STRUCTURAL CRYSTALLOGRAPHIC RELATION BETWEEN SODIUM SULFATE AND POTASSIUM SULFATE AND SOME OTHER SYNTHETIC SULFATE MINERALS*†

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Abstract

A study of the structural crystallographic relations between the following sulfate compounds has been made using x-ray methods as the main tool: Na_2SO_4 - K_2SO_4 , Na_2SO_4 - Li_2SO_4 , K_2SO_4 - Li_2SO_4 , K_2SO_4 - $(NH_4)_2SO_4$ and Na_2SO_4 - $(NH_4)_2SO_4$.

Aphthitalite, a sodium potassium sulfate mineral, has been prepared in the laboratory from aqueous solutions as well as from fused melts of various sodium and potassium sulfate proportions. X-ray methods reveal that at high temperatures close to fusion, sodium sulfate and potassium sulfate are isomorphous and form a complete series of solid solutions. The same synthetic mineral, prepared from aqueous solutions, has been found by x-ray investigation and checked by chemical analysis to have a limited range of solid solution varying between the ratios of 1K:1Na to 5K:1Na when crystallized at 70° C. and limited to the almost invariable ratio of 3K:1Na at room temperature.

X-ray powder data are given for LiKSO₄ and LiNaSO₄, and also for the NH₄KSO₄ member of the continuous series of crystalline solid solution (NH₄)₂SO₄-K₂SO₄. It is shown by the x-ray powder method that complete immiscibility exists between (NH₄)₂SO₄ and Na₂SO₄ at 70° C.

For LiNaSO₄ c_0 =9.76 ű0.02, a_0 =7.64 ű0.02, space group P31c, Z=6, g. (determined)=2.515, g. (calc.)=2.527; basal twinning with 0001 as twinning plane is common.

INTRODUCTION

The study of the structural relation between sodium sulfate and potassium sulfate is of particular interest in the field of crystallography because of the fact that each compound occurs in more than one crystallographic modification (polymorph) and that there has been some controversy as to whether there exists a solid solution relationship or isomorphism, or both, between certain polymorphs of the two compounds. The existence of such solid solution or isomorphism, if any, is of special interest in structural crystallography because of the big difference in ionic radii between sodium (0.98 Å) and potassium (1.33 Å), which is equal to 0.35 Å or 35.7% of the smaller ion (sodium). Sodium and potassium are not generally grouped together in isomorphous series. Potassium is usually grouped with rubidium and cesium but not with sodium. Tutton (1922) in working out the isomorphous relationship between the alkali sulfates excluded sodium sulfate from his series.

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RELATION BETWEEN SODIUM AND POTASSIUM SULFATE 119

Aphthitalite (or glaserite) has for a long time been assigned the composition $3K_2SO_4 \cdot Na_2SO_4$ or $K_3Na(SO_4)_2$. It has been shown by a number of investigators, Bücking (1889; Douglashall region in Germany), Teeple (1921; Searles Lake, California), Kurnakov, *et al.* (1936; Ural-Emba District, Russia), and Kurnakov, *et al.* (1938; Permian Sea and the salt lakes of Western Kazakhstan, Russia), to be widespread in saline deposits of lake basins. The mineral occurs also around volcanoes, e.g. Vesuvius, Scacchi (1875) and Bellanca (1942). Common among all these investigators, with the exception of Bellanca (1942), is the invariable composition $3K_2SO_4 \cdot Na_2SO_4$ which they assigned to the mineral aphthitalite.

