

1 **Modeling dislocation glide and lattice friction in Mg₂SiO₄ wadsleyite**
2 **in conditions of the Earth's transition zone**

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4 [revision 2]

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11 Thermally activated dislocation glide in Mg₂SiO₄ wadsleyite at 15 GPa has been
12 modeled to investigate its potential contribution to plastic deformation of wadsleyite in the
13 Earth's transition zone. Modeling is based on a multiphysics approach that allows to calculate
14 the constitutive equations associated with single slip for a wide range of temperatures and
15 strain rates typical for the laboratory and the Earth's mantle. The model is based on the core
16 structures of the rate limiting $\frac{1}{2}\langle 111 \rangle\{101\}$ and [100](010) dissociated screw dislocations.
17 After quantifying their lattice friction, glide is modeled through an elastic interaction model
18 that allows to calculate the critical configurations that trigger elementary displacements of
19 dissociated dislocations. The constitutive relations corresponding to glide are then deduced
20 with Orowan's equation to describe the average intracrystalline plasticity. The high stresses
21 predicted by the model are found to be in good agreement with experimental data on plastic
22 deformation of wadsleyite at high-pressure conditions. Moreover, it is found that even at
23 appropriate mantle strain rates, glide of dislocations remain difficult with CRSS's typically
24 larger than 100 MPa. This implies the inefficiency of dislocation glide to the overall plastic
25 deformation of Mg₂SiO₄ wadsleyite under transition zone conditions.
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27 *Keywords:* wadsleyite; transition zone; plastic deformation; dislocation glide; dissociated
28 dislocations; glide mobility
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Introduction

32

33 The 410 km seismic discontinuity is widely accepted to be the consequence of the
34 phase transformation of olivine into wadsleyite. The discontinuity is due to the along going
35 changes in physical properties between both polymorphs (Goldschmidt 1931; Ringwood and
36 Major 1966; Akimoto and Sato 1968; Irifune and Ringwood 1987). This phase change is
37 likely to influence the convective pattern at the top of the transition zone since mantle flow is
38 controlled by the viscosity of the constituent mantle phases. As $(\text{Mg,Fe})_2\text{SiO}_4$ wadsleyite is
39 considered to be the primary phase from 410 to 520 km depth, its rheological properties will
40 determine the solid-state flow in the uppermost part of the mantle transition zone. The
41 rheological contrast between the upper mantle and the top of the transition zone may have
42 implications for the fate of subducting slabs that enter the Earth's transition zone as inferred
43 from seismic tomography (van der Hilst et al. 1997; Grand et al. 1997; Fukao et al. 2001;
44 Fukao and Obayashi 2013). The effect on global mantle convection still remains unsolved
45 (Davies 1995; Bunge et al. 1996; Bunge et al. 1997; Bina et al. 2001; Karason and van der
46 Hilst 2000; Karato et al. 2001; Zhao 2004). Therefore, describing the plastic deformation of
47 wadsleyite is mandatory to gain insight into the convective flow at the boundary between the
48 upper and the lower mantle.

49 Wadsleyite is a sorosilicate with an orthorhombic crystal structure of space group
50 *Imma*. Previous studies (Dupas et al. 1994; Sharp et al. 1994; Dupas-Bruzek et al. 1998;
51 Thurel 2001; Thurel, Douin and Cordier 2003; Metsue et al. 2010) suggest that the two easiest
52 slip systems are $\frac{1}{2}\langle 111 \rangle \{101\}$ and $[100](010)$. They involve dislocations dissociated into
53 collinear partials. Numerous deformation experiments have been conducted to investigate the
54 plasticity of wadsleyite (Chen et al. 1998; Thurel and Cordier 2003; Thurel, Douin and
55 Cordier 2003; Thurel et al. 2003; Nishihara et al. 2008; Farla et al. 2014; Hustoft et al. 2013;

56 Kawazoe et al. 2010; Kawazoe et al. 2013). Despite a considerable amount of mechanical data
57 obtained under laboratory conditions, it remains experimentally impossible to derive
58 constitutive equations related to the extremely low strain rate conditions of the Earth's mantle
59 without the need of extrapolations.

60 As such, we propose to use a computational mineral physics approach to study plastic
61 deformation of wadsleyite at 15 GPa. Regarding plastic deformation, dislocation glide is often
62 considered as one of the most efficient strain producing deformation mechanisms in
63 intracrystalline plasticity. However, in contrast to the latter hypothesis, Ritterbex et al. (2015)
64 show the inefficient contribution of dislocation glide to the overall plasticity of Mg_2SiO_4
65 ringwoodite under transition zone conditions. Starting from Metsue et al. (2010), who
66 calculated the easiest slip systems and determined the associated dislocation core structures in
67 Mg_2SiO_4 wadsleyite at 15 GPa, the aim of the present work is to determine the glide mobility
68 of these rate controlling dislocations as a function of stress and temperature. Since the
69 modeling approach of Ritterbex et al. (2015) was based on the mobility of dissociated
70 dislocations, the same methods will be applied to investigate the potential contribution of
71 dislocation glide to the plasticity of wadsleyite under the conditions of the upper transition
72 zone.

73 To move in high pressure silicates as wadsleyite, dislocations have to overcome their
74 intrinsic lattice resistance. Plastic slip in this so-called thermally activated regime, is mainly
75 governed by sluggish glide of long $\frac{1}{2}\langle 111 \rangle \{ 101 \}$ and $[100](010)$ screw segments (Metsue et
76 al. 2010). If a dislocation bows-out in its glide plane under the conjugate action of stress and
77 thermal activation, it activates non-screw segments that leave behind straight slow moving
78 screw lines, which in turn will account for most of the plastic strain produced. Based on this
79 mechanism, our model is able to determine the temperature threshold T_a (athermal
80 temperature) above which dislocation-dislocation interactions will govern the mobility of

81 dislocations, *i.e.* the temperature threshold below which the glide mobility of dislocations is
82 primarily dominated by lattice resistance as experienced by the rate controlling screw
83 segments.

