

1 **Revision 2**

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3 **A COMPARATIVE STUDY OF TWO PHASE EQUILIBRIA MODELING TOOLS:**
4 **MORB EQUILIBRIUM STATES AT VARIABLE PRESSURE AND H₂O**
5 **CONCENTRATIONS**

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ABSTRACT

19 Phase equilibria modeling is a powerful petrological tool to address both forward and inverse
20 geological problems over a broad range of crustal and upper mantle conditions of pressure (P),
21 temperature (T), composition (X) and redox (f_{O_2}). The development of thermodynamic databases,
22 relatively realistic activity–composition (a – X) relations for solids, melts and fluids, pressure-
23 volume-temperature (PVT) equations of state (EOS), and efficient numerical algorithms

24 represent an inflection point in our ability to understand the nexus between tectonics and
25 petrogenesis. While developed—and typically applied in isolation—by either metamorphic or
26 igneous petrologists, some of the published thermodynamic models have overlapping P – T – X
27 calibration ranges, which enables comparisons of model outcomes for similar conditions within
28 the range of applicability. In this paper, we systematically compare the results of two such
29 models that are routinely used for calculating phase equilibria in melt-bearing systems: rhyolite-
30 MELTS (Ghiorso et al., 2012; Ghiorso and Gualda, 2015) and the metabasite set of Green et al.
31 (2016) using the thermodynamic database ds62 (Holland and Powell, 2011) (hereafter denoted as
32 “HPx-mb16”). We selected a N-MORB composition and modeled closed system equilibrium
33 phase relations as a function of temperature at 0.25 GPa and 1 GPa for N-MORB with 0.5 wt%
34 and 4 wt% H₂O. Our results show that phase relations exhibit some key differences that, in some
35 instances, impact geological inferences. For example, clinopyroxene and plagioclase stabilities
36 are expanded to higher temperatures in HPx-mb16 compared to predictions from rhyolite-
37 MELTS. Orthopyroxene and olivine are stable in greater proportions and at wider temperature
38 ranges in rhyolite-MELTS compared to HPx-mb16. Importantly, HPx-mb16 predicts amphibole
39 in all runs presented here, whereas amphibole is only predicted at high- P –high-H₂O (1 GPa and
40 4 wt% H₂O) in rhyolite-MELTS, and in lesser amounts. Garnet stability is systematically
41 expanded at higher temperatures and the proportion is greater in rhyolite-MELTS. In addition to
42 phase assemblage differences, phase compositions may differ. For example, plagioclase anorthite
43 content is systematically higher in HPx-mb16 (for the same set of conditions) whereas garnet
44 Mg# is higher in rhyolite-MELTS. Calculated amphibole compositions are substantially different
45 between the two models as well. Liquid compositions also show important differences. High- T
46 liquids are generally similar in SiO₂ contents but diverge at lower temperatures; in these cases,

47 HPx-mb16 liquids are SiO₂-depleted compared to those produced by rhyolite-MELTS. Liquids
48 are also systematically and substantially more mafic in HPx-mb16, and alumina and the alkali
49 concentrations are relatively different and show different trends as a function of temperature at
50 constant pressure. Overall, liquid compositions show the greatest differences near the solidus.
51 Differences in modal abundances of phases and liquid compositions influence liquid trace-
52 element signatures, and these differences can affect geological interpretations. Finally, a
53 comparison between melting experiments of basaltic bulk composition and both thermodynamic
54 models shows that rhyolite-MELTS better reproduces the higher temperature experiments,
55 whereas HPx-mb16 better reproduces the lower temperature experiments. We discuss these and
56 other similarities and differences in order to highlight the strengths and limitations of each
57 model, and to recognize that modeling results have important implications for interpretations of
58 geologic processes. We recognize that our results are informed by a small subset of calculations
59 over a limited range of conditions—our results encourage further comparisons over a wider
60 range of conditions and compositions.

61
62 **Key words:** phase equilibria modeling, computational petrology, rhyolite-MELTS, Theriak-
63 Domino, thermodynamics

64

65 INTRODUCTION

66 The use of thermodynamics to comprehensively model multiphase and multicomponent igneous and
67 metamorphic systems is one of the most important developments in the Earth Sciences of the past
68 several decades (Ghiorso and Sack, 1995; Powell et al., 1998). Phase equilibria modeling can predict
69 equilibrium phase relationships over a wide range of pressure and temperature conditions (P – T) for a

70 variety of bulk compositions at various redox conditions (Powell et al., 1998, 2005; Powell and Holland,
71 2008; Gaulda et al., 2012). While there are inherent limitations associated with the use of any phase
72 equilibrium model—including the neglect of reaction kinetics, solid and liquid state diffusion, spatial P –
73 T gradients, and uncertainties associated with thermodynamic properties of relevant substances—their
74 utility to reproduce first-order observations of key Earth processes is evident (see, e.g., seminal work of
75 Bowen, 1928, 1945; Thompson, 1967; Carmichael et al., 1974). Successes include phase equilibria
76 modeling that has described magmatic systems and metamorphism in a host of environments including
77 volcanic arcs, subduction zones, orogenic terranes, and large igneous provinces (e.g. Kerrick and
78 Connolly, 2001; White and Powell, 2002; Johnson et al., 2008; Fowler and Spera, 2010; Bohrsen et al.,
79 2014; Yakymchuck and Brown, 2014; García-Arias and Stevens, 2017; Palin et al., 2017; Hernández-
80 Uribe and Palin, 2019; Heinonen et al., 2019; among many others).

81 Crystallization and partial melting are crucial for understanding heat advection and matter
82 exchange between the mantle and the crust as the formation, extraction, ascent and crystallization of
83 magma is a primary mechanism that leads to differentiation on Earth and other planetary bodies
84 (England and Thompson, 1986; Brown, 2007). Accurate phase equilibria predictions (of liquid-bearing
85 systems) are thus key components of the earth scientist’s toolbox to understand crucial geological
86 processes. Multiphase and multicomponent thermodynamic modeling of partially or totally molten
87 systems has been possible since the 1980’s and the pioneering efforts have been greatly extended and
88 improved over the past thirty years (Berman, 1988; Essene, 1989; Holland and Powell, 1998, 2011;
89 Ghiorso and Sack, 1995; Ghiorso, 2004). Standard state thermodynamic data, volatile species pressure-
90 volume-temperature (PVT) data, and activity–composition (a – X) relations for crystalline and liquid
91 solutions (collectively referred hereafter as “the thermodynamic model”) commonly used in igneous
92 petrology include those in the MELTS package (rhyolite-MELTS, pMELTS, and pHMELTS

93 calibrations; Ghiorso and Sack, 1995; Asimow and Ghiorso, 1998; Ghiorso et al., 2002; Asimow et al.,
94 2004; Gualda et al., 2012; Ghiorso and Gualda, 2015). The thermodynamic model commonly used in
95 metamorphic petrology is mostly based on the work of Powell and Holland (1988) and Holland and
96 Powell (1998, 2011), although there are other examples (cf., Lanari and Duesterhoeft, 2018). For
97 metamorphic systems, modeling of granitic liquid compositions is possible with the White et al. (2014)
98 silicate liquid $a-X$ relations based on previous liquid relations (Holland and Powell, 1998, 2001; White
99 et al., 2001, 2007), whereas basaltic melting can be modeled with the $a-X$ relations of Jennings and
100 Holland (2015) and Green et al. (2016). Updated $a-X$ relations that allow modeling of melt-bearing
101 equilibria in ultramafic-to-felsic metamorphic systems were recently published by Holland et al. (2018)
102 and Tomlinson and Holland (2021). We emphasize that although different thermodynamic models are
103 preferred by igneous and metamorphic petrologists, the models have overlapping calibration ranges and
104 are used for exactly the same purpose—modeling phase equilibria and compositions in liquid-bearing
105 silicate systems. At equilibrium closed-system conditions, partial melting of a metabasic lithology and
106 crystallization of a basaltic liquid exhibit identical phase relations at a given $P-T$ state point.

107 Despite the common use of phase equilibria modeling in petrology, to the best of our
108 knowledge, there have not been systematic studies to examine differences among
109 thermodynamic models where calibrations overlap. While the study of Jennings and Holland
110 (2015) and Holland et al. (2018) do compare their $a-X$ relations to results from pMELTS, the
111 focus of those papers was not a systematic comparison of the predicted equilibria. Existing
112 comparative studies in metamorphic petrology explore the differences of the various Holland and
113 Powell thermodynamic databases (e.g. Korhonen et al., 2014; Guevara and Caddick, 2016; Pan
114 et al., 2020; Starr et al., 2020), and compare model predictions with experiments and natural
115 samples (e.g. White et al., 2011; Forshaw et al., 2019; Santos et al., 2019; García-Arias, 2020;

116 Bartoli and Carvalho, 2021; Gervais and Trapy, 2021). The MELTS package collection has also
117 been compared to results of other thermobarometric methods on natural samples (e.g., Pamukcu
118 et al., 2015), experimental studies not included in the model calibrations (e.g., Hirschmann et al.,
119 1998; Neave et al., 2019; Pichavant et al., 2019), and between different MELTS calibrations
120 (e.g., Balta and McSween, 2013).

121 In this study, we take a combined approach. We systematically compare phase equilibria
122 calculated with rhyolite-MELTS (Ghiorso et al., 2012; Ghiorso and Gualda, 2015) and the
123 “metabasite set” of Green et al. (2016) (“HPx-mb16”, calculated using Theriak-Domino; de
124 Capitani and Brown, 1987; de Capitani and Petrakakis, 2010) for the equilibrium states of a mid-
125 ocean ridge basalt (MORB) at different P – T conditions and different initial H₂O contents from
126 near-liquidus to solidus temperatures along the fayalite–magnetite–quartz (FMQ) oxygen buffer.
127 These two thermodynamic approaches (i.e., rhyolite MELTS and HPx-mb16) are the most
128 commonly used by igneous and metamorphic petrologists, respectively, to describe liquid-
129 bearing mafic systems. We also evaluate how closely the calculated MORB phase equilibria
130 between rhyolite-MELTS and HPx-mb16 compare with independent relevant experiments (i.e.,
131 not used in the calibration). We discuss the implications of our results within the framework of
132 trace-element modeling and examine the geologic implications of the differences in model
133 outcomes. By comparing the effects of pressure and H₂O concentration on the phase equilibria
134 during equilibrium melting and crystallization of a MORB using two extant thermodynamic
135 models, we provide our perspective on model uncertainty associated with the choice of
136 modeling. The critical insight of our work is to recognize the strengths of the thermodynamic
137 models, to highlight similarities and differences in order to illustrate how the choice of
138 thermodynamic models can lead to different geologic interpretations.

139

140

THERMODYNAMIC MODELS

141 Phase equilibria modeling relies on standard state thermodynamic data, EOS's and a - X relations
142 for solid and liquid solutions. A thermodynamic database includes standard state properties for
143 all phases, the form and numerical values defining PVT , and isobaric heat capacity expressions
144 for all phases (Berman, 1988; Essene, 1989; Holland and Powell, 1998, 2011; Ghiorso and Sack,
145 1995; Ghiorso, 2004). These parameters are obtained from experimental, calorimetric and other
146 studies (e.g., spectroscopy), and some are statistically treated to obtain the best-fit value for a
147 desired parameter from multiple experiments (e.g., least-squares regressions used by Holland and
148 Powell databases). In order to be "internally consistent", all thermodynamic parameters must be
149 compatible with thermodynamic definitions and identities, adhere to a set of reference values,
150 consider simultaneously all the experimental data, and reproduce primary data within their
151 uncertainties (Lanari and Duisterhoeft, 2018, and references therein). The rhyolite-MELTS
152 thermodynamic database is based on Berman (1988) with modifications (see Ghiorso and Sack,
153 1995; Asimow and Ghiorso, 1998; Gualda et al., 2012; Ghiorso and Gualda, 2015 for details).
154 The thermodynamic data used in HPx-mb16 utilizes version 6.2 of Holland and Powell (2011).
155 Some important differences between these thermodynamic data include—but are not limited
156 to—how the equations of state of the solid phases are calculated (i.e. using the Tait equation of
157 state in Holland and Powell (2011) vs. the EOS modified from Berman (1988) in the MELTS
158 package) and the isobaric 1-bar heat capacity dependence on temperature (i.e., the Robie et al.
159 (1978) equation in Holland and Powell (2011) vs. the high- T form used in the Berman and
160 Brown (1985) equation for the MELTS package). Furthermore, the PVT properties of fluid
161 utilized in the MELTS package are calculated using the model of Ghiorso and Gualda (2015),

162 whereas in Holland and Powell (2011) the equation of state of Pitzer and Sterner (1995) is used.
163 For a comprehensive review of all the parameters used in these two thermodynamic models, the
164 reader is referred to the original references.

165 In addition to standard state thermodynamic properties for pure phases, one must also
166 treat the non-ideal properties of crystalline, liquid and gaseous solutions. The excess Gibbs
167 energies of multicomponent solutions are handled using $a-X$ relations that relate Gibbs excess
168 energies as a function of pressure, temperature, and solution composition to activity coefficients.
169 The solid solution models describe the thermodynamics of mixing between end-members of the
170 multicomponent solution and reflect the elemental substitutions that take place in crystalline
171 solids including ordering and exsolution. The $a-X$ relations for solid-solution phases commonly
172 contain end-member proportions, crystallographic site fractions, mixing parameters (also known
173 as the Margules parameter), ideal parameters, and thermodynamic adjustments (Lanari and
174 Duesterhoeft, 2018, and references therein). Mixing relationships can be ideal, symmetrical, or
175 asymmetrical, depending on the behavior of the Margules parameter pair. The excess Gibbs
176 energy is normally a function of temperature and pressure. We discuss the $a-X$ relations (and the
177 elements considered) that were used in this work in the next section and other details are given in
178 the Supplementary Table S1.

