

## Appendix 2 - Error analysis

The uncertainties associated with  $y$ , estimated composition, are computed as follows:

$$\sigma_y^2 = \sigma_{SE}^2 + \sigma_{y_{uc}}^2$$

Where:

$$\sigma_{SE}^2 = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

Where  $n$  is the number of datasets in the regression;  $y_i$  and  $\hat{y}_i$  are the observed and calculated  $y$  values of the regression data, respectively.

and

$$\sigma_{y_{uc}}^2 = \frac{1}{m} \sum_{j=1}^m (\hat{y}_j - \hat{y}_{j_{\sigma_{uc}}})^2$$

Where  $m$  is the number of unit-cell parameters in the function (e.g., five in plagioclase),  $\hat{y}_j$  is the composition calculated with your input unit-cell parameters,  $\hat{y}_{j_{\sigma_{uc}}}$  is the calculated composition calculated with the error associated with your unit-cell parameter added to the unit-cell parameter [e.g.,  $a_{\sigma_{uc}} = (a + \sigma_a)$ ].

Errors associated with arithmetical equations were computed with the following formula:

$$\sigma_{y_i}^2 = \sum_i^n \sigma_{x_i}^2$$

Where  $\sigma_{x_i}$  is the uncertainty associated with each coefficient in the equation.

$$\text{Root-Mean-Square Error (RMSE)} = \sqrt{\frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{n}}$$

Where  $n$  is the number of datasets in the regression;  $y_i$  and  $\hat{y}_i$  are the observed and calculated  $y$  values of the equation, respectively.