

1 Revision 1

2 Interfacial structures and acidity constants of  
3 goethite from first principles molecular  
4 dynamics simulations

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## ABSTRACT

15 In this paper, we report a first principles molecular dynamics (FPMD) study of  
16 interfacial structures and acidity constants of goethite. The pK<sub>a</sub>s of the groups on  
17 (010), (110), and (021) surfaces (in *Pbnm*) are derived with the FPMD based vertical  
18 energy gap technique. The results indicate that major reactive groups include  
19  $\equiv\text{Fe}_2\text{OH}_2$  and  $\equiv\text{FeOH}_2$  on (010),  $\equiv\text{FeOH}_2$ ,  $\equiv\text{Fe}_3\text{OLH}$ , and  $\equiv\text{Fe}_3\text{OUH}$  on (110), and  
20  $\equiv\text{FeO}_h\text{H}_2$  and  $\equiv\text{Fe}_2\text{OH}$  on (021). The interfacial structures were characterized in detail  
21 with a focus on the hydrogen bonding environment. With the calculated pK<sub>a</sub> values,  
22 the point of zero charges (PZCs) of the three surfaces are derived and the overall PZC  
23 range of goethite is found to be consistent with the experiment. We further discuss the  
24 potential applications of these results in future studies towards understanding the  
25 environmental processes of goethite.

26 **Keywords:** Goethite, acidity constant, interfacial structure, first principles  
27 molecular dynamics

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## INTRODUCTION

31 Goethite is the most thermodynamically stable iron oxyhydroxides at ambient  
32 temperature (Cornell and Schwertmann, 2003; Majzlan et al., 2003; Gleason et al.,  
33 2008). It is ubiquitous in soils (Sparks, 2003), lakes and marine sediments (van der  
34 Zee et al., 2003), acid mine drainage precipitates (McCarty et al., 1998; Peretyazhko  
35 et al., 2009), and on Mars (Klingelhoefer et al., 2005). Goethite usually expresses  
36 acicular habit and is enclosed by (110), (010), and (021) surfaces (Cornell and  
37 Schwertmann, 2003). Due to its high specific surface area (up to 200 m<sup>2</sup>/g)  
38 (Schwertmann and Taylor, 1989) and reactivity (Schwertmann and Cornell, 2000),  
39 goethite has a profound effect on the retention of heavy metals cations and  
40 negatively-charged moieties (e.g., As/P oxyanions and organic acids) (Fendorf et al.,  
41 1997; Randall et al., 1999; Filius et al., 2000; Ostergren et al., 2000; Kaiser and  
42 Guggenberger, 2007).

43 Due to the presence of amphoteric surface groups (i.e. OH/OH<sub>2</sub> of singly, doubly,  
44 and triply coordinated Fe sites), goethite surfaces can both donate and accept protons,  
45 and the interfacial properties including complexing of cations and anions are  
46 pH-dependent. For example, the adsorption capacities of heavy metal cations and  
47 oxyanions increase and decrease with pH, respectively (Grossl et al., 1997; Kim et al.,  
48 2011; Mamindy-Pajany et al., 2011; Komárek et al., 2018). It was also found that  
49 As/P oxyanions and carboxylate groups can form bidentate complexes at low pH and  
50 monodentate or hydrogen-bonded outer-sphere complexes at high pH (Fendorf et al.,  
51 1997; Manning et al., 1998; Filius et al., 2000; Ona-Nguema et al., 2005; Persson and

52 Axe, 2005; Hanna et al., 2014; Marsac et al., 2016; Yang et al., 2016; Yan and Jing,  
53 2018). As common heavy metal contaminants in water and soils, Pb(II) and Cd(II)  
54 were selected as model cations in many experimental and modeling studies (Spadini  
55 et al., 1994; Venema et al., 1997; Randall et al., 1999; Ostergren et al., 2000; Elzinga  
56 et al., 2001; Boily et al., 2005; Granados-Correa et al., 2011; Leung and Criscenti,  
57 2017; Liu et al., 2018). Using extended x-ray absorption fine structure (EXAFS)  
58 spectroscopy, it was found that Pb(II) and Cd(II) form predominantly edge-sharing  
59 and corner-sharing complexes on goethite, respectively (Randall et al., 1999;  
60 Ostergren et al., 2000). Despite the extensive studies, the microscopic complexation  
61 mechanisms of heavy metal cations, including the complexing sites and structures on  
62 different facets and the corresponding pH-dependence were still poorly understood.

