1	Effect of structural water on the elasticity of orthopyroxene
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14	Abstract:
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16	As a major nominally anhydrous mineral (NAM) in the Earth's upper mantle, orthopyroxene could
17	host up to several hundred ppm $H_2O$ in its crystal structure and transport the $H_2O$ to the deep Earth.
18	To study the effect of structural $H_2O$ on the elasticity of orthopyroxene, we have measured the
19	single-crystal elasticity of $Mg_{1.991}Al_{0.065}Si_{1.951}O_6$ with 842-900 ppm H <sub>2</sub> O and 1.64±0.20 wt.% Al <sub>2</sub> O <sub>3</sub>
20	at ambient conditions using Brillouin spectroscopy. The best-fit single-crystal elastic moduli ( $C_{ij}s$ ),
21	bulk $(K_{S0})$ and shear $(G_0)$ modulus of the hydrous Al-bearing orthopyroxene were determined as:
22	$C_{11}=235(2)$ GPa, $C_{22}=173(2)$ GPa, $C_{33}=222(2)$ GPa, $C_{44}=86(1)$ GPa, $C_{55}=82(1)$ GPa, $C_{66}=82(1)$ GPa,
23	$C_{12}=75(3)$ GPa, $C_{13}=67(2)$ GPa, and $C_{23}=49(2)$ GPa, $K_{50}=111(2)$ GPa, and $G_{0}=78(1)$ GPa.
24	Systematic analysis based on the results presented in this and previous studies suggests that the
25	incorporation of 842-900 ppm H <sub>2</sub> O would increase $C_{13}$ by 12.0(7)% and decrease $C_{23}$ by 8.6(8)%.
26	The effects on $C_{11}$ , $C_{22}$ , $C_{33}$ , $C_{44}$ , $C_{66}$ , $K_{50}$ and $V_P$ are subtle if not negligible when considering the
27	uncertainties. The $C_{55}$ , $C_{12}$ , $G_0$ , and $V_S$ are not affected by the presence of structural H <sub>2</sub> O. Although

- 28 laboratory experiments show that Fe,Al-bearing orthopyroxenes can host up to 0.8 wt% H<sub>2</sub>O in its
- 29 structure, future high pressure-temperature elasticity measurements on orthopyroxene with higher
- $H_2O$  content are needed to help better quantify this effect.
- 31 Keywords: Elasticity; Orthopyroxene; Structural water; Seismic velocities
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#### 33 **1. Introduction**

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Water, in the form of structural H<sub>2</sub>O or free H<sub>2</sub>O, is transported into the deep Earth's interior 35 primarily via subduction. As an important carrier of structural H<sub>2</sub>O, NAMs contain a small amount 36 of H<sub>2</sub>O in the form of hydroxyl as point defects in their crystalline structures (Demouchy and 37 Bolfan-Casanova, 2016; Ni et al., 2017; Ohtani, 2005, 2015; Ohtani et al., 2004). The bonded 38 structural H<sub>2</sub>O can reach up to 1.2-3.1wt.% in the experimentally synthesized NAM crystals (Inoue 39 et al., 1995; Kohlstedt et al., 1996). Moreover, a hydrous ringwoodite inclusion containing ~1.5 wt.% 40 H<sub>2</sub>O was recently discovered in a natural diamond (Pearson et al., 2014), further highlighting the 41 critical role that NAMs played as a possible major volatile reservoir in the deep Earth. Structural 42 43 H<sub>2</sub>O significantly impacts the ionic diffusion, dislocation motion, electrical conductivity, phase transitions, melting temperature, and viscosity of mantle minerals (Costa and Chakraborty, 2008; 44 Demouchy and Bolfan-Casanova, 2016; Jacobsen et al., 2010; Yoshino et al., 2009; Zhang et al., 45 2012). In particular, recent studies have suggested that the presence of structural  $H_2O$  can result in 46 some observable seismic signatures in the deep Earth (Kong et al., 2020; Van der Meijde et al., 2003; 47 Yuan and Beghein, 2013). Consequently, evaluating the effect of structural H<sub>2</sub>O on the elastic 48 properties of NAMs is crucial to understand the seismic structure, volatile recycling, and mantle 49 mineralogy in the deep Earth (e.g. Ni et al., 2017; Ohtani, 2015; Ohtani et al., 2004). 50

