

1 **Revision 1**

2 **A Refined Estimation of Li in Mica by a Machine Learning Method**

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9 **ABSTRACT**

10 Li-rich micas are crucial in the exploration for and exploitation of Li resources. The
11 determination of Li in mica using classical bulk chemical methods or in-situ
12 microanalytical techniques is expensive and time-consuming and has a high-quality
13 requirement for micas and reference materials. Although simple linear and nonlinear
14 empirical equations have been proposed, they are inconsistent with the complex
15 physico-chemical mechanisms of Li incorporation and commonly lead to large errors. In
16 this study, we introduce a refined method of multivariate polynomial regression using a
17 machine learning algorithm to estimate Li from multiple major oxide abundances. The
18 performance of our regression model is evaluated using the coefficient of determination
19 (R^2) and the root-mean-square error (RMSE) of the independent test sets. The
20 best-performed models show R^2 of 0.95 and a RMSE of 0.35 wt% for the test set of
21 dataset 1 (all compiled data, $n = 2124$) and R^2 of 0.96 and a RMSE of 0.22 wt% for the

22 test set of dataset 2 (only data obtained using in-situ techniques, n = 1386). Our results
23 indicate that integration of electron probe microanalysis and multivariate polynomial
24 regression (based on dataset 1) presents a robust and convenient approach to quantify Li
25 in micas. The application of the proposed approach to micas from central Inner Mongolia,
26 NE China, suggests that in addition to the Weilasituo ore bodies, the Jiabusi granite and
27 greisen and the Shihuiyao metamorphic sediment formation have good potential for Li
28 exploration. Our study also provides preliminary constraints on the genesis of Li deposits.
29 **Keywords:** Li in mica, multivariate polynomial regression, machine learning, Li
30 resources

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32 INTRODUCTION

33 Micas are members of phyllosilicates in which the unit structure consists of one octahedral
34 (O) sheet between two opposing tetrahedral (T) sheets to form a ‘TOT’ layer. Due to their
35 specific layered structure and flexible crystal lattice, micas are able to accommodate rare
36 elements, such as Li, Rb and Cs, in the interlayer or octahedral structural sites to various
37 extents ([Bailey 1984](#); [Rieder et al. 1999](#)).

38 Lithium is the lightest solid element in the alkali metal group. Due to its unique electrical
39 and mechanical properties, Li is widely used in the ceramic and glass industries,
40 rechargeable batteries, lubricating greases, metallurgy, air treatment, pharmaceuticals, and
41 polymer products ([Naumov and Naumova 2010](#); [Bradley et al. 2017](#)). With the increased
42 demand of Li in batteries for electric vehicles (EVs), Li has been recently defined as one of

43 the strategic metals for green technology ([Gruber et al. 2011](#); [Kesler et al. 2012](#); [Linnen et](#)
44 [al. 2012](#); [Bradley et al. 2017](#); [Tian et al. 2018](#)). Li-rich micas, such as zinnwaldite and
45 lepidolite, constitute a dominant component of Li resources ([Linnen et al. 2012](#); [Bradley et](#)
46 [al. 2017](#); [Martin et al. 2017](#); [Rentsch et al. 2018](#)). Quantification of the Li contents in micas
47 is important for the exploitation of Li resources. In addition, a detailed study of
48 composition and microstructure of micas could be used to interpret the complex
49 magmatic-hydrothermal evolution of granitic magmas and associated mineralization
50 ([Černý et al. 1985](#); [Henderson et al. 1989](#); [Charoy et al. 1995](#); [Breiter et al. 1997, 2019](#);
51 [Mohamed et al. 1999](#); [Roda et al. 2007](#); [Vieira et al. 2011](#); [Neiva 2013](#); [Breiter et al. 2017a](#);
52 [Garate-Olave et al. 2018](#); [Codeço et al. 2020a](#)).

53 The electron probe microanalysis (EPMA) is the most frequently used analytical technique
54 to obtain qualitative elemental compositions of solid polished samples at a micrometer
55 scale. However, EPMA cannot be utilized to detect Li because of its low atomic number.
56 Although some classical bulk techniques (such as wet chemistry) and microanalytical
57 methods (such as laser ablation-inductively coupled plasma mass spectrometry
58 (LA-ICP-MS) and secondary ion-mass spectrometry (SIMS)) are capable of determining
59 Li, they are expensive and time-consuming and have high-quality requirements for the
60 analyzed samples and reference materials. Alternatively, an empirical approach has been
61 proposed based on linear or nonlinear correlations between Li_2O and other major
62 components, such as SiO_2 , MgO or F , in micas determined by EPMA or other analytical
63 methods ([Monier and Robert 1986](#); [Stone et al. 1988](#); [Henderson et al. 1989](#); [Tindle and](#)

64 [Webb 1990](#); [Tischendorf et al. 1997](#); [Tischendorf 1999](#)). Empirical equations, which are
65 either generalized, as those obtained by [Tindle and Webb \(1990\)](#), [Tischendorf et al. \(1997\)](#)
66 and [Tischendorf \(1999\)](#), or formulated for particular cases, are commonly used
67 ([Roda-Robles et al. 2006, 2018](#); [Roda et al. 2007](#); [Neiva et al. 2008](#); [Van Lichtervelde et al.](#)
68 [2008](#); [Vieira et al. 2011](#); [Martins et al. 2012](#); [Neiva 2013](#); [Li et al. 2015](#); [Xie et al. 2015](#);
69 [Legros et al. 2016](#); [Ballouard et al. 2020](#); [Yin et al. 2020](#)). Based on 14 published empirical
70 equations, a computer program called LIMICA was developed by [Yavuz \(2001\)](#). However,
71 these empirical equations were proposed for specified types of micas with distinct
72 compositional ranges. Use of these equations for determination of the Li₂O content can be
73 problematic given that some equations are only applicable for a specific Li₂O content.
74 Moreover, the simple correlations between Li₂O and other individual major components
75 are limited to small datasets used in the regression and inconsistent with the complex
76 physico-chemical mechanisms of Li incorporation, which leads to significant errors in their
77 applications ([Förster et al. 2005](#); [Thiergärtner 2010](#); [Breiter et al. 2017b](#); [Breiter et al.](#)
78 [2019](#); [Ballouard et al. 2020](#)).

79 In this study, we use a compilation of >2000 mica compositions from various rock types,
80 including Li₂O and the following 10 major components: SiO₂, Al₂O₃, TiO₂, FeO_T, MgO,
81 MnO, CaO, Na₂O, K₂O, and F. These data are regressed using a multivariate polynomial
82 regression (MPR) based machine learning (ML) method to refine the equation for
83 estimating Li in micas over a wide range of chemical compositions. We then discuss the
84 uncertainties and limitations of the refined equation and compare the performance of the

85 MPR model with previously published empirical equations. Finally, we apply the refined
86 equation to estimate the Li₂O contents of micas from various types of rocks in central
87 Inner Mongolia, NE China. Our results provide preliminary constraints on the potential
88 for finding new Li resources in NE China.

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METHODS

91 **Experimental Datasets**

92 Mica compositions were collected from the published literature using the following
93 criteria: a) Major components of SiO₂, TiO₂, Al₂O₃, FeO_T (total Fe expressed as FeO),
94 MnO, MgO, CaO, Na₂O, K₂O, F, and Li₂O were compiled, whereas H₂O and trace
95 elements were excluded due to the lack of qualified data in most literature sources -
96 otherwise, it is assumed that their influence on the behavior of Li is minor and can be
97 ignored; b) The compiled oxides were determined using either in-situ microanalysis, such
98 as EPMA, LA-ICP-MS or SIMS, or classical bulk chemistry on pure mica separates; c) Li
99 contents were obtained from the grains or spots that were the same as or close to those from
100 which the other oxides were analyzed; and d) The micas that occurred as post-formation
101 residuals modified at disequilibrium conditions or showed abnormal compositions were
102 excluded. To avoid computational errors, the compositions that are below detection limits
103 were set to 0.000001 wt%, and the data with symbols “<” and “<<” were recalculated by
104 multiplying them with 0.8 and 0.2, respectively. After this data cleaning, a total of 2124

105 compositions from 94 published literature sources (years 1960–2020) were used for
106 further data processing.