The composition and structure of aphthitalite have been the subject matter of argument and discussion since 1891. The problem is: Is there any crystallographic relation between sodium sulfate and potassium sulfate? Retgers (1891) stated that there is no isomorphism between sodium sulfate and potassium sulfate. He considered aphthitalite as a double salt of the composition 3K₂SO₄+Na₂SO₄. Van't Hoff (1903), on the other hand, regarded aphthitalite as an isomorphous compound of the not closely investigated hexagonal modifications of both components. Gossner (1904) considered aphthitalite as a binary compound of a constant chemical composition, NaK₃(SO₄)₂. Van't Hoff and Barschall (1906) pointed to the existence of a series of solid solutions including the composition NaK₃(SO₄)₂. Druzhinin (1938), investigating the system Na₂SO₄--K₂SO₄-H₂O at the temperature of 25° C., considered aphthitalite as a solid solution of the definite chemical compound K₃Na(SO₄)₂ with Na₂SO₄ and reported that the compound permits substitution of Na for K within the range K/Na=2.44 to 3.00. Perrier and Bellanca (1940) and Bellanca (1942) using both thermal analysis technique and x-ray powder photographs believe that the compound is not K₃Na(SO₄)₂ but rather KNaSO₄. This forms solid solutions with K₂SO₄ (up to 73 mol per cent total content of the latter) and with Na₂SO₄ (up to 75 mol per cent). Bredig (1942) states that aphthitalite should be considered simply as a solid solution of the high temperature forms of both potassium sulfate and sodium sulfate. Frondel (1950) gives the formula for aphthitalite as $(KNa)_3Na(SO_4)_2$. Winchell (1951) considers aphthitalite, NaK₃(SO₄)₂, as "a double saltnot a crystal solution." He mentions that the Na:K ratio seems to vary from about 1:4 to about 1:1.

Sodium sulfate exists in five polymorphous modifications: I, (II), III, (IV), and V. Using the x-ray powder method, Kracek and Ksanda (1930) showed that Na_2SO_4 I is stable above 240° C., Na_2SO_4 III is metastable below 185° C. but inert when dry at ordinary temperatures, and Na_2SO_4 V is stable at ordinary temperatures. Polymorphs II and IV are unstable at ordinary pressure. Na_2SO_4 V is equivalent to the natu-

rally occurring mineral thenardite, a rare salt lake deposit and also found near some volcanoes.

Potassium sulfate exists in two polymorphous modifications, namely: (1) a high-temperature modification, called alpha- K_2SO_4 , stable above 590° C. and is uniaxial negative, and (2) a low-temperature modification called beta- K_2SO_4 , stable at room temperature, orthorhombic, with the space group *Pmcn*. Arcanite is the name of the mineral having the composition K_2SO_4 (equivalent to beta- K_2SO_4) and is said to be of very rare occurrence (Frondel, 1950).

Table 1 is a summary of the crystallographic data of the various sulfates mentioned above.

Substance	System	Space Group	a _o	bo	Co	z	Ref
Na ₂ SO ₄							
I	Hex.		5.39		7.25	2	1
III	Orth.	Pbnn	5.59	8.93	6.98	4	2
V	Orth.	Fddd	5.85	12.29	9.75	8	3
K ₂ SO ₄							
α	Hex.		5.71		7.85	2	4
β	Orth.	Pmcn	5.77	10.06	7.52	4	5
NaK ₃ (SO ₄) ₂	Hex.	P3m	5.65		7.33	1	6
NaKSO ₄	Hex.	$P\overline{3}m$	5.643		7.259	2	7

m	4
TADTE	н.
LADLE	д,

1. Calculated from data of Kracek and Ksanda (1930).

2. Frevel (1940).

3. Zachariassen and Ziegler (1932).

4. Bredig (1942).

5. Strukturbericht (1937).

6. Gossner (1928).

7. Bellanca (1942).

The Relation Between Sodium Sulfate and Potassium Sulfate

The System Na₂SO₄-K₂SO₄ (Fused samples)

Samples were prepared by fusing mixtures of Na₂SO₄ and K₂SO₄ ranging in molecular ratios from 4:1 to 1:4. These gave very similar powder photographs, and it seems apparent that when crystallizing from a melt, there is a continuous solid solution between the hexagonal forms of Na₂SO₄ and K₂SO₄. The pure end members always invert to a lower

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symmetry modification upon cooling. On the other hand, there is a range of compositions between the end members in which the hexagonal form of the solid solution is stable. On either side of this stable range, as the end member is approached, the originally formed solid solution unmixes, yielding the pure end member, which inverts on cooling, and a stable solid solution phase containing a lower percentage of the end member than was present in the melt.

The limits of this range in which the solid solution is stable are difficult to determine in samples prepared from melts. The material is so fine grained, and the variation in refractive indices so slight, that optical differentiation of a pure end member and a solid solution close to that end member is impractical. The x-ray powder photographs of samples approaching the end members in composition show increasing evidence of a phase consisting of the inverted end member. But in the range of 3:1 to 1:3, or even 4:1 to 1:4, this unmixing and inversion is negligible. This difficulty in establishing definite limits for the stable range in material prepared by fusion is not encountered when using single crystals prepared from solution. These are discussed later.