63 The identities and intrinsic acidity constants of surface groups on goethite are  
64 central to the understanding of the pH-dependent interfacial processes. Unfortunately,  
65 current experimental techniques are unable to distinguish the pKas of minerals with so  
66 many facets and surface sites. Several theoretical approaches including MUSIC  
67 method, static density functional theory (DFT) calculations, and first-principles  
68 molecular dynamics (FPMD) simulations have been utilized to calculate the pKas of  
69 goethite. MUSIC method (Hiemstra et al., 1989) correlates the surface pKa with the  
70 undersaturation of surface oxygen based on bond valence and it is able to calculate the  
71 acidities of groups on different surfaces (Hiemstra et al., 1996). With this method, the  
72 pKas of the groups on (110), (021), and (100) surfaces were obtained, and the  
73 corresponding point of zero charge (PZC) matched with the measured values

74 (Venema et al., 1998; Gaboriaud and Ehrhardt, 2003). Despite this agreement, the  
75 pKas cannot be uniquely determined using MUSIC method. For example, essentially  
76 different pKas were obtained for several groups when hydrogen bond contributions  
77 and Fe-O distances derived from classical molecular dynamics simulations were used  
78 as the input of MUSIC (Boily, 2012). According to previous studies, the pKa values  
79 predicted by MUSIC with different proton bond valences and hydrogen bonding  
80 environments can vary up to 5 and 8 pKa units, respectively (Boily et al., 2001;  
81 Gaboriaud and Ehrhardt, 2003). Aquino et al. (2008) derived pKa values based on the  
82 deprotonation free energies from static DFT calculations with cluster surface models  
83 and simplified continuum solvent models. However, the cluster models cannot  
84 distinguish the pKas of different surfaces.

85 In recent years, FPMD method with periodic surface model and explicit solvent  
86 have been applied to calculate the free energies for a variety of chemical processes at  
87 mineral-water interfaces (Boulet et al., 2006; Watts et al., 2014; Churakov, 2015;  
88 Gaigeot and Sulpizi, 2016; Pouvreau et al., 2017; Churakov and Liu, 2018; Gaigeot  
89 and Sulpizi, 2020). For example, by employing FPMD based free energy calculations,  
90 Klyukin et al. (2018) investigated the release of iron from goethite (110) and (021)  
91 facets. Leung and Criscenti (2012) calculated the potential of mean force associated  
92 with the deprotonation of  $\equiv\text{FeOH}_2$  on (110) surface and obtained a pKa of 7.0.  
93 However, to our knowledge, a dataset of pKas at the FPMD level is still lacking for  
94 goethite surfaces.

95 FPMD based vertical energy gap method developed by Sprik group at Cambridge  
96 has proven powerful in pKa prediction (Sulpizi and Sprik, 2008; Costanzo et al.,  
97 2011). This method has been validated on molecular acids spanning over 20 pKa units  
98 with an accuracy of 2 pKa units (Park et al., 2006; Cheng et al., 2009; Sulpizi and  
99 Sprik, 2010; Costanzo et al., 2011; Mangold et al., 2011; Cheng et al., 2014). It has  
100 been successfully applied to derive the pKas of surface groups of oxides (Cheng and  
101 Sprik, 2010; Gaigeot et al., 2012; Sulpizi et al., 2012; Liu et al., 2014a; Gittus et al.,  
102 2018), hydroxides (Liu et al., 2013a) and clay minerals (Liu et al., 2013b; Liu et al.,  
103 2014b). In the present study, this technique was applied to calculate the pKas of major  
104 surfaces of goethite (i.e. (010), (110), and (021)). The interfacial structures are  
105 characterized in detail and the reactive groups have been identified based on the  
106 calculated pKas.