107 Considering the varying accuracies in the mica compositions, two types of datasets were
108 used for regression: dataset 1 consisting of the whole compiled data ($n = 2124$), and
109 dataset 2 screened to contain data determined by two or more in-situ techniques on the
110 same or closely located spots ($n = 1386$) (Table S1). In dataset 1, most of the micas are
111 from granites, pegmatites and other granitic rocks, and the rest are from greisens,
112 carbonatites, kimberlites, lamproites, lherzolites and metamorphic rocks including
113 eclogites, migmatites, gneisses and schists. They cover a wide range of compositions with
114 31.40–59.65 wt% SiO₂, 0–8.56 wt% TiO₂, 0.04–38.77 wt% Al₂O₃, 0–35.84 wt% FeO_T,
115 0–7.60 wt% MnO, 0–29.98 wt% MgO, 0–3.42 wt% CaO, 0–2.24 wt% Na₂O, 4.79–12.57
116 wt% K₂O, 0–10.34 wt% F, and 0–7.70 wt% Li₂O. In the classification diagram of
117 Tischendorf et al. (1997), these micas plot in a broad field covering (Li-) phengite,
118 (Li-)muscovite, zinnwaldite, lepidolite, protolithionite, siderophyllite, lepidomelane,
119 Fe-biotite, Mg-biotite and phlogopite, with a minor portion of them plotting in the
120 taeniolite and alumino-phlogopite fields (Fig. 1a). Compared to dataset 1, dataset 2
121 contains similar rock types but their compositional range is narrower: 33.50–59.17 wt%
122 SiO₂, 0.04–37.88 wt% Al₂O₃, 0–27.32 wt% FeO_T, 0–3.86 wt% MnO, 0–1.38 wt% Na₂O,
123 5.62–11.62 wt% K₂O, and 0–6.93 wt% Li₂O. As shown in the classification diagram,
124 dataset 2 is concentrated in the (Li-) phengite, (Li-)muscovite and phlogopite fields, with
125 fewer compositions in the fields of other mica types (Fig. 1b). Lepidomelane, taeniolite

126 and alumino-phlogopite compositions are absent in dataset 2.

127

128 **Regression analysis**

129 Regression analysis is one of the classical models that are commonly used in the ML
130 algorithms. It is a statistical method for estimating the relationship between a dependent
131 variable y and one or more independent variables x . The linear regression model is the
132 most common and basic statistical method, the equation of which can be expressed as:

$$133 \quad y = \beta_0 + \sum_{i=1}^k \beta_i x_i + \varepsilon \quad (1)$$

134 where β_0 is the intercept, β_i is the linear effect parameter, and ε represents the error. In
135 particular, the linear relationship between one dependent variable and one independent
136 variable is called simple linear regression. But in most cases, especially those related to
137 complex geological processes, the observational data cannot be well modeled by a simple
138 linear regression model. Instead, multivariate polynomial regression (MPR) is considered
139 to be more appropriate to model nonlinear relationships between variables ([Draper and
140 Smith 1998](#)). Taking bivariate quadratic polynomial regression as an example, the model
141 is formulated as:

$$142 \quad y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_{11} x_1^2 + \beta_{22} x_2^2 + \beta_{12} x_1 x_2 + \varepsilon \quad (2)$$

143 where β_0 is the intercept, β_1 and β_2 are the linear effect parameters, β_{11} and β_{22} are the
144 quadratic effect parameters, β_{12} is the interaction effect parameter, and ε is the error.
145 This equation can be expressed in a matrix form as:

$$146 \quad \mathbf{Y} = \boldsymbol{\beta}\mathbf{X} + \boldsymbol{\varepsilon} \quad (3)$$

155 The parameter β is generally estimated using the ordinary least square (OLS) method by
156 minimizing the sum of squared residuals (SSR), where

157
$$\text{SSR} = (\beta X - Y)^T (\beta X - Y) \quad (6)$$

158 Theoretically, a sufficiently high-degree polynomial can approximate any nonlinear
159 relationships (Draper and Smith 1998). Thus, it is reasonable and appropriate to use the
160 MPR to express the complicated relationship between Li_2O and other major components
161 in mica. We applied a MPR-based ML algorithm with Python coding in the open-source
162 Anaconda distribution. The code is available on GitHub at the following URL
163 (<https://github.com/luwang9103/MPR-Li-mica.git>). The degree of an approximate
164 polynomial was chosen by testing the performance of model fitting at each step with a
165 successively increasing degree, keeping it as low as possible. Given the problems of
166 multicollinearity and overfitting, which commonly occur in the MPR, a method of elastic
167 net regularization was performed (Zou and Hastie 2005). Elastic net is a regularized
168 regression method that linearly combines the L1 and L2 penalties of the lasso and ridge
169 methods and aims at minimizing the loss function of

170
$$J(\beta) = \frac{1}{2} (\beta X - Y)^T (\beta X - Y) + \alpha \rho \|\beta\|_1 + \frac{\alpha(1-\rho)}{2} \|\beta\|_2^2 \quad (7)$$

171 where ρ is the mixing parameter between lasso ($\rho=0$) and ridge ($\rho=1$) and α is a
172 constant coefficient. This method deals with bias-variance tradeoff to avoid overfitting
173 and reduces the influence of multicollinearity simultaneously. Multicollinearity leads to
174 small eigenvalues of $X^T X$, thus the variance of the regression coefficient β can be very
175 large with the OLS method (equation 6). The regularization constructs an alternative

176 estimator by adding penalties that gives a smaller variance of β . Specifically, the ridge
177 shrinks the coefficients of less important variables to near zero, and the lasso reduces the
178 number of irrelevant variables. The elastic net method combines the advantages of the two
179 regressions (Zou and Hastie 2005). Because two parameters of ρ and α are needed in
180 the elastic net, we performed a two-dimension grid search to tune the parameters by using
181 nested loops. We iterated through the values from 0.1 to 1 for both parameters with a step
182 size of 0.1. After 100 iterations, the optimal parameter pair that gives the highest R^2
183 scores was chosen.

184 The two datasets of this work were treated individually when performing the ML. For
185 both datasets, 70% of the data were used as a training set to yield the regression model
186 and 30% were used as a test set to evaluate the accuracy and uncertainty of the model.
187 The split of the datasets was based on a random sampling method. We conducted 20
188 replications of the random splitting, training and testing procedures to provide a robust
189 estimation of the predictive performance, which is evaluated with the coefficient of
190 determination (R^2) and the root-mean-square error (RMSE).

191

192

RESULTS

193 Our results show that a cubic polynomial with regularized parameters of $\rho = 0.1$ and
194 $\alpha = 0.1$ exhibits a good performance of regression. For the dataset 1 model, the R^2 values
195 calculated from the training set are stable at 0.93–0.96 with RMSE values of 0.30–0.38
196 wt%, while the R^2 values calculated from the test set vary from 0.87 to 0.95 with RMSE

197 values of 0.35–0.54 wt% (Table 1). The results of the best predictive performance are
198 visualized in figure 2. Both the training and test sets display good correlations between
199 the predicted and measured Li_2O values, although minor deviations from the one to one
200 straight line exist (Fig. 2a). In the error distribution diagram, 84% predictions in the test
201 set have errors less than the RMSE (0.35 wt%) and only 3% predictions display
202 deviations higher than 1 wt% (Fig. 3a). Comparatively, the dataset 2 model performs
203 better with R^2 values of 0.96–0.97 and RMSE values of 0.19–0.22 wt% for the training
204 set and R^2 values of 0.92–0.96 and RMSE values of 0.22–0.33 wt% for the test set (Table
205 1). In the predicted Li_2O vs. measured Li_2O diagram, the best-performed training and test
206 sets exhibit remarkable positive trends and most of the predicted values plot close to the
207 1:1 straight line (Fig. 2b). Except for one data with the error of 1.14 wt%, the predicted
208 values of the test set show deviations within 1 wt%, 80% of which are less than the
209 RMSE of 0.22 wt% (Fig. 3b).

210

211 DISCUSSIONS

212 Accuracy and uncertainty of the MPR method

213 The high R^2 (>0.87) and low RMSE (<0.54 wt%) values for the test sets, which were not
214 used during the training procedure, characterize the robust and accurate prediction level
215 of the MPR method. However, the fitting and predictive performance of the dataset 2
216 model is better than that of the dataset 1 model. Regression analysis is strongly influenced
217 by the quality of the original data. The mica compositions of dataset 2 are limited to those

218 obtained by the combined EPMA and SIMS/LA-ICP-MS methods on the same or closely
219 associated spots representing homogeneous or nearly homogeneous compositions of the
220 analyzed micro-domains. The analytical errors are less than $\pm 2\%$ for most major elements
221 and less than $\pm 3\text{--}10\%$ for Li_2O with various abundances ([Kalt et al. 2001](#); [Roda-Robles et](#)
222 [al. 2012](#); [Forni et al. 2016](#); [Xie et al. 2018](#)). In addition to in-situ microanalyses, dataset 1
223 contains bulk chemical analyses by classical wet chemistry, atomic spectrometry and
224 X-ray fluorescence analysis, which display similar analytical errors with in-situ
225 techniques ([Barrière and Cotten 1979](#); [Neiva 1980](#); [Silva and Neiva 1990](#); [Gomes and](#)
226 [Neiva 2005](#)). However, these bulk chemical analyses may cause serious biases when the
227 mica separates contain inclusions of other minerals or show zoned or heterogeneous
228 compositions, which is commonly the case in rare metal occurrences related to magmatic
229 differentiation and hydrothermal processes ([Charoy and Noronha 1996](#)). Propagation of
230 these inherited measurement errors leads to the relatively larger uncertainties in the
231 dataset 1 model.

232 Other factors that affect the uncertainties of both dataset models may include: 1) The total
233 Fe content is used for regression since ferric and ferrous iron cannot be distinguished in
234 most studies; 2) Some trace elements that may be enriched in particular micas and have
235 strong correlations with lithium, such as Rb_2O , Cs_2O , SnO_2 and Ga_2O_3 ([Tischendorf et al.](#)
236 [2001](#)), have not been compiled; and 3) Both in-situ and bulk analyses of micas show large
237 analytical errors in low concentration ranges.

