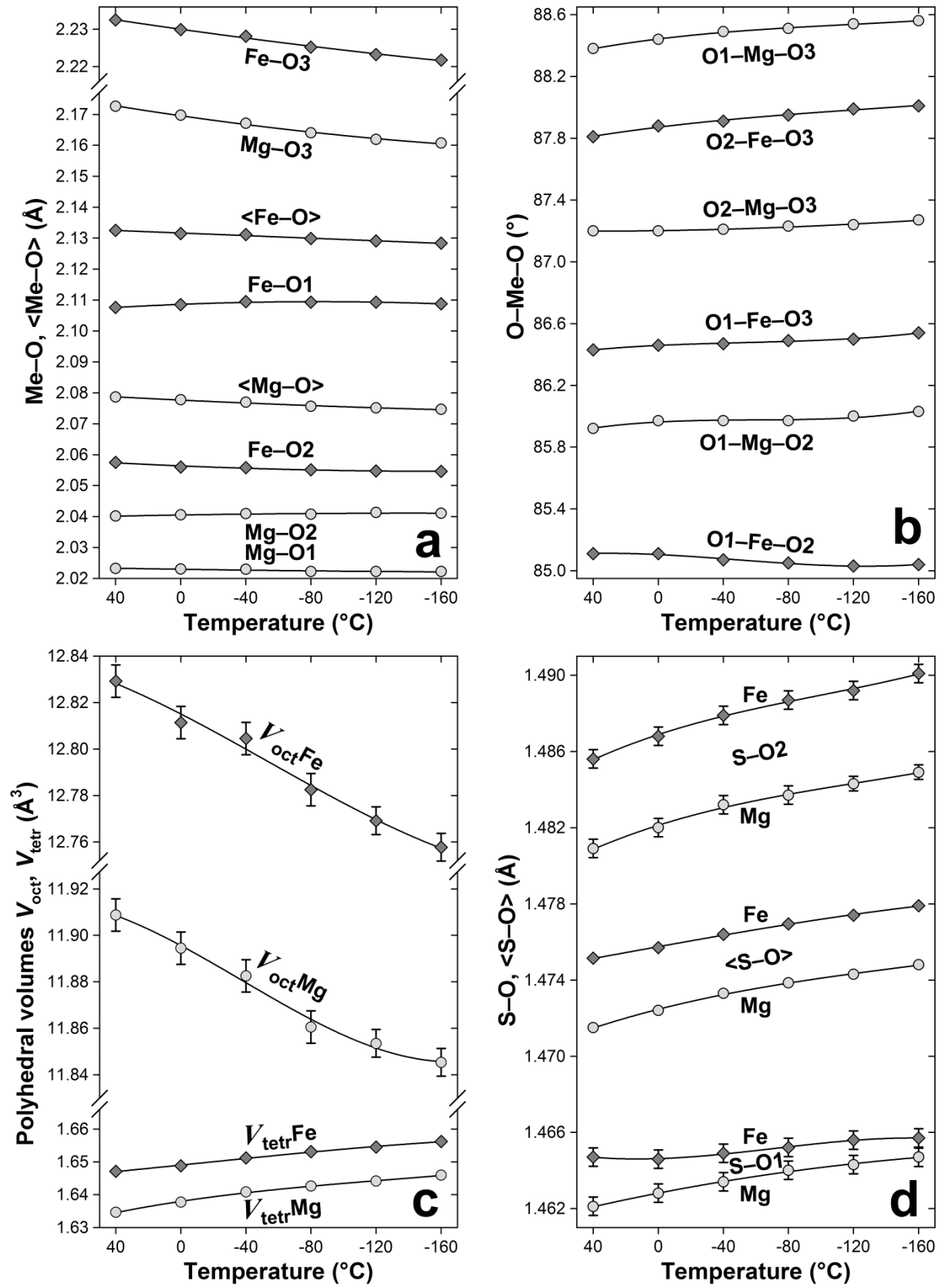


Figure 7