84 The kinematics of thermally activated glide depend strongly on the specific atomic
85 arrangements that build the dislocation cores. The core structures belonging to the easiest
86 $\frac{1}{2}\langle 111 \rangle\{101\}$ and $[100](010)$ slip systems which have been calculated by Metsue et al.
87 (2010) are reevaluated by making use of the Peierls-Nabarro-Galerkin (PNG) method. Lattice
88 friction experienced by dislocations on each slip system is then calculated and described by
89 the Peierls potential and its derivative, the Peierls stress. Here, however the main purpose is to
90 model the glide mobility based on the thermally-activated motion of the rate controlling
91 dislocation character of the easiest slip systems over the Peierls barriers by nucleation and
92 propagation of unstable kink-pairs. This can be described through an elastic interaction
93 model, initially proposed by Koizumi et al. (1993). This model has been extended to
94 dissociated dislocations and successfully applied to Mg_2SiO_4 ringwoodite by Ritterbex et al.
95 (2015). It is adopted in the present work to handle kink-pair formation on dissociated
96 dislocations as they occur in wadsleyite. Dislocation mobilities are finally determined from
97 the stress dependence on the nucleation rate of kink-pairs. Single slip constitutive equations
98 describing the temperature dependency on the *CRSS*, will be derived by solving Orowan's
99 equation as a function of steady-state strain rate. This will be compared to recent data of
100 experimentally deformed wadsleyite. The results enable us to address the role of lattice
101 friction on the dislocation mobility in wadsleyite under pressure and temperature conditions
102 of the upper transition zone. The outcome will be compared to what has been inferred for
103 dislocation glide in Mg_2SiO_4 ringwoodite by Ritterbex et al. (2015). Finally, implications for
104 the rheology of transition zone will be discussed.

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Multiscale modeling

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109 Parallell to Ritterbex et al. (2015), our numerical multiscale model relies on two main
110 steps. First, determining the lattice friction experienced by dislocations that belong to the
111 easiest slip systems. This is calculated in the framework of the Peierls-Nabarro (PN) model
112 (Peierls 1940; Nabarro 1947). Secondly, the elastic interaction model used in Ritterbex et al.
113 (2015) will be applied to calculate the enthalpy variations related to critical configurations
114 that trigger elementary displacements of the rate controlling dissociated dislocations in
115 wadsleyite. Finally, dislocation glide will be described through single slip mobilities which
116 are deduced from the latter results.

117

Dislocation core structures and lattice friction

118

119
120 The element free Galerkin method based PNG model (Denoual 2007) has been used
121 by Metsue al. (2010) to model dislocations belonging to the easiest slip systems:
122 $\frac{1}{2}\langle 111 \rangle\{101\}$ and $[100](010)$. The calculations rely on the γ -surfaces of the potential slip
123 planes that takes into account the effect of pressure on atomic bonding.

124 Here the main interest is to quantify the lattice friction of the easiest dislocations by
125 calculating the Peierls potential. This is computed in the framework of the PN model, by
126 making use of the disregistry u_m and of the γ -surfaces (Ritterbex et al. 2015). The disregistry
127 $u_m = u_m^a - u_m^b$ refers to the relative displacement between two misfit half planes a and b , as
128 the material is decomposed into two elastic half crystals A and B . The Peierls potential V_p (Eq.
129 1) can now be obtained by the addition of the following two energy contributions: 1)
130 summation of the non-elastic misfit energy between m pairs of crystal planes:

131 $V_m = \sum_{m=-\infty}^{m=+\infty} \gamma(u_m) a'$ (Christian and Vitek, 1970; Joós et al. 1994) and 2) summation of the
132 elastic strain energy: $V_e = 1/2 \cdot a' \cdot \left\{ \sum_{m=-\infty}^{m=+\infty} [\partial\gamma/\partial u_m(u_m)]^a u_m^a + \sum_{m=-\infty}^{m=+\infty} [\partial\gamma/\partial u_m(u_m)]^b u_m^b \right\}$ (Wang
133 2006). The previous expressions stand for moving the core structure over the Peierls
134 periodicity a' from one to the next stable position in the crystal lattice.

135

136 $V_p = V_m + V_e$ (1)

137

138 The Peierls stress can now be given by $\tau_p = \max\{\Sigma\}$, where $\Sigma = b^{-1}\nabla V_p$ corresponds to the
139 Peierls force with b being the modulus of the Burgers vector. The Peierls stress can be seen as
140 a pure mechanical measure of the lattice friction and can equally be understood as the CRSS at
141 0 K.

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143 **Kink-pair formation on dissociated dislocations**

144

145 The same approach as in Ritterbex et al. (2015) is used to calculate the saddle point
146 energies ΔH^{crit} of ΔH required to nucleate a bulge from the initial dissociated dislocation
147 lines bowing out over the Peierls potential V_p . This is considered to be the controlling step of
148 thermally activated motion of dislocations in high lattice friction materials (Kubin 2013). In
149 the presence of low and intermediate stresses, the widths of the complete bulges, which are
150 known as kink-pairs, are much larger than the spread of the individual kinks along the
151 dislocation line (Koizumi et al. 1994). Therefore the model relies on the assumption of
152 displacing elementary segments of width w on the initial dislocation line by the nucleation of

153 rectangular kink-pairs of height h (Fig. 1). The enthalpy variation ΔH that describes kink-
154 pair formation on dissociated dislocations can be formulated as follows:

155

$$156 \quad \Delta H = \Delta E_{elastic} + c_i \Delta P_p + \Delta W_{sf} + c_i W_p \quad (2)$$