238

239 Comparison with previous methods

240 The empirical approach of calculating Li_2O in micas on the basis of major component
241 correlations has been employed for a long time. Based on a dataset of approximately 400
242 wet chemical analyses, [Tindle and Webb \(1990\)](#) gave an empirical equation of $\text{Li}_2\text{O} =$
243 $0.287 \times \text{SiO}_2 - 9.552$ for Li-bearing trioctahedral micas with $\text{MgO} < 8$ wt%. [Tischendorf](#)
244 [et al. \(1997\)](#) proposed a revised equation of $\text{Li}_2\text{O} = 0.289 \times \text{SiO}_2 - 9.658$ ($n = 232$), which
245 was applicable to trioctahedral micas with $\text{Li}_2\text{O} > 0.6$ wt%, $\text{MgO} < 3$ wt% and $\text{SiO}_2 > 34$
246 wt% ([Tischendorf 1999](#)). The other good non-linear equations ($R^2 > 0.8$) relating Li_2O and
247 individual major components, such as MgO and F , for trioctahedral and dioctahedral
248 micas are summarized in [Table 2](#).

249 For comparison, we use the same test sets of the best-performed dataset 1 and dataset 2
250 models to calculate Li_2O contents by applying these empirical equations. When using the
251 test set of the dataset 1 model (total $n = 638$), < 170 micas match the recommended ranges
252 of validity for the SiO_2 and Li_2O relations ([Table 3](#)). As illustrated in [Figs. 4a and 4b](#), the
253 calculated Li_2O contents (orange cross) are more scattered than those predicted by the
254 MPR, with R^2 of 0.82 and a RMSE of 0.73 wt% for the equation of [Tindle and Webb](#)
255 [\(1990\)](#) and R^2 of 0.68 and a RMSE of 0.88 wt% for the equation of [Tischendorf et al.](#)
256 [\(1997\)](#). The nonlinear Li_2O - MgO correlation of [Tischendorf et al. \(1997\)](#) is applicable to
257 a larger number of micas ($n = 220$), but the predicted results show serious deviations
258 from the measured values ([Fig. 4c](#)). The two Li_2O - F equations for the trioctahedral micas
259 ($n > 300$) perform well, though the predicted results are biased to higher values in the

260 Li_2O range of 3–5 wt% with overestimations reaching 5 wt% (Figs. 4d-e). Their overall
261 R^2 and RMSE values are 0.78–0.82 and 0.85–0.95 wt%, respectively (Table 3). The
262 Li_2O -F equation for the dioctahedral micas ($n = 306$) is limited to Li_2O contents of less
263 than 3 wt% and the calculated results are worse than the MPR predictions with R^2 of 0.51
264 and a RMSE of 0.40 wt% (Fig. 4f; Table 3). Each of the four renewed Li_2O -MgO
265 equations of Tischendorf (1999) is for a distinct mica type. However, because these
266 mica-types are not quantitatively defined, we are unable to apply these equations to our
267 data, and hence they are not further discussed here. To reduce the influences of analytical
268 errors, we further compare the predictive performances among different methods using
269 the test set of the dataset 2 model. The results from empirical equations are similar to
270 those obtained from dataset 1 with relatively higher accuracy but are still worse than
271 those of the MPR method (Fig. 5; Table 3).

272 Above all, our study indicates that although the previously proposed equations show a
273 good fit for the dataset used in original regression, their application to independent micas
274 are burdened with errors to different extents. Moreover, these equations are only
275 available for either trioctahedral or dioctahedral micas with specific compositional ranges.
276 It is sometimes contradictory that the Li_2O content can be used as an application criterion
277 where Li_2O is absent for the mica to be calculated (Table 2). As shown in figures 4 and 5,
278 the predicted data falling outside the validity range of empirical equations (blue cross)
279 could lead to large errors. In contrast, our MPR method has a better generalization

280 capability that is applicable to different types of micas with a wider range of
281 compositions, thus exhibiting a more precise and accurate predictive performance.
282 On the other hand, some authors use good linear correlations ($R^2 > 0.9$) between F and
283 Li_2O that were obtained from a limited amount of analytical data (in-situ techniques) to
284 estimate the Li_2O contents of other unmeasured micas (Table 2; Roda et al. 2007; Van
285 Lichtervelde et al. 2008; Vieria et al. 2011; Codeço et al. 2020a). The positive
286 relationship between F and Li_2O is consistent with the incompatible behavior of these two
287 elements, especially during magmatic or hydrothermal processes. However, in the F vs.
288 Li_2O diagrams (Fig. 6), both dioctahedral and trioctahedral micas from dataset 2 show
289 overall scattered linear trends (R^2 of 0.52 and 0.79). The influence of analytical error can
290 be neglected due to the high precision of dataset 2. Thus, it is considered that only few
291 micas with particular occurrences and compositions may yield strong linear correlations
292 between Li_2O and F and the equations based on their relations have a limited application.

293

294

IMPLICATIONS

295 Implications for estimating Li in micas

296 The simplified formula of micas is given as $IM_{2-3}\square_{1-0}T_4O_{10}A_2$, where *I* represents
297 interlayer cations commonly composed of K, Na, Ca, Ba and rarely Rb, Cs, and NH_4 ; *M*
298 refers to either trioctahedral or dioctahedral cations of Li, Fe^{2+} , Fe^{3+} , Mg, Al, Ti, Mn^{2+} ,
299 Mn^{3+} , Zn, Cr, and V; \square represents a vacancy; *T* refers to tetrahedral cations generally
300 including Si, Al, Fe^{3+} and rarely B and Be; and *A* refers to anions of F, OH, Cl, and S

301 (Rieder et al. 1999). Lithium enters the mica crystal lattice via several competing
302 substitution mechanisms, which include $3\text{Li}^{\text{VI}} \leftrightarrow \text{Al}^{\text{VI}} + 2\Box^{\text{VI}}$, $\text{Si}^{\text{IV}} + 2\text{Li}^{\text{VI}} \leftrightarrow 2\text{Al}^{\text{VI}} + \Box^{\text{VI}}$,
303 and $2\text{Si}^{\text{IV}} + \text{Li}^{\text{VI}} \leftrightarrow 3\text{Al}^{\text{Tot}}$ for Al-rich micas, and $\text{Si}^{\text{IV}} + \text{Li}^{\text{VI}} \leftrightarrow \text{Al}^{\text{IV}} + \text{R}^{\text{VI}}$, $\text{Si}^{\text{IV}} + 2\text{Li}^{\text{VI}} \leftrightarrow$
304 3R^{VI} and $\text{Al}^{\text{VI}} + \text{Li}^{\text{VI}} \leftrightarrow 2\text{R}^{\text{VI}}$, where $\text{R}^{\text{VI}} = \text{Fe} + \text{Mg} + \text{Mn}$, for Fe-rich micas (Foster 1960;
305 Henderson et al. 1989; Charoy et al. 1995; Roda-Robles et al. 2006; Roda et al. 2007;
306 Vieira et al. 2011; Martins et al. 2012; Breiter et al. 2017b). The incorporation of F in the
307 OH site has a close correlation with the incorporation of Li in the octahedral site (Foster
308 1960; Roda et al. 2007; Van Lichtervelde et al. 2008). In addition, the substitutions in the
309 octahedral and tetrahedral sites influence the size of the interlayer site, which is further
310 associated with the various occupations of interlayer cations (Van Lichtervelde et al.
311 2008). Therefore, the incorporation of Li in micas is controlled by complex
312 physico-chemical mechanisms. The previous empirical equations that were derived from
313 the correlations between Li_2O and individual major components, such as SiO_2 , MgO and
314 F, using a limited dataset led to the loss of information, which is interpreted as the main
315 reason for their biased estimations.

316 The MPR method proposed in this study is based on a statistical evaluation of large
317 datasets that contain 10 major components (SiO_2 , Al_2O_3 , MgO , FeO_T , MnO , TiO_2 , CaO ,
318 Na_2O , K_2O , F) and Li_2O . Although the variables used for regression cannot cover all the
319 factors that affect the Li incorporation, the MPR shows a more precise, accurate and
320 robust prediction power than the empirical equations. Moreover, it is generalized to
321 almost all types of micas and the input oxides can be easily obtained by EPMA. It is

322 noted that although the dataset 1 model yields relatively larger uncertainties than the
323 dataset 2 model, the former is still recommended here because it covers a wider range of
324 mica types and compositions. Considering the limited number of aluminophlogopite and
325 tainiolite in the compilation, our method may cause large errors for these two mica types.
326 The micas that have undergone modification under disequilibrium conditions are not
327 suggested for prediction. In this study, a user-friendly Excel spreadsheet is provided for
328 calculating Li_2O from EPMA data (Table S2).