## 107 COMPUTATIONAL METHODS

### 108 **The models**

109 The crystal parameters of goethite used to build surface models are  $a=4.616 \text{ \AA}$ ,  $b=$   
110  $9.956 \text{ \AA}$ ,  $c=3.025 \text{ \AA}$  and  $\alpha=\beta=\gamma=90^\circ$  (in *Pbnm*) (Alvarez et al., 2008). The (010)  
111 surface (Figure 1a) consisted of  $2 \times 1 \times 3$  unit cells and it was cut from the bulk crystal  
112 based on the structure from crystal truncation rod analysis (Ghose et al., 2010). Singly  
113 and doubly coordinated groups exist on this surface (i.e.  $\equiv\text{FeOH}_2$  and  $\equiv\text{Fe}_2\text{OH}$ ). (110)  
114 and (021) surfaces were cleaved from the bulk crystal according to the structures  
115 available in the literature (Aquino et al., 2007; Rustad and Boily, 2010; Boily, 2012;  
116 Kubicki et al., 2012; Leung and Criscenti, 2012; Alexandrov and Rosso, 2015;

117 Kubicki et al., 2017). One singly coordinated group ( $\equiv\text{FeOH}$ ), one doubly coordinated  
118 group ( $\equiv\text{Fe}_2\text{OH}$ ), and three triply coordinated groups (lower site:  $\equiv\text{Fe}_3\text{O}_L\text{H}$ ; upper  
119 site:  $\equiv\text{Fe}_3\text{O}_U\text{H}$ ; site without proton:  $\equiv\text{Fe}_3\text{O}$ ) are present on (110) surface (Figure 1b).  
120 On (021) surface (Figure 1c), there are two kinds of singly coordinated groups  
121 ( $\equiv\text{FeO}_h\text{H}_2$  coordinated with water and  $\equiv\text{FeOH}$  coordinated with OH) and two doubly  
122 coordinated groups ( $\equiv\text{Fe}_2\text{OH}$  at structural O site and  $\equiv\text{Fe}_2\text{O}_h\text{H}$  at structural OH site).  
123 All of the surface models created in the present study bear no net charge.

124 The surface models were placed in 3D periodically repeated orthorhombic cells  
125 with a solution region of 16 Å. The dimensions of the simulation cells are  
126  $9.074 \times 9.233 \times 28.000 \text{ \AA}^3$  for (010) system,  $9.074 \times 10.975 \times 26.000 \text{ \AA}^3$  for (110) system,  
127 and  $9.233 \times 11.650 \times 26.000 \text{ \AA}^3$  for (021) system. 45, 53, and 58 water molecules were  
128 randomly placed in the solution regions of (010), (110), and (021) systems  
129 respectively. These numbers were determined from the density of bulk water. The  
130 water density profiles derived from the trajectories (Figure S1 in the Supplemental<sup>1</sup>  
131 material) suggested that the ambient water density was reached in the bulk regions.

### 132 **FPMD Details**

133 The CP2K/QUICKSTEP package (VandeVondele et al., 2005; Hutter et al., 2014)  
134 was used to conduct all FPMD simulations. In this package, the electronic structures  
135 were calculated with the hybrid Gaussian and Plane Wave (GPW) approach (Lippert  
136 et al., 1997). A double- $\zeta$  Gaussian-type orbital basis (VandeVondele and Hutter, 2007)  
137 with polarization functions (DZVP) was employed to construct the electronic  
138 wavefunctions. The plane wave basis was expanded to 360 Ry to represent the

139 electron density. The Goedecker-Teter-Hutter (GTH) pseudopotentials (Goedecker et  
140 al., 1995) were used to represent the core electrons states. The  
141 Perdew–Burke–Ernzerhof (PBE) functional (Perdew et al., 1997) was used to describe  
142 the exchange-correlation interaction. Van der Waals interactions were taken into  
143 account by using the DFT-D3 dispersion corrections (Grimme et al., 2010). Wave  
144 functions were optimized to a tolerance of 1.0E-6.

145 All calculations were spin-polarized with the spin multiplicity set to unity.  
146 Antiferromagnetic ordering was adopted as the initial spin configurations for all the  
147 systems with up/down spin Fe atoms locating at alternating layers along [010]  
148 direction (Kubicki et al., 2008; Martin et al., 2009; Kerisit et al., 2016; Bylaska et al.,  
149 2020) (Figure 1). The antiferromagnetic configuration was maintained during the  
150 simulations. Our calculations predicted a pKa of 7.3 for  $\equiv\text{FeOH}_2$  on (110) surface,  
151 which is consistent with 7.0 obtained by Leung and Criscenti (2012) using DFT+U  
152 based FPMD simulation. This agreement indicates that the Hubbard U correction does  
153 not have obvious influence on the pKa estimate for the current systems.

