

1 **Revision 4**

2 **Valleyite: A new magnetic mineral with the sodalite-type structure**

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## ABSTRACT

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Valleyite,  $\text{Ca}_4(\text{Fe,Al})_6\text{O}_{13}$ , is a new sodalite-type mineral discovered in late Pleistocene basaltic scoria from the Menan Volcanic Complex near Rexburg, Idaho, USA. It is an oxidation product of basaltic glass during the early stage of the scoria formation and is associated with hematite ( $\alpha\text{-Fe}_2\text{O}_3$ ), maghemite ( $\gamma\text{-Fe}_2\text{O}_3$ ), luogufengite ( $\varepsilon\text{-Fe}_2\text{O}_3$ ) and quartz on the surface of vesicles. The measured crystal size of valleyite ranges from  $\sim 250$  nm to  $\sim 500$  nm. The empirical chemical formula of valleyite is  $(\text{Ca}_{3.61}\text{Mg}_{0.39})(\text{Fe}_{3.97}\text{Al}_{1.91}\text{Ti}_{0.09})\text{O}_{13}$ . The mineral has a space group of  $I\bar{4}3m$ ; its unit-cell parameter refined from synchrotron X-ray powder diffraction data is:  $a = 8.8852(7)$ , unit cell volume =  $701.46(17) \text{ \AA}^3$ , and  $Z = 2$ . The seven strongest lines of the obtained X-ray diffraction pattern [ $d(\text{\AA})(I)(hkl)$ ] are:  $6.287(43.1)(011)$ ;  $4.4395(5.3)(002)$ ;  $3.6284(100)(112)$ ;  $3.1395(5.2)(022)$ ;  $2.8011(36.5)(013)$ ;  $2.5644(29.4)(222)$ ; and  $2.3750(31.5)(123)$ . The (Fe,Al)-O bond distance and unit cell edge are slightly larger than those reported for synthetic  $\text{Ca}_4\text{Al}_6\text{O}_{13}$ , presumably due to the presence of the larger  $\text{Fe}^{3+}$  cations, compared with  $\text{Al}^{3+}$ , in the structure. Density functional theory calculations predict that valleyite may be a metastable phase at low temperatures. Measured Curie temperatures for valleyite and luogufengite are 645K and 519K, respectively. Their magnetization hysteresis loop indicates the magnetic exchange coupling between valleyite (soft magnet) and luogufengite (hard magnet), which aids in the understanding of magnetic properties and paleo-magnetism of basaltic rocks. This new mineral, valleyite, with the sodalite-type cage structure is potentially a functional magnetic material.

47 **Keywords:** Valleyite, Sodalite-type structure, Luogufengite, Hematite, Scoria, Magnetic property,  
48 synchrotron X-ray diffraction, Transmission electron microscopy

## 49 INTRODUCTION

50 The new nano-mineral, valleyite, was discovered in late Pleistocene (~10,000 years)  
51 basaltic scoria from the Menan Volcanic Complex near Rexburg, Idaho, USA. The Menan  
52 Volcanic Complex consists of broad, flat volcanoes, formed by low-viscosity eruptions, with  
53 tholeiitic basalts dominating the surface exposures (Russell and Brisbin, 1990; Hackett and  
54 Morgan, 1988; Hughes et al. 1999). The formation of scoria was related to the interaction of  
55 external water with the late-stage (late Pleistocene) eruption in the center of the Menan complex  
56 (Hackett and Morgan, 1988; Hughes et al. 1999). In general, the scoria with a brown and dark  
57 color contains more valleyite nano-grains than the red scoria.

58 In this study, the crystal structure, chemical composition, and magnetic properties of  
59 valleyite are presented. The mineral name has been approved by the Commission on New  
60 Minerals, Nomenclature and Classification (CNMNC) of the International Mineralogical  
61 Association, (IMA 2017-026) (Xu et al. 2017a). The newly discovered mineral species of  
62  $\text{Ca}_4(\text{Fe,Al})_6\text{O}_{13}$  is named after Prof. John W. Valley (born in 1948) of the University of  
63 Wisconsin – Madison. Prof. Valley was the President of the Mineralogical Society of America  
64 (MSA) during 2005-2006. His groundbreaking contributions to mineralogy, petrology, and  
65 geochemistry have led to a deeper understanding of Earth's crustal evolution from early Earth to  
66 the Anthropocene. Valleyite is deposited in the collection of the Geology Museum of the  
67 Department of Geoscience, University of Wisconsin-Madison, with specimen numbers UWGM  
68 2352 and UWGM2353.

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## 70 SAMPLES AND METHODS

71 The samples were carefully scratched off from the vesicles' surfaces of the collected

72 basaltic scoria (Supplementary Fig. S1). These samples were placed in a 10M NaOH solution at  
73 80 °C for 2 days to remove the silicate glass by following previous procedures (Xu et al. 2017b;  
74 Lee et al. 2018). After washing the sample powders with distilled water several times, valleyite  
75 was enriched using a magnetic bar to reduce the portion of non-magnetic minerals. The valleyite  
76 sample was further enriched by an iron needle to pick up the remnant magnetized crystals. These  
77 magnetic enrichment steps were repeated 5-7 times.

78 For comparison, a synthetic valleyite sample was prepared through thermal  
79 decomposition of a clay mineral, nontronite, from Quincy, WA, as described in Lee and Xu  
80 (2016). Crushed nontronite powders were loaded into an alumina boat, which was then placed in  
81 a furnace to be heated at 850 °C for 2 days in air. After heating, the sample was quenched in cold  
82 water. Isolation of the ferric oxides from amorphous SiO<sub>2</sub> was performed by dissolving the  
83 sample in a 10 M NaOH solution at 80 °C for 2 days. After washing with distilled water several  
84 times, synthetic valleyite, together with luogufengite and hematite, was obtained. The synthetic  
85 valleyite can also be enriched using the magnetic enrichment steps for natural valleyite,  
86 described above.

87 High-resolution X-ray powder diffraction data were collected at beamline 11-BM of the  
88 Advanced Photon Source (APS) at Argonne National Laboratory. Diffraction patterns were  
89 recorded using a wavelength ( $\lambda$ ) of 0.414631 Å for the natural sample and of 0.414584 Å for the  
90 synthetic sample. Finely ground powders of the samples were placed into polyimide tubes with  
91 an inner diameter of 1 mm for the synchrotron XRD measurements. The sample-to-detector  
92 distance and beam center position were calibrated using a LaB<sub>6</sub> standard. Diffraction data of an  
93 empty polyimide tube were collected for background removal in the data reduction. The crystal  
94 structure of valleyite and the ratios of mineral phases presented in the sample were determined

95 with the Rietveld method using the MDI JADE 9 software. A pseudo-Voigt function was used to  
96 fit the peak profiles, accounting for the effects of nano-grain broadening and lattice strains.  
97 Positions for the Fe and one oxygen atom (O<sub>2</sub>) in valleyite are at special positions. Because the  
98 sample contains only ~10 wt.% of valleyite, it is not possible to accurately refine the  $U_{\text{iso}}$  values.  
99 Thus we fixed the  $U_{\text{iso}}$  values at those for the synthetic Ca<sub>4</sub>Al<sub>6</sub>O<sub>13</sub> phase reported by Peters et al.  
100 (2007).

101         Bright-field and dark-field transmission electron microscopy (TEM) images, high-  
102 resolution TEM (HRTEM) images, and selected-area electron diffraction (SAED) patterns were  
103 obtained using a Philips CM200-UT microscope operated at 200 kV. TEM samples were  
104 prepared by depositing a suspension of the enriched samples on a lacy carbon-coated Cu grid.  
105 The chemical composition was obtained using a TEM-EDS system equipped with a Li-drifted Si  
106 detector (Oxford instruments Link ISIS). An electron beam diameter of ~50 nm was used for  
107 collecting X-ray EDS spectra with fayalite, anorthite, forsterite, and titanite as the standards to  
108 quantify the element fractions of Fe, Ca, Al, Mg, and Ti in the samples.

109         Magnetic hysteresis loops of the powder samples were obtained using a superconducting  
110 quantum interference device (SQUID) magnetometer (MPMS 3, Quantum Design). The  
111 measurements were conducted under applied magnetic fields of -1 to 1 Tesla at room  
112 temperature. From 300K to 1000 K, the thermal evolution of magnetization has been measured  
113 under an applied 1 kOe in a Lakeshore Vibrating Sample Magnetometer (VSM).

