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5	Carbonation and the Urey Reaction
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9 10	Abstract
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11	There are three major reservoirs for carbon in the Earth at the present time, the core, the mantle,
12	and the continental crust. The carbon in the continental crust is mainly in carbonates (limestones,
13	marbles, etc). In this paper we consider the origin of the carbonates. In 1952 Harold Urey proposed that
14	calcium silicates produced by erosion reacted with atmospheric CO ₂ to produce carbonates, this is now
15	known as the Urey reaction. In this paper we first address how the Urey reaction could have scavenged
16	a significant mass of crustal carbon from the early atmosphere. At the present time the Urey reaction
17	controls the CO ₂ concentration in the atmosphere. The CO ₂ enters the atmosphere by volcanism and is
18	lost to the continental crust through the Urey reaction. We address this process in some detail. We then
19	consider the decay of the Paleocene-Eocene thermal maximum (PETM). We quantify how the Urey
20	reaction removes an injection of CO ₂ into the atmosphere. A typical decay time is 100,000 years but
21	depends on the variable rate of the Urey reaction.
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28	Introduction
29	The continental crust is a major reservoir for carbon in the Earth. A major question in geology
30	is the origin of the carbon, principally in calcium carbonates. The first successful attempt to explain the
31	origin of calcium carbonates (limestones, marbles) in the continental crust was given by Urey (1952).
32	The basic equation he gave was of the form
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34	$CaSiO_3 + CO_2 \Leftrightarrow CaCO_3 + SiO_2$ (1)
35	
36	He proposed that atmospheric CO ₂ combines with a calcium silicate to generate a calcium carbonate
37	plus silica. A direct quote from his paper states: "As carbon dioxide was formed it reacted with silicates
38	to form limestone. Of course, the silicates may have been a variety of minerals, but the presence of CO_2
39	was always kept at a low level by this reaction or similar reactions just as it is now."
40	In the current literature an expanded version of the Urey reaction is given (Blattler and Higgins
41	2017). In order to include the role of acid rain the Urey reaction takes the form
42	$CaSiO_{3} + 2CO_{2} + H_{2}O \rightarrow Ca^{2+} + 2HCO_{3}^{-} + SiO_{2}$ $\rightarrow CaCO_{3} + SiO_{2} + CO_{2} + H_{2}O$ (2)
43	
44	The carbonation takes place when carbon dioxide (carbonic acid) in acid rain dissolves calcium silicate
45	(wollastonite) sediments to give calcium, bicarbonate, and silica. The resulting calcium and bicarbonate
46	ions flow in rivers to the oceans where either organic or inorganic precipitation produces the calcium
47	carbonate.
48	The three large reservoirs for carbon in the Earth at the present time are the core, mantle, and

49 continental crust. We assume that the core is an isolated reservoir and neglect its role. About one per

50 cent of the carbon in the Earth is in the continental crust. Wadepohl (1995) has given a comprehensive 51 study of the composition of the continental crust with an emphasis on carbon. He gives an estimate for the total mass of carbon (c) in the continental crust (cc) at the present time (y) of ${}^{c}M_{ccp} = 4.2 \times 10^{7}$ Gt. 52 53 Haves and Waldbauer (2006) have reviewed the literature on carbon in the continental crust and suggest that it may be as high as ${}^{c}M_{ccp} = 10^{8}$ Gt. DePaolo (2015) gives a range of 6 to 7 x 10⁷ Gt. In 54 this paper we take a representative value to be ${}^{c}M_{ccp} = 5 \times 10^{7}$ Gt. The mass of carbon in the ocean is 55 about a factor of 10^3 less than the mass of carbon in the continental crust (Houghton 2007). 56 57 Urey (1952, 1956) clearly recognized that the reaction he proposed would efficiently remove 58 CO₂ from the Earth's atmosphere, but at that time little was known about the early atmosphere. 59 Although the mass of carbon in the atmosphere today is small (850 Gt), the mass may have been much 60 higher in the past. One of the major differences between Venus and the Earth is atmospheric 61 composition. The atmospheric pressure on Venus is about a factor of 100 greater than the atmospheric 62 pressure on Earth and is 96% carbon dioxide. The mass of carbon in the Venus atmosphere (a) at the present time (p) is ${}^{c}M_{ap} = 1.28 \times 10^{8}$ Gt. Scaling the atmospheric carbon masses to the overall masses of 63 Venus and the Earth gives an estimate of the mass of carbon (c) in the early atmosphere (t=0) of the 64 Earth. The estimated value is ${}^{c}M_{a0} = 1.57 \times 10^{8}$ Gt (Kasting and Ackerman 1986). 65 66 Carbon from the atmosphere to the continental crust 67 One hypothesis for the origin of the carbon in the continental crust is that it was extracted directly from the atmosphere relatively early in Earth's history. The estimated mass of carbon (c) in the 68 early atmosphere (a) given above, ${}^{c}M_{a0} = 1.57 \times 10^{8}$ Gt, is substantially larger than the total estimated 69 carbon in the continental crust given above, ${}^{c}M_{ccp} = 5 \times 10^{7}$ Gt. The hypothesis of direct extraction 70 71 from the atmosphere has been discussed in some detail by Kramers (2002) and by Lowe and Tice 72 (2004).

