A comparison of the structures and geometric stabilities of stilpnomelane and parsettensite: A distance least-squares (DLS) study

STEPHEN GUGGENHEIM

Department of Geological Sciences, University of Illinois at Chicago, Chicago, Illinois 60680, U.S.A.

R. A. Eggleton

Department of Geology, Australian National University, Canberra, ACT 2601, Australia

ABSTRACT

Structural models for the islandlike modulated phyllosilicates, stilpnomelane and parsettensite, were examined by distance least-squares (DLS) calculations. Parsettensite occurs naturally only near the Mn end-member, whereas stilpnomelane may be both Mn and Fe²⁺ rich. Models for compositions between Fe²⁺ and Mn²⁺ end-member stilpnomelane demonstrated that the stilpnomelane structure is geometrically stable across the composition range. In principle, therefore, stilpnomelane may occur at Mn end-member compositions. DLS calculations indicated also that Fe²⁺- and Mn²⁺-rich stilpnomelane-cell edge lengths are geometrically controlled; *c* is fixed at approximately 17.835 Å ($d_{001} =$ 12.13 Å). DLS-derived atomic coordinates are given for stilpnomelane.

Misfit in stilpnomelane between the tetrahedral and octahedral sheets is relieved by warping of the octahedral sheet and by adjustments to the double six-membered ring interisland connectors. These adjustments include an in-plane tetrahedral rotation and out-of-plane tilting. In Mg- or Fe³⁺-rich stilpnomelane, Si to Si distances within the interisland connectors are reduced and Si to Si repulsions increase. Thus, tetrahedral tilting in the interisland connectors increases, along with the magnitude of the d_{001} value. In contrast to parsettensite, however, only limited tilting of the tetrahedra in these connectors may occur, which accounts for the different d_{001} values in the two model structures.

In parsettensite, double four-membered ring interisland connectors do not allow for tetrahedral rotation, and, therefore, parsettensite requires the nearly perfect alignment of islands. Thus, parsettensite probably cannot have a composition with smaller octahedral cations (e.g., Fe^{2+}).

INTRODUCTION

Stilpnomelane (Eggleton, 1972) and parsettensite (Eggleton and Guggenheim, 1994) are modulated layer silicates with continuous octahedral sheets coordinated by partial sheets of silicate tetrahedral rings. These rings form islands that are three tetrahedral rings wide, with islands connected by inverted tetrahedra. The two structures differ, however, by the topology of the island linkage. Parsettensite has partially tilted tetrahedra that form fourmembered interisland connectors, thereby producing double four-membered rings to connect adjacent layers and $d_{001} = 12.6$ Å. In contrast, stilpnomelane has sixmembered ring interisland connectors and, thus, double six-membered rings to connect adjacent layers, with a resulting $d_{001} = 12.1 - 12.6$ Å, depending on composition (see below). Figures depicting the geometry of the structures may be found in Eggleton (1972) and Eggleton and Guggenheim (1994).

The parsettensite structure is known to exist near Mn end-member compositions only (Eggleton and Guggenheim, 1994). Stilpnomelane, however, commonly occurs with Fe-rich compositions, although considerable Mg and Mn substitutions are possible (Dunn et al., 1984, 1992). Where Mn is present, the amount of Mn substitution in stilpnomelane only approaches about half the possible octahedral sites. In addition, at least for the limited number of Mn-dominant stilpnomelane samples known, Mn is associated with a significant proportion of smaller cations, such as Mg and Zn. Guggenheim and Eggleton (1987, 1988), in a review of modulated phyllosilicate systematics, discussed the importance of misfit between the lateral dimensions of the octahedral and tetrahedral sheets in such structures. A major feature of such structures is a warping of the octahedral sheets, either wavelike or domelike, depending on the nature of the modulation. However, the relationships of the interisland connectors to misfit between the tetrahedral and octahedral sheets are not well understood.

A distance least-squares (DLS) investigation was made to establish geometric constraints on the stilpnomelane structure with Fe vs. Mn octahedral occupancy as the important variable. This study was made (1) to determine why parsettensite has a d_{001} value of near 12.6 Å, whereas a Mn-rich stilpnomelane has a value near 12.1 Å, and (2) to establish the role, if any, of the interisland connectors in relieving misfit between the tetrahedral and octahedral components. An investigation of the extent of cation substitutions in stilpnomelane is potentially more revealing petrologically than an alternate investigation regarding the extent of cation substitutions in parsettensite because stilpnomelane is a rock-forming mineral. In addition, however, data given below suggest that it may not be possible to predict accurately an appropriate set of cell parameters for a hypothetical Fe-rich parsettensite, which is a requirement for a successful DLS investigation of this type.