329

330 **Application of the MPR to exploration of Li deposits in NE China**

331 Recent studies have discovered a series of Li-W-Sn-Nb-Ta deposits in central Inner
332 Mongolia of northeastern China, which are located at depth in a previously explored
333 Weilasituo ore district dominated by volcanic-subvolcanic Cu-Pb-Zn-Ag deposits (Fig. 7;
334 Wang et al. 2017; Li et al. 2018; Gao et al. 2019). More than 600 Kt of ore with an
335 average Li grade of 1.25 wt% have been estimated in this region, indicative of good
336 prospects for exploitation (Li et al. 2017). Gao et al. (2019) conducted a detailed analysis
337 of mica compositions from the Weilasituo ore bodies. Their results reflect the
338 predominant ore minerals of zinnwaldites, which contain 3.5–5 wt% Li_2O contents
339 measured by LA-ICP-MS (Gao et al. 2019). To test the predictive capability of our
340 method in the specific case, we start by applying the Excel spreadsheet provided in this
341 study to predict the Li_2O contents of the Weilasituo micas (60 analyses) from Gao et al.
342 (2019), which have not been used in the ML. The predicted values are in good agreement

343 with the measured Li_2O contents within limited errors of ± 0.5 wt% (Fig. 8a). The
344 prediction of the Li_2O - SiO_2 equations is comparable with our method (Figs. 8b-c), but the
345 Li_2O - MgO and Li_2O - F equations perform worse (Figs. 8d-f).

346 To further explore the potential Li resources in central Inner Mongolia of NE China, we
347 collected 12 rock samples on the basis of geochemical anomalies, including granites,
348 greisens, pegmatites, quartz porphyry and metamorphic rocks from the Weilasituo, Jabusi,
349 Shihuiyao and Bayangen areas (Fig. 7). Micas in these samples occur as subhedral to
350 euhedral crystals and represent the main Li-bearing minerals. Representative
351 compositional profiles of 2 to 6 mica grains were performed by EPMA for each sample.
352 The analyzed method and chemical compositions of micas (471 analyses) are given in
353 Test S1 and Table S3. We predict 2.66–4.43 wt% Li_2O for micas from the Weilasituo
354 quartz porphyry (sample WLST-5), which is comparable with the reported values of 3.72–
355 4.22 wt% Li_2O (Gao et al. 2019), while micas from a plagioclase gneiss (sample WLST-1)
356 of the metamorphic basement mainly consists of Mg-biotites with predicted Li_2O contents
357 of 0–0.24 wt% (Fig. 9). In addition to the Weilasituo mining area, the Jiabusi area seems
358 to have a good potential for Li resources in terms of dominant Li-rich micas in the granite
359 and greisen samples (samples JBS-1-4), with the compositions ranging from Li-phengite
360 and zinnwaldite to lepidolite (Fig. 9). Especially, lepidolites in sample JBS-2 show Li_2O
361 contents of 4.80–6.69 wt%, which are higher than the zinnwaldites in the Weilasituo ore
362 bodies (up to 4.85 wt% Li_2O ; Gao et al. 2019). In the Bayangen area, micas from the
363 granite, pegmatite and quartz schist (samples BYG-6-8) are phengites with low Li_2O

364 abundances of 0–0.44 wt% (Fig. 9). In the Shihuiyao area, the greisen (sample SHY-1) and
365 granite (sample SHY-3) contain phengite-muscovite with 0–0.72 wt% Li_2O , while the
366 surrounding metamorphic sedimentary rock (sample SHY-2) contains Li-bearing phengite
367 with higher Li_2O of 0.60–2.93 wt% (mostly >2 wt%; Fig. 9). In summary, our work
368 suggests that Li in micas from the Jiabusi granite and greisen (avg. Li_2O 3.35 wt%) and the
369 Shihuiyao metamorphic sediment (avg. Li_2O 2.44 wt%) reach industrial standards and
370 have good prospects for exploitation.

371 Furthermore, the various types and compositions of micas in rocks from different
372 occurrences may provide crucial mineralogical constraints on metallogenic processes. In
373 the Weilasituo area, the Li_2O contents of Mg-biotites from the plagioclase gneiss of the
374 metamorphic basement (0–0.24 wt% Li_2O) are lower than those of zinnwaldites from the
375 plagioclase gneiss surrounding the ore veins (4.28–4.49 wt% Li_2O ; Gao et al. 2019),
376 indicating that the wall rock was probably metasomatized by ore-bearing hydrothermal
377 fluids. In the Shihuiyao area, micas from the metamorphic sediment are enriched in Li_2O
378 relative to the intrusive granite or greisen, which probably indicates an input of Li from
379 Li-rich sources during sedimentation. Metamorphism may also contribute the increase of
380 Li in micas.

381 Considering that Li preferentially partitions into the melt during partial melting or
382 fractionation processes, the variations of Li at the mineral scale is routinely used as a
383 geochemical tracer for understanding and reconstruction of magmatic and mineralizing
384 processes (Charoy et al. 1995; Henderson et al. 1989; Neiva 2013; Breiter et al. 2017a;

385 [Garate-Olave et al. 2018](#); [Bretier et al. 2019](#)). Back-scattered electron (BSE) images show
386 that most mica grains in the studied samples display heterogeneous or zoned patterns.
387 The chemical profiles determined by EPMA with Li₂O calculated by the MPR method
388 exhibit similar compositional characteristics, especially for the Jiabusi samples, which
389 display various compositions for individual grains ([Table S3](#)). As illustrated in [figure 10a](#),
390 a mica grain from sample JBS-1 has core-to-rim zoning, characterized by a wide, darker
391 core of zinnwaldite (Li <2.2 apfu) and a thin, lighter rim of lepidolite (Li >2.2 apfu), with
392 their contact being regular. The lepidolite crystals from sample JBS-2 show a similar
393 compositional zoning with a BSE-dark core and a BSE-light rim ([Fig. 10b](#)). A
394 quantitative analysis demonstrates that Li enrichment in the rim domain (Li >3 apfu)
395 exceeds that of the core domain (Li <3 apfu) ([Fig. 10b](#)). The core-rim patterns and
396 various chemical compositions of micas in the Jiabusi area probably indicate that the Li
397 mineralization is related to highly fractionated granitic magmas, although more work is
398 needed to confirm this in the future. It is noted that the application of in-situ techniques to
399 obtain complex compositional features in mica grains is sometimes hampered by the large
400 beam diameter (30–100 μm for LA-ICP-MS) required for analysis. Integration of EPMA
401 (beam diameter ≤5 μm) and MPR methods presents a robust and convenient approach for
402 conducting microanalysis of Li in micas.

403

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CONCLUSIONS

405 Our study provides a new MPR analysis using a ML algorithm to estimate the Li₂O
406 contents of mica from their compositions obtained by EPMA. This method is more
407 precise, accurate and generalized than the previously published empirical equations.
408 Application of MPR to samples from central Inner Mongolia, NE China, suggests that in
409 addition to the Weilasituo ore bodies, Li-rich micas from the Jiabusi granite and greisen
410 and the Shihuiyao metamorphic sediment formation have good prospects for Li
411 exploitation. Integration of EPMA and MPR provides a robust and convenient approach
412 for conducting microanalysis of Li in micas. Detailed analysis of mica compositions in
413 different rocks enhances our understanding of the mineralization in the Jiabusi and
414 Shihuiyao ore bodies, with the former likely being associated with Li-enriched
415 sedimentary sources and the latter likely relating to highly fractionated granitic magmas.

416

417

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TABLES

TABLE 1. R^2 and RMSE values for training and test sets by the MPR method

No.	Training set		Test set	
	R^2	RMSE (wt%)	R^2	RMSE (wt%)
<i>Dataset1</i>				
1	0.95	0.31	0.94	0.39
2	0.95	0.32	0.94	0.37
3	0.95	0.32	0.95	0.35
4	0.95	0.32	0.92	0.40
5	0.96	0.30	0.91	0.44
6	0.95	0.32	0.94	0.36
7	0.95	0.31	0.93	0.41
8	0.95	0.32	0.89	0.48
9	0.95	0.32	0.93	0.39
10	0.95	0.32	0.95	0.36
11	0.95	0.32	0.90	0.47
12	0.95	0.32	0.92	0.42
13	0.96	0.30	0.87	0.54
14	0.95	0.32	0.94	0.36
15	0.95	0.32	0.93	0.39
16	0.95	0.30	0.93	0.43
17	0.96	0.31	0.90	0.46
18	0.96	0.31	0.88	0.50
19	0.95	0.32	0.91	0.45
20	0.93	0.38	0.92	0.44
<i>Dataset2</i>				
1	0.96	0.22	0.95	0.26
2	0.97	0.21	0.95	0.25
3	0.97	0.21	0.94	0.24
4	0.97	0.19	0.94	0.31
5	0.97	0.21	0.94	0.28
6	0.97	0.20	0.93	0.29
7	0.97	0.20	0.93	0.27
8	0.97	0.20	0.94	0.30
9	0.97	0.20	0.93	0.26
10	0.96	0.20	0.94	0.29
11	0.97	0.20	0.92	0.30
12	0.97	0.19	0.93	0.31

13	0.97	0.21	0.94	0.27
14	0.96	0.21	0.96	0.26
15	0.97	0.19	0.92	0.33
16	0.96	0.22	0.96	0.22
17	0.97	0.20	0.93	0.28
18	0.97	0.20	0.93	0.30
19	0.97	0.21	0.94	0.27
20	0.97	0.20	0.93	0.31

Note: n = 20 random splitting for each data model.

