

## Estimating the thermodynamic properties ( $\Delta G_f^0$ and $\Delta H_f^0$ ) of silicate minerals at 298 K from the sum of polyhedral contributions

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### ABSTRACT

Many physical properties of silicate minerals can be modeled as a combination of basic polyhedral units (Hazen, 1985, 1988). It follows that their thermodynamic properties could be modeled as the sum of polyhedral contributions. We have determined, by multiple regression, the contribution of the  $^{[4]}\text{Al}_2\text{O}_3$ ,  $^{[6]}\text{Al}_2\text{O}_3$ ,  $^{[6]}\text{Al}(\text{OH})_3$ ,  $^{[4]}\text{SiO}_2$ ,  $^{[6]}\text{MgO}$ ,  $^{[6]}\text{Mg}(\text{OH})_2$ ,  $^{[6]}\text{CaO}$ ,  $^{[8-2]}\text{CaO}$ ,  $^{[6-8]}\text{Na}_2\text{O}$ ,  $^{[8-12]}\text{K}_2\text{O}$ ,  $\text{H}_2\text{O}$ ,  $^{[6]}\text{FeO}$ ,  $^{[6]}\text{Fe}(\text{OH})_2$ , and  $^{[6]}\text{Fe}_2\text{O}_3$  components to the total  $\Delta G_f^0$  and  $\Delta H_f^0$  of a selected group of silicate minerals. Using these data we can estimate the  $\Delta G_f^0$  and  $\Delta H_f^0$  of other silicate minerals from a weighted sum of the contribution of each oxide and hydroxide component:  $\Delta G_f^0 = \sum n_i g_i$ , and  $\Delta H_f^0 = \sum n_i h_i$ , where  $n_i$  is the number of moles of the oxide or hydroxide per formula unit and  $g_i$  and  $h_i$  are the respective molar free energy and enthalpy contribution of 1 mol of each oxide or hydroxide component. The technique outlined here can be used to estimate the thermodynamic properties of many silicate phases that are too complex or too impure to give reliable calorimetric measurements.

Experimentally measured  $\Delta G_f^0$  and  $\Delta H_f^0$  vs. predicted  $\Delta G_f^0$  and  $\Delta H_f^0$  for the minerals used in the model have associated average residuals of 0.26% and 0.24%, respectively. Thermodynamic properties of minerals not used in the model but for which there are experimentally determined calorimetric data have average differences between measured and predicted values of 0.25% for  $\Delta G_f^0$  for 18 minerals and 0.22% for  $\Delta H_f^0$  for 20 minerals.

### INTRODUCTION

Clay and zeolite minerals are very important phases in the near-surface environment, and the understanding of their thermodynamic properties is essential to modeling many geochemical processes. But, experimental measurements of the free energy of formation and enthalpy of formation ( $\Delta G_f^0$  and  $\Delta H_f^0$ , respectively) are few because they are difficult to perform. Problems associated with determining thermodynamic properties of clay and zeolite minerals include their chemical complexity and highly variable composition. The estimation technique for  $\Delta G_f^0$  and  $\Delta H_f^0$  developed here offers a reasonable way to approximate thermodynamic properties of clays and zeolites.

For silicate minerals, many other techniques exist for estimating  $\Delta G_f^0$  (Nriagu, 1975; Chen, 1975; Tardy and Garrels, 1974, 1976, 1977; Karpov and Kashik, 1968; Mattigod and Sposito, 1978; La Iglesia and Aznar, 1986; Sposito, 1986) and  $\Delta H_f^0$  (Kubaschewski and Alcock, 1979; Hemingway, 1982; Vieillard and Tardy, 1988). A complete discussion here of each technique and associated errors would be quite lengthy; therefore, only a short summary will be presented. The data base used for most of the  $\Delta G_f^0$  estimation techniques is based on solubility measurements of clay minerals. In these techniques, the estimation is based on the combined contributions of hydroxide components [i.e.,  $\text{Si}(\text{OH})_4$ ,  $\text{Al}(\text{OH})_3$ , etc.] rather

than both hydroxide and oxide polyhedra. Karpov and Kashik used a multiple linear-regression technique to estimate the  $\Delta G_f^0$  contribution of 36 different oxides to the overall  $\Delta G_f^0$  of silicate minerals; however they ignored the hydroxide contributions. Tardy and Garrels (1976) developed an expression that describes the difference between  $\Delta G_f^0$  of the simple oxide or hydroxide vs.  $\Delta G_f^0$  of that same oxide or hydroxide within the silicate structure. This technique was extended further to include  $\Delta H_f^0$  (Vieillard and Tardy, 1988). This basic technique of breaking down minerals into their "building block" components is also used in  $S^0$  estimation (Robinson and Haas, 1983; Holland, 1989). Robinson and Haas's  $S^0$  estimates have small errors within the original data set but when applied outside the model data base, the estimates have much larger associated errors. The Robinson and Haas method of estimating entropy could be refined further if hydroxyls were viewed as parts of polyhedral units, and the simple oxide and hydroxide phases were removed from the model, as will be demonstrated later. Holland's estimation technique gives further refinement to the estimation of  $S^0$  by including a volume correction and considering magnetic contributions when estimating entropy.

This paper describes a multiple linear-regression technique to determine the contribution of oxide and hydroxide components to the  $\Delta G_f^0$  and  $\Delta H_f^0$  of silicate minerals. The technique is based on the observation that silicate minerals have been shown to act as a combination

**TABLE 1.** Minerals selected for the thermodynamic regression models and the relative contribution of their polyhedral components

Component: Coordination no.:	Al <sub>2</sub> O <sub>3</sub> 4	Al <sub>2</sub> O <sub>3</sub> 6	Al(OH) <sub>3</sub> 6	SiO <sub>2</sub> 4	K <sub>2</sub> O 8-12	MgO 6	Mg(OH) <sub>2</sub> 6	H <sub>2</sub> O	CaO 6	CaO 8-z	Na <sub>2</sub> O 6-8	FeO 6	Fe(OH) <sub>2</sub> 6	Fe <sub>2</sub> O <sub>3</sub> 6
1. Kaolinite	0.0	0.33	1.33	2.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2. Muscovite	0.5	0.67	0.67	3.0	0.5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
3. Margarite	1.0	0.67	0.67	2.0	0.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0
4. Talc	0.0	0.0	0.0	4.0	0.0	2.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5. Pyrophyllite	0.0	0.67	0.67	4.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
6. Microcline	0.5	0.0	0.0	3.0	0.5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
7. Low albite	0.5	0.0	0.0	3.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5	0.0	0.0	0.0
8. Anorthite	1.0	0.0	0.0	2.0	0.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0
9. Analcime	0.5	0.0	0.0	2.0	0.0	0.0	0.0	1.0	0.0	0.0	0.5	0.0	0.0	0.0
10. Lawsonite	0.67	0.0	0.67	2.0	0.0	0.0	0.0	1.0	1.0	0.0	0.0	0.0	0.0	0.0
11. Ferrosiilite	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1.0	0.0	0.0
12. Fayalite	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	2.0	0.0	0.0
13. Leucite	0.5	0.0	0.0	2.0	0.5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
14. Leonardite	1.0	0.0	0.0	4.0	0.0	0.0	0.0	3.5	0.0	1.0	0.0	0.0	0.0	0.0
15. Tremolite	0.0	0.0	0.0	4.0	0.0	2.0	0.5	0.0	0.0	1.0	0.0	0.0	0.0	0.0
16. Jadeite	0.0	0.5	0.0	2.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5	0.0	0.0	0.0
17. Diopside	0.0	0.0	0.0	2.0	0.0	1.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0
18. Merwinite	0.0	0.0	0.0	2.0	0.0	1.0	0.0	0.0	3.0	0.0	0.0	0.0	0.0	0.0
19. Monticellite	0.0	0.0	0.0	1.0	0.0	1.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0
20. Grossular	0.0	1.0	0.0	3.0	0.0	0.0	0.0	0.0	0.0	3.0	0.0	0.0	0.0	0.0
21. Zoisite	0.0	1.33	0.33	3.0	0.0	0.0	0.0	0.0	0.0	2.0	0.0	0.0	0.0	0.0
22. Mordenite	0.47	0.0	0.0	5.06	0.0	0.0	0.0	3.47	0.0	0.29	0.18	0.0	0.0	0.0
23. Yugawaralite	0.5	0.0	0.0	3.0	0.0	0.0	0.0	2.0	0.0	0.5	0.0	0.0	0.0	0.0
24. Grunerite	0.0	0.0	0.0	4.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	3.0	0.5	0.0
25. Minnesotaitite	0.0	0.0	0.0	4.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	2.0	1.0	0.0
26. Riebeckite	0.0	0.0	0.0	4.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5	1.0	0.5	0.5
27. Chrysotile	0.0	0.0	0.0	2.0	0.0	1.0	2.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
28. Paragonite	0.5	0.67	0.67	3.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5	0.0	0.0	0.0
29. Phlogopite	0.5	0.0	0.0	3.0	0.5	2.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
30. Laumontite	1.0	0.0	0.0	4.0	0.0	0.0	0.0	4.0	0.0	1.0	0.0	0.0	0.0	0.0
31. Nepheline	0.5	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5	0.0	0.0	0.0
32. Greenalite	0.0	0.0	0.0	2.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1.0	2.0	0.0
33. Prehnite	0.67	0.0	0.67	3.0	0.0	0.0	0.0	0.0	1.0	1.0	0.0	0.0	0.0	0.0
34. Acmite	0.0	0.0	0.0	2.0	0.0	0.0	0.0	0.0	0.0	0.0	0.5	0.0	0.0	0.5

