

1 **Revision 1**

2 **Effect of hydration on the single-crystal elasticity of pyrope at high**  
3 **pressure and high temperature conditions: implications for the**  
4 **Earth's upper mantle**

5 DAWEI FAN<sup>1,\*</sup>, JINGUI XU<sup>1</sup>, CHANG LU<sup>2</sup>, SERGEY N. TKACHEV<sup>4</sup>, BO LI<sup>1,3</sup>,  
6 ZHILING YE<sup>1,3</sup>, SHIJIE HUANG<sup>1,3</sup>, VITALI B. PRAKAPENKA<sup>4</sup>, WENGE  
7 ZHOU<sup>1,\*</sup>

8 <sup>1</sup>Key Laboratory of High-Temperature and High-Pressure Study of the Earth's Interior, Institute of  
9 Geochemistry, Chinese Academy of Sciences, Guiyang, Guizhou 550081, China

10 <sup>2</sup>Department of Geological Sciences, Jackson School of Geosciences, The University of Texas at  
11 Austin, Austin, Texas 78712, U.S.A.

12 <sup>3</sup>University of Chinese Academy of Sciences, Beijing 100049, China

13 <sup>4</sup>Center for Advanced Radiation Sources, University of Chicago, Chicago, Illinois 60437, U.S.A.

14 \*Email: [fandawei@vip.gyig.ac.cn](mailto:fandawei@vip.gyig.ac.cn); [zhouwenge@vip.gyig.ac.cn](mailto:zhouwenge@vip.gyig.ac.cn)

15 **ABSTRACT:**

16 The elasticity of single-crystal hydrous pyrope with ~900 ppmw H<sub>2</sub>O has been  
17 derived from sound velocity and density measurements using *in situ* Brillouin light  
18 spectroscopy (BLS) and synchrotron X-ray diffraction (XRD) in the diamond anvil  
19 cell (DAC) up to 18.6 GPa at room temperature and up to 700 K at ambient pressure.  
20 These experimental results are used to evaluate the effect of hydration on the  
21 single-crystal elasticity of pyrope at high pressure and high temperature (*P-T*)  
22 conditions to better understand its velocity profiles and anisotropies in the upper  
23 mantle. Analysis of the results shows that all of the elastic moduli increase almost  
24 linearly with increasing pressure at room temperature, and decrease linearly with  
25 increasing temperature at ambient pressure. At ambient conditions, the aggregate  
26 adiabatic bulk and shear moduli ( $K_{S0}$ ,  $G_0$ ) are 168.6(4) GPa and 92.0(3) GPa,

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

27 respectively. Compared to anhydrous pyrope, the presence of ~900 ppmw H<sub>2</sub>O in  
28 pyrope does not significantly affect its  $K_{S0}$  and  $G_0$  within their uncertainties. Using the  
29 third-order Eulerian finite-strain equation to model the elasticity data, the pressure  
30 derivatives of the bulk  $[(\partial K_S/\partial P)_T]$  and shear moduli  $[(\partial G/\partial P)_T]$  at 300 K are derived  
31 as 4.6(1) and 1.3(1), respectively. Compared to previous BLS results of anhydrous  
32 pyrope, an addition of ~900 ppmw H<sub>2</sub>O in pyrope slightly increases the  $(\partial K_S/\partial P)_T$ , but  
33 has a negligible effect on the  $(\partial G/\partial P)_T$  within their uncertainties. The temperature  
34 derivatives of the bulk and shear moduli at ambient pressure are  $(\partial K_S/\partial T)_P=-0.015(1)$   
35 GPa/K and  $(\partial G/\partial T)_P=-0.008(1)$  GPa/K, which are similar to those of anhydrous  
36 pyrope in previous BLS studies within their uncertainties. Meanwhile, our results also  
37 indicate that hydrous pyrope remains almost elastically isotropic at relevant high  $P$ - $T$   
38 conditions, and may have no significant contribution to seismic anisotropy in the  
39 upper mantle. In addition, we evaluated the seismic velocities ( $V_P$  and  $V_S$ ) and the  
40  $V_P/V_S$  ratio of hydrous pyrope along the upper mantle geotherm and a cold subducted  
41 slabs geotherm. It displays that hydrogen has also no significant effect on the seismic  
42 velocities and the  $V_P/V_S$  ratio of pyrope at the upper mantle conditions.

43

44 **Keywords:** Hydrous pyrope, Single-crystal elasticity, High pressure and high  
45 temperature, Brillouin light scattering, Upper Mantle

46

47

48

49

50

51

52

53

54

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

### 55 INTRODUCTION

56 Silicate garnet is an important constituent in the Earth's upper mantle and transition  
57 zone (e.g. Anderson 1989; Anderson and Bass 1984; Bina 2013; Duffy and Anderson  
58 1989; Fan et al. 2009, 2011, 2015b, 2015c, 2017a; Frost 2008; Ita and Stixrude 1992;  
59 McDonough and Sun 1995). Mantle compositional models such as pyrolite and  
60 piclogite contain ~15% and ~22% of garnet in the upper mantle, respectively (e.g.  
61 Bass and Anderson 1984; Ringwood 1975). The percentage can increase to ~40% or  
62 even more in the transition zone because pyroxenes progressively dissolve into garnet  
63 with increasing pressure (Li B W et al. 2018), forming majorite-garnet solid solutions  
64 (Herzberg and Gasparik 1991; Ringwood 1991). Garnet is also one of the important  
65 mineral for eclogite (e.g. Kimura et al. 2013; Liu 1980; Xu et al. 2019), formed by  
66 high-pressure metamorphism of basalt or gabbro at subduction zones (Poli and  
67 Schmidt 2002; Ringwood 1982). Although most natural garnets are complex solid  
68 solutions, the most significant component of mantle garnets is its Mg end-member  
69 pyrope ( $\text{Mg}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ ) (Rickwood et al. 1968; Sinogeikin and Bass 2002). Therefore,  
70 pyrope or pyrope-rich garnet is an important mantle mineral, irrespective of what  
71 compositional model of Earth's mantle is assumed (Ringwood 1975; Ita and Stixrude  
72 1992).

73 In addition, previous studies have revealed that hydrogen could be incorporated  
74 into nominally anhydrous minerals (NAMs) as structurally bound hydroxyl defects  
75 (e.g. Ingrin and Skogby 2000; Skogby 2006; Smyth 1987). NAMs in the Earth's  
76 mantle thus have significant implications for the Earth's deep water cycle (e.g.  
77 Bolfan-Casanova et al. 2000; Hirschmann 2006; Hirschmann and Kohlstedt 2012;  
78 Smyth and Jacobsen 2006). Water can incorporate in garnets as OH- defects  
79 associated with charge balancing or oxidation-reduction reactions, or it may substitute  
80 Si in the hydrogarnet substitution (Lu and Keppler 1997; Mookherjee and Karato  
81 2010; Withers et al. 1998). Pyrope is a well-known hydrous-bearing NAMs phase in  
82 the upper mantle (e.g. Ackermann et al. 1983; Rossman et al. 1989). Natural

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

83 pyrope-rich garnets from ultrahigh-pressure metamorphic rocks and kimberlite  
84 xenoliths generally contain tens to hundreds of ppmw H<sub>2</sub>O (e.g. Aines and Rossman  
85 1984a, 1984b; Bell and Rossman 1992a, 1992b; Beran and Libowitzky 2006; Li H Y  
86 et al. 2018). Moreover, experiments on water solubility in garnets also indicated that  
87 pyrope and pyrope-rich garnets could dissolve certain amounts of hydrogen, ranging  
88 from a few hundred to ~ 1000 ppmw H<sub>2</sub>O (Geiger et al. 1991; Lu and Keppler 1997;  
89 Mookherjee and Karato 2010; Withers et al. 1998).

90 The accurate knowledge about the elastic property of pyrope or pyrope-rich garnet  
91 is critical for deducing seismic velocities and density profiles and further constructing  
92 reliable mantle mineralogy models (e.g. Bass and Anderson 1984; Bass et al. 2008;  
93 Duffy and Anderson 1989; Weidner and Wang 2000). Up to now, numerous equation  
94 of state studies of pyrope using XRD technique at high pressure/high temperature  
95 have been reported (e.g. Leger et al. 1990; Levien et al. 1979; Sato et al. 1978; Wang  
96 et al. 1998; Zhang et al. 1998; Zou et al. 2012a). Additionally, the elastic properties of  
97 pyrope at ambient and high pressure/temperature conditions have also been  
98 investigated using theoretical calculations (e.g. Li et al. 2011; Hu et al. 2016).  
99 Moreover, the adiabatic bulk and shear moduli of polycrystalline pyrope have been  
100 reported up to 24 GPa and 1700 K by ultrasonic interferometry technique (e.g.  
101 Chantel et al. 2016; Chen et al. 1997, 1999; Gwanmesia et al. 2006, 2007; Sumino  
102 and Nishizawa 1978; Suzuki and Anderson 1983; Zou et al. 2012b). On the other  
103 hand, BLS is another common technique to measure the elasticity of minerals (e.g.  
104 Bass and Zhang 2015; Speziale et al. 2014). It has tremendous advantages in deriving  
105 the complete set of elastic moduli in single-crystal minerals at extremely high *P-T*  
106 conditions (e.g. Fan et al. 2015a; Mao et al. 2015; Murakami et al. 2007; Yang et al.  
107 2015; Zhang et al. 2016). There have been a number of single-crystal elasticity studies  
108 on pyrope at ambient conditions (e.g. Leitner et al. 1980; O'Neill et al. 1991), high  
109 pressure (e.g. Conrad et al. 1999; Sinogeikin and Bass 2000), and high temperature  
110 (e.g. Sinogeikin and Bass 2002) conditions using BLS technique. Recently, Lu et al.

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

111 (2013) measured the single-crystal elasticity of Fe-bearing pyrope at high  $P$ - $T$   
112 conditions using BLS technique, which provided the detailed description of Fe effect  
113 on the elastic moduli of pyrope.

114 Furthermore, the effect of hydrogen on the elasticity of other major mantle minerals  
115 (e.g. olivine, wadsleyite, and ringwoodite) has been studied extensively at ambient  
116 and high pressure/high temperature conditions (e.g. Inoue et al. 1998; Jacobsen et al.  
117 2004, 2008; Mao et al. 2008, 2010, 2011, 2012; Sinogeikin et al. 2003; Wang et al.  
118 2003, 2006). However, there is only one study on the acoustic velocities and  
119 single-crystal elastic moduli of hydrous pyrope (~180 ppmw) using BLS technique at  
120 ambient conditions (O'Neill et al. 1991). The effect of hydration on the acoustic  
121 velocities and elastic moduli of pyrope at high  $P$ - $T$  conditions remains unavailable,  
122 even though it is highly desirable to use its single-crystal elasticity for understanding  
123 the geodynamic processes of the upper mantle. Up to now, only Fan et al. (2017b)  
124 conducted the high  $P$ - $T$  equation of state study of hydrous pyrope using  
125 synchrotron-based XRD technique.

126 In this study, we measured the acoustic velocities ( $V_P$  and  $V_S$ ) of single-crystal  
127 hydrous pyrope at high pressures up to ~18.6 GPa and high temperatures up to 700 K  
128 using BLS technique, and derived its full set of single-crystal elastic moduli at high  
129  $P$ - $T$  conditions. Based on our results, we further evaluated the effects of hydrogen on  
130 the elastic moduli, sound velocities, and elastic anisotropies of pyrope. Finally, we  
131 applied our results to discuss the hydrogen effect on the velocity profile and  $V_P/V_S$   
132 ratio of pyrope in the Earth's upper mantle.

### 133 **EXPERIMENTAL METHODS**

134 The single-crystal hydrous pyrope was synthesized in a multi-anvil pressure  
135 apparatus (YJ-3000T), at the Institute of Geochemistry, Chinese Academy of Sciences,  
136 Guiyang, China. More detailed information about the sample synthesis and sample  
137 characterization were presented elsewhere by Fan et al. (2017b). Here we briefly  
138 report results from Electron probe microanalysis (EPMA), Fourier transform infrared

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

139 (FTIR), and XRD. EPMA results show that our sample is homogeneous with a  
140 chemical formula as  $\text{Mg}_{3.006}\text{Al}_{1.995}\text{Si}_{3.005}\text{O}_{12}$ . Hydrogen concentrations were  
141 determined by FTIR spectroscopy and the absorption bands were readily attributed to  
142 structural bonded hydroxyl groups in pyrope (Geiger et al. 1991; Mookherjee and  
143 Karato 2010; Withers et al. 1998). The water content in our sample was determined to  
144 be  $\sim 900(\pm 100)$  ppmw using the formula of Bell et al. (1995). Meanwhile, the XRD  
145 pattern of our sample confirmed a cubic structure with lattice parameter  $a=11.460(3)$   
146 Å at ambient conditions, yielded the unit-cell volume  $V_0=1505.24(8)$  Å<sup>3</sup> and density  
147  $\rho=3.557(4)$  g/cm<sup>3</sup>. The unit-cell volume of our hydrous pyrope at ambient conditions  
148 is  $\sim 0.15\%$  higher than anhydrous pyrope (Du et al. 2015; Zhang et al. 1998), which  
149 agrees with previous studies for other mantle minerals (e.g. Holl et al. 2008; Smyth et  
150 al. 2003; Smyth and Jacobsen 2006; Ye et al. 2010, 2012).