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TABLE 2. Summary of published empirical equations for estimating Li₂O contents in tri- and di-octahedral micas

Equations	Analyzed number	Goodness of fit (R^2)	Range of validity (wt%)
$\text{Li}_2\text{O}^a = (0.287 \times \text{SiO}_2) - 9.552$	400	0.90	Trioctahedral micas with MgO <8
$\text{Li}_2\text{O}^{b,c} = (0.289 \times \text{SiO}_2) - 9.658$	232	0.91	Trioctahedral micas with Li ₂ O >0.6, MgO <3, SiO ₂ >34
$\text{Li}_2\text{O}^c = [2.7 / (0.35 + \text{MgO})] - 0.13$	434	0.88	Trioctahedral micas with MgO = 0.01 to 20
$\text{Li}_2\text{O}^c = 0.237 \times \text{F}^{1.544}$	501	0.85	Trioctahedral micas with F = 0.1–9
$\text{Li}_2\text{O}^c = 0.177 \times \text{F}^{1.642}$	439	0.91	Trioctahedral micas excluding aplites and pegmatites
$\text{Li}_2\text{O}^c = 0.3935 \times \text{F}^{1.326}$	199	0.84	Diocahedral mica
$\text{Li}_2\text{O}^b = 2.1 / (0.356 + \text{MgO}) - 0.088$	870	0.91	Normal group of trioctahedral

			micas with MgO = 0–24.5
$\text{Li}_2\text{O}^b = 98/(12.8+\text{MgO})-0.3$	22	0.94	High Li-Mg, Al-poor group of trioctahedral micas with MgO = 0–29.0
$\text{Li}_2\text{O}^b = 50.3/(6.5+\text{MgO})-1.54$	84	0.90	High Li-Mg, Al-rich group of trioctahedral micas with MgO = 0–26.2
$\text{Li}_2\text{O}^d = 0.7200 \times F - 0.6120$	9	0.97	—
$\text{Li}_2\text{O}^e = 0.7823 \times F + 0.0131$	42	0.92	—
$\text{Li}_2\text{O}^f = 0.5387 \times F - 0.1205$	11	0.97	—
$\text{Li}_2\text{O}^g = 0.5808 \times F - 0.0669$	—	—	—

^aTindle and Webb (1990). ^bTischendorf (1999). ^cTischendorf et al. (1997). ^dRoda et al. (2007).

^eVan Lichterfelde et al. (2008). ^fVieira et al. (2011). ^gMartins et al. (2012).

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TABLE 3. R^2 and RMSE values for the best-performed MPR model and published empirical equations

Equations	Dataset1			Dataset2		
	Number	R^2	RMSE (wt%)	Number	R^2	RMSE (wt%)
MPR ^a	638	0.95	0.35	416	0.96	0.22
$\text{Li}_2\text{O}^b = (0.287 \times \text{SiO}_2) - 9.552$	164	0.82	0.73	51	0.84	0.68

$\text{Li}_2\text{O}^{\text{c,d}}=(0.289\times\text{SiO}_2)-9.658$	124	0.68	0.88	33	0.52	0.78
$\text{Li}_2\text{O}^{\text{d}}=[2.7/(0.35+\text{MgO})]-0.13$	220	0.53	1.86	80	0.57	1.30
$\text{Li}_2\text{O}^{\text{d}}=0.237\times\text{F}^{1.544}$	311	0.82	0.95	168	0.80	0.74
$\text{Li}_2\text{O}^{\text{d}}=0.177\times\text{F}^{1.642}$	394	0.78	0.85	143	0.78	0.81
$\text{Li}_2\text{O}^{\text{d}}=0.3935\times\text{F}^{1.326}$	306	0.51	0.40	242	0.53	0.33

^athis study. ^bTindle and Webb (1990). ^cTischendorf (1999). ^dTischendorf et al. (1997).

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FIGURE CAPTIONS

860 **FIGURE 1.** Compiled mica compositions from dataset 1 (a) and dataset 2 (b) plotted in
861 the classification diagram of Tischendorf et al. (1997). Mineral abbreviations:
862 lepidomelane (Lpm), protolithionite (Prl), siderophyllite (Sdr), biotite (Bt), phlogopite
863 (Phl), lepidolite (Lpd), zinnwaldite (Znw), phengite (Ph), muscovite (Ms), and taeniolite
864 (Tae).

865 **FIGURE 2.** Predicted vs. measured Li_2O contents for the best-performed dataset 1 (a)
866 and dataset 2 (b) models using the MPR method.

867 **FIGURE 3.** Error distributions for the test set of the best-performed dataset 1 (a) and
868 dataset 2 (b) models.

869 **FIGURE 4.** Predicted vs. measured Li_2O contents for the published empirical equations
870 using the test set of the best-performed dataset 1 model. The green diamonds refer to
871 predicted results of the MPR method. The orange crosses refer to predicted results of
872 micas that match the recommended ranges of validity for the empirical equations, and the

873 blue crosses are those falling outside the ranges of validity.

874 **FIGURE 5.** Predicted vs. measured Li_2O contents for the published empirical equations
875 using the test set of the best-performed dataset 2 model. The symbols are the same as
876 those in figure 4.

877 **FIGURE 6.** Li_2O vs. F diagrams for di- and tri-octahedral micas in dataset 2.

878 **FIGURE 7. (a)** Location of central Inner Mongolia (modified after [Jahn 2004](#)). **(b)**
879 Geological sketch map of central Inner Mongolia showing lithological and tectonic units
880 (modified after [Lu et al. 2020](#) and [Qian et al. 2017](#)). Abbreviations: NCC–North China
881 craton. TC–Tarim craton. WLST–Weilasituo. SHY–Shihuiyao. BYG–Bayangen. JBS–
882 Jiabusi. SMACM–South Mongolia–Uliastai active continental margin. HOAC–
883 Hegenshan ophiolite accretionary complex. BAAC–Baolidao arc accretionary complex.
884 SOAC–Solonker ophiolite accretionary complex. OAC–Ondor Sum subduction
885 accretionary complex. BA–Bainaimiao arc.

886 **FIGURE 8.** Predicted vs. measured Li_2O contents for the MPR method and empirical
887 equations on micas from [Gao et al. \(2019\)](#).

888 **FIGURE 9.** Classification diagram of [Tischendorf et al. \(1997\)](#) illustrating mica
889 compositions of rock samples from the Weilasituo, Jiabusi, Shihuiyao and Bayangen
890 areas. Mineral abbreviations are the same as those in figure 1.

891 **FIGURE 10.** Photomicrographs (polarized plane), BSE images and Li (apfu) profiles of
892 representative mica grains from the Jiabusi area. Mineral abbreviations: albite (Ab),
893 lepidolite (Lpd), elbaite (Elb), zinnwaldite (Znw), fluorite (Fl), topaz (Tpz).