179 One approach to calculate phase equilibria is by solving simultaneous non-linear
180 equations to build up an array of points and lines that make up the phase diagram by using
181 Schreinemakers' analysis (e.g., THERMOCALC; Powell et al., 1998), whereas another approach
182 is Gibbs free energy minimization to determine the most stable phase assemblage at specific state
183 points. This second approach is used in the MELTS package (Ghiorso and Sack, 1995; Asimow

184 and Ghiorso, 1998; Gualda et al., 2012; Ghiorso and Gualda, 2015) and in Theriak-Domino and
185 Perple_X (Connolly, 2005; de Capitani and Petrakakis, 2010).

186

187

PETROLOGICAL MODELING

188 **Modeling setups**

189 Phase equilibria calculations for this study were performed using rhyolite-MELTS and Theriak-
190 Domino in the $\text{Na}_2\text{O}-\text{CaO}-\text{K}_2\text{O}-\text{FeO}-\text{MgO}-\text{Al}_2\text{O}_3-\text{SiO}_2-\text{H}_2\text{O}-\text{TiO}_2-\text{O}_2$ (NCKFMASHTO)
191 system. This system was chosen because the HPx-mb16 model was calibrated in this 10-
192 component system (Green et al., 2016), which is also appropriate for rhyolite-MELTS.

193 For the rhyolite-MELTS runs, we used the internally consistent thermodynamic database
194 of Berman (1988) with some modifications (Gualda et al., 2012; Ghiorso and Gualda, 2015) and
195 the $a-X$ relations for solid-solution phases included in the rhyolite-MELTS calibration
196 (Supplementary Table S1), i.e., silicate liquid (Ghiorso and Sack, 1995); pyroxene (Sack and
197 Ghiorso, 1994); orthopyroxene, biotite, olivine (Sack and Ghiorso, 1989); amphibole (Ghiorso et
198 al., 1995); garnet (Berman, 1990; Berman and Koziol, 1991); feldspar (Elkins and Grove, 1990);
199 spinel (Sack and Ghiorso 1991a, b); and rhombohedral oxide (Ghiorso, 1990; Ghiorso and Sack,
200 1991; Ghiorso and Evans, 2008). Note that, despite its name, rhyolite-MELTS is meant for
201 modeling mafic systems and the prefix “rhyolite” only refers to the latest calibration that is more
202 suitable also for felsic systems than the preceding MELTS versions (Gualda et al., 2012;
203 <http://melts.ofm-research.org>).

204 For the Theriak-Domino runs, we utilized the Theriak-Domino version from D. K.
205 Tinkham (<https://dtinkham.net/peq.html>), the internally consistent thermodynamic database ds62
206 (Holland and Powell, 2011), and the “metabasite set” of $a-X$ relations for solution phases

207 (Supplementary Table S1) from Green et al. (2016); these include: liquid, augite and
208 clin amphibole (Green et al., 2016); garnet, biotite, chloritoid, muscovite–paragonite, and
209 chlorite (White et al., 2014); epidote (Holland and Powell, 2011); plagioclase (Holland and
210 Powell, 2003); magnetite–spinel (White et al., 2002); and ilmenite–hematite (White et al., 2000).
211 Pure phases include albite, quartz, rutile, and titanite.

212 In all comparative calculations in this study, we computed equilibrium state points only;
213 fractionation was not used except as a preliminary step in rhyolite-MELTS to determine the
214 appropriate version of rhyolite-MELTS. Hence our calculations apply equally to equilibrium
215 crystallization and equilibrium partial melting as these processes are thermodynamically
216 identical.

217 The wide P – T – X ranges of the modeling software enable near-infinite possibilities for
218 model comparison. Here, we focus on a detailed comparison of one of the most widely used
219 average compositions in petrological modeling, that of the mean N-MORB from Gale et al.
220 (2013) (Table 1). Modeling intermediate and/or felsic systems is outside of the scope of this
221 study. To explore the effects of H₂O in our calculation, we utilized two initial H₂O-contents: 0.5
222 wt% and 4 wt% to account for relatively dry and wet conditions. The oxygen chemical potential
223 was controlled by imposing the FMQ buffer in all calculations.

224 Calculations were carried out at 0.25 GPa and 1 GPa, which approximate upper and
225 lower crustal conditions, and were calculated isobarically over the temperature interval between
226 600 °C to the liquidus temperature (calculated by rhyolite-MELTS) in discrete steps. In rhyolite-
227 MELTS, the FMQ buffer is not maintained below the solidus, and thus, results below such
228 conditions are not discussed in this study.

229

230 **Comparison methodology**

231 We performed a comparison using four sets of conditions. These include: (1) a low-*P*–low-H₂O
232 run (i.e., at 0.25 GPa and 0.5 wt% H₂O), (2) a low-*P*–high-H₂O run (i.e., at 0.25 GPa and 4 wt%
233 H₂O), (3) a high-*P*–low-H₂O run (i.e., at 1 GPa and 0.5 wt% H₂O), and (4) a high-*P*–low-H₂O
234 run (i.e., at 1 GPa and 4 wt% H₂O). All calculations were carried out at discrete temperatures
235 spanning the solidus to liquidus (or near-liquidus) temperatures along the selected pressures. As
236 noted earlier, the equilibrium (closed system) states computed apply to both crystallization and
237 melting, because at equilibrium, the liquid–solid–fluid relationships are the same for closed-
238 system melting or crystallization. Thus, we emphasize that although the calculations (and Figs. 1,
239 2, and 4–7) proceed up temperature from near-solidus toward near-liquidus (i.e., equilibrium
240 partial melting), the calculations are equally applicable to down-temperature equilibrium
241 crystallization since there is no fractionation of solids from liquid.

242 Because there are several versions of rhyolite-MELTS, we followed the decision tree on
243 the rhyolite-MELTS website (<http://melts.ofm-research.org/LIQUIDS-decision-tree.html>) in
244 order to choose the appropriate version for each calculation. All the rhyolite-MELTS runs were
245 calculated with the version v1.2.0 with the exception of the low-*P*–high-H₂O run (i.e. at 0.25
246 GPa and 4 wt% H₂O), where v1.1.0 was used.

247 Phase modal proportions are shown using mode boxes, which include the calculated
248 normalized mass proportions (wt%) of all predicted phases at each calculated state point (Figs. 1
249 and 2; mineral proportions in vol% are also shown in Supplementary Figures S1–S2). When
250 more than one phase of the same solid solution were stable at a single state point (e.g., two
251 clinopyroxenes predicted by rhyolite-MELTS), the phase masses were combined for simplicity.
252 Calculated modal proportions are given in Table 2 every 100 °C from 900 (or 800 °C) to 1100

253 °C. The detailed description of the calculated phase equilibria evolution for the four scenarios is
254 given in Appendix 1.

255 Liquid compositions are reported from the liquidus (calculated with rhyolite-MELTS) or
256 near liquidus (HPx-mb16) to the solidus (Figs. 3–7). Given that the rhyolite-MELTS liquid $a-X$
257 model, in contrast to the Green et al. (2016) liquid $a-X$ model, considers both FeO and Fe₂O₃,
258 the Fe content of the calculated compositions was recalculated to FeO^t allowing for direct
259 comparison. Liquid compositions are given in Tables S2 and S3 every 100 °C from 900 (or 800
260 °C) to 1100 °C . Compositions are reported in the table only when liquid is stable in both
261 rhyolite-MELTS and HPx-mb16 models at the same $P-T$ conditions. The full liquid
262 compositional evolution is described in Appendix 1.

263 In addition to providing a first-order comparison of the phase relations and liquid
264 compositions, we also compare compositions of clinopyroxene, feldspar, orthopyroxene,
265 amphibole and garnet, which are the most abundant minerals. A detailed description of the phase
266 compositions at each state point can be found in the Appendix 1 and in Supplementary Figures
267 S3–S6. Only the most significant mineral-compositional differences and characteristics are
268 presented and discussed in the sections below.

269

270 **Models caveats**

271 Both of the thermodynamic models used here (i.e., rhyolite-MELTS and HPx-b16) have
272 significant caveats, limitations, and uncertainties, mainly related to the thermodynamic data and
273 the $a-X$ models. A detailed discussion is beyond the scope of this paper; the reader is referred to
274 the original works and developers' websites to find important information related to the models
275 (rhyolite-MELTS, <http://melts.ofm-research.org>; HPx-mb16, <https://hpxeosandthermocalc.org>).

276 Below, we only outline the calibration ranges where the thermodynamic models should yield
277 reliable results and some important caveats pertinent to our comparison work.

278 Rhyolite-MELTS is recommended for modeling relatively dry mafic and hydrous silicic
279 systems at < 2 GPa. Phase equilibria calculations via rhyolite-MELTS are not recommended at
280 conditions close to the solidus (and subsolidus) and/or for intermediate and calc-alkaline systems
281 with modally significant amphibole, muscovite, and biotite (<http://melts.ofm-research.org>;
282 Gualda et al., 2012). Rhyolite-MELTS calculations are further recommended for volcanic
283 systems where the melt fraction is > 50 wt% (Gualda et al., 2012).

284 Calculations with the HPx-mb16 model are recommended for modeling partial melting of
285 hydrous metabasites at < 1.3 GPa. Reliable phase equilibria can be calculated at subsolidus and
286 suprasolidus conditions up to ~1050 °C (Green et al., 2016; Palin et al., 2016); yet, modeling
287 phase equilibria near- or at the liquidus is not recommended as the liquid $a-X$ model accounts for
288 neither Fe₂O₃ and TiO₂.

289

290

MODEL COMPARISON

291 Differences in the calculated phase proportions

292 Overall, rhyolite-MELTS calculates more liquid at higher temperatures (closer to the liquidus)
293 but less liquid at lower temperatures (closer to the solidus) compared to HPx-mb16 (Figs. 1 and
294 2). For example, in the low- P -low-H₂O run at 1100 °C, rhyolite-MELTS predicts ~33 wt%
295 liquid, whereas HPx-mb16 predicts ~50 wt% liquid (~36 vol% and ~53 vol%, respectively; Figs.
296 1a and c; Fig. S1a and c; Table 2). The position of the solidi vary depending on pressure between
297 the two models as well. In the low- P runs, the solidus is located at higher temperature (e.g., ~850
298 °C vs ~730 °C in the high-H₂O run; Figs. 1b and d) whereas in the high- P run, it is located at

299 lower temperature (e.g., ~760 °C vs ~890 °C in the low-H₂O run; Figs. 2a and c) in rhyolite-
300 MELTS compared to HPx-mb16. In all the calculations, a higher H₂O content decreases the
301 solidus temperature (Figs. 1 and 2).

302 Clinopyroxene and plagioclase stabilities are expanded to higher temperatures in HPx-
303 mb16 regardless of the conditions (Figs. 1 and 2). At temperatures closer to the solidus, rhyolite-
304 MELTS predicts higher amounts of these phases, and the specific temperatures where rhyolite-
305 MELTS predicts more of these phases depend on the specific run (Figs. 1 and 2; Table 2). For
306 example, in the low-*P*-high-H₂O run at 900 °C, rhyolite-MELTS predicts ~32 wt% of
307 clinopyroxene and ~27 wt% of plagioclase (~24 vol% and ~26 vol%, respectively), whereas
308 HPx-mb16 predicts ~21 wt% clinopyroxene and ~22 wt% plagioclase (~16 vol% and ~21 vol%,
309 respectively) (Figs. 1b and d; Fig. S1b and d; Table 2). Plagioclase proportion is systematically
310 higher in rhyolite-MELTS at any given temperature in the low-*P* runs. For example, at 830 °C in
311 the low-*P*-high-H₂O run, rhyolite-MELTS calculates ~46 wt% of plagioclase whereas HPx-
312 mb16 predicts ~25 wt% (~43 vol% and ~25 vol%, respectively; Figs. 1b and d; Fig. S1b and d).
313 By contrast, in the high-*P* runs, plagioclase systematics are different; in the low-H₂O run
314 rhyolite-MELTS calculates less amount of plagioclase compared to HPx-mb16, whereas in high-
315 H₂O run, only HPx-mb16 predicts plagioclase (Fig. 2; Table 2).

316 Orthopyroxene and olivine proportions are systematically higher in the rhyolite-MELTS
317 low-*P* runs compared to HPx-mb16 low-*P* runs (Fig. 1); olivine stability is typically expanded to
318 higher temperatures in rhyolite-MELTS compared to HPx-mb16. In the low-*P*-low-H₂O run,
319 olivine is not stable in rhyolite-MELTS but predicted in a small temperature window in the HPx-
320 mb16 calculation (Fig. 1). By contrast, in the high-*P* runs, orthopyroxene and olivine are not
321 stable except orthopyroxene only in the low-H₂O HPx-mb16 run.

322 A crucial systematic difference at all P - T - H_2O conditions is the stability of amphibole.
323 HPx-mb16 predicts amphibole in all runs; the amount of amphibole increases with increasing
324 pressure and H_2O (Figs. 1c, 1d, 2c, and 2d; Table 2). By contrast, in the rhyolite-MELTS
325 calculations, amphibole is only predicted in the high- P -high- H_2O run (Fig. 2b). The amount of
326 amphibole, and its temperature-interval of stability, are not comparable with HPx-mb16 (Figs.
327 2b-d). For example, in the high- P -high- H_2O run at 700 °C, rhyolite-MELTS predicts ~2 wt% of
328 amphibole compared to ~63 wt% in HPx-mb16 (~1 vol% and ~57 vol%, respectively; Figs. 2b
329 and d; Fig. S2b and d). At 600 °C in the same run, the modal difference remains considerable:
330 rhyolite-MELTS predicts ~22 wt% of amphibole whereas in HPx-mb16 modal amphibole is ~66
331 wt% (~20 vol% and ~61 vol%, respectively; Figs. 2b and d; Fig. S2b and d).