157

158 Eq. (2) shows the dependency of the kink-pair formation enthalpy ΔH on the total variation in
159 elastic energy $\Delta E_{elastic}$, the change in Peierls energy ΔP_p , the variation in stacking fault
160 energy ΔW_{sf} and work W_p performed by the applied stress on the partials. The model is
161 based on the necessity to form a kink-pair on both partials in order to move the complete
162 dislocation. This can occur either through “correlated” nucleation of kink-pairs along both
163 partials or through independent nucleation that starts on one and is followed by the formation
164 of a kink-pair on the other partial. As such, it has been taken into account that each equivalent
165 partial has to overcome half of the complete Peierls potential V_p (Eq. 1). The constants c_i in
166 Eq. 2 refer to $c_i = c_u = 1$ for uncorrelated and $c_i = c_c = 2$ for correlated kink-pair nucleation.
167 The critical nucleation enthalpy $\Delta H^{crit}(w^{crit}, h^{crit})$ can thus be found as the saddle point
168 configuration of $\Delta H(w, h)$ as a function of the resolved shear stress τ .

169 Figure 1 shows the characteristics of kink-pair nucleation on collinear dissociated
170 dislocations under the action of a resolved shear stress. Starting from Fig. 1a at low stress
171 conditions, kink-pair nucleation is forced to occur in a correlated manner on both partials,
172 since the work done by the stress cannot overcome the increase in absolute energy related to
173 substantial changes in the equilibrium stacking fault width d inherent to uncorrelated
174 nucleation (Möller 1978, Takeuchi 1995; Mitchell et al. 2003). Only small local variations of
175 the stacking fault are allowed. The small variations in d , in case of low-energy stacking fault
176 systems (e.g. partials separated by a large equilibrium distance d), are able to reduce the

177 saddle point configuration of the metastable system by lowering the stacking fault energy
178 without any change in elastic interaction between the partials. Under these low stress
179 conditions, the widths w_1 (partial 1) and w_2 (partial 2) between the kink-pairs are relatively
180 equal. However, if stress increases, one of the kink-pairs tend to collapse and the kink-pair
181 nucleation process becomes gradually decoupled: independent uncorrelated kink-pair
182 nucleation on both partials become favorable (Fig. 1b and c). This implies that uncorrelated
183 nucleation of kink-pairs can only occur and is favorable at $\tau \geq \tau_c$, where τ_c is equal to a
184 critical stress. See supplementary material and Ritterbex et al. (2015) for a detailed
185 description of the kink-pair model.

186

187 **Results**

188

189 **Dislocation cores and their lattice friction**

190

191 The dislocation core structures belonging to the easiest $\frac{1}{2} \langle 111 \rangle \{101\}$ and $[100](010)$
192 slip systems have been calculated by Metsue et al. (2010) using the PNG method.
193 Calculations relied on the γ -surfaces of the potential slip planes. Metsue et al. (2010) shows
194 that dislocation core structures of both slip systems are more confined for the screw than for
195 the edge dislocations. As a consequence, lattice friction will be lower for the edge than for the
196 screw dislocations. As the edge characters exhibit lower lattice friction, the mobility of the
197 $\frac{1}{2} \langle 111 \rangle \{101\}$ and the $[100](010)$ screw dislocations will account for most of the plastic
198 strain produced during deformation since the amount contributed by the faster edge segments
199 is negligible. We have reevaluated the core structures of the $\frac{1}{2} \langle 111 \rangle \{101\}$ and $[100](010)$
200 screw dislocations following Metsue et al. (2010). The resulting dislocation core structures
201 are shown in Fig. 2 by the disregistry and its derivative, the local Burgers vector density. This

202 shows the dissociation of both screw dislocations into two collinear partials. The Burgers
203 vector reaction for the $\frac{1}{2}\langle 111 \rangle$ screw in the $\{101\}$ plane is $\frac{1}{2}\langle 111 \rangle = \frac{2}{10}\langle 111 \rangle + \frac{3}{10}\langle 111 \rangle$.
204 The Burgers vector reaction for the $[100]$ screw in the (010) plane is $[100] = \frac{1}{2}[100] +$
205 $\frac{1}{2}[100]$. It is worth to mention that the equilibrium stacking fault width d (see Fig. 2) between
206 the partials is always found to be equal to an integer multiple of the Peierls periodicity a' . This
207 means that both partials occupy the minimum energy configuration in the crystal system
208 under equilibrium conditions, so that both partials are well placed into the wells of the Peierls
209 potential.

210 The Peierls potentials are derived according to Eq. 1 and Peierls stresses are evaluated
211 by the maximum derivative of the Peierls potentials. Tables 1 and 2 show the properties
212 related to the dislocation core structures and Peierls stresses for both slip systems,
213 respectively. Peierls potentials and their derivatives are shown in Fig. 3. Both slip systems
214 have a value of $\tau_p / \mu \sim 3.5 \times 10^{-2}$. A value of $\tau_p / \mu \sim 5 \times 10^{-2}$ has been found in Mg_2SiO_4
215 ringwoodite (Ritterbex et al. 2015) with respect to the rate controlling dislocations of the
216 easiest slip systems. A comparison with $\tau_p / \mu \sim 1 \times 10^{-2}$ in MgO (Amodeo et al. 2011) at
217 similar pressure conditions indicates higher lattice friction in both high-pressure polymorphs
218 of olivine.