154 Born-Oppenheimer type molecular dynamics (BOMD) simulations were carried  
155 out with a time step of 0.5 fs. NVT ensemble with the Nosé-Hoover chain thermostat  
156 was adopted to propagate the simulations. The temperature was controlled at 330 K.  
157 This temperature was intended to avoid the glassy behavior of liquid water at a lower  
158 temperature (VandeVondele et al., 2004). For each FPMD simulation, an equilibration  
159 runs for at least 2.0 ps was conducted, followed by a production run for over 10.0 ps.



160 The pKa values of goethite surface groups were evaluated with the half-reaction  
161 scheme of the vertical energy gap method (Sulpizi and Sprik, 2008; Cheng et al.,  
162 2009; Costanzo et al., 2011; Cheng and Sprik, 2012). With this method, the free  
163 energy change of the deprotonation reaction is calculated as the integral of the  
164 ensemble averages of the vertical energy gaps obtained from a series of FPMD  
165 trajectories along the alchemical path from reactant state to product state. The details  
166 are given in section S2 in the Supplemental<sup>1</sup> material.

## 167 **RESULTS AND DISCUSSION**

### 168 **Interfacial structures and pKas**

169 **(010) surface.** During the free MD simulation, two H<sub>2</sub>O ligands out of 12 ≡FeOH<sub>2</sub>  
170 groups left from the Fe atoms, indicating a weak interaction between Fe and the  
171 coordinated water. Similar detachment was also observed in the FPMD study of Chen  
172 et al. (2017). ≡FeOH<sub>2</sub> can donate hydrogen bonds to solvent water and the average  
173 coordination number (CN) of water O around the H of ≡FeOH<sub>2</sub> is 0.5 (Figure 3a).  
174 ≡Fe<sub>2</sub>OH donates a hydrogen bond to ≡Fe<sub>3</sub>O in the bulk and at the same time it accepts  
175 on average 0.7 hydrogen bonds from the solvent water (Figure 3b).

176 The calculated energy gaps and deprotonation free energies of (010) surface  
177 groups are listed in Supplemental<sup>1</sup> Table S2, and the obtained pKas are summarized in  
178 Table 1. It can be seen that the vertical energy gaps converge within 0.26 eV  
179 (Supplemental<sup>1</sup> Table S2) and the calculated pKas have statistical errors within 2.0  
180 pKa units (Tables 1-3). The calculated pKa of ≡FeOH<sub>2</sub> is 10.9, indicating that this  
181 group remains protonated in the near neutral pH range and the deprotonated form can

182 occur under basic conditions. The pKas of  $\equiv\text{Fe}_2\text{OH}$  and  $\equiv\text{Fe}_2\text{OH}_2$  are 15.4 and 4.7,  
183 respectively, implying that  $\equiv\text{Fe}_2\text{OH}$  is the most possible form, whereas  $\equiv\text{Fe}_2\text{OH}_2$   
184 mainly occurs in acidic pH range. Using hydrogen bond valence derived from  
185 classical molecular dynamics simulations, MUSIC method predicted a pKa of 4.3 for  
186  $\equiv\text{Fe}_2\text{OH}_2$ , which is consistent with our prediction (Boily, 2012). No MUSIC result  
187 was reported for  $\equiv\text{Fe}_2\text{OH}$  to the best of our knowledge.