The DLS approach (Meier and Villiger, 1969) uses interatomic distances in a least-squares refinement. Atomic positional positions are adjusted so that the calculated distances match, as best as possible, the distances used as input. Because the distances may be given weights equal to interatomic forces, the modeling approach may be considered an analogy to a force model. The distances used for input are generally established by using interatomic distances from similar materials. In this study on parsettensite and stilpnomelane, the only parameters derived experimentally are those based on cell parameters and space group and, of course, the topology (polyhedral linkages) of the structure as derived in the structure determinations (Eggleton, 1972; Eggleton and Guggenheim, 1994). Thus, because the models utilize such limited observed data, the procedure confirms only that the linkages are dimensionally reasonable. However, even if the linkages are plausible, the technique cannot determine the correctness of the structure without ancillary techniques.

Experimental methods

Both the stilpnomelane and the parsettensite structures have interatomic distances at the Mn end-member in common. DLS input parameters for parsettensite included Mn-O distances (2.230 Å at 0.5 weight), T-O distances (1.625 Å at 1.0), O-O distances about the Mn sites (3.280 Å at 0.07), O-O distances about the T sites (2.655 Å at 0.07), and T-T distances (3.100 Å at 0.3). Because of differences in Al occupancy, the input for stilpnomelane was identical, except for T-O distances of 1.633 Å (wt = 1.0) and O-O distances about the tetrahedra of 2.665 Å (wt = 0.07). No attempt was made to model the positions of exchangeable cations for either structure. These cations do not represent an integral part of the structure, and first coordination spheres are difficult to locate. The DLS program (DLS-76) of Baerlocher et al. (1978) was used in the analysis, along with bond distances from Shannon (1976) and weights primarily from Baur (1977).

Parsettensite

DLS modeling was done in space group C2/m using a = 39.1, b = 22.84, c = 17.95 Å and $\beta = 135.6^{\circ}$ (Eggleton and Guggenheim, 1994). Because of the expected misfit between the tetrahedral and octahedral sheets, a small domed shape (± 0.2 Å) was imparted to the apical O plane associated with the Mn sheet, with the dome crest at the center of the islands. There were 98 independent

atoms, 267 variables, and 414 distances. Besides parameters held invariant by special positions, all z coordinates of the apical O atoms and O atoms at z = 0.5 were fixed for five cycles of refinement, after which only space group invariant coordinates and O z coordinates at z = 0.5 were fixed. This model, using the above input distances, assumes complete Al vs. Si disorder. Refinement converged in six additional cycles (R = 0.006), and atom positions are given in Table 3 of Eggleton and Guggenheim (1994).

Additional DLS models were made to determine ^[4]Al ordering, with Al being concentrated either in the island regions or in the interisland (double four-membered ring) connectors. The latter model would not converge; Al-rich tetrahedra expanded to unreasonable sizes (T-O distances of 1.82 Å). This result, therefore, suggests that this model is topologically impossible. The model, involving Al-rich tetrahedra within the islands, could not be distinguished by DLS refinement from the original model, with complete Si vs. Al disorder.

Stilpnomelane

Starting atomic coordinates were derived from figures in Eggleton (1972), which resulted in 168 independent atoms, 494 variables, and 767 observations (distances) in $P\overline{1}$ symmetry. The M1 site was held fixed, as were the six apical O z coordinates (z = 0.00) for the interisland tetrahedral connectors. Similar to parsettensite, a domelike shape was imparted to the apical O plane. Unlike in parsettensite, where only one composition is known, cell parameters from many stilpnomelane compositions may be used to extrapolate to a hypothetical Mn end-member composition based on Eggleton and Chappell (1978) and the ideal cell geometry (Eggleton, 1972).