219

220 **Thermal activation of glide: kink-pair mechanism**

221

222 Critical enthalpies associated with kink-pair nucleation are calculated in the
223 framework of the elastic interaction model as adapted to dissociated dislocations (Ritterbex et
224 al. 2015). Based on linear elasticity, the shear modulus μ and the Poisson ratio ν at 15 GPa
225 have been deduced using the DisDi software (Douin 1987). As the latter relies on Stroh theory,

226 the anisotropic elastic parameter $K(\theta)$ for the screw character is given by $K(0^\circ) = \mu$ and for
227 the edge character by $K(90^\circ) = \mu/(1-\nu)$. Finally, the core structures (Fig. 2 and Table 1) of
228 the $\frac{1}{2}\langle 111 \rangle\{101\}$ and the $[100](010)$ screw dislocations and the quantification of their
229 intrinsic lattice friction (Fig. 3 and Table 2) are used to calculate the critical nucleation
230 enthalpies ΔH^{crit} .

231 Kink-pair nucleation on the $\frac{1}{2}\langle 111 \rangle\{101\}$ screw dislocation can be described as in the
232 general case for dissociated dislocations as already discussed in Ritterbex et al. (2015). This
233 means that correlated nucleation of kink-pairs is captured by the single critical activation
234 enthalpy ΔH_c^{crit} . Uncorrelated kink-pair nucleation is essentially determined by the outward
235 motion of the leading partial associated with the nucleation process as shown in Fig. 1c.

236 This is not the case for the $[100](010)$ screw dislocation since the equilibrium
237 dissociation width d is equal to a single period a' of the Peierls potential (Table 1): kink-pair
238 nucleation that starts from the trailing partial is not possible. The evolution of the critical
239 nucleation enthalpy with resolved shear stress for this slip system is therefore entirely given
240 by ΔH_c^{crit} (Fig. 4), since the uncorrelated nucleation process as shown in Fig. 1b is completely
241 governed by the critical enthalpy $\Delta H_{u,t1}^{crit} \approx \Delta H_c^{crit}$, associated with the outward motion of the
242 leading partial.

243 The elastic interaction model is restricted to the low and intermediate stress regime
244 (Caillard and Martin 2003). However, the critical nucleation enthalpies can be extrapolated up
245 to the Peierls stress using the classical formalism of Kocks et al. (1975):

246

$$247 \quad \Delta H^{crit}(\tau) = \Delta H_0 \left(1 - \left(\tau_{eff} / \tau_p \right)^p \right)^q \quad (3)$$

248

249 where ΔH_0 is equal to $\Delta H_c^{crit}(\tau = 0)$ and $\Delta H_u^{crit}(\tau = \tau_c)$ for the correlated and uncorrelated
250 kink-pair nucleation mechanisms, respectively. τ_{eff} is defined as the effective resolved shear
251 stress. For correlated nucleation $\tau_{eff} = \tau$ and for uncorrelated nucleation $\tau_{eff} = \alpha(\tau - \tau_c)$,
252 with $\alpha = \tau_p / (\tau_p - \tau_c) \approx 1$, where τ_c is equal to the critical resolved shear stress above which
253 uncorrelated nucleation is able to occur (Table 3). The empirical parameters p and q are
254 obtained from a least square minimization between the Kocks formalism (Eq. 3) and the
255 evolution of $\Delta H^{crit}(\tau)$ of kink-pair nucleation as calculated with the elastic interaction
256 model. Results of the critical nucleation enthalpies as a function of resolved shear stress for
257 both slip systems are presented in Fig. 4.

258

259 **Dislocation mobility**

260

261 The dislocation velocity depends on the waiting time for a kink-pair nucleation
262 process to occur at both partials under the action of applied resolved shear stress and thermal
263 activation. This waiting time can be expressed in terms of the rate of kink-pair nucleation J .
264 The dislocation velocity is given by Eq. 4, where a' (Peierls periodicity) is the unit distance to
265 move a complete (dissociated) dislocation.

266

$$267 \quad v(\tau, T) = a' J \quad (4)$$

268

269 The rate of kink-pair nucleation J (Dorn and Rajnak 1964; Guyot and Dorn 1967; Möller
270 1978) is given by

271

$$J = \nu_0 \frac{b_p}{w^{crit}(\tau)} \frac{L}{c_i b_p} \exp\left(-\frac{\Delta H^{crit}(\tau)}{k_b T}\right) \quad (5)$$

273

274 where b_p is the modulus of the Burgers vector of the partials, w^{crit} is the critical width
275 between kink-pairs, ν_0 is equal to the Debye frequency, k_b is the Boltzmann constant and T is
276 the temperature. The pre-exponential factor on the right side of Eq. 5 is composed of two
277 contributions of which the first one is equal to the vibration frequency $\nu_0 b_p / w^{crit}$ of the
278 partial segments where nucleation initiates. The second contribution is the number of
279 potential activation sites $L / c_i b_p$, taking into account that only the resonance modes allow
280 correlated nucleation on both partials to occur. The average length L of the dislocation
281 segments can be expressed in terms of the dislocation density ρ_m as $L = 1 / \sqrt{\rho_m}$. The
282 dislocation density ρ_m is taken to be $10^{12} m^{-2}$ under experimental and $10^8 m^{-2}$ under mantle
283 conditions to take into account the stress differences between both regimes.

284 Following Möller (1978), the average dislocation mobility can now be formulated as:

285

$$v(\tau, T) = \frac{1}{2} a' [J_c + J^*] \quad (6)$$

287

288 where J_c corresponds to the rate of correlated kink-pair nucleation (Eq. 5). If
289 $\tau < \tau_c \rightarrow J^* = J_c$ and if $\tau \geq \tau_c \rightarrow J^* = J_u$ where J_u corresponds to the nucleation rate
290 associated with uncorrelated kink-pair nucleation (Eq. 5).

