1	Revision 1
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3	Barometric constraints based on apatite inclusions in garnet
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12	Running title: Apatite-in-garnet barometry

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15	ABSTRACT
16	Compiled volumetric data for fluor-, chlor- and hydroxyl-apatite has been fitted to a
17	pressure-volume-temperature $(P-V-T)$ equation of state for volume calculation at elevated P and
18	T. The regressions were used to assess the potential of apatite inclusions in garnet for
19	thermobarometric applications, according to the pressurization of inclusions resulting from
20	elastic differences between the inclusion and host minerals. Isomeke contours (lines in pressure
21	temperature space, representing permissible entrapment conditions that yield a given inclusion
22	pressure) were calculated and show that apatite inclusions in garnet are a particularly useful
23	barometer, owing to the large differences in the bulk moduli and similar thermal expansivities
24	between apatite and garnet. Heating experiments were conducted on fluorapatite inclusions in
25	andraditic garnets from the Casting Copper skarn, NV, to assess the variation in measured
26	inclusion pressure with heating relative to that predicted with isotropic elastic theory. Negligible
27	departures between theoretical and measured pressurization suggests no significant correction is
28	needed for applying room- T inclusion pressure measurements for barometry constraints.
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30 Keywords: apatite, garnet, pressure, heating, Raman spectroscopy

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INTRODUCTION

32	Apatite is the most abundant phosphate mineral on Earth and commonly occurs as an
33	accessory phase in igneous and metamorphic rocks, and as detritus in sedimentary rocks. The
34	chemistry of Ca-apatite is Ca ₅ (PO ₄) ₃ X, where X is occupied by a halogen element or volatile
35	compound, with the major endmembers being fluorapatite (FAP), chlorapatite (CAP) and
36	hydroxyapatite (HAP), in which X= F, Cl and OH, respectively. Pure FAP and HAP have been
37	experimentally shown to be stable at pressures up to 11-13 GPa at 1300-1800 K before
38	decomposing to a Ca ₃ (PO ₄) ₂ pseudomorph (Murayama et al. 1986), and apatite is stable to at
39	least 7.5 GPa at 950 °C when a component in mid-ocean ridge basalts (Konzett and Frost 2009).
40	Thus, apatite is stable at conditions from Earth's surface through the upper mantle. The
41	ubiquitous occurrence of apatite as an accessory phase in a wide variety of rock types and across
42	large ranges of pressure (P) and temperature (T) makes apatite an attractive mineral for
43	petrologic applications such as interpreting pressure-temperature-time paths. Here, we describe
44	application of apatite in thermobarometry, according to the physical properties of apatite
45	inclusions in garnet.

The growth of minerals in rocks may result in the encapsulation of crystallites (either 46 preexisting mineral grains, or mineral grains produced via metamorphic reactions) within larger 47 mineral grains. At the time of entrapment, the molar volumes of the host and inclusion minerals 48 49 correspond exactly to the same P-T conditions of encapsulation. However, upon exhumation, any elastic difference between the host and inclusion may lead to the pressurization of the inclusion 50 mineral, such that at Earth's surface inclusion pressure (P_{incl}) differs from the externally applied 51 52 pressure (1 bar). Garnet commonly occurs as poikiloblasts in metamorphic rocks, in which inclusions of quartz, calcite, micas, feldspars, and accessory phases are commonly reported. 53

Analysis of inclusions in garnet has been used for numerous purposes, including: bracketing the timing of garnet growth (Catlos et al. 2001), correlating garnet growth to deformation and fabric development (e.g., Passchier and Trouw 2005, and references therein), reconstructing conditions of early-prograde deformation (Ashley et al. *accepted*), constraining fluid flux and composition (e.g., Vry and Brown 1991), and barometry from pressurized quartz inclusions (e.g., Rosenfeld

59 and Chase 1961; Enami et al. 2007; Ashley et al. 2014).

Garnet is a suitable host mineral for thermobarometry of mineral inclusions because it is 60 61 an isotropic host with a high bulk modulus. The high bulk modulus of garnet allows for stress 62 retention within the inclusions, leading to the development and preservation of inclusion pressure upon exhumation. Previous studies of mineral inclusions have focused mainly on 63 thermobarometry based on inclusions of silica polymorphs within garnet (namely quartz and 64 coesite). However, similar to quartz, apatite is a relatively soft, compressible mineral that would 65 be expected to develop pressurization if entrapped at elevated pressures and exhumed to Earth's 66 67 surface. As noted above, apatite is a common accessory phase and is a typical inclusion phase within garnet in some environments. Moreover, apatite is characterized by a sharp, easily 68 resolvable Raman band at ca. 964 cm⁻¹, and experimental data for the pressure-dependent shift of 69 70 this Raman band are available (e.g., Comodi et al. 2001; Schouwink et al. 2010). In this paper, 71 we present new modeling of the physical and spectroscopic characteristics of apatite for 72 applications in thermobarometry. This modeling indicates that apatite inclusions in garnet 73 represent a robust barometer. To test this approach, fluorapatite inclusions and andradite garnet from the Casting Copper skarn, NV, are measured for a range of temperatures (-175 to 275 °C) 74 75 to internally test the ability of the modeling approach to replicate inclusion pressure variations 76 with heating and cooling.