The value for d_{001} for stilpnomelane varies from 12.6 to about 12.15 Å for compositions where the octahedral cation radius (r_o) is between about 0.66 and 0.70 Å, but it remains nearly constant (about 12.13 Å) for compositions between values for r_o of 0.71–0.76 Å. Thus d_{001} for Mn end-member stilpnomelane is expected to be similar upon extrapolation (12.13 Å), resulting in c = 17.835 Å. The *a* dimension varies linearly from r_o values of 0.65–0.76 Å (linear equation: a = 18.6345 + 4.5738r, R = 0.97). Therefore, the derived Mn end-member cell parameters are a = b = 22.43 Å, c = 17.835 Å, $\alpha = 125.125^\circ$, $\beta = 96.015^\circ$, $\gamma = 120.0^\circ$.

DLS calculations were made also for an Fe²⁺ endmember stilpnomelane and intermediate compositions at (Fe_{0.3}Mn_{0.7}), (Fe_{0.5}Mn_{0.5}), and (Fe_{0.7}Mn_{0.3}). Cell dimensions for an Fe²⁺ end-member stilpnomelane are a = b= 22.20 Å, c = 17.835 Å, $\alpha = 125.03^{\circ}$, $\beta = 95.98^{\circ}$, and $\gamma = 120.0^{\circ}$. The Fe-O distance was assigned at 2.180 Å, and O-O distances around the M sites were given values of 3.07 Å. Bond distances for intermediate compositions were assumed to be linear between the two end-members. The refinements converged within 18 cycles to an *R* value of 0.01. Because the atomic coordinates for stilpnomelane have not been published previously, they are listed for Fe end-member stilpnomelane in Table 1. Estimated