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The Earth's pyrolitic upper mantle is primarily composed of olivine, orthopyroxene, clinopyroxene, and garnet. The effects of structural  $H_2O$  on the elasticity of olivine and its high-pressure polymorphs have been extensively studied (Buchen et al., 2018; Inoue et al., 1998; Jacobsen et al., 2008; Kavner, 2003; Mao et al., 2008; Mao et al., 2011; Mao et al., 2012; Schulze et al., 2018). It was suggested that the presence of 1 wt.% structural  $H_2O$  in the olivine polymorphs could reduce seismic velocities up to ~2.5% (Inoue et al., 1998; Jacobsen et al., 2008; Mao et al., 2008;

2011; Mao et al., 2012) and enhance the S-wave splitting anisotropy (Inoue et al., 1998; Jacobsen et 58 al., 2008). However, recent studies showed that high pressure would suppress the effect of structural 59 H<sub>2</sub>O and the hydration-induced reductions of sound velocities vanish at transition zone 60 pressure-temperature conditions (Buchen et al., 2018; Schulze et al., 2018). Moreover, the effects of 61 structural H<sub>2</sub>O on the elastic properties of the Na, Al bearing-clinopyroxene and garnet were found 62 to be negligible at room temperature condition (Fan et al., 2019; Mans et al., 2019). Although the 63 orthorhombic orthopyroxene is the second most abundant mineral in the pyrolitic upper mantle, 64 there has been no report about the effect of structural H<sub>2</sub>O on its single-crystal elastic properties to 65 date. 66

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Compared with olivine, H<sub>2</sub>O preferably partitions into orthopyroxene at depth above ~300 km in the 68 upper mantle (Demouchy and Bolfan-Casanova, 2016; Sakurai et al., 2014) and the incorporation of 69 Al as chemical impurity enhances this partitioning process (Grant et al., 2006; Rauch and Keppler, 70 2002; Smyth et al., 2007). There are two substitution mechanisms for structural H<sub>2</sub>O in aluminous 71 orthopyroxene. One is  $Al^{3+} + H^+$  substitution for  $Si^{4+}$  and the other is  $Al^{3+} + H^+$  substitution for 2 72  $Mg^{2+}$ . Laboratory-synthesized orthopyroxene crystals with high Al<sub>2</sub>O<sub>3</sub> content (9-12 wt.%) can host 73 up to ~0.8 wt.% H<sub>2</sub>O in its crystal structure (Mierdel et al., 2007), although natural orthopyroxenes 74 commonly show lower H<sub>2</sub>O concentration on the level of several hundred to 1000 ppm (Ohtani, 75 2015; Xu et al., 2018). 76

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Orthopyroxene presents the lowest isotropic aggregate compressional and shear velocities ( $V_P$  and 78  $V_{\rm S}$ ) among all major upper mantle minerals, and has been proposed as a candidate to explain the low 79 seismic velocity zones in the upper mantle (Reynard et al., 2010). Single crystal elastic properties of 80 Al, Fe, and Ca-bearing orthopyroxene have been experimentally determined in a wide 81 compositional range (Bass and Weidner, 1984; Chai et al., 1997; Flesch et al., 1998; Jackson et al., 82 1999, 2007; Perrillat et al., 2007; Picek, 2015; Qian et al., 2018; Reynard et al., 2010; Webb and 83 Jackson, 1993; Zhang et al., 2013; Zhang and Bass, 2016). The incorporation of Fe significantly 84 reduces the elastic moduli of orthopyroxene, whereas Al increases them (Picek, 2015). The 85 incorporation of Ca, on the other hand, slightly decreases the elastic properties of orthopyroxene 86 (Perrillat et al., 2007). In this study, to evaluate the effect of structural H<sub>2</sub>O on elastic properties of 87

orthopyroxene, we conducted single-crystal Brillouin spectroscopy measurements of synthetic Al-bearing orthopyroxene with 842-900 ppm  $H_2O$  at ambient conditions.