The lattice constants, a_o and c_o , for some members of this high-temperature solid solution series of aphthitalite, have been determined from the corresponding powder photographs. These are given, together with the published data on Na₂SO₄ I (calculated from data of Kracek and Ksanda, 1930) and α -K₂SO₄ (Bredig, 1942), in Table 2. This table shows clearly the increase in the unit cell dimensions as the result of the substitution of potassium for sodium.

	Na ₂ SO ₄ I	Na ₄ K	Na ₃ K	NaK	NaK ₃	NaK4	α -K ₂ SO ₄
ao	5.39	5.49	5.50	5.64	5.66	5.67	5.710
Co	7.25	7.26	7.265	7.27	7.33	7.39	7.85

TABLE 2

Thin sections and crushed fragments showed aphthitalite to be uniaxial positive. The values of ω and ϵ increase with higher content of potassium. They range from 1.485 to 1.493 for ω , and from 1.492 to 1.500 for ϵ (Na light; values ± 0.002). Winchell (1951) gives the range for ω as 1.487 to 1.491, and for ϵ 1.492 to 1.499, in good agreement with the values found for the synthetic material. The general trend of increase of indices is shown graphically in Fig. 1.

Using the pycnometer method a general increase in the specific gravity was found in going from the high-sodium members to the high-potassium members. The determined specific gravity values range from 2.68 (for Na₄K) to 2.71 (for NaK₄) with an experimental error of ± 0.01 . Winchell (1951) gives the specific gravity of 2.7 for aphthitalite of the composition NaK₃(SO₄)₂. Gossner (1928) gave the value of 2.697 for the same composition. The specific gravity of aphthitalite from Vesuvius was reported by Bellanca (1943) to be 2.697. The determined specific gravities were found to be in general agreement with those calculated according to the increasing lattice constants given in Table 2.



Fig. 1

The System $Na_2SO_4 - K_2SO_4 - H_2O$ (Aqueous solutions)

X-ray powder photographs of crystals grown from aqueous solutions of various molecular ratios of sodium sulfate and potassium sulfate proved to be similar to those taken for the fused aphthitalites. Also powder photographs of crystals obtained from aqueous solution and then fused were found to be similar to those of the unfused ones. This indicates that the crystals grown from aqueous solutions at the temperatures of 70°, 50° , 35° and 20° C. are anhydrous. Weissenberg photographs of these crystals showed the hexagonal symmetry and yielded the space group of $P\overline{3m}$, in agreement with that given by Gossner (1928) and Bellanca (1943). The powder photographs of the various crystals, formed at the same temperature but grown from solutions of different composition show either the aphthitalite type of pattern or that of the end members, Na_2SO_4 V or β -K₂SO₄. It is quite apparent that the crystals do not have the same chemical composition as that of the solution from which they crystallize. Table 3 shows the results of the chemical analyses in terms

Composition of Solution		Tempera-	Tempera- ture		Composition of Crystals Produced			
Na ₂ SO ₄	;	$\mathrm{K}_2\mathrm{SO}_4$	ture	tively	pattern	Na ₂ SO ₄	:	K_2SO_4
	%			%			%	
75.0	3	25.0	70° C.		Na ₂ SO ₄ V	100.0	:	
66.7	:	33.3	70° C.	28.0	Aphthit.	42.0	5	58.0
50.0	:	50.0	70° C.	31.6	Aphthit.	33.0		67.0
33.3	:	66.7	70° C.	39.2	Aphthit.	12.9	2	87.1
25.0	:	75.0	70° C.	45.1	β -K ₂ SO ₄			100.0
20.0	3	80.0	70° C.	45.1	β -K ₂ SO ₄		:	100.0
66.7	1	33.3	50° C.	34.6	Aphthit.	26.0	:	74.0
50.0	1	50.0	50° C.	35.8	Aphthit.	23.0	:	77.0
33.3	3	66.7	50° C.	40.5	Aphthit.	12.0	:	88.0
25.0	\$	75.0	50° C.	45.5	B-K2SO4		:	100.0
20.0	\$	80.0	50° C.	45.5	β -K ₂ SO ₄	-	:	100.0
66.7	1	33.3	35° C.	34.0	Aphthit.	27.0	•	73.0
50.0	3	50.0	35° C.	35.8	Aphthit.	23.0	:	77.0
33.3	2	66.7	35° C.	40.6	Mixture	11.0	:	89.0
25.0	4	75.0	35° C.	45.0	β -K ₂ SO ₄	-	:	100.0
20.0	:	80.0	35° C.	45.0	β -K ₂ SO ₄		:	100.0
66.7	:	33.3	20° C.	35.6	Aphthit.	24.0	;	76.0
50.0	:	50.0	20° C.	36.4	Aphthit.	22.0	:	78.0
33.3	5	66.7	20° C.	45.5	β -K ₂ SO ₄	1000	:	100.0
25.0	:	75.0	20° C.	45.5	β -K ₂ SO ₄			100.0
20.0	3	80.0	20° C.	45.5	β -K ₂ SO ₄		;	100.0