Figure 2

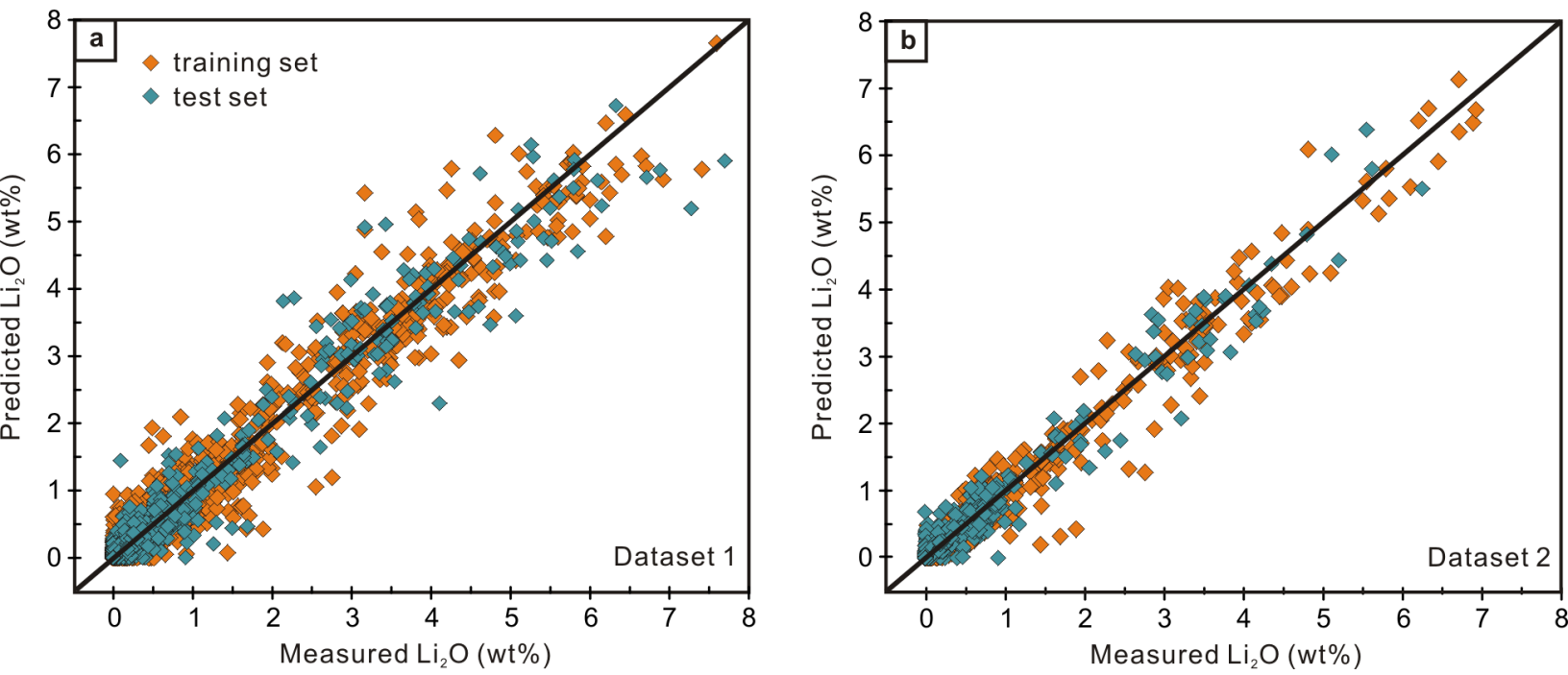


Figure 3

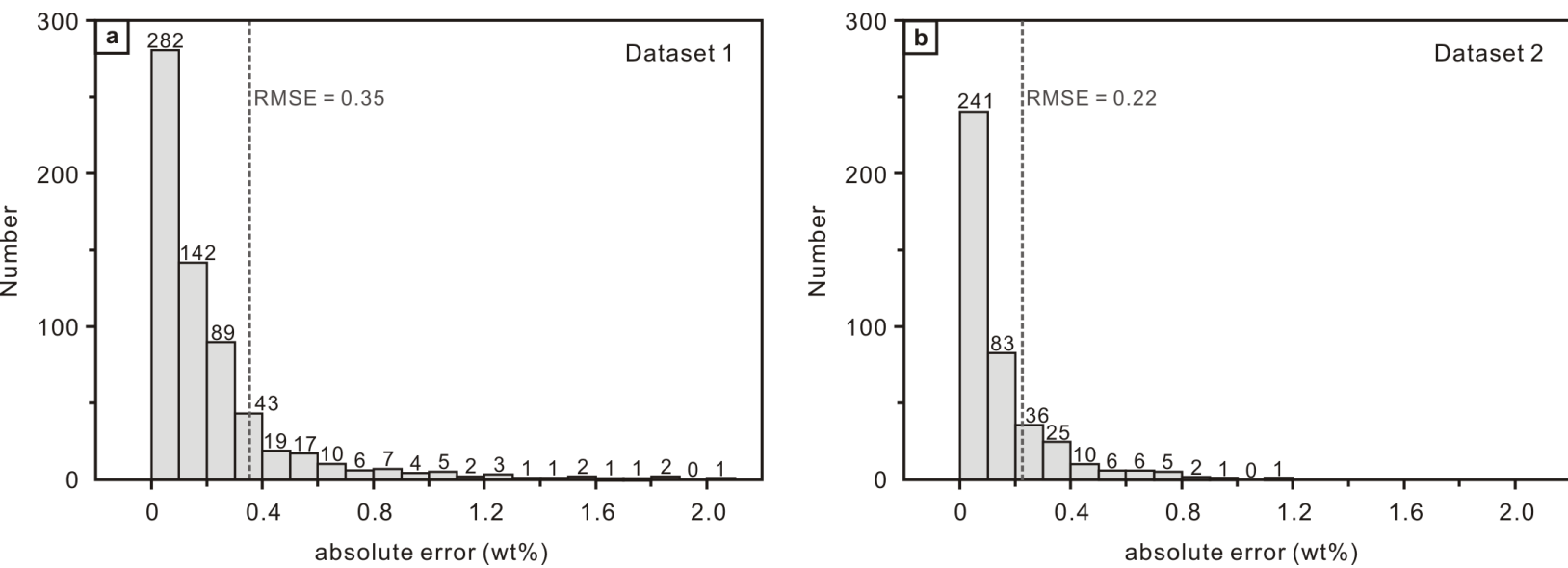


Figure 4

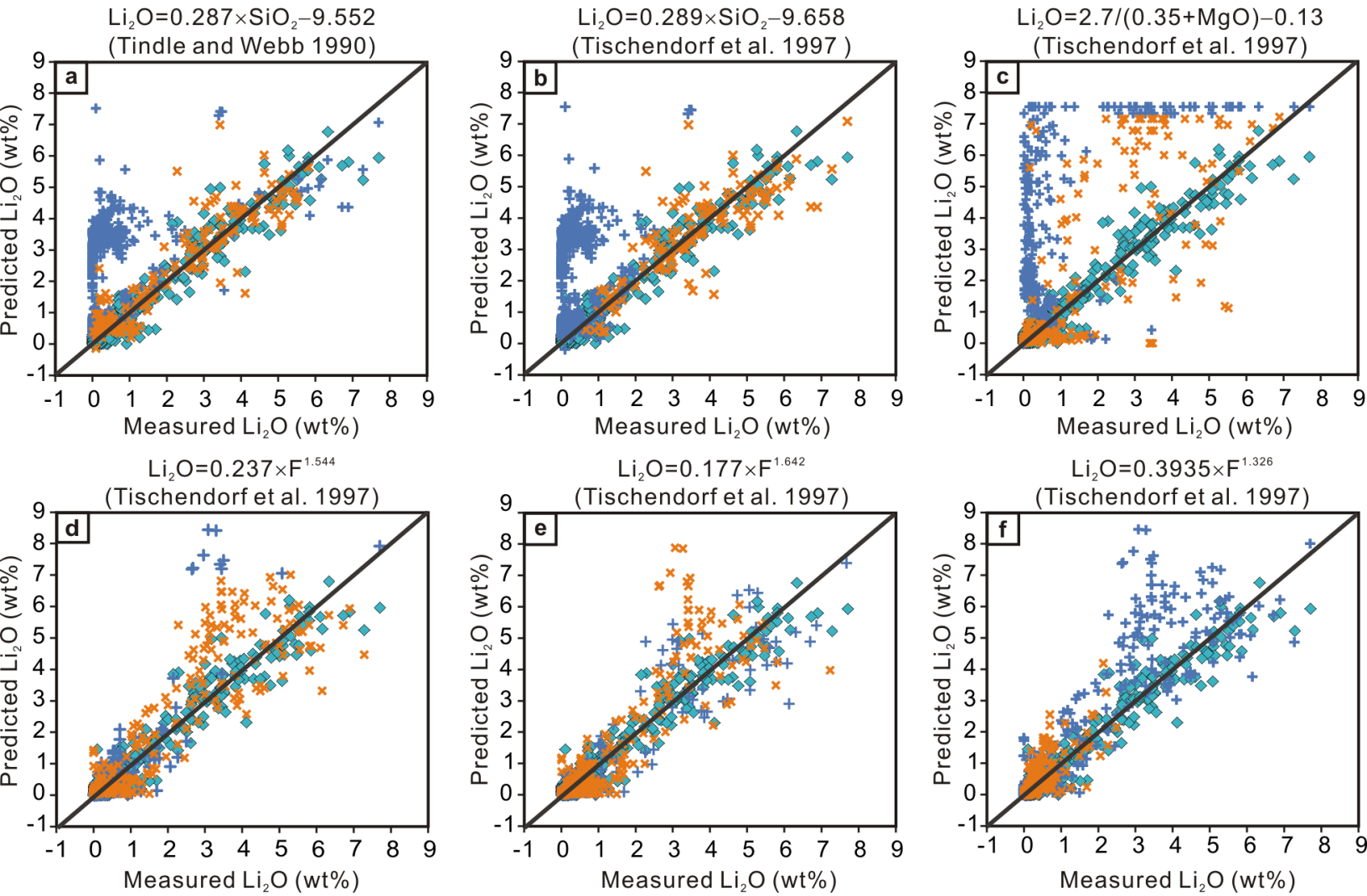