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Methods

79 Parameterization of the elastic properties of apatite endmembers

80 Experimental data on the unit-cell volume of apatite were fitted to a pressure-volumetemperature equation of state (*P-V-T* EOS) to permit calculation of volumes at any *P* and *T* 81 condition of interest. We used the modified 3rd-order Tait EOS of Holland and Powell (2011), 82 83 which applies a thermal pressure formulation to correct for volume expansion at elevated 84 temperature. The volumetric data was compiled from the sources listed in Table 1. EOS 85 regressions were completed using the program *EosFit7-GUI* (Gonzalez-Platas et al. 2016) 86 assuming hexagonal symmetry (Hughes et al. 1989), which applies the refinement methodology 87 after Angel et al. (2014). Estimated standard deviations (ESDs) in elastic moduli were calculated 88 through a least-squares fitting approach using the pressure, temperature and volume standard deviations reported in the experimental literature (Table 1). An estimated Einstein temperature 89 (θ_E) was calculated following the protocol of Holland and Powell (2011), using the standard 90 91 entropy at 298 K (S°_{298}) and 21 atoms per unit formula for apatite; the quality of θ_E estimation was evaluated by ensuring minimized ESDs occurred at the value calculated and that significant 92 improvements were not made on the refinements when the temperature was varied. The 93 94 calculated elastic moduli are listed in Table 2, with a comparison of modeled and experimental 95 molar volumes shown in Figure 1. Volumes of garnet at elevated P and T were calculated using 96 the thermochemical database of Holland and Powell (2011, and references therein).

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98 Elastic theory and modeling encapsulation pressures

99 Entrapment pressure was calculated for a given inclusion pressure (*P_{incl}*) by applying the
100 1D isotropic elastic model of Guiraud and Powell (2006):

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$$\left(\frac{V_{1,298}}{V_0}\right)_{host} = \left(\frac{V_{incl,298}}{V_0}\right)_{incl} - \frac{3}{4G} \cdot \left(\boldsymbol{P}_{incl} - \boldsymbol{P}_{ext}\right) \quad \text{eq. 1}$$

103

104 where V_0 is volume at the conditions of entrapment, $V_{P,298}$ is volume at Earth's surface (P of 1 105 bar for garnet and P_{incl} for the inclusion), G is the shear modulus of the host, and P_{ext} is the 106 externally applied pressure at the time of measurement (1 bar). The procedure for computing 107 entrapment pressure at a given temperature is as follows: For a known (measured) P_{incl} and a known or inferred entrapment T, the value of the entrapment pressure is adjusted iteratively and 108 the V_0 's of the inclusion and host are computed at each pressure value. Entrapment pressure is 109 110 determined when both sides of eq. 1 are equal. The "isomeke" (Adams et al. 1975) of a given P_{incl} corresponds to the locus to temperature-entrapment pressure points that satisfy eq. 1. As 111 112 such, to construct the isomeke, the procedure described above is repeated for a range of entrapment Ts to determine the corresponding entrapment pressures. In this study, an isomeke 113 114 contour map was generated for each apatite endmember included in garnet, $X_3Y_2(SiO_4)_3$ (Fig. 2). 115 The garnet endmembers included here include almandine, pyrope and andradite. Almandine and pyrope represent maximum and minimum entrapment pressure estimates, respectively, for garnet 116 117 endmembers with the Y-site occupied by Al and the X-site occupied by Fe, Mn, Mg and Ca. 118 Andradite, $Ca_3Fe_2(SiO_4)_3$, is a common garnet species in hydrothermal skarn deposits, and is characterized by elastic moduli significantly different from those of other modeled garnets. The 119 120 shear moduli for almandine, pyrope and andradite are 921, 902 and 860 kbar, respectively (Wang 121 and Ji, 2001). Although not included in Fig. 2, isomekes for other garnet endmembers (e.g.,

spessartine, grossular) can be estimated based on those for the calculated (extreme) endmembers, according to the relative magnitudes of their compressibilities, expansivities and shear moduli. For example, isomekes for grossular (shear modulus ca. 98.1 GPa) would fall between those projected for apatite in almandine (Fig. 2a-c) and pyrope (Fig. 2d-f), and would be <1 kbar offset from either of these latter two endmembers