Note: Minerals used in  $\Delta G_f^\circ$  model: 1-27, 33, 34. Minerals used in  $\Delta H_f^\circ$  model: 1-32.

of basic polyhedral units (Hazen, 1985). Using this polyhedral approach, volume, bulk modulus (Hazen, 1985), stable-isotope fractionation (Savin and Lee, 1988), and refractive index (Bloss et al., 1983) can be modeled accurately. In turn, it seems reasonable that the thermodynamic properties of minerals could be estimated by summing the contributions of the individual polyhedra. We have determined, by multiple linear regression, the contribution of  $^{[4]}Al_2O_3$ ,  $^{[6]}Al_2O_3$ ,  $^{[6]}Al(OH)_3$ ,  $^{[4]}SiO_2$ ,  $^{[6]}MgO$ ,  $^{[6]}Mg(OH)_2$ ,  $^{[6]}CaO$ ,  $^{[8-z]}CaO$ ,  $^{[6-8]}Na_2O$ ,  $^{[8-12]}K_2O$ ,  $H_2O$ ,  $^{[6]}FeO$ ,  $^{[6]}Fe(OH)_2$ , and  $^{[6]}Fe_2O_3$  components to the total  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  of a selected group of silicate minerals, where the  $z$  in  $^{[8-z]}CaO$  represents coordination of these CaO polyhedra in zeolite structures. We propose that the thermodynamic properties of many silicate phases that are too complex and too impure to give reliable calorimetric measurements can be estimated by summing the contributions of these components for the mineral of interest.

This approach has many advantages over other estimation techniques. First, thermodynamic properties of the minerals used to calibrate the model are based on calorimetric and high-temperature phase-equilibrium measurements rather than on harder-to-determine solubility measurements. Second, it is conceptually simple and compelling to analyze a silicate mineral's properties in terms of the contributions of its "building block" oxide

and/or hydroxide. Third, this technique is simple to implement because only the chemical formula and the coordination number of the polyhedra composing the mineral are needed. Finally, because of the large body of data available for use in the regression model, small errors in individual measurements have little effect on the estimated coefficients.

## METHODS

A critically selected thermodynamic data base for 34 minerals was used (Table 1). The "building block" components for each mineral and the associated coordination numbers in the  $^{[4]}Al_2O_3$ - $^{[6]}Al_2O_3$ - $^{[6]}Al(OH)_3$ - $^{[4]}SiO_2$ - $^{[6]}MgO$ - $^{[6]}Mg(OH)_2$ - $^{[6]}CaO$ - $^{[8-z]}CaO$ - $^{[6-8]}Na_2O$ - $^{[8-12]}K_2O$ - $H_2O$ - $^{[6]}FeO$ - $^{[6]}Fe(OH)_2$ - $^{[6]}Fe_2O_3$  system were determined (Table 1). For example, the mineral kaolinite [ $Al_2Si_2O_5(OH)_4$ ] is composed of 2  $^{[4]}SiO_2$ , 0.667  $^{[6]}Al_2O_3$ , and 0.667  $^{[6]}Al(OH)_3$  polyhedra. When  $Al^{3+}$ ,  $Fe^{3+}$ ,  $Mg^{2+}$ , and  $Fe^{2+}$  are in six-fold coordination in the octahedral sheet of 1:1 and 2:1 phyllosilicate minerals, they were distributed as 0.6666 hydroxide and 0.3333 oxide, and 0.3333 hydroxide and 0.6666 oxide, respectively. This distribution is consistent with structural constraints on the distribution of oxide and hydroxide polyhedra (Weaver and Pollard, 1973). The number of  $^{[4]}SiO_2$  polyhedra for an individual mineral in the regression model was not allowed to exceed

**TABLE 2.** The  $g_i$  and  $h_i$  of each polyhedral type

Polyhedral unit	$g_i$ (kJ·mol <sup>-1</sup> )	Error (kJ·mol <sup>-1</sup> )	$h_i$ (kJ·mol <sup>-1</sup> )	Error* (kJ·mol <sup>-1</sup> )
<sup>14</sup> Al <sub>2</sub> O <sub>3</sub>	-1631.32	13.3	-1716.24	11.0
<sup>6</sup> Al <sub>2</sub> O <sub>3</sub>	-1594.52	15.3	-1690.18	15.9
<sup>6</sup> Al(OH) <sub>3</sub>	-1181.62	13.2	-1319.55	12.2
<sup>4</sup> SiO <sub>2</sub>	-853.95	4.6	-910.97	3.2
<sup>6</sup> MgO	-628.86	10.6	-660.06	7.9
<sup>6</sup> Mg(OH) <sub>2</sub>	-851.86	10.2	-941.62	9.1
<sup>6</sup> CaO	-669.13	5.9	-696.65	5.2
<sup>18-2</sup> CaO	-710.08	7.2	-736.04	7.1
<sup>6-8</sup> Na <sub>2</sub> O	-672.50	26.0	-683.00	18.4
<sup>18-12</sup> K <sub>2</sub> O	-722.94	27.4	-735.24	21.1
H <sub>2</sub> O	-239.91	5.7	-292.37	4.6
<sup>6</sup> FeO	-266.29	6.8	-290.55	5.4
<sup>6</sup> Fe(OH) <sub>2</sub>	-542.04	24.6	-596.07	8.2
<sup>6</sup> Fe <sub>2</sub> O <sub>3</sub>	-776.07	33.0	-939.18	35.6

\* Standard error of the estimate.

5.0 to avoid over-weighting the contribution of a particular mineral. If the sum of the associated <sup>14</sup>SiO<sub>2</sub> polyhedra totaled more than five, one-half of the chemical formula was used. The rationale of this breakdown process was aided by a discussion of coordination numbers in silicates presented in Robinson and Haas (1983). A tabulation of the polyhedral coordination of oxide components of many silicate minerals is given by Smyth and Bish (1988).