291 Dislocation velocity profiles $v(\tau)$ at fixed temperatures for both $\frac{1}{2}\langle 111 \rangle \{101\}$ and
292 $[100](010)$ screw dislocations are shown in Fig 5. The critical shear stress τ_c below which

293 only correlated kink-pair nucleation can occur is equal to about 500 MPa and 900 MPa for the
294 $\frac{1}{2}\langle 111 \rangle\{101\}$ screw and $[100](010)$ screw dislocations, respectively (Table 3). Figure 5a
295 shows the resolved shear stress dependence of the velocities for both screw dislocations at
296 1700 K in a log-log plot. This clearly shows that the velocity of the $\frac{1}{2}\langle 111 \rangle\{101\}$ screws,
297 independent of the applied stress, is always larger than that of the $[100](010)$ screw
298 dislocations. The small window in Fig. 5a shows the same velocity curves in a semi-log plot
299 which gives a better insight into the velocity differences with stress between both screw
300 dislocations. Here, we can observe that at high, but mainly at intermediate stress values, the
301 velocity differences between both slip systems are relatively large and decrease with
302 decreasing stress. At very low stress levels (what can be expected in mantle conditions), the
303 dislocation velocities for both screws become more comparable. Typical laboratory strain
304 rates of $\dot{\epsilon} = 10^{-5} \text{ s}^{-1}$ correspond to dislocation velocities of about $v = 2 \times 10^{-8} \text{ m/s}$. The stresses
305 associated with these velocities are in the order of 0.5-2 GPa. In contrast, dislocation
306 velocities related to mantle strain rates of $\dot{\epsilon} = 10^{-16} \text{ s}^{-1}$ are about $v = 2 \times 10^{-15} \text{ m/s}$ with
307 stresses of $\sim 200\text{-}1000 \text{ MPa}$. At room temperature, the velocity evolution with stress of the
308 same screw dislocations are shown in Fig. 5b. Here, physically relevant dislocation glide only
309 takes place in the high stress regime where uncorrelated nucleation of kink-pairs govern the
310 dislocation mobility. The overall trend of the velocity profiles at room temperature are
311 comparable to the results at 1700 K. Stresses of about 1-4 GPa are required to obtain
312 dislocation velocities corresponding to typical laboratory strain rates at room temperature.
313 Finally, one can observe that the dislocation velocities at the Peierls stress for each individual
314 dislocation are strictly independent of temperature since this stress corresponds to the
315 resolved shear stress required to move an infinite dislocation at the absolute zero. At the
316 Peierls stress, the mobility of dislocations is governed by other mechanisms than the
317 nucleation of kink-pairs and the results of $\lim_{\tau \rightarrow \tau_p} v(\tau)$ are considered to be unphysical.

318

Discussion

319

320 General discussion

321 In 2010, Metsue et al. already modeled the core structures of dislocations in
322 wadsleyite using the PNG model. Here, the core structures of the rate controlling
323 $\frac{1}{2}\langle 111 \rangle\{101\}$ and $[100](010)$ screw dislocations are recalculated using the same approach,
324 showing a good agreement with results previously obtained by Metsue et al. (2010). Lattice
325 friction of these screw dislocations are quantified by explicit calculation of the Peierls
326 potentials within the framework of the PN model. The Peierls stresses calculated in this study
327 are about one order of magnitude larger than the ones of Metsue et al. (2010). However, the
328 relative differences between both screw dislocations are found to be equal. Nevertheless, the
329 values of τ_p obtained in this study are more in line with what can be expected from
330 experiments (Nishihara et al. 2008; Kawazoe et al. 2013; Hustoft et al. 2013; Farla et al.
331 2015).

332 We show that the Burgers vector reaction for the $[100]$ screw dislocation in the (010)
333 plane corresponds to $[100] = \frac{1}{2}[100] + \frac{1}{2}[100]$. This dissociation is collinear and both partials
334 are strictly equivalent. The collinear partials of the $\frac{1}{2}\langle 111 \rangle$ screw dislocation in the $\{101\}$
335 plane with Burgers vector reaction: $\frac{1}{2}\langle 111 \rangle = \frac{2}{10}\langle 111 \rangle + \frac{3}{10}\langle 111 \rangle$ are not equivalent.
336 However, the asymmetry between the partials is small and is neglected throughout the
337 calculations of the dislocation mobility. As a matter of fact, the core structure of this
338 dislocation is widely spread with a large equilibrium stacking fault width ($d=35.8 \text{ \AA}$) (Fig.
339 2b). This significant core extension is confirmed by clear weak-beam dark-field observation
340 of both partials of the $\frac{1}{2}\langle 111 \rangle\{101\}$ dislocation using transmission electron microscopy
341 (TEM) (Thurel and Cordier 2003). The effect of this low energy stacking fault on the mobility

342 is more important than the small difference between both partials. So formally, we assume
343 both partials of the $\frac{1}{2}\langle 111 \rangle$ dislocation to be equal to $\frac{1}{4}\langle 111 \rangle$.

344 In the second part of the work, dislocation mobilities related to single slip systems are
345 calculated. Dislocation velocities are obtained by using the elastic interaction model, based on
346 the thermal activation of glide of dissociated dislocations (Ritterbex et al. 2015). Figure 5a
347 clearly shows a pronounced difference in the evolution of $v(\tau)$ at 1700 K for both screw
348 dislocations considered. This difference is directly related to the difference in evolution of
349 $\Delta H^{crit}(\tau)$ (Fig. 4). The latter, once more, is the consequence of the different core structures
350 between the $[100](010)$ and $\frac{1}{2}\langle 111 \rangle\{101\}$ screw dislocations: $[100](010)$ exhibits narrow
351 dissociation with a confined spreading of the partials, whether $\frac{1}{2}\langle 111 \rangle\{101\}$ is characterized
352 by an extended dissociation with a wide spread of the partials (Fig. 2). These features finally
353 determine the velocity evolution $v(\tau)$ of the dislocations. The results further show that
354 correlated nucleation of kink-pairs which coincide along both partials is possible at every
355 stress, whereas uncorrelated nucleation is only possible and becomes more favorable than
356 correlated nucleation at $\tau \geq \tau_p$ due to lower critical nucleation enthalpies. This implies that
357 dislocation glide operating by the Peierls mechanism at low temperatures and high deviatoric
358 stress (in most cases, laboratory conditions), will be mainly governed by uncorrelated
359 nucleation of kink-pairs. However, at high temperatures and small deviatoric stresses (more
360 likely to represent mantle conditions), glide will be predominantly controlled by correlated
361 nucleation of kink-pairs on both partials.