114         To study the stability of valleyite, we conducted theoretical calculations using density  
115 functional theory (DFT) as implemented in the Vienna Ab Initio Simulation Package (VASP)  
116 (Kresse and Furthmüller, 1996). An end-member valleyite Ca<sub>4</sub>Fe<sub>6</sub>O<sub>13</sub> supercell containing two  
117 formula units (46 atoms) and multiple valleyite (Ca<sub>3.5</sub>Mg<sub>0.5</sub>)(Fe<sub>4</sub>Al<sub>2-x</sub>Ti<sub>x</sub>)O<sub>13</sub> ( $x = 0, 0.125, 0.5$ )

118 supercells containing two formula units (46 atoms,  $x = 0$  and 0.5) and 16 formula units (368  
119 atoms,  $x = 0.125$ ) were simulated in the sodalite-type structure (space group  $I\bar{4}3m$ ). We used  
120 projector augmented wave (PAW)-type (Kresse and Joubert, 1999) pseudopotentials fit for the  
121 Perdew-Burke-Ernzerhof (PBE) (Perdew et al. 1996) generalized gradient approximation (GGA)  
122 exchange-correlation functional. We used the PBE GGA exchange-correlation functional with  
123 Hubbard  $U$  correction (GGA+ $U$ ) (Anisimov et al. 1997) with  $U = 5.3$  eV for the Fe atoms,  
124 consistent with the value used in the Materials Project database (Jain et al. 2013). A planewave  
125 energy cutoff of 500 eV was used and all calculations were performed with spin polarization  
126 enabled. Both ferromagnetic and antiferromagnetic spin configurations were simulated. For the  
127 antiferromagnetic configuration, the magnetic moments were ordered to contain an equal number  
128 of up and down spins on Fe-containing  $\{100\}$  planes. For the case of  $(\text{Ca}_{3.5}\text{Mg}_{0.5})(\text{Fe}_4\text{Al}_{2-x}\text{Ti}_x)\text{O}_{13}$   
129  $(x = 0)$ , four different antiferromagnetic spin orderings were considered to test the effect  
130 of spin ordering on the total energy. The energy variation with different antiferromagnetic  
131 orderings was found to be  $\sim 20$  meV/Fe, which is small and on the order of  $kT$  at room  
132 temperature. For the composition of  $(\text{Ca}_{3.5}\text{Mg}_{0.5})(\text{Fe}_4\text{Al}_{2-x}\text{Ti}_x)\text{O}_{13}$  ( $x = 0$ ), 4 different Mg  
133 configurations on the (Ca, Mg) sublattice and 5 different Al configurations on the (Fe, Al)  
134 sublattice were performed, and for the composition  $(\text{Ca}_{3.5}\text{Mg}_{0.5})(\text{Fe}_4\text{Al}_{2-x}\text{Ti}_x)\text{O}_{13}$  ( $x = 0.5$ ), 4  
135 different Ti configurations on the (Al, Ti) sublattice were performed in order to assess the impact  
136 of the configuration of minor alloying cations on the calculated stability. Overall, it was found  
137 that the impact of alloying element configuration on the total energy is small, on the order of  $\sim 50$   
138 meV/Mg,  $\sim 35$  meV/Al and  $\sim 100$  meV/Ti for Mg, Al and Ti alloying, respectively. These total  
139 energy differences arising from different alloying cation configurations resulted in very small  
140 differences in calculated stability and formation energies, typically  $< 5$  meV/atom. Brillouin zone

141 sampling was performed with the Monkhorst-Pack scheme with a  $4\times 4\times 4$   $k$ -point mesh (46 atom  
142 supercells) and  $2\times 2\times 2$   $k$ -point mesh (368 atom supercell) (Monkhorst and Pack, 1976). All key  
143 input/output calculation files are included as part of the supplementary materials, including  
144 relaxed structures, calculated total energies and magnetic moments.

145 Stability calculations were performed using convex hull analysis of the DFT-calculated  
146 total energies as implemented in the Pymatgen (Ong et al. 2013) toolkit assuming a system open  
147 to oxygen and ambient conditions of  $T = 298$  K and  $p(\text{O}_2) = 0.2$  atm following previous work  
148 (Jacobs et al. 2018). These conditions result in an oxygen chemical potential of  $\mu_{\text{O}} = -5.25$  eV/O,  
149 which was calculated using experimental thermochemical data and standard DFT  
150 thermochemistry equations following previous work (Jacobs et al. 2012). In addition to convex  
151 hull analysis as a probe of the material stability, we also calculated the formation energy of  
152 valleyite relative to decomposition to its constituent binary oxides of the same oxidation states.  
153 For example, for the case of  $(\text{Ca}_{3.5}\text{Mg}_{0.5})(\text{Fe}_4\text{Al}_{2-x}\text{Ti}_x)\text{O}_{13}$  ( $x = 0.5$ ), the reaction formation energy  
154 of  $3.5\text{CaO} + 0.5\text{MgO} + 2\text{Fe}_2\text{O}_3 + 0.75\text{Al}_2\text{O}_3 + 0.5\text{TiO}_2 \rightarrow (\text{Ca}_{3.5}\text{Mg}_{0.5})(\text{Fe}_4\text{Al}_{1.5}\text{Ti}_{0.5})\text{O}_{13} +$   
155  $0.125\text{O}_2$  was calculated using DFT-calculated binary oxide energies tabulated in the Materials  
156 Project database. Note that these oxide reference states are all modelled as ferromagnetic. The  
157 formation energies are included as a second stability metric in addition to convex hull analysis  
158 based on recent work (Ye et al. 2018) claiming that convex hull analysis can yield results that  
159 vary unpredictably even for similar materials chemistries.

160

## 161 **RESULTS AND DISCUSSION**

162 The synchrotron XRD pattern of a treated scoria sample reveals the occurrence of  
163 valleyite, together with luogufengite, hematite, calcite, and quartz (Fig. 1). Major peaks from

164 valleyite that occur at the low-angle side can be clearly resolved (Fig. 1). Table 1 lists the  
165 diffraction peaks of valleyite. The diffraction peaks from valleyite are sharper than those from  
166 nanophase luogufengite, which has a smaller average size (40 nm).

167 The nano-crystals of valleyite were characterized using HRTEM and SAED (Figs. 2 and  
168 3). The size of valleyite crystals ranges from ~250 nm to ~500 nm. SAED patterns indicate that  
169 valleyite has cubic ( $I\bar{4}3m$ ) symmetry. The mineral displays crystallographic forms of {100},  
170 {111}, and  $\{1\bar{1}1\}$  (Figs. 2, 3). Its morphology is illustrated in supplementary materials (Figure  
171 S2). The chemical formula,  $(\text{Ca}_{3.61}\text{Mg}_{0.39})(\text{Fe}_{3.97}\text{Al}_{1.91}\text{Ti}_{0.09})\text{O}_{13}$ , was calculated from X-ray EDS  
172 spectra (Table 2). A representative X-ray EDS spectrum from valleyite is illustrated in figure 3e.

173 The crystal structure was determined based on an input model of synthetic sodalite-like  
174 phase  $\text{Ca}_4\text{Al}_6\text{O}_{13}$  (Peters et al. 2007) with our EDS-measured formula (Table 2) using Rietveld  
175 analysis. Fractional coordinates, occupancies and isotropic displacement parameters of all the  
176 atoms are listed in Table 3. The structure of valleyite consists of a framework of corner-sharing  
177  $(\text{Fe,Al})\text{O}_4$  tetrahedra with  $\text{Ca}^{2+}$  cations occupying the cavities (Fig. 4). Comparisons among  
178 sodalite (Hassan et al., 2004), synthetic  $\text{Ca}_4\text{Al}_6\text{O}_{13}$  (Peters et al., 2007), and valleyite are  
179 illustrated in Figure 5. The structures with different sizes of tetrahedra display a different degree  
180 of distortion in their di-trigonal rings (Fig. 5). The  $(\text{Fe,Al})\text{-O}$  bond distance and unit cell edge are  
181 slightly larger than those reported for synthetic  $\text{Ca}_4\text{Al}_6\text{O}_{13}$  due to the presence of the larger  $\text{Fe}^{3+}$   
182 cations, compared with  $\text{Al}^{3+}$ , in the structure (Table. 4).

183 The synthetic valleyite, together with  $\varepsilon\text{-Fe}_2\text{O}_3$  (synthetic luogufengite) and  $\alpha\text{-Fe}_2\text{O}_3$   
184 (synthetic hematite), were obtained from thermal decomposition of a Fe(III)-dominated clay  
185 mineral of nontronite (see Figure S3 in supplementary materials). The synthetic phases have  
186 approximately the same particle sizes as their natural phase counterparts, based on the similar



187 FWHMs (Full Width at Half Maximum) of their XRD peaks.

188 Valleyite is a magnetic material because it can be readily picked up and enriched  
189 together with luogufengite from pre-magnetized powders using an iron needle. Figure 6 shows  
190 evolution of magnetization of the treated sample from 300 to 1000 K, indicating Curie  
191 temperatures for luogufengite and valleyite are 519K and 645K and, respectively. The Curie  
192 temperature for luogufengite is very close to a reported value of a synthetic Al-bearing  $\epsilon$ -Fe<sub>2</sub>O<sub>3</sub>  
193 (Nanai et al., 2009). The magnetization of valleyite is estimated to be ~9.2 emu/g at room  
194 temperature based on the ~0.9 emu/g demagnetization of 9.8(3) wt. % valleyite in the analysed  
195 sample. The magnetic transitions are relatively wide, which can be attributed to the large particle  
196 size distribution (Tucek et al. 2010). The remaining magnetic signal above 645 K is associated  
197 with canted antiferromagnetic hematite (López-Sánchez et al. 2016).

198 The magnetic hysteresis loop of the treated sample (a mixture of luogufengite, hematite,  
199 and valleyite with a small amount of calcite and quartz; Figure 1) shows a coercive field of 0.17  
200 Tesla (T) with a remnant magnetism of ~9.5 emu g<sup>-1</sup> at room temperature (Figure 7). The shape  
201 of the hysteresis loop is typical of an exchange coupled phase of magnetically hard and soft  
202 magnets, indicating the magnetic exchange coupling between luogufengite (hard magnet) and  
203 valleyite (relatively soft magnet) (Neupane et al. 2017). Figure 6a shows a magnetic hysteresis  
204 loop of synthetic Al-bearing luogufengite with ~ 10 mole % of Al in the structure (Ohkoshi et al.  
205 2005). The small amount of hematite cannot affect the hysteresis loop due to its weak magnetic  
206 property (Supplementary Figure S4) (Ohkoshi et al. 2005). The hysteresis loop of valleyite is  
207 similar to a soft magnet in the magnetic coupling system of SrFe<sub>12-y</sub>Al<sub>y</sub>O<sub>19</sub> (soft magnet) /  
208 Ni<sub>0.5</sub>Zn<sub>0.5</sub>Fe<sub>2</sub>O<sub>4</sub> (hard magnet) (Neupane et al. 2017), and hard-soft magnetic nanocomposite with  
209 the composition of (90%) SrFe<sub>10</sub>Al<sub>2</sub>O<sub>19</sub> / (10%) Co<sub>0.8</sub>Ni<sub>0.2</sub>Fe<sub>2</sub>O<sub>4</sub> (Torkian and Ghasemi, 2018).