188 **(110) surface.** Most of the OHs of  $\equiv\text{FeOH}$  sites show orientations parallel to the  
189 surface and the rest pointed towards the solution region (Figure 4). Therefore, the  
190 parallelly orientated  $\equiv\text{FeOH}$  can accept hydrogen bonds from both  $\equiv\text{Fe}_3\text{O}_L\text{H}$  groups  
191 and solvent water while the others donate hydrogen bonds to solvent water (Figure 4).  
192 The different orientations of OHs were also observed on other (hydr)oxides surfaces,  
193 e.g., gibbsite (Liu et al., 2013a), corundum (Gaigeot et al., 2012), and hematite (von  
194 Rudorff et al., 2016). The OHs of  $\equiv\text{FeOH}$  can switch between the two orientations  
195 and the overall CN between water H and the O of  $\equiv\text{FeOH}$  is 0.97 (Figure 5a). The  
196 OHs of  $\equiv\text{Fe}_2\text{OH}$  and  $\equiv\text{Fe}_3\text{O}_U\text{H}$  point towards the solution region, and both donate  
197 hydrogen bonds to solvent water, with an average CN of 0.97 (Figure 6b) and 0.85  
198 (Figure 5b) respectively.  $\equiv\text{Fe}_2\text{OH}$  also accepts one hydrogen bond from solvent water  
199 (Figure 6a).  $\equiv\text{Fe}_3\text{O}$  has no contact with water because of the steric hindrance (Figure  
200 5c).

201 The pKas of  $\equiv\text{FeOH}$  and  $\equiv\text{FeOH}_2$  are 15.0 and 7.3 respectively (Table 2).  
202 Although the computed pKa of  $\equiv\text{FeOH}$  is smaller than the MUSIC prediction 19.6  
203 (Venema et al., 1998), they both indicate that  $\equiv\text{FeOH}$  is inert. The pKa of  $\equiv\text{FeOH}_2$  is

204 similar to the previous FPMD result 7.0 (Leung and Criscenti, 2012) and the MUSIC  
205 result 7.7 (Venema et al., 1998). However, the MUSIC prediction for these groups  
206 will be significantly different if a different hydrogen bonding environment was used  
207 (11.7 or 3.7 and 23.6 or 15.6 would be obtained for  $\equiv\text{FeOH}_2$  and  $\equiv\text{FeOH}$  when it was  
208 assumed that 1 or 3 hydrogen bonds were formed with water) (Gaboriaud and  
209 Ehrhardt, 2003). Nevertheless, the calculated pKas suggest that  $\equiv\text{FeOH}$  can get  
210 protonated and therefore both  $\equiv\text{FeOH}$  and  $\equiv\text{FeOH}_2$  can exist in normal pH range.

211  $\equiv\text{Fe}_2\text{OH}$  and  $\equiv\text{Fe}_2\text{OH}_2$  have pKas of 13.9 and -0.5, respectively, which are close to  
212 the MUSIC predictions 12.3 and 0.4 (Venema et al., 1998). Such a low acidity  
213 constant for  $\equiv\text{Fe}_2\text{OH}_2$  indicates that  $\equiv\text{Fe}_2\text{OH}$  hardly accepts a second proton at  
214 common pH.

215 The pKa values of  $\equiv\text{Fe}_3\text{OLH}$ ,  $\equiv\text{Fe}_3\text{OUH}$ , and  $\equiv\text{Fe}_3\text{OH}$  are calculated to be 10.7, 9.7,  
216 and 0.3, respectively. MUSIC method cannot discriminate  $\equiv\text{Fe}_3\text{OLH}$  and  $\equiv\text{Fe}_3\text{OUH}$   
217 and gave a pKa of 11.7 (Venema et al., 1998). This value agrees with the pKas  
218 obtained for  $\equiv\text{Fe}_3\text{OLH}$  and  $\equiv\text{Fe}_3\text{OUH}$ . However, this should be considered fortuitous  
219 as the hydrogen bonding environments are different for these two groups:  $\equiv\text{Fe}_3\text{OLH}$   
220 forms a hydrogen bond with  $\equiv\text{FeOH}$  while  $\equiv\text{Fe}_3\text{OUH}$  donates a hydrogen bond to  
221 water. For  $\equiv\text{Fe}_3\text{OH}$ , the MUSIC result was -0.2 (Venema et al., 1998), close to our  
222 prediction. Overall, the calculated pKas indicate that  $\equiv\text{Fe}_3\text{OLH}$  and  $\equiv\text{Fe}_3\text{OUH}$  are  
223 stable in common pH.