73 The basic hypothesis is that the mass flux of carbon from the atmosphere to the continental 74 crust, ${}^{c}J_{a-cc}$ is controlled by the availability of calcium silicates. In order for the Urey reaction to extract 75 CO₂ from the atmosphere the early Earth must have had continental crust in order to generate surface 76 deposits of calcium silicate. In addition, the Earth must have had oceans in order for the acid rain to 77 catalyze the Urey reaction between atmospheric CO₂ and the service deposits of calcium silicates. Little 78 data are available for timing the initiation of the extraction of CO₂ from the atmosphere. We will 79 assume that the process begins at a time t_0 after the early bombardment and the solidification of the 80 magma ocean at about 4.4 Ga. We further assume that the Urey reaction extracted carbon from the 81 atmosphere at a constant rate ${}^{c}J_{a-cc}$ until the concentration of CO₂ in the atmosphere was reduced to a very low level. During the time, $t_0 < t < t_0 + \tau_{a-cc}$, the Urey reaction extracts atmospheric carbon to the 82 83 continental crust. We will specify the mass of carbon extracted from the atmosphere and obtain

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$${}^{c}J_{a-cc} = \frac{{}^{c}M_{a0}}{\tau_{a-cc}}$$
 (3)

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We assume that the mass of carbon in the atmosphere ${}^{c}M_{a}$ decreases linearly in time from ${}^{c}M_{a0}$ to zero 86 87 during the time period τ_{a-cc} and the mass of carbon in the continental crust increases linearly in time. Assuming all the carbon in the continental crust ${}^{c}M_{ccp}$ was extracted from the atmosphere the 88 89 dependence on time is given by 90 ${}^{c}M_{cc} = 0$ $0 \le t \le t_0$ 91 ${}^{c}M_{cc} = {}^{c}M_{ccp} \left[(t - t_0) / (\tau_{a - cc}) \right] \qquad t_0 \le t \le t_0 + \tau_{a - cc}$ 92 (4) 93 ${}^{c}M_{cc} = {}^{c}M_{ccp}$ $t_0 + \tau_{a-cc} \le t \le t_p$ 94

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Taking ${}^{c}M_{ccp} = 5 \times 10^{7}$ Gt, $t_{0} = 1$ Gyr, and $\tau_{a-cc} = 1$ Gyr, the dependence of ${}^{c}M_{cc}$ on t is given in Fig. 1. The required flux of carbon from the atmosphere to the continental crust is ${}^{c}J_{a-cc} = 50$ Mtyr⁻¹. It must be

98 emphasized that the value of $\tau_{a \cdot cc}$ is uncertain and the flux ${}^{c}J_{a \cdot cc}$ is expected to have considerable 99 variability in time. However it is quite clear that the extraction of carbon from the atmosphere to the 100 continental crust would have been carried out early in Earth's history.

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Removal of the volcanic addition of carbon to the atmosphere

When excess carbon in the atmosphere has been depleted by the Urey reaction an approximate steady-state balance is established between the volcanic input of carbon into the atmosphere and the extraction by the Urey reaction. We approximate this balance by the relation

$$106 \quad {}^{c}J_{a-cc} = \frac{{}^{c}M_{a}}{\tau_{u}} \tag{5}$$

107 where ${}^{c}J_{a-cc}$ is the rate of volcanic input of carbon into the atmosphere. We assume that this extraction 108 rate is constant and is proportional to the mass of carbon in the atmosphere ${}^{c}M_{a}$. The characteristic time 109 τ_{u} takes account of the rate at which acid rain can interact with calcium silicate sediments, and although 110 we assume that τ_{u} is constant it clearly can be a function of time.