210 Strong exchange coupling occurs between a soft magnet and hard magnet in a magnetic  
211 nanocomposite when the radius of the soft magnet is smaller than the critical exchange length for  
212 the soft magnet (Kneller and Hawig, 1991). The critical exchange length for magnetite ranges  
213 from  $\sim 50$  nm to 1000 nm (Muxworthy and Williams, 2006). The observed crystal size of  
214 valleyite is within this range.

215 DFT calculations were performed on a synthetic ( $\text{Ca}_4\text{Fe}_6\text{O}_{13}$ ) and multiple natural  
216 ( $\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_{2-x}\text{Ti}_x)\text{O}_{13}$ ) valleyite compositions, including the case of  $x = 0.125$ , which has a  
217 simulated composition close to the measured valleyite composition of ( $\text{Ca}_{3.61}\text{Mg}_{0.39}$ )( $\text{Fe}_{3.97}\text{Al}_{1.91}\text{Ti}_{0.09}$ ) $\text{O}_{13}$   
218 from EDS (see Supplementary Figure 5). The main goal of these DFT calculations is to  
219 obtain a qualitative scale of the stability of valleyite. Table 5 contains a summary of the stability  
220 calculations for each valleyite composition considered in this work.

221 From Table 5, the stability calculations of synthetic valleyite  $\text{Ca}_4\text{Fe}_6\text{O}_{13}$  indicate that it is  
222 105 (42) meV/atom above the convex hull and 70 (7) meV/atom vs. decomposition to binary  
223 oxides for ferromagnetic (antiferromagnetic) configurations, respectively. The substitution of  
224 12.5% of Ca with Mg and 33% of Fe with Al (close to the Mg and Al content in natural valleyite)  
225 to make  $\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_2)\text{O}_{13}$  results in a stability of 86 (74) meV/atom above the convex hull  
226 and 41 (29) meV/atom vs. decomposition to binary oxides for ferromagnetic (antiferromagnetic)  
227 configurations, respectively. The addition of Mg and Al has resulted in partial stabilization of the  
228 ferromagnetic state and destabilization of the antiferromagnetic state. The magnitude of the  
229 energies above the convex hull of synthetic valleyite and non-Ti containing natural valleyite ( $x =$   
230 0) suggests that these materials are energetically metastable at low (room) temperature.

231 The replacement of Al in  $\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_2)\text{O}_{13}$  with Ti to form  
232  $\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_{1.875}\text{Ti}_{0.125})\text{O}_{13}$  ( $x = 0.125$ ), the composition close to the experimentally derived

233 composition of natural valleyite,  $(\text{Ca}_{3.61}\text{Mg}_{0.39})(\text{Fe}_{3.97}\text{Al}_{1.91}\text{Ti}_{0.09})\text{O}_{13}$ , results in a marked  
234 stabilization of the material compared to when no Ti is present. Both the ferromagnetic and  
235 antiferromagnetic arrangements result in these materials residing on the convex hull (note that  
236 the ferromagnetic arrangement is 30 meV/atom above the hull when considering its stability  
237 together with the antiferromagnetic arrangement), and have negative formation energies (i.e., are  
238 stable) relative to decomposition to the constituent binary oxides. At this time, it is unclear what  
239 role Ti plays in the stabilization of valleyite, however it is apparent that higher Ti concentrations  
240 than  $x = 0.125$  (e.g.  $x = 0.5$  to make  $\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_{1.5}\text{Ti}_{0.5})\text{O}_{13}$ ) result in destabilization with an  
241 energy above the convex hull of 170 meV/atom (see Table 1). We note here the addition of Ti  
242 results in the reduction of  $\text{Fe}^{3+}$  to  $\text{Fe}^{2+}$ , as evidenced by the loss of  $1 \mu_B$  on Fe per  $\text{Ti}^{4+}$  added.  
243 From this result, we speculate there may be a range of Ti concentrations resulting in stabilization  
244 of the naturally occurring valleyite mineral, and that destabilization at higher Ti content may be  
245 due to Ti-Ti interactions and/or the instability of  $\text{Fe}^{2+}$  in the tetrahedral Fe-O bonding  
246 environment of the sodalite structure.

247 Comparisons can be made between the DFT-predicted magnetic moments and the  
248 measured magnetization of natural valleyite  $(\text{Ca}_{3.61}\text{Mg}_{0.39})(\text{Fe}_{3.97}\text{Al}_{1.91}\text{Ti}_{0.09})\text{O}_{13}$ . Simulating the  
249 ferromagnetic state of  $\text{Ca}_4\text{Fe}_6\text{O}_{13}$  and  $\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_2)\text{O}_{13}$  indicates that  $\text{Fe}^{3+}$  exists in the high  
250 spin state with a moment of  $4.3 \mu_B/\text{Fe}$ , with O carrying a small magnetic moment of about  $0.25$   
251  $\mu_B/\text{O}$ . Note that ascribing the total magnetic moment to Fe results in an Fe moment of  $5 \mu_B/\text{Fe}$ ,  
252 which is typical for Fe in the high spin state. For  $\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_2)\text{O}_{13}$ , these combined  
253 moments amount to a magnetization of  $\sim 20 \mu_B/(\text{formula unit}) \approx 7.6 \text{ emu/g}$ . This value is in  
254 reasonable agreement with the experimentally measured valleyite magnetization value of  $\approx 9.2$   
255 emu/g. We note here the stability calculations indicated that the ferromagnetic state tended to be

256 slightly less stable than the antiferromagnetic state. However, it is worth noting that no effort was  
257 made to model ferrimagnetic or paramagnetic states of valleyite, so we cannot make quantitative  
258 comparisons of the relative stabilities of these magnetic states.

259

## 260 **IMPLICATIONS**

261 This study demonstrates that a combination of advanced synchrotron XRD (Xu et al.  
262 2000, 2002, 2010; Zhang et al. 2002) with high-resolution TEM is a powerful approach to  
263 identify nano-minerals in geological systems and to determine their nanocrystalline structures  
264 (Xu et al. 2017b). Especially, the high brilliance and high coherence of synchrotron X-rays  
265 enables the clear separation of weak and broad XRD peaks of nanocrystalline phases, which  
266 cannot be resolved or detected by conventional XRD, particularly for complex, multiphase  
267 natural samples. In addition, direct imaging and analysis by high-resolution TEM combined with  
268 SAED and X-ray EDS spectra allow determination of the structures and chemistry of minerals at  
269 the nanoscale. We expect that this integrated approach will be employed to discover many new  
270 nano-minerals in the future.

271 Valleyite is a new magnetic material with low density framework structure. The magnetic  
272 exchange coupling in nano-minerals may hold the key for understanding the unusual magnetization  
273 phenomena seen in some igneous rocks from Earth, Mars and the moon (Heaman, 1997; Acuña et al.  
274 1999; Stevenson, 2001). The observed exchange-coupled magnetic property between valleyite  
275 (soft magnet) and luogufengite (hard magnet) in the scoria samples will shed light on the paleo-  
276 magnetism, i.e., high remnant magnetization, of basaltic and related rocks. Furthermore, the  
277 magnetic valleyite phase with a sodalite-type structure may potentially be a functional magnetic  
278 material with magnetic, medical, and biochemical applications (Newsam, 1986).

279

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288

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- 387

388 **FIGURE CAPTIONS**

389 **Figure 1.** Experimental and calculated XRD patterns (overlapping black and red lines,  
390 respectively) of a Fe-oxide sample dominated by luogufengite (L), valleyite (V), and hematite  
391 (H). The residual between the measured and calculated profiles is shown right under the XRD  
392 pattern. The weight percentages of mineral phases in the sample were calculated using the  
393 Rietveld method. The strongest peak ( $d_{112} = 3.628 \text{ \AA}$ ) and the second strongest peak ( $d_{011} =$   
394  $6.287 \text{ \AA}$ ) (see the insert at upper-left corner for the enlarged peaks) are very similar to the (102)  
395 diffraction peak from hematite and (110) diffraction peak from labradorite ( $\sim 6.263 \text{ \AA}$ ). The (011)  
396 peak from valleyite is also close to the (011) broad peak from luogufengite. Careful sample  
397 preparation and high-resolution synchrotron XRD greatly helped the discovery of valleyite.  
398 Broad peaks from luogufengite are due to its much smaller (nano-size) crystals (Xu et al. 2017b).

399  
400 **Figure 2.** (a) Bright-field TEM image showing a valleyite crystal, together with much smaller  
401 crystals of luogufengite (Luo) and silica-dominated glass. The crystal displays forms of {100}  
402 and {111}. (b) A [001] zone-axis selected-area electron diffraction (SAED) pattern of valleyite.  
403 (c) Bright-field TEM image showing a valleyite crystal along the  $[\bar{1}11]$ -direction with its SAED  
404 pattern (d). An ideal crystal shape projected along the [111] direction is inserted at the lower-  
405 right corner. In (a) and (c), all the Miller indices show traces of planes perpendicular to the  
406 images. The (111) plane displays similarly as (110). Rounded corners are due to resorption at  
407 high temperature after the crystals formed.