362 Steady-state plastic flow as a consequence of single slip can now be formulated by
363 relating the glide mobility $v(\tau, T)$ to the macroscopic strain rate $\dot{\epsilon}$ by the use of Orowan's
364 equation: $\dot{\epsilon} = \rho_m b v(\tau, T)$, where ρ_m corresponds to the mobile dislocation density and b
365 equals the modulus of the complete Burgers vector for each respective slip system.

366 Deformation under laboratory conditions

367

368 In order to compare the results of our model with mechanical data available from high
369 P,T-experiments, we solve Orowan's equation as function of strain rate $\dot{\epsilon}$ for which the
370 resolved shear stress τ can then be seen as the critical resolved shear stress *CRSS*. We have
371 calculated the *CRSS* over a broad range of temperatures for a typical laboratory strain rate of
372 $\dot{\epsilon} = 10^{-5} \text{ s}^{-1}$. Figure 6 shows the results for the slip of the rate governing $\frac{1}{2}\langle 111 \rangle \{101\}$ and
373 $[100](010)$ screw dislocations. The transition of the curves to the dotted lines at 2500 K marks
374 the onset to melting for the Mg_2SiO_4 system around 15 GPa. This demonstrates that
375 dislocation glide in wadsleyite at laboratory strain rates always operates in the thermally-
376 activated regime, since the athermal temperature would be higher than the melting
377 temperature. It means that intracrystalline plasticity under laboratory conditions is mainly
378 governed by the mobility of the rate controlling slip systems. The results show that slip of the
379 $\frac{1}{2}\langle 111 \rangle \{101\}$ screws is always easier than slip of the $[100](010)$ screw dislocations for the
380 whole stress range $0 < \text{CRSS} \leq \tau_p$. Furthermore, one can observe that the evolution of the
381 $\text{CRSS}(T)$ for both screw dislocations is significantly different. This is directly related to the
382 difference in core structure between both screw dislocations and the subsequent difference in
383 equilibrium stacking fault energies. Whereas the evolution at high *CRSS* and low *T* for
384 $[100](010)$ screws is roughly linear, the same evolution for the $\frac{1}{2}\langle 111 \rangle \{101\}$ screw
385 dislocations is highly exponential. At high *T* where both curves converge towards each other,
386 the difference in $\text{CRSS}(T)$ are found to be the smallest. Fig. 6 shows a remarkably good
387 agreement between our theoretical predictions and the experimental data available. It is worth
388 to mention that the deformation experiments used from (Nishihara et al. 2008; Kawazoe et al.
389 2010; Kawazoe et al. 2013; Hustoft et al. 2013; Farla et al. 2015) were performed on
390 polycrystalline wadsleyite samples. The raw experimental data rather display the temperature

391 dependence on the effective flow stress than on the *CRSS* related to single slip systems as in
392 our calculations. Only a fraction of the effective flow stress is resolved in the slip direction
393 within each single slip plane. As such, the experimental data are divided by two
394 (corresponding to the maximum of the Schmid factor) in order to be compared with our
395 resolved shear stresses in Fig. 6. The latter assumption may be too simple as more
396 deformation mechanisms may be involved in the experiments and effects of impurities and
397 hardening due to texture formation has not been taken into account in our model. However, a
398 posteriori TEM observations of deformed samples in some of the experimental studies (*e.g.*
399 Hustoft et al. 2013; Farla et al. 2015) clearly reveal the potential contribution of dislocation
400 glide to the overall deformation under laboratory conditions by the development of dense
401 microstructures with high dislocation densities ($>10^{12} m^{-2}$). Furthermore, the agreement
402 between the experimental data and the evolution of the *CRSS* with *T* of the rate controlling
403 dislocations shows that glide controls largely the mechanical behavior in laboratory
404 conditions.

405

406 **Deformation under transition zone conditions**

407

408 Strain rate is one of the important physical conditions that determine the potential
409 contribution of a deformation mechanism to the overall plasticity. Unfortunately, there is a
410 large discrepancy between the very low strain rates at which the high-pressure silicates of the
411 Earth's mantle deform and the laboratory conditions which correspond to strain rates of about
412 $10^{-5} s^{-1}$. Experimental constitutive equations therefore have to rely on the extrapolation down
413 to typical mantle strain rates of $10^{-16} s^{-1}$. However, the extrapolation cannot account for the
414 intrinsic strain rate dependency on the mobility of the defects.

415 By modeling the glide mobility of the rate controlling dislocations, we are able to
416 calculate the evolution of $CRSS(T)$ for typical mantle strain rates $\dot{\epsilon} = 10^{-16} s^{-1}$ without the
417 need of extapolation. Modeling of the glide plasticity has been performed at 15 GPa, since
418 wadsleyite is stable in the upper half of the transition zone, from 410-520 km at a pressure
419 range of 13-18 GPa, which corresponds to a temperature interval around 1700 K. Results of
420 the evolution of the $CRSS(T)$ are shown in Fig. 7. One can observe that the minimum $CRSS$
421 lies around 200 MPa for the easiest slip system up to over 600 MPa for the more difficult slip
422 system at 1700 K. The results show that glide in wadsleyite under mantle conditions still
423 occurs in a regime where the $CRSS$ is temperature dependent (thermally activated regime).
424 This implies that plastic deformation by dislocation glide in wadsleyite under conditions of
425 the upper transition zone is governed by the average mobility of the rate governing screw
426 dislocations. However, it has to be mentionned that the temperature dependency of the $CRSS$
427 is a function of the applied strain rate and the mobile dislocation density.