111 A comprehensive model for the variability of atmospheric CO₂ over Phanerozoic times has been 112 given by Berner and Kothavala (2001). This model, GEOCARB 3, is complex and involves both 113 organic and inorganic processes. Transport of carbon between the atmosphere, oceans, and continental 114 crust is quantified on the million year time scale. The balance is dominated by the exchange of carbon 115 between carbonates in the continental crust and carbon in the surficial reservoirs (oceans and 116 atmosphere) and organic carbon (Berner and Calderia, 1997). When erosion is high, the Urey reaction 117 extracts CO₂ from the atmosphere adding carbonates to the continental crust. High erosion rates are 118 associated with low sea level and large continental areas. When erosion is low, the Urey reaction 119 operates in the opposite direction (from right to left in Eq.(1)) with carbonates decomposing to give

120	CO ₂ . An example of this metamorphic process is the subduction of carbonate sediments and the
121	generation and return to the atmosphere of CO_2 in subduction zone volcanics (Frezzotti et al. 2011).
122	The present mass of carbon in the atmosphere is 860 Gt (400 ppmv CO ₂), but this is not a quasi-
123	equilibrium value because of the anthropogenic addition at high fluxes (3.5 Gtyr ⁻¹). We will take the
124	1900 value of 650 Gt (300 ppmv CO ₂) as the present equilibrium value. This is a typical value for the
125	current glacial epoch (0 to 50 Ma). Values given by the GEOCARB 3 Model are generally consistent
126	with observations (Royer 2014). Between 50 and 250 Ma the average values were about 3000 Gt.
127	During the major glacial epoch between 250 and 350 Ma low observed values near 650 Gt are found.
128	Between 350 and 550 Ma values were considerably higher, typically near 10,000 Gt. This variability
129	reflects variations in both of the variables in Eq. (3), the volcanic flux ${}^{c}J_{a-cc}$ into the atmosphere and the
130	characteristic time τ_u .
131	Carbon from the mantle to the continental crust
132	The second hypothesis for the origin of the carbon in the continental crust is that it comes from
133	the mantle. If the volcanic flux of carbon out of the mantle at ocean ridges and hot spots exceeds the
134	carbon lost to the mantle at subduction zones, the difference will be added to the continental crust.
135	Some of the volcanic carbon input will enter the atmosphere and will be transferred to the continental
136	crust through the Urey reaction. However, some will enter the oceans and will be converted directly to
137	carbonates without entering the atmosphere.
138	Rates of carbon loss from the mantle by volcanism and lost by subduction will certainly vary
139	over geologic time, but the variations are uncertain. Again, we assume that the plate tectonic processes
140	required for carbon transfer began at a time t_0 after the solidification of the magma ocean at about 4.5
141	Ga. We further assume that the transfer of carbon out of the mantle has been at a constant rate ${}^{c}J_{m-cc}$
142	until the present time t_p . Assuming all the carbon in the continental crust has been extracted from the

143 mantle, the dependence on time is given by

144

145
$${}^{c}M_{cc} = 0$$
 $0 \le t \le t_0$
146 ${}^{c}M_{cc} = {}^{c}M_{ccp}[(t-t_0)/(t_p-t_0)]$ $t_0 \le t \le t_p + \tau_{a-cc}$ (6)

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148 The mass of carbon in the continental crust increases linearly in time over the period t_0 to t_p . The 149 required flux of carbon from the mantle to the continental crust is given y

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$${}^{c}J_{m-cc} = \frac{{}^{c}M_{ccp}}{t_{p} - t_{0}}$$
 (7)

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153 Taking ${}^{c}M_{ccp} = 5 \ge 10^{7}$ Gt, $t_{0} = 1$ Gyr, and $t_{p} = 4.4$ Gyr the dependence of ${}^{c}M_{cc}$ on t is given in Fig 1. The 154 required flux of carbon from the mantle to the continental crust is ${}^{c}J_{m-cc} = 14.7$ Mtyr⁻¹.

We next consider the estimate for the present loss of carbon from the mantle to the atmosphere. 155 Dasgupta and Hirschmann (2010) have summarized the available data on the loss of carbon from the 156 mantle to the surface reservoirs and give values in the range ${}^{c}J_{m-s} = 36 \pm 24$ Mtyr⁻¹. Just as carbon is 157 158 lost from the mantle by volcanism, carbon is returned to the mantle by subduction. A detailed study of 159 carbon fluxes at subduction zones has been given by Kelemen and Manning (2015). These authors suggest that the downward flux of carbon at global subduction zones is 53 ± 13 Mtyr⁻¹. However a 160 substantial fraction of this carbon never makes it to the mantle due to subduction zone volcanism. They 161 suggested that 24 ± 24 Mtyr⁻¹ reach the mantle. Clearly it is quite possible that all the carbon in the 162 163 continental crust could have come from the mantle. This conclusion was also given by Hayes and 164 Waldbauer (2006).