TABLE 1. Derived atomic coordinates for stilpnomelane

Atom	x	y	z	Atom	×	y	z
Fe1	0.3038	0.3533	0.5300	016	0.4199	0.0228	0.4077
Fe2	0.2171	0.4317	0.5217	017	0.4963	0.4307	0.4015
Fe3	0.1335	0.2639	0.5223	018	0.4945	0.6794	0.3978
Fe4	0.3803	0.5102	0.5144	019	0.5024	0.9361	0.4048
Fe5	0.0476	0.3439	0.5155	020	0.5013	0.1847	0.4037
Feo	0.2153	0.1784	0.5180	021	0.5791	0.3430	0.3951
Fe8	0.2964	0.4217	0.5075	023	0.5732	0.0009	0.3079
Fe9	0.1295	0.5084	0.5124	024	0.5854	0.1016	0.4045
Fe10	0.9679	0.1768	0.5164	025	0.6673	0.2635	0.3991
Fe11	0.0452	0.0893	0.5095	026	0.6583	0.5019	0.3836
Fe12	0.3828	0.2617	0.5153	027	0.6624	0.7626	0.3932
Fe13	0.5416	0.3321	0.4984	028	0.6708	0.0213	0.4071
Fe14	0.2087	0.6698	0.5035	029	0.7459	0.4235	0.3895
Fe15	0.9037	0.4212	0.5066	030	0.7440	0.0735	0.3817
Fe17	0.7931	0.0841	0.5036	032	0.7529	0.3343	0.4000
Fe18	0.8732	-0.0021	0.4972	033	0.8387	0.3502	0.4038
Fe19	0.2947	0.0882	0.5075	034	0.8292	0.5908	0.3864
Fe20	0.3747	0.0009	0.5004	O35	0.8333	0.8500	0.3950
Fe21	0.4616	0.1711	0.5043	036	0.8447	0.1116	0.4178
Fe22	0.3752	0.7519	0.5028	037	0.9233	0.2738	0.4125
Fe23	0.2905	0.8323	0.4992	038	0.9119	0.5086	0.3899
Si1	0.2804	0.0032	0.2901	039	0.9098	0.7599	0.3650
Si2	0.1991	0.3526	0.2869	041	0.0052	0.4375	0.4087
Si3	0.0380	0.2717	0.2876	042	0.0000	0.6807	0.3947
Si4	0.9582	0.1107	0.2882	043	0.0057	0.9416	0.4064
Si5	0.0390	0.0298	0.2872	044	0.0109	0.1986	0.4221
S16 Ci7	0.2029	0.1141	0.2933	045	0.0931	0.3635	0.4215
Si8	0.4320	0.5075	0.2001	040	0.0043	0.5996	0.4013
Si9	0.9534	0.3451	0.2751	048	0.0933	0.1160	0.4211
Si10	0.7952	0.0274	0.2841	049	0.2221	0.1652	0.2497
Si11	0.9530	0.8591	0.2728	O50	0.2224	0.2847	0.2468
Si12	0.2797	0.0268	0.2821	051	0.1010	0.2826	0.2454
Si14	0.3039	0.4910	0.2002	052	0.9801	0.1031	0.2461
Si15	0.1940	0.5873	0.2722	054	0.3023	0.0437	0.2455
Si16	0.0307	0.5022	0.2684	055	0.3366	0.2757	0.2378
Si17	0.7899	0.2606	0.2703	O56	0.2184	0.4012	0.2405
Si18	0.7090	0.0993	0.2710	057	0.9791	0.2800	0.2396
S(19 S:00	0.7066	0.8552	0.2678	058	0.8596	0.0402	0.2444
Si20	0.0312	0.7741	0.2023	059	0.9794	0.9180	0.2362
Si22	0.1950	0.8583	0.2716	061	0.4506	0.2656	0.2240
Si23	0.4366	0.0994	0.2712	062	0.4472	0.3860	0.2210
Si24	0.5120	0.2557	0.2630	O63	0.4505	0.5083	0.2190
Si25	0.8615	0.5596	0.1301	064	0.3340	0.5130	0.2299
5120	0.7219	0.5600	0.1311	065	0.2133	0.5158	0.2339
Si28	0.5819	0.2803	0.1309	067	0.09333	0.3957	0.2293
Si29	0.7212	0.2791	0.1311	068	0.8550	0.2722	0.2316
Si30	0.8603	0.4191	0.1303	O69	0.7323	0.1525	0.2297
Si31	0.5280	0.8945	0.1308	070	0.7398	0.0396	0.2371
Si32	0.3877	0.8937	0.1302	071	0.7369	0.9153	0.2348
5133	0.2476	0.7543	0.1305	072	0.7298	0,7871	0.2239
Si35	0.3865	0.6149	0.1313	074	0.0342	0.7927	0.2200
Si36	0.5268	0.7543	0.1313	075	0.0964	0.7883	0.2280
01	0.1801	0.2865	0.4307	076	0.2166	0.9163	0.2361
02	0.1723	0.5253	0.4153	077	0.3399	0.0380	0.2357
03	0.1683	0.7695	0.4023	078	0.4575	0.1496	0.2265
04	0.1737	0.0295	0.4142	079	0.5613	0.25/2	0.2012
06	0.2511	0.6855	0.4055	081	0.3370	0.4043	0.1909
07	0.2526	0.9391	0.4045	082	0.2105	0.6185	0.2080
08	0.2607	0.2036	0.4273	083	0.9605	0.4907	0.2054
09	0.3383	0.3627	0.4241	084	0.7324	0.2618	0.2071
010	0.3346	0.6048	0.4107	085	0.6077	0.0133	0.2058
012	0.3349	0.0000	0.4050	080	0.0000	0.7811	0.2033
013	0.4188	0.2730	0.4115	088	0.9616	0.6575	0.2044
014	0.4149	0.5193	0.4087	089	0.2115	0.7845	0.2070
015	0.4160	0.7686	0.4046	090	0.4405	0.0130	0.2062

TABLE 1.—Conti

Atom	x	y	z	Atom	x	y	z
091	0.8454	0.4906	0.1493	0100	0.2782	0.7082	0.1495
092	0.8134	0.5970	0.1667	0101	0.3249	0.6255	0.1671
093	0.6728	0.4951	0.1548	0102	0.4546	0.7107	0.1531
094	0.5846	0.3685	0.1677	0103	0.8241	0.4906	0.0000
095	0.6718	0.3164	0.1519	0104	0.6683	0.4881	0.0000
O96	0.8124	0.3669	0.1665	O105	0.5125	0.3321	0.0000
O97	0.5555	0.8551	0.1674	O106	0.5102	0.1776	0.0000
O98	0.4544	0.8839	0.1501	0107	0.6673	0.1761	0.0000
099	0.3266	0.8546	0.1665	O108	0.8230	0.3314	0.0000

standard deviations are not included because they have no physical meaning.

