The barometer tremolite + tschermakite + 2 albite = 2 pargasite + 8 quartz: Constraints from experimental data at unit silica activity, with application to garnet-free natural assemblages

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ABSTRACT

Garnet is notably absent in mafic to felsic lithologies, in low-*P* metamorphic terranes, and in Mgrich bulk compositions in high-*P* regionally metamorphosed terranes. In the absence of garnet, existing mineral barometers cannot be applied for estimating metamorphic pressure. A new garnet-free, horn-blende-plagioclase barometer has been formulated based on the reaction tremolite + tschermakite + 2 albite = 2 pargasite + 8 quartz. The intra- and cross-site mixing parameters for hornblende were retrieved exclusively from experimental data in the *P*-*T* window 1–15 kbar and 650–950 °C, after screening the available data for the presence of quartz. A linear least-squares fit to the coexisting hornblende and plagioclase composition in the experiments yields the following barometric expressions:

 $P_{1}(\text{kbar}) = [-9.326 + 0.01462\text{T}(\text{K}) + \text{RT}\text{ln}K_{\text{ideal}} - 98.698X_{\text{Na}}^{\text{A}} - 33.213X_{\text{K}}^{\text{A}} - 20.338X_{\text{Na}}^{\text{Ma}} - 39.101X_{\text{Fe}^{2+}}^{\text{M3}} + 100.392X_{\text{M2}}^{\text{M2}} + 131.03X_{\text{Fe}^{2+}}^{\text{M2}} + 82.479X_{\text{Fe}^{3+}}^{\text{M2}} - 118.653X_{\text{Al}}^{\text{Al}} - 2\text{RT}\text{ln}\gamma_{\text{Ab}}]/(-\Delta V)$

and

 $P_{2}(\text{kbar}) = [-1.869 + 0.0076T (\text{K}) + \text{RTln}K_{\text{ideal}} - 102.692X_{\text{Na}}^{4} - 35.251X_{\text{K}}^{4} - 15.969X_{\text{Na}}^{\text{M4}} - 40.499X_{\text{Fe}^{2+}}^{\text{M13}} + 93.069X_{\text{Al}}^{\text{M2}} + 130.750X_{\text{Fe}^{2+}}^{\text{M2}} + 74.226X_{\text{Fe}^{3+}}^{\text{M2}} - 104.402X_{\text{Al}}^{\text{T1}} - 2\text{RTln}\gamma_{\text{Ab}}]/(-\Delta V)$

where

$$K_{\text{ideal}} = \left[\frac{16(X_{\text{Na}}^{A})(X_{\text{Al}}^{\text{T1}})}{(X_{\Box}^{A})(X_{\text{Si}}^{\text{T1}})(X_{\text{Ab}})}\right]^{2}$$

 X_i^j denotes the mole fraction of cation *i* in site *j* of amphibole, X_{Ab} and γ_{Ab} are the mole fraction and activity coefficient of albite in plagioclase, respectively, and ΔV is the volume change for the reaction. In the expression for P_2 , the first two terms in the numerator on the right-hand side corresponding to ΔH° and ΔS° , respectively, were adopted from an internally consistent thermodynamic database. In the expression for P_1 , the first term on the right-hand side of the numerator, $\Delta \hat{H}$ (-9.326 kJ) = $\Delta H^\circ + a_9$, where a_9 is a mixing parameter, and the second term $\Delta S^\circ = 0.01462$ kJ/K, were retrieved by a linear least-squares fit to the experimental data. The formulations reproduced experimental P values within 2 kbar for 83% of the experimental runs. The cumulative precision (1 σ) of pressure estimated using the formulations varied between 800 and 2000 bars for errors propagated due to uncertainties in P-T, volume, and thermometric estimate, and inaccuracies in estimated composition of phases. In natural assemblages spanning a pressure range of 2.5 to 12.5 kbar, the quartz–hornblende–plagioclase barometers yielded pressure within 2 kbar of the P-value recommended by the authors, and is consistent with the stable Al₂SiO₅ polymorph in associated metapelites.

Keywords: Thermobarometry, hornblende, plagioclase, quartz, thermodynamics, mixing parameters of hornblende, experimental petrology, mafic rocks, silica-saturated, metamorphic petrology