151 Pyrope has a cubic structure with only three independent elastic moduli ( $C_{11}$ ,  $C_{12}$ ,  
152 and  $C_{44}$ ), and therefore, a single crystallographic orientation is sufficient to constrain  
153 all three of them using BLS measurements. The crystallographic plane of sample  
154 piece is (0.34, -0.53, 0.92) determined by single-crystal XRD at beamline 13-BMD of  
155 the GeoSoilEnviroConsortium for Advanced Radiation Sources (GSECARS) of  
156 Advanced Photon Source (APS), Argonne National Laboratory (ANL). We  
157 double-sides polished our sample pieces to  $\sim 20\text{-}30$  μm thickness with successively  
158 finer grits down to a final 3M diamond lapping film of 1 μm grainsize. The thinly  
159 polished platelet was then cleaved into several square pieces of the desired size ( $\sim 150$   
160 μm) for high-pressure/high temperature measurements.

161 High-pressure BLS combined with XRD measurements were conducted on the  
162 single-crystal hydrous pyrope in a short symmetrical DAC at 13-BMD beamline of  
163 APS. An incident X-ray beam of 0.3344 Å wavelength focused to a  $3\times 7$  μm<sup>2</sup> area was  
164 used to determine the unit-cell volume of crystal in the DACs. Round Re gasket of  
165 250 μm thick and 3 mm in diameter was pre-indented to  $\sim 55$  μm thickness using a  
166 pair of 500 μm culet size diamond anvils. Subsequently, a cylindrical 300 μm

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

167 diameter hole was drilled in the pre-indented area as the sample chamber. A  
168 single-crystal platelet with a diameter of  $\sim 150\ \mu\text{m}$  was then placed into the sample  
169 chamber, together with some ruby spheres of approximately  $5\ \mu\text{m}$  in diameter as the  
170 pressure indicator (Mao et al. 1986) for neon gas loading as well as for high-pressure  
171 experiments. The neon pressure medium was loaded into the sample chamber using  
172 the gas-loading system at GSECARS of APS (Rivers et al. 2008). Pressures were  
173 measured from ruby fluorescence spectra, while pressure uncertainties were  
174 calculated using multiple measurements before and after collection of BLS spectra for  
175 each pressure point. The XRD spectra were used to determine density at each pressure  
176 before and after BLS measurements (Table 1).

177 High-temperature BLS experiments were also performed at 13-BMD beamline of  
178 APS. A single-crystal hydrous pyrope ( $\sim 150\ \mu\text{m}$ ) was loaded into an  
179 externally-heated DAC (EHDAC), which was equipped with an alumina ceramic  
180 heater coiled with two Pt wires of  $200\ \mu\text{m}$  in diameter and 48 cm in length (Fan et al.  
181 2019; Kantor et al. 2012; Lu et al. 2013; Mao et al. 2015; Yang et al. 2014, 2016). Re  
182 was used as the gasket material and pre-indented to  $\sim 55\ \mu\text{m}$  thickness using a pair of  
183 diamond anvils with  $500\ \mu\text{m}$  culet size and then a  $300\ \mu\text{m}$  diameter sample chamber  
184 was drilled at the center of pre-indentation. The single-crystal hydrous pyrope sample  
185 was sealed in the sample chamber. An R-type thermocouple was attached to one of  
186 diamond surface approximately  $500\ \mu\text{m}$  away from its culet and clad with a ceramic  
187 adhesive (Resbond 920) for temperature measurements. To minimize temperature  
188 instability for each heating run, we firstly heated the sample chamber to a given  
189 temperature and then kept it at this temperature for at least 30 minutes. Temperatures  
190 of the sample chamber were actively stabilized within  $\pm 1\ \text{K}$  using the  
191 temperature-power feedback program with a remotely controlled Tektronix Keithley  
192 DC power supply during the experiments (Sinogeikin et al. 2006). Single-crystal  
193 XRD patterns of hydrous pyrope before and after BLS measurements were also  
194 collected to determine the lattice parameters and densities of the sample at high

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

195 temperatures (Table 2). Temperatures were increased every 100 K from room  
196 temperature (300 K) to maximum temperature (700 K), and then decreased to room  
197 temperature to check for possible changes in the lattice parameters and elastic moduli  
198 at ambient conditions. From Table 2, we can find that the lattice parameters and  
199 elastic moduli at ambient conditions of our hydrous pyrope are highly consistent  
200 before and after heating. In addition, we did not measure the water content of our  
201 sample after the high-temperature BLS measurements due to the relatively small size  
202 and thickness of our sample. However, the previous study has determined the water  
203 content of the hydrous garnet after heating up to  $\sim 1273$  K and indicated the water  
204 loss of hydrous sample less than 10% (Dai et al. 2012). The maximum experimental  
205 temperature in this study ( $\sim 700$  K) is significantly lower than that in previous study  
206 ( $\sim 1273$  K) (Dai et al. 2012). Therefore, we infer that there is no obvious water loss  
207 during the high temperature BLS measurements in this study, which is also consistent  
208 with the previous study that demonstrated that the intrinsic hydrogen loss in hydrous  
209 pyrope occurs at temperatures of  $\geq 500$  °C (Bell et al. 1995).

210 The Brillouin system at 13-BMD beamline was equipped with a Coherent Verdi V2  
211 solid-state laser with a wavelength of 532 nm, a Perkin-Elmer photomultiplier  
212 detector (model: MP983), and a JRS six-pass tandem Fabry-Pérot interferometer (Lu  
213 et al. 2013; Yang et al. 2014). BLS spectra were collected in the symmetric forward  
214 scattering geometry with an external scattering angle of  $50^\circ$ , which was calibrated  
215 using the elastic moduli of standard silicate glass, distilled water, and single-crystal  
216 MgO (Ostwald et al. 1977; Polian et al. 2002; Sinogeikin and Bass 2000). The laser  
217 beam focused on the sample position was approximately 15  $\mu\text{m}$  in diameter. The  
218 acoustic velocities ( $V_P$  and  $V_S$ ) of our sample were derived from analysis of the  
219 measured Brillouin frequency shift as follows:

$$220 \quad V_{P,S} = \frac{\lambda_0 \Delta \nu_B}{2 \sin \frac{\theta}{2}} \quad (1)$$



## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

221 where  $V_{P,S}$  is the acoustic velocities,  $\lambda_0$  is the incident laser wavelength,  $\Delta\nu_B$  is the  
222 Brillouin frequency shift, and  $\theta$  is the external scattering angle.

### 223 RESULTS AND DATA ANALYSES

224 BLS and XRD spectra of single-crystal hydrous pyrope sample are collected up to  
225  $\sim 18.6$  GPa at room temperature in 2-3 GPa pressure interval and up to 700 K at room  
226 pressure in 100 K temperature interval. For all of the Brillouin spectra, one  
227 quasi-longitudinal and one quasi-transverse acoustic mode are observed. Typical  
228 Brillouin spectra at high pressure/high temperature conditions are shown in Figure 1.  
229 The measured frequency shifts are converted to velocities along the horizontal axis  
230 using equation (1). Most spectra show strong  $V_P$  and  $V_S$  peaks with high  
231 signal-to-noise ratios except for some crystallographic directions where  $V_P$  peaks are  
232 weakly observable (Fig. 1). Brillouin signals of neon pressure medium are also  
233 observed at pressures below  $\sim 8$  GPa, but they are too weak to be seen when the  
234 pressures are increased above 8 GPa. For each platelet at each given  $P$ - $T$  conditions,  
235 Brillouin spectra are collected in 19 different crystallographic directions from 0 to  $180^\circ$   
236 of the azimuthal angle at every  $10^\circ$  (Fig. 2). The variation in measured  $V_P$  and  $V_S$  as a  
237 function of azimuthal angle are not observed outside experimental uncertainties,  
238 indicating that our hydrous pyrope is almost elastically isotropic at ambient and high  
239 pressure/high temperature conditions (Fig. 2). Furthermore, both  $V_P$  and  $V_S$  of hydrous  
240 pyrope increase with increasing pressure, and decrease with increasing temperature.

241 Individual elastic moduli ( $C_{ij}$ ) of single-crystal hydrous pyrope at each given  
242 pressure/temperature conditions (Tables 1 and 2) are obtained by fitting the measured  
243 spatial dispersion (velocity vs. orientation) of  $V_P$  and  $V_S$  to Christoffel's equation  
244 using non-linear least square method (Every 1980):

$$245 \quad |C_{ijkl}n_jn_l - \rho V_{P,S}^2 \delta_{ik}| = 0 \quad (2)$$

246 where  $C_{ijkl}$  are the elastic constant in full suffix notation,  $n_j$  and  $n_l$  are the direction  
247 cosines of the phonon along the propagation direction,  $\rho$  is the density at each  
248 pressure/temperature condition,  $\delta_{ik}$  is the Kronecker delta function. The

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

249 root-mean-square (RMS) deviation of the fitting are about 20 m/s, indicating excellent  
250 agreement between measured and calculated sound velocities at ambient and high  
251 pressure/temperature conditions (Fig. 2). Previous studies also indicated that the  
252 single-crystal elastic moduli of pyrope could be calculated by averaging the measured  
253 acoustic velocities (e.g. Lu et al. 2013; Sinogeikin and Bass 2000). From Table S1,  
254 we notice that the single-crystal elastic moduli of hydrous pyrope derived from the  
255 non-linear least-squares fitting are indistinguishable within their uncertainties from  
256 those calculated values by averaging the measured acoustic velocities assuming that  
257 pyrope is elastically isotropic. All of the individual elastic moduli ( $C_{11}$ ,  $C_{12}$ , and  $C_{44}$ )  
258 for hydrous pyrope increase smoothly with increasing pressure, and decrease with  
259 increasing temperature (Fig. 3).

260 Using the derived individual elastic moduli ( $C_{11}$ ,  $C_{12}$ , and  $C_{44}$ ) of hydrous pyrope,  
261 the adiabatic bulk and shear moduli ( $K_S$  and  $G$ ) are calculated according to the  
262 Voigt-Reuss-Hill averages (Hill 1952). The aggregate adiabatic bulk ( $K_{S0}$ ) and shear  
263 moduli ( $G_0$ ) of hydrous pyrope at ambient conditions are 168.6(4) and 92.0(3) GPa,  
264 respectively. The pressure derivatives of elastic moduli at 300 K (Tables 3 and 4) are  
265 obtained by fitting the elastic moduli at high pressure using the third-order Eulerian  
266 finite-strain equation (Figs. 3a and 4a) (Birch 1978). The pressure derivatives of the  
267 individual ( $C_{ij}$ ) and aggregate ( $K_S$  and  $G$ ) elastic moduli at room temperature are  
268 derived to be  $(\partial C_{11}/\partial P)_T=6.2(1)$ ,  $(\partial C_{12}/\partial P)_T=3.7(1)$ ,  $(\partial C_{44}/\partial P)_T=1.5(1)$ ,  
269  $(\partial K_S/\partial P)_T=4.6(1)$ , and  $(\partial G/\partial P)_T=1.3(1)$ , respectively. Due to the limited temperature  
270 range for high-temperature data, a linear equation is applied to obtain the temperature  
271 derivatives of elastic moduli (Figs. 3b and 4b). The temperature derivative of  
272 individual and aggregate elastic moduli at ambient pressure (Tables 3 and 4) are  
273 derived to be  $(\partial C_{11}/\partial T)_P=-0.028(1)$  GPa/K,  $(\partial C_{12}/\partial T)_P=-0.009(1)$  GPa/K,  
274  $(\partial C_{44}/\partial T)_P=-0.006(1)$  GPa/K,  $(\partial K_S/\partial T)_P=-0.015(1)$  GPa/K, and  $(\partial G/\partial T)_P=-0.008(1)$   
275 GPa/K, respectively. The aggregate  $V_P$  and  $V_S$  of our hydrous pyrope at high  
276 pressure/temperature conditions (Fig. 5) are calculated using the following equations:

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

277 
$$V_P = \sqrt{\frac{K_S + \frac{4G}{3}}{\rho}} \quad (3)$$

278 
$$V_S = \sqrt{\frac{G}{\rho}} \quad (4)$$

279 **DISCUSSION**

280 **Hydrogen effect on the elasticity of pyrope at high *P-T* conditions**

281 In order to understand the effect of hydrogen on the elasticity of pyrope, we  
282 compare our results with literature values for pyrope obtained from BLS and  
283 ultrasonic interferometer measurements. Tables 3 and 4 show a complete list of  
284 individual ( $C_{ij}$ s) and aggregate ( $K_{S0}$  and  $G_0$ ) elastic moduli obtained in the present  
285 study for hydrous pyrope along with those previous studies of anhydrous pyrope.  
286 Compared to anhydrous pyrope (e.g. Sinogeikin and Bass 2000, 2002a) (Table 3), the  
287 addition of ~900 ppmw H<sub>2</sub>O in our pyrope sample has negligible effects on the  
288 individual elastic moduli  $C_{ij}$  values at ambient conditions within experimental  
289 uncertainties. Our aggregate bulk,  $K_{S0}$ , and shear moduli,  $G_0$ , at ambient conditions of  
290 hydrous pyrope are 168.6(4) and 92.0(3) GPa, respectively (Table 4). The presence of  
291 ~900 ppmw H<sub>2</sub>O in our hydrous pyrope also does not affect the values of  $K_{S0}$  and  $G_0$   
292 within experimental uncertainties compared to anhydrous pyrope (Table 4). This is  
293 consistent with the conclusion from the study by O'Neill et al. (1991), who deduced  
294 that there might have no discernable effect of hydrogen on the elastic properties of  
295 pyrope at ambient conditions, though the water solubility in their hydrous pyrope is  
296 significantly smaller (~180 ppmw H<sub>2</sub>O) than our hydrous pyrope (~900 ppmw H<sub>2</sub>O).