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# 91 2. Materials and Methods

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Hydrous Al-bearing orthopyroxene crystals were synthesized at 5.5 GPa and 1473 K using a 93 multi-anvil large volume press at National Cheng Kung University. Starting materials were oxide 94 95 and hydroxide mixtures of SiO<sub>2</sub>, MgO, Mg(OH)<sub>2</sub>, and Al(OH)<sub>3</sub>. Detailed synthesis method and procedure can be found in Hua et al. (2020). The size of the synthesized crystals ranges from 100 to 96 200 µm. The chemical composition of the crystals measured in this study was determined using a 97 JEOL 8200 Electron Microprobe at the Institute of Meteoritics at University of New Mexico, 98 operating at 15 kV accelerating voltage and 20 nA beam current. The element standards were 99 olivine for Mg and Si, enstatite oxygen standard for O, and orthoclase for Al. The chemical formula 100 is determined to be Mg<sub>1.991</sub>Al<sub>0.065</sub>Si<sub>1.951</sub>O<sub>6</sub> with 39.82(43) wt.% MgO, 58.18(73) wt.% SiO<sub>2</sub>, and 101 1.64(20) wt.% Al<sub>2</sub>O<sub>3</sub>. The H<sub>2</sub>O content was measured by SIMS technique and determined to be 102 103 842-900 ppm (Hua et al., 2020).

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Three hydrous Al-bearing orthopyroxene crystals, which were examined to be inclusion-free under 105 petrographic microscope, were selected and double-side polished with Al<sub>2</sub>O<sub>3</sub> polishing film. The 106 thicknesses of the samples were 18-20 µm. The orientations and unit cell parameters of two samples 107 were determined in the Atlas X-Ray Diffraction Lab at the University of Hawai'i at Manoa and the 108 third one was measured at 13-BM-C, GeoSoilEnviroCARS (GESCARS), Advanced Phonon Source, 109 Argonne National Laboratory. The experimental setup and details can be found in Mans et al. (2019). 110 The face normals of the three polished crystals are (0.940, -0.150, 0.307), (-0.566, 0.675, 0.472), 111 and (-0.099, -0.558, -0.824) referring to the fractional coordinate system for orthopyroxene with 112 unit cell axes a, b, and c as basis vectors. The accuracy of the measured plane normal is better than 113 0.5°, which arises from the angular difference between the rotational axis of the DAC sample holder 114 and the incident X-ray beam at the Atlas X-Ray diffraction Lab at University of Hawaii and 115 GSECARS sector13BMC. The unit cell parameters (a=5.175(3) Å, b=8.804(7) Å, c=18.216(3) Å, 116 and V=829.84(83) Å<sup>3</sup>) were determined by analyzing the X-ray diffraction images from all three 117

samples, and the density was then calculated to be  $\rho_0=3.218(3)$  g/cm<sup>3</sup> using the chemical formula and unit cell volume.

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Brillouin spectroscopy measurements were conducted in the high-pressure laser spectroscopy 121 laboratory at the University of New Mexico. A 300 mW single-mode diode-pumped solid state laser 122 with a wavelength ( $\lambda_0$ ) of 532 nm was employed as the light source. A Sandercock-type 6-pass 123 tandem Fabry-Pérot interferometer was used for resolving the Brillouin frequency shift. The optical 124 125 setup of the Brillouin spectroscopy system can be found in Zhang et al. (2015). All the experiments were conducted using a 50° symmetric forward scattering geometry. The scattering angle ( $\theta$ ) was 126 calibrated to be 50.77(5)° before the experiments by a standard Corning 7980 silica glass, whose 127 velocities have been precisely measured by the GHz ultrasound interferometry (Zhang et al. 2011). 128 The sample crystal was placed on top of the culet of a diamond anvil cell for Brillouin experiments. 129 The tilting and non-parallelism of the sample and the diamond anvil cell are negligible in the 130 experiments. Under cross-polarized illumination of the petrographic microscope, the interference 131 color of the double-side polished crystals is even, suggesting uniform thickness across the crystals. 132 133 On the other hand, as part of the alignment process, we have also examined the tilting using the laser beam reflected at the diamond cutlets, tables and crystal surfaces with 0° incident angle. The 134 reflected laser beams match each other and the incident laser beam nicely, suggesting that the tilting 135 is minimal. We calibrated the free spectral range (FSR) between the FP1 peaks under reflection 136 mode of the interferometer for at least 6 times before and after every experimental run, and the 137 difference is always within 0.5 channels for a total of 1024-channel setup. This propagates to an 138 uncertainty of less than 0.05% of the FSR and thus less than 0.005 km/s for each velocity 139 measurement, which is within the resolution of Brillouin measurements of 0.03 km/s. The  $v_P$  and  $v_S$ 140 were measured at 13 different  $\chi$  angles (0°, 30°, 60°, 90°, 120°, 150°, 180°, 195°, 225°, 255°, 285°, 141 315°, 345°) for all 3 crystals along the 360° azimuth. The differences between determined velocities 142 at  $\chi=0^{\circ}$  and  $\chi=180^{\circ}$  are within 0.05 km/s, again suggesting minimal geometrical errors in the 143 experiments. The typical collection time for each spectrum is 10 minutes. Figure 1 shows a typical 144 Brillouin spectrum and the signal-to-noise ratios are  $\sim 3$  and  $\sim 7$  for  $v_P$  and  $v_S$ , respectively. 145