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128 Raman spectroscopy and heating experiments

Samples analyzed in this study included fluorapatite from Durango, Mexico, and 129 130 fluorapatite inclusions within andradite garnet from Casting Copper, Nevada. The Durango 131 apatite sample was a single crystal, which was cut into a ca. 500 µm-thick wafer and doubly polished. The Casting Copper apatite grains are µm-sized inclusions within euhedral garnet 132 133 grains. The garnet grains were cut into $\sim 1000 \,\mu$ m-thick wafers and doubly polished. Apatite inclusions within the garnet grains were then identified using transmitted light microscopy. 134 135 Polishing of the garnet samples also resulted in some apatite inclusions being exposed on the polished surface of the garnet wafer, and these exposed inclusions were identified using reflected 136 light microscopy. 137

Unpolarized Raman spectra were collected using a Thermo Nikolet Almega microRaman
system at the Mike Scott Laboratory for Mineralogy and Crystallography at the University of
Arizona. Raman spectra were collected in a back-scattering arrangement. We used a 532 nm
excitation laser, with laser power set to ~100 mW. Focusing of the excitation laser onto the
polished apatite wafer (Durango) and the apatite inclusions within garnet grains (Casting
Copper) was accomplished using a Nikon 10x, long working distance objective on an Olympus

BX51 microscope. The spectrometer position was calibrated using the ca. 1100 cm⁻¹ Raman line
of sparry calcite.

146 For the heating and cooling experiments, we used a Linkam THMSG600 stage mounted 147 on the Raman microprobe. Temperature settings of the stage were calibrated using synthetic fluid-inclusion standards (triple point of CO₂ at -56.6 °C; triple point of H₂O at 0.01 °C; critical 148 149 point of H₂O at 374.1 °C), and is accurate to within ± 0.1 °C from subzero temperatures to ~100 $^{\circ}$ C, and to within ± 0.5 $^{\circ}$ C at higher temperatures. Temperature-dependent Raman measurements 150 (Fig. 3) were conducted at 50 °C increments from 25 to +275°C, and each measurement was 151 152 replicated also on the cooling path from 275 to 25 °C to confirm that the inclusions had not been 153 modified by plastic deformation. Subsequently, the samples were also analyzed along a cooling path at 50 °C increments from 25 to -175 °C, with replicate analyses conducted along the 154 associated re-heating path to room temperature. At each temperature (from -175 to 275 °C), we 155 analyzed the wafer of the Durango apatite standard, and several inclusions at or below the 156 157 surface of the Casting Copper garnet wafers. The calcite standard was analyzed before and after each temperature profile to check and potentially correct for spectrometer drift (no drift was 158 detected). 159

Raman spectra were analyzed using the software package PeakFit v.4.11 from SYSTAT Software Inc. The workflow involved a linear baseline subtraction followed by peak fitting using a Gaussian+Lorentzian Area model. Satisfactory fitting of the apatite v_{964} peak (i.e., the phosphate symmetric stretch, $v_1(A_g+E_{2g})$ mode; Comodi et al., 2001) was accomplished by using three peaks: the main sharp peak centered at ca. 964 cm⁻¹, and two broader, shorter peaks centered at ca. 950 and 1030 cm⁻¹. The latter of these peaks corresponds to the asymmetric stretch, $v_{3b}(E_{2g})$ vibrational mode of phosphate, according to Comodi et al. (2001). The peak

centered at ca. 950 cm⁻¹ is manifested only as a slight, lower-wavenumber shoulder on the larger 167 v_{964} peak; according to Liu et al. (2008), this shoulder represents a distortion of the symmetric 168 stretching mode owing to radiation damage (fission tracks) in apatite. Our estimated uncertainty 169 on peak position is approximately ± 0.141 cm⁻¹, according to replicate measurements and peak 170 fitting performed on the Durango apatite standard during every analytical session. 171 The methods for defining the pressure- and temperature-dependent Raman waveshifts of 172 minerals is described in detail by Watenphul and Schmidt (2012). Briefly, the shift in Raman 173 174 peak position with respect to that at a reference temperature and pressure (normally, 25 °C and 1