The data were regressed to determine  $g_i$  and  $h_i$  (the contribution of 1 mol of component to the free energy and enthalpy of the mineral, respectively) for the following models:  $\Delta G_f^0 = \sum n_i g_i$  (29 minerals) and  $\Delta H_f^0 = \sum n_i h_i$  (32 minerals), where  $n_i$  is the number of moles of component  $i$ . Entropy values ( $S^0$ ) can be determined using the equation  $\Delta G_f^0 = \Delta H_f^0 - T\Delta S_f^0$ , where  $\Delta S_f^0 = S_{\text{elements}}^0 - S^0$ .  $S^0$  estimations from both a regression model  $S^0 = \sum n_i s_i$  (25 minerals) and from the above equation were found to have much larger associated errors and to be more sensitive to the coordination than enthalpy and free-energy values. We suggest using these techniques only for rough estimates of  $S^0$ . The technique of Holland (1989) gives more accurate estimates of  $S^0$  and can be used in conjunction with our  $\Delta H_f^0$  model to produce an internally consistent set of  $\Delta G_f^0$ ,  $\Delta H_f^0$ , and  $S^0$  values.

A few minerals showed poor agreement between measured and predicted values. Beware of minerals such as pyrope, akermanite, and wollastonite that have oxides with unusual coordination numbers because data for polyhedra with these coordination numbers are not specified by the model. Other minerals that resulted in poor fits to the model include Ca-Al pyroxene, forsterite, cordierite, andradite, and gehlenite. We have no explanation for their inconsistency.

## RESULTS

Table 2 lists  $g_i$  and  $h_i$  and their errors derived from the model. Tables 3 and 4 show measured  $\Delta G_f^0$  and  $\Delta H_f^0$  versus those predicted using  $g_i$  and  $h_i$  from Table 2. The average difference between the predicted and the mea-

**TABLE 3.** Comparison of  $\Delta G_f^0$  (measured) versus  $\Delta G_f^0$  (predicted) for the 29 minerals used in the model and the associated errors

Mineral	$\Delta G_f^0$ (measured) (kJ·mol <sup>-1</sup> )	$\Delta G_f^0$ (predicted) (kJ·mol <sup>-1</sup> )	Residuals (kJ·mol <sup>-1</sup> )	% Residual
1. Kaolinite	-3799.4	-3814.9	15.5	0.41
2. Muscovite	-5595.5	-5589.7	-5.8	0.10
3. Margarite	-5854.8	-5859.1	4.3	0.07
4. Talc	-5536.1	-5525.4	-10.7	0.19
5. Pyrophyllite	-5265.9	-5266.6	0.6	0.01
6. Microcline	-3742.3	-3739.0	-3.4	0.09
7. Low albite	-3711.7	-3713.8	2.0	0.05
8. Anorthite	-4002.1	-4008.3	6.3	0.16
9. Analcime	-3091.7	-3099.7	8.0	0.26
10. Lawsonite	-4525.6	-4492.2	-33.4	0.74
11. Ferrosilite	-1117.1	-1120.2	-3.1	0.28
12. Fayalite	-1379.4	-1386.5	-7.2	0.52
13. Leucite	-2875.9	-2885.0	9.1	0.32
14. Leonardite	-6598.6	-6596.9	-1.7	0.03
15. Tremolite	-5814.0	-5809.5	-4.4	0.08
16. Jadeite	-2850.8	-2841.4	-9.4	0.33
17. Diopside	-3036.6	-3046.8	10.3	0.34
18. Merwinite	-4339.4	-4344.1	4.7	0.11
19. Monticellite	-2143.2	-2151.9	8.8	0.41
20. Grossular	-6295.3	-6286.6	-8.7	0.14
21. Zoisite	-6495.3	-6501.9	6.6	0.10
22. Mordenite	-6247.6	-6246.0	-1.6	0.03
23. Yugawaralite	-4193.9	-4212.4	18.5	0.44
24. Grunerite	-4494.4	-4485.7	-8.7	0.19
25. Minnesotait	-4474.8	-4490.4	15.6	0.35
26. Chrysotile	-4034.0	-4040.5	6.5	0.16
27. Prehnite	-5816.4	-5816.3	-0.1	0.00
28. Riebeckite	-4699.9	-4677.4	-22.5	0.48
29. Acmite	-2409.7	-2432.2	22.5	0.93
Average				0.26

Note: 1, 4, 6, 7, 8, 9, 10, 12, 13, 14, 15, 16, 17, 18, 19, and 26—Robie et al. (1978). 2, 5, and 20—Krupka et al. (1979). 3, 21, and 27—Hemingway et al. (1982). 22—Johnson et al. (1986). These data were determined by calorimetry.

23—Zeng and Liou (1982). 11, 24, and 25—Miyano and Klein (1983). 28 and 29—Makarov et al. (1984). These data were determined from phase-equilibrium reversals.

asured values is 0.26% for  $\Delta G_f^0$  and 0.24% for  $\Delta H_f^0$ , and these differences are normally distributed. The average reported associated errors ( $2\sigma$ ) for the experimentally determined thermodynamic values are 0.16% for  $\Delta G_f^0$  and 0.13% for  $\Delta H_f^0$ . Approximately 50% of the estimated values fall within the range of the error ( $2\sigma$ ) reported for the experimentally determined data.

The accuracy of the models was tested by predicting the thermodynamic properties of minerals not used to develop the model. Table 5a compares the results of the model with calorimetrically determined thermodynamic data for 20 different minerals and gives associated differences. Average residuals for these minerals are 0.25% for  $\Delta G_f^0$  for 18 minerals and 0.22% for  $\Delta H_f^0$  for 20 minerals. Table 5b shows that  $\Delta G_f^0$  values derived from solubility measurements of clays agree with those predicted by this model with an average difference of 0.54% between the predicted and measured  $\Delta G_f^0$  for 18 minerals.

## DISCUSSION

A comparison of the  $g_i$  and  $h_i$  from these models to the  $\Delta G_f^0$  and  $\Delta H_f^0$  for the simple oxide or hydroxide compo-

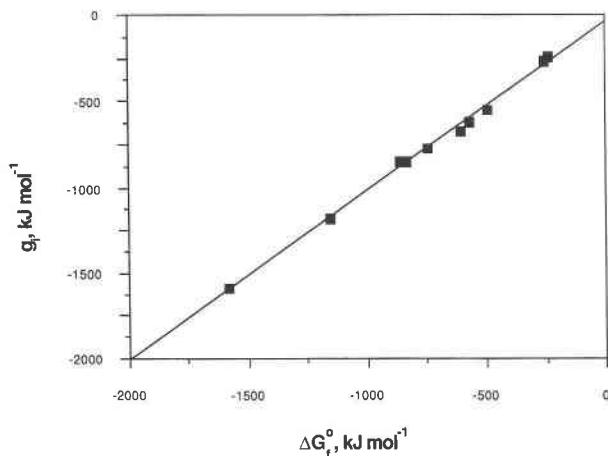


Fig. 1. Graph of the  $g_i$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) versus  $\Delta G_{f,\text{ox-hyd}}^0$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) data from Table 6. The associated regression equation is  $g_i = -35.55 + 0.990\Delta G_{f,\text{ox-hyd}}^0$  with an  $R$  value equal to 1.00.