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147 Under a forward symmetric scattering geometry, the Brillouin shift  $\Delta \omega$ , which is the difference

between incident laser frequency ( $\omega_i$ ) and scattered light frequency ( $\omega_s$ ), depends on the velocity along the probed phonon direction, the laser wavelength  $\lambda_0$ , and the external experimental angle between the incident and the scattered light  $\theta^*$  (Speziale et al., 2014; Whitfield et al., 1976; Zhang et al., 2015),

$$\Delta \omega = \omega_i - \omega_s = 2sin\left(\frac{\theta_*}{2}\right)\frac{\nu}{\lambda_0} \tag{1}$$

where v is the speed of the acoustic phonons in the sample.

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The nine independent  $C_{ij}$ s can be calculated from the obtained phonon direction –  $v_P - v_S$  data set by a least-squares inversion of the Christoffel equation (Weidner and Carleton, 1977).

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$$\det |c_{ijkl}n_jn_l - \rho v^2 \delta_{ik}| = 0 \tag{2}$$

where  $c_{ijkl}$  is the 4<sup>th</sup> order elasticity tensor,  $n_j$  and  $n_l$  are the directional cosines of the wave 158 vector,  $\rho$  is density, and  $\delta_{ik}$  is the Kronecker delta (Musgrave, 1970). The predetermined plane 159 normal by single-crystal X-ray diffraction were fixed during the inversion process. The angular 160 uncertainty of less than 0.5° for the plane normal would result in an uncertainty of less than 0.01 161 162 km/s in the measured acoustic velocities, which is well below the Brillouin measurement uncertainty of 0.03 km/s. However, we did refine the actual individual experimental phonon 163 directions. Given a starting  $C_{ij}$  model of orthopyroxene (Zhang and Bass, 2016), we calculated a set 164 of phonon directions for each Brillouin measurement after fixing the plane normals. Then based on 165 the phonon direction  $-v_P - v_S$  data set, we calculated the best-fit Cij model through a least-square 166 inversion of the Christoffel equation. Afterwards, we then recalculate the phonon directions of each 167 measurement based on this newly obtained best-fit  $C_{ij}$  model. The recalculated phonon directions 168 and the velocities were used as the input to calculate an updated  $C_{ii}$  model for another round. This 169 170 process was repeated for 2-3 times until the difference in root-mean-square (RMS) residuals of two successive runs was less than 0.001km/s. The final best fit  $C_{ij}$  model we obtained has the RMS error 171 of 0.055 km/s. 172

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### 174 **3. Results**

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176 The best-fit  $C_{ij}$ s are:  $C_{11}$ =235(2) GPa,  $C_{22}$ =173(2) GPa,  $C_{33}$ =222(2) GPa,  $C_{44}$ =86(1) GPa,  $C_{55}$ =82(1)