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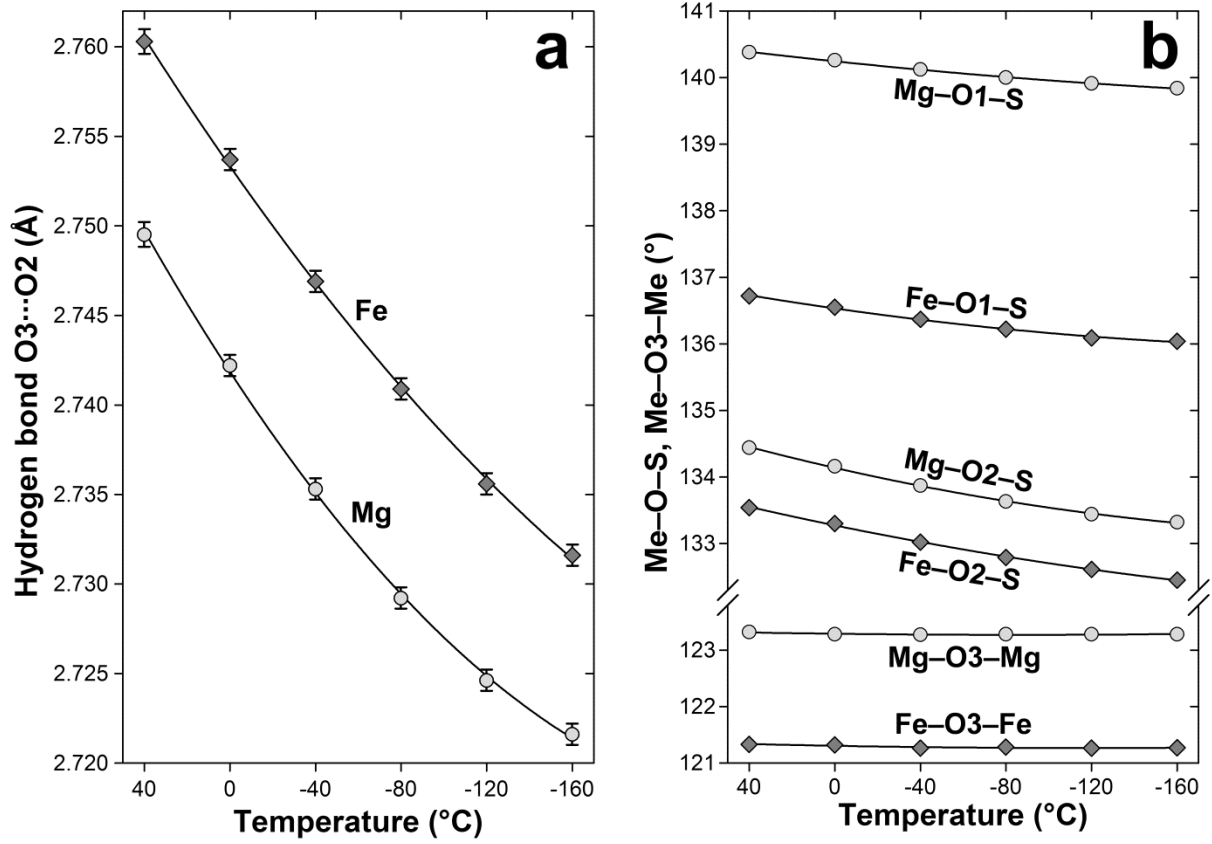