408  
409 **Figure 3.** (a) Bright-field TEM image showing a broken piece of valleyite crystal. (b) High-  
410 resolution TEM image and its FFT pattern (inserted at the lower-left corner) of valleyite from a

411 thin corner of the crystal. (c, d) SAED patterns of the valleyite crystal along the [001] and [12]  
412 zone-axes, respectively. All the SAED patterns indicate a body-centered Bravais lattice ( $I$ ), i.e.,  
413  $h + k + l = 2n$ . (e) A representative X-ray EDS spectrum from valleyite. Cu peaks are from the  
414 holey carbon-coated Cu grid that holds the specimen. Si peak is from silica-rich glass coating  
415 and fluorescence from the Li-drifted silicon detector of the X-ray EDS system.

416

417 **Figure 4.** Polyhedral atomic models of the valleyite structure: (a) projection along the a-axis; and  
418 (b) projection along the [111] zone-axis. Brown tetrahedra: (Fe,Al)O<sub>4</sub>; Large green sphere: Ca;  
419 Small red sphere: O.

420

421 **Figure 5.** Crystal structures of sodalite (Hassan et al. 2004), synthetic Ca<sub>4</sub>Al<sub>6</sub>O<sub>13</sub> (Peters et al.,  
422 2007) and the newly discovered valleyite. The unit cell of valleyite is slightly larger than that of  
423 synthetic Ca<sub>4</sub>Al<sub>6</sub>O<sub>13</sub>. The framework changes through distortion of di-trigonal rings to  
424 accommodate the different sizes of (Fe,Al)O<sub>4</sub> tetrahedra or (Fe,Al)-O bond distances. For clarity,  
425 Na and Ca atoms are omitted.

426

427 **Figure 6.** Temperature dependence magnetization of the valleyite-bearing sample from 300 to  
428 1000 K measured on warming in 1kOe.

429

430 **Figure 7.** Room-temperature magnetic hysteresis loops of (a) synthetic Al-bearing  $\epsilon$ -Fe<sub>2</sub>O<sub>3</sub>, (b)  
431 valleyite (schematic), and (c) natural sample composed of valleyite, luogufengite and hematite.

432

Table 1. Powder X-ray diffraction data ( $d$  in Å)  
 for valleyite.

$d_{obs}$	$I_{obs}$	$d_{clac}$	$I_{clac}$	$hkl$
<b>6.2871</b>	<b>45.1</b>	<b>6.2826</b>	<b>43.1</b>	<b>0 1 1</b>
4.4395	6.4	4.4425	5.3	0 0 2
<b>3.6284</b>	<b>100.0</b>	<b>3.6273</b>	<b>100.0</b>	<b>1 1 2</b>
3.1395	7.9	3.1413	5.2	0 2 2
<b>2.8011</b>	<b>39.6</b>	<b>2.8097</b>	<b>36.5</b>	<b>0 1 3</b>
<b>2.5644</b>	<b>32.1</b>	<b>2.5649</b>	<b>29.4</b>	<b>2 2 2</b>
<b>2.3750</b>	<b>27.3</b>	<b>2.3746</b>	<b>31.5</b>	<b>1 2 3</b>
2.2188	4.5	2.2213	1.1	0 0 4
2.0976	8.7	2.0942	10.9	1 1 4
1.9877	6.5	1.9868	8.5	0 2 4
1.8192	5.9	1.8136	6.5	2 2 4
1.5604	10.4	1.5707	13.5	0 4 4

Table 2. Chemical composition of valleyite.

Analysis No.	1	2	3	4	5	Average
Fe <sub>2</sub> O <sub>3</sub> (wt.%)	49.21	49.62	49.89	49.58	49.56	49.57
CaO	31.58	31.70	31.54	31.49	31.58	31.58
Al <sub>2</sub> O <sub>3</sub>	15.31	15.05	14.94	15.48	15.23	15.20
MgO	2.52	2.39	2.39	2.58	2.38	2.45
TiO <sub>2</sub>	1.38	1.25	1.25	0.87	1.25	1.20
Fe	3.94	3.98	4.01	3.97	3.99	3.97
Ca	3.60	3.62	3.61	3.59	3.62	3.61
Al	1.92	1.89	1.88	1.94	1.92	1.91
Mg	0.40	0.38	0.39	0.41	0.38	0.39
Ti	0.11	0.10	0.08	0.07	0.10	0.09
Average chemical formula: (Ca <sub>3.61</sub> Mg <sub>0.39</sub> )(Fe <sub>3.97</sub> Al <sub>1.91</sub> Ti <sub>0.09</sub> )O <sub>13</sub>						
Notes: All calculations are based on 13 oxygen atoms.						

Table 3. Atomic parameters of valleyite.

Space group ( $I\bar{4}3m$ )						
Atom	Occupancy	x	y	z	$U_{iso} (\text{\AA}^2)^*$	
Ca	Ca <sub>0.90</sub> Mg <sub>0.10</sub>	0.1543 (7)	0.1543 (7)	0.1543 (7)	0.012	
Fe	Fe <sub>0.66</sub> Al <sub>0.32</sub> Ti <sub>0.02</sub>	1/4	1/2	0	0.012	
O1	O <sub>1.00</sub>	0.3602 (5)	0.3602 (5)	0.9107 (6)	0.020	
O2	O <sub>1.00</sub>	0	0	0	0.039	

Lattice parameters:  $a = 8.8852 (7) \text{\AA}$

\*From Peters et al. (2007)

Table 4. Bond distances ( $\text{\AA}$ ) for valleyite and synthetic Ca<sub>4</sub>Al<sub>6</sub>O<sub>13</sub>.

Valleyite Ca <sub>4</sub> (Fe,Al) <sub>6</sub> O <sub>13</sub>		Synthetic Ca <sub>4</sub> Al <sub>6</sub> O <sub>13</sub>	
Fe-O1	1.770 (5) x 4	Al-O1	1.737 (4) x 4
Ca-O1	2.285 (9) x 3	Ca-O1	2.311 (5) x 3
Ca-O2	2.375 (7) x 1	Ca-O2	2.374 (18) x 1

**Table 5.** Summary of valleyite stability assessment from DFT calculations. For the stability values, the first/second value corresponds to the stability of the simulated ferromagnetic/antiferromagnetic state, respectively. Note for  $x=0.5$  the antiferromagnetic state was not simulated. A summary of decomposition products and phase fractions can be found in the calculation output files included as part of the supplementary materials.

Simulated Valleyite Composition	Energy above convex hull (meV/atom) (FM/AFM)	Formation energy relative to binary oxides (meV/atom) (FM/AFM)
$\text{Ca}_4\text{Fe}_6\text{O}_{13}$	105 / 42	70 / 7
$\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_{2-x}\text{Ti}_x)\text{O}_{13}$ ( $x = 0$ )	86 <sup>1</sup> / 74 <sup>2</sup>	41 <sup>1</sup> / 29
$\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_{2-x}\text{Ti}_x)\text{O}_{13}$ ( $x = 0.125$ )	0 <sup>3</sup> / 0	-290 / -320
$\text{Ca}_{3.5}\text{Mg}_{0.5}(\text{Fe}_4\text{Al}_{2-x}\text{Ti}_x)\text{O}_{13}$ ( $x = 0.5$ )	170 <sup>4</sup> / n/a	121 <sup>4</sup> / n/a

<sup>1</sup> The 86 meV/atom stability value is the average over four Mg and five Al configurations, which have a combined range from 85-90 meV/atom. The corresponding average formation energy of 41 meV/atom has a range of 39-42 meV/atom.