TABLE 3

of the percentage of potassium in each crystal and the corresponding composition of the crystal in terms of the molecular percentage of the two end members. The chemical analyses, made by the periodate method (Willard, Boyle 1941), are within the range of experimental error of $\pm 1.0\%$. The values in Table 3 were then used in the construction of Fig. 2 which shows the relationship between the composition of the crystals and that of the solutions from which they were grown at the various temperatures of 70°, 50°, 35°, and 20° C. The results of the chemical analyses are in agreement with those of x-rays.

The range of the limited solid solution series of aphthitalite, formed from the pure compounds dissolved in distilled water, is shown in Fig.

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3, based on the results of both chemical analyses and powder photographs. It is interesting to note that the range of the solid solution decreases with decrease in temperature until it finally shrinks to a very small range at 20° C. At this temperature aphthitalite acts like a compound of fixed composition, and explains why many previous investiga-



Fig. 2

tors had so regarded it. Perrier and Bellanca (1940) stated that aphthitalites of volcanic origin occur in nature with the ratio of K_2SO_4 to Na_2SO_4 varying from 3:1 to 1:3. When formed from aqueous solutions, on the other hand (artificially or in salt deposits), it always shows the ratio approximately 3:1. This last statement seems to be true only at temperatures of 30° or lower.



FIG. 3

The Crystal Structure of the Isomorphous Series Na_2SO_4 I, Aphthitalite, and β -K₂SO₄

Gossner (1928) described a structure for NaK₃(SO₄)₂, and Bellanca (1943) reported a closely related structure for NaKSO₄. Bredig (1941) proposed a structure type A₂XO₄, with a hexagonal unit cell $P\overline{3}m1$ and Z=2, for a series of compounds, principally at high temperatures. These included CaSiO₄ and alkaline earth phosphates, as well as alkali sulfates. No atomic positions were suggested.

In the space group P3m1, the positions of the 4 metal atoms are not all structurally equivalent. Two occur at $\pm \frac{1}{3} \frac{2}{3} z$; one at 000 and one at 00 $\frac{1}{2}$. In these three types of positions the number and arrangement of the oxygen atoms surrounding the metal atoms are different. For the structures of NaK₃(SO₄)₂ and NaKSO₄, as determined by Gossner and Bellanca,

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respectively, the distances from the metal to oxygen vary considerably. In all cases they are greater than the sum of the commonly used values of the ionic radii, and for one position considerably greater. This could account for the unusually small changes in unit cell dimensions with marked changes in the relative proportions of Na and K, and also offers an explanation of why these two elements, which do not usually replace each other in solid solution series, do so in this case.

It would seem most probable that the replacement of Na by K is selective, rather than occurring randomly over the 2+1+1 metal positions. If, starting with a low K content, additional K ions can replace Na ions in positions where the Na to O distance is greater than necessary (in so far as required by Na radius+O radius), the impact on unit cell dimensions will not be appreciable until these positions are filled. This would explain the comparatively small changes in the values of a_o and c_o until outside the 4:1 and 1:4 range of Na and K. The comparatively large change in c_o at the K end of the series occurs when even the positions with least room, originally filled by Na, must now be occupied by K. The smaller change, chiefly in a_o , at the Na end of the series may be attributed to the fact that here the cell dimensions are chiefly controlled by the close packing of O atoms.