RESULTS

Stilpnomelane

The DLS calculations indicate that solid solution in stilpnomelane between Fe and Mn end-members is plausible on the basis of geometric connectivity. Comparisons between Fe²⁺ and Mn²⁺ end-members as derived by DLS indicate that both the islands and the interisland connectors adjust to compensate for the variation in octahedral cation size. Misfit is relieved between the tetrahedral and octahedral sheets in both Fe and Mn structures by the warping of the octahedral sheet (maximum variation in Δz for Fe cations of 0.28 vs. 0.32 Å for Mn) to form a dome and out-of-plane tilting of the attached tetrahedral sheets, with the Mn structure having greater curvature. In order to achieve interlayer connectivity, three island boundaries must meet at a six-membered silicate ring.

The tetrahedral rotation angle, α , involves an in-plane rotation of adjacent tetrahedra in opposite directions around the silicate ring. For ideal phyllosilicates, tetrahedral rotation is usually considered a measure of misfit between the octahedral sheet and the attached tetrahedral sheet, with a larger α value indicating greater misfit. For these phyllosilicates, the tetrahedral sheet is laterally larger than the octahedral sheet, and thus inplane rotation reduces a tetrahedral sheet that is too large. In the case of stilpnomelane, however, the tetrahedral sheet is laterally smaller than the octahedral sheet. Thus, the rotation angle is not a useful parameter for describing the silicate rings within the islands, since they are fully extended, but α can be used to describe the silicate rings that serve as interisland connectors.

The α values for the interisland connectors are 11° for the Mn end-member and 13.5° for Fe, which represent approximately a 1% change in lateral length for an idealized single tetrahedral ring. This result suggests that island boundary positions as they relate to island neighbors, in plan view, are only slightly affected by differences in the Mn and Fe²⁺ sizes. Thus, because the interisland connectors in stilpnomelane do not link directly to the octahedral sheets, α is determined for the most part by the remaining space available between island boundaries.

Interisland connectors are tilted out of plane, however, with greater tilt for the Fe end-member than for the Mn end-member (Mn: ~7°, Fe: ~13°). This result may indicate that the c cell edge is incorrect for the following reasons: (1) the tilt involves primarily the z coordinate of the [4]Si and O atoms, (2) atomic coordinates were constrained to fit within a fixed cell, and (3) the c edge length was extrapolated from samples that were compositionally quite Fe rich. In order to test the validity of the c edge length, the Mn end-member c edge length was arbitrarily increased in size by 1 and by 4% to determine if the interisland tetrahedral rings would be affected. Interestingly, unreasonable distortions in the interisland tetrahedral sites occur, with bond distances varying from 1.615 to 1.641 Å for the 1% increase in c and 1.633–1.652 Å for the 4% increase. In both cases, however, the tetrahedra within the connector rings did not increase their tilt. This result indicates that the derived c edge length for Mn end-member stilpnomelane is reasonable, that the length is geometrically controlled, and that the observed tetrahedral tilts from the analysis are a requirement for the geometric connectivity of the islands. Clearly, however, there is a geometric limit to the amount of tetrahedral tilting within the connector rings, which cannot be compensated by a change in cell dimensions. In addition, the result argues against a similar DLS treatment for a hypothetical Fe end-member analysis for parsettensite, unless cell-parameter data for more Fe-rich samples become available.

Application of DLS analysis of stilpnomelane to parsettensite

A fundamental difference between the stilpnomelane and parsettensite structures is that six-membered ring connectors serve to join three adjacent island boundaries in stilpnomelane, but four-membered ring connectors link only two adjacent islands in parsettensite. Because the results from the DLS analysis of stilpnomelane solid solutions suggest that misfit is relieved by adjustments to the islands and (to a lesser degree) the island connectors, and because the geometry of the connectors in parsettensite differs from that in stilpnomelane, it is difficult to assess in detail how the two geometries may relieve misfit between the tetrahedral and octahedral sheets. For example, in parsettensite, warping of the octahedral sheet $(\Delta z = 0.24 \text{ Å})$ is less than in stilpnomelane (Fe: 0.28 Å, Mn: 0.32 Å), but the significance of these differences cannot be easily evaluated.

Although the stilpnomelane d_{001} value is about 12.13 Å at Mn end-member compositions, this spacing is considerably less than that of parsettensite ($d_{001} = 12.6$ Å). The parsettensite model, as indicated by Fourier analysis (Eggleton and Guggenheim, 1994) and the DLS analysis, has considerable tetrahedral tilting associated with the four-membered ring interisland connector, which is clearly not a requirement in the six-membered ring tetrahedral connectors in stilpnomelane. The higher tetrahedral tilt in parsettensite may reduce Si-Si repulsion by placing the shared O atom of the four-membered ring more directly between the Si atoms than they would be if the bases of the tetrahedra were, as in the six-membered rings in stilpnomelane, parallel to (001). Thus, the difference in the d_{001} values between a Mn-rich stilpnomelane and parsettensite is the ability of the four-membered ring connectors in parsettensite to tilt so that a tetrahedral edge can be vertical; island curvature is not the major factor.