Figure 8

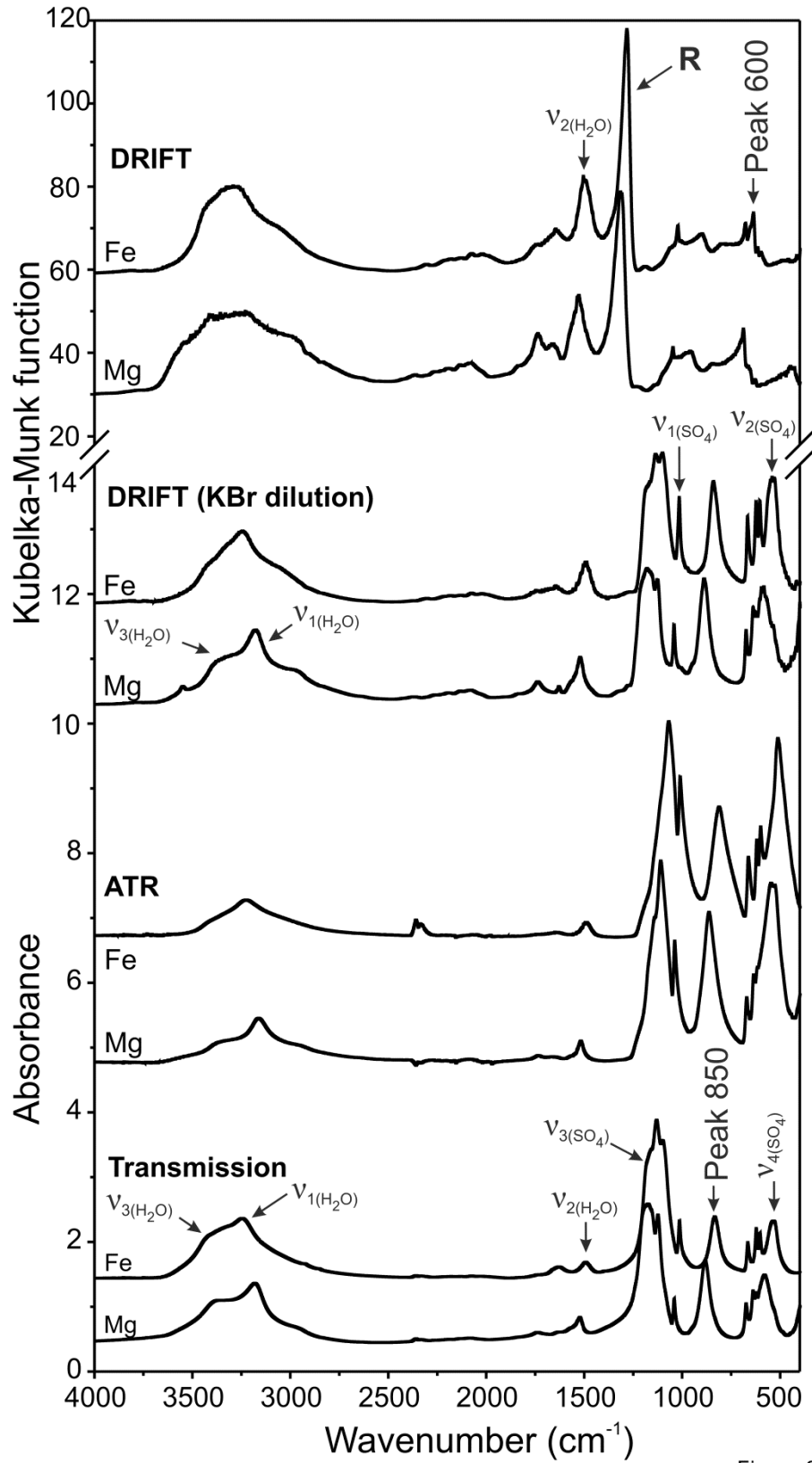
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Figure 9