332 Garnet is only stable in the high- P runs in both models. Its stability is systematically
333 expanded to higher temperature and the proportion is greater in rhyolite-MELTS compare to
334 HPx-mb16 (Fig. 2). For instance, in the high- P -low- H_2O run at 800 °C, rhyolite-MELTS
335 predicts ~32 wt% of garnet whereas HPx-mb16 predicts ~15 wt% (~27 vol% and ~12 vol%,
336 respectively; Figs. 2a and c; Fig. S2a and c; Table 2). Unexpectedly, higher H_2O increases the
337 proportion of garnet in rhyolite-MELTS (Figs. 2a and b). On the other hand, follows the opposite
338 trend relative to H_2O (Figs. 2c and d), i.e., a higher H_2O inhibits garnet stabilization.

339 Other minor phases such as quartz and Fe-Ti oxides also show differences between the
340 models (Figs. 1 and 2). Quartz is predicted at relatively similar temperatures (± 50 °C) but is
341 systematically higher in proportion in rhyolite-MELTS in the low- H_2O runs but lower in the
342 high- H_2O runs (Figs. 1 and 2). By contrast, proportions of Fe-Ti oxides are relatively similar (± 2
343 wt%), although the predicted phase is always different in the low- P runs: rhyolite-MELTS

344 predicts a spinel group phase (ulvospinel–magnetite) whereas HPx-mb16 predicts rutile that is
345 replaced by ilmenite at lower temperature (Figs. 1 and 2).

346 The models predict H₂O-saturation conditions at different *P–T* conditions (Figs. 1 and 2).
347 In the low-*P*–low-H₂O run, H₂O-saturated conditions are only attained in rhyolite-MELTS (Fig.
348 1a). By contrast, in the low-*P*–high-H₂O run, all calculations reach H₂O-saturated conditions,
349 although H₂O as a phase occurs at higher temperatures and in lower proportion in HPx-mb16
350 (Figs. 1b and d). In the small temperature interval where H₂O is in excess in HPx-mb16 but not
351 in rhyolite-MELTS (i.e., ~1100–1000 °C; Figs. 1b and d), the liquid proportion is higher in
352 rhyolite-MELTS (Figs. 1b and d). In the high-*P* runs, H₂O-saturated conditions are only reached
353 in the high-H₂O run in both models (Figs. 2b and d). Similar to the low-*P* runs, H₂O occurs at
354 slightly higher temperatures in HPx-mb16 runs (Figs. 2b and d).

355 In all our calculations, there are four phases that are only stable in either rhyolite-MELTS
356 or in HPx-mb16. These are analcime (only predicted by rhyolite-MELTS) and epidote, titanite,
357 and rutile (only predicted by HPx-mb16). (Figs. 1 and 2).

358

359 **Differences in the calculated phase compositions**

360 **Liquid compositions.** The calculated silicate liquids follow relatively similar compositional
361 trends as a function of temperature (Fig. 3); changes in liquid composition are controlled by the
362 crystallization or consumption of phases which, as noted above, differ between models.

363 Generally, high-*T* liquid compositions are relatively similar in SiO₂ but for most
364 calculations, diverge at lower temperatures. In the low-*P*–low-H₂O run, where the SiO₂ is
365 enriched in HPx-mb16 at high temperatures compared to the liquid predicted by rhyolite-MELTS
366 (Fig. 4a). At lower temperatures in the low-H₂O runs, HPx-mb16 liquid compositions are SiO₂-

367 depleted compared to rhyolite-MELTS (up to ~5 wt%; Figs. 4a and 6a); by contrast, in the high-
368 H₂O runs, the HPx-mb16 liquid compositions are SiO₂-enriched compared to rhyolite-MELTS
369 (up to ~16 wt%; Figs. 5a and 7a). The liquid SiO₂ contents in the low-*P*-high-H₂O runs in
370 rhyolite-MELTS and HPx-mb16 are almost identical (Fig. 5a)

371 Calculated liquids are systematically—and substantially—more mafic in the HPx-mb16
372 than in rhyolite-MELTS (up to ~18 wt% higher in the high-*P*-low-H₂O run at 1080°C; Fig. 6c).
373 Liquid FeO^t + MgO in HPx-mb16 shows a distinct enrichment at high temperatures that is not
374 observed in rhyolite-MELTS (Figs. 4c, 5c, 6c, and 7c). These changes are less significant as the
375 H₂O content increases at the same pressure (Figs. 4c and 5c); the high-*P*-high-H₂O run show the
376 least difference in liquid FeO^t + MgO (Fig. 7c).

377 The liquid CaO and H₂O contents have similar compositional trends in both models, and
378 tend to be higher in rhyolite-MELTS. The relative difference in the CaO and H₂O contents is
379 greater in the low-*P* runs (up to 5 wt% in CaO and ~4 wt% in H₂O Figs. 4f and 5f); by contrast,
380 in the high-*P* runs, the difference in the liquid CaO and H₂O content is smaller (Figs. 6f and 7f).
381 In all the runs, the H₂O liquid content tend to diverge the most at lower temperatures (Figs. 4f,
382 5f, 6f, and 7f).

383 Liquid Al₂O₃ and alkali contents are relatively different between the models throughout.
384 The liquid Al₂O₃ content follow different trends in all the runs (Figs. 4b, 5b, 6b, and 7b); the
385 alkali content are relatively similar in all the low-*P* runs (Figs. 4d and 5d). In the high-*P* runs,
386 within 1200–900 °C (in the low-H₂O content run) and 1100–750 °C (in the high-H₂O content
387 run), rhyolite-MELTS calculated liquid composition is greater in the alkali contents compared to
388 the HPx-mb16 liquid composition (up to 2–3 wt%; Figs. 6d and 7d).

389 Overall, liquid compositions show the greatest difference at lower temperatures, closer to
390 the solidus: the low-*P* runs are the most similar (especially CaO and alkalis; Figs. 4 and 5),
391 whereas in the high-*P* runs, compositional differences are more distinct (especially in the case of
392 SiO₂, Al₂O₃, and H₂O; Figs. 6 and 7).

393

394 **Mineral compositions.** Details of the mineral chemical evolution and the results derived from
395 both models can be found in Appendix 1 and in the Supplementary Figures S2–S5. Among the
396 most important differences is that the clinopyroxene shows similar Mg# [Mg# = Mg/(Fe²⁺ +
397 Mg)] at temperatures near the liquidus, but with decreasing temperature, rhyolite-MELTS
398 predicts higher clinopyroxene Mg# values compared to HPx-mb16 in all runs. Plagioclase
399 anorthite content is systematically higher in HPx-mb16 at any temperature compared to rhyolite-
400 MELTS in all the runs. In the high-*P* runs, garnet Mg# values are systematically higher in
401 rhyolite-MELTS compared to HPx-mb16 at any given temperature; almandine and grossular
402 contents are systematically higher and pyrope contents lower in HPx-mb16. Calculated
403 amphibole compositions are substantially different between rhyolite-MELTS and HPx-mb16,
404 reflecting the complexity and difficulty modeling *a*-*X* relations in multisite-multicomponent
405 amphibole phases using available experimental data (Supplementary Table S4). The Si, Mg# and
406 Ca contents are systematically higher in rhyolite-MELTS than in HPx-mb16 at any given
407 temperature in the high-*P*–high-H₂O run.

408

409 **TRACE-ELEMENT SIGNATURES OF MODEL LIQUIDS**

410 Here, we explore the effect of calculated phase relations on the trace-element signatures of the
411 liquids. We used calculated liquid and solid fractions (Supplementary Table S5) along with

412 liquid–mineral partition coefficients to model the liquid trace-element signatures at (1) 900 °C in
413 the low-*P*–low-*H*₂O run, (2) 1000 °C in the high-*P*–low-*H*₂O run, and (3) 850 °C in the high-*P*–
414 high-*H*₂O run. These three scenarios were selected because of the markedly different predicted
415 equilibria between the models. Trace-element modeling was performed at the given state point
416 using mass balance equations found elsewhere (e.g., Shaw, 2006; Spera et al., 2007). A wide
417 selection of variably incompatible trace elements was chosen, and partition coefficients were
418 from Bédard (2006) (Supplementary Table S6). To highlight the similarities and differences in
419 trace element signatures resulting solely from phase assemblage differences, constant liquid–
420 mineral partition coefficients (for each mineral) were used. The starting bulk trace-element
421 composition was that of mean N-MORB from Gale et al. (2013). The results are given in Table 3
422 and illustrated in normalized incompatible trace-element diagrams and REE diagrams in Figure
423 8.

424 In the low-*P*–low-*H*₂O run at 900 °C, the stable phase assemblage predicted by rhyolite-
425 MELTS is liquid–plagioclase–orthopyroxene–clinopyroxene–magnetite (Fig. 1c). The calculated
426 liquid trace-element pattern (Figures 8a and b) is relatively enriched in Ta and Zr, and depleted
427 in Ba, Pb, Sr, Eu, and Ti. The liquid composition is further characterized by a low Sr/Y ratio
428 (Sr/Y = 0.44; Table 3), and is not strongly fractionated in REE (La/Yb = 1.86; Table 3). The
429 chondrite-normalized REE pattern shows a strong negative Eu anomaly ($\text{Eu}/\text{Eu}^* = [\text{Eu}/(\text{Sm} \times$
430 $\text{Nd})^{0.5}] = 0.07$; Table 3), and is characterized by a flat heavy-REE (HREE) slope (Yb/Gd = 0.62;
431 Table 6). The calculated paragenesis using HPx-mb16 is liquid–plagioclase–amphibole–
432 orthopyroxene–clinopyroxene–ilmenite (Fig. 1c). While the HPx-mb16 liquid compositions
433 show relatively lower concentrations of all the considered trace elements, most of trace elements
434 are similar to those calculated with rhyolite-MELTS. Exceptions are Ta, Gd and Tb which are

435 much lower in concentration in HPx-mb16. The liquid composition is characterized by low Sr/Y
436 (Sr/Y = 0.76) and La/Yb (La/Yb = 2.26) ratios (Table 3), a strong Eu negative anomaly (Eu/Eu*
437 = 0.12; Table 3), and a flat HREE slope (Yb/Gd = 0.78; Table 3).

438 In the high-*P*–low-H₂O run, the stable phase assemblage at 1000°C for the rhyolite-
439 MELTS run is liquid–plagioclase–clinopyroxene–garnet (Fig. 2c). The calculated trace-element
440 compositions are shown in Figures 8c and d. The liquid incompatible trace-element pattern is
441 slightly enriched in Ta and Ti but depleted in Ba and Sr, and further characterized by a moderate
442 Sr/Y ratio (Sr/Y = 10.93; Table 3). It is also strongly fractionated in light to heavy REE (La/Yb =
443 35.24; Table 3) because garnet is a stable phase. The REE pattern does not show a negative Eu
444 anomaly (Eu/Eu* = 0.30; Table 3), and is characterized by a steep HREE slope (Yb/Gd = 0.18;
445 Table 3). The paragenesis in HPx-mb16 is liquid–plagioclase–amphibole–orthopyroxene–
446 clinopyroxene–ilmenite (Fig. 2c). The incompatible trace-element pattern of HPx-mb16 is
447 similar to that of rhyolite-MELTS for highly incompatible elements, but there are significant
448 differences in terms of Eu, Gd, Ta, and HREE; the liquid composition is also characterized by a
449 low Sr/Y ratio (Sr/Y = 0.80; Table 3). The REE pattern is not fractionated (La/Yb = 2.12; Table
450 6), shows a strong negative Eu anomaly (Eu/Eu* = 0.12; Table 3), and is enriched in HREE
451 (Yb/Gd = 0.72; Table 3).

452 In the high-*P*–high-H₂O run at 850 °C, the paragenesis predicted by MELTS is liquid–
453 clinopyroxene–garnet (Fig. 2d). The calculated trace-element compositions are shown in Figures
454 8e and f. The calculated incompatible trace-element pattern is slightly enriched in Pb, Sr, and Ti
455 and slightly depleted in Th. The liquid composition has a high Sr/Y ratio (Sr/Y = 142.48; Table
456 3) and is strongly fractionated in LREE/HREE (La/Yb = 74.96; Table 3) due to residual garnet.
457 The REE pattern further shows a small positive Eu anomaly (Eu/Eu* = 0.48; Table 3), and is

458 characterized by a steep HREE slope ($Yb/Gd = 0.17$; Table 3). The calculated paragenesis in
459 HPx-mb16 is liquid–amphibole–orthopyroxene–clinopyroxene–garnet–titanite (Fig. 2d). The
460 incompatible trace-element pattern is depleted in highly incompatible elements but enriched in
461 more compatible elements relative to that of the rhyolite-MELTS liquid. The pattern is further
462 characterized by a slight enrichment in Pb, Sr, and Zr and depletion in Ti; the liquid composition
463 has a moderate Sr/Y ratio ($Sr/Y = 12.07$; Table 3). The REE pattern is not fractionated ($La/Yb =$
464 3.54 ; Table 3), does not show an Eu negative anomaly ($Eu/Eu^* = 0.37$; Table 3), and is enriched
465 in HREE ($Yb/Gd = 0.81$; Table 3).

466

467 **Contrasting liquid trace-element signatures: the effect of contrasting mineral assemblages**

468 As discussed in the previous sections, both models yield significant differences in calculated
469 phases and their relative abundances. Unsurprisingly, this directly affects the trace-element
470 signatures of the liquids. For example, partitioning of Ba, Sr, and Eu into plagioclase (Gromet
471 and Silver, 1983), means that the increase of plagioclase stability at higher temperatures in HPx-
472 mb16 relative to rhyolite-MELTS and the differences in plagioclase proportion will lead to
473 differences in the concentrations of the Ba, Sr, and Eu in liquids in equilibrium with their
474 associated crystals at each state point (Fig. 8; Table 3). The considerable effect of the discordant
475 phase equilibria on the trace-element budget is also well illustrated by the contrasting garnet
476 stabilities in the different models. Garnet is more stable in all rhyolite-MELTS calculations, and
477 since it is an important HREE repository (e.g., Bea et al., 1994), its fractionation causes notable
478 HREE depletions in the corresponding rhyolite-MELTS liquid compositions (Fig. 8; Table 3).