GPa, C<sub>66</sub>=82(1) GPa, C<sub>12</sub>=74(3) GPa, C<sub>13</sub>=67(2) GPa, and C<sub>23</sub>=49(2) GPa (Table 1). Figure 2 shows 177 the measured acoustic velocities of the three samples (Supplementary Material Table S1-S3) and the 178 179 velocities predicted by the best-fit  $C_{ii}$  model. If the laboratory geometrical errors are negligible, the velocities of orthopyroxene measured at  $\chi$  angle along the 360 ° azimuth should be the same as the 180 velocities determined at  $\chi$ -180°. Figure 2 plots the data measured at  $\chi$  between 180°-360° together 181 with the data measured below  $180^{\circ}$ . The internal consistency between the data collected at  $(0^{\circ}, 30^{\circ})$ , 182 60°, 90°, 120°, 150°) and (180°, 195°, 225°, 255°, 285°, 315°, 345°) again suggests the minimal 183 geometrical errors in this study. Voigt-Reuss-Hill (VRH) averaging scheme was employed to 184 calculate the  $K_{S0}$  and  $G_0$  (Hill, 1963), which yielded 111(2) GPa and 78(1) GPa, respectively. The 185 aggregate  $V_P$  and  $V_S$  are calculated to be 8.18(3) km/s and 4.94(2) km/s, respectively. 186

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Our study demonstrates that the effects of Al<sub>2</sub>O<sub>3</sub> and structural H<sub>2</sub>O on the elasticity of 188 orthopyroxene are coupled, and there is no existing study to quantify the contribution of Al<sub>2</sub>O<sub>3</sub>. The 189 elastic properties of Fe-bearing orthopyroxene with Al<sub>2</sub>O<sub>3</sub> content ranging from 0.4-5.0 wt.% have 190 been studied (Chai et al., 1997; Jackson et al., 2007; Webb and Jackson, 1993; Zhang and Bass, 191 192 2016). Decoupling the effects of Fe and Al<sub>2</sub>O<sub>3</sub> is feasible because the effect of Fe on the elasticity of orthopyroxene within a wide range of Fe# (Fe# =  $\frac{[FeO]}{[FeO] + [MgO]}$ ) from 0-100 had been studied (Picek, 193 2015). The  $C_{11}$ ,  $C_{22}$ ,  $C_{33}$ ,  $C_{44}$ ,  $C_{55}$ , and  $C_{66}$  of Fe-bearing orthopyroxene decrease with Fe#, whereas 194  $C_{12}$ ,  $C_{13}$ , and  $C_{23}$  are insensitive to Fe#. To quantify the Al<sub>2</sub>O<sub>3</sub> effect on the elastic properties of 195 orthopyroxene, we would need to firstly evaluate the effect of Fe. Since the Fe# is less than 15 in 196 the Al-bearing orthopyroxene samples studied by Chai et al. (1997), Jackson et al. (2007), and 197 Zhang and Bass (2016), we choose the data with the compositional range of interest for Fe# 0-15 in 198 Picek (2015) together with previous studies (Jackson et al., 1999, 2007) to re-analyze the 199 200 single-crystal elasticity data of Fe-bearing Al-free orthopyroxene. We found that increasing the Fe# by 1 would decrease C<sub>11</sub>, C<sub>22</sub>, C<sub>33</sub>, C<sub>44</sub>, C<sub>55</sub>, and C<sub>66</sub> by -0.38(15) GPa, -0.48(13) GPa, -0.68(6) GPa, 201 -0.06(1) GPa, 0 GPa, and -0.10(1) GPa, respectively. On the other hand, there is ~1.1 wt.% CaO in 202 the Al,Fe-bearing orthopyroxene samples of Chai et al. (1997) and Zhang and Bass (2016). The 203 effect of Ca on the elasticity of orthopyroxene had been carefully studied and 1.1 wt.% CaO would 204 reduce the C<sub>11</sub>, C<sub>22</sub>, C<sub>33</sub>, C<sub>44</sub>, C<sub>55</sub>, C<sub>66</sub>, C<sub>12</sub>, C<sub>13</sub>, and C<sub>23</sub> by 2.2%, 1.7%, 3.5%, 0.56%, 3.8%, -0.75%, 205

206 2.1%, 3.4%, and 5.6%, respectively (Jackson et al., 1999; Perrillat et al., 2007).