- 175 bar) is expressed as:
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$$\Delta \boldsymbol{\nu}_i(\boldsymbol{P}, \boldsymbol{T}) = \boldsymbol{\nu}_i(\boldsymbol{P}, \boldsymbol{T}) - \boldsymbol{\nu}_i\left(\boldsymbol{P}_{ref}, \boldsymbol{T}_{ref}\right)$$
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$$= (\Delta \boldsymbol{\nu}_i)_{\boldsymbol{P}, \boldsymbol{T}_{ref}} + (\Delta \boldsymbol{\nu}_i)_{\boldsymbol{T}, \boldsymbol{P}_{ref}} + (\Delta \boldsymbol{\nu}_i)_{\boldsymbol{P}, \boldsymbol{T}} \qquad \text{eq. 2}$$

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where $(\Delta v_i)_{P,T_{ref}}$ is the pressure-dependent contribution at the reference temperature, $(\Delta v_i)_{T,P_{ref}}$ 180 is the temperature-dependent contribution at the reference pressure, and $(\Delta v_i)_{PT}$ is the 181 182 remaining contribution referred to by Watenphul and Schmidt (2012) as the "cross term." The latter term reflects any variation in the temperature dependence with changing pressure or the 183 184 pressure dependence with changing temperature. For several minerals, available experimental data indicate that the cross term is negligible and can be assumed to be zero (e.g., quartz: 185 186 Schmidt and Ziemann, 2000; fully crystalline zircon: Schmidt et al., 2013). However, this 187 assumption must be tested on a case-by-case basis for other minerals. Inclusion pressures for fluorapatite inclusions at room temperature can be determined 188 through the *P*-sensitive frequency shift of the 964 cm⁻¹ band or by *in situ* X-ray diffraction (Fig. 189

190 4). The polynomial for the $P - \Delta v_{964}$ relationship at 25 °C, calculated with the experimental

- 191 data of Schouwick et al. (2010), is
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$$\boldsymbol{P}(\mathbf{bar}) = \left(\boldsymbol{a} \cdot (\Delta \boldsymbol{\nu}_{964})_{\boldsymbol{P},\boldsymbol{T}_{ref}}^{2}\right) + \left(\boldsymbol{b} \cdot (\Delta \boldsymbol{\nu}_{964})_{\boldsymbol{P},\boldsymbol{T}_{ref}}\right) \qquad \text{eq. 3}$$

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where *a* and *b* are regression parameters equal to 7.35 ± 1.88 and 2265 ± 59 , respectively. The results obtained using this expression are very similar to pressures calculated using the equation of Comodi et al. (2001). The parameter $(\Delta \nu_{964})_{P,T_{ref}}$ represents the difference between the measured peak position and the reference (1 bar) peak position, at the reference temperature of 25 °C.

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RESULTS

The data shown in Fig. 5 allow us to define the temperature-dependent portion of eq. 2. For this regression analysis, we included both the temperature-dependent waveshift of the Durango fluorapatite standard, as well as the temperature-dependent waveshift of a Casting Copper apatite inclusion that was exposed to the sample surface during polishing. Thus, all data shown in Fig. 5 correspond to a reference pressure of 1 bar. The polynomial expression derived from regression analysis of these data is:

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 $(\Delta \nu_{964})_{T,P_{ref}} (\mathbf{cm}^{-1}) = \mathbf{c} \cdot \mathbf{T}^2 + \mathbf{d} \cdot \mathbf{T} + \mathbf{e} \qquad \text{eq. 4}$

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- where T is in °C and c, d and e are regression coefficients equal to -0.0000134 ± 0.0000011 , -
- 212 0.0070 ± 0.00018, and 0.287 ± 0.029, respectively (Fig. 4). The parameter $(\Delta \nu_{964})_{T,P_{ref}}$

213	represents the temperature-dependent waveshift, relative to 25 °C, at the reference pressure of 1
214	bar. Combining equations 2, 3 and 4 (Watenphul and Schmidt, 2012) yields the general
215	expression:
216	
217	$P(\text{bar}) = a \cdot (\Delta v_{964} - c \cdot T^2 - d \cdot T - e)^2 + b \cdot (\Delta v_{964} - c \cdot T^2 - d \cdot T - e) \qquad \text{eq. 5}$
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219	Equation 5 represents the combined temperature- and pressure-dependent Raman shift,
220	and can thus be used to compute inclusion pressures from -175 to 275 °C. Coefficients a-e are
221	the same as those listed for eqs. 3 and 4 (above). Notice that eq. 5 assumes a negligible cross

term, analogous to the study by Watenphul and Schmidt (2012), although validation of thisassumption for apatite will require future experiments.