479 The HPx-mb16 trace-element patterns always show negative Ti anomalies, whereas
480 trace-element patterns of rhyolite-MELTS calculations only show negative Ti anomalies in the

481 high-*P*–low- H_2O case (Fig. 8; Table 3). The negative Ti anomalies in HPx-mb16 trace-element
482 patterns are controlled by partitioning of Ti into titanite, ilmenite, and amphibole (where
483 present), whereas such phases are never stable in rhyolite-MELTS calculations. In the only
484 example where there is a negative Ti anomaly (Fig. 8; Table 3) in rhyolite-MELTS, the main Ti
485 repository is magnetite.

486 A key difference in the mineral assemblage predicted by rhyolite-MELTS and HPx-mb16
487 models is the presence of amphibole. This mineral has relatively high partition coefficients for
488 MREE and HREE (Table S6; Bédard, 2006) likely accounting for the depletion in MREE and
489 HREE contents in amphibole-rich HPx-mb16 calculations compared to those of rhyolite-
490 MELTS, as well as to HPx-mb16 calculations with less amphibole (Fig. 8; Table 3).

491 Other trace elements (e.g., Cs, Rb, Th, U, and light-REE) are mainly incompatible to the
492 solid phases present in the calculations, thus the concentrations in the melt are only slightly
493 affected by the choice of the thermodynamic model (Fig. 8; Table 3). Rather subtle relative
494 differences in their concentrations can be observed in the high-*P*–high- H_2O run (Fig. 8; Table 3).
495 Highly incompatible elements may thus generally represent better proxies to model
496 crystallization or anatectic processes with both rhyolite-MELTS and HPx-mb16, since they are
497 less prone to differ significantly with model choice.

498

499 **COMPARING MODELS TO PETROLOGICAL EXPERIMENTS**

500 To further assess the robustness of the phase equilibria models, we compared model predictions
501 with results from low- and high-*P* petrological experiments. We selected the experimental
502 studies of Berndt et al. (2005) and Sen and Dunn (1994) as benchmarks for the comparison. We
503 used the synthetic MORB B1 composition from Berndt et al. (2005) and compared the phase

504 equilibria at 0.2 GPa and 950 °C and 1000 °C. These conditions correspond to their runs 148 and
505 153 (their Table 3c). The data in Berndt et al. (2005) were not used in either rhyolite-MELTS or
506 HPx-mb16 calibrations. In addition, we utilized the natural basaltic amphibolite from the Sen
507 and Dunn (1994) experiment and compared the phase equilibria at 1.5 GPa and 975 °C and 1025
508 °C. These conditions correspond to their runs B17 and M2 (their Table 2). Although data from
509 Sen and Dunn (1994) were not used to calibrate HPx-mb16, Sen and Dunn data did form a very
510 small part of the data used to calibrate rhyolite-MELTS (Ghiorso et al., 2002). The Berndt et al.
511 (2005) experiments considered oxygen fugacities corresponding to the FMQ buffer whereas the
512 Sen and Dunn (1994) oxygen fugacity corresponds to FMQ = + 0.5. Here, for simplicity,
513 calculations with both rhyolite-MELTS and HPx-mb16 were run along the FMQ buffer. Phase
514 proportions from the Berndt et al. (2005) and Sen and Dunn (1994) experiments as well as phase
515 equilibria calculations with rhyolite-MELTS (v1.2.0) and HPx-mb16 are shown in Figure 9 and
516 given in Table 4; experimental and calculated liquid compositions are given in Table 5.

517

518 **MORB B1 of Berndt et al. (2005)**

519 Phase equilibria at 950 °C slightly differs between the models and experiment 153 (Fig. 9a;
520 Table 4). Liquid–olivine–clinopyroxene–plagioclase–amphibole–H₂O is the observed
521 paragenesis in the experiment. Rhyolite-MELTS differs from the experiment in that it stabilizes
522 orthopyroxene and a small amount of magnetite but not amphibole. HPx-mb16 stabilizes
523 amphibole, clinopyroxene, and plagioclase as in the experiment but with additional
524 orthopyroxene and a small amount of ilmenite and no olivine. The liquid proportion in the
525 experiment is similar to that predicted in HPx-mb16 but significantly lower in rhyolite-MELTS.
526 Clinopyroxene and plagioclase proportions are relatively similar in HPx-mb16 compared to the

527 experiment; rhyolite-MELTS predicts higher proportions of these phases than both HPx-mb16
528 and the experiment. The olivine proportion is higher in the rhyolite-MELTS model compared to
529 the experiment. On the other hand, the proportion of amphibole observed in the experiment is
530 similar to that predicted by HPx-mb16. In general, HPx-mb16 is able to better reproduce the
531 phase relations from the experiment 153. The rhyolite-MELTS liquid composition is relatively
532 similar to that of the experiment in terms of MgO and CaO contents whereas the HPx-mb16
533 liquid composition is in relative agreement with regards to all the other major oxides (Table 5).
534 Significant differences include the MgO and K₂O contents; for instance, the liquid's MgO
535 content in rhyolite-MELTS is within ~5% of the experiment whereas the K₂O content is within
536 ~382% of the experiment. By contrast, the the HPx-mb16 calculated MgO content is within
537 ~115% of the experiment whereas the K₂O content is within ~74% of the experiment. Note that
538 the large relative difference in the K₂O content is exacerbated by low K₂O contents.

539 At 1000 °C, the rhyolite-MELTS and HPx-mb16 models, and the experiment 148 of
540 Berndt et al. (2005) show the same phase assemblage, melt–olivine–clinopyroxene–plagioclase–
541 H₂O, with the exception of a very small amount of ilmenite that is predicted in HPx-mb16.
542 However, the phase proportions are somewhat different (Fig. 9b; Table 4); both rhyolite-MELTS
543 and HPx-mb16 predict considerably less liquid than observed in the experiment, and both models
544 predict more plagioclase. Rhyolite-MELTS predicts slightly more olivine than measured in the
545 experiment whereas the HPx-mb16 predicts slightly less olivine than in the experiment. Modeled
546 and experimental clinopyroxene proportions are similar. Overall, rhyolite-MELTS is able to
547 better reproduce the phase equilibria from experiment 148. The HPx-mb16 calculated liquid
548 composition is relatively similar to that of the experiment in terms of SiO₂, Al₂O₃, and H₂O
549 contents, whereas the rhyolite-MELTS liquid composition is in reasonable agreement with the

550 experiment for all the other major oxides (Table 5). Important differences in the compositions
551 include the MgO and K₂O contents; for example, the MgO liquid content in rhyolite-MELTS is
552 within ~3% of the experiment whereas the liquid's K₂O content is within ~38% of the
553 experiment. On the other hand, the HPx-mb16 calculated liquid MgO content is within ~74% of
554 the experiment and the K₂O content within ~51% of the experiment.

555

556 **Natural basaltic amphibolite of Sen and Dunn (1994)**

557 The stable phase assemblage in the 975 °C experiment M2 is liquid–clinopyroxene–plagioclase–
558 amphibole–garnet–rutile. Rhyolite-MELTS model does not stabilize plagioclase, amphibole, or
559 rutile, whereas HPx-mb16 stabilizes the same experimental phase assemblage with the exception
560 of plagioclase (Fig. 9c; Table 4). Phase proportions are relatively different between both models
561 and the experiment; the calculated liquid fractions are considerably higher than in the
562 experiment. The calculated clinopyroxene proportion in HPx-mb16 is similar to that in the
563 experiment but considerably higher in rhyolite-MELTS. Similarly, the garnet proportions
564 predicted by both models are significantly higher than in the experiment. The calculated
565 amphibole proportion in HPx-mb16 is relatively less than in the experiment. Rutile occurs as
566 minor phase in both HPx-mb16 and the experiment. In general, HPx-mb16 better reproduces the
567 phase relations at 975 °C. The rhyolite-MELTS liquid composition is relatively similar to that of
568 the experiment in terms of FeO^t and MgO liquid contents whereas the HPx-mb16 liquid
569 composition is in relative agreement with the experiment for all the other major oxides (Table 5).
570 Significant differences include the FeO^t and K₂O contents; for instance, the FeO^t liquid content
571 in rhyolite-MELTS is within ~29% of the experiment whereas the liquid K₂O content is within

572 ~86% of the experiment. On the other hand, the HPx-mb16 calculated FeO^{t} liquid content is
573 within ~73% of the experiment and the K_2O content is within ~32% of the experiment.

574 The observed paragenesis at 1025 °C in the Sen and Dunn (1994) experiment B17 is
575 liquid–clinopyroxene–amphibole–garnet–rutile. HPx-mb16 predicts the same phases, whereas
576 rhyolite-MELTS differs from the experiment in that it stabilizes neither amphibole nor rutile.
577 Proportions of most other phases are fairly similar between the computed models and the
578 experiment, although HPx-mb16 predicts relatively more liquid and less clinopyroxene (Fig. 9d;
579 Table 4). The proportion of garnet calculated with rhyolite-MELTS is considerably higher than
580 in the experiment, whereas HPx-mb16 predicts a relatively higher amount of garnet. The
581 amphibole proportion observed in the experiment is similar to that predicted by HPx-mb16.
582 Rutile occurs as a minor phase in both HPx-mb16 and the experiment. In general, HPx-mb16
583 better reproduces the phase relations of the experiment M2. The rhyolite-MELTS liquid
584 composition is relatively similar to that of the experiment in terms of SiO_2 , FeO^{t} , and MgO
585 contents, whereas the HPx-mb16 liquid composition is in relative agreement with all other major
586 element oxides (Table 5). Important differences include the FeO^{t} and Na_2O contents; for
587 example, the FeO^{t} liquid content in rhyolite-MELTS is within ~32% of the experiment whereas
588 the liquid Na_2O content is within ~79% of the experiment. By contrast, the HPx-mb16 calculated
589 FeO^{t} is within ~78% of the experiment and the liquid's Na_2O content within ~1% of the
590 experiment.

591

592

DISCUSSION

593 Although a minor oxide and therefore not as important as many of the major element oxides, the
594 lack of the TiO_2 component in the Green et al. (2016) liquid a - X relations precludes accurately

595 modeling phase equilibria at or near liquidus conditions using HPx-mb16 in the NCKFMASHTO
596 system. As TiO₂ cannot be incorporated into the liquid, there is always a Ti-bearing stable phase
597 at high-*T*; this, in turn, affects the overall phase equilibria including the liquid compositions. For
598 instance, rhyolite-MELTS predicts the liquidus at ~1340–1100 °C, whereas in the HPx-mb16
599 model is unable to model these conditions; clinopyroxene and/or plagioclase, and a Ti-bearing
600 phase are already present at the liquidus conditions predicted by rhyolite-MELTS (Figs. 1 and 2).
601 Recently, Holland et al. (2018) and Tomlinson and Holland (2021) published *a–X* relations for
602 relevant crystalline solutions enabling modeling of peridotitic to granitic liquids. This set of *a–X*
603 relations includes more complex liquid and clinopyroxene *a–X* relations (including TiO₂ and
604 Fe₂O₃ in the liquid, and TiO₂ and K₂O in the clinopyroxene) than in the *a–X* relations from HPx-
605 mb16. In the first instance, this set of *a–X* relations might represent a better approach to
606 modeling suprasolidus processes than HPx-mb16; yet, a recent study indicates that phase
607 equilibria calculated with the Holland et al. (2018) relations are not significantly different from
608 calculations performed with HPx-mb16; moreover, HPx-mb16 produces similar compositions
609 and better reproduces the FeO^l and MgO liquid contents from experiments than the Holland et al.
610 (2018) *a–X* relations (García-Arias, 2020).

611 When comparing our model predictions to experiments, rhyolite-MELTS and HPx-mb16
612 better reproduce phase equilibria within the *P–T* conditions in which they were calibrated to be
613 used. The phase equilibria predicted by rhyolite-MELTS are broadly similar to the high-*T*
614 experiments compared to those predicted by HPx-mb16 (Fig. 9; Tables 4 and 5); by contrast, at
615 temperatures less than ~1000 °C, HPx-mb16 provides more robust liquid-present phase
616 equilibria (Fig. 9; Tables 4 and 5) as it better reproduces the considered experiments compared to

617 rhyolite-MELTS. Importantly, as shown in some works (e.g. White et al., 2007; Green et al.,
618 2016), HPx-mb16 is able to accurately capture subsolidus equilibria.

619 One of the key differences between the rhyolite-MELTS and HPx-mb16 models is how
620 H₂O is partitioned in the liquid and hydroxyl (OH) in the crystalline phases. Amphibole is
621 predicted in HPx-mb16 calculations whereas amphibole stability and modal abundance are quite
622 limited in rhyolite-MELTS (Figs. 1 and 2; Table 2). In the calculations presented here, rhyolite-
623 MELTS partitions H₂O into liquid and/or analcime and/or a coexisting fluid phase (Figs. 1 and 2;
624 Table 2). These results illustrate the acknowledged limitation of rhyolite-MELTS in modeling
625 amphibole (and biotite)-bearing phase equilibria (<http://melts.ofm-research.org/>; Ghiorso and
626 Gualda, 2015). The HPx-mb16 model may therefore be the best choice to model equilibrium
627 melting and crystallization in scenarios where significant amounts of modal amphibole are
628 observed or predicted.

629 While not considered in our present study, the use of the HPx-mb16 model to study
630 fractional crystallization or any other open-system process would be relatively laborious for this
631 task with the current software available (i.e., Theriak-Domino, Perple_X, and THERMOCALC),
632 although several works using these software have successfully modeled open-system processes
633 (e.g., Yakymchuk and Brown, 2014; Kendrick and Yakymchuk, 2020; Stuck and Diener, 2020;
634 Johnson et al., 2021; Hernández-Montenegro et al., 2021)

635 Furthermore, it is important to note that recent comparative study assessing the
636 robustness of the Green et al. (2016) clinopyroxene and amphibole $a-X$ relations shows
637 discrepancies between the phase equilibria calculations and natural rocks in the proportions and
638 compositions (Forshaw et al., 2019; Santos et al., 2019); yet, our comparisons with the
639 experiments show that the difference in proportions are not as significant as suggested in those

640 studies. We argue that these different outcomes may be related to different bulk-rock
641 compositions used in the comparisons.