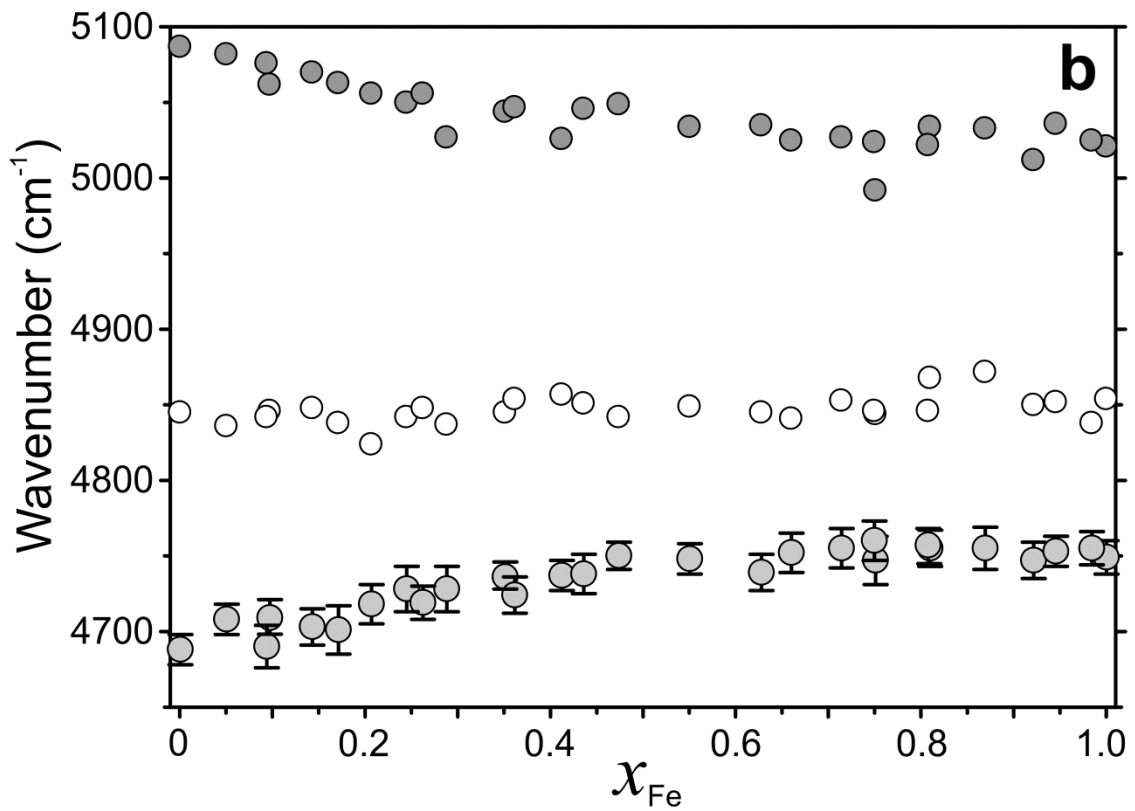
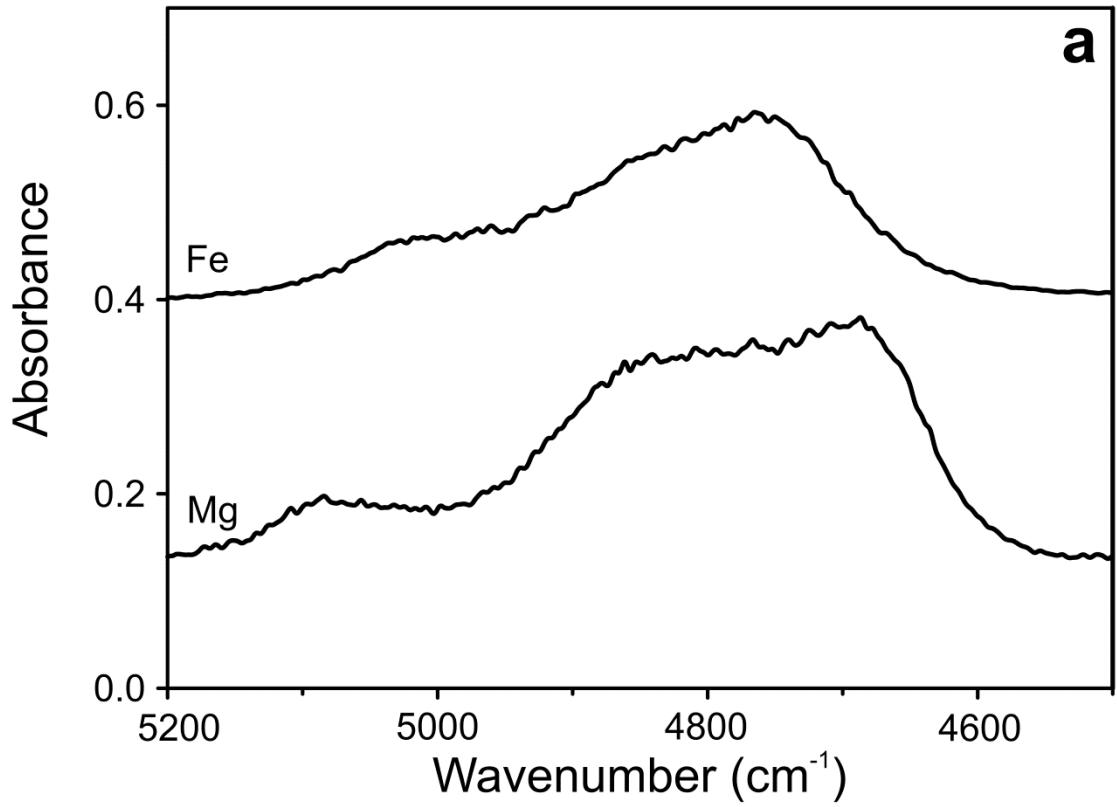