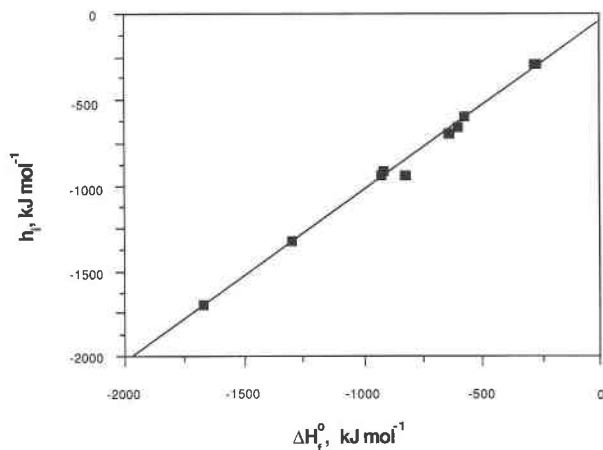


Fig. 2. Graph of the  $h_i$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) versus  $\Delta H_{f,\text{ox-hyd}}^0$  ( $\text{kJ}\cdot\text{mol}^{-1}$ ) data from Table 6. The associated regression equation is  $h_i = -38.29 + 0.995\Delta H_{f,\text{ox-hyd}}^0$  with an  $R$  value equal to 1.00.

TABLE 4. Comparison of  $\Delta H_f^0$  (measured) versus  $\Delta H_f^0$  (predicted) for the 32 minerals used in the model and the associated errors

Mineral	$\Delta H_f^0$ (measured) ( $\text{kJ}\cdot\text{mol}^{-1}$ )	$\Delta H_f^0$ (predicted) ( $\text{kJ}\cdot\text{mol}^{-1}$ )	Residual ( $\text{kJ}\cdot\text{mol}^{-1}$ )	% Residual
1. Kaolinite	-4133.6	-4144.7	11.1	0.27
2. Muscovite	-5971.6	-5965.1	-6.5	0.11
3. Paragonite	-5941.5	-5939.0	-2.5	0.04
4. Margarite	-6239.6	-6241.3	1.7	0.03
5. Phlogopite	-6213.9	-6220.4	6.5	0.10
6. Talc	-5915.9	-5905.6	-10.3	0.17
7. Pyrophyllite	-5639.8	-5650.4	10.6	0.18
8. Microcline	-3967.7	-3958.7	-9.0	0.22
9. Low albite	-3935.1	-3932.5	-2.6	0.07
10. Anorthite	-4227.8	-4234.8	7.0	0.16
11. Analcime	-3309.8	-3313.9	4.1	0.12
12. Laumontite	-7277.2	-7265.6	-11.5	0.16
13. Lawsonite	-4863.9	-4834.8	-29.1	0.60
14. Ferrosillite	-1194.9	-1201.5	6.7	0.56
15. Fayalite	-1479.4	-1492.1	12.7	0.86
16. Leucite	-3038.7	-3047.7	9.0	0.30
17. Nepheline	-2092.1	-2110.6	18.5	0.88
18. Leonardite	-7123.2	-7119.4	-3.8	0.05
19. Tremolite	-6177.5	-6170.9	-6.7	0.11
20. Jadeite	-3029.4	-3008.5	-20.9	0.69
21. Diopside	-3210.8	-3218.0	7.3	0.23
22. Merwinite	-4566.8	-4571.9	5.2	0.11
23. Monticellite	-2262.7	-2267.7	5.0	0.22
24. Grossular	-6636.3	-6631.2	-5.1	0.08
25. Zoisite	-6891.1	-6898.4	7.3	0.10
26. Mordenite	-6756.2	-6765.7	9.5	0.14
27. Yugawaralite	-4518.1	-4543.8	25.7	0.57
28. Grunerite	-4824.2	-4813.6	-10.6	0.22
29. Minnesotait	-4823.0	-4821.0	-2.0	0.04
30. Chrysotile	-4361.7	-4365.2	3.6	0.08
31. Greenalite	-3301.0	-3304.6	3.6	0.10
32. Riebeckite	-5043.6	-5043.6	0.0	0.00
Average				0.24

Note: 2, 7, 13, and 24—Krupka et al. (1979). 4 and 25—Hemingway et al. (1982). 5—Clemens et al. (1987). 6, 8, 9, 10, 11, 15, 16, 17, 18, 19, 20, 21, 22, 23, and 30—Robie et al. (1978). 26—Johnson et al. (1986). These data were determined by calorimetry.

1—Hemley et al. (1980). 3 and 12—Berman et al. (1985). 27—Zeng and Liou (1982). 14, 28, 29, and 31—Miyano and Klein (1983). 32—Makarov et al. (1984). These data were determined from phase-equilibrium reversals.

ments (Table 6) shows that there is a good correlation between  $g_i$  and  $\Delta G_f^0$  (Fig. 1) and between  $h_i$  and  $\Delta H_f^0$  (Fig. 2). These graphs show that free energy and enthalpy of formation of an oxide or hydroxide component in a silicate mineral generally is more negative than those of the simple oxide or hydroxide mineral by  $\sim 36 \text{ kJ}\cdot\text{mol}^{-1}$  and  $\sim 38 \text{ kJ}\cdot\text{mol}^{-1}$ , respectively. The abundance of silicate minerals relative to free oxides and hydroxides in nature is consistent with this relationship.

The correlation lines in Figures 1 and 2 can be used to approximate a  $g_i$  or  $h_i$  for polyhedra not determined by this model. For example, experimental data for a mineral containing a  $\text{Fe}(\text{OH})_3$  polyhedron was not available to incorporate into these models, but  $g_i$  and  $h_i$  can be approximated by using the experimentally determined  $\Delta G_f^0[\text{Fe}(\text{OH})_3]$  and  $\Delta H_f^0[\text{Fe}(\text{OH})_3]$ . The values of  $\Delta G_f^0 = -696.50 \text{ kJ}\cdot\text{mol}^{-1}$  and  $\Delta H_f^0 = -823.0 \text{ kJ}\cdot\text{mol}^{-1}$  (Wagman et al., 1982) can be used along with  $g_i = -35.6 + 0.990\Delta G_f^0$  and  $h_i = -38.3 + 0.995\Delta H_f^0$  to estimate  $g_i = -725.0 \text{ kJ}\cdot\text{mol}^{-1}$ , and  $h_i = -856.8 \text{ kJ}\cdot\text{mol}^{-1}$ . However, the errors associated with these estimates are unknown and may be large.

Table 7 describes the protocol to follow when estimating the thermodynamic properties of a silicate mineral using the model described above. It shows, as an example, the estimation of  $\Delta G_f^0$  for an illite [ $\text{K}_{0.75}(\text{Al}_{1.75}\text{Mg}_{0.25})\text{Si}_{3.5}\text{Al}_{0.5}\text{O}_{10}(\text{OH})_2$ ]. The estimated  $\Delta G_f^0$  of this illite is  $-5463.0 \text{ kJ}\cdot\text{mol}^{-1}$ . Using an analogous procedure, it was found that  $\Delta H_f^0 = -5837.3 \text{ kJ}\cdot\text{mol}^{-1}$ . Note that the procedure for distributing the octahedral cations in step 2b is based on crystallographic constraints (Weaver and Pollard, 1973). On the other hand, the distribution of cations into the interlayer of chlorites (step 2c) is based on a thermodynamic argument, which results in the most negative (stable)  $\Delta G_f^0$  for a given composition. Also, using  $\Delta G_{f,\text{ox-hyd}}^0$  and  $\Delta H_{f,\text{ox-hyd}}^0$  for cations in the chlorite interlayer is justified by the fact that chlorite interlayers act as

**TABLE 5A.** Measured  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  determined by calorimetry compared to their predicted values for 20 minerals