Pressures of fully encapsulated apatite inclusions from Casting Copper were calculated 224 225 using eq. 5, with the reference peak position (ν_{964}) determined based on the measurements of the inclusion exposed to the sample surface (Table 3). The Durango apatite standard was not 226 227 used for the reference peak position because we noted systematic differences between the 1 bar peak positions of Durango standard versus the exposed apatite inclusions from Casting Copper 228 (Table 3). These differences are thought to reflect chemical effects according to substitutions in 229 the X (halogen) site in the apatite structure. Specifically, apatite from Durango contains 230 approximately ~3.5 wt% F and 0.4 wt% Cl on average (Young et al., 1969) whereas apatite 231 232 inclusions from Casting Copper contain on average 2.7 wt% F and 0.1 wt% Cl (D. Barkoff, 233 unpublished data), with more significant mixing between the F and OH endmembers. Thus, 234 standardizing the inclusion measurements according to an exposed inclusion on the sample

235	surface seems to be the best practice, implicitly accounting for the chemical composition of the
236	apatite inclusions in a given sample.

237	The fully encapsulated inclusions of apatite in garnet from Casting Copper exhibit
238	negative waveshifts at 25 °C, indicating that the inclusions are under tension at ambient
239	temperature. Similar phenomena have been reported for quartz inclusions in garnet from
240	relatively high-temperature, low-pressure terranes (e.g., Kouketsu et al. 2014; Ashley et al.,
241	2015). During heating to 275 °C, the fully encapsulated inclusions undergo progressive
242	pressurization (Table 3, Fig. 6), owing to the differential thermal expansion of inclusion and
243	host. Conversely, cooling the sample to subzero temperatures results in decreased pressure
244	within the inclusions (i.e., increased tensile stress). The pressure variations within the inclusions
245	induced by both heating and cooling appear to be elastic and reversible in nature, as indicated by
246	the replicate analyses conducted during re-cooling/re-heating the sample to room temperature
247	(Table 3).

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DISCUSSION

250 Temperature and Pressure sensitivity of the v_{964} band of apatite

Equations 4 and 5 allow us to assess the temperature and pressure sensitivity of the v_{964} band of apatite, which are factors in evaluating the usefulness of apatite for barometry. From eq. 4, the average $\delta v / \delta P$ slope of apatite is approximately ~4.4 cm⁻¹/GPa at 1 bar, increasing gradually with increasing pressure. For comparison, the average $\delta v / \delta P$ slope of the ~464 cm⁻¹ peak of quartz is 9 cm⁻¹/GPa (Schmidt and Ziemann 2000), and that of the ~1008 cm⁻¹ peak of fully crystalline zircon is 5.7 cm⁻¹/GPa. As such, apatite is less suitable for spectroscopic barometry (i.e., has a lesser peak shift for equivalent pressurization) than these two latter

258	minerals, but nevertheless the apatite pressure is still resolvable and quantifiable by peak fitting.
259	In terms of temperature sensitivity, the 464 cm ⁻¹ band of quartz exhibits a modest temperature
260	sensitivity of only ~-0.014 cm ⁻¹ / $^{\circ}$ C (Schmidt and Ziemann 2000), making quartz well suited for
261	pressure determination at elevated temperatures, for example in hydrothermal diamond-anvil
262	cells (HDACs). Fully crystalline zircon shows a greater and more variable temperature
263	sensitivity of the 1008 cm ⁻¹ peak position, from ~-0.03 cm ⁻¹ / $^{\circ}$ C at room temperature to ~-0.04
264	cm ⁻¹ /°C at T \ge 500 °C (Schmidt et al. 2013). Schmidt et al. (2013) noted that relative sensitivity
265	of the zircon peak position to temperature implies that temperatures must be well known in order
266	to use zircon as pressure sensor in HDACs. In comparison, apatite shows a relatively modest
267	temperature sensitivity of the ca. 964 cm ⁻¹ peak position, more comparable to that of quartz: at
268	room temperature, $\delta v / \delta T$ of the apatite 964 cm ⁻¹ peak is just -0.008 cm ⁻¹ /°C, and at 300 °C
269	$\delta v/\delta T$ and the same peak is -0.015 cm ⁻¹ /°C. As such, apatite may be a fairly suitable
270	spectroscopic pressure sensor for HDAC experiments. Certainly, quartz provides a better
271	pressure sensitivity, but in some circumstances quartz becomes unsuitable for HDAC
272	experiments because of high solubility in aqueous fluids (e.g., Schmidt et al. 2013) such that the
273	quartz grain used for barometry may be partially or completely dissolved in the aqueous solution
274	within the HDAC. In such cases, apatite may represent an alternative. For example, Antignano
275	and Manning (2008) reported fluorapatite solubilities in H_2O that were in some cases
276	approximately three orders of magnitude less than that of quartz at similar pressure-temperature
277	conditions.