642

643

IMPLICATIONS

644 From the examples presented here, the lesson is clear: the modeling tool choice, and an
645 understanding of model constraints, uncertainties, and the similarities (and differences) among
646 models are critical to accurately convey the geological implications of a computational result.
647 Below, we highlight selected examples of how model choice can influence geologic
648 interpretations. The examples cited below are illustrative since we only present a small subset of
649 possible compositions and conditions, and yet, the underlying principal conclusion likely
650 remains relevant to all model-based studies of the magmatic evolution of the crust and upper
651 mantle.

652 HPx-mb16 and rhyolite-MELTS yield distinctly different minerals assemblages for some
653 of the runs. For example, at 850 °C in the low-*P*-high-H₂O run, the crystalline phases in
654 equilibrium with liquid predicted by rhyolite-MELTS correspond to a granulitic assemblage
655 whereas in HPx-mb16, an amphibolite-like assemblage is predicted (Figs. 1b and d). Similarly,
656 at 800 °C in the high-*P*-low-H₂O run, rhyolite-MELTS predicts a plagioclase-bearing garnet
657 pyroxenite crystalline assemblage whereas HPx-mb16 predicts a garnet amphibolite crystalline
658 assemblage (Figs. 2a and c; Table 2). As a consequence of the difference in amphibole stability,
659 the distribution of H₂O content among solid phases is different depending on the modeling tool.
660 This has important implications for modeling crustal anatexis and growth processes. For
661 example, the fertility (i.e., the potential to melt) of these solid assemblages will differ
662 significantly; amphibole dehydration melting of the amphibolitic cumulate would promote

663 greater liquid fractions (for the same pressure and temperature conditions) compared to the dry
664 granulitic and/or pyroxenite cumulate; different modeling approaches will lead to different
665 volumes of liquid, and thus in different crustal growth rates. The differences of the calculated
666 phases can also affect petrophysical properties such as density, seismic velocities, and thermal
667 conductivity (e.g., Carlson and Miller, 2004; Whittington et al, 2009). For example, at 900 °C in
668 the high-*P*–high-H₂O run (Figs. 2a and c; Table 2), the dry crystalline assemblage predicted by
669 rhyolite-MELTS (i.e., the garnet pyroxenite) has a significantly higher density ($\rho = 3.59 \text{ g/cm}^3$)
670 than the hydrated mineral assemblage predicted by the HPx-mb16 model ($\rho = 2.82 \text{ g/cm}^3$); such
671 differences may influence interpretations invoking crustal foundering via gravitational
672 instabilities which in turn may drastically affect the compositional stratification of the crust.
673 Differences in thermal diffusivity would also be expected between the hydrous and anhydrous
674 mineral assemblages, which would affect heat flow and the associated local geotherms. Thus, the
675 choice of modeling approach may yield different interpretations for the development of
676 chemical stratification of continental crust, the potential for crustal delamination, and the thermal
677 and rheological crustal structure.

678 Observed differences between the calculated liquid compositions may have important
679 implications for forward modeling of igneous processes. For instance, different calculated melt
680 compositions may lead to distinct liquid lines of descent representing different magma series
681 (Fig. 3; e.g., Carmichael et al, 1974). In the low-*P*–high-H₂O run, the HPx-mb16 liquid
682 composition produced by equilibrium crystallization follows a subalkaline tholeiitic trend
683 whereas the liquid calculated with rhyolite-MELTS evolves first along a subalkaline trend but
684 then follows an alkaline series trend when equilibrium crystallization is greater than 50%
685 complete (Fig. 3b). These model differences could lead to differences in, for example,

686 hypotheses about tectonic setting. Furthermore, our results show that calculated liquid
687 compositions diverge more at near-solidus temperatures, the difference being greater in the high-
688 *P* calculations (Fig. 3). These differences have implications for modeling processes such as
689 crustal assimilation because the composition of small degree (near solidus) anatectic melts can
690 have profound impact on the major and trace element, isotopic, and phase equilibria signatures of
691 crustally contaminated magmas (e.g., Bohrsen et al., 2014). Our results therefore concur with the
692 recognized limitation of thermodynamic modeling at “lower” temperatures, particularly using
693 rhyolite-MELTS (<http://melts.ofm-research.org/>) (e.g., rhyolite-MELTS is suggested to perform
694 best when a silicate liquid is present in the phase assemblage, as illustrated in the comparison
695 with the experiments (Fig. 9; Tables 4 and 5).

696 The difference in the calculated liquid compositions coupled with the calculated solid
697 fractions may significantly impact interpretation of tonalite-trondhjemite-granodiorite (TTGs)
698 and adakite petrogenesis. The major elements commonly used to identify and classify TTGs and
699 adakites (e.g., high Mg# and low K₂O/Na₂O) are some of the elements that vary the most
700 between the models. (Figs. 4–7), complicating their use in documenting the petrogenesis of such
701 rocks (e.g. Moyen, 2011; Palin et al., 2016; Hernández-Uribe et al., 2020). The solid assemblage
702 controls the trace-element liquid signature, which has been considered diagnostic of the source
703 depth and composition of the liquid (Moyen and Martin, 2012). TTGs are subdivided into high-,
704 medium-, and low-pressure groups based on the Sr/Y and La/Yb ratios, which are controlled by
705 garnet, plagioclase, rutile, and amphibole stabilities (Moyen, 2011; Moyen and Martin, 2012).
706 According to our results, the presence or absence, and abundance of such phases may vary
707 substantially between the two thermodynamic models examined here (Figs. 1 and 2; Table 2).
708 For example, garnet stability is increased in rhyolite-MELTS compared to HPx-mb16, whereas

709 plagioclase stability is expanded to higher temperatures in HPx-mb16 but generally predicted in
710 lower proportions (Figs. 1 and 2). Such differences could easily lead to contrasting trace-element
711 signatures (Table 3) and thus result in different explanations for tectonic environments of
712 formation for TTGs (e.g., slab melting during subduction vs. melting of a thickened crust; Martin
713 et al., 2014; Palin et al., 2016; Johnson et al., 2017). This emphasizes the need for careful
714 consideration of model limitations and uncertainties.

715 Statements about model performance are nuanced and must be thoughtfully considered
716 depending on the particular application under study, including the inherent geological
717 uncertainties not associated with the thermodynamic model *per se*. There may be cases where the
718 geological uncertainties are larger than the model uncertainties or vice versa. A careful parsing
719 of all uncertainties—intermodel, intramodel and geologic—is critical when applying
720 thermodynamic models to Earth systems.

721 The comparisons presented in this study are illustrative not exhaustive. We performed
722 equilibrium modeling using a single bulk composition (N-MORB) over a modest range of
723 pressures and bulk H₂O contents. We did not consider fractional or open-system processes, nor
724 other redox conditions; such comparisons are outside of the scope of a single paper. In felsic
725 and/or open systems, which often show considerably higher degrees of geochemical
726 heterogeneity, the differences between the models may be larger, especially when amphibole and
727 sheet silicate crystalline solutions are more abundant. We hope our work spurs additional work
728 including further comparative examination of other thermodynamic conditions (composition,
729 volatiles, redox, pressure, phase assemblages) and models.

730 From our limited set of comparative calculations, there are three major points. The first is
731 that our results show how the choice of petrological modeling tool can influence conclusions

732 about associated geological processes. We have shown that for the same model input (e.g., P – T –
733 H_2O), model choice may lead to different interpretations of crustal structure, density, and melting
734 systematics. The second point is that different models are better suited to modeling different P – T
735 ranges, and that studies such as ours are needed to highlight these differences for users more
736 comprehensively. For example, HPx-mb16 is likely better suited for modeling water-rich
737 systems with hydrous mineral phases (e.g., volcanic arc settings) at lower temperatures, whereas
738 rhyolite-MELTS may work better for drier systems at lower pressures and higher temperatures
739 (e.g., MORB and OIB's). Third, our work illustrates the importance of using multiple petrological
740 indicators to assess the efficacy of one model versus another. Major- and trace-element and
741 isotopic compositions of mineral phases as well as mineral proportions can enhance the choice of
742 a best-fit model compared to using melt compositional data only.

743 While the current thermodynamic databases and a – X relations for solid-solution phases
744 used in the igneous and metamorphic petrology communities provide a framework for forward
745 modeling of important igneous and metamorphic processes, the ultimate goal should be to
746 develop an internally consistent thermodynamic database and a – X relations applicable to both
747 subsolidus metamorphic processes as well as suprasolidus igneous and metamorphic processes.
748 This methodological development should proceed hand-in-hand with new petrological
749 experiments that fill the current gap in knowledge (especially at high pressure conditions) and
750 with a development of a user-friendly software with the capability to model the range of closed
751 and open-system processes that are relevant to igneous and metamorphic systems (e.g.,
752 equilibrium/fractional melting/crystallization and crustal assimilation). In parallel with model
753 development and enhancement, systematic comparative studies—such as the one presented
754 here—are necessary to thoroughly assess and test predictions from different models and to

755 compare to experimental and natural data. We hope our study provokes others to continue to
756 explore the strengths and weaknesses of the available multicomponent and multiphase phase
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758

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767

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1032

1033 **FIGURE CAPTIONS**

1034 **Figure 1.** Equilibrium phase assemblages at 0.25 GPa for a N-MORB composition. (a, b)
1035 rhyolite-MELTS and (c, d) HPx-mb16. (a, c) Low-H₂O (0.5 wt% H₂O) calculations. (b, d) High-
1036 H₂O (4 wt% H₂O) calculations. Mineral abbreviations follow Whitney and Evans (2010) with the
1037 exception of “L” and “F” which refer to liquid and fluid, respectively.

1038 **Figure 2.** Equilibrium phase assemblages at 1 GPa for a N-MORB composition. (a, b) rhyolite-
1039 MELTS and (c, d) HPx-mb16. (a, c) Low-H₂O (0.5 wt% H₂O) calculations. (b, d) High-H₂O (4
1040 wt% H₂O) calculations. Mineral abbreviations follow Whitney and Evans (2010) with the
1041 exception of “L” and “F” which refer to liquid and fluid, respectively.

1042 **Figure 3.** Total alkali-silica (TAS) classification diagram (Le Bas et al., 1986) for the calculated
1043 N-MORB liquids (liquid compositions correspond to those presented in Figs. 1 and 2). Liquid
1044 compositions are shown every 10 °C from the liquidus to the solidus.

1045 **Figure 4.** Liquid compositional evolution (wt%) at 0.25 GPa for a low-H₂O (0.5 wt H₂O) N-
1046 MORB composition. (a–f) Calculated liquid compositions as a function of temperature. (g–i)
1047 Liquid compositions shown in Harker diagrams. Approximate liquid fractions (wt%) are shown
1048 in (a) for comparison between modeling approaches. Mineral abbreviations follow Whitney and
1049 Evans (2010) with the exception of “L” and “F” which refer to liquid and fluid, respectively.

1050 **Figure 5.** Liquid compositional evolution (wt%) at 0.25 GPa for a high-H₂O (4 wt H₂O) N-
1051 MORB composition. (a–f) Modeled liquid compositions as a function of temperature. (g–i)
1052 Modeled liquid compositions shown in Harker diagrams. Approximate liquid fractions (wt%) are
1053 shown in (a) for comparison between modeling approaches. Mineral abbreviations follow
1054 Whitney and Evans (2010) with the exception of “L” and “F” which refer to liquid and fluid,
1055 respectively.

1056 **Figure 6.** Liquid compositional evolution (wt%) at 1 GPa for a low-H₂O (0.5 wt H₂O) N-MORB
1057 composition. (a–f) Modeled liquid compositions as a function of temperature. (g–i) Modeled
1058 liquid compositions shown in Harker diagrams. Approximate liquid fractions (wt%) are shown in
1059 (a) for comparison between modeling approaches. Mineral abbreviations follow Whitney and
1060 Evans (2010) with the exception of “L” and “F” which refer to liquid and fluid, respectively.

1061 **Figure 7.** Liquid compositional evolution (wt%) at 1 GPa for a high-H₂O (4 wt H₂O) N-MORB
1062 composition. (a–f) Modeled liquid compositions as a function of temperature. (g–i) Modeled
1063 liquid compositions shown in Harker diagrams. Approximate liquid fractions (in wt%) are shown
1064 in (a) for comparison between modeling approaches. Mineral abbreviations follow Whitney and
1065 Evans (2010) with the exception of “L” and “F” which refer to liquid and fluid, respectively.

1066 **Figure 8.** Liquid incompatible trace-element patterns at (a–b) 900 °C in the low-*P*–low-H₂O run,
1067 (c–d) 1000 °C in the high-*P*–low-H₂O run, and (e–f) 850 °C in the high-*P*–high-H₂O run. (a), (c),

1068 and (e) normalized to primitive mantle (Sun and McDonough, 1989) and (b), (d), and (f)
1069 normalized to chondrite (McDonough and Sun, 1995). The orange line is mean N-MORB from
1070 Gale et al. (2013).

1071 **Figure 9.** Phase proportion comparison experiments of basaltic compositions and model
1072 predictions. (a, b) Comparison with Berndt et al. (2005) experiments (BKH). (c, d) Comparison
1073 with Sen and Dunn, 1994 (SD). Phase proportions are shown on an anhydrous basis (recalculated
1074 to 100%). In the SD experiments, rutile is also present as a trace phase. Rhyolite-MELTS models
1075 where calculated with rhyolite-MELTS v1.2.0. Mineral abbreviations follow Whitney and Evans
1076 (2010) with the exception of “L” and “F” which refer to liquid and fluid, respectively.

1077

1078 **TABLE CAPTIONS**

1079 **Table 1.** Bulk-rock compositions used for petrological modeling (normalized wt%).

1080 **Table 2.** Phase proportions of N-MORB at 0.25 and 1 GPa (wt%).

1081 **Table 3.** Liquid trace-element compositions (ppm).