Mineral (Ref.)*	Chemical formula	$\Delta G_f^\circ$ (pred.) (kJ·mol <sup>-1</sup> )	$\Delta G_f^\circ$ (meas.) (kJ·mol <sup>-1</sup> )	% Difference	$\Delta H_f^\circ$ (pred.) (kJ·mol <sup>-1</sup> )	$\Delta H_f^\circ$ (meas.) (kJ·mol <sup>-1</sup> )	% Difference
Nepheline (1)	Na <sub>0.78</sub> K <sub>0.22</sub> AlSiO <sub>4</sub>	-2011.4	—	—	-2116.3	-2110.3	0.28
Mesolite (2)	Na <sub>0.676</sub> Ca <sub>0.657</sub> Al <sub>1.990</sub> Si <sub>3.01</sub> O <sub>10</sub> ·2.647H <sub>2</sub> O	-5530.6	-5513.2	0.32	-5946.6	-5947.1	0.01
Natrolite (2)	Na <sub>2</sub> Al <sub>2</sub> Si <sub>3</sub> O <sub>10</sub> ·2.0H <sub>2</sub> O	-5345.5	-5316.6	0.54	-5716.9	-5718.6	0.03
Scolecite (2)	CaAl <sub>2</sub> Si <sub>3</sub> O <sub>10</sub> ·3.0H <sub>2</sub> O	-5623.0	-5597.9	0.45	-6062.3	-6049.0	0.22
Stilbite (3)	Na <sub>0.136</sub> Ca <sub>1.02</sub> K <sub>0.006</sub> Al <sub>2.180</sub> Si <sub>8.820</sub> O <sub>18</sub> ·7.33H <sub>2</sub> O	-10132.1	-10143.0	0.11	-11025.2	-11034.6	0.09
Ca-olivine (4)	Ca <sub>2</sub> SiO <sub>4</sub>	-2192.2	-2199.7	0.34	-2304.3	-2316.5	0.53
Kyanite (4)	Al <sub>2</sub> SiO <sub>5</sub>	-2448.5	-2444.0	0.18	-2601.2	-2594.3	0.26
Prehnite (4)	Ca <sub>2</sub> Al <sub>2</sub> Si <sub>3</sub> O <sub>10</sub> (OH) <sub>2</sub>	***	-5816.4	***	-6189.5	-6193.6	0.07
Hedenbergite (5)	CaFeSi <sub>2</sub> O <sub>6</sub>	-2684.3	-2674.3	0.37	-2848.5	-2837.6	0.38
Almandine (6)	Fe <sub>3</sub> Al <sub>2</sub> Si <sub>3</sub> O <sub>12</sub>	-4955.2	-4951.3	0.08	-5294.7	-5275.5	0.36
Oligoclase (7)	Ca <sub>0.2</sub> Na <sub>0.8</sub> Al <sub>1.2</sub> Si <sub>2.8</sub> O <sub>8</sub>	-3772.7	-3754.3	0.49	-3993.0	-3977.3	0.39
Andesine (7)	Ca <sub>0.4</sub> Na <sub>0.6</sub> Al <sub>1.4</sub> Si <sub>2.6</sub> O <sub>8</sub>	-3831.6	-3818.3	0.35	-4053.5	-4041.7	0.29
Labradorite (7)	Ca <sub>0.5</sub> Na <sub>0.5</sub> Al <sub>1.5</sub> Si <sub>2.5</sub> O <sub>8</sub>	-3861.1	-3848.9	0.32	-4083.7	-4072.3	0.28
Bytownite (7)	Ca <sub>0.8</sub> Na <sub>0.2</sub> Al <sub>1.8</sub> Si <sub>2.2</sub> O <sub>8</sub>	-3949.4	-3959.7	0.26	-4174.4	-4184.0	0.23
Merlionite (8)	KAlSi <sub>1.94</sub> O <sub>5.88</sub> ·1.69H <sub>2</sub> O	-3239.2	-3241.4	0.07	-3487.1	-3481.8	0.15
Merlionite (8)	KAlSi <sub>1.81</sub> O <sub>5.62</sub> ·1.69H <sub>2</sub> O	-3128.2	-3123.3	0.16	-3368.7	-3359.9	0.26
Merlionite (8)	K <sub>0.80</sub> Na <sub>0.20</sub> AlSi <sub>1.94</sub> O <sub>5.88</sub> ·1.81H <sub>2</sub> O	-3263.0	-3272.2	0.28	-3517.0	-3519.0	0.06
Merlionite (8)	K <sub>0.81</sub> Na <sub>0.09</sub> AlSi <sub>1.81</sub> O <sub>5.62</sub> ·1.79H <sub>2</sub> O	-3150.0	-3144.6	0.17	-3395.6	-3387.3	0.25
Merlionite (8)	Na <sub>0.81</sub> K <sub>0.19</sub> AlSi <sub>1.94</sub> O <sub>5.88</sub> ·2.13H <sub>2</sub> O	-3324.4	-3325.8	0.04	-3594.6	-3591.2	0.10
Merlionite (8)	Na <sub>0.81</sub> K <sub>0.19</sub> AlSi <sub>1.81</sub> O <sub>5.62</sub> ·2.18H <sub>2</sub> O	-3225.4	-3225.3	0.00	-3490.8	-3488.3	0.07
Average				0.25			0.22

Note: — = not determined. \*\*\* = value used in the model.

\* References: (1) Robie et al. (1978). (2) Johnson et al. (1983). (3) O'Hare et al. (1986). (4) Hemingway et al. (1982). (5) Robie et al. (1987). (6) Chatterjee (1987). (7) Naumov et al. (1974). (8) Donahoe et al. (1990a, 1990b).

simple oxide-hydroxide phases rather than as part of the silicate lattice. The presence of Fe(OH)<sub>2</sub> and Mg(OH)<sub>2</sub> in chlorite interlayers will be proposed later in this paper as a buffer to control the Fe<sup>2+</sup> and Mg<sup>2+</sup> contents of natural waters.

The difference between the thermodynamic properties

of the oxide or hydroxide components in silicate minerals ( $g_i$  and  $h_i$ ) and those components in simple minerals ( $\Delta G_f^\circ$  and  $\Delta H_f^\circ$ ) is primarily a result of each interaction of the polyhedron with its nearest neighbors. For example, Al(OH)<sub>3</sub> in gibbsite is surrounded by six Al(OH)<sub>3</sub> polyhedra, whereas an Al(OH)<sub>3</sub> polyhedron in the silicate

**TABLE 5B.**  $\Delta G_f^\circ$  determined from solubility measurements compared to predicted  $\Delta G_f^\circ$  for 18 minerals along with the  $\Delta H_f^\circ$  predicted by the model