224 **(021) surface.** On (021) surface, the coordinated  $\text{H}_2\text{O}$  of  $\equiv\text{FeO}_h\text{H}_2$  sites are loosely  
225 bound and can leave the surface spontaneously during the free MD simulation. This

226 observation is consistent with the low desorption energy of  $\sim 0.5$  kcal/mol for  $\text{H}_2\text{O}$  on  
227 this site (Alexandrov and Rosso, 2015).  $\equiv\text{FeO}_h\text{H}_2$  accepts hydrogen bonds from  
228 solvent water with a CN of 0.3 (Figures 7a and 8a). The two OHs of  $\equiv\text{FeO}_h\text{H}_2$  also  
229 donate hydrogen bonds to the nearby  $\equiv\text{FeOH}$  and  $\equiv\text{Fe}_2\text{OH}$  groups (Figure 7b).  $\equiv\text{FeOH}$   
230 can donate and accept hydrogen bonds to/from solvent water, with a CN of 0.7 and  
231 0.3, respectively (Figures 7a and 9).  $\equiv\text{Fe}_2\text{OH}$  and  $\equiv\text{Fe}_2\text{O}_h\text{H}$  donate hydrogen bonds to  
232  $\equiv\text{FeOH}$  (Figure 7b).  $\equiv\text{Fe}_2\text{OH}$  also donates hydrogen bonds to solvent water with a CN  
233 of 0.3 (Figure 8b), while  $\equiv\text{Fe}_2\text{O}_h\text{H}$  accepts hydrogen bonds from solvent water with a  
234 CN of 0.4 (Figure 8c). Overall, the interaction between the first layer water and  
235 surface groups on (021) surface is weaker compared to those on (010) and (110)  
236 surfaces, as revealed by the smaller CNs between surface groups and water.

237 The calculated  $\text{pK}_a$  of  $\equiv\text{FeO}_h\text{H}_2$  is 10.0 (Table 3), close to the MUSIC result 11.9  
238 (Venema et al., 1998).  $\equiv\text{FeOH}$  and  $\equiv\text{FeOH}_2$  have  $\text{pK}_a$ s of 12.2 and 2.3, respectively,  
239 indicating that  $\equiv\text{FeOH}_2$  rarely happens and  $\equiv\text{FeOH}$  is the most possible form in  
240 common pH range. MUSIC results were 20.0 and 8.1 for  $\equiv\text{FeOH}$  and  $\equiv\text{FeOH}_2$ ,  
241 respectively (Venema et al., 1998), which are substantially higher than our results.

242 The calculated  $\text{pK}_a$ s for  $\equiv\text{Fe}_2\text{O}_h\text{H}/\equiv\text{Fe}_2\text{O}_h\text{H}_2$  and  $\equiv\text{Fe}_2\text{OH}/\equiv\text{Fe}_2\text{OH}_2$  are 13.2/0.8  
243 and 5.2/-1.3, respectively. The higher  $\text{pK}_a$  value of  $\equiv\text{Fe}_2\text{O}_h\text{H}$  compared to  $\equiv\text{Fe}_2\text{OH}$  is  
244 consistent with the different roles they played in hydrogen bonding, that is,  $\equiv\text{Fe}_2\text{O}_h\text{H}$   
245 was proton acceptor while  $\equiv\text{Fe}_2\text{OH}$  was proton donor. MUSIC predictions were  
246 19.6/7.7 for  $\equiv\text{Fe}_2\text{O}_h\text{H}/\equiv\text{Fe}_2\text{O}_h\text{H}_2$  and 11.9/0.0 for  $\equiv\text{Fe}_2\text{OH}/\equiv\text{Fe}_2\text{OH}_2$  (Venema et al.,  
247 1998). Although these values were different from our results, the MUSIC predictions

248 also demonstrated a decreasing trend from  $\equiv\text{Fe}_2\text{O}_h\text{H}$  to  $\equiv\text{Fe}_2\text{OH}$ . Overall, our  
249 calculated pKas suggest that the protonated  $\equiv\text{Fe}_2\text{O}_h\text{H}_2$  and  $\equiv\text{Fe}_2\text{OH}_2$  rarely occur;  
250  $\equiv\text{Fe}_2\text{O}_h\text{H}$  is inactive in normal pH range and  $\equiv\text{Fe}_2\text{OH}$  can get deprotonated in slightly  
251 acidic conditions.