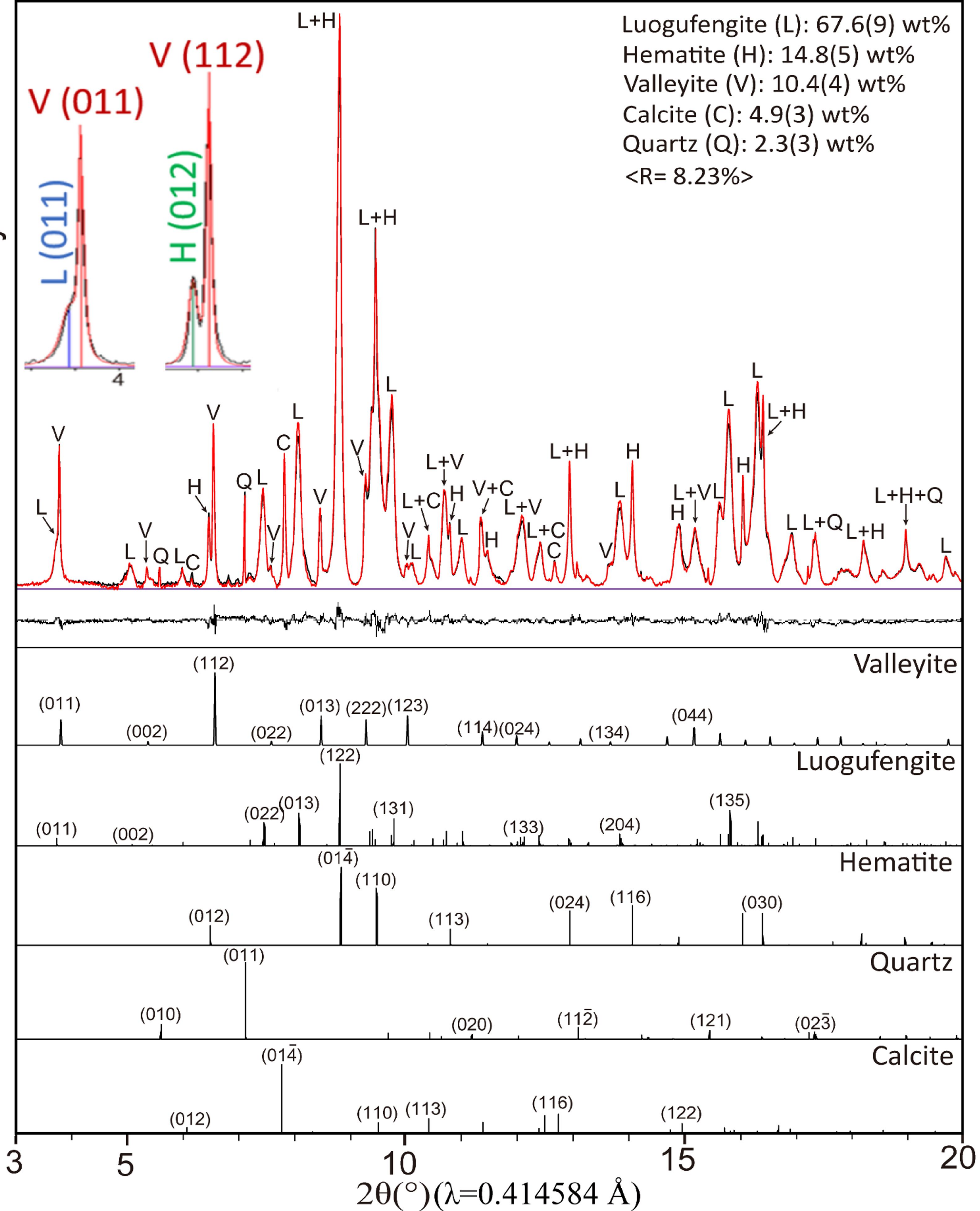
<sup>2</sup> The 74 meV/atom stability value is the average over four antiferromagnetic ordering arrangements, which have a range from 70-79 meV/atom.

<sup>3</sup> As both the FM and AFM state lie on the convex hull, if both phases are included in the analysis then the FM state is 30 meV/atom, not 0 meV/atom, above the convex hull.

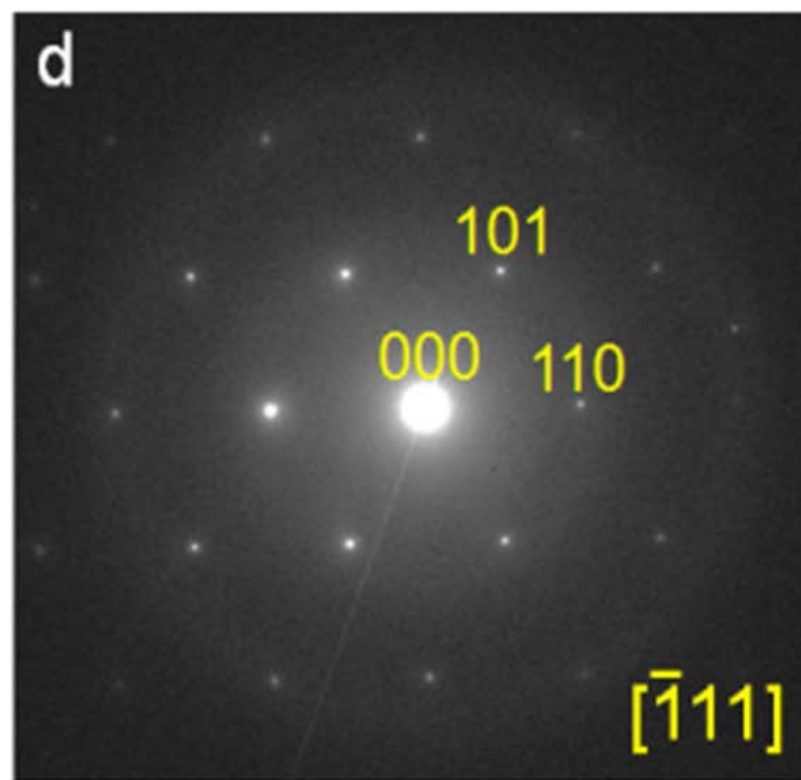
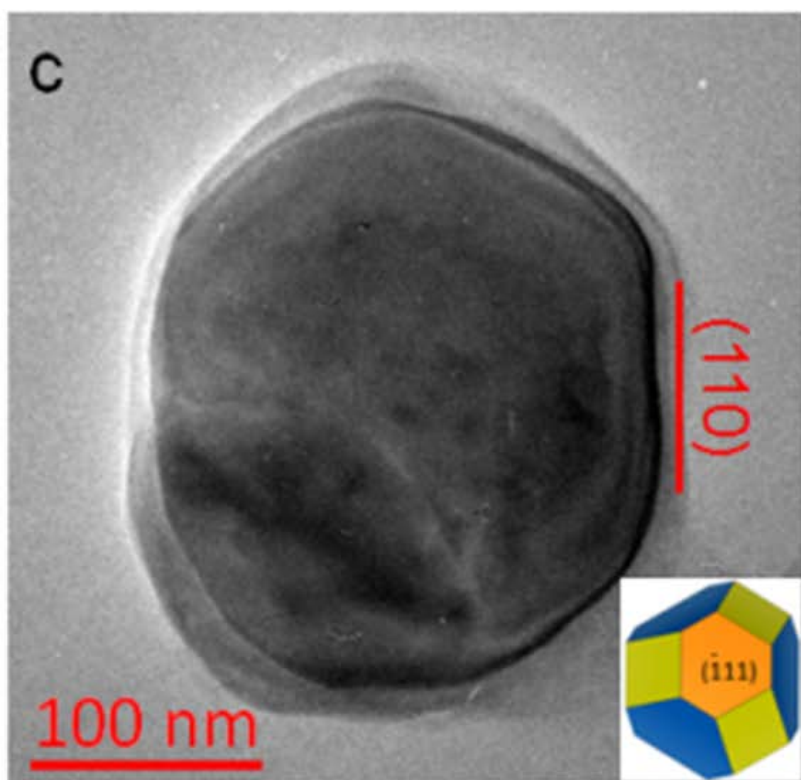
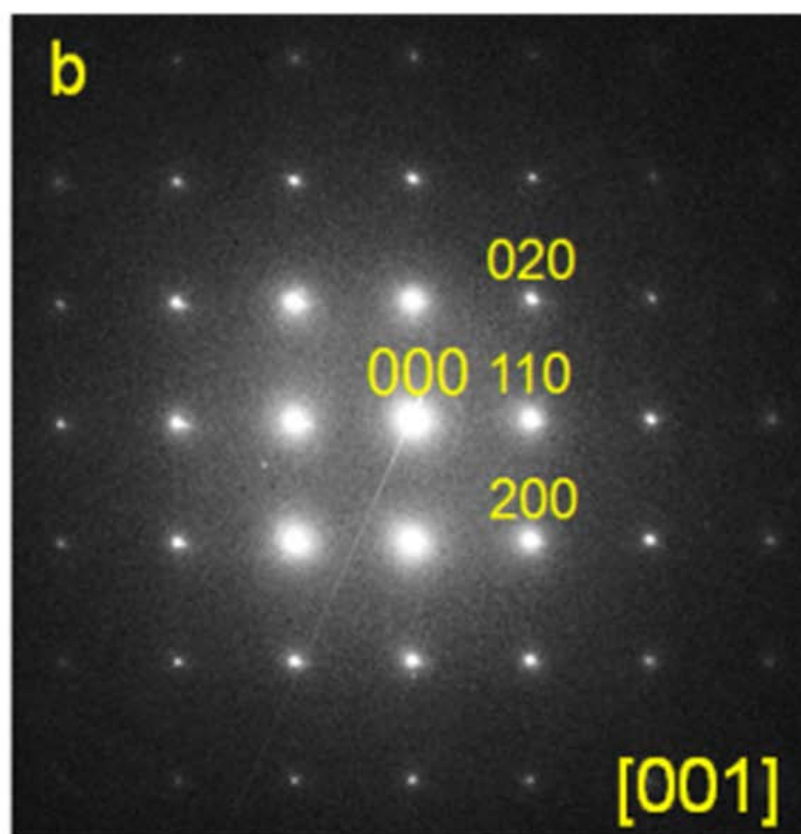
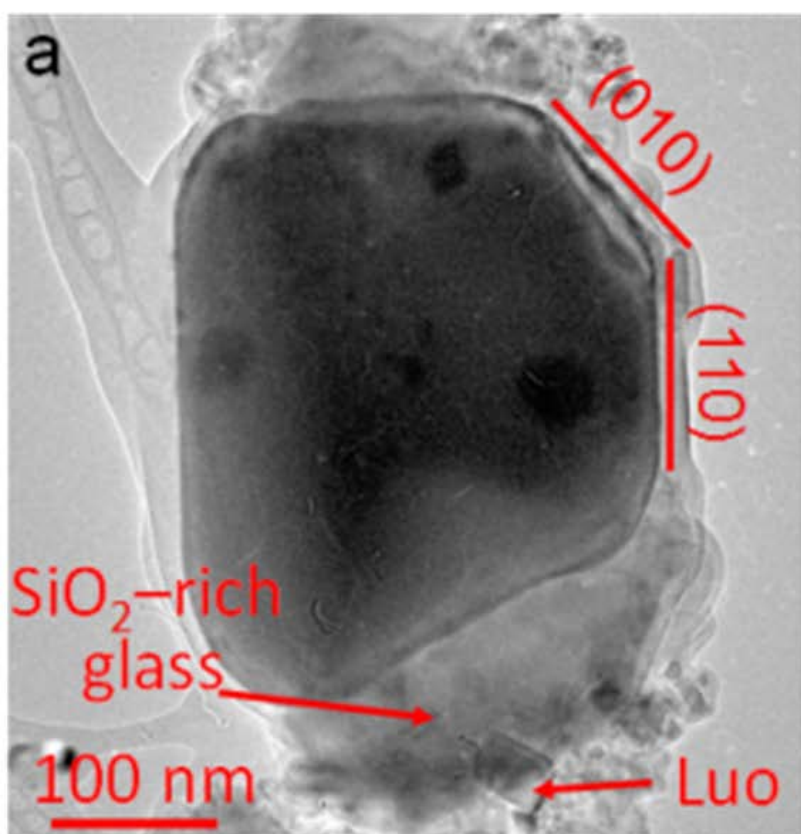
<sup>4</sup> The 170 meV/atom stability value is the average over four Ti configurations, which have a range from 168-173 meV/atom. The corresponding average formation energy of 121 meV/atom has a range of 118-123 meV/atom.