Mineral (Ref.)*	Chemical formula	$\Delta G_f^\circ$ (pred.) (kJ·mol <sup>-1</sup> )	$\Delta G_f^\circ$ (meas.) (kJ·mol <sup>-1</sup> )	% Difference	$\Delta H_f^\circ$ (pred.) (kJ·mol <sup>-1</sup> )
Kerolite (9)	Mg <sub>3</sub> Si <sub>4</sub> O <sub>10</sub> (OH) <sub>2</sub> ·H <sub>2</sub> O	-5765.3	-5828.03	1.07	-6198.0
Sepiolite (9)	Mg <sub>2</sub> Si <sub>3</sub> O <sub>7.5</sub> (OH)·3H <sub>2</sub> O	-4650.8	-4692.80	0.89	-5070.9
Chlorite 1 (10)	(Al <sub>1.44</sub> Fe <sub>0.07</sub> Fe <sub>0.99</sub> Mg <sub>3.24</sub> )Al <sub>1.03</sub> Si <sub>2.97</sub> O <sub>10</sub> (OH) <sub>8</sub>	-7819.8	-7793.00	0.34	-8477.2
Chlorite 2 (10)	(Al <sub>1.75</sub> Fe <sub>0.12</sub> Fe <sub>2.81</sub> Mg <sub>1.16</sub> )Al <sub>1.16</sub> Si <sub>2.84</sub> O <sub>10</sub> (OH) <sub>8</sub>	-7321.5	-7319.00	0.03	-7952.3
Chlorite 3 (10)	(Al <sub>1.60</sub> Fe <sub>0.23</sub> Mg <sub>1.05</sub> )Al <sub>1.53</sub> Si <sub>2.47</sub> O <sub>10</sub> (OH) <sub>8</sub>	-7282.0	-7290.00	0.11	-7932.6
Chlorite 4 (10)	(Al <sub>1.38</sub> Fe <sub>0.21</sub> Fe <sub>0.57</sub> Mg <sub>3.52</sub> )Al <sub>1.01</sub> Si <sub>2.99</sub> O <sub>10</sub> (OH) <sub>8</sub>	-7888.2	-7869.00	0.24	-8553.5
Fithian illite (11)	K <sub>0.64</sub> (Al <sub>1.54</sub> Fe <sub>0.23</sub> Mg <sub>0.19</sub> )Al <sub>0.49</sub> Si <sub>3.51</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5329.6	-5443.40	2.09	-5715.0
Great Lake illite (11)	K <sub>0.59</sub> (Al <sub>1.58</sub> Fe <sub>0.24</sub> Mg <sub>0.16</sub> )Al <sub>0.35</sub> Si <sub>3.65</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5299.2	-5345.90	0.87	-5683.0
Big Bend illite (11)	K <sub>0.60</sub> Na <sub>0.04</sub> (Al <sub>1.43</sub> Fe <sub>0.42</sub> Mg <sub>0.16</sub> )Al <sub>0.52</sub> Si <sub>3.48</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5268.5	-5333.34	1.21	-5656.5
Clay Spur (12)	K <sub>0.02</sub> Ca <sub>0.1</sub> Na <sub>0.27</sub> (Al <sub>1.52</sub> Fe <sub>0.19</sub> Mg <sub>0.22</sub> )Al <sub>0.06</sub> Si <sub>3.94</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5227.6	-5226.40	0.02	-5612.8
Cheto (12)	K <sub>0.02</sub> Ca <sub>0.185</sub> Na <sub>0.02</sub> (Al <sub>1.52</sub> Fe <sub>0.14</sub> Mg <sub>0.33</sub> )Al <sub>0.07</sub> Si <sub>3.93</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5251.8	-5245.30	0.12	-5639.4
K-Beidellite (13)	K <sub>0.37</sub> Ca <sub>0.01</sub> Na <sub>0.07</sub> (Al <sub>1.41</sub> Fe <sub>0.15</sub> Fe <sub>0.055</sub> Mg <sub>0.205</sub> )Al <sub>0.45</sub> Si <sub>3.55</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5234.5	-5215.40	0.36	-5625.5
Mg-Beidellite (13)	K <sub>0.095</sub> Ca <sub>0.01</sub> Na <sub>0.07</sub> Mg <sub>0.135</sub> (Al <sub>1.41</sub> Fe <sub>0.15</sub> Fe <sub>0.055</sub> Mg <sub>0.205</sub> )Al <sub>0.45</sub> Si <sub>3.55</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5219.3	-5200.10	0.37	-5614.1
Smectite (14)	Mg <sub>0.225</sub> (Al <sub>1.345</sub> Fe <sub>0.405</sub> Mg <sub>0.27</sub> )Al <sub>0.30</sub> Si <sub>3.70</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5174.2	-5214.70	0.78	-5568.5
Al: Belle Fouche (15)	Al <sub>0.0883</sub> (Al <sub>1.515</sub> Fe <sub>0.225</sub> Mg <sub>0.29</sub> )Al <sub>0.065</sub> Si <sub>3.935</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5193.9	-5213.40	0.37	-5587.3
Mg: Belle Fouche (15)	Mg <sub>0.1325</sub> (Al <sub>1.515</sub> Fe <sub>0.225</sub> Mg <sub>0.29</sub> )Al <sub>0.065</sub> Si <sub>3.935</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5207.4	-5222.80	0.29	-5600.1
Al: Aberdeen (15)	Al <sub>0.1983</sub> (Al <sub>1.29</sub> Fe <sub>0.335</sub> Mg <sub>0.445</sub> )Al <sub>0.18</sub> Si <sub>3.82</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5185.8	-5200.00	0.27	-5581.0
Mg: Aberdeen (15)	Mg <sub>0.2076</sub> (Al <sub>1.29</sub> Fe <sub>0.335</sub> Mg <sub>0.445</sub> )Al <sub>0.18</sub> Si <sub>3.82</sub> O <sub>10</sub> (OH) <sub>2</sub>	-5206.9	-5218.70	0.23	-5601.0
Average				0.54	

\* References: 9—Stoessel (1988). 10—Kittrick (1982). 11—Kittrick (1984). 12—Huang and Keller (1973). 13—Misra and Upchurch (1976). 14—Carson et al. (1976). 15—Kittrick (1971a, 1971b, 1971c).

**TABLE 6.**  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  of the free oxide or hydroxide phases compared to  $g$ , and  $h$ , from the multiple linear-regression model

Oxide or hydroxide	$\Delta G_f^{\circ, \text{ox-hyd}}$ (kJ·mol <sup>-1</sup> )	$g_i$ (kJ·mol <sup>-1</sup> )	$\Delta H_f^{\circ, \text{ox-hyd}}$ (kJ·mol <sup>-1</sup> )	$h_i$ (kJ·mol <sup>-1</sup> )
<sup>16</sup> Al <sub>2</sub> O <sub>3</sub>	-1582.23	-1594.52	-1675.70	-1690.18
Al(OH) <sub>3</sub>	-1154.89	-1181.62	-1293.13	-1319.55
SiO <sub>2</sub>	-856.29	-853.95	-910.70	-910.97
MgO	-569.20	-628.86	-601.49	-660.06
Mg(OH) <sub>2</sub>	-833.51	-851.86	-924.54	-941.62
H <sub>2</sub> O	-237.14	-239.91	-285.83	-292.37
<sup>18</sup> CaO	-603.49	-669.13	-635.09	-696.65
FeO	-251.16	-266.29	-272.04	-290.55
Fe <sub>2</sub> O <sub>3</sub>	-742.68	-776.07	-824.64	-939.18
Fe(OH) <sub>2</sub>	-492.04	-542.04	-574.04	-596.07

Note: All measured thermodynamic data from Robie et al. (1978), except for Fe(OH)<sub>2</sub>, which is from Nordstrom et al. (1984).

minerals considered in this model is generally surrounded by, at most, only two Al(OH)<sub>3</sub> polyhedra with the other sites occupied by other tetrahedral components (generally SiO<sub>2</sub>). The presence of these other components in the nearest-neighbor sites clearly stabilizes the Al(OH)<sub>3</sub> in the silicates by the amount  $g_i - \Delta G_f^\circ \approx 28 \text{ kJ}\cdot\text{mol}^{-1}$ . The amount of this stabilization varies from site to site depending on the composition of the nearest-neighbor shell, but the efficacy of the model presented here demonstrates that this stabilization value is fairly constant for a wide variety of sites in a wide range of silicate compositions, regardless of structure type. Conversely, however, this consideration means that the coefficients derived in this model are likely to be useful only for silicates. Notice that in Table 6 the only polyhedron in which  $g_i > \Delta G_f^\circ$  is SiO<sub>2</sub>; this is consistent with quartz's being a very common mineral.

Thermodynamic data for ordered phases were chosen, whenever available, to create this model. As a result it seems likely that the estimated  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  values should be closest to those for a completely ordered mineral. Please note, however, that the variation in these values between ordered and disordered phases is generally smaller than the uncertainty of the estimate. For example, the differences between  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  for microcline versus sanidine is 0.07% and 0.20%, respectively (Robie et al., 1978), whereas the uncertainty of our estimate of these values for microcline are on the order  $\pm 0.25\%$ . A more sophisticated model will be necessary to develop enough resolution to account for order-disorder effects on these thermodynamic quantities.