In stilpnomelane, the interisland connectors have the ability to reduce their lateral dimensions by tetrahedral rotation. In contrast, parsettensite connectors, which are four-membered rings, cannot accomplish such reductions. Thus, parsettensite requires the nearly perfect alignment of islands, since connections are made by rigid four-membered rings. For islands that are too small, neighboring islands are imperfectly aligned, and parsettensite cannot exist.

In Mg- or Fe³⁺-rich stilpnomelane with relatively small lateral dimensions of the islands, the six-membered ring connectors can pull the tetrahedra of neighboring islands closer to maintain registry. However, the interisland connectors approach a ditrigonal configuration with the reduction in size of the lateral axes. As tetrahedral rotation increases within the interisland connectors, Si to Si distances are reduced and Si-Si repulsions would increase, thereby causing tilting of tetrahedra and an increase in the d_{001} value.

The question of the possible coexistence of Mn-rich stilpnomelane and parsettensite remains. Perhaps, because the Mn-Si ratios differ for parsettensite and stilpnomelane, the apparent lack of parsettensite and Mn-rich stilpnomelane intergrowths, which are not yet known to exist, may simply be a result of bulk chemistry. Nothing is known about the stability relations of either Mn-rich stilpnomelane or parsettensite, and experimental studies are needed for a better understanding of their phase relations.

ACKNOWLEDGMENTS

We appreciate the efforts of the reviewers of this paper, H.R. Wenk, P. Heaney, G. Guthrie, and an anonymous reviewer. We gratefully acknowledge the Geochemistry Program and the U.S.-Australia Cooperative Science Program of the National Science Foundation for providing support under grant EAR-9003688, the Australian Research Council for support, and the University of Illinois at Chicago for providing a sabbatical leave for S.G.

References cited

- Baerlocher, C., Hepp, A., and Meier, W.M. (1978) DLS-76: A program for the simulation of crystal structures by geometric refinement. Institute of Crystallography and Petrography, ETH Zurich, Switzerland.
- Baur, W.H. (1977) Computer simulation of crystal structures. Physics and Chemistry of Minerals, 2, 3–20.
- Dunn, P.J., Peacor, D.R., and Simmons, W.B. (1984) Lennilenapeite, the Mg-analogue of stilpnomelane, and chemical data on other stilpnomelane species from Franklin, New Jersey. Canadian Mineralogist, 22, 259-263.
- Dunn, P.J., Peacor, D.R., and Su, S.-C. (1992) Franklinphilite, the manganese analog of stilpnomelane, from Franklin, New Jersey. Mineralogical Record, 23, 465–468.

Eggleton, R.A. (1972) The crystal structure of stilpnomelane. II. The full cell. Mineralogical Magazine, 38, 693-711.

- Eggleton, R.A., and Chappell, B.W. (1978) The crystal structure of stilpnomelane. III. Chemistry and physical properties. Mineralogical Magazine, 42, 361–368.
- Eggleton, R.A., and Guggenheim, S. (1994) The use of electron optical methods to determine the crystal structure of a modulated phyllosilicate: Parsettensite. American Mineralogist, 79, 426-437.
- Guggenheim, S., and Eggleton, R.A. (1987) Modulated 2:1 layer silicates: Review, systematics, and predictions. American Mineralogist, 72, 724– 738.

(1988) Crystal chemistry, classification, and identification of mod-

ulated layer silicates. In Mineralogical Society of America Reviews in Mineralogy, 19, 675-725.

- Meier, W.M., and Villiger, H. (1969) Die Methode der Abstandsverfeinerung zur Bestimmung der Atomkoordinaten idealisierter Gerüststrukturen. Zeitschrift für Kristallographie, 129, 411–423.
- Shannon, R.D. (1976) Revised effective ionic radii and systematic studies of interatomic distances in halides and chalcogenides. Acta Crystallographica, A32, 751–767.

Manuscript received August 14, 1992 Manuscript accepted January 7, 1994