297 Our results also show that hydration has no visible effect on the pressure and  
298 temperature derivatives of  $C_{ij}$ s in pyrope within experimental uncertainties (Table 3).  
299 This is clearly different from the effect of composition (e.g. Fe and Ca) on the  
300 temperature derivatives of  $C_{ij}$ s in pyrope-rich garnet, where a distinctly larger  
301 temperature derivative of  $C_{12}$  and lower temperature derivative of  $C_{11}$  and  $C_{44}$  for  
302 (Fe,Ca)-bearing pyrope-rich garnet reported by Lu et al. (2013).

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

303 The  $(\partial K_S/\partial P)_T$  of our hydrous pyrope is 4.6 (Fig. 4 and Table 4), which is slightly  
304 higher than most results of anhydrous pyropes [ $(\partial K_S/\partial P)_T=4.1-4.51$ ] (Table 4), except  
305 a distinctly lower value ( $(\partial K_S/\partial P)_T=3.2$ ) reported by Conrad et al. (2000) and higher  
306 value ( $(\partial K_S/\partial P)_T=5.3$ ) reported by Chen et al. (1999). Moreover, the  $(\partial G/\partial P)_T$  of our  
307 hydrous pyrope ( $(\partial G/\partial P)_T=1.3$ ) is indistinguishable from most previous studies  
308 ( $(\partial G/\partial P)_T=1.3-1.5$ ) on anhydrous pyrope within experimental uncertainties, except for  
309 two slightly higher values ( $(\partial G/\partial P)_T=1.66$  and 1.7) reported from ultrasonic  
310 interferometry experiments by Gwanmesia et al. (2006) and Chantel et al. (2016),  
311 respectively. Furthermore, our derived  $(\partial K_S/\partial T)_P$  and  $(\partial G/\partial T)_P$  of hydrous pyrope are  
312 indistinguishable from previous BLS values for anhydrous pyrope within their  
313 uncertainties, but their absolute values appeared to be slightly lower than most of  
314 those from ultrasonic interferometry measurements except a consistent  $(\partial G/\partial T)_P$   
315 absolute value reported by Chantel et al. (2016) (Table 4). Therefore, we conclude  
316 that the presence of  $\sim 900$  ppmw H<sub>2</sub>O in our pyrope slightly enhances the  $(\partial K_S/\partial P)_T$ ,  
317 but does not distinctly affect the  $K_{S0}$ ,  $G_0$ ,  $(\partial G/\partial P)_T$ ,  $(\partial K_S/\partial T)_P$ , and  $(\partial G/\partial T)_P$  within  
318 their uncertainties.

319 **Hydrogen effect on the elastic anisotropy of pyrope at high  $P$ - $T$  conditions**

320 Elastic wave anisotropy is a critical feature of the upper mantle (e.g. Karato 1998).  
321 One advantage of using single-crystal samples in BLS is that we can obtain the full  
322 elastic moduli and put a constraint on the elastic anisotropy. The elastic anisotropy of  
323 minerals expresses the difference in stiffness of materials in different crystallographic  
324 directions, which can provide insights into seismic anisotropy and can be an indicator  
325 of the mechanical stability of materials (e.g. Hu et al. 2016; Sinogeikin and Bass  
326 2000). Thus, knowledge of elastic anisotropy for hydrous pyrope at high  $P$ - $T$  may  
327 shed light on understanding the seismic anisotropy within the Earth's upper mantle.

328 For the cubic pyrope, the elastic anisotropy factor ( $A$ ) can be expressed as (Karki et  
329 al. 1997; Sinogeikin and Bass 2000):

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

$$330 \quad A = \frac{2C_{44} + C_{12}}{C_{11}} - 1 \quad (5)$$

331 where  $A$  indicates the deviation from elastic isotropy, with  $A=0$  for an elastically  
332 isotropic material. Analysis of these parameters using our data show that the absolute  
333  $A$  values of our hydrous pyrope slightly decreases with increasing pressure and  
334 temperature, where  $A$  are -0.026 at ambient pressure, 0.001 at 18.53 GPa, and -0.019  
335 at 700 K. Moreover, our hydrous pyrope at ambient conditions has slightly higher  
336 absolute  $A$  value than anhydrous pyrope ( $A=-0.006$  to  $-0.008$ ) (e.g. Sinogeikin and  
337 Bass, 2000, 2002a; O'Neill et al. 1991). However, all these absolute  $A$  values are still  
338 pretty small and very close to zero. Thus, our results indicate that hydrogen does not  
339 have a significant effect on the elastic anisotropy of pyrope. Hydrous pyrope remains  
340 elastically isotropic at high pressure/high temperature conditions compared to the  
341 other (olivine, orthopyroxene, and clinopyroxene) major minerals in the upper mantle  
342 (e.g. Mao et al. 2015; Sang et al. 2014; Zhang et al. 2016). Therefore, pyrope may not  
343 have a significant contribution to seismic anisotropy in the upper mantle, at least  
344 when its water content is less than 900 ppmw.

### 345 **IMPLICATION**

#### 346 **Hydrogen effect on the velocity profiles of pyrope in the Earth's upper mantle**

347 The NAMs in the Earth's deep mantle may serve as a large internal reservoir of  
348 water and are important for understanding the evolution and dynamics of Earth's  
349 interior (e.g. Bell and Rossman 1992a; Beran and Libowitzky 2006; Ohtani 2005,  
350 2015). Hydration of NAMs has been proposed to correlate with the observed velocity  
351 anomalies in the Earth's mantle (e.g. Nolet and Zielhuis 1994; Ohtani 2005; Song et  
352 al. 2004; van der Meijde et al. 2003). With the obtained elastic moduli of hydrous  
353 pyrope at high  $P$ - $T$  conditions in this study, we evaluate the effect of hydration on the  
354 sound velocities of pyrope at upper mantle conditions.

355 The presence of ~900 ppmw water in pyrope lowers its  $V_P$  and  $V_S$  by ~0.7% at  
356 ambient conditions (Sinogeikin and Bass 2000). Furthermore, for a better

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

357 understanding of the hydrogen influence on the velocity behavior of pyrope, we have  
358 modeled the velocity profiles of hydrous pyrope along the upper mantle geotherm  
359 (Katsura et al. 2010) and a cold subducted slabs geotherm (Eberle et al. 2002) using  
360 the updated high- $P/T$  elasticity results. Our modeling here is limited to the  
361 upper-mantle region ranging from 200 km to 400 km depth because of the much more  
362 complex mineralogical, geochemical, and seismic heterogeneities above 200 km  
363 depth (e.g. Jordan 1975; Grand and Helmberger 1984). The modeled results are then  
364 compared with the velocity profiles of anhydrous pyrope (Sinogeikin and Bass 2000,  
365 2002a) and (Fe, Ca)-bearing pyrope-rich garnet (Lu et al. 2013). Briefly, the  
366 third-order Eulerian finite-strain equation and the third-order Birch-Murnaghan  
367 equation of state (Birch 1978) are used to obtain the  $K_S$ ,  $G$ ,  $V_P$  and  $V_S$  of relevant  
368 minerals by extrapolating the experimentally-derived elastic moduli and their  $P$ - $T$   
369 derivatives to relevant  $P$ - $T$  conditions (see Lu et al. 2013 for details). By allowing  
370 elastic parameters to vary within their plausible ranges, the uncertainties ( $\pm 1\sigma$ ) of  
371 extrapolation results can also be estimated.

372 Figure 6 shows the calculated velocity-depth relationships of hydrous pyrope along  
373 with those of anhydrous phase. Because of larger pressure derivative of  $K_S$  and similar  
374 temperature derivative of  $K_S$ , the  $V_P$  of hydrous pyrope increases more rapidly with  
375 depth than that of anhydrous pyrope. Moreover, the  $V_P$  of hydrous pyrope crosses and  
376 exceeds that of anhydrous phase at  $\sim 200$  km and  $\sim 270$  km depth along the upper  
377 mantle geotherm and the cold subducted slabs geotherm, respectively. However,  
378 considering the error bars presented in Fig. 6, the  $V_P$  profiles are indistinguishable  
379 between hydrous and anhydrous pyrope at 200-400 km depth. Similarly, due to the  
380 small effects of hydrogen on the pressure derivative of  $G$ , the difference in the  $V_S$   
381 between hydrous and anhydrous pyrope is also within the uncertainties over the  
382 200-400 km depth.

383 On the other hand, hydrogen can enhance the anelasticity (e.g. Karato 1995) and  
384 may further change the  $V_P$  and  $V_S$ . Combining the anelastic effect, the change of  $V_P$

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

385 and  $V_S$  associated with  $\sim 900$  ppmw H<sub>2</sub>O in pyrope at the Earth's upper mantle may be  
386 greater than that observed here. However, although up to several hundred ppmw H<sub>2</sub>O  
387 have been found in some natural garnets (e.g. Aines and Rossman 1984a, 1984b; Li H  
388 Y et al. 2018), most of the mantle-derived garnets typically contain  $<100$  ppmw H<sub>2</sub>O  
389 (e.g. Beran and Libowitzky 2006; Ohtani 2015). Combined with the limited effect of  
390  $\sim 900$  ppmw H<sub>2</sub>O on the velocities of pyrope, we thus infer that hydrogen has no  
391 significant effect on the velocity profiles of pyrope at upper mantle conditions.  
392 Nevertheless, compared to the effect of hydrogen on the velocities of pyrope, the  
393 effect of compositions (e.g. Fe and Ca) is significant. Accordingly, the velocity  
394 reduction produced by the effect of Fe and Ca is  $\sim 2\text{-}3\%$  either along the upper mantle  
395 geotherm or along the cold subducted slabs geotherm (Fig. 6). Therefore, the  
396 elasticity studies of hydrous (Fe, Ca)-bearing pyrope-rich garnet at high  $P$ - $T$   
397 conditions are needed to provide a more comprehensive understanding of the coupled  
398 effect of compositions (e.g. Fe and Ca) and hydration on the elasticity and velocity  
399 profiles of garnet and then the Earth's upper mantle.

### 400 **Hydrogen effect on the $V_P/V_S$ ratio of pyrope in the Earth's upper mantle**

401 The  $V_P/V_S$  ratio has been proposed as one of the possible indicators to determine the  
402 composition in the deep Earth (e.g. Anderson and Bass 1984; Duan et al. 2018; Li and  
403 Neuville 2010; Mao et al. 2010), such as the silica content of continental crust  
404 (Christensen 1996). It has been widely used to infer the thermal and compositional  
405 state of the upper mantle (e.g. Afonso et al. 2010; Chou et al. 2009; Lee 2003; Niu et  
406 al. 2004; Speziale et al. 2005). Here, we have investigated the effect of hydration on  
407 the  $V_P/V_S$  ratio of pyrope. The  $V_P/V_S$  ratio of the hydrous pyrope at ambient conditions  
408 is 1.78, which is the same with the anhydrous pyrope (1.78) (Sinogeikin and Bass  
409 2000). The  $V_P/V_S$  ratio increases with pressure at an average rate of  $5.03 \times 10^{-3} \text{ GPa}^{-1}$ ,  
410 but it remains constant with increasing temperature from 300 K to 700 K. At the depth  
411 of 400 km, the  $V_P/V_S$  ratio of the hydrous pyrope increases to 1.86 along the upper  
412 mantle geotherm and to 1.85 along the cold subducted slabs geotherm, which are  $\sim 0.5\%$

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

413 higher than that of the anhydrous phase. A similar increase in the  $V_P/V_S$  ratio caused  
414 by hydration was observed for ringwoodite (Jacobsen and Smyth 2006; Sinogeikin et  
415 al. 2003). However, this contrasts with the behavior of olivine for which a  $\sim 0.7\%$   
416 decreased in the  $V_P/V_S$  ratio was observed in the hydrous olivine relative to anhydrous  
417 phase (Mao et al. 2010; Zha et al. 1996). Figure 7 also shows a comparison of the  
418  $V_P/V_S$  ratio for hydrous and anhydrous pyrope with the (Fe,Ca)-bearing pyrope-rich  
419 garnet. We notice although all garnets exhibit the increased  $V_P/V_S$  ratio with  
420 increasing depths, the hydrous pyrope has the highest value throughout the upper  
421 mantle depths. However, considering the uncertainties of the  $V_P/V_S$  ratio presented in  
422 Fig. 7, the variation of the  $V_P/V_S$  ratio among these garnet samples should be limited  
423 at 200-400 km depth. This confirms the results of the previous study, which indicated  
424 that the variation of mineral composition has only a weak effect on the  $V_P/V_S$  ratio of  
425 the upper mantle (Duan et al. 2018). Finally, we infer that the hydrogen has also no  
426 significant effect on the  $V_P/V_S$  ratio of pyrope at upper mantle conditions, especially  
427 for the limited hydration level ( $<100$  ppmw  $H_2O$ ) of mantle-derived garnets.