428 Finally, it follows from our study that the relative ease of glide of the different slip
429 systems, as derived by the intrinsic lattice friction and defined by the Peierls stress, is not
430 affected by temperature and strain rate, since glide of the $\frac{1}{2}\langle 111 \rangle \{ 101 \}$ remains easier than
431 $[100](010)$ glide in the whole range of conditions considered. Together with the fact that
432 $\frac{1}{2}\langle 111 \rangle \{ 101 \}$ has more symmetrical variants than $[100](010)$, we estimate that
433 $\frac{1}{2}\langle 111 \rangle \{ 101 \}$ slip will play a dominant role in dislocation glide governed deformation of
434 (poly)crystalline wadsleyite under both natural and laboratory conditions.

435

436 **Implications**

437

438 The above results show the inefficiency of dislocation glide as a strain producing
439 deformation mechanism under transition zone conditions. To compare the wadsleyite results

440 to glide in ringwoodite, we calculate the viscosities η associated with single slip as
441 $\eta = CRSS(T = 1700K) / 2\dot{\epsilon}$. A viscosity between $(0.9 - 3) \times 10^{24}$ Pa s can be attributed to
442 slip of the $\frac{1}{2}\langle 111 \rangle\{101\}$ and $[100](010)$, respectively. Similar single slip viscosities in the
443 order of 10^{24} Pa s were found for Mg_2SiO_4 ringwoodite (Ritterbex et al. 2015) deforming by
444 dislocation glide. As for comparison, a viscosity at transition zone depth in the order of
445 $10^{21} - 10^{22}$ Pa s may be expected from global joint inversion (Mitrovica and Forte 2004).
446 This shows that the sole contribution of dislocation glide is unlikely to account for the overall
447 plasticity of Mg_2SiO_4 wadsleyite and ringwoodite under transition zone conditions. It is
448 essentially the evolution of the critical kink-pair nucleation enthalpies $\Delta H^{crit}(\tau)$ that
449 determine the constitutive equations as shown in Fig. 6 and 7. Typical values of the critical
450 nucleation enthalpies at low stress conditions of the mantle for the rate controlling
451 dislocations in both high pressure polymorphs of olivine are found to be $\lim_{\tau \rightarrow 0} \Delta H^{crit} > 10$ eV.
452 This is what makes glide difficult to activate.

453 High values of the $CRSS(T)$ regarding pure single slip dislocation glide suggest that
454 other mechanisms may control the deformation of wadsleyite and ringwoodite in the Earth's
455 transition zone. In fact, the transition zone is characterized by a number of phase
456 transformations which may give rise to transformation plasticity, sometimes referred to as
457 transformational superplasticity. The phase transformations, furthermore are often
458 accompanied by grain size reduction which may enhance diffusion mechanisms as is the same
459 for water weakening processes due to the water bearing capacity of wadsleyite and
460 ringwoodite (Chen et al. 1998; Huang et al. 2005). Finally, significant lattice friction that is
461 opposed to glide may also activate climb controlled diffusion based intracrystalline
462 deformation.

463 Nevertheless, some studies report about the local stagnation of slabs where subducting
464 lithosphere deflects laterally just above or within the Earth's transition zone (van der Hilst et
465 al. 1991; van der Hilst et al. 1997; Tajima and Grand 1995; Fukao et al. 2001; Grand 2002;
466 Zhao 2004; Fukao and Obayashi 2013). Local slab stagnation in the transition zone may
467 therefore be related to high lattice resistance associated with plastic slip in both wadsleyite
468 and ringwoodite, whereas it is expected that more efficient deformation mechanisms other
469 than dislocation glide have to be responsible for the overall plasticity of both high pressure
470 polymorphs of olivine in the Earth's transition zone. This must at least be the case where
471 slabs penetrate unhindered into the lower mantle.

472

473

Conclusion

474

475 Dislocation glide in Mg_2SiO_4 wadsleyite has been modeled at 15 GPa under laboratory
476 and natural conditions. The model relies on the core structures of the rate governing
477 $\frac{1}{2}\langle 111 \rangle\{101\}$ and $[100](010)$ screw dislocations. A crucial feature of these screw
478 dislocations is the collinear dissociation into partials which determines their mobility.
479 Intrinsic resistance of the crystal lattice that is opposed to glide has been calculated and used
480 to model thermal activation of these dissociated dislocations in order to calculate the
481 respective glide velocities. Plastic deformation by dislocation glide is finally presented as the
482 response of the temperature dependency of the *CRSS* to an applied strain rate at steady-state
483 conditions. A good agreement between our results at typical laboratory strain rates of
484 $\dot{\epsilon} = 10^{-5} \text{ s}^{-1}$ and experimental data on plastic deformation of wadsleyite demonstrates that
485 dislocation glide controls largely the mechanical behavior at laboratory conditions. This
486 validation allows to calculate the constitutive equations related to dislocation glide for typical
487 mantle strain rates of $\dot{\epsilon} = 10^{-16} \text{ s}^{-1}$. It is clear that lattice friction in wadsleyite cannot be

488 neglected at those low strain rates in a similar way as in Mg_2SiO_4 ringwoodite, that has
489 already been studied. This indicates the inefficiency of dislocation glide as a strain producing
490 deformation mechanism under transition zone conditions. The results suggest that dislocation
491 glide is not an efficient deformation mechanism to operate in natural conditions for both high
492 pressure polymorphs of olivine. This implies the necessity of deformation mechanisms other
493 than dislocation glide to be responsible for the overall plasticity of wadsleyite and
494 ringwoodite in the Earth's transition zone.