1082 **Table 4.** Comparison of phase proportions between experiments of basaltic compositions and
1083 model predictions (wt%).

1084 **Table 5.** Comparison of liquid compositions between experiments of basaltic compositions and
1085 model predictions (wt%).

1086

1087 **SUPPLEMENTARY MATERIAL**

1088 **Appendix 1.** The Appendix 1 describes the phase evolution as well as the liquid and mineral
1089 composition evolution. The appendix also include the mineral composition comparison between

1090 rhyolite-MELTS and HPx-mb16, Supplementary Tables S1–S4, and Supplementary Figures
1091 S1–S6.

1092 **Figure S1.** Equilibrium phase assemblages at 0.25 GPa for a N-MORB composition in vol%. (a,
1093 b) rhyolite-MELTS and (c, d) HPx-mb16. (a, c) Low-H₂O (0.5 wt% H₂O) calculations. (b, d)
1094 High-H₂O (4 wt% H₂O) calculations. Mineral abbreviations follow Whitney and Evans (2010)
1095 with the exception of “L” and “F” which refer to liquid and fluid, respectively.

1096 **Figure S2.** Equilibrium phase assemblages at 1 GPa for a N-MORB composition in vol%. (a, b)
1097 rhyolite-MELTS and (c, d) HPx-mb16. (a, c) Low-H₂O (0.5 wt% H₂O) calculations. (b, d) High-
1098 H₂O (4 wt% H₂O) calculations. Mineral abbreviations follow Whitney and Evans (2010) with the
1099 exception of “L” and “F” which refer to liquid and fluid, respectively.

1100 **Figure S3.** Calculated clinopyroxene compositions (in atoms per formula unit, a.p.f.u.) at (a–f)
1101 0.25 GPa and (g–l) 1 GPa. (a–c and g–i) Clinopyroxene compositions in a low-H₂O (0.5 wt%)
1102 MORB composition. (d–f and j–l) Clinopyroxene compositions in a high-H₂O (4 wt%)MORB
1103 composition. Mineral abbreviations are the same as in Figure 1.

1104 **Figure S4.** Calculated anorthite content (An) in plagioclase. (a) Plagioclase compositions at 0.25
1105 GPa for a low-H₂O (0.5 wt%) MORB composition. (b) Plagioclase compositions at 0.25 GPa for
1106 a high-H₂O (4 wt%) MORB composition. (c) Plagioclase compositions at 1 GPa for a low-H₂O
1107 (0.5 wt%) MORB composition. Mineral abbreviations are the same as in Figure 1.

1108 **Figure S5.** Calculated orthopyroxene compositions (in atoms per formula unit, a.p.f.u.) at 0.25
1109 GPa for a low-H₂O (0.5 wt%) MORB composition.

1110 **Figure S6.** Calculated garnet compositional evolution (in end-member proportions) at 1 GPa for
1111 a low-H₂O (0.5 wt%) MORB composition.

- 1112 **Table S1.** Components considered in the activity–composition relations used in this work (see
1113 text for detail).
- 1114 **Table S2.** Liquid compositions of N-MORB at 0.25 GPa (wt%).
- 1115 **Table S3.** Liquid compositions of N-MORB at 1 GPa (wt%).
- 1116 **Table S4.** Amphibole composition comparison at 1 GPa (wt%).
- 1117 **Table S5.** Phase proportions used for trace-element modeling (wt%).
- 1118 **Table S6.** Partition coefficients from Bedard (2006).