### 428 **Acknowledgments**

429 We would like to thank two anonymous reviewers for their thorough and helpful comments and  
430 Prof. Jennifer Kung for handling this paper. We also thank Z. Mao for providing the Igor fitting  
431 code. D. W. Fan acknowledges financial support from the National Natural Science Foundation of  
432 China (41772043), the Joint Research Fund in Huge Scientific Equipment (U1632112) under the  
433 cooperative agreement between NSFC and CAS, CAS "Light of West China" Program (Dawei  
434 Fan, 2017), and Youth Innovation Promotion Association CAS (Dawei Fan, 2018434). J. G. Xu  
435 acknowledges financial support from the National Natural Science Foundation of China  
436 (41802043), and China Postdoctoral Science Foundation (Grant No. 2018M631104). This work  
437 was performed at GeoSoilEnviroCARS (The University of Chicago, Sector 13), Advanced Photon  
438 Source (APS), Argonne National Laboratory. GeoSoilEnviroCARS is supported by the National  
439 Science Foundation (EAR-0622171) and the Department of Energy (DE-FG02-94ER14466) under  
440 Contract No. DE-AC02-06CH11357. This research used resources at the Advanced Photon



FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

441 Source, a U.S. Department of Energy (DOE) Office of Science User Facility operated for the DOE  
442 Office of Science by Argonne National Laboratory under Contract No. DE-AC02-06CH11357.

443 **REFERENCES CITED**

444 Ackermann, L., Cemič, L, and Langer, K. (1983) Hydrogarnet substitution in pyrope: a possible  
445 location for “water” in the mantle. *Earth and Planetary Science Letters*, 62, 208-214.

446 Afonso, J.C., Ranalli, G., Fernández, M., Griffin, W.L., O’Reilly, S.Y., and Faul, U. (2010) On  
447 the  $V_P/V_S$ -Mg# correlation in mantle peridotites: Implications for the identification of thermal  
448 and compositional anomalies in the upper mantle. *Earth and Planetary Science Letters*, 289,  
449 606-618.

450 Aines, R., and Rossman, G.R. (1984a) The hydrous component in garnets: pyralspites. *American*  
451 *Mineralogist*, 69, 1116-1126.

452 Aines, R., and Rossman, G.R. (1984b) Water content of mantle garnets. *Geology*, 12, 720-723.

453 Anderson, D.L. (1989) Composition of the Earth. *Science*, 243, 367-370.

454 Anderson, D.L., and Bass, J.D. (1984) Mineralogy and composition of the upper mantle.  
455 *Geophysical Research Letters*, 11, 637-640.

456 Bass, J.D., and Anderson, D.L. (1984) Composition of the upper mantle: geophysical tests of two  
457 petrological models. *Geophysical Research Letters*, 11, 229-232.

458 Bass, J.D., and Zhang, J.S. (2015) Theory and practice: techniques for measuring high-P-T  
459 elasticity. *Treatise on Geophysics (Second Edition)*, 2, 293-312.

460 Bass, J.D., Sinogeikin, S.V., and Li, B. (2008) Elastic properties of minerals: A key for  
461 understanding the composition and temperature of Earth’s interior. *Elements*, 4, 165-170.

462 Bell, D.R., Ihinger, P.D., and Rossman, G.R. (1995) Quantitative analysis of trace OH in garnet  
463 and pyroxenes. *American Mineralogist*, 80, 465-474.

464 Bell, D.R., and Rossman, G.R. (1992a) Water in Earth’s mantle: The role of nominally anhydrous  
465 minerals. *Science*, 255, 1391-1397.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 466 Bell, D.R., and Rossman, G.R. (1992b) The distribution of hydroxyl in garnets from the  
467 subcontinental mantle of southern Africa. *Contributions to Mineralogy and Petrology*, 111,  
468 161-178.
- 469 Beran, A., and Libowitzky, E. (2006) Water in natural mantle minerals II: olivine, garnet and  
470 accessory minerals. *Reviews in Mineralogy and Geochemistry*, 62, 169-191.
- 471 Bina, C.R. (2013) Mineralogy: Garnet goes hungry. *Nature Geoscience*, 6, 335-336.
- 472 Birch, F. (1978) Finite strain isotherm and velocities for single-crystal and polycrystalline NaCl at  
473 high pressure and 300 K. *Journal of Geophysical Research*, 83, 1257-1268.
- 474 Bolfan-Casanova, N., Keppler, H., and Rubie, D.C. (2000) Water partitioning between nominally  
475 anhydrous minerals in the MgO-SiO<sub>2</sub>-H<sub>2</sub>O system up to 24 GPa: implications for the  
476 distribution of water in the Earth's mantle. *Earth and Planetary Science Letters*, 182, 209-221.
- 477 Chantel, J., Manthilake, G.M., Frost, D.J., Beyer, C., Ballaran, T.B., Jing, Z.C., Wang, Y.B. (2016)  
478 Elastic wave velocities in polycrystalline Mg<sub>3</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>-pyrope garnet to 24 GPa and 1300 K.  
479 *American Mineralogist*, 101, 991-997.
- 480 Chen, G.L., Miletich, R., Mueller, K., and Spetzler, H.A. (1997) Shear and compressional mode  
481 measurements with GHz ultrasonic interferometry and velocity-composition systematics for the  
482 pyrope-almandine solid solution series. *Physics of the Earth and Planetary Interiors*, 99,  
483 273-287.
- 484 Chen, G.L., Cooke, J.A.Jr., Gwanmesia, G.D., Liebermann, R.C. (1999) Elastic wave velocities of  
485 Mg<sub>3</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>-pyrope garnet to 10 GPa. *American Mineralogist*, 84, 384-388.
- 486 Christensen, N.I. (1996) Poisson's ratio and crustal seismology. *Journal of Geophysical Research*,  
487 101, 3139-3156.
- 488 Conrad, P.G., Zha, C.S., Mao, H.K., and Hemley, R.J. (1999) The high-pressure, single-crystal  
489 elasticity of pyrope, grossular, and andradite. *American Mineralogist*, 84, 374-383.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 490 Dai, L.D., Li, H.P., Hu, H.Y., Shan, S.M., Jiang, J.J., and Hui, K.S. (2012) The effect of chemical  
491 composition and oxygen fugacity on the electrical conductivity of dry and hydrous garnet at  
492 high temperatures and pressures. *Contributions to Mineralogy and Petrology*, 163, 689-700.
- 493 Du, W., Clark, S.M., Walker, D. (2015) Thermo-compression of pyrope-grossular garnet solid  
494 solutions: non-linear compositional dependence. *American Mineralogist*, 100, 215-222.
- 495 Duan, Y.F., Li, X.Y., Sun, N.Y., Ni, H.W., Tkachev, S.N., and Mao, Z. (2018) Single-crystal  
496 elasticity of  $\text{MgAl}_2\text{O}_4$ -spinel up to 10.9 GPa and 1000 K: Implication for the velocity structure  
497 of the top upper mantle. *Earth and Planetary Science Letters*, 481, 41-47.
- 498 Duffy, T.S., and Anderson, D.L. (1989) Seismic velocities in mantle minerals and the mineralogy  
499 of the upper mantle. *Journal of Geophysical Research*, 94, 1895-1912.
- 500 Eberle, M.A., Grasset, O., and Sotin, C. (2002) A numerical study of the interaction between the  
501 mantle wedge, subducting slab, and overriding plate. *Physics of the Earth and Planetary  
502 Interiors*, 134, 191-202.
- 503 Every, A. (1980) General closed-form expressions for acoustic waves in elastically anisotropic  
504 solids. *Physical Review B*, 22, 1746-1760.
- 505 Fan, D.W., Fu, S.Y., Yang, J., Tkachev, S.N., Prakapenka, V.B., and Lin, J.F. (2019) Elasticity of  
506 single-crystal periclase at high pressure and temperature: the effect of iron on the elasticity and  
507 seismic parameters of ferropericlase in the lower mantle. *American Mineralogist*, 104, 262-275.
- 508 Fan, D.W., Kuang, Y.Q., Xu, J.G., Li, B., Zhou, W.G., and Xie, H.S. (2017a) Thermoelastic  
509 properties of grossular–andradite solid solution at high pressures and temperatures. *Physics and  
510 Chemistry of Minerals*, 44, 137-147.
- 511 Fan, D.W., Lu, C., Xu, J.G., Yan, B.M., Yang, B., and Chen, J.H. (2017b) Effects of water on  
512 P-V-T equation of state of pyrope. *Physics of the Earth and Planetary Interiors*, 267, 9-18.
- 513 Fan, D.W., Ma, M.N., Wei, S.Y., Chen, Z.Q., and Xie, H.S. (2013) High pressure elastic behavior  
514 of synthetic  $\text{Mg}_3\text{Y}_2(\text{SiO}_4)_3$  garnet up to 9GPa. *Advances in Materials Science and Engineering*,  
515 2013, 502702.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 516 Fan, D.W., Mao, Z., Yang, and J., Lin, J.F. (2015a) Determination of the full elastic tensor of  
517 single crystals using shear wave velocities by Brillouin spectroscopy. American Mineralogist,  
518 100, 2590-2601.
- 519 Fan, D.W., Wei, S.Y., Liu, J., Li, Y.C., and Xie, H.S. (2011) High pressure X-ray diffraction study  
520 of a grossular-andradite solid solution and the bulk modulus variation along this solid solution.  
521 Chinese Physics Letters, 28, 076101.
- 522 Fan, D.W., Xu, J.G., Ma, M.N., Liu, J., and Xie, H.S. (2015b)  $P$ - $V$ - $T$  equation of state of  
523 spessartine-almandine solid solution measured using a diamond anvil cell and in situ  
524 synchrotron X-ray diffraction. Physics and Chemistry of Minerals, 42, 63-72.
- 525 Fan, D.W., Xu, J.G., Ma, M.N., Wei, S.Y., Zhang, B., Liu, J., and Xie, H.S. (2015c)  $P$ - $V$ - $T$   
526 equation of state of  $\text{Ca}_3\text{Cr}_2\text{Si}_3\text{O}_{12}$  uvarovite garnet by using a diamond-anvil cell and in-situ  
527 synchrotron X-ray diffraction. American Mineralogist, 100, 588-597.
- 528 Fan, D.W., Zhou, W.G., Liu, C.Q., Liu, Y.G., Wan, F., Xing, Y.S., Liu, J., Bai, L.G., and Xie, H.S.  
529 (2009) The thermal equation of state of  $(\text{Fe}_{0.86}\text{Mg}_{0.07}\text{Mn}_{0.07})_3\text{Al}_2\text{Si}_3\text{O}_{12}$  almandine.  
530 Mineralogical Magazine, 73, 95-102.
- 531 Frost, D.J. (2008) The upper mantle and transition zone. Elements, 4, 171-176.
- 532 Geiger, C.A., Langer, K., Bell, D.R., Rossman, G.R., and Winkler, B. (1991) The hydroxide  
533 component in synthetic pyrope. American Mineralogist, 76, 49-59.
- 534 Grand, S.P., and Helmberger, D.V. (1984) Upper mantle shear structure of North America.  
535 Geophysical Journal International, 76, 399-438.
- 536 Gwanmesia, G.D., Jackson, I., and Liebermann, R.C. (2007) In search of the mixed derivative  
537  $\partial^2 M / \partial P \partial T$  ( $M=G, K$ ): joint analysis of ultrasonic data for polycrystalline pyrope from gas- and  
538 solid-medium apparatus. Physics and Chemistry of Minerals, 34, 85-93.
- 539 Gwanmesia, G.D., Zhang, J.Z., Darling, K., Kung, J., Li, B.S., Wang, L.P., Neuville, D.,  
540 Liebermann, R.C. (2006) Elasticity of polycrystalline pyrope ( $\text{Mg}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ ) to 9 GPa and  
541 1000 °C. Physics of the Earth and Planetary Interiors, 155, 179-190.

## FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 542 Herzberg C., and Gasparik T. (1991) Garnet and pyroxenes in the mantle: A test of the majorite  
543 fractionation hypothesis. *Journal of Geophysical Research*, 96, 16263-16274.
- 544 Hill, R. (1952) The elastic behaviour of a crystalline aggregate. *Proceedings of the Physical*  
545 *Society-Section A*, 65, 349-354.
- 546 Hirschmann, M. (2006) Water, melting, and the deep earth H<sub>2</sub>O cycle. *Annual Review of Earth*  
547 *and Planetary Sciences*, 34, 629-653.
- 548 Hirschmann, M., and Kohlstedt, D. (2012) Water in Earth's mantle. *Physics Today*, 65, 40-45.
- 549 Holl, C.M., Smyth, J.R., Jacobsen, S.D., Frost, D.J. (2008) Effects of hydration on the structure  
550 and compressibility of wadsleyite,  $\beta$ -(Mg<sub>2</sub>SiO<sub>4</sub>). *American Mineralogist*, 93, 598-607.
- 551 Hu, Y., Wu, Z.Q., Dera, P.K., and Bina, C.R. (2016) Thermodynamic and elastic properties of  
552 pyrope at high pressure and high temperature by first-principles calculations. *Journal of*  
553 *Geophysical Research*, 121, 6462-6476.
- 554 Ingrin, J. and Skogby, H. (2000) Hydrogen in nominally anhydrous upper-mantle minerals:  
555 concentration levels and implications. *European Journal of Mineralogy*, 12, 543-570.
- 556 Inoue, T., Weidner, D.J., Northrup, P.A., and Parise, J.B. (1998) Elastic properties of hydrous  
557 ringwoodite ( $\gamma$ -phase) in Mg<sub>2</sub>SiO<sub>4</sub>. *Earth and Planetary Science Letters*, 160, 107-113.
- 558 Ita, J., and Stixrude, L. (1992) Petrology, elasticity, and composition of the mantle transition zone.  
559 *Journal of Geophysical Research*, 97, 6849-6866.
- 560 Jacobsen, S.D., Jiang, F., Mao, Z., Duffy, T.S., Smyth, J.R., Holl, C.M., and Frost, D.J. (2008)  
561 Effects of hydration on the elastic properties of olivine. *Geophysical Research Letters*, 35,  
562 L14303.
- 563 Jacobsen, S.D., and Smyth, J.R. (2006) Effect of water on the sound velocities of ringwoodite in  
564 the transition zone. In: Jacobsen, S.D., van der Lee, S. (Eds.), *Earth's deep water cycle*.  
565 American Geophysical Union, Washington, D.C., pp. 131-145.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 566 Jacobsen, S.D., Smyth, J.R., Spetzler, H.A., Holl, C.M., and Frost, D.J. (2004) Sound velocities  
567 and elastic constants of iron-bearing hydrous ringwoodite. *Physics of the Earth and Planetary*  
568 *Interiors*, 143-144, 47-56.
- 569 Jordan, T.H. (1975) Lateral heterogeneity and mantle dynamics. *Nature* 257, 745-750.
- 570 Kantor, I., Prakapenka, V., Kantor, A., Dera, P., Kurnosov, A., Sinogeikin, S., Dubrovinskaia, N.,  
571 and Dubrovinsky, L. (2012) BX90: A new diamond anvil cell design for X-ray diffraction and  
572 optical measurements. *Review of Scientific Instruments*, 83, 125102.
- 573 Karato, S. (1995) Effects of water on seismic wave velocities in the upper mantle. *Proceedings of*  
574 *the Japan Academy*, 71, 61-66.
- 575 Karato, S. (1998) Seismic anisotropy in the deep mantle, boundary layers and the geometry of  
576 mantle convection. *Pure and Applied Geophysics*, 151, 565-587.
- 577 Karki, B.B., Stixrude, L., Clark, S.L., Warren, M.C., Ackland, G.J., and Crain, J. (1997) Structure  
578 and elasticity of MgO at high pressure. *American Mineralogist*, 82, 51-60.
- 579 Katsura, T., Yoneda, A., Yamazaki, D., Yoshino, T., Ito, E. (2010) Adiabatic temperature profile  
580 in the mantle. *Physics of the Earth and Planetary Interiors*, 183, 212-218.
- 581 Kimura, M., Sugiura, N., Mikouchi, T., Hirajima, T., Hiyagon, H., and Takehana, Y. (2013)  
582 Eclogitic clasts with omphacite and pyrope-rich garnet in the NWA 801 CR2 chondrite.  
583 *American Mineralogist*, 98, 387-393.
- 584 Lee, C.T.A. (2003) Compositional variation of density and seismic velocities in natural peridotites  
585 at STP conditions: implications for seismic imaging of compositional heterogeneities in the  
586 upper mantle. *Journal of Geophysical Research*, 108, B92441.
- 587 Leger, J.M., Redon, A.M., and Chateau, C. (1990) Compressions of synthetic pyrope, spessartine  
588 and uvarovite garnets up to 25 GPa. *Physics and Chemistry of Minerals*, 17, 161-167.
- 589 Leitner, B.J., Weidner, D.J., Liebermann, R.C. (1980) Elasticity of single crystal pyrope and  
590 implications for garnet solid solution series. *Physics of the Earth and Planetary Interiors*, 22,  
591 111-121.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 592 Levien, L., Prewitt, C.T., and Weidner, D.J. (1979) Compression of pyrope. American  
593 Mineralogist, 64, 805-808.
- 594 Li, B.S., and Neuville, D.R. (2010) Elasticity of diopside to 8 GPa and 1073 K and implications  
595 for the upper mantle. Physics of the Earth and Planetary Interiors, 183, 398-403.
- 596 Li, B.W., Ge, J.H., and Zhang, B.H. (2018) Diffusion in garnet: a review. Acta Geochimica, 37,  
597 19-31.
- 598 Li, H.Y., Chen, R.X., Zheng, Y.F., and Hu, Z.C. (2018) Water in garnet pyroxenite from the Sulu  
599 orogen: Implications for crust-mantle interaction in continental subduction zone. Chemical  
600 Geology, 478, 18-38.
- 601 Li, L., Weidner, D.J., Brodholt, J., Alfè, D., and Price, G.D. (2011) Ab initio molecular dynamic  
602 simulation on the elasticity of Mg<sub>3</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>12</sub> pyrope. Journal of Earth Science, 22, 169-175.
- 603 Liu, L.G. (1980) The mineralogy of an eclogitic Earth mantle. Physics of the Earth and Planetary  
604 Interiors, 23, 262-267.
- 605 Lu, R., and Keppler, H. (1997) Water solubility in pyrope to 100 kbar. Contributions to  
606 Mineralogy and Petrology, 129, 35-42.
- 607 Lu, C., Mao, Z., Lin, J.F., Zhuravlev, K.K., Tkachev, S.N., and Prakapenka, V.B. (2013) Elasticity  
608 of single-crystal iron-bearing pyrope up to 20 GPa and 750 K. Earth and Planetary Science  
609 Letters, 361, 134-142.
- 610 Mao, H.K., Xu, J., and Bell, P.M. (1986) Calibration of the ruby pressure gauge to 800 kbar under  
611 quasi-hydrostatic conditions. Journal of Geophysical Research, 91, 4673-4676.
- 612 Mao, Z., Fan, D.W., Lin, J.F., Yang, J., Tkachev, S.N., Zhuravlev, K., and Prakapenka, V.B.  
613 (2015) Elasticity of single-crystal olivine at high pressures and temperatures. Earth and  
614 Planetary Science Letters, 426, 204-215.
- 615 Mao, Z., Jacobsen, S.D., Frost, D.J., McCammon, C.A., Hauri, E.H., and Duffy, T.S. (2011)  
616 Effect of hydration on the single-crystal elasticity of Fe-wadsleyite to 12 GPa. American  
617 Mineralogist, 96, 1606-1612.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 618 Mao, Z., Jacobsen, S.D., Jiang, F.M., Smyth, J.R., Holl, C.M., and Duffy, T.S. (2008) Elasticity of  
619 hydrous wadsleyite to 12 GPa: implications for Earth's transition zone. *Geophysical Research*  
620 *Letters*, 35, L21305.
- 621 Mao, Z., Jacobsen, S.D., Jiang, F.M., Smyth, J.R., Holl, C.M., Frost, D.J., and Duffy, T.S. (2010)  
622 Velocity crossover between hydrous and anhydrous forsterite at high pressures. *Earth and*  
623 *Planetary Science Letters*, 293, 250-258.
- 624 Mao, Z., Lin, J.F., Jacobsen, S.D., Duffy, T.S., Chang, Y.Y., Smyth, J.R., Frost, D.J., Hauri, E.H.,  
625 and Prakapenka, V.B. (2012) Sound velocities of hydrous ringwoodite to 16 GPa and 673 K.  
626 *Earth and Planetary Science Letters*, 331-332, 112-119.
- 627 McDonough, W.F., and Sun, S.S. (1995) The composition of the Earth. *Chemical Geology*, 120,  
628 223-253.
- 629 Mookherjee, M., and Karato, S. (2010) Solubility of water in pyrope-rich garnet at high pressures  
630 and temperature. *Geophysical Research Letters*, 37, L03310.
- 631 Murakami, M., Sinogeikin, S.V., Hellwig, H., Bass, J.D., and Li, J. (2007) Sound velocity of  
632 MgSiO<sub>3</sub> perovskite to Mbar pressure. *Earth and Planetary Science Letters*, 256, 47-54.
- 633 Niu, F., Levander, A., Cooper, C.M., Lee, C.T.A., Lenardic, A., James, D.E. (2004) Seismic  
634 constraints on the depth and composition of the mantle keel beneath the Kaapvaal craton. *Earth*  
635 *and Planetary Science Letters*, 224, 337-346.
- 636 Nolet, G., Zielhuis, A. (1994) Low S velocities under the Tornquist-Teisseyre zone: evidence for  
637 water injection into the transition zone by subduction. *Geophysical Research Letters*, 99,  
638 15813-15820.
- 639 Ohtani, E. (2005) Water in the mantle. *Elements*, 1, 25-30.
- 640 Ohtani, E. (2015) Hydrous minerals and the storage of water in the deep mantle. *Chemical*  
641 *Geology*, 418, 6-15.
- 642 O'Neill, B., Bass, J.D., Rossman, G.R., Geiger, C.A., and Langer, K. (1991) Elastic properties of  
643 pyrope. *Physics and Chemistry of Minerals*, 17, 617-621.



FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 644 Ostwald, J., Pazold, W., and Weis, O. (1977) High-resolution Brillouin spectroscopy of water.  
645 Applied Physics, 13, 351-356.
- 646 Poli, S., and Schmidt, M.W. (2002) Petrology of subducted slabs. Annual Review of Earth and  
647 Planetary Sciences, 30, 207-235.
- 648 Polian, A., Vo-Thanh, D., and Richet, P. (2002) Elastic properties of  $\alpha$ -SiO<sub>2</sub> up to 2300 K from  
649 Brillouin scattering measurements. Europhysics Letters, 57, 375-381.
- 650 Rickwood, P.C., Mathias, M., Siebert, J.C. (1968) A study of garnets from eclogite and peridotite  
651 xenoliths found in kimberlite. Contributions to Mineralogy and Petrology, 19, 271-301.
- 652 Ringwood, A.E. (1975) Composition and petrology of the Earth's mantle. McGraw-Hill, New  
653 York.
- 654 Ringwood, A.E. (1982) Phase transformations and differentiation in subducted lithosphere:  
655 implications for mantle dynamics, basalt petrogenesis, and crustal evolution. The Journal of  
656 Geology, 90, 611-643.
- 657 Ringwood, A.E. (1991) Phase transformations and their bearing on the constitution and dynamics  
658 of the mantle. Geochimica et Cosmochimica Acta, 55, 2083-2110.
- 659 Rivers, M., Prakapenka, V.B., Kubo, A., Pullins, C., Holl, C.M., and Jacobsen, S.D. (2008) The  
660 COMPRES/GSECARS gas-loading system for diamond anvil cells at the Advanced Photon  
661 Source. High Pressure Research, 28, 273-292.
- 662 Rossman, G.R., Beran, A., and Langer, K. (1989) The hydrous component of pyrope from the  
663 Dora Maira Massif, Western Alps. Physics and Chemistry of Minerals, 1, 151-154.
- 664 Sang, L.Q., and Bass, J.D. (2014) Single-crystal elasticity of diopside to 14 GPa by Brillouin  
665 scattering. Physics of the Earth and Planetary Interiors, 228, 75-79.
- 666 Sato, Y., Akaogi, M., and Akimoto, S. (1978) Hydrostatic compression of the synthetic garnets  
667 pyrope and almandine. Journal of Geophysical Research, 83, 335-338.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 668 Sinogeikin, S.V., and Bass, J.D. (2000) Single-crystal elasticity of pyrope and MgO to 20 GPa by  
669 Brillouin scattering in the diamond cell. *Physics of the Earth and Planetary Interiors*, 120,  
670 43-62.
- 671 Sinogeikin, S.V., and Bass, J.D. (2002) Elasticity of pyrope and majorite-pyrope solid solutions to  
672 high temperatures. *Earth and Planetary Science Letters*, 203, 549-555.
- 673 Sinogeikin, S.V., Bass, J.D., and Katsura, T. (2003) Single-crystal elasticity of ringwoodite to  
674 high pressures and high temperatures: implications for 520 km seismic discontinuity. *Physics of*  
675 *the Earth and Planetary Interiors*, 136, 41-66.
- 676 Sinogeikin, S.V., Bass, J.D., Prakapenka, V., Lakshtanov, D., Shen, G., Sanchez-Valle, C., and  
677 Rivers, M. (2006) Brillouin spectrometer interfaced with synchrotron radiation for simultaneous  
678 X-ray density and acoustic velocity measurements. *Review of Scientific Instruments*, 77,  
679 103905.
- 680 Skogby, H. (2006) Water in natural mantle minerals I: Pyroxenes. *Reviews in Mineralogy and*  
681 *Geochemistry*, 62, 155-167.
- 682 Smyth, J.R. (1987)  $\beta$ -Mg<sub>2</sub>SiO<sub>4</sub>: A potential host for water in the mantle? *American Mineralogist*,  
683 72, 1051-1055.
- 684 Smyth, J.R., Holl, C.M., Frost, D.J., Jacobsen, S.D., Langenhorst, F., McCammon, C.A. (2003)  
685 Structural systematics of hydrous ringwoodite and water in Earth's interior. *American*  
686 *Mineralogist*, 88, 1402-1407.
- 687 Smyth, J.R. and Jacobsen, S.D. (2006) Nominally anhydrous minerals and Earth's deep water  
688 cycle. In Jacobsen, S.D., and van der Lee, S. (Eds.) *Earth's Deep Water Cycle*. Geophysical  
689 *Monograph Series*, vol. 168, pp. 1-11, American Geophysical Union, Washington, D.C.
- 690 Song, T.A., Helmberger, D.V., and Grand, S.P. (2004) Low-velocity zone atop the 410-km  
691 seismic discontinuity in the northwestern United States. *Nature*, 427, 530-533.
- 692 Speziale, S., Jiang, F., and Duffy, T.S. (2005) Compositional dependence of the elastic wave  
693 velocities of mantle minerals: implications for seismic properties of mantle rocks. In: van der