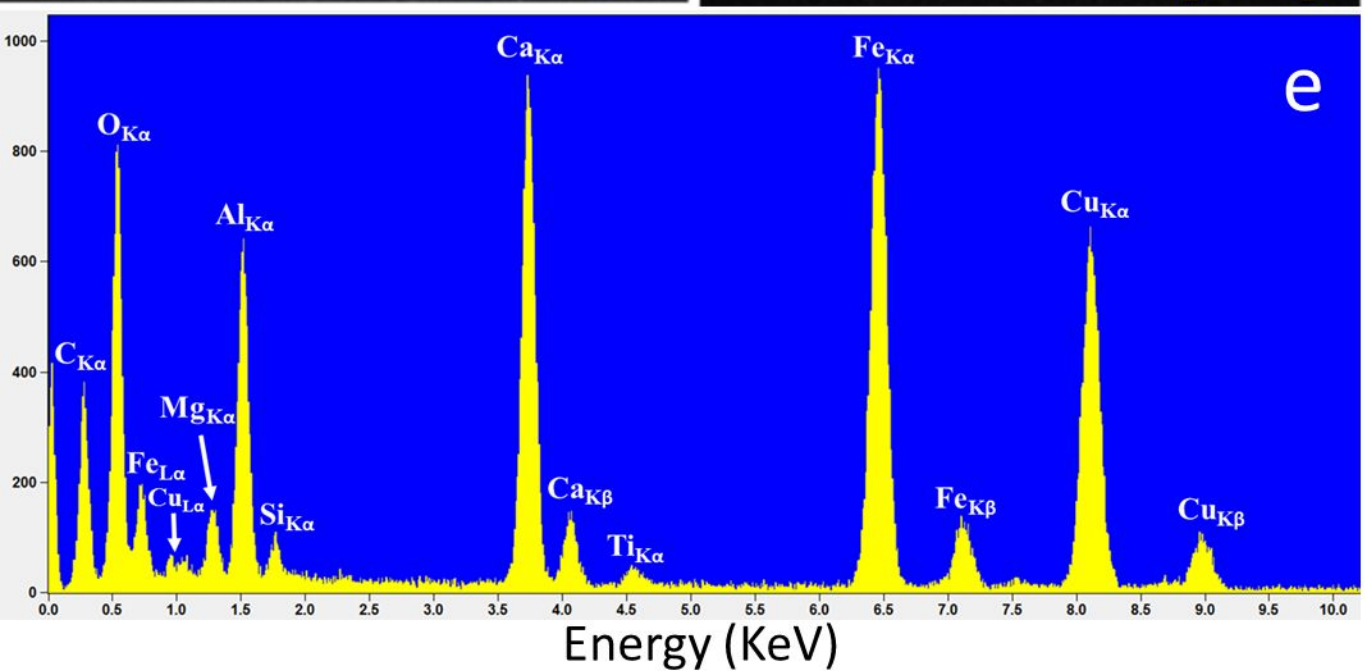
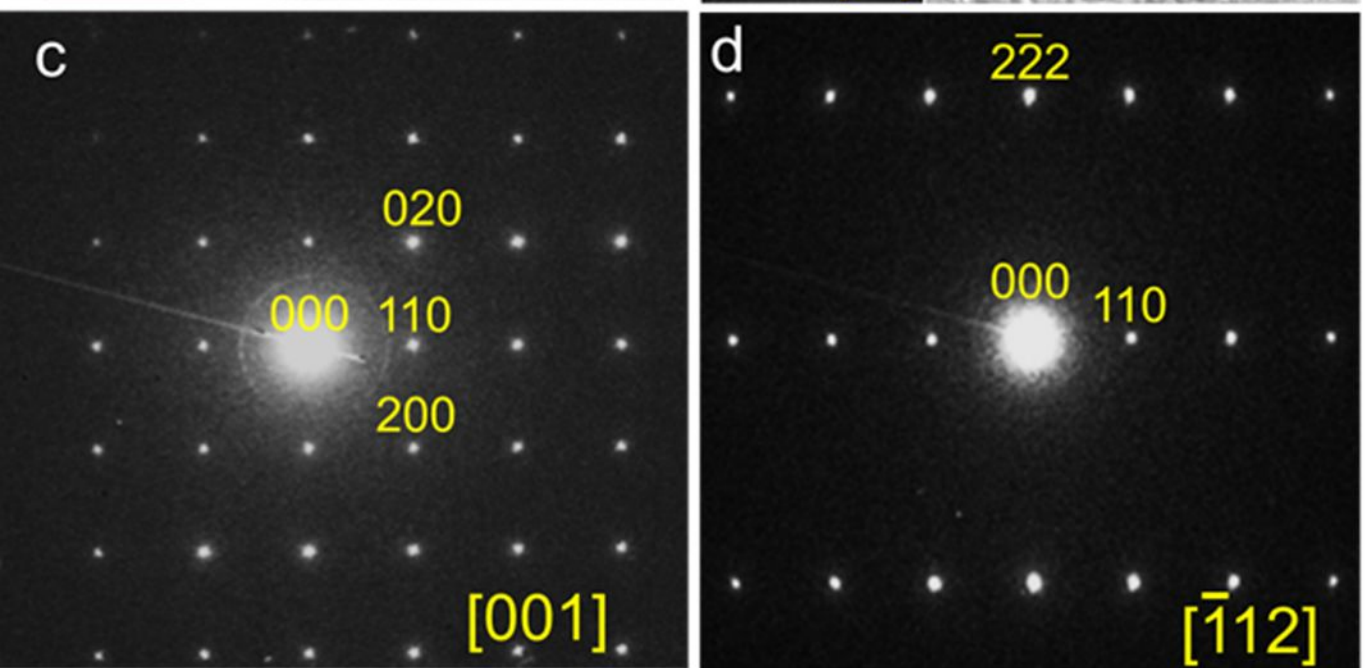
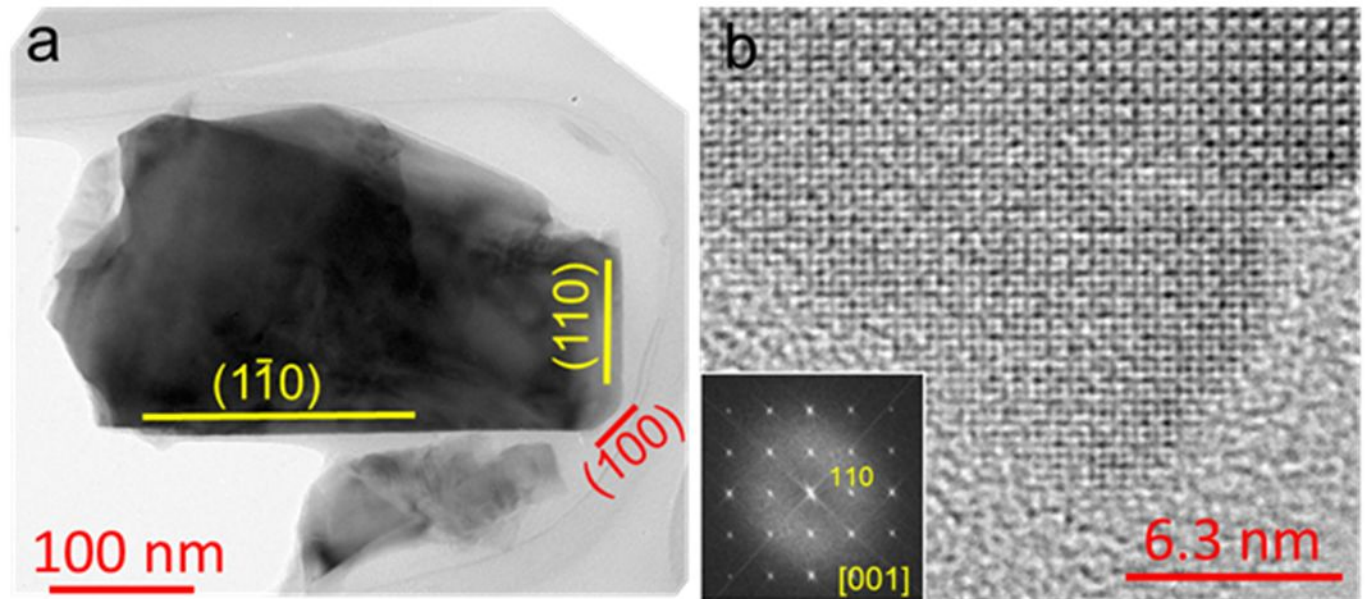