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After removing the effects of both Fe and Ca, we plotted the single-crystal and aggregate elastic 208 moduli, as well as aggregate velocities of orthopyroxene as a function of Al<sub>2</sub>O<sub>3</sub> content in Figure 3 209 (Supplementary Material Table S4). The shaded area describes the effect of Al<sub>2</sub>O<sub>3</sub> on the elasticity 210 of orthopyroxene within the 95% confidence interval. The comparison between the data obtained in 211 this study for hydrous Al-bearing orthopyroxene and previous anhydrous Al-bearing orthopyroxene 212 in Figure 3 makes it possible to evaluate the effect of structural H<sub>2</sub>O. The  $C_{11}$ ,  $C_{22}$ ,  $C_{33}$  of the 213 hydrous Al-bearing orthopyroxene are 1.7(2)%, 3.0(1)% and 2.1(4)% lower compared with its 214 anhydrous counterparts, although the difference is subtle considering the experimental uncertainty. 215 On the other hand, the decrease of  $C_{23}$  is more significant, up to 8.6(8)%. Interestingly, structural 216 H<sub>2</sub>O increases  $C_{44}$ ,  $C_{66}$ , and  $C_{13}$  of the Al-bearing orthopyroxene by 2.6(3)%, 4.1(2)%, and 12.0(7)%, 217 respectively. Structural H<sub>2</sub>O has negligible effect on  $C_{55}$ ,  $C_{12}$ ,  $Ks_0$ ,  $G_0$  and Vs, although  $V_P$  is slightly 218 decreased. 219

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In addition, we also calculated the universal anisotropy  $(A^U)$ , azimuthal  $V_P$   $(A^{V_P})$ , and radial  $V_S$ anisotropy  $(D^{V_S})$  of the hydrous Al-bearing orthopyroxene (Ranganathan and Ostoja-Starzewski, 2008).  $A^U$  describes the overall elastic anisotropy for materials with arbitrary symmetry and can be calculated as follows,

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$$A^{U} = 5\frac{G_{V}}{G_{R}} + \frac{K_{S,V}}{K_{S,R}} - 6$$
(3)

where *G* and *K<sub>s</sub>* are the shear and bulk moduli and the subscripts *V* and *R* represent Voigt and Reuss bound, respectively.  $A^{Vp}$  and  $D^{Vs}$  are the maximum  $v_P$  difference along different directions and maximum  $v_s$  difference between the two orthogonally polarized shear waves propagating along the same direction, respectively.

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$$A^{V_P} = \frac{v_{P,max} - v_{P,min}}{v_{P_{VRH}}} \tag{4}$$

$$D^{V_S} = \frac{|v_{S_1} - v_{S_2}|_{max}}{v_{S_{VRH}}}$$
(5)

The calculated anisotropy indices are 0.115(10), 0.148(6), and 0.153(6) and presented in Figure 4. With increasing the Al<sub>2</sub>O<sub>3</sub>,  $A^U$  and  $A^{Vp}$  decrease, whereas  $D^{Vs}$  slightly increases. Compared with the anisotropy indices of anhydrous Al-bearing orthopyroxene, those of hydrous Al-bearing orthopyroxene seem higher, although the increase of  $D^{Vs}$  and  $A^{Vp}$  are too small to be considered significant. The  $A^U$  is most sensitive to the structural H<sub>2</sub>O. 842-900 ppm H<sub>2</sub>O increases the  $A^U$  by 14.4(30)%.