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 694 Hilst, et al. (Eds.) Earth's deep mantle: structure, composition, and evolution. Geophysical  
695 Monograph Series, vol. 160, pp. 301-320, American Geophysical Union, Washington, D.C.
- 696 Speziale, S. Marquardt, H., Duffy, T.S. (2014) Brillouin Scattering and its Application in  
697 Geosciences. *Reviews in Mineralogy & Geochemistry*, 78, 543-603.
- 698 Sumino, Y., and Nishizawa, O. (1978) Temperature variation of elastic constants of  
699 pyrope-almandine garnets. *Journal of Physics of the Earth*, 26, 239-252.
- 700 Suzuki, I., and Anderson, O.L. (1983) Elasticity and thermal expansion of a natural garnet up to  
701 1000 K. *Journal of Physics of the Earth*, 31, 125-138.
- 702 Thieblot, L., Roux, J., Richet, P. (1998) High-temperature thermal expansion and decompositions  
703 of garnets. *European Journal of Mineralogy*, 10, 7-15.
- 704 van der Meijde, M., Marone, F., Giardini, D., van der Lee, S. (2003) Seismic evidence for water  
705 deep in Earth's upper mantle. *Science*, 300, 1556-1558.
- 706 Wang, J., Sinogeikin, S.V., Inoue, T., and Bass, J.D. (2003) Elastic properties of hydrous  
707 ringwoodite. *American Mineralogist*, 88, 1608-1611.
- 708 Wang, J., Sinogeikin, S.V., Inoue, T., and Bass, J.D. (2006) Elastic properties of hydrous  
709 ringwoodite at high-pressure conditions. *Geophysical Research Letters*, 33, L14308.
- 710 Wang, Y., Weidner, D.J., Zhang, J., Gwanresia, G.D., Liebermann, R.C., and Bass, J.D. (1998)  
711 Thermal equation of state of garnets along the pyrope-majorite join. *Physics of the Earth and  
712 Planetary Interiors*, 105, 59-71.
- 713 Weidner, D.J., and Wang, Y. (2000) Phase transformations: implications for mantle structure. In:  
714 Karato, S.I. et al. (Eds.) Earth's Deep Interior: Mineral Physics and Tomography From the  
715 Atomic to the Global Scale. *Geophysical Monograph Series*, vol. 117. pp. 215-235, American  
716 Geophysical Union, Washington, D.C.
- 717 Withers, A.C., Wood, B.J., and Carroll, M.R. (1998) The OH content of pyrope at high pressure.  
718 *Chemical Geology*, 147, 161-171.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

- 719 Xu, J.G., Zhang, D.Z., Fan, D.W., Dera, P., Shi, F., and Zhou, W.G. (2019) Thermoelastic  
720 properties of eclogitic ternary garnets and omphacites: Implications for deep subduction of  
721 oceanic crust and density anomalies in the upper mantle. *Geophysical Research Letters*, 46,  
722 179-188.
- 723 Yang, J., Lin, J.F., Jacobsen, S.D., Seymour, N.M., Tkachev, S.N., and Prakapenka, V.B. (2016)  
724 Elasticity of ferropericlase and seismic heterogeneity in the Earth's lower mantle. *Journal of*  
725 *Geophysical Research*, 121, 8488-8500.
- 726 Yang, J., Mao, Z., Lin, J.F., and Prakapenka, V.B. (2014) Single-crystal elasticity of the  
727 deep-mantle magnesite at high pressure and temperature. *Earth and Planetary Science Letters*,  
728 392, 292-299.
- 729 Yang, J., Tong, X.Y., Lin, J.F., Okuchi, T., and Tomioka, N. (2015) Elasticity of ferropericlase  
730 across the spin crossover in the Earth's lower mantle. *Scientific Reports*, 5, 17188.
- 731 Ye, Y., Smyth, J.R., Hushur, A., Manghnani, M.H., Lonappan, D., Dera, P., Frost, D.J. (2010)  
732 Crystal structure of hydrous wadsleyite with 2.8% H<sub>2</sub>O and compressibility to 60 GPa.  
733 *American Mineralogist*, 95, 1765-1772.
- 734 Ye, Y., Brown, D.A., Smyth, J.R., Panero, W.R., Jacobsen, S.D., Chang, Y.Y., Townsend, J.P.,  
735 Thomas, S.M., Hauri, E.H., Dera, P., Frost, D.J. (2012) Compressibility and thermal expansion  
736 of hydrous ringwoodite with 2.5(3) wt% H<sub>2</sub>O. *American Mineralogist*, 97, 573-582.
- 737 Zha, C.S., Duffy, T.S., Downs, R.T., Mao, H.K., Hemley, R.J. (1996) Sound velocity and  
738 elasticity of single-crystal forsterite to 16 GPa. *Journal of Geophysical Research*, 101,  
739 17535-17545.
- 740 Zhang, J.S. and Bass, J.D. (2016) Single-crystal elasticity of natural Fe-bearing orthoenstatite  
741 across a high-pressure phase transition. *Geophysical Research Letters*, 43, 8473-8481.
- 742 Zhang, L., Ahsbahs, H., and Kutoglu, A. (1998) Hydrostatic compression and crystal structure of  
743 pyrope to 33 GPa. *Physics and Chemistry of Minerals*, 25, 301-307.

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

744 Zou, Y.T., Gréaux, S., Irifune, T., Whitaker, M.L., Shinmei, T., and Higo, Y. (2012a) Thermal  
745 equation of state of  $\text{Mg}_3\text{Al}_2\text{Si}_3\text{O}_{12}$  pyrope garnet up to 19 GPa and 1,700 K. *Physics and*  
746 *Chemistry of Minerals*, 39, 589-598.

747 Zou, Y.T., Irifune, T., Gréaux, S., Whitaker, M.L., Shinmei, T., Ohfuji, H., Negishi, R., and Higo,  
748 Y. (2012b) Elasticity and sound velocities of polycrystalline  $\text{Mg}_3\text{Al}_2(\text{SiO}_4)_3$  garnet up to 20GPa  
749 and 1700K. *Journal of Applied Physics*, 112, 014910.

750 **Figure Captions**

751 **Figure 1.** Representative Brillouin spectra of single-crystal hydrous pyrope at 18.6  
752 GPa and 300 K (a), and 1 atm and 700 K (b). Open circles: experimental data; solid  
753 lines: fitted  $V_P$  and  $V_S$  peaks, respectively. The average collection time was  $\sim 40$  min  
754 and  $\sim 20$  min for each spectrum of high-pressure and high-temperature measurements,  
755 respectively. The (0.34, -0.53, 0.92) crystallographic plane of single-crystal hydrous  
756 pyrope sample was used for both BLS experiments. Experimental uncertainties are  
757 smaller than the symbols. (Color online.)

758

759 **Figure 2.**  $V_P$  and  $V_S$  velocities of single-crystal hydrous pyrope as a function of the  
760 azimuthal angle measured at 18.6 GPa and 300 K (a), and 1 atm and 700 K (b). Open  
761 circles: experimental data; solid lines: modeled results. Error bars are smaller than the  
762 symbols when not shown. (Color online.)

763

764 **Figure 3.** Single-crystal individual elastic moduli ( $C_{11}$ ,  $C_{12}$ , and  $C_{44}$ ) of hydrous  
765 pyrope as a function of pressure (a) and temperature (b) compared with previous  
766 study of anhydrous pyrope. Solid symbols represent our experimental data; solid lines  
767 are modeled results using the third-order finite-strain equation fitting (a) or a linear  
768 fitting (b); dashed lines represent the experimental data of anhydrous pyrope  
769 (Sinogeikin and Bass 2000, 2002). Error bars are smaller than the symbols when not  
770 shown. (Color online.)

771

FAN ET AL., SINGLE-CRYSTAL ELASTICITY OF HYDROUS PYROPE

---

772 **Figure 4.** Adiabatic bulk ( $K_S$ ) and shear modulus ( $G$ ) of hydrous pyrope as a function  
773 of pressure (a) and temperature (b) compared with previous study of anhydrous  
774 pyrope. Solid symbols represent our experimental data; solid lines are modeled results  
775 using the third-order finite-strain equation fitting (a) or a linear fitting (b); dashed  
776 lines represent the experimental data of anhydrous pyrope (Sinogeikin and Bass 2000,  
777 2002). Error bars are smaller than the symbols when not shown. (Color online.)

778

779 **Figure 5.** Aggregate compressional ( $V_P$ ) and shear velocity ( $V_S$ ) of hydrous pyrope as  
780 a function of pressure (a) and temperature (b) compared with previous study of  
781 anhydrous pyrope. Solid symbols represent our experimental data; solid lines are  
782 modeled results using the third-order finite-strain equation fitting (a) or a linear fitting  
783 (b); dashed lines represent the experimental data of anhydrous pyrope (Sinogeikin and  
784 Bass 2000, 2002). Error bars are smaller than the symbols when not shown. (Color  
785 online.)

786

787 **Figure 6.** Modeled velocities of pyrope garnets in the Earth's upper mantle along the  
788 upper mantle geotherm and cold subducted slabs geotherm. Red lines: hydrous pyrope  
789 (this study; Fan et al. 2017b); blue lines: anhydrous pyrope (Sinogeikin and Bass,  
790 2000, 2002; Zou et al. 2012a); black lines: (Fe,Ca)-bearing pyrope (Lu et al. 2013;  
791 Thieblot et al. 1998). Error bars represent the propagated uncertainties ( $\pm 1\sigma$ ). (Color  
792 online.)

793

794 **Figure 7.** Comparison of modeled  $V_P/V_S$  ratio of hydrous pyrope with anhydrous  
795 pyrope and (Fe,Ca)-bearing pyrope in the Earth's upper mantle along the upper  
796 mantle geotherm and cold subducted slabs geotherm. Error bars represent the  
797 propagated uncertainties ( $\pm 1\sigma$ ). (Color online.)

Table 1 Densities, elastic moduli and aggregate velocities of hydrous pyrope at high pressure and ambient temperature

<i>P</i> (GPa)	Density (g/cm <sup>3</sup> )	<i>C</i> <sub>11</sub> (GPa)	<i>C</i> <sub>12</sub> (GPa)	<i>C</i> <sub>44</sub> (GPa)	<i>K</i> <sub>V</sub> (GPa)	<i>K</i> <sub>R</sub> (GPa)	<i>K</i> <sub>S</sub> (GPa)	<i>G</i> <sub>V</sub> (GPa)	<i>G</i> <sub>R</sub> (GPa)	<i>G</i> (GPa)	<i>V</i> <sub>P</sub> (km/s)	<i>V</i> <sub>S</sub> (km/s)	<i>V</i> <sub>P</sub> / <i>V</i> <sub>S</sub>	<i>AV</i>
0.0001	3.557(2)	294.5(5)	105.7(6)	90.5(4)	168.6(4)	168.6(4)	168.6(4)	92.1(2)	92.0(3)	92.0(3)	9.05(1)	5.09(1)	1.78(1)	-0.026(1)
0.9(1)	3.577(2)	301.7(5)	109.9(6)	91.4(4)	173.8(3)	173.8(3)	173.8(3)	93.1(2)	93.2(3)	93.2(3)	9.13(1)	5.10(1)	1.79(1)	-0.030(1)
3.4(2)	3.629(3)	316.8(6)	119.2(7)	94.3(5)	185.1(4)	185.1(4)	185.1(4)	96.0(2)	96.1(2)	96.1(2)	9.29(1)	5.15(1)	1.81(1)	-0.028(1)
5.8(2)	3.677(3)	331.6(6)	126.3(5)	97.7(4)	194.7(5)	194.7(5)	194.7(5)	99.6(2)	99.7(2)	99.7(2)	9.44(1)	5.21(1)	1.81(1)	-0.030(1)
7.5(1)	3.709(2)	339.7(7)	133.5(6)	100.6(5)	202.2(4)	202.2(4)	202.2(4)	101.6(2)	101.6(2)	101.6(2)	9.54(1)	5.23(1)	1.82(1)	-0.015(1)
10.1(2)	3.757(2)	355.2(7)	142.6(7)	103.5(5)	213.5(3)	213.5(3)	213.5(3)	104.6(2)	104.6(3)	104.6(3)	9.69(1)	5.28(1)	1.84(1)	-0.016(1)
12.3(2)	3.795(3)	368.5(8)	150.6(7)	106.8(5)	223.2(3)	223.2(3)	223.2(3)	107.6(1)	107.7(2)	107.7(2)	9.83(1)	5.33(1)	1.85(1)	-0.012(1)
15.5(3)	3.849(3)	387.4(7)	162.5(6)	110.7(6)	237.5(4)	237.5(4)	237.5(4)	111.4(2)	111.4(2)	111.4(2)	10.01(1)	5.38(1)	1.86(1)	-0.009(1)
18.6(2)	3.899(3)	404.6(8)	174.8(8)	115.2(6)	251.4(5)	251.4(5)	251.4(5)	115.1(1)	115.1(2)	115.1(2)	10.19(1)	5.43(1)	1.88(1)	0.0010(2)

Numbers in parenthesis represent standard deviations.