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279 Applicability of apatite inclusions in garnet for barometry constraints

280	Figure 2 shows the significant dependence on entrapment pressure and not on entrapment
281	temperature for the pressurization of apatite inclusions in garnet, indicating that apatite
282	inclusions in garnet are suitable for barometric constraints. The slope of the contoured isomekes
283	and the spacing between them can be explained by comparing the elastic moduli between the
284	inclusions and hosts. Andradite, which has the greatest thermal expansivity of the modeled
285	garnet species (2.86 x 10^{-5} K ⁻¹ ; Holland and Powell, 2011) and thus that most similar to apatite
286	$(3.0-3.4 \text{ x } 10^{-5} \text{ K}^{-1})$, exhibits the smallest thermal dependency (i.e., flatter isomeke slopes; Fig.
287	2). Andradite also has a lower bulk modulus compared to almandine and pyrope, resulting in less
288	pressure sensitivity of the barometer (i.e., isomekes are spaced further apart). Chlorapatite has
289	the lowest thermal expansivity and therefore the least thermal dependence for entrapment
290	pressure constraint. Interestingly, chlorapatite inclusions in andradite transition from isomeke
291	contours with a slight positive slope at low P , to no slope at ~6 kbar, to a negative slope at higher
292	P (Fig. 2h). This latter phenomenon results from the thermal expansivity of and radius being
293	greater than that of CAP at elevated P. However, caution should be used when using the fitted
294	equation of state for CAP because the lack of high-quality P - V data resulted in the poorest
295	quality of fit and the largest uncertainties on the elastic parameters among the three apatite
296	endmembers (Table 2). Regardless, all apatites show good pressure sensitivity that makes any
297	endmember suitable for barometric constraints. Mixing between FAP and HAP is expected to
298	only introduce small changes to the calculated entrapment pressures as long as the dominant
299	endmember isomeke contours are used. The isothermal bulk modulus of carbonated
300	hydroxyapatite is significantly decreased by the presence of carbonate (up to $\sim 20\%$; Liu et al.
301	2011; Forien et al. 2015). This lower bulk modulus is advantageous for barometry, resulting in
302	improved pressure retention and sensitivity of the apatite-in-garnet barometer. Calorimetric

303	measurements made by Hovis and Harlov (2010) for mixing between the fluor- and chlorapatite
304	species recognized a high degree of thermodynamic non-ideality (without any detected
305	miscibility gap); therefore caution should be used when applying this technique to inclusions
306	with significant mixing along the F-Cl join. We recommend using the fluorapatite projections
307	whenever possible because fluorapatite is the most abundant endmember of apatite in rocks
308	(Hovis et al. 2015), especially at higher temperatures where devolitization reduces the mole
309	fraction of hydroxyapatite, and most of the single-crystal compression and heating experimental
310	data has been reported for this endmember, allowing for improved EOS fitting.

311

312 Insights gained from *in situ* heating experiments on apatite inclusions within garnet

313 Heating experiments conducted on inclusions in garnet are important for two reasons. Firstly, the heating experiments can be used to confirm that the inclusions record residual 314 pressures owing to elastic deformation. The difference between the Raman peak position of 315 316 Durango apatite and the Casting Copper apatite exposed at the sample surface (described above) 317 highlights a potential complexity in using apatite inclusions for barometry: Namely, that the 318 Raman peak position is affected by the chemical composition of apatite. Quartz inclusions in 319 garnet, which have been more commonly used in barometry, do not suffer from this complication 320 owing to extremely limited solid solution in quartz. Apatite, by contrast, can accommodate an 321 array of major and trace elements, and as such, the reference standard for computing Δv_{964} 322 should be closely matched to the targeted unknowns. The procedure described herein, using one or more apatite inclusions exposed to the surface of the same garnet crystal as reference, 323 324 provides an obvious method to ensure close matching of reference and unknown. However, the

possibility of a single garnet grain hosting apatite grains of different compositions cannot be excluded a priori. Therefore, heating experiments provide a method to test that the Raman shift exhibited by encapulated inclusions records a reproducible inclusion pressure. For example, the inclusions shown in Fig. 6 show pressurization with increasing temperature, and a return to tensile conditions upon subsequent cooling – neither of which would occur as a result of chemical differences between inclusion and reference material. Thus the heating experiments provide confidence that the inclusions are not compromised.