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# 239 4. Discussion and Implications

Within the crystal structure of orthopyroxene, Si-O tetrahedra are connected by the bridging atom 240 O3 to form chains extending along the c-axis, and the (Mg,Fe)-O octahedra are linked with each 241 other through edge-shearing (Fig. S1). The M1 and M2 sites are at the centers of edge-sharing 242 octahedron and discontinuous octahedron, respectively. Compared to Mg, Fe prefers occupying the 243 slightly larger M2 site (Thompson and Downs, 2003). As suggested by Duffy and Vaughan (1988) 244 and Bass and Weidner (1984) for anhydrous orthopyroxene, the C11, C22 and C33 are controlled by 245 the stiffness of the M1, M2 octahedra site and the compressibility of the Si-O tetrahedra chain, 246 respectively. The shear elastic moduli C<sub>44</sub>, C<sub>55</sub>, and C<sub>66</sub> are strongly affected by site ordering. 247 Among them, C<sub>44</sub> is more sensitive to composition and C<sub>55</sub> and C<sub>66</sub> are more sensitive to the 248 octahedra stacking along a-axis. Finally, the off-diagonal elastic moduli C<sub>12</sub>, C<sub>13</sub>, and C<sub>23</sub> vary 249 250 slightly with either structure or composition. The substitution mechanism in hydrous orthopyroxene is dominated by the replacement of  $Si^{4+}$  with  $Al^{3+} + H^+$  in the tetrahedral site or  $Al^{3+} + H^+$  for 2 Mg<sup>2+</sup> 251 in the M1 site (Mierdel et al., 2007). The reduction of C<sub>11</sub>, C<sub>22</sub> and C<sub>33</sub> caused by incorporation of 252 842-900 ppm structural H<sub>2</sub>O is insignificant considering the uncertainty, suggesting that the 253 substitution into the tetrahedral and octahedral sites does not induce a significant change in the 254 compressibility along the a, b and c-axis. Among C44, C55, and C66, C55 shows the least 255 compositional variation (Duffy and Vaughan, 1988). This is consistent with our observed increase of 256 C<sub>44</sub> and C<sub>66</sub> yet negligible change in C<sub>55</sub> as shown in Figure 3. The changes of the off-diagonal C<sub>ij</sub>s 257 such as C<sub>12</sub>, C<sub>13</sub>, and C<sub>23</sub> observed in this study is difficult to be explained structurally, possibly 258 related to the complicated effect caused by both the substitution of Al<sup>3+</sup> into the tetrahedral site and 259 the vacancies in the octahedral M1 and M2 sites introduced by hydration (Hua et al., 2020). 260 Measurements of orthopyroxene with higher H<sub>2</sub>O concentrations may provide further insight into 261 the hydrogen induced elasticity variations. 262

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Although 842-900 ppm structural H<sub>2</sub>O has limited effect on the single-crystal elasticity of

orthopyroxene, Mierdel et al. (2007) suggested that the incorporated structural H<sub>2</sub>O could reach up 265 to 0.8 wt.% in the Fe-bearing orthopyroxene with high Al<sub>2</sub>O<sub>3</sub> contents. With such a high H<sub>2</sub>O 266 content, the subtle decrease of  $V_P$  and increase of  $D^{V_s}$  and  $A^{V_p}$  can be more significant. In addition, 267 the incorporation of Al and H<sub>2</sub>O in orthopyroxene has an important effect on the development of 268 deformation fabrics, which enhances the Vp anisotropy significantly (Manthilake et al., 2013). 269 Considering the extremely high heterogeneity in the Earth's upper mantle and lower crust, the 270 hydration effect in terms of seismic anisotropy can be important in the lithologies that are enriched 271 in orthopyroxene, e.g. orthopyroxenite and pyroxenite (Arai et al., 2006; Smith et al., 1999), 272 although future measurements at high pressure-temperature conditions on orthopyroxene with 273 higher H<sub>2</sub>O concentrations are needed to better quantify this effect. 274

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Sample orientation measurements: P. K. D. and D. Z.; Resources: J.S.Z; Writing-origin draft
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# 415 **Figure captions**



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Figure 1. Representative Brillouin spectrum of the sample with plane normal (-0.566, 0.675, 0.472) measured at  $\chi = 0^{\circ}$  for 10 minutes.





Figure 2. Acoustic velocities as a function of laboratory angle for the three hydrous Al-bearing orthopyroxene samples. The solid diamond and circle are measured  $v_P$  and  $v_S$ , respectively. Assigning the measured  $v_S$  as either  $v_{SI}$  or  $v_{S2}$  has negligible effect on the calculated  $C_{ij}$  model. The dashed curves are calculated from the best fit single-crystal  $C_{ij}$  model.