Table 2 Densities, elastic moduli and aggregate velocities of hydrous pyrope at ambient pressure and high temperature

<i>T</i> (K)	Density (g/cm <sup>3</sup> )	<i>C</i> <sub>11</sub> (GPa)	<i>C</i> <sub>12</sub> (GPa)	<i>C</i> <sub>44</sub> (GPa)	<i>K</i> <sub>V</sub> (GPa)	<i>K</i> <sub>R</sub> (GPa)	<i>K</i> <sub>S</sub> (GPa)	<i>G</i> <sub>V</sub> (GPa)	<i>G</i> <sub>R</sub> (GPa)	<i>G</i> (GPa)	<i>V</i> <sub>P</sub> (km/s)	<i>V</i> <sub>S</sub> (km/s)	<i>V</i> <sub>P</sub> / <i>V</i> <sub>S</sub>	<i>AV</i>
300 <sup>a</sup>	3.557(3)	294.8(6)	105.5(4)	90.7(5)	168.6(5)	168.6(5)	168.6(5)	92.2(3)	92.3(4)	92.3(4)	9.05(1)	5.09(1)	1.78(1)	-0.027(1)
300	3.557(2)	294.5(5)	105.7(6)	90.5(4)	168.6(4)	168.6(4)	168.6(4)	92.0(2)	92.1(3)	92.0(3)	9.05(1)	5.09(1)	1.78(1)	-0.026(1)
400	3.546(3)	291.8(4)	104.9(4)	89.9(2)	167.2(3)	167.2(3)	167.2(3)	91.3(2)	91.3(2)	91.3(2)	9.03(1)	5.07(1)	1.78(1)	-0.024(1)
500	3.534(2)	289.1(5)	104.1(6)	89.3(3)	165.8(3)	165.8(3)	165.8(3)	90.6(1)	90.6(2)	90.6(2)	9.00(1)	5.06(1)	1.78(1)	-0.022(1)
600	3.523(3)	286.6(5)	103.2(5)	88.7(4)	164.3(3)	164.3(3)	164.3(3)	89.9(2)	89.9(2)	89.9(2)	8.98(1)	5.05(1)	1.78(1)	-0.021(1)
700	3.511(3)	283.4(5)	102.3(6)	87.9(4)	162.7(4)	162.7(4)	162.7(4)	89.0(2)	89.0(3)	89.0(3)	8.95(1)	5.03(1)	1.78(1)	-0.019(1)

Numbers in parenthesis represent standard deviations.

<sup>a</sup>) Represents measurement at temperature decreased from 700 K to room temperature.



Table 3 Single-crystal elastic moduli and their pressure and temperature derivatives of hydrous pyrope at ambient conditions in comparison to previous studies <sup>a</sup>

References	Composition	Method	$C_{11}$ (GPa)	$C_{12}$ (GPa)	$C_{44}$ (GPa)	$(\partial C_{11}/\partial P)_T$	$(\partial C_{12}/\partial P)_T$	$(\partial C_{44}/\partial P)_T$	$(\partial C_{11}/\partial T)_P$ (GPa/K)	$(\partial C_{12}/\partial T)_P$ (GPa/K)	$(\partial C_{44}/\partial T)_P$ (GPa/K)
This study	Hydrous Prp100 <sup>c</sup>	BLS	294.5(5)	105.7(6)	90.5(4)	6.2(1)	3.7(1)	1.5(1)	-0.028(1)	-0.009(1)	-0.006(1)
O'Neill et al. (1991)	Hydrous Prp100 <sup>d</sup>	BLS	296.2(5)	111.1(6)	91.6(3)	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>
Leitner et al. (1980)	Prp100	BLS	295(2)	117(1)	90(3)	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>
Sinogeikin and Bass (2000)	Prp100	BLS	297(3)	108(2)	93(2)	5.8(4)	3.2(4)	1.3(3)	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>
Sinogeikin and Bass (2002)	Prp100	BLS	298(3)	107(2)	93(2)	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	-0.031(3)	-0.006(2)	-0.007(2)
Lu et al. (2013)	Prp68Alm24Grs5	BLS	290(2)	106(2)	92.2(6)	6.0(1)	3.5(1)	1.2(1)	-0.021(4)	-0.0163(5)	-0.003(1)

Numbers in parenthesis represent standard deviations. Prp: Pyrope; Alm: Almandine; Grs: Grossular; BLS: Brillouin Light Scattering.

<sup>a</sup>) Only Brillouin scattering results are listed for pyrope garnet.

<sup>b</sup>) The value is not available in the text.

<sup>c</sup>) ~900 ppmw H<sub>2</sub>O.

<sup>d</sup>) ~180 ppmw H<sub>2</sub>O.

Table 4 Bulk and shear moduli and their pressure and temperature derivatives of hydrous pyrope at ambient conditions in comparison to previous studies <sup>a</sup>

References	Composition	Methods	$K_{S0}$ (GPa)	$G_0$ (GPa)	$(\partial K_S/\partial P)_T$	$(\partial G/\partial P)_T$	$(\partial K_S/\partial T)_P$ (GPa/K)	$(\partial G/\partial T)_P$ (GPa/K)
This study	Hydrous Prp100	BLS	168.6(4)	92.0(3)	4.6(1)	1.3(1)	-0.015(1)	-0.008(1)
O'Neill et al. (1991)	Hydrous Prp100	BLS	172.8(3)	92.0(2)	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>
Leitner et al. (1980)	Prp100	BLS	177(1)	89(1)	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>	— <sup>b</sup>
Conrad et al. (2000)	Prp100	BLS	172.7 <sup>c</sup>	92 <sup>c</sup>	3.2 <sup>c</sup>	1.4 <sup>c</sup>	— <sup>b</sup>	— <sup>b</sup>
Sinogeikin and Bass (2000)	Prp100	BLS	171(2)	94(2)	4.1(3)	1.3(2)	— <sup>b</sup>	— <sup>b</sup>
Sinogeikin and Bass (2002)	Prp100	BLS	171(2)	94(2)	— <sup>b</sup>	— <sup>b</sup>	-0.014(2)	-0.009(1)
Lu et al. (2013)	Prp68Alm24Grs5	BLS	168(2)	92(1)	4.4(1)	1.2(1)	-0.017(1)	-0.005(1)
Chen et al. (1999)	Prp100	UI	171(20)	92(1)	5.3(4)	1.6(2)	— <sup>b</sup>	— <sup>b</sup>
Gwanmesia et al. (2006)	Prp100	UI	175(2)	91(1)	3.9(3)	1.7(2)	-0.018(2)	-0.010(1)
Zou et al. (2012)	Prp100	UI	170.0(2)	93.2(1)	4.51(2)	1.51(2)	-0.0170(1)	-0.0107(1)
Chantel et al. (2016)	Prp100	UI	172(2)	89.1(5)	4.38(8)	1.66(5)	-0.018(2)	-0.008(1)

Numbers in parenthesis represent standard deviations.

<sup>a)</sup> Only Brillouin scattering and ultrasonic interferometry results are listed for pyrope garnet.

<sup>b)</sup> The value is not available in the text.

<sup>c)</sup> The uncertainty is not available in the text.