In Fig. 1 we give examples of the two limiting cases, the carbon in continental crust comesentirely from the atmosphere and the carbon comes entirely from the mantle. In the first case the

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167	addition is early in time and in the second case it is more uniform in time. Observations of the mass of
168	carbonates in the continental crust as a function of age could distinguish between the two cases, but the
169	data are sparse. Observations of the mass of carbon in the atmosphere as a function of time could also
170	be a constraint. An example given by Rye et al. (1995) utilizing studies of paleosols concluded that the
171	mass of carbon in the atmosphere at 2.2 to 2.75 Ga was less than 10^5 Gt. The conclusion is that the
172	extraction of a significant mass of carbon from the atmosphere to the continental crust was completed
173	by $t = 2$ Gyr. However how large this mass was is uncertain.
174	PETM
175	The decay of the Paleocene-Eocene thermal maximum (PETM) can be used to quantitatively
176	constrain the role of the Urey reaction. The PETM was a period of elevated global temperatures (4 to 5
177	degrees C) and high atmospheric CO ₂ beginning at 56.3 Ma, the onset lasted less than 10 Kyr and the
178	subsequent decay lasted about 100 Kyr (McInerney and Wing 2011). Storey et al. (2007) have made a
179	strong case for associating the PETM with flood volcanism resulting from the opening of the north
180	Atlantic.
181	Isotope studies have quantitatively documented the PETM. These studies have been reviewed
182	by Gutjahr et al. (2017). These authors also provided estimates for the carbon content of the
183	atmosphere during the PETM. They suggest that the background carbon mass in the atmosphere before
184	and after the PETM was ${}^{c}M_{ab} = 1400$ Gt and the peak mass of carbon was ${}^{c}M_{a0} = 3050$ Gt.
185	We now carry out an analysis of the decay of the PETM due to the loss of CO ₂ from the
186	atmosphere by the Urey reaction. We extend the balance given in Eq. (5) to include the transient
187	removal of carbon from the atmosphere and write
188	

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$$\frac{d^{c}M_{a}}{dt} = {}^{c}J_{(a-cc)b} - \frac{{}^{c}M_{a}}{\tau_{u}}$$
 (8)

190 191 From Eq. (5) the background mass of carbon in the atmosphere is given by 192 ${}^{c}M_{ab} = au_{u}{}^{c}J_{(a-cc)b}$ 193 (9) 194 We prescribe an initial mass of carbon in the atmosphere at t = 0, ${}^{c}M_{a0}$ and solve Eq. (7) taking τ_{u} to be 195 196 constant with the result 197 ${}^{c}M_{a} = ({}^{c}M_{a0} - {}^{c}M_{ab})e^{-t/\tau_{u}} + {}^{c}M_{ab}$ 198 (10)199 The excess mass of carbon in the atmosphere ${}^{c}M_{a0} - {}^{c}M_{ab}$ decays exponentially as the Urey reaction 200 201 extracts carbon from the atmosphere. We next obtain the dependence of atmosphere carbon mass on time during PETM based on the 202 model dependence given in Eq. (10). Taking the values ${}^{c}M_{ab} = 1400$ Gt and ${}^{c}M_{a0} = 3050$ Gt with τ_{u} 203 204 =100 kyr the model results are given in Figure 2. 205 We now return to Eq. (9). This result relates the background atmospheric carbon mass ${}^{c}M_{ab}$ to the background rate of volcanic input of CO₂ carbon into the atmosphere ${}^{c}J_{(a-cc)b}$ and the Urey reaction 206 rate τ_u . During the PETM we have taken the background carbon mass ${}^{c}M_{ab} = 1400$ Gt. Taking $\tau_u = 100$ 207 kyr we find from Eq. (9) that ${}^{c}J_{(a-cc)b} = 14$ Mtyr⁻¹. This is an independent determination of the volcanic 208 209 flux of carbon into the atmosphere at that time. As discussed above we take the present equilibrium mass of carbon in the atmosphere to be ${}^{c}M_{ab} = 6500$ Gt. Assuming that ${}^{c}J_{(a-cc)b} = 14$ Mtyr⁻¹ we require 210 211 from Eq. (9) that $\tau_u = 50$ kyr. This is our estimated relaxation time for a carbon excursion today. 212