The Relation Between Lithium Sulfate and Potassium Sulfate

The System Li₂SO₄-K₂SO₄-H₂O (Aqueous solutions)

Li₂SO₄ is not known to occur as a natural mineral. It is monoclinic and may be prepared by fusion of the common reagent salt, Li₂SO₄· H₂O, which is also monoclinic. The ionic radii of Li⁺ and K⁺ are 0.78 Å and 1.33 Å, respectively. The earliest investigation of the compound LiKSO₄ goes back to Schabus (1855) who erroneously described it as an isomorphous mixture of Li₂SO₄ and K₂SO₄. Later the substance was investigated by Rammelsberg (1866), Scacchi (1867), Wyrouboff (1880, 1882 and 1890), Wulff (1890, 1893), and Traube (1892 and 1894). Their descriptions were concerned with the morphology of the crystals which were found to be hexagonal pyramidal, with a:c=1:1.6755 (Traube, 1892).

During the crystallization of mixtures of lithium sulfate and potassium sulfate from aqueous solutions, the common reagent salt $\text{Li}_2\text{SO}_4 \cdot \text{H}_2\text{O}$ was used. Two types of solutions were prepared, namely, neutral (i.e. the pure salts dissolved in distilled water) and acidic (i.e. a few drops of concentrated H_2SO_4 were added to the solution in distilled water). Crystallization was made at room temperature and at 70° C. ($\pm 3^\circ$). The compositions of the solutions were in the following molecular ratios

when calculated in terms of Li₂SO₄:K₂SO₄=4.30:1, 3.44:1, 2.58:1, 1.72:1, 0.86:1, 1:2.32, and 1:3.48, respectively. Platy hexagonal crystals, with well developed basal pinacoids, were formed from most of the solutions. Laue photographs show hexagonal symmetry, and Weissenberg photographs yielded the space group $P6_3$, with $a_o = 5.13$ Å and $c_o = 8.60$ (± 0.02 Å), in agreement with the data of Bradley (1925) for LiKSO₄. Powder photographs of crystals grown from the various solutions at two different temperatures were made, with the results shown in Table 4.

	Type of a	-ray powder phot	ographs of cryst	als formed	
Mol. ratio of Li ₂ SO4:K ₂ SO4	at 7	0° C.	at 20° C.		
in solution	From Neut, sol.	Acid sol.	Neut. sol.	Acid sol.	
4.30:1.0	LiKSO4	mixture of Li ₂ SO ₄ · H ₂ O and LiKSO ₄	LiKSO4	LiKSO₄	
3.44:1.0	LiKSO4	LiKSO4	LiKSO4	LiKSO4	
2.58:1.0	LiKSO4	LiKSO4	LiKSO ₄	LiKSO4	
1.72:1.0	LiKSO4	LiKSO4	LiKSO4	LiKSO4	
0.86:1.0	LiKSO4	LiKSO4	β -K ₂ SO ₄	β -K ₂ SO ₄	
1.00:2.32	mixture of				
	β-K2SO4 & LiKSO4	LiKSO₄	β -K ₂ SO ₄	β-K ₂ SO ₄	
1.00:3.48	β-K ₂ SO ₄	β-K ₂ SO ₄	β -K ₂ SO ₄	β-K₂SO₄	

TABLE 4

The powder pattern data are given in Table 5, There is no change in the spacings of the lines on the films, indicating that the crystals represent a compound of fixed chemical composition, with no solid solution relationship. As an additional check, chemical analyses were made. These are shown in Table 6, and the results show clearly that the potassium content in crystals grown from different solutions is almost constant, and corresponds to the 1:1 ratio of K:Li.