Figure 5

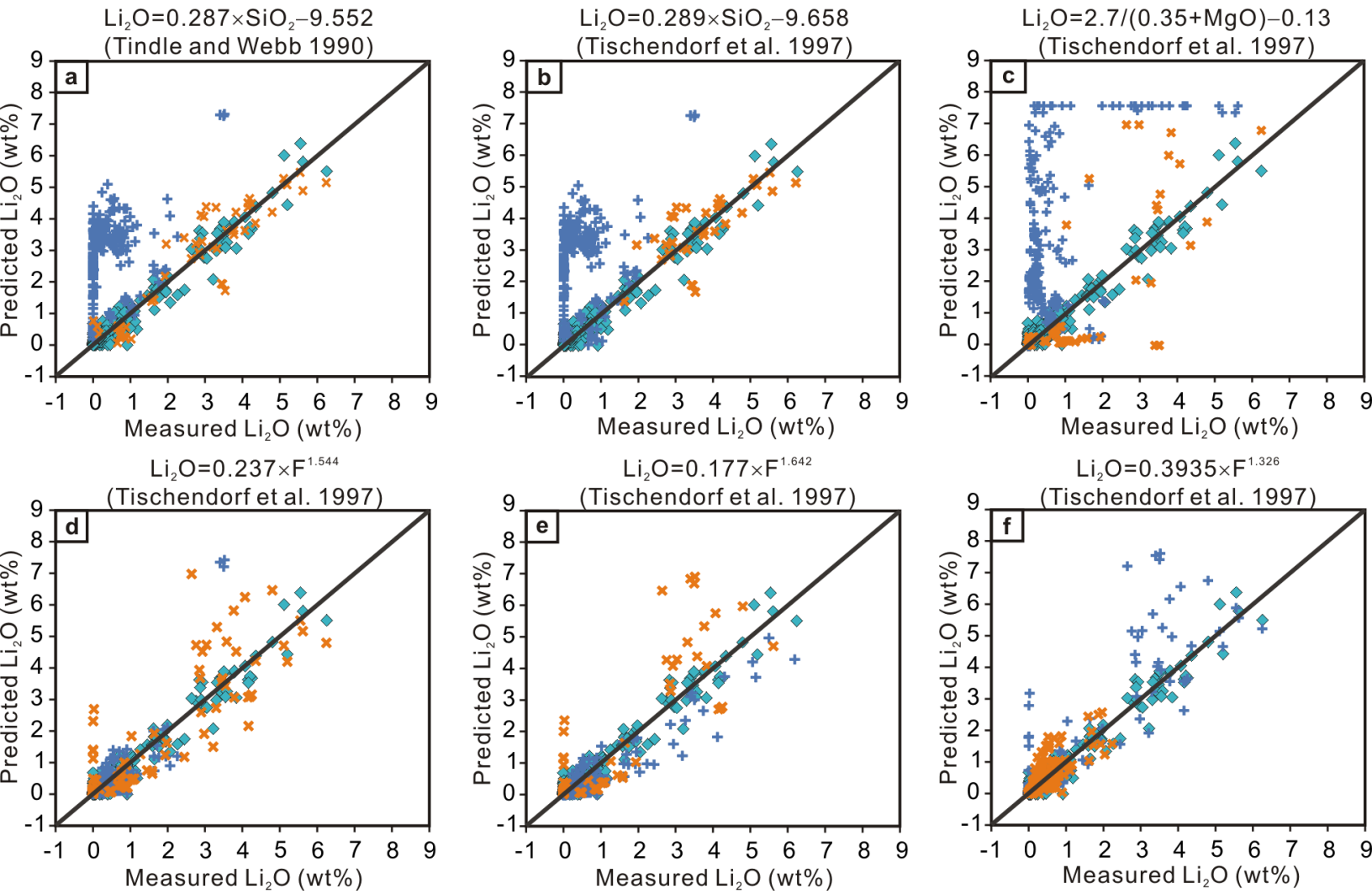


Figure 6

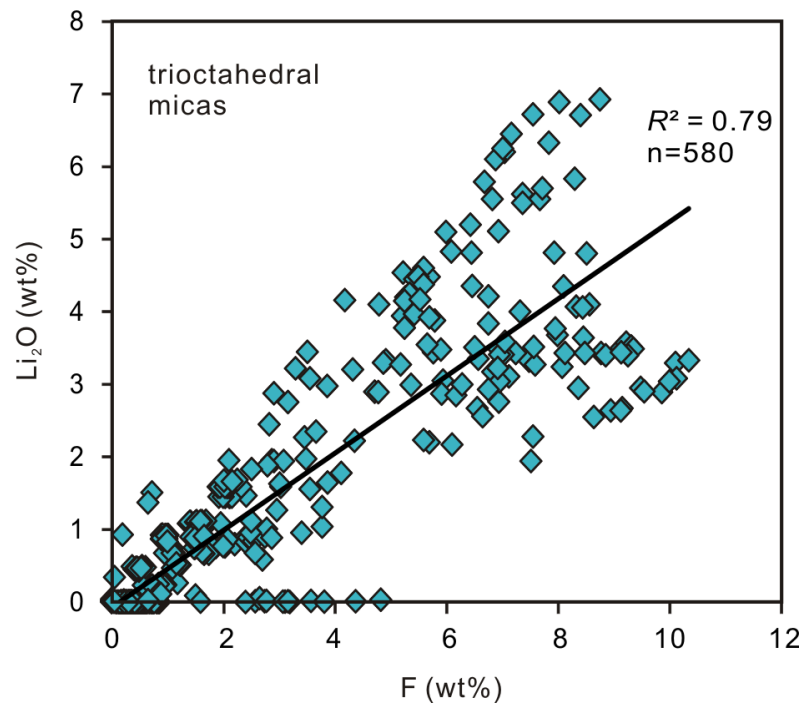
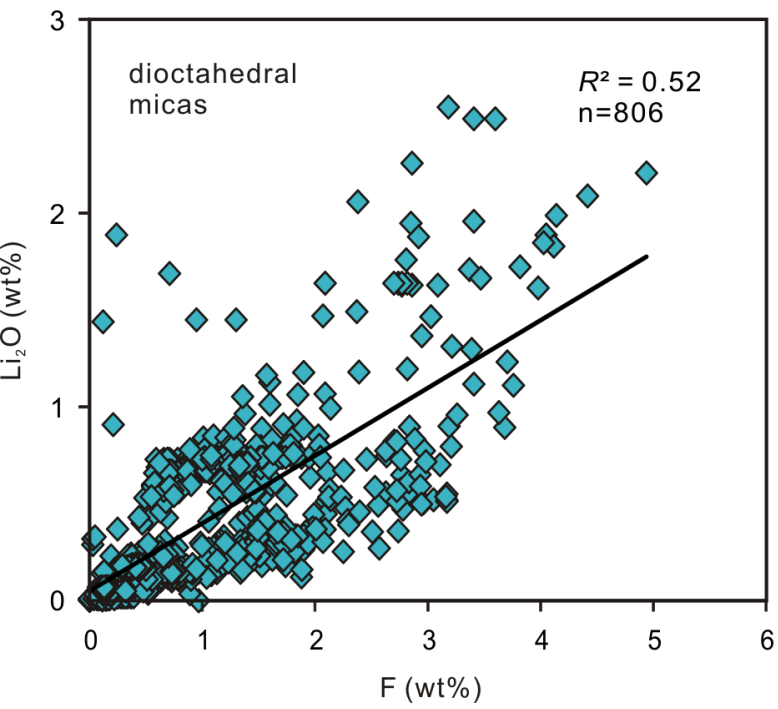