Figure 10

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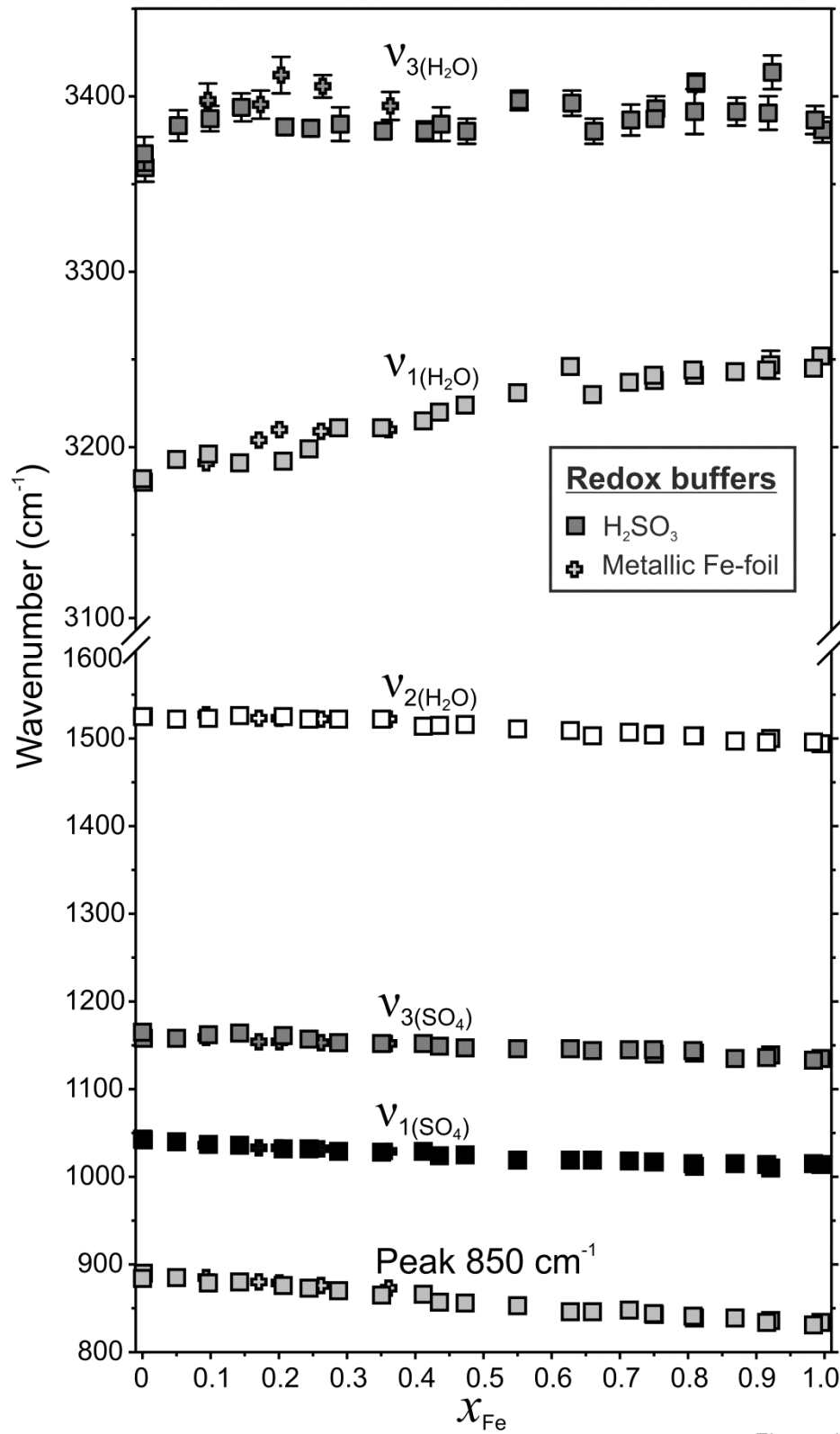