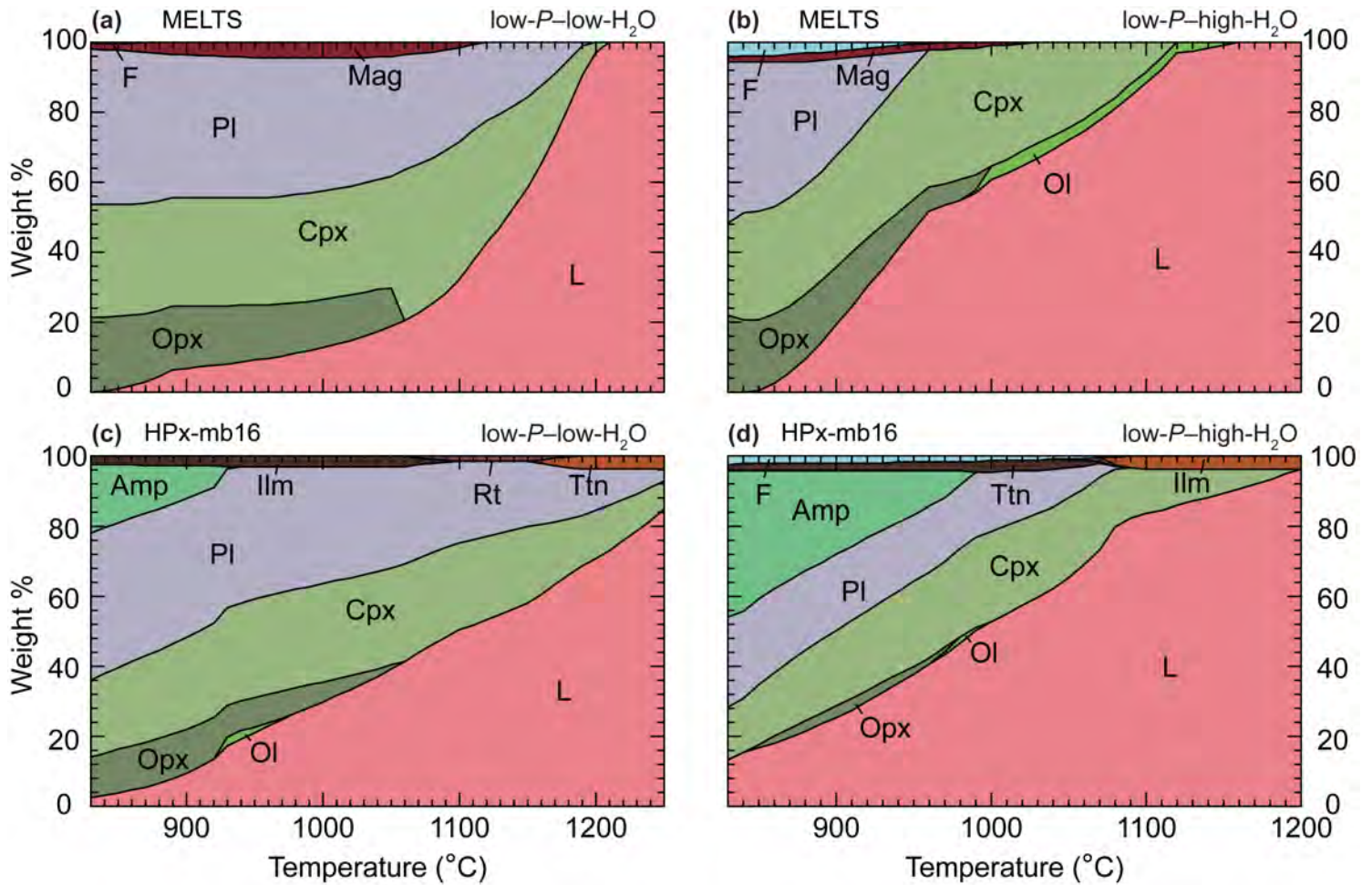


Figure 1

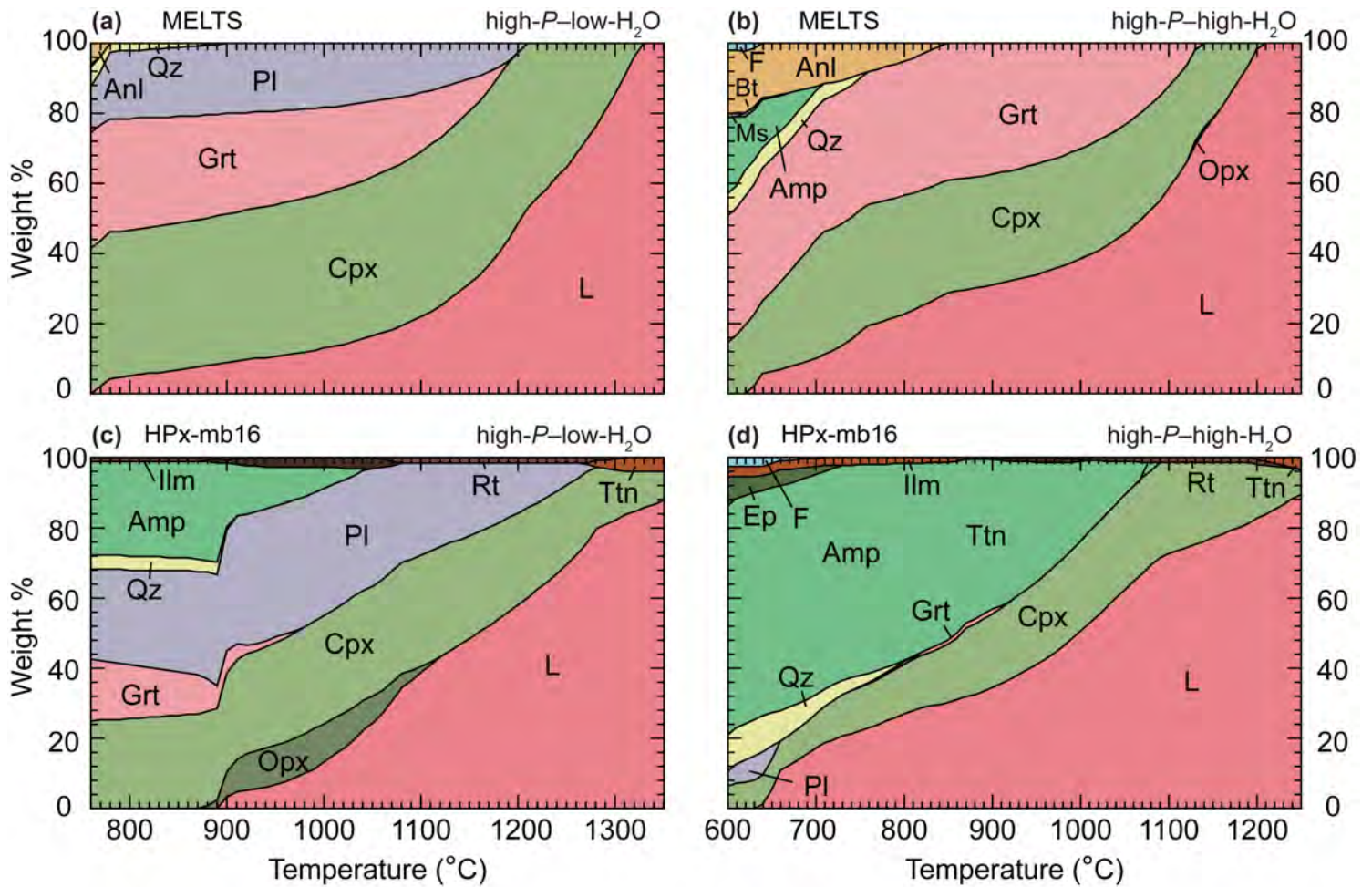


Figure 2

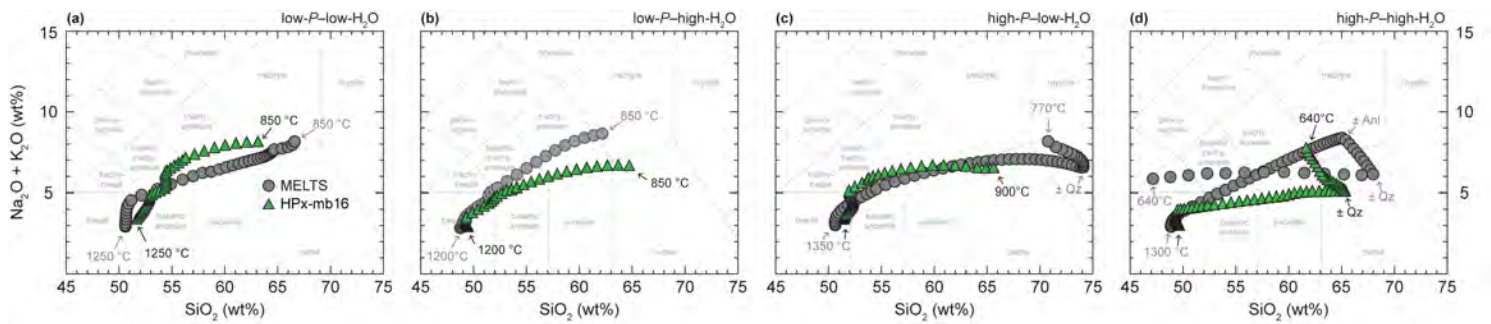


Figure 3

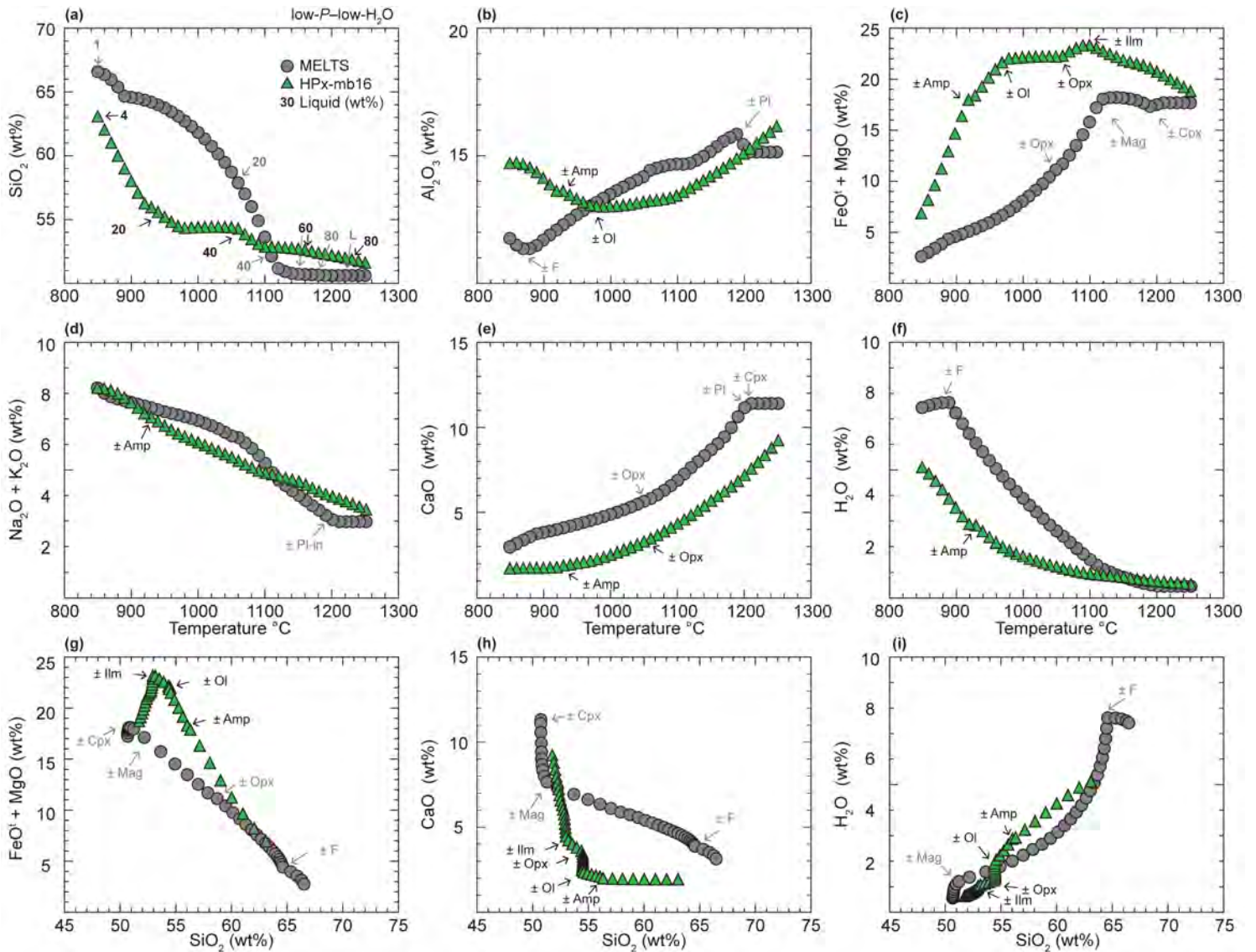


Figure 4

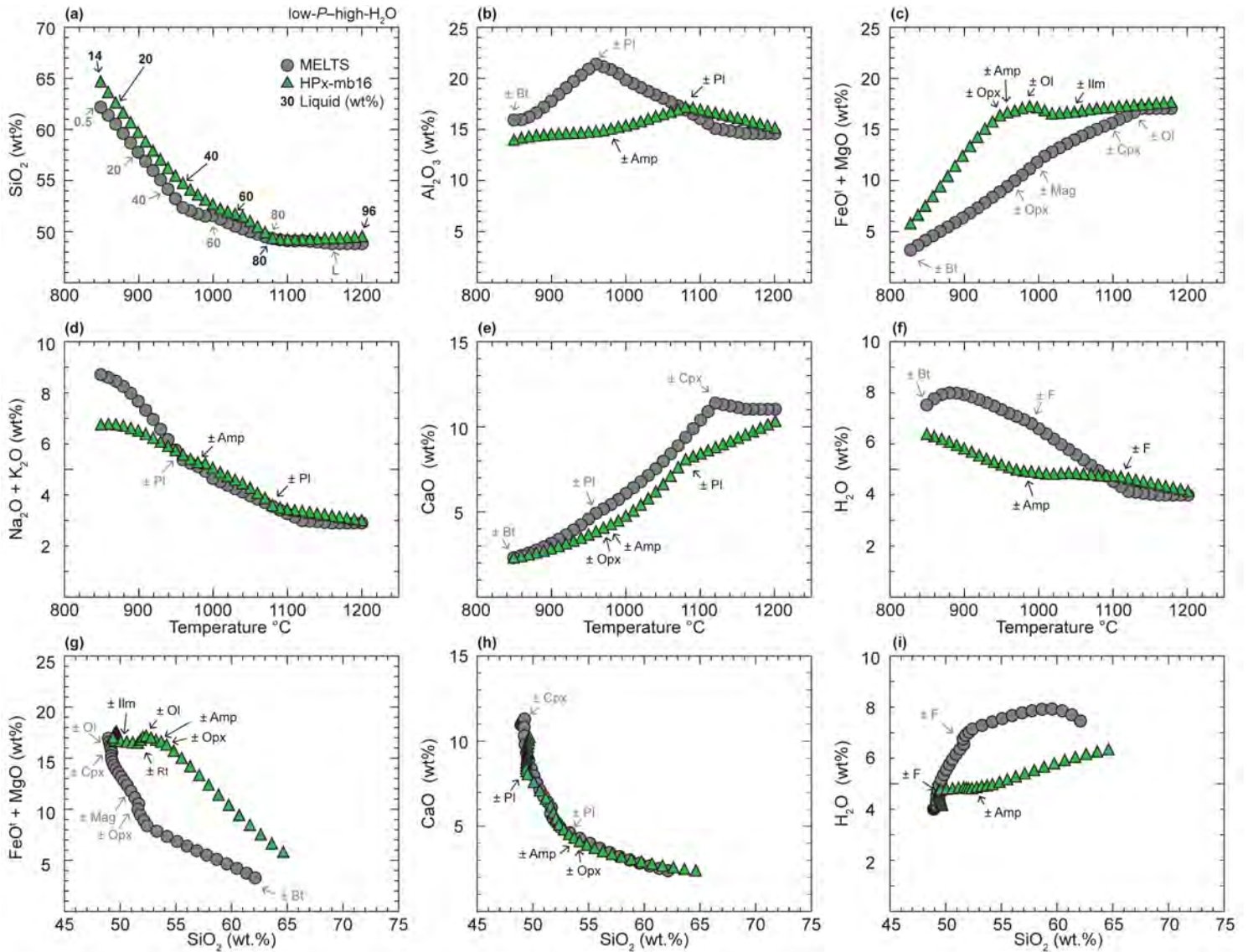


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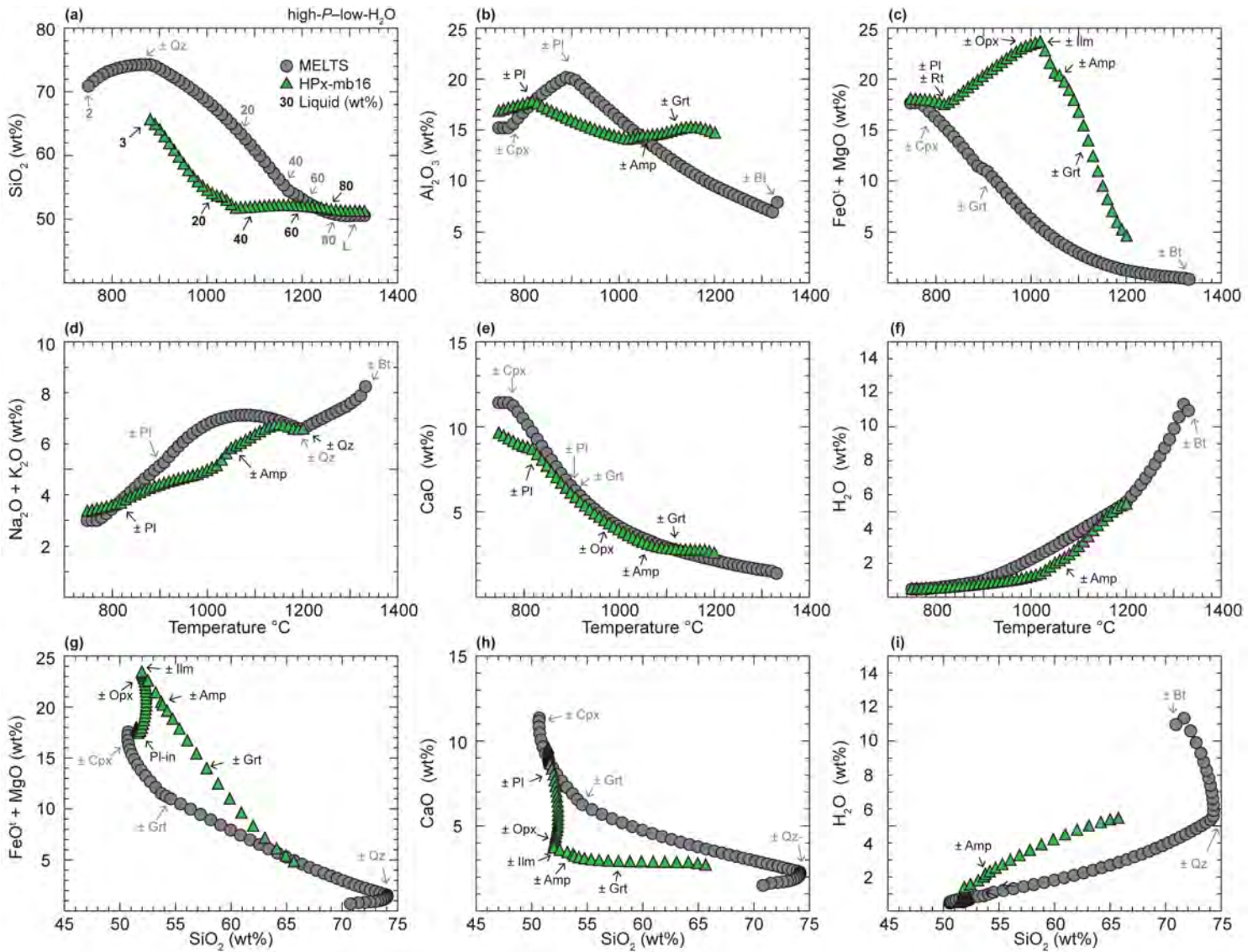