The System Li₂SO₄-K₂SO₄ (Fused samples)

Powder photographs of samples prepared by fusing mixtures of Li_2SO_4 and K_2SO_4 in various proportions likewise indicate clearly that there is no solid solution relationship. Only one mixture of the approximate ratio of 1:1 gave rise to the LiKSO₄ pattern alone. All other mixtures gave the LiKSO₄ pattern together with that of either Li₂SO₄ or K₂SO₄, depending upon the proportions of the mixture. Thus even at the higher

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d observed	d calc.	$hk \cdot l$	I observed
4.33 Å	4.31 Å	00 · 2	1
4.00	3.96	$10 \cdot 1$	10
3.12	3.10	$10 \cdot 2$	9
2.58	2.57	11.0	7
2.47	2.47	$11 \cdot 1$	2
2.22	$ \begin{cases} 2.225 \\ 2.21 \end{cases} $	$20 \cdot 0$ $11 \cdot 2$	5
2.16	2.165 2.155	$\begin{array}{c} 20 \cdot 1 \\ 00 \cdot 4 \end{array}$	5
1.985	1.98	20 · 2	1
1.66	$ \begin{cases} 1.655 \\ 1.650 \end{cases} $	21 · 1) 11 · 4∫	3
1.61	1.61	$10 \cdot 5$	1
1.58	1.57	$21 \cdot 2$	3
1.50	1,49	30.0	3
1.37	1.36	20 - 5	2

TABLE 5. POWDER PHOTOGRAPH DATA FOR LIKSO4

TABLE 6

Composition of solution in terms of mol. ratio Li ₂ SO ₄ :K ₂ SO ₄	Percentage of K in crystals	Theoretical percentage of K in LiKSO4	Type of powder pattern
3.44:1	27.8	27.5	LiKSO4
2.58:1	27.0	27.5	LiKSO4
1.72:1	27.7	27.5	LiKSO ₄
0.86:1	28.6	27.5	LiKSO ₄
3.44:1*	28.0	27.5	LiKSO4
2.58:1*	28.2	27.5	LiKSO4

* Crystallized from slightly acid solution.

temperature near fusion, the LiKSO₄ structure does not permit substitution of either Li or K for the other, unless there was unmixing during cooling. The cooling was relatively rapid, and if there was any tendency for a solid solution to form, it is probable that it would have persisted as a metastable phase, especially close to the 1:1 ratio.

THE RELATION BETWEEN LITHIUM SULFATE AND SODIUM SULFATE The System Li₂SO₄-Na₂SO₄-H₂O (Aqueous solutions)

The earliest investigation of crystals of LiNaSO₄ found reported is

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that of Scacchi (1867), who determined the axial ratio for the ditrigonal pyramidal crystals to be a:c=1:0.5624. Traube (1892) reported the specific gravity of LiNaSO₄ as 2.369. This last value was not confirmed in the present study. The crystals used by these early investigators were obtained from aqueous solutions at about 50° C., and also from acid solutions, with or without the addition of NaCl.



Fig. 4

Crystals were grown from solutions containing a wide range of ratios of Li₂SO₄ and Na₂SO₄. Better crystals were obtained when a few drops of H₂SO₄ were added to the solutions, and crystallization was carried out at about 70° C. Most of the crystals were elongated parallel to the caxis. A fairly common feature observed on these crystals is an equatorial marking around the prism zone. Figure 4 shows some free hand drawings of typical crystals as they appear under low magnification with the binoculars. In most cases the mark appears as an even straight line, which may completely surround the crystal (Fig. 4, c, d, e, f and g), or only partly surround it (Fig. 4a). Under higher magnification, this line shows as a series of tiny disconnected re-entrant angles. In many cases at the intersection of this line with an edge, there is a more prominent re-entrant angle (Fig. 4, b, e and g). On the two circle goniometer, the parts of a prism face on either side of the line either reflect light simultaneously, or else give signals separated by only a few minutes of arc. Usually the prism faces continue uninterrupted on both sides of the line (Fig. 4, d and e), but in some cases the faces are interrupted, and different forms are shown on the two sides (Fig. 4, c, f, and g). Since the crystals of LiNaSO₄ do not have a horizontal symmetry plane, it is believed that this line represents twinning on (0001).

No previous x-ray work has been reported on LiNaSO₄. Laue photographs at first glance appear to show a 6-fold axis of symmetry, but careful inspection reveals a few reflections which indicate the true symmetry to be 3-fold. (Laue symmetry $\overline{3} 2/m$). This is verified by Weissenberg photographs. Lattice constants of the hexagonal unit cell (P) were found to be $a_0 = 7.64$ Å and $c_0 = 9.76$ Å (± 0.02 Å), giving an axial ratio of a:c=1:1.277. The pyramidal faces gave poor reflections. Measurements on the two circle goniometer show two sets of pyramidal faces, separated by 30°, which in terms of the unit cell dimensions are 10.2 and 11.4. If the latter were assumed to be the unit pyramid $10 \cdot 1$, the derived axial ratio would be 0.58, close to that given by Scacchi. The characteristic missing reflections on the Weissenberg photographs are *hh2hl* with *l* odd, indicating a c glide plane. In the Laue class $\overline{3} 2/m$ the only possible space groups with a c glide are $P\overline{3}1c$ and P31c. Since LiNaSO₄ crystals are known to be pyroelectric (Traube, 1892), space group $P\overline{3}1c$ is ruled out.