The second reason that heating experiments on mineral inclusions are useful is for testing 332 333 the quality of the modeling approach when calculating entrapment pressures. For quartz 334 inclusions in garnet, a significant offset between modeled and measured P_{incl} with heating and 335 cooling has been observed (Ashley et al. 2016). This offset was also detected when calculating 336 entrapment pressure for measurements made at each temperature step. In theory, the calculated 337 entrapment pressure should be identical for each temperature step. However, calculated 338 entrapment pressure exhibited an apparent decrease when the encapsulated inclusions were 339 heated. Independent *P*-*T* estimates are in best agreement with entrapment pressures calculated 340 from measurements obtained when inclusions were heated to the reported formation temperature. 341 There are several factors that may lead to this discrepancy (applying a 1D elastic model for an 342 anisotropic phase, difficulties in accurately modeling quartz volume in proximity of the α - to β -343 quartz transition, etc.), but regardless the current modeling approach results in entrapment 344 pressure overestimation when using room-T measurements in the case of quartz inclusions. In 345 contrast, the heating experiments on apatite inclusions show pressure variations that are in good agreement with the model predictions (Fig. 6). As such, these results suggest that the model 346

provides good predictions for apatite inclusions within andradite garnet, which suggests thatentrapment pressures can be reliably calculated using this approach.

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350 **IMPLICATIONS FOR BAROMETRY** 351 Apatite inclusions in garnet can be used for barometry across a wide range of P-T352 conditions. Apatite inclusions will be especially useful for rocks in which no other means of 353 pressure estimation is available. Whereas barometry based on chemical equilibrium through net-354 transfer reactions is common in petrology, numerous environments and systems lack mineral 355 assemblages appropriate for pressure constraints. Certain inclusion minerals are useful 356 petrogenic indicators of formation conditions based solely on phase stability (e.g., coesite, 357 diamond). For minerals such as apatite, which are stable over wide ranges of P and T, estimation 358 of retained inclusion pressures based on spectroscopic measurements is a rapidly developing 359 technique in petrologic studies. While apatite-in-garnet has not been used for such applications to 360 date, the extensive stability of apatite in metamorphic and igneous systems, coupled with the 361 ubiquity of apatite in a wide range of rock compositions, make apatite an attractive inclusion 362 mineral to consider for geobarometry. Moreover, apatite exhibits less of a dependence on 363 entrapment temperature than other inclusion-host systems commonly used for barometry (e.g., quartz inclusions in garnet), especially considering chlorapatite inclusions in andradite. Thus, 364 365 apatite inclusions in garnet permit reasonable pressure estimation even if temperature is only 366 loosely constrained. Heating experiments provide an internal validation that the application of a 367 1D (isotropic) elastic model is sufficient for calculating entrapment conditions. This is a benefit 368 over using quartz inclusions in garnet because a significant departure between calculated and 369 measured inclusion pressure with heating is observed for quartz, and a correction is needed to

370	account for the overestimation in entrapment pressures (Ashley et al. 2016). Extensive
371	thermodynamic characterization of mixing in the apatite F-Cl-OH ternary system is still required
372	to better resolve modifications to the elastic parameters in chemically impure crystals. Further
373	research conducting high-resolution P-V-T studies on apatites of different compositions and
374	investigations into P- and T-induced Raman waveshift may further improve the resolution of this
375	technique.
376	
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477	FIGURE CAPTIONS
478	
479	Figure 1. Fitted curves from the Tait equation of state of fluorapatite compared to the
480	experimental data of (a) Hovis et al. (2014) and (b) Schouwink et al. (2010).
481	
482	Figure 2. Isomeke contours for inclusion pressures (in kbar) for apatite inclusions in garnet.
483	Inclusion endmembers include fluorapatite (a,d,g), chlorapatite (b,e,h) and
484	hydroxyapatite (c,f,i). Garnet species modeled as host phase includes almandine (a-c),
485	pyrope (d-f) and andradite (g-i).
486	
487	Figure 3. (a) Example of peak fitting protocol used in this study, showing the fitted v_{964}
488	(phosphate symmetric stretch) and v_{950} (radiation damage) peaks. The lower wavenumber
489	tail of the v_{1030} (phosphate antisymmetric stretch) peak is visible on the right hand side.
490	See text for additional details. (b) The v_{964} Raman band of Durango fluorapatite, as a
491	function of temperature. Spectra in black were acquired along the heating path, whereas
492	spectra in dashed gray lines were acquired along the cooling path.
493	
494	Figure 4. Pressure-sensitive Raman waveshift regression for fluorapatite calculated from the
495	experimental data of Schouwink et al. (2010). The polynomial expression can be used to
496	calculate inclusion pressures for fully encapsulated apatite inclusions and formation
497	pressure can be determined using the isomeke contours in Figure 2.
498	