Intensity

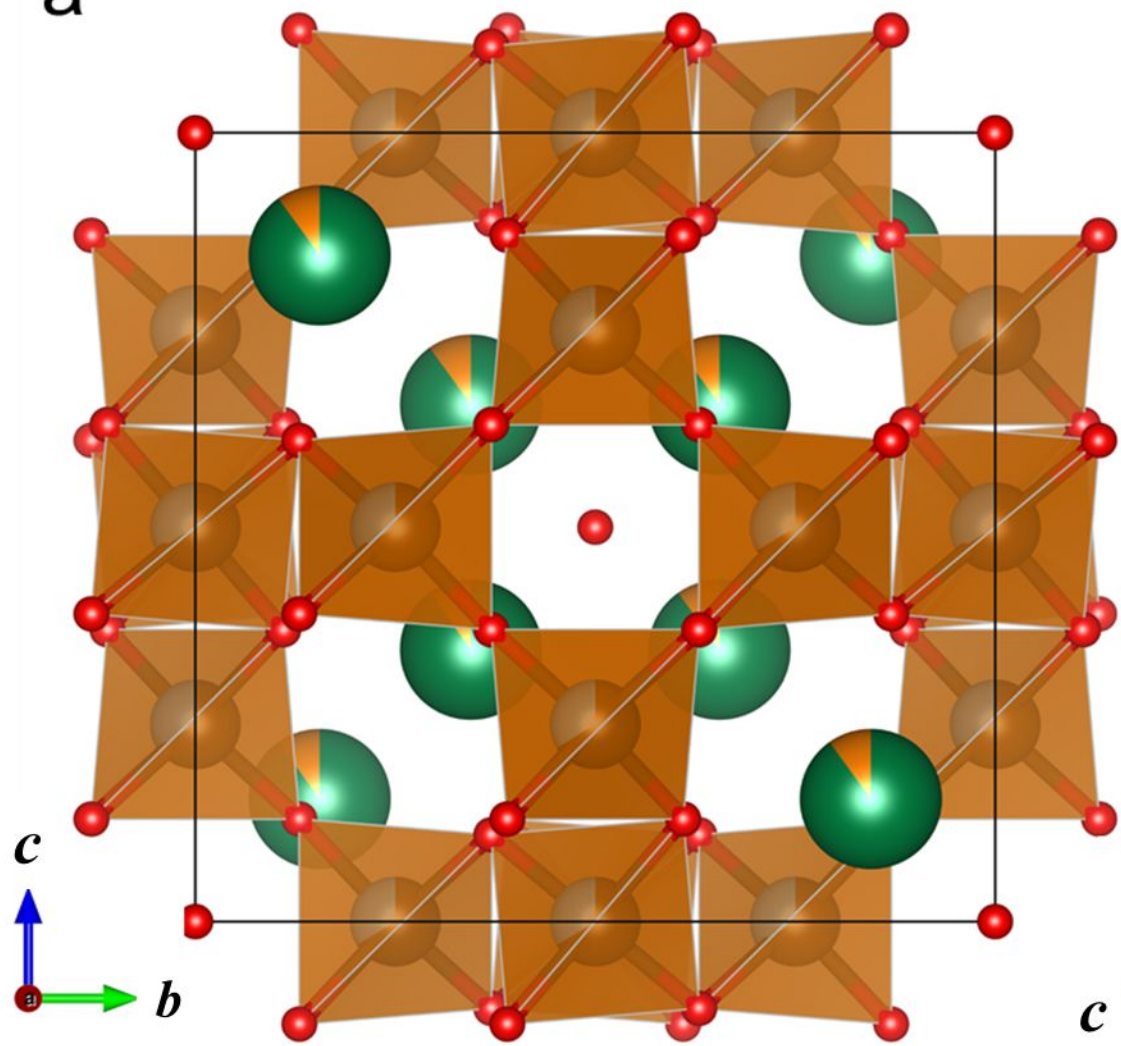
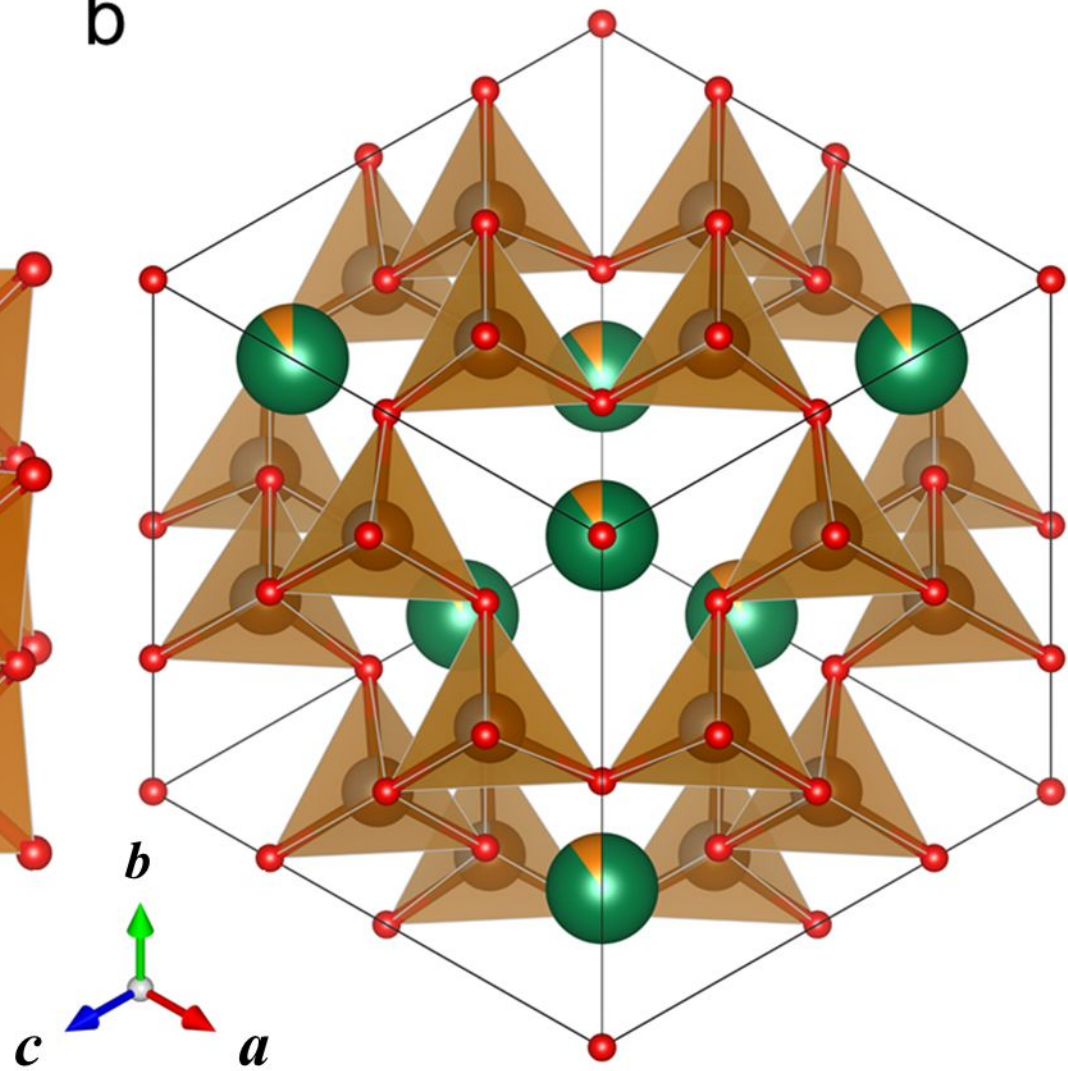