The specific gravity of the crystals was determined by diluting acetylene tetrabromide until they remained suspended in it. The specific gravity of the liquid was then found to be 2.515, which is quite different from the value of 2.369 reported by Traube (1892). Because of this discrepancy, an approximate check was made with the Gladstone and Dale Law. Using the specific refractive energy values (Larsen and Berman, 1934) of LiNaSO₄, and the refractive indices, namely $\epsilon = 1.495$ and $\omega = 1.490$, the specific gravity of this compound was determined to be 2.54. Using the experimentally determined value of 2.515, the number of formula weights of NaLiSO₄ in the unit cell was found to be 5.97 \cong 6.

Powder photograph data are given for LiNaSO₄ in Table 7. No change in the spacings of the powder patterns of the various samples was found, indicating the absence of any solid solution relationship between Li_2SO_4 and Na_2SO_4 . Since these two compounds and the compound LiNaSO₄ all crystallize in different systems, no extensive solid solution would be expected.

The System Li₂SO₄-Na₂SO₄ (Fused samples)

X-ray powder photographs were made of samples prepared by fusing mixtures of varying proportions of Li_2SO_4 and Na_2SO_4 . Only one mixture of the approximate ratio 1:1 gave rise to a pattern consisting solely of

d observed	d calc.	hk·l	I observed
3.94 Å	3.95 Å	10 · 2	8
3.83	3.82	11.0	10
3.04	3.02	11 - 2	7
2.94	2.94	10.3	7
2.75	2.745	20.2	9
2.425	$\begin{cases} 2.445 \\ 2.430 \end{cases}$	$\begin{array}{c} 00 \cdot 4 \\ 12 \cdot 1 \end{array}$	4
2.31	2.32	20.3	3
2.215	$ \begin{cases} 2.23 \\ 2.20 \end{cases} $	$12 \cdot 2$ 30 \cdot 0	3
2.15	2.15	30 1	4
2.01	2.01	30 · 2	1
1.97	1.97	$20 \cdot 4$	2
1.91	1.91	22.0	5
1.88	1.88	10.5	1
1.83	$\begin{cases} 1.83 \\ 1.825 \end{cases}$	$13 \cdot 0$ $30 \cdot 3$	2
1.745	1.75	$12 \cdot 4$	1
1.69	1.685	20.5	1
	(1.65	40.0)	
1.64	1.635	40.1	2
	1.63	00.6	
1.60	`	i suveni i contri	2
1.565			2
1.545			2
1,505	1.50	11.6	3
1.47			4
1.44			4

TABLE 7. POWDER PHOTOGRAPH DATA FOR LINaSO4

LiNaSO4 lines. All other ratios gave the pattern of LiNaSO4 together with that of either Li₂SO₄ or Na₂SO₄, thus verifying the results obtained from the crystals. As was mentioned in the case of fused Li-K sulfate mixtures, there is the possibility of limited solid solution near the fusion temperature, with unmixing on cooling.

The System (NH₄)₂SO₄-K₂SO₄-H₂O (Aqueous solutions)

Ammonium sulfate occurs in nature as the mineral mascagnite. Both mascagnite and arcanite (β -K₂SO₄) are orthorhombic and have the space group Pmcn (Winchell, 1951). Because of the isomorphism of the two compounds and the similarity of the ionic radii of NH4 and K (1.43 and 1.33Å, respectively) complete solid solution between the two would be expected. Such was reported by Fock (1892). X-ray evidence completely

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substantiates this. Crystals formed from solutions of varying proportions do not have the same composition as the solution (Table 8), but are shown by both Weissenberg and powder photographs to be structurally alike, with gradual decrease in lattice constants with increasing potassium.

	a_o	Do	Co
$(NH_4)_2SO_4$	5.95 Å	10.56 Å	7.72 Å
NH4KSO4	5.84	10.08	7.52
β -K ₂ SO ₄	5.70	9.99	7.34

The measured spacings and intensities of the powder photograph lines of various NH_4 -K sulfate solid solutions are in agreement with the published data for the mineral taylorite as given by Winchell and Benoit (1951).