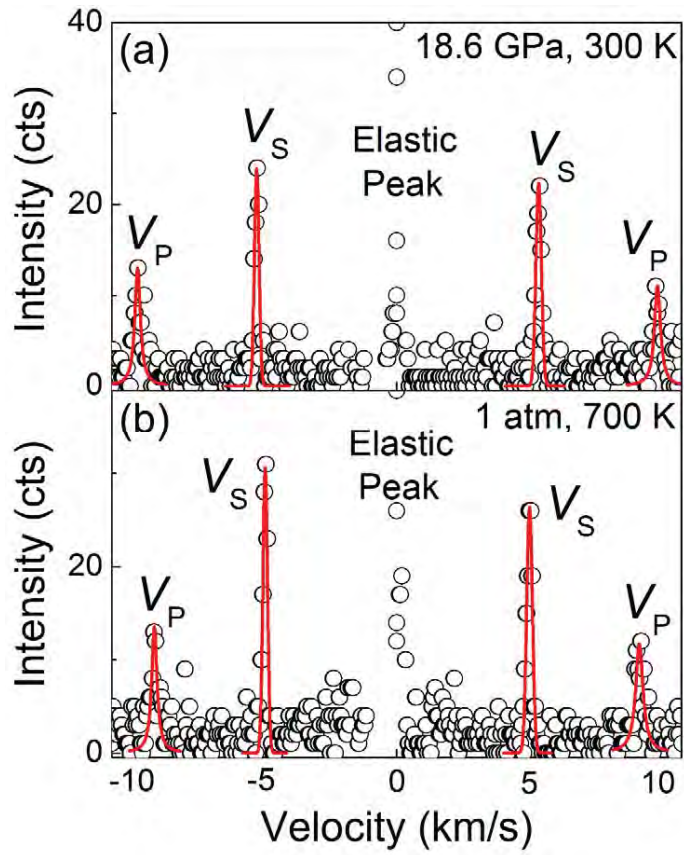


Fig. 1

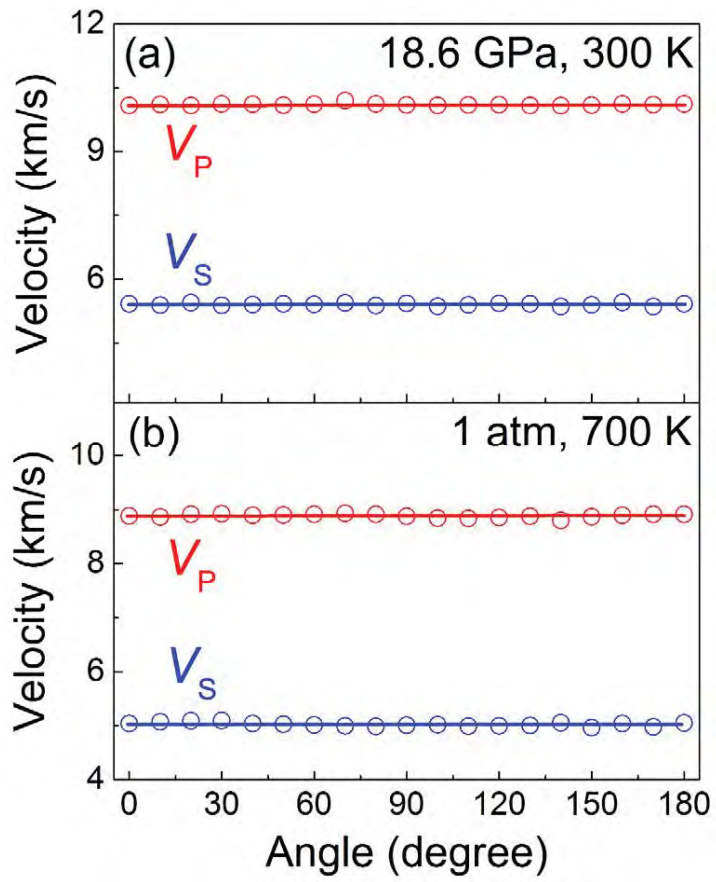


Fig. 2

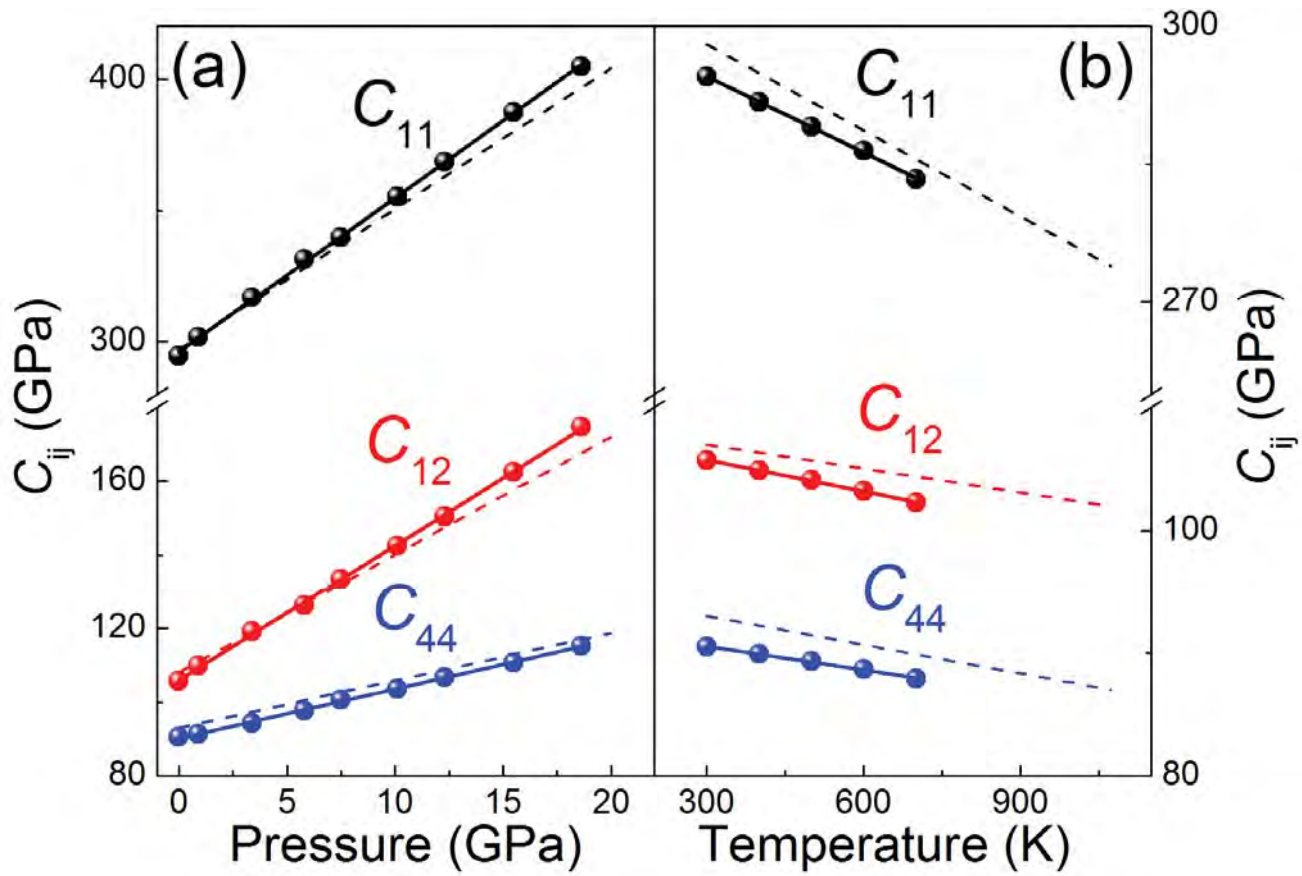


Fig. 3

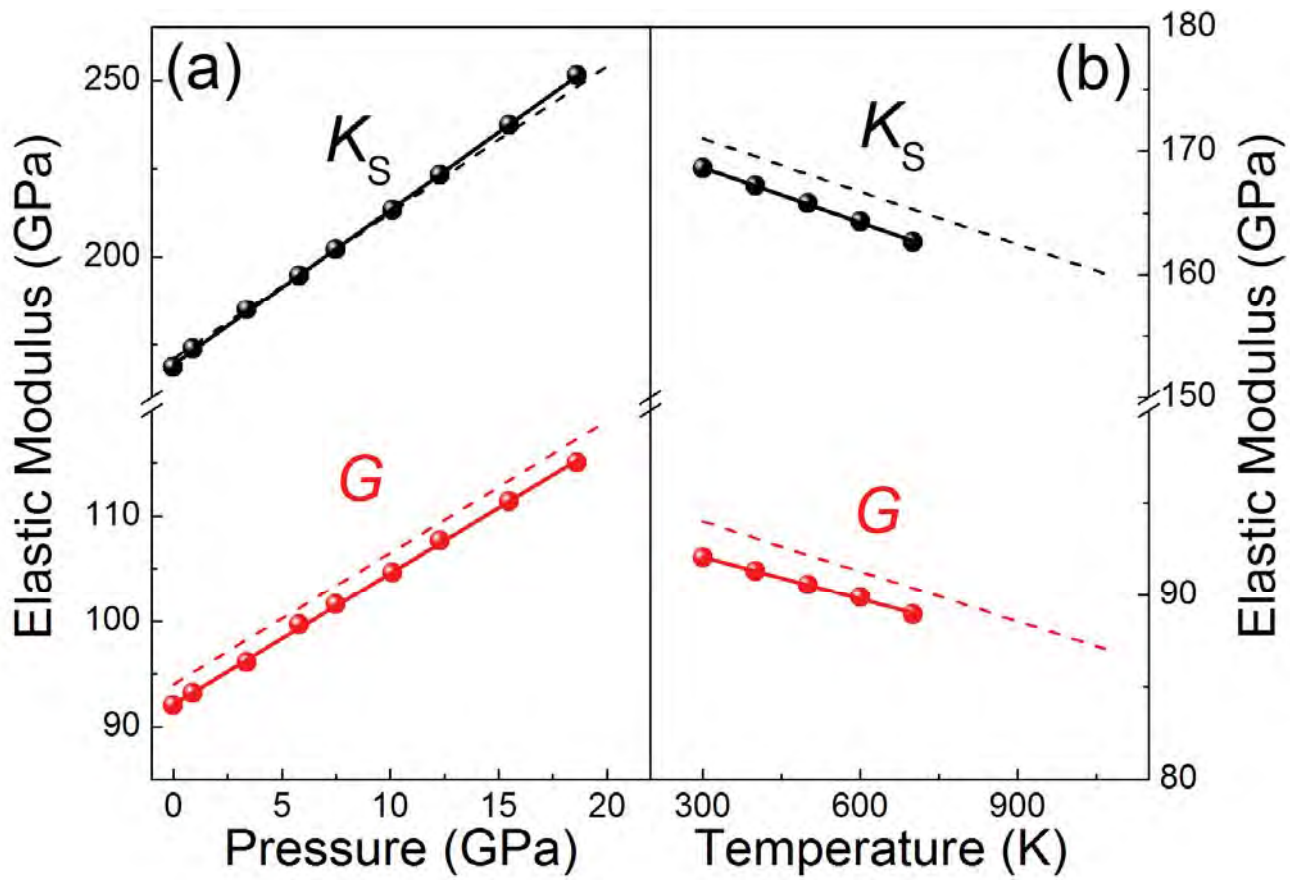


Fig. 4

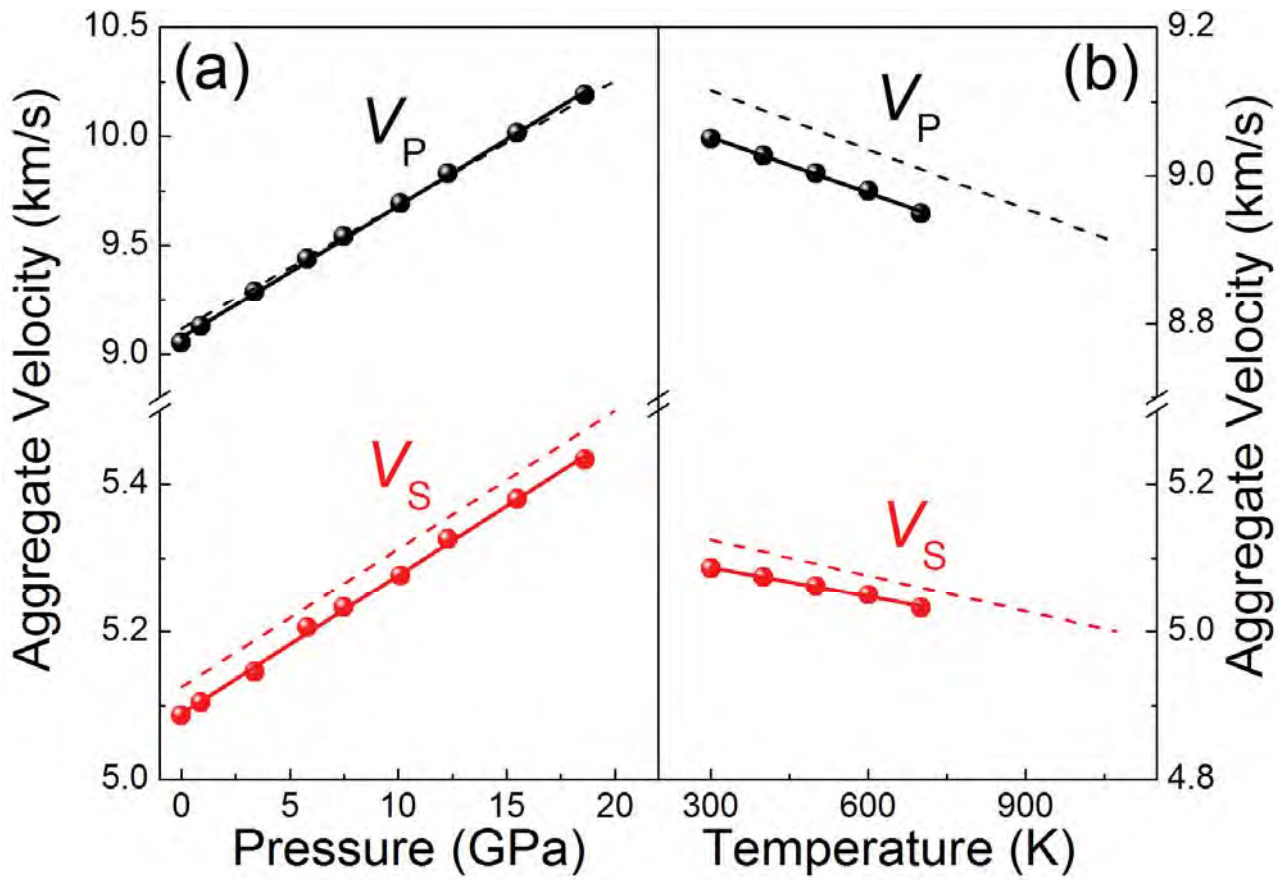


Fig. 5

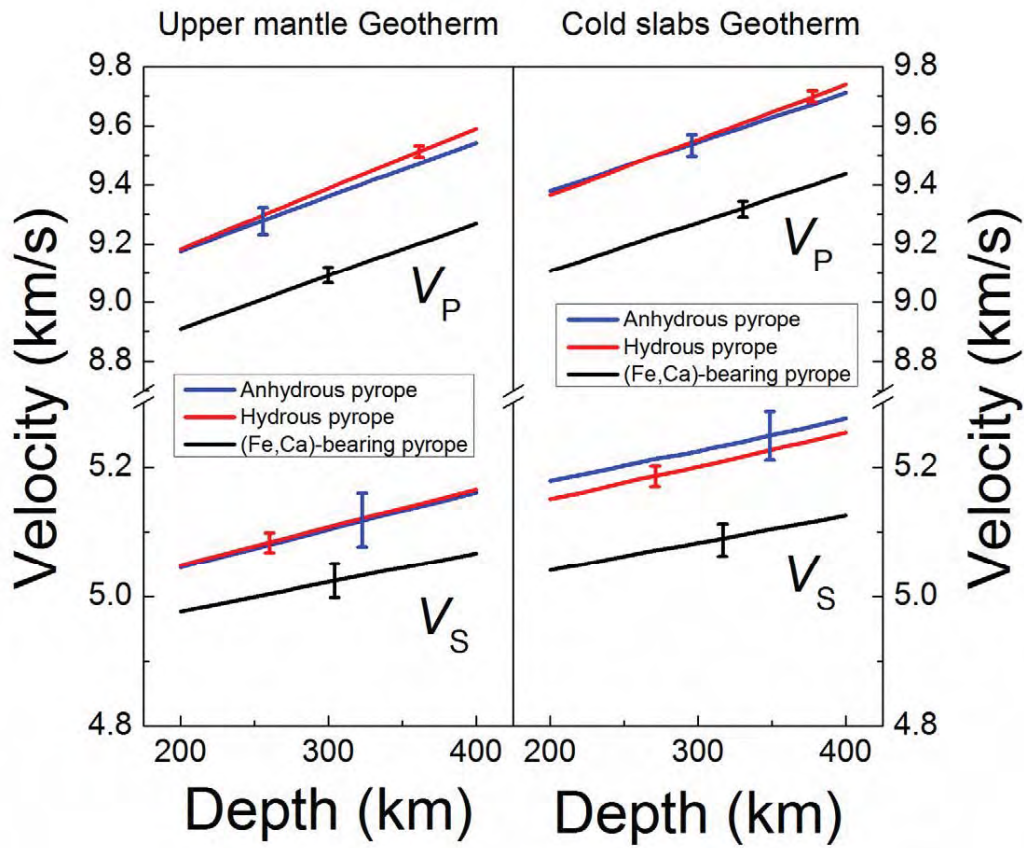


Fig. 6



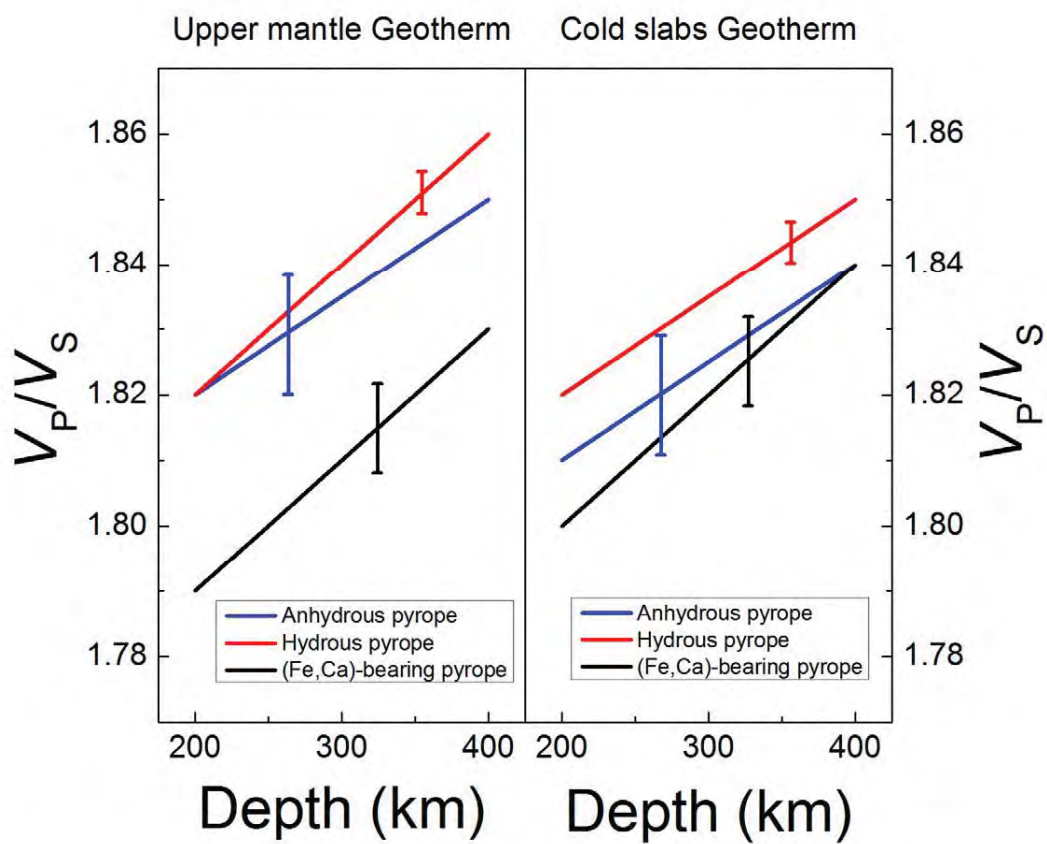


Fig. 7