495

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497

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Figure captions

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725 Figure 1: Kink-pair nucleation on collinear dissociated dislocations with equilibrium
726 stacking fault width d . (a) Correlated nucleation process: coherently simultaneous kink-pair
727 nucleation on partial dislocations. (b) Uncorrelated nucleation: kink-pair nucleation starting
728 from the leading partial followed by a nucleation of the trailing partial. (c) Uncorrelated
729 nucleation: kink-pair nucleation starting from the trailing partial followed by the nucleation of
730 the leading partial.

731

732 Figure 2: Results of the PNG calculations in form of the disregistry (red continuous
733 line) and its derivative, the local density of the Burgers vector (green dotted line) of the: a)
734 $[100](010)$ screw dislocations and b) $\frac{1}{2}\langle 111 \rangle\{101\}$ screw dislocations.

735

736 Figure 3: Peierls potentials $V(p)$ and subsequent Peierls force $\Sigma = b^{-1}\nabla V_p$ calculated
737 in the framework of the PN model and based on the dislocation structures for the a)
738 $[100](010)$ screw and b) $\frac{1}{2}\langle 111 \rangle\{101\}$ screw dislocations. The potentials give a pure
739 mechanical measure of the lattice friction of both slip systems which will serve as input to
740 calculate the thermally activated mobility the respective screw dislocations.

741

742 Figure 4: Evolution of the critical kink-pair nucleation enthalpy as a function of the
743 resolved shear stress (normalized by the Peierls stress) for the $[100](010)$ screw and the
744 $\frac{1}{2}\langle 111 \rangle\{101\}$ screw dislocations. Results are shown for correlated nucleation and the
745 relevant elementary steps of the uncorrelated nucleation processes.

746

747 Figure 5: Glide velocity of the $\frac{1}{2}\langle 111 \rangle\{101\}$ and $[100](010)$ screw dislocations as a
748 function of the resolved shear stress at: a) 1700 K and b) 300 K.

749

750 Figure 6: Constitutive relation shown as the critical resolved shear stress (*CRSS*)
751 versus temperature at a fixed strain rate of $\dot{\epsilon} = 10^{-5} \text{ s}^{-1}$ for thermally activated glide of the rate
752 controlling $\frac{1}{2}\langle 111 \rangle\{101\}$ and $[100](010)$ screw dislocations. The mobile dislocation density
753 is taken to be $\rho_m = 10^{12} \text{ m}^{-2}$. The experimental effective flow stresses are divided by two
754 (corresponding to the maximum of the Schmid factor) to be converted into apparent resolved
755 shear stresses since deformation experiments were performed on polycrystalline samples.

756

757 Figure 7: Constitutive relations shown as the critical resolved shear stress (*CRSS*)
758 versus temperature at a fixed strain rate of $\dot{\epsilon} = 10^{-16} \text{ s}^{-1}$ for thermally activated glide of the rate
759 controlling $\frac{1}{2}\langle 111 \rangle\{101\}$ and $[100](010)$ screw dislocations. The dislocation density is taken
760 to $\rho_m = 10^8 \text{ m}^{-2}$ to adjust to the low stress regime in the Earth's mantle. The shaded area
761 depicts the stability field of wadsleyite in the upper transition zone at 15 GPa.

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Tables

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Dislocation	b_p (Å)	$K(\theta=0^\circ)$ (GPa)	$K(\theta=90^\circ)$ (GPa)	a' (Å)	ξ (Å)	d (Å)
[100](010)	2.803	123	185	4.028	2.0	5.4
$\frac{1}{2}\langle 111 \rangle \{101\}$	$b_{p1}=2.987$ $b_{p2}=4.480$	128	171	7.3	$\xi_1=8.4$ $\xi_2=12.5$	35.8

784 Table 1: Core structures of the $\frac{1}{2}\langle 111 \rangle \{101\}$ and [100](010) screw dislocations with Peierls
785 periodicity a' . $K(\theta)$ is equal to the anisotropic elastic parameter, ξ corresponds to the width of
786 each partial, d is equal to the equilibrium stacking fault width taken as the distance between
787 the partials and τ_p corresponds to the Peierls stress.

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Dislocation	τ_p (GPa)	ΔH_0 (eV)	p	q
[100](010)	4.8	12.5	0.5	1.03
$\frac{1}{2}\langle 111 \rangle \{101\}$	3.5	12.3	0.5	1.61

791 Table 2: Key features and parameterization related to the glide as a result of correlated kink-
792 pair nucleation of the governing screw dislocations. ΔH_0 is the critical nucleation enthalpy at
793 $\tau = 0$, a' the Peierls periodicity, τ_p corresponds to the Peierls stress and p and q are together
794 with ΔH_0 the empirical fitting parameters of Eq. 5.

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Dislocation	τ_p (GPa)	τ_c (GPa)	ΔH_0 (eV)	p	q
[100](010)	4.8	0.89	8.6	<i>n/a</i>	<i>n/a</i>
$\frac{1}{2}\langle 111 \rangle \{101\}$	3.5	0.455	5.3	1.0	5.0

798 Table 3: Key features and parameterization related to the glide as a result of uncorrelated
799 kink-pair nucleation of $\frac{1}{2}\langle 111 \rangle \{101\}$ screw dislocation, where ΔH_0 is the critical nucleation
800 enthalpy at $\tau = \tau_c$. The remaining parameters are defined as in Table 2. The uncorrelated
801 kink-pair nucleation of the [100](010) screw dislocations can be described as in Table 2 since
802 it is constrained to kink-pair nucleation starting at the leading partial.

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