The crystals obtained from the various solutions of mixtures of potassium and ammonium sulfates were chemically analyzed so as to determine potassium quantitatively. A known amount of the dry powdered material was ignited first to remove NH_3 and the amount of potassium was then determined by the periodate method (Willard and Boyle, 1941). The results of the chemical analysis are given in Table 8. The table shows clearly how the composition of the crystals varies continuously with the change in the composition of the solution.

Comp. of solution K ₂ SO ₄ :(NH ₄) ₂ SO ₄	Temp. of crystalliza- tion	% K determined quant.	Type of x-ray powder pattern	Comp. of crystals K ₂ SO ₄ : (NH ₄) ₂ SO ₄
25.0:75.0	70° C.	21.05	xtalline solid soln.	46.3:53.7
33.3:66.7	70° C.	31.8	xtalline solid soln.	70.0:30.0
50.0:50.0	70° C.	39.4	xtalline solid soln.	86.5:13.5
66.7:33.3	70° C.	42.8	xtalline solid soln.	94.0: 6.0
75.0:25.0	70° C.	43.2	xtalline solid soln.	95.0: 5.0

TABLE 8

THE RELATION BETWEEN SODIUM SULFATE AND AMMONIUM SULFATE The System Na₂SO₄-(NH₄)₂SO₄-H₂O (Aqueous solutions)

No mineral having the composition of pure sodium ammonium sulfate has been reported. Ammonian aphthitalite, $(KNH_4)_3Na(SO_4)_2$, from the Chincha Islands has been described by Frondel (1950). Although Na₂SO₄ III, Na₂SO₄ V and $(NH_4)_2SO_4$ are all orthorhombic, their space groups are different. Since the ionic radii of NH₄ and Na are quite different, no solid solution of the $(NH_4)_2SO_4$ with either form of Na₂SO₄ would be expected. This was verified by powder photographs of crystals obtained from solutions of varying proportions of the two sulfates at 70° C. No evidence of solid solution was found. Samples could not be prepared by melting, since ammonium sulfate dissociates readily at higher temperatures.

SUMMARY AND CONCLUSIONS

1. Aphthitalite, a sodium potassium sulfate mineral, has been prepared in the laboratory from aqueous solutions as well as from fused melts of various sodium and potassium sulfate proportions. Using x-ray methods, powder, rotation and Weissenberg, it is revealed that at high temperatures close to fusion, sodium sulfate and potassium sulfate are isomorphous and form a complete series of solid solutions. The same synthetic mineral, prepared from aqueous solution has been found, by x-ray investigation and checked by chemical analysis, to have a limited range of solid solution varying between the ratios of 1K:1Na to 5K:1Na at 70° C. and is limited to the almost invariable ratio of 3K:1Na at room temperature. A gradual increase in the lattice constants as well as in the refractive indices has been observed, with increasing potassium content in the synthesized aphthitalites of the high-temperature complete solid solution series. It is concluded, therefore, that aphthitalite whether of composition NaK₃(SO₄)₂ or NaKSO₄ is to be considered simply as a solid solution member of the high temperature forms of sodium sulfate and potassium sulfate.

2. LiKSO₄ and LiNaSO₄, both hexagonal but with different space groups (i.e. different structures), are found to represent double compounds between Li_2SO_4 and K_2SO_4 and Li_2SO_4 and Na_2SO_4 , respectively. No solid solution relationship was revealed by x-ray analysis.

3. The following data have been determined for LiNaSO₄: $a_o = 7.64$, $c_o = 9.76 \ (\pm 0.02\text{\AA})$; $a_o: c_o = 1:1.277$; Z=6; space group P31c; measured specific gravity 2.515, calculated specific gravity 2.527. Twinning on (0001) common.

4. Complete solid solution and isomorphous relationship between ammonium sulfate and potassium sulfate have been verified by x-ray methods.

5. There is no solid solution between sodium sulfate and ammonium sulfate at 70° C.

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