Figure 6

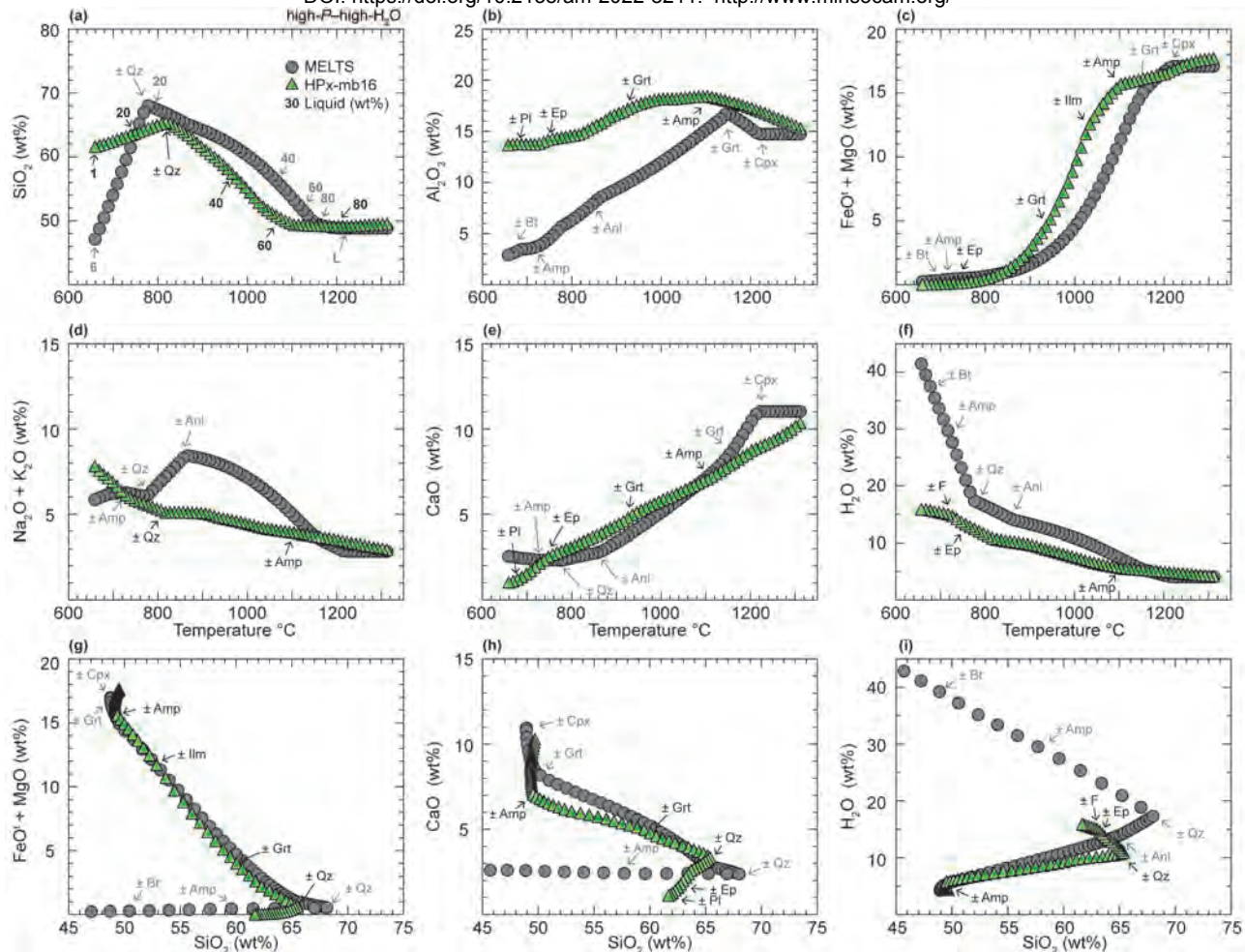


Figure 7

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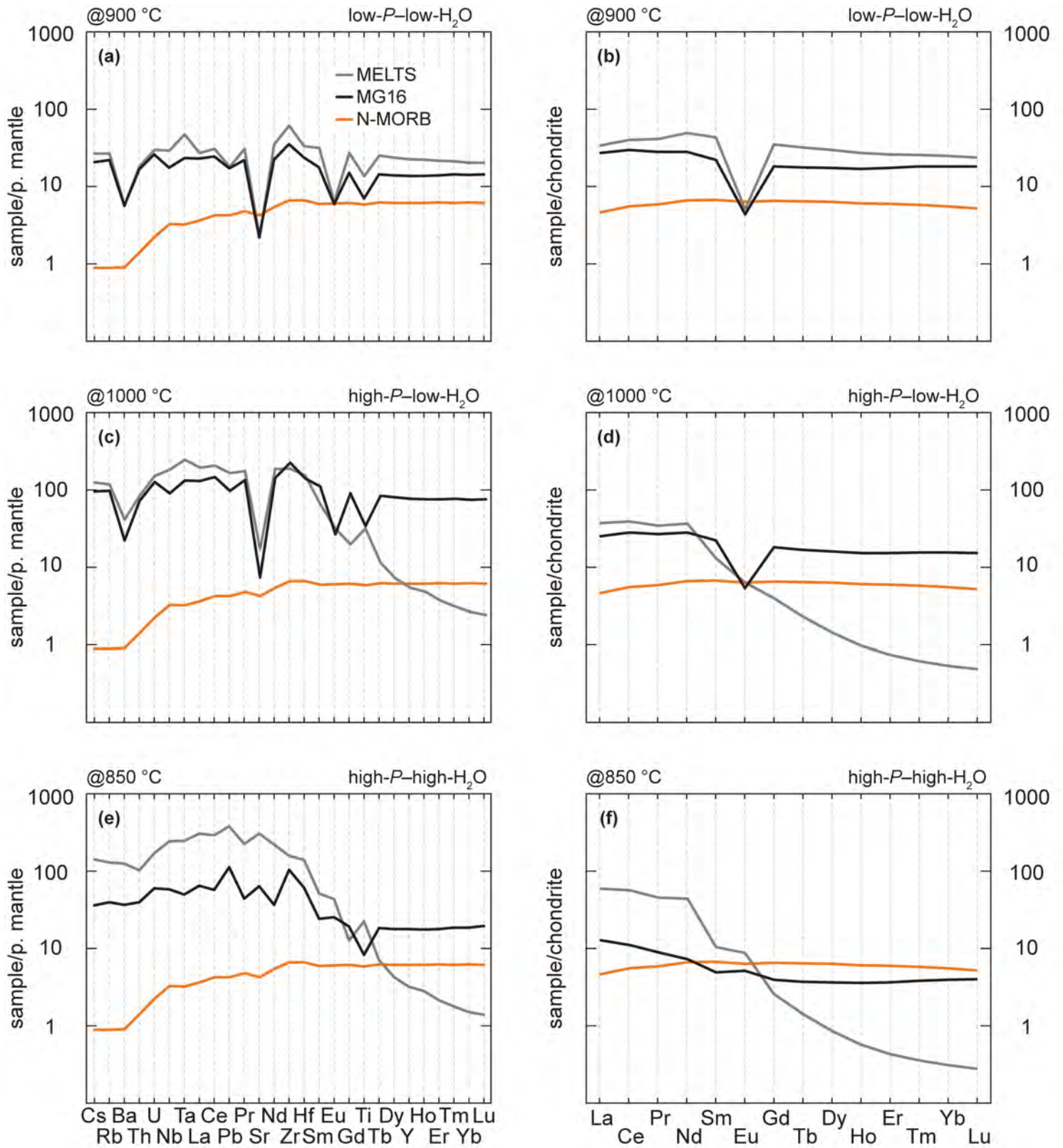


Figure 8

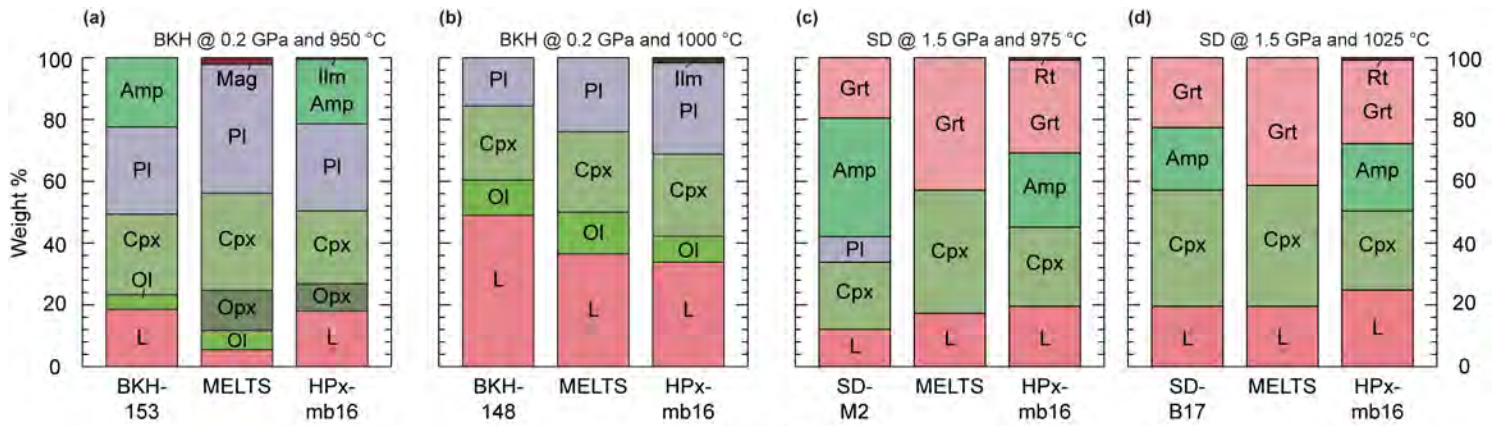


Figure 9

Table 1. Bulk-rock compositions used for petrological modelling (normalized wt%).

	N-MORB-0.5	N-MORB-4
SiO ₂	50.69	48.91
TiO ₂	1.54	1.48
Al ₂ O ₃	15.21	14.68
FeO ^t	9.86	9.52
MgO	7.80	7.53
CaO	11.41	11.01
Na ₂ O	2.85	2.75
K ₂ O	0.14	0.14
H ₂ O	0.50	4.00
Total	100.00	100.00

All compositions correspond to the mean N-MORB from Gale et al. (2013) but with different H₂O contents.

Table 2. Phase proportions of N-MORB at 0.25 and 1 GPa (wt%).

	L	Ol	Opx	Cpx	Grt	Fsp	Qz	Amp	Anl	Ilm	Mag	Ttn	Rt	F	Total	Solids	Fluid	Melt	Total
0.25 Gpa																			
<i>0.5 wt% H₂O</i>																			
900 °C																			
MELTS	7	-	18	31	-	41	-	-	-	-	4	-	-	-	100	93	-	7	100
HPx-mb16	9	-	13	26	-	40	-	9	-	3	-	-	-	-	100	91	-	9	100
1000 °C																			
MELTS	13	-	14	31	-	38	-	-	-	-	5	-	-	-	100	87	-	13	100
HPx-mb16	30	-	6	28	-	33	-	-	-	3	-	-	-	-	100	70	-	30	100
1100 °C																			
MELTS	32	-	-	39	-	27	-	-	-	-	2	-	-	-	100	68	-	32	100
HPx-mb16	50	-	-	25	-	23	-	-	-	-	-	-	2	-	100	50	-	50	100
<i>4 wt% H₂O</i>																			
900 °C																			
MELTS	19	-	17	32	-	27	-	-	-	-	2	-	-	2	100	78	2	19	100
HPx-mb16	26	-	3	21	-	22	-	24	-	2	-	-	-	2	100	72	2	26	100
1000 °C																			
MELTS	61	4	-	34	-	-	-	-	-	-	1	-	-	-	100	39	-	61	100
HPx-mb16	52	1	-	25	-	17	-	-	-	3	-	-	-	1	100	46	1	52	100
1100 °C																			
MELTS	88	3	-	8	-	-	-	-	-	-	-	-	-	-	100	12	-	88	100
HPx-mb16	84	-	-	13	-	-	-	-	-	-	-	-	4	<1	100	16	<1	84	100
1 Gpa																			
<i>0.5 wt% H₂O</i>																			
800 °C																			
MELTS	5	-	-	42	32	19	2	-	-	-	-	-	-	-	100	95	-	5	100
HPx-mb16	0	-	-	26	15	27	4	27	-	-	-	-	1	-	100	100	-	0	100
900 °C																			
MELTS	9	-	-	42	29	20	<1	-	-	-	-	-	-	-	100	91	-	9	100
HPx-mb16	3	-	7	28	7	35	1	18	-	1	-	-	1	-	100	97	-	3	100
1000 °C																			
MELTS	13	-	-	44	25	18	-	-	-	-	-	-	-	-	100	87	-	13	100
HPx-mb16	13	-	11	31	-	36	-	6	-	3	-	-	-	-	100	87	-	13	100
1100 °C																			
MELTS	22	-	-	47	17	14	-	-	-	-	-	-	-	-	100	78	-	22	100
HPx-mb16	39	-	2	32	-	26	-	-	-	-	-	-	2	-	100	61	-	39	100
<i>4 wt% H₂O</i>																			
800 °C																			
MELTS	23	-	-	34	38	-	-	-	5	-	-	-	-	-	100	77	-	23	100
HPx-mb16	27	-	-	14	-	1	<1	56	-	-	-	-	2	-	100	73	-	27	100
900 °C																			
MELTS	31	-	-	32	37	-	-	-	-	-	-	-	-	-	100	69	-	31	100
HPx-mb16	34	-	-	21	1	-	-	43	-	<1	-	1	-	-	100	66	-	34	100
1000 °C																			
MELTS	38	-	-	32	30	-	-	-	-	-	-	-	-	-	100	62	-	38	100
HPx-mb16	50	-	-	26	-	-	-	23	-	1	-	1	-	-	100	50	-	50	100
1100 °C																			
MELTS	59	-	-	29	12	-	-	-	-	-	-	-	-	-	100	41	-	59	100
HPx-mb16	73	-	-	26	-	-	-	-	-	-	-	1	-	-	100	27	-	73	100

Mineral abbreviations follow Whitney & Evans (2010) with the exception of "L" and "F" which refer to liquid and fluid, respectively.

Table 3. Liquid trace-element compositions (ppm).

Table 4. Comparison of phase proportions between experiments of basaltic compositions and model predictions (wt%).

	0.2 GPa and 950 °C					0.2 GPa and 1000 °C					1.5 GPa and 975 °C				
	BKH (153)	MELTS	HPx-mb16	% diff. ¹	% diff. ²	BKH (148)	MELTS	HPx-mb16	% diff. ¹	% diff. ²	SD (M2)	MELTS	HPx-mb16	% diff. ¹	% diff. ²
L	19	6	18	-70	-3	49	37	33	-25	-31	12	17	20	40	61
Ol	5	6	-	29	-	11	14	9	19	-24	-	-	-	-	-
Opx	-	13	9	-	-	-	-	-	-	-	-	-	-	-	-
Cpx	26	31	24	21	-9	24	26	27	8	10	21	40	26	89	21
Pl	29	42	28	47	-1	16	24	30	53	90	9	-	-	-	-
Amp	22	-	21	-	-8	-	-	-	-	-	39	-	24	-	-39
Ilm	-	-	<1	-	-	-	-	2	-	-	-	-	-	-	-
Mag	-	2	-	-	-	-	-	-	-	-	-	-	-	-	-
Grt	-	-	-	-	-	-	-	-	-	-	19	43	30	122	58
Rt	-	-	-	-	-	-	-	-	-	-	tr	-	<1	-	-

¹difference between the experiment and MELTS; ²difference between the experiment and HPx-mb16. tr—trace; BKH—Berndt et al. (2005); SD—Sen & Dunn (1994). Mineral abbreviations of "L" which refers to liquid. Phase proportions are shown in an anhydrous basis (recalculated to 100%).

Table 5. Comparison of liquid compositions between experiments of basaltic compositions and model predictions (wt%).

L fraction (wt. %)	0.2 GPa and 950 °C					0.2 GPa and 1000 °C					1.5 GPa and 925 °C				
	BKH (153)	MELTS	HPx-mb1	% diff. ¹	% diff. ²	BKH (148)	MELTS	HPx-mb1	% diff. ¹	% diff. ²	SD (M2)	MELTS	HPx-mb1	% diff. ¹	% diff. ²
SiO ₂	55.77	59.67	55.60	7	0	50.83	54.83	53.90	8	6	65.29	67.33	63.18	3	-3
TiO ₂	1.13	0.30	–	-74	–	1.19	0.52	–	-56	–	0.76	0.39	–	-49	–
Al ₂ O ₃	16.78	14.10	14.48	-16	-14	18.37	15.73	15.00	-14	-18	18.53	12.25	18.16	-34	-2
FeO [†]	8.56	4.89	10.96	-43	28	8.16	7.46	10.85	-9	33	2.85	2.02	4.93	-29	73
MgO	2.40	2.28	5.16	-5	115	3.61	3.70	6.29	3	74	0.72	0.54	1.21	-25	68
CaO	6.30	4.72	3.19	-25	-49	9.10	7.36	4.28	-19	-53	2.63	2.13	3.11	-19	18
Na ₂ O	3.96	6.62	5.80	67	46	3.75	4.48	5.22	19	39	6.49	10.26	5.81	58	-10
K ₂ O	0.22	1.06	0.38	382	74	0.15	0.21	0.23	38	51	2.73	5.08	3.59	86	32
H ₂ O	4.88	6.36	4.42	30	-10	4.83	5.71	4.22	18	-13	–	–	–	–	–
Total	100	100	100			100	100	100			100	100	100		

¹difference between the experiment and MELTS; ²difference between the experiment and HPx-mb16. tr—trace; BKH—Berndt et al. (2005); SD—Sen & Dunn (1994); L—liquid.