Figure 11

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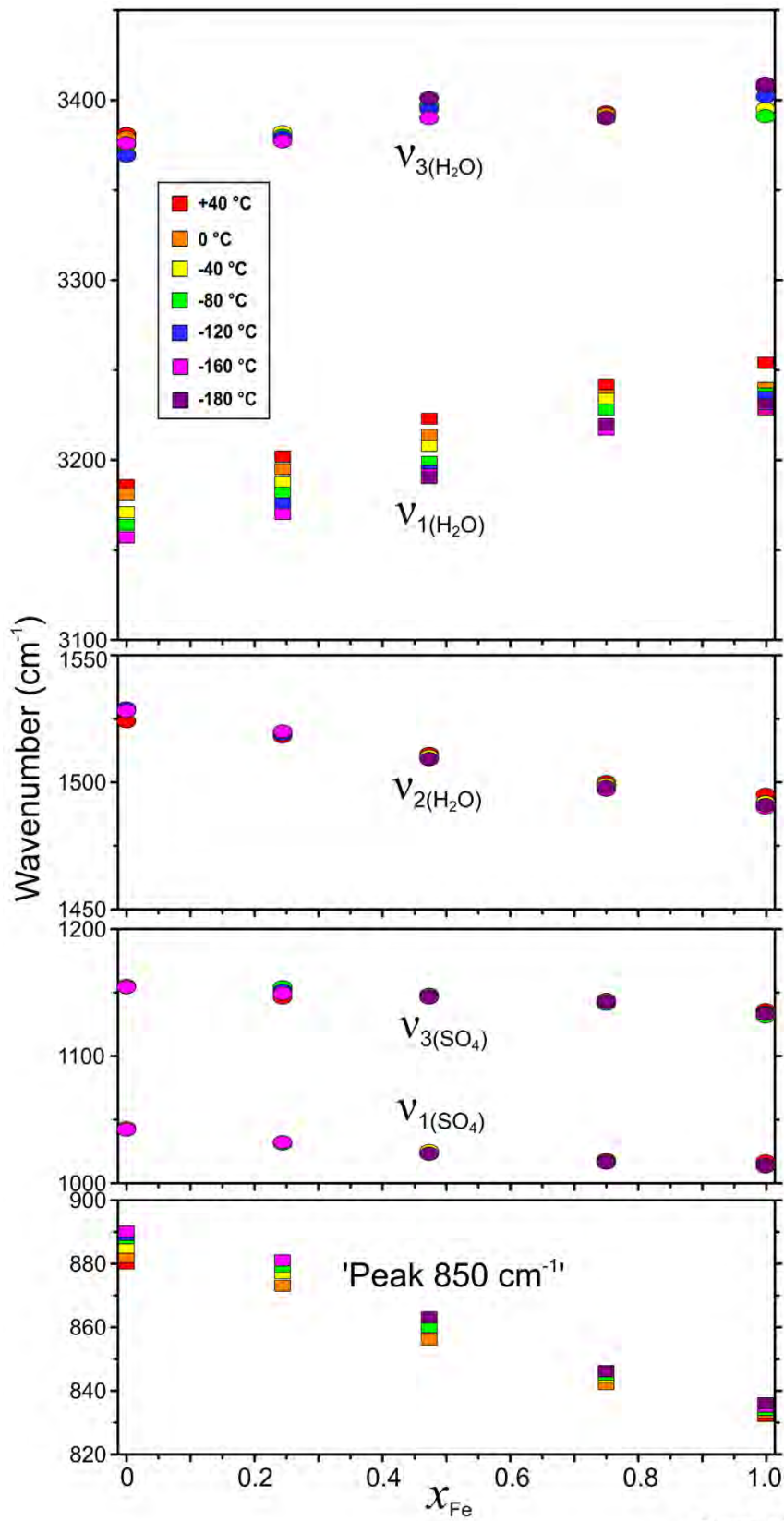