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Figure 3. The effect of structural H<sub>2</sub>O on the elasticity of orthopyroxene. The open circle, rectangle, triangle, and diamond symbols represent the elastic properties of anhydrous Al-bearing orthopyroxenes from Jackson et al. (1999), Jackson et al. (2007), Zhang and Bass (2016), and Chai et al. (1997), respectively, after removing the Fe and Ca effects according to Picek (2015) and Perrillat et al. (2007). The shaded areas are bounded by the 95% confidence interval after linear-fitting. The solid star represents the data of hydrous Al-bearing orthopyroxene determined in this study. Most error bars are smaller than the symbols.



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Figure 4. The effect of structural water on the  $A^{U}$ ,  $A^{Vp}$ , and  $D^{Vs}$  of orthopyroxene. The symbols are the same as those in Figure 3.

436 437 Table 1. The effect of chemical impurities on the elasticity of MgSiO<sub>3</sub> orthopyroxene.

	Hydrous Al-bearing Orthopyroxene (this study)	Al,Fe,Ca-bearing Orthopyroxene (Zhang and Bass, 2016)	Al,Fe,Ca-bearing Orthopyroxene (Chai et al., 1997)	Al,Fe-bearing Orthopyroxene (Jackson et al., 2007)	Ca-bearing Orthopyroxene (Perrillat et al., 2007)	End-member Orthopyroxene(Jackson et al., 1999)
H <sub>2</sub> O (ppm)	842-900	-	-	-	0	0
Fe#	0	8.4	9.5	0.2	0	0
Al <sub>2</sub> O <sub>3</sub> (wt. %)	1.64	2.5	5.0	0.4	0	0
CaO (wt. %)	0	1.1	1.1	0	1.9	0
$C_{11}$ (GPa)	235(2)	232.2(5)	236.9(10)	236(1)	224.1(1)	233(1)
$C_{22}$ (GPa)	173(2)	175.7(7)	180.5(8)	173(1)	165.8(2)	171(1)
$C_{33}$ (GPa)	222(2)	222.9(6)	230.4(10)	216(1)	202.9(1)	216(1)
$C_{44}$ (GPa)	86(1)	82.2(4)	84.3(12)	84(1)	82.2(1)	83(1)
$C_{55}$ (GPa)	82(1)	77.3(3)	79.4(8)	79(1)	73.8(1)	79(1)
$C_{66}$ (GPa)	82(1)	78.1(6)	80.1(12)	80(1)	77.1(1)	77(1)
$C_{12}$ (GPa)	75(3)	79.5(9)	79.6(16)	74(1)	71.4(1)	73(2)
$C_{13}$ (GPa)	67(2)	61.2(6)	63.2(18)	57(1)	52.7(1)	56(2)
$C_{23}$ (GPa)	49(2)	54.1(8)	56.8(24)	50(1)	45.2(1)	50(3)
$\rho$ (g/cm <sup>3</sup> )	3.218	3.288(4)	3.304	3.196(4)	3.209	3.194(6)
K <sub>S,Voigt</sub> (GPa)	112(1)	113(1)	116.3(5)	109.5(15)	103.5(15)	108.7(15)
G <sub>S,Voigt</sub> (GPa)	79.1(5)	76.6(7)	78.6(4)	78.6(7)	74.9(11)	77.2(7)
K <sub>S,Reuss</sub> (GPa)	110(1)	112(1)	114.6(5)	107.4(15)	101.5(15)	106.7(15)

G <sub>S,Reuss</sub> (GPa)	77.7(5)	75.2(7)	77.3(4)	77.3(7)	73.5(11)	75.9(7)	
<i>K<sub>s,vRH</sub></i> (GPa)	111(2)	113(1)	115.5(5)	108.5(15)	102.5(15)	107.6(15)	
G <sub>S,VRH</sub> (GPa)	78.4(1)	75.9(7)	78.1(4)	77.9(7)	74.2(11)	76.8(7)	
$V_P$ (km/s)	8.18(3)	8.06(3)	8.15(1)	8.15(8)	7.92	8.11	
$V_{S}$ (km/s)	4.94(2)	4.80(2)	4.86(1)	4.94(5)	4.81	4.90	

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