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Discussion

214 Urey (1952) proposed the Urev reaction, Eq. (1), to explain the origin of carbonates in the 215 continental crust. He argued that the reaction would essentially remove all CO₂ from the atmosphere. It 216 is now accepted that in analogy to Venus, there may have been a large mass of carbon in the Earth's early atmosphere, as much as 10^8 Gt. However, only a fraction of this may have survived the moon 217 218 forming impact. We give a very simplified model for the extraction of carbon from the atmosphere to 219 the continental curst, taking the extraction rate ${}^{c}J_{a-cc}$ to be constant. There are basically no constraints 220 on the variation of this rate with time. If a significant fraction of the carbon in the continental crust was 221 extracted from the atmosphere, it is likely that it occurred early in Earth's history as illustrated in Fig. 1. 222 The Urey reaction also controls the equilibrium mass of carbon in the atmosphere after the 223 removal of any large initial concentration. The input of carbon to the atmosphere is from volcanism and 224 we show that the equilibrium mass of carbon in the atmosphere ${}^{c}M_{ab}$ is proportional to the rate of volcanic injection ${}^{c}J_{a-cc}$ divided by a characteristic Urey time τ_{u} . We quantify the value of τ_{u} by 225 studying the observed relaxation of the Paleocene-Eocene thermal maximum, which occurred at 56 Ma. 226 and the relaxation time is about $\tau_u = 10^5$ yrs. 227 228 We also give a simplified model for the extraction of carbon from the atmosphere to the 229 continental crust. If the volcanic loss of carbon from the mantle by volcanism exceeds the return of 230 carbon by subduction, the difference is added to the continental crust. If the volcanic carbon enters the 231 oceans organic precipitation creates carbonates. If the volcanic carbon enters the atmosphere it enters 232 the continental crust by the Urev reaction. Current estimates of carbon fluxes from and to the mantle 233 are sufficient to have produced all the carbon in the continental crust. At the present time it is not 234 possible to quantify the relative importance of carbon addition to the continental crust from the early 235 atmosphere and the mantle.

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This is a preprint, the final version is subject to change, of the American Mineralogist (MSA) Cite as Authors (Year) Title. American Mineralogist, in press. DOI: https://doi.org/10.2138/am-2019-6880 236 237 **Implications** 238 We have addressed two major questions concerning carbon in the atmosphere in this paper. The 239 first is the origin of the carbon in the continental crust. We conclude that it is possible the carbon could 240 have been extracted either from the early atmosphere or from the mantle over a longer period of time. 241 Studies of the concentration of carbon in the atmosphere and continental crust over geologic time are 242 required and should receive a high priority. 243 The second question we have addressed is the relaxation of injections of carbon into the atmosphere back to equilibrium values. We quantify this by studying the Paleocene-Eocene thermal 244 245 maximum (PETM). This has obvious implications for the recovery from the process of anthropogenic 246 injection of carbon into the atmosphere. We find the relaxation time to be about 50,000 yrs. 247 248 References 249 Berner, R. A., Caldeira, K. (1997) The need for mass balance and feedback in the geochemical carbon 250 cycle. Geology 25, 955–956. 251 Berner, R. A., Kothavala, Z. (2001). GEOCARB III: A revised model of atmospheric CO₂ over 252 Phanerozoic time. American Journal of Science 301, 182–204. Blättler, C. L., Higgins, J. A. (2017). Testing Urey's carbonate-silicate cycle using the calcium isotopic 253 254 composition of sedimentary carbonates. Earth and Planetary Science Letters 479, 241-251. 255 Dasgupta, R., and M. M. Hirschmann (2010), The deep carbon cycle and melting in Earth's interior, 256 Earth and Planetary Science Letters, 298, 1-13. DePaolo, D. J. (2015). Sustainable carbon emissions: The geologic perspective. MRS Energy & 257 258 Sustainability 2, E9.

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Figure Captions

Figure 1. Dependence of the mass of carbon in the continental crust ${}^{c}M_{cc}$ on time. Two limiting models

are given for adding the present mass ${}^{c}M_{ccp} = 5 \times 10^{7}$ Gt. 1) Addition from the atmosphere beginning at

- 299 $t_0 = 1$ Gyr. All atmospheric carbon is transferred in $\tau_{a-cc} = 1$ Gyr at a constant flux ${}^{c}J_{a-cc} = 50$ Mtyr⁻¹. 2).
- 300 Addition from the mantle beginning at $t_0 = 1$ Gyr. Carbon is added at a constant flux ${}^{c}J_{m-cc} = 14.7$
- 301 Mtyr⁻¹ to the present.
- 302

303

- Figure 2: Dependence of the atmosphere carbon mass values ${}^{c}M_{a}$ for the PETM anomaly on time t_{PETM}
- relative to the onset of the anomaly. The values are from our relaxation model given in Eq. (11) with
- 306 ${}^{c}M_{ab} = 1400 \text{ Gt} \text{ and } {}^{c}M_{a0} = 3050 \text{ Gt} \text{ and } \tau_{u} = 100 \text{ kyr.}$

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