Figure 12

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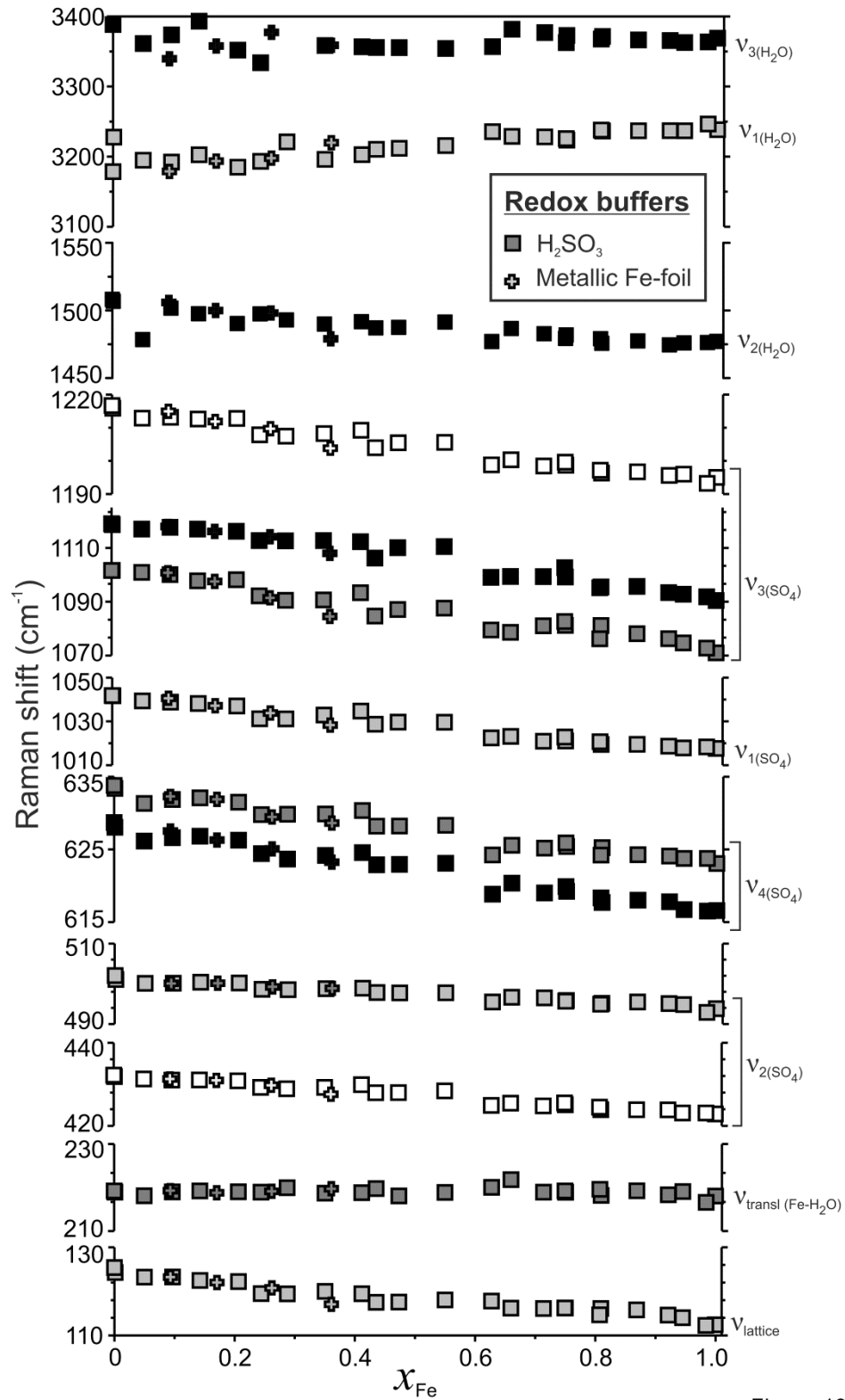


Figure 13

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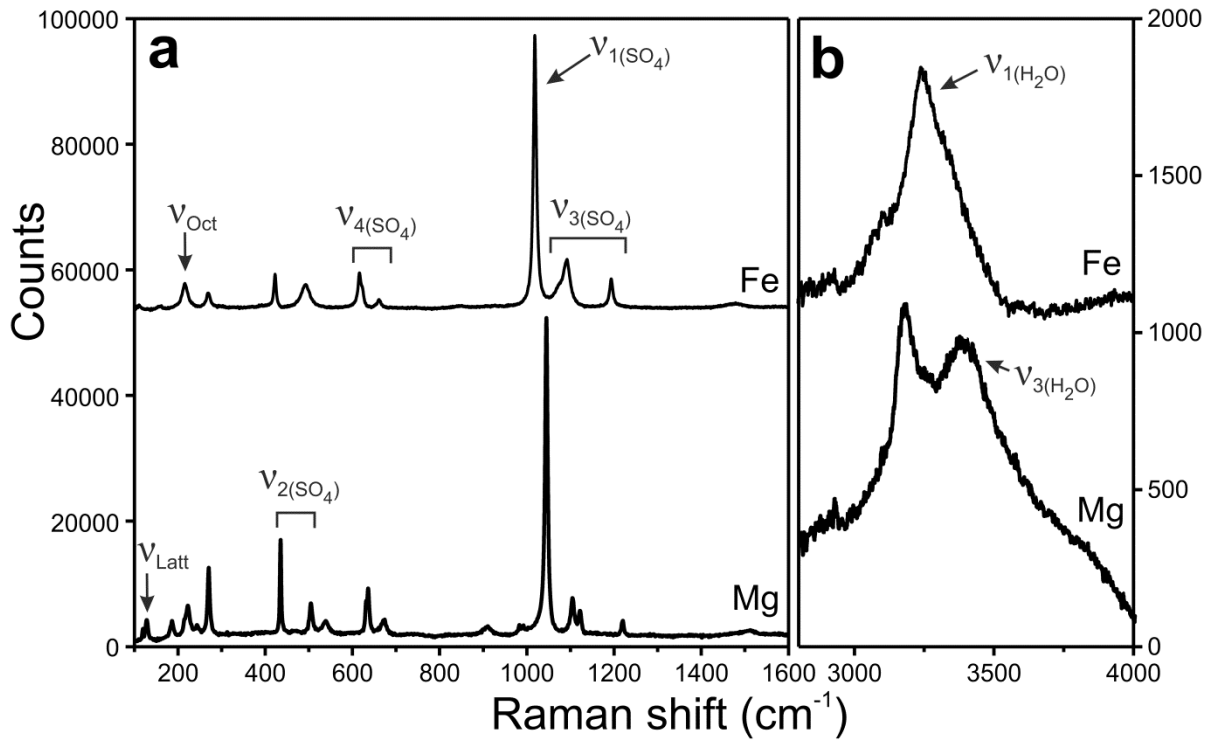