This technique has a wide variety of applications in predicting thermodynamic properties of common zeolites and clays. First, the relative stability of clays in the K<sub>2</sub>O-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub>-H<sub>2</sub>O system will be discussed. Using the thermodynamic data in Table 8 a log  $a_{\text{K}^+}/a_{\text{K}^+}$  versus log  $a_{\text{H}_4\text{SiO}_4}$  diagram at 298 K was constructed (Fig. 3). Figure 3 shows the metastability of Al-montmorillonite and Al-illite, which agrees with the 298-K experimental data of Sass et al. (1987). In order to represent natural compositions more closely, we determined the effect on  $\Delta G_f^\circ$  of the sub-

**TABLE 7.** Method of estimation of  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  (in kJ·mol<sup>-1</sup>) for a mineral

- Determine chemical composition (analytical electron microscopy, microprobe, X-ray fluorescence, or wet-chemical analysis).
- Determine coordination based on known structures.
  - For Ca-bearing zeolite minerals with an unknown coordination number, the polyhedra is simply represented with a "z."
  - For 1:1 phyllosilicate minerals, distribute the octahedral cations as 0.6666 hydroxide and 0.3333 oxide. For 2:1 phyllosilicate minerals, the octahedral cations are distributed as 0.3333 hydroxide and 0.6666 oxide.
  - For chlorites, distribute cations into the interlayer in the order Al<sup>3+</sup> > Fe<sup>2+</sup> > Mg<sup>2+</sup> > Fe<sup>3+</sup> until the (OH)<sub>interlayer total</sub> = 8. The remaining cations are then distributed into the octahedral sheet following the method in 2B.
- Determine the number of polyhedra,  $n$ , of each component in the formula unit.
- Multiply  $n$  by the  $g_i$  and  $h_i$  values (Table 2). The interlayer thermodynamic contribution for chlorites is then calculated by multiplying  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  of free oxide or hydroxide (Table 6) by the corresponding values of  $n$  determined in 2C.
- Calculate  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  for the mineral of interest by summing the polyhedral contributions.

#### Example: Estimation of the $\Delta G_f^\circ$ of an illite

- Chemical formula = K<sub>0.75</sub>(Al<sub>1.75</sub>Mg<sub>0.25</sub>)Si<sub>3.5</sub>Al<sub>0.50</sub>O<sub>10</sub>(OH)<sub>2</sub>
- In this structure the polyhedra are <sup>14</sup>Al<sub>2</sub>O<sub>3</sub>, <sup>16</sup>Al<sub>2</sub>O<sub>3</sub>, <sup>18</sup>Al(OH)<sub>3</sub>, <sup>14</sup>SiO<sub>2</sub>, <sup>16</sup>MgO, <sup>16</sup>Mg(OH)<sub>2</sub>, and <sup>18-12</sup>K<sub>2</sub>O.
- The number of each polyhedra are 0.2500<sup>14</sup>Al<sub>2</sub>O<sub>3</sub>, 0.5833<sup>16</sup>Al<sub>2</sub>O<sub>3</sub>, 0.5833<sup>18</sup>Al(OH)<sub>3</sub>, 3.500<sup>14</sup>SiO<sub>2</sub>, 0.1666<sup>16</sup>MgO, 0.08333<sup>16</sup>Mg(OH)<sub>2</sub>, and 0.3750<sup>18-12</sup>K<sub>2</sub>O.
- $\Delta G_f^\circ = 0.2500g_i^{14}\text{Al}_2\text{O}_3 + 0.5833g_i^{16}\text{Al}_2\text{O}_3 + 0.5833g_i^{18}\text{Al}(\text{OH})_3 + 3.500g_i^{14}\text{SiO}_2 + 0.1666g_i^{16}\text{MgO} + 0.08333g_i^{16}\text{Mg}(\text{OH})_2 + 0.3750g_i^{18-12}\text{K}_2\text{O}$   
 $\Delta G_f^\circ = \{0.2500(-1631.32) + (0.5833)(-1594.52) + (0.5833)(-1181.62) + (3.500)(-853.95) + (0.1666)(-628.86) + (0.08333)(-851.86) + (0.3750)(-722.94)\}$
- $\Delta G_f^\circ = -5463.0 \text{ kJ}\cdot\text{mol}^{-1}$ ;  $\Delta H_f^\circ$  can be determined the same way.

stitution of various cations (Fe<sup>3+</sup>, Fe<sup>2+</sup>, and Mg<sup>2+</sup>) into the montmorillonite and illite structures (Table 8). Figure 3 shows how these cation substitutions shift the kaolinite-montmorillonite-illite triple point. Notice that the Fe<sup>3+</sup> substitution seems to cause the greatest degree of stabilization of montmorillonite and illite. When writing reactions containing Fe<sup>3+</sup>, Fe<sup>2+</sup>, and Mg<sup>2+</sup>, the concentrations of these cations in solution were assumed to be controlled by FeOOH, Fe(OH)<sub>2</sub>, and Mg(OH)<sub>2</sub> solubilities. The choice of Fe(OH)<sub>2</sub> and Mg(OH)<sub>2</sub> as controls of Fe<sup>2+</sup> and Mg<sup>2+</sup> concentrations assumes the presence of chlorite interlayers containing these components, as previously discussed. If an amorphous ferric hydroxide phase controls the Fe<sup>3+</sup> concentration, the kaolinite-montmorillonite-illite triple point becomes even more stable relative to kaolinite, microcline, and pyrophyllite.

This technique was also used to estimate the  $\Delta G_f^\circ$  of three K-zeolites: clinoptilolite, erionite, and phillipsite (Table 8). The results show that phillipsite is stable at SiO<sub>2</sub> concentrations of <12 ppm; erionite, between 12 and 16 ppm; and clinoptilolite, >16 ppm (Fig. 4). Extensive zeolite formation (clinoptilolite, erionite, and phillipsite) at surface conditions (25 °C) has been observed in

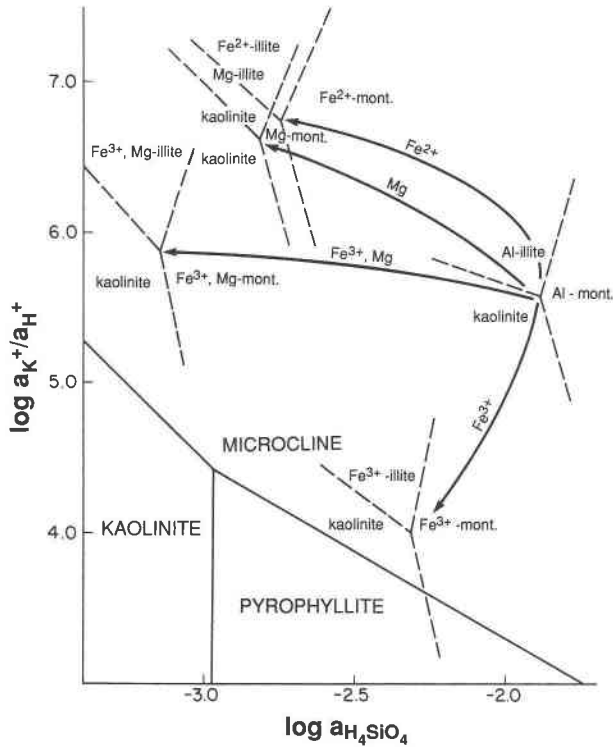


Fig. 3. Activity-activity diagram of the  $K_2O-Al_2O_3-SiO_2-H_2O$  system at 298 K showing the stable microcline-kaolinite-pyrophyllite triple point. This diagram also shows the effect of  $Mg^{2+}$ ,  $Fe^{3+}$ ,  $Fe^{2+}$ , and both  $Mg^{2+}-Fe^{3+}$  substitution (arrows) on the stability of the kaolinite-montmorillonite-illite triple point. Chemical compositions and thermodynamic data are given in Table 8.

altered volcanic tuffs (Hay, 1986; Sheppard and Gude, 1973). Senkayi et al. (1987) observed the coexistence of opal-CT-kaolinite-clinoptilolite at high silica concentrations, and Iijima (1978) reported that clinoptilolite and phillipsite are prominent in sediments in coexistence with interstitial water that has  $SiO_2$  concentrations of between 6–42 ppm and 5–21 ppm, respectively. The constructed activity diagram (Fig. 4) is consistent with these natural observations.