Figure 7

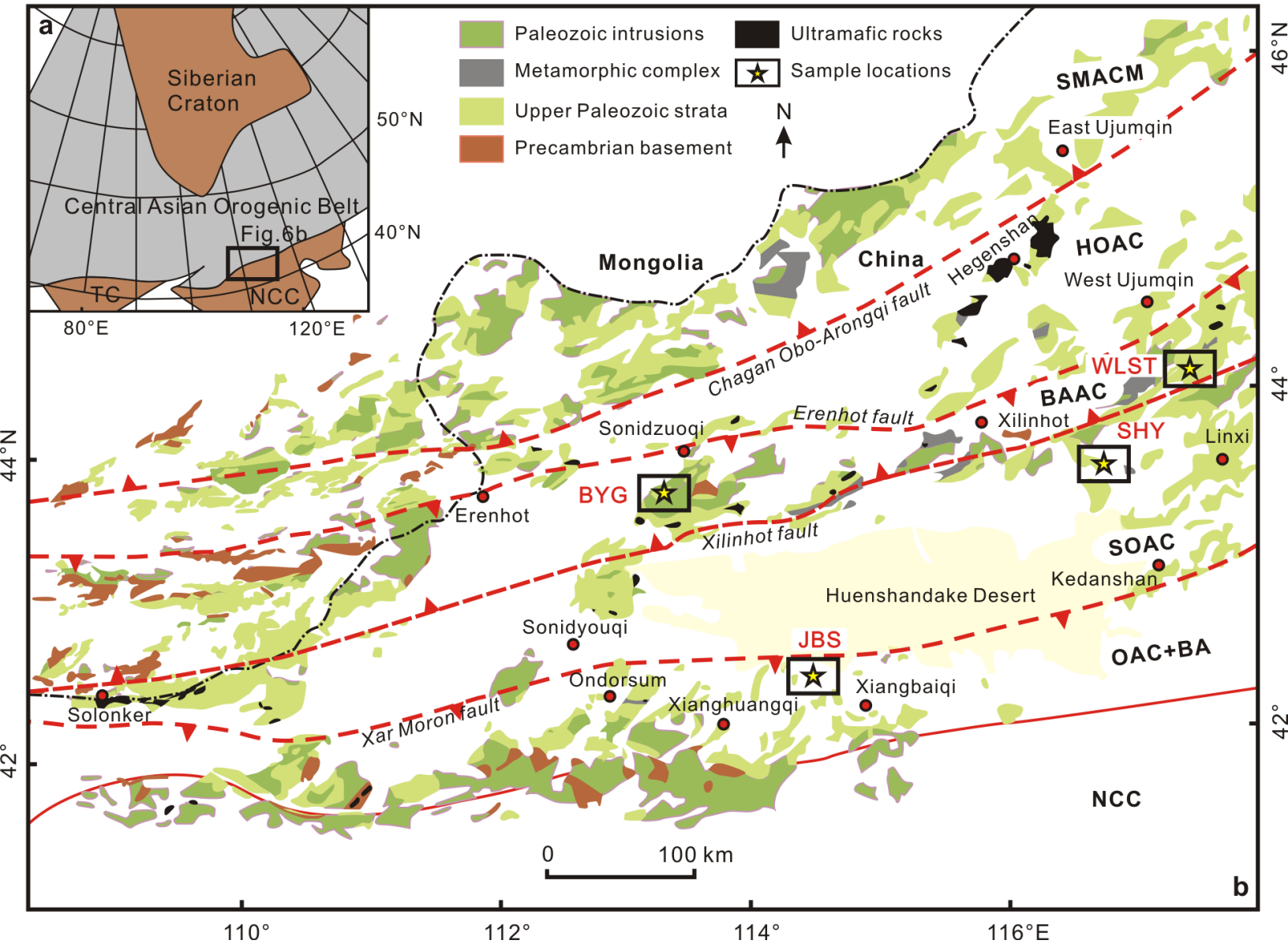


Figure 8

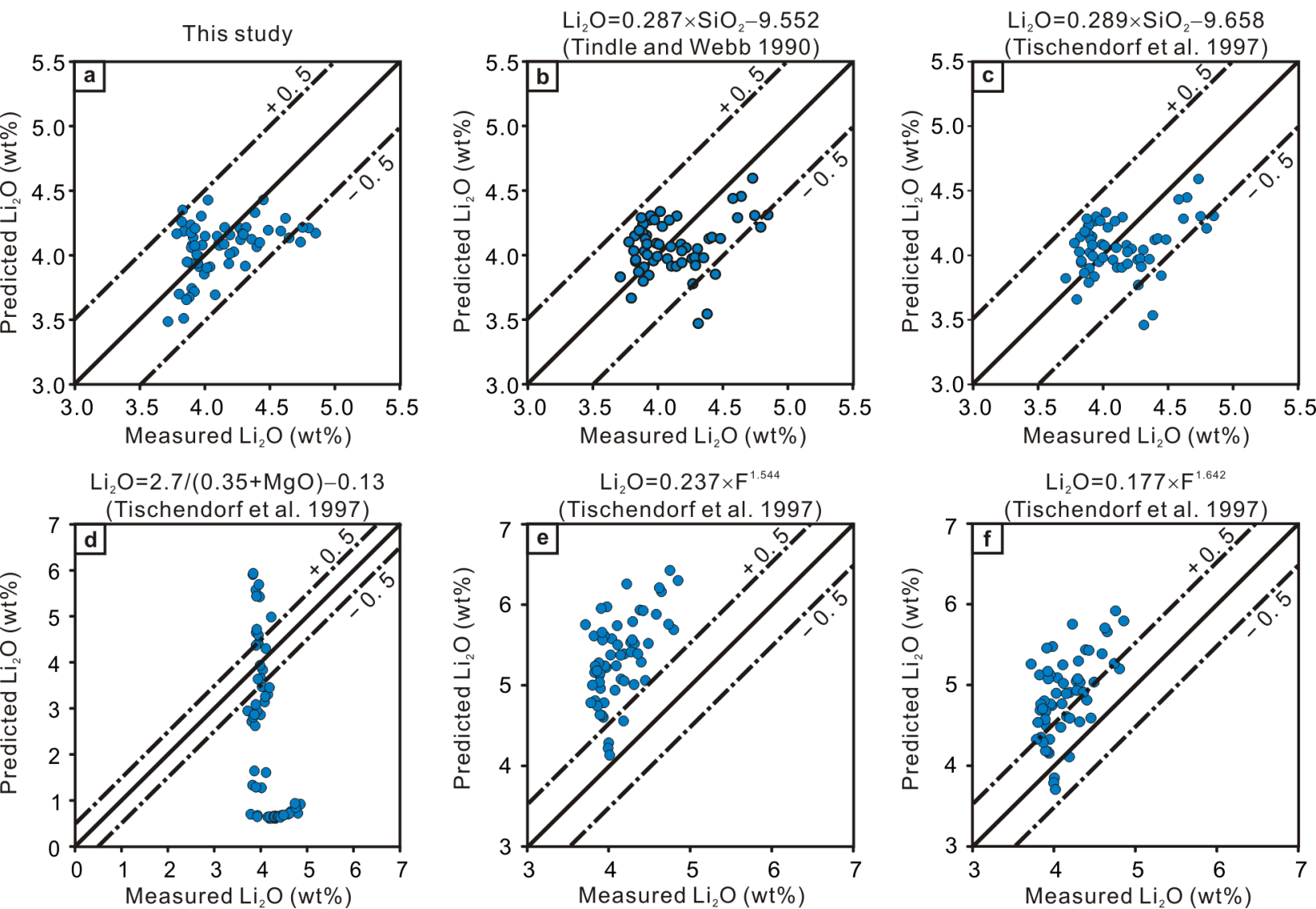


Figure 9

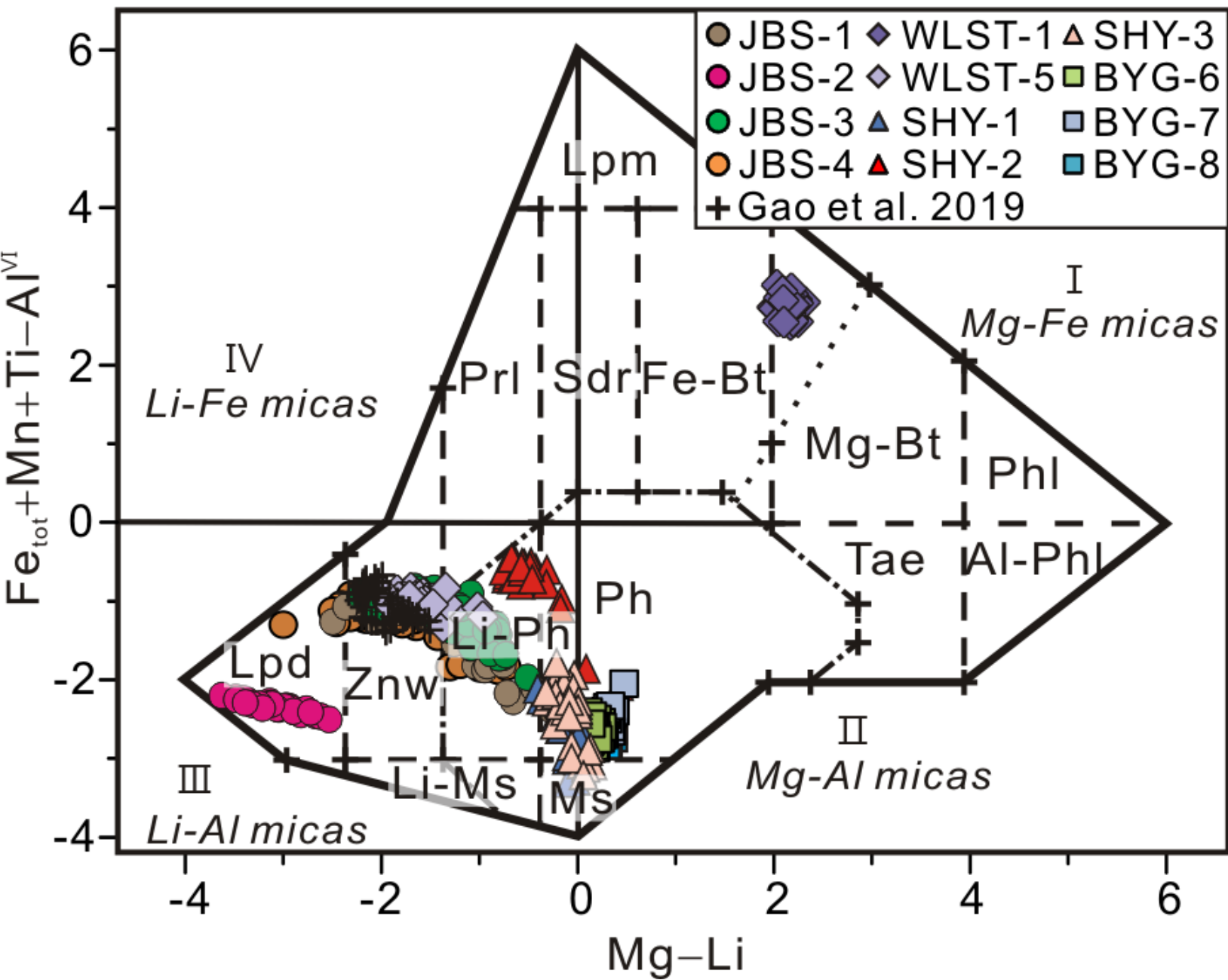


Figure 10