Figure 14

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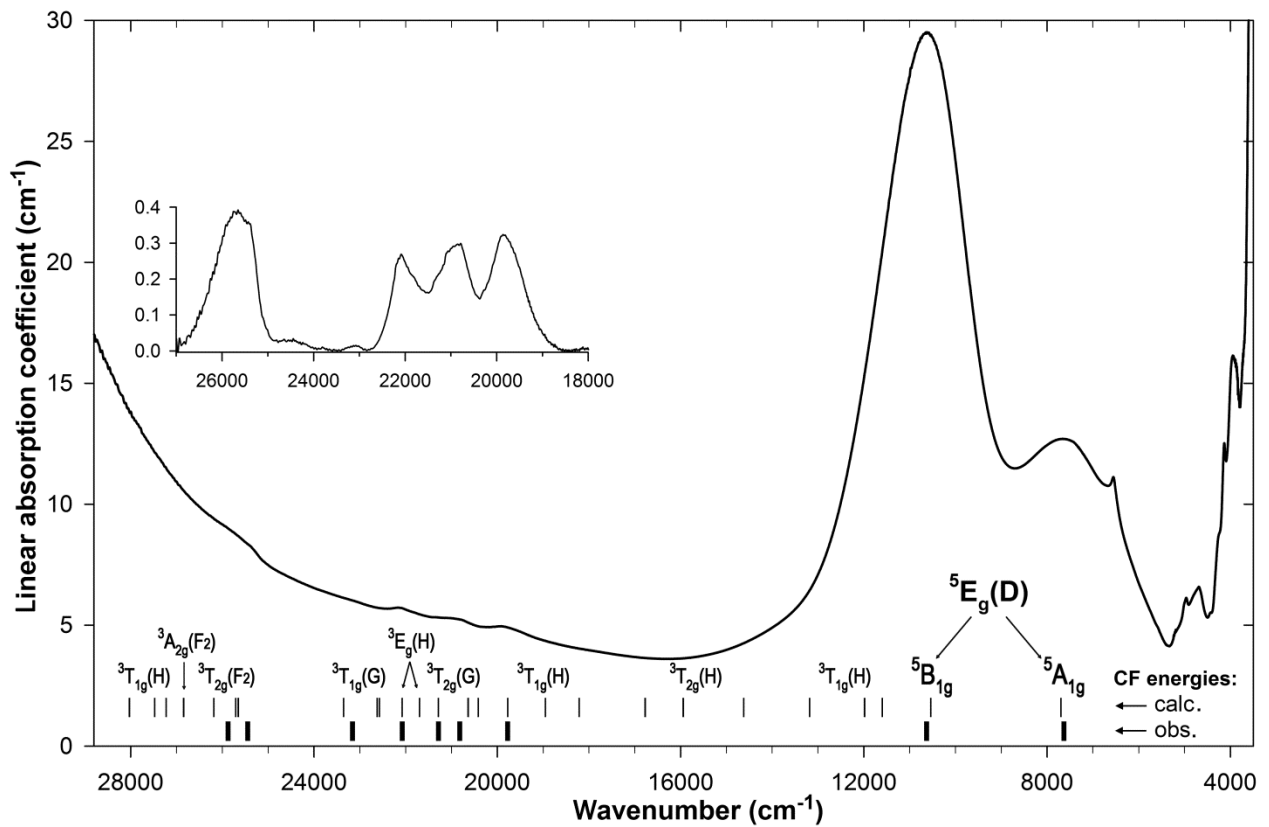


Figure 15

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