CONCLUSIONS

The multiple linear-regression technique presented here is a simple and effective way to estimate the  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$  of silicate minerals. The only data needed for this estimation technique are the chemical composition and the coordination of the “building block” polyhedra in the mineral of interest. The advantages of the technique include its simplicity (it can be programmed into a micro-computer spreadsheet program), the fact that the model is based on calorimetric and high-temperature phase-equilibrium measurements rather than more-difficult-to-perform solubility measurements, and its ability to model a wide range of silicate minerals. The technique gives results that agree quite well with a wide range of calorimetric and solubility data not used to derive the reported coefficients.

Although this technique seems to give reliable results for most cases, it should be used with some caution. We already know that the model presented here fails to predict accurately the thermodynamic properties of Ca-Al pyroxene, forsterite, cordierite, andradite, and gehlenite. There is no question that experimentally determined

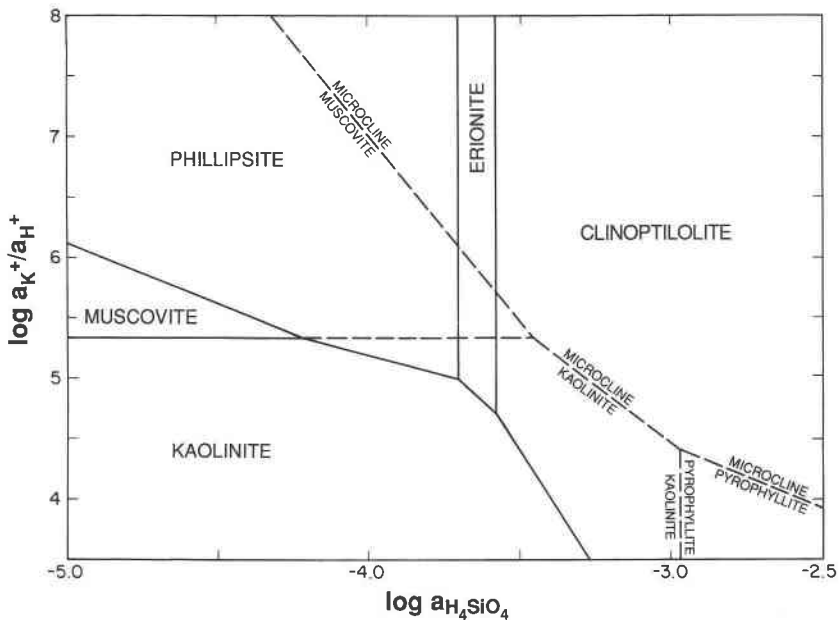


Fig. 4. Activity-activity diagram of the  $K_2O-Al_2O_3-SiO_2-H_2O$  system at 298 K showing three K-zeolite phases (phillipsite, erionite, and clinoptilolite). Thermodynamic data taken from Table 8.

TABLE 8.  $\Delta G_f^\circ$  data used in the calculation of  $K_2O-Al_2O_3-SiO_2-H_2O$  diagrams

Species	Chemical formula	$\Delta G_f^\circ$ (kJ·mol <sup>-1</sup> )
1. Kaolinite	$Al_2Si_2O_5(OH)_4$	-3799.4
2. Pyrophyllite	$Al_2Si_4O_{10}(OH)_2$	-5265.9
3. Microcline	$KAlSi_3O_8$	-3742.3
4. Muscovite	$KAl_3(Si_3Al)O_{10}(OH)_2$	-5595.5
5. Water	$H_2O$	-237.1
6. Silicic acid	$H_4SiO_4$	-1309.2
7. Goethite	$FeOOH$	-488.7
8. Brucite	$Mg(OH)_2$	-833.5
9. Ferrous hydroxide	$Fe(OH)_2$	-492.0
10. Potassium ion	$K^+$	-282.7
11. Illite (Al)	$K_{0.75}Al_2(Si_{3.25}Al_{0.75})O_{10}(OH)_2$	-5508.9
12. Montmorillonite (Al)	$K_{0.3}Al_1.9Si_4O_{10}(OH)_2$	-5282.5
13. Illite (Mg)	$K_{0.75}Al_{1.75}Mg_{0.25}(Si_{3.50}Al_{0.50})O_{10}(OH)_2$	-5463.0
14. Montmorillonite (Mg)	$K_{0.30}Al_{1.70}Mg_{0.30}Si_4O_{10}(OH)_2$	-5308.3
15. Illite (Fe <sup>2+</sup> )	$K_{0.75}Al_{1.75}Fe_{0.25}(Si_{3.50}Al_{0.50})O_{10}(OH)_2$	-5376.7
16. Montmorillonite (Fe <sup>2+</sup> )	$K_{0.30}Al_{1.70}Fe_{0.30}Si_4O_{10}(OH)_2$	-5204.8
17. Illite (Fe <sup>3+</sup> )	$K_{0.75}Al_{1.8}Fe_{0.4}(Si_{3.25}Al_{0.75})O_{10}(OH)_2$	-5338.9
18. Montmorillonite (Fe <sup>3+</sup> )	$K_{0.30}Al_{1.5}Fe_{0.4}Si_4O_{10}(OH)_2$	-5112.4
19. Illite (Fe <sup>3+</sup> , Mg)	$K_{0.75}Al_{1.35}Fe_{0.4}Mg_{0.25}(Si_{3.50}Al_{0.50})O_{10}(OH)_2$	-5293.0
20. Montmorillonite (Fe <sup>3+</sup> , Mg)	$K_{0.30}Al_{1.3}Fe_{0.4}Mg_{0.30}Si_4O_{10}(OH)_2$	-5138.3
21. Erionite	$KAlSi_5O_8 \cdot 3H_2O$	-4458.7
22. Phillipsite	$K_2Al_2Si_5O_{16} \cdot 6H_2O$	-9240.6
23. Clinoptilolite	$KAlSi_3O_8 \cdot 4H_2O$	-6406.5

Note: 1-3, 5, 7, 8, and 10—Robie et al. (1978). 4—Krupka et al. (1979). 6—Rimstidt (1984). 9—Nordstrom et al. (1984). 11-23—This model.

thermodynamic data are more accurate than these estimates and should be used in calculations when available. Furthermore, users should always consider whether the predictions of this approach make sense in terms of their geologic and/or geochemical experience.

The overall usefulness of this model is demonstrated by showing a few examples in the  $K_2O-Al_2O_3-SiO_2-H_2O$  system. These activity-activity diagrams show that the clay-mineral relations and the zeolite stability ranges determined using the estimated data agree well with experimental and geologic observations. Thus, the overall approach can be used to derive information on clay and zeolite mineral stabilities and then to develop a better understanding of chemical reactions that occur during diagenesis. The  $\Delta G_f^\circ$  values estimated from the model can be extrapolated to higher temperatures using estimated  $\Delta H_f^\circ$  in the van't Hoff equation or by developing a similar model using higher-temperature experimental data. In addition, it is likely that this technique could successfully model the thermodynamic properties of other complex mineral families (e.g., sulfates, phosphates, arsenates, and vanadates). Finally, this research extends the use of the "polyhedral approach" (Hazen, 1988) in modeling the thermodynamic properties of silicate minerals from  $S^0$  (Robinson and Haas, 1983; Holland, 1989) to include  $\Delta G_f^\circ$  and  $\Delta H_f^\circ$ . The success of these "polyhedral models" strongly supports the concept that the properties of silicate minerals are mostly determined by nearest-neighbor interactions rather than by the longer-range ordering used to classify these minerals into structure types.

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