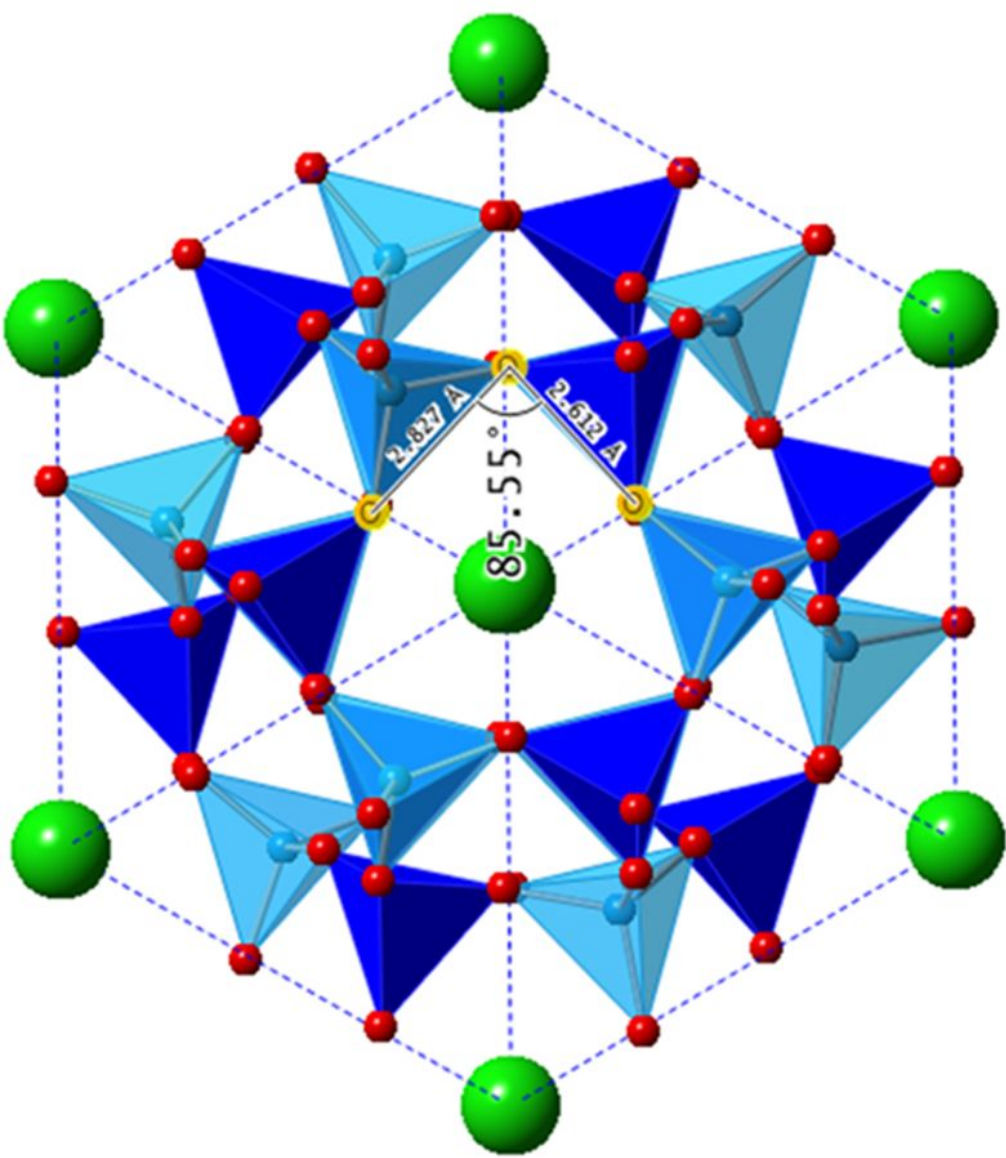




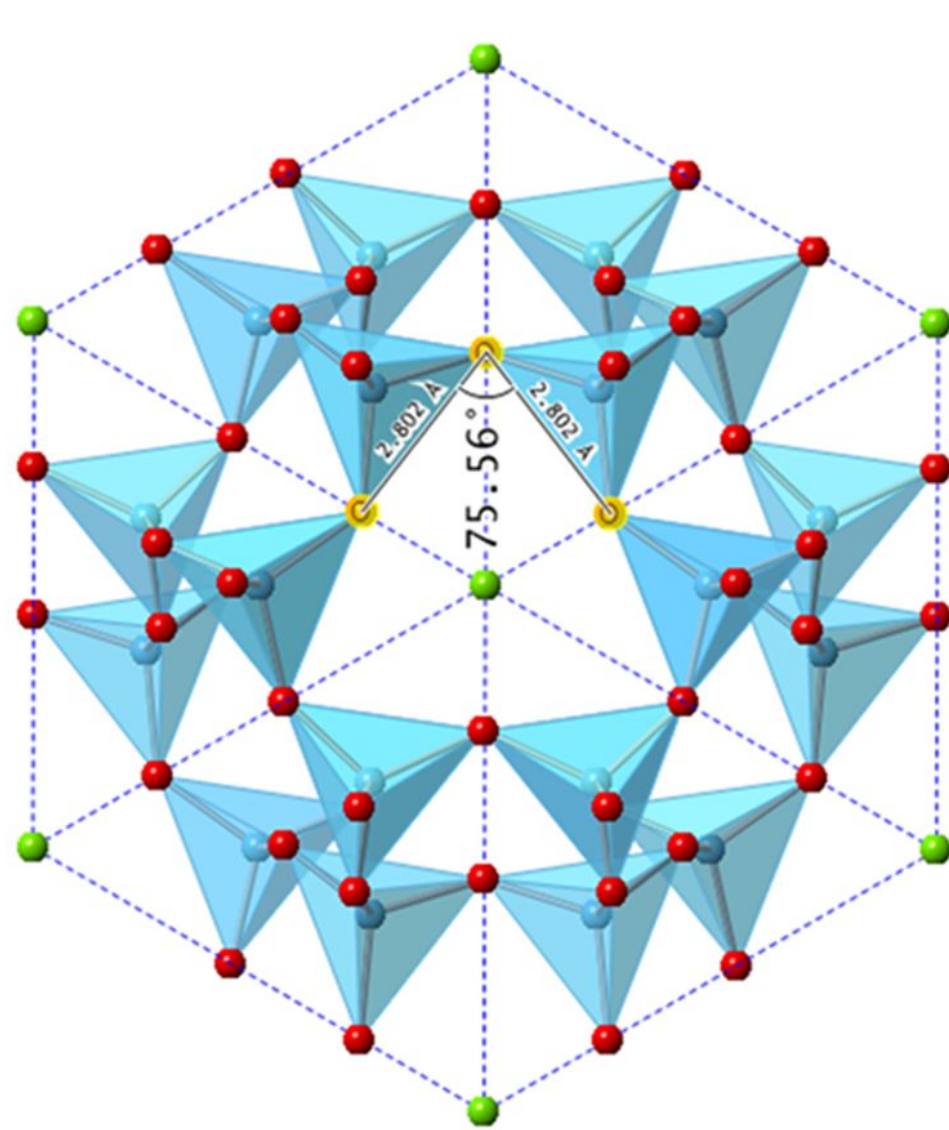




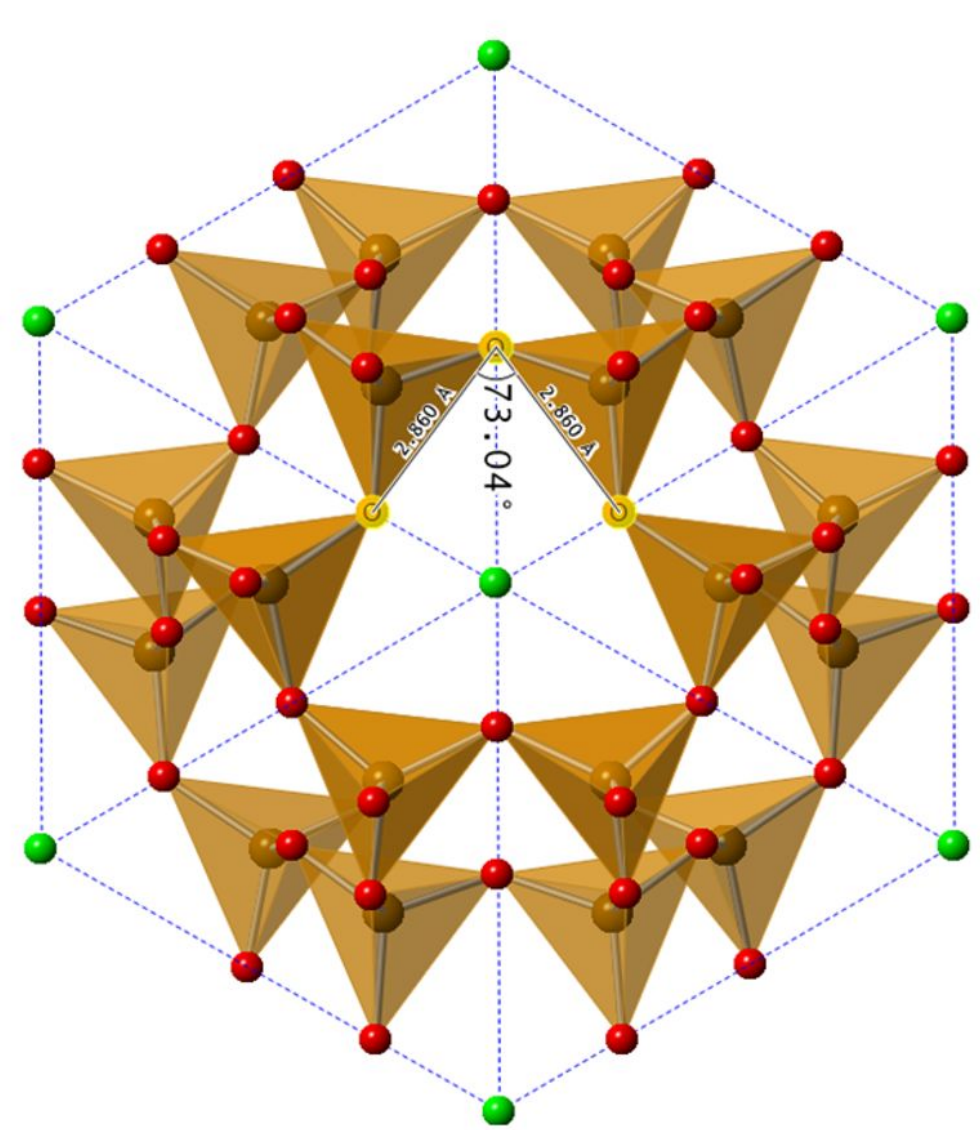
**a****b**



Sodalite



Synthetic Ca<sub>4</sub>Al<sub>6</sub>O<sub>13</sub>



Valleyite