499	Figure 5. Temperature-sensitive Raman waveshift regression for Durango (fluor)apatite and
500	apatite from the Casting Copper mine, Yerington district, NV.
501	
502	Figure 6. Inclusion pressures of the Casting Copper apatite inclusions as a function of
503	temperature. The line shows the predicted P_{incl} -T relationship, calculated with the 1D
504	elastic model.
505	
506	





Figure 2



Figure 3



Figure 4



Figure 5



Figure 6



Table 1. Sources of volume data used for EOS fitting of apatite endmembers

	Thermal Expansion	Compressibility
fluorapatite	Hovis et al. (2014) – Durango,	Schouwink et al. (2010) – Durango,
	Mexico	Mexico
chlorapatite	Hovis et al. (2015) – APS26 (synthetic)	Brunet et al. (1999) – synthetic
hydroxyapatite	Hovis et al. (2014) – Holly Springs, Georgia	Brunet et al. (1999) – synthetic

Note: Sample localities are given for natural samples. Please see respective sources for additional information, including apatite chemistry.

Table 2. Thermodynamic properties and modified Tait *P*-*V*-*T* EOS fit parameters of apatite

	S° ₂₉₈ (J mol ⁻¹ K ⁻¹)	V ₂₉₈ (Å ³)	α ₂₉₈ x 10 ⁶ (K ⁻¹)	к ₂₉₈ (kbar)	κ'_{298}	κ ^{''} ₂₉₈ (kbar ⁻¹)	$ heta_E$ (K)
Fl-apatite	$383.2(1.5)^1$	525.86(3)	32.9(3)	868(5)	5.63(15)	-0.00648	430.82
Cl-apatite	$400.6(1.6)^1$	544.86(11)	30.0(2.5)	846(58)	6.6(1.0)	-0.00779	416.83
OH-apatite	$390.4(1.7)^2$	529.32(3)	33.6(7)	913(15)	5.55(26)	-0.00608	424.92

Note: κ_{298}'' is an estimated value from the EOS fitting and the Einstein temperature (θ_E) is estimated by $\theta_E = 10636/(S_{298}^\circ/n_i + 6.44)$, where n_i is the number of atoms in the endmember *i* (see Holland and Powell 2011 for details).

¹Dachs et al. (2010); ²Robie and Hemingway (1995)

 Table 3. Raman spectroscopic heating data on apatite samples

Т	Durango ¹	CC01 ²		CCO2 ³			CC06 ³	
(°C)	V964	V ₉₆₄	V ₉₆₄	Δv_{964}^{4}	P (bar)	V ₉₆₄	Δv_{964}^{4}	P (bar)
25	965.32	966.24	965.76	-0.51	-1380	965.76	-0.51	-1380
75	965.17	966.08	965.51	-0.76	-1003	965.62	-0.65	-754
125	964.63	965.53	965.23	-1.04	-542	965.13	-1.14	-768
175	963.90	964.85	964.76	-1.51	-358	964.67	-1.60	-562
225	963.31	964.22	964.04	-2.23	-589	963.99	-2.28	-702
275	962.68	963.58	963.77	-2.50	351	963.57	-2.70	-103
225	963.37	964.32	964.29	-1.98	-23	964.29	-1.98	-23
175	963.96	964.96	964.82	-1.45	-223	964.72	-1.55	-449
125	964.70	965.60	965.24	-1.03	-519	965.10	-1.17	-835
75	965.00	966.02	965.63	-0.64	-731	965.56	-0.71	-890
25	965.33	966.32	965.71	-0.56	-1492	965.83	-0.44	-1222
-25	965.71	966.65	966.26	-0.01	-1041	966.29	0.02	-973
-75	965.99	966.98	966.43	0.16	-1296	966.65	0.38	-799
-125	966.37	967.33	966.70	0.43	-1174	966.73	0.46	-1106
-175	966.42	967.33	966.56	0.29	-1826	966.51	0.24	-1939
-125	966.30	967.48	966.68	0.41	-1219	966.75	0.48	-1061
-75	965.92	966.96	966.62	0.35	-867	966.44	0.17	-1274
-25	965.67	966.68	966.39	0.12	-747	966.13	-0.14	-1334
25	965.31	966.24	965.89	-0.38	-1086	965.89	-0.38	-1086

¹Fluorapatite standard from Durango (Cerro de Mercado mine), Mexico

²Fluorapatite inclusion in garnet from the Casting Copper mine, Yerington district, NV. Exposed at the sample surface.

³Fluorapatite inclusion in garnet from the Casting Copper mine, Yerington district, NV. Fully encapsulated within garnet.

⁴Waveshifts relative to average v_{964} for CC01 at 25 °C and 1 bar (966.27 ± 0.05 cm⁻¹)