## 252 **Surface charging**

253 PZC is an important parameter in surface complexation reactions because it  
254 determines the sign of surface charges at a certain pH. PZC of a certain surface can be  
255 estimated based on the surface pKas (Table 4). For the (010) surface, the PZC is  
256 estimated to be 7.8, which is determined by the pKas of  $\equiv\text{FeOH}_2$  and  $\equiv\text{Fe}_2\text{OH}_2$ .  
257 Similarly, the PZCs of (110) and (021) are 8.5 and 3.8, respectively. Therefore, the  
258 PZC of a whole goethite should be in the range of 3.8~8.5, which is consistent with  
259 the experimental range of 5.6~9.5 (Lutzenkirchen, 2002; Lützenkirchen et al., 2008;  
260 Kosmulski, 2009). The PZC values of (010) and (110) surfaces are very close, and  
261 they are significantly higher than the PZC of (021) surface.

262 At pH below 3.8 (i.e. PZC of (021) surface), all three surfaces are positively  
263 charged and therefore adsorption of heavy metal cations is inhibited. This is  
264 consistent with the fact that heavy metals do not show adsorption (e.g. Cd, Zn) or only  
265 marginal adsorption (e.g. Pb, Cu) on goethite at pH below 3.8 (Komárek et al., 2018).  
266 As pH increases, the net charges on (010) and (110) surfaces decrease and they bear  
267 net negative charges at pH above 7.8 and 8.5, respectively. These values are in  
268 general coincidence with the pH range where the adsorption capacity reached the  
269 maximum (Komárek et al., 2018).

270

## IMPLICATIONS

271 Based on the computed pK<sub>a</sub>s, the surface sites available for complexing metal  
272 cations can be derived and they include ≡FeOH on (010) surface, ≡FeOH, ≡Fe<sub>3</sub>O<sub>L</sub>,  
273 and ≡Fe<sub>3</sub>O<sub>U</sub> on (110) surface, and ≡Fe<sub>2</sub>O, ≡FeOH, and ≡FeO<sub>h</sub>H on (021) surface. The  
274 complexation mechanisms of heavy metals at a certain pH can be deduced based on  
275 the distributions of available complexing sites. As an example, the distance between  
276 two neighboring ≡FeOH groups on (110) surface is ~3.0 Å, and therefore a bidentate  
277 corner-sharing complex can form on these sites in near-neutral conditions (Randall et  
278 al., 1999). The relative stabilities of the complexes on different sites can be obtained  
279 by comparing FPMD calculated free energies. For example, with such an approach we  
280 investigated the thermodynamics of Cd(II) and Ni(II) complexes formed on clay edge  
281 sites (Zhang et al., 2016; Zhang et al., 2017).

282 There is a consensus that anionic groups (e.g. soil organic matters (SOMs), As/P  
283 oxyanions) can form inner-sphere complexes on goethite via ligand exchange  
284 reactions (Gu et al., 1994; Grossl et al., 1997; Kaiser et al., 1997; Kaiser et al., 2007;  
285 Kim et al., 2011). pH dependence of complexation of anionic groups can be derived  
286 by integrating surface pK<sub>a</sub>s and FPMD computed adsorption free energies, e.g. with  
287 this approach we investigated the complexation mechanisms of acetate, quinone, and  
288 phosphate on clay edges as a function of pH (Liu et al., 2017; Lützenkirchen et al.,  
289 2018; Zhang et al., 2020).

290 The pK<sub>a</sub>s calculated in the present study are of high accuracy and can be directly  
291 applied with SCMs (Nie et al., 2017; Han and Katz, 2019) to investigate the

292 adsorption behaviors. For example, based on the surface sites and pKas derived in our  
293 prior studies (Liu et al., 2012a; Liu et al., 2012b; Liu et al., 2013b; Liu et al., 2014b).  
294 Tournassat et al. developed a SCM for clay edges, that successfully reproduced the  
295 experimental acid-base titration data of montmorillonite (Tournassat et al., 2016) and  
296 the adsorption of uranyl over a wide range of pH and concentration conditions  
297 (Tournassat et al., 2018; Zhang et al., 2018). The integration of the computed intrinsic  
298 pKas into the SCM modeling can establish direct links between macroscopic  
299 experiments and microscopic properties, that can thus help uncover the adsorption  
300 mechanisms. Overall, the structures and pKas obtained in the present study form a  
301 microscopic basis for understanding the environmental and geochemical processes at  
302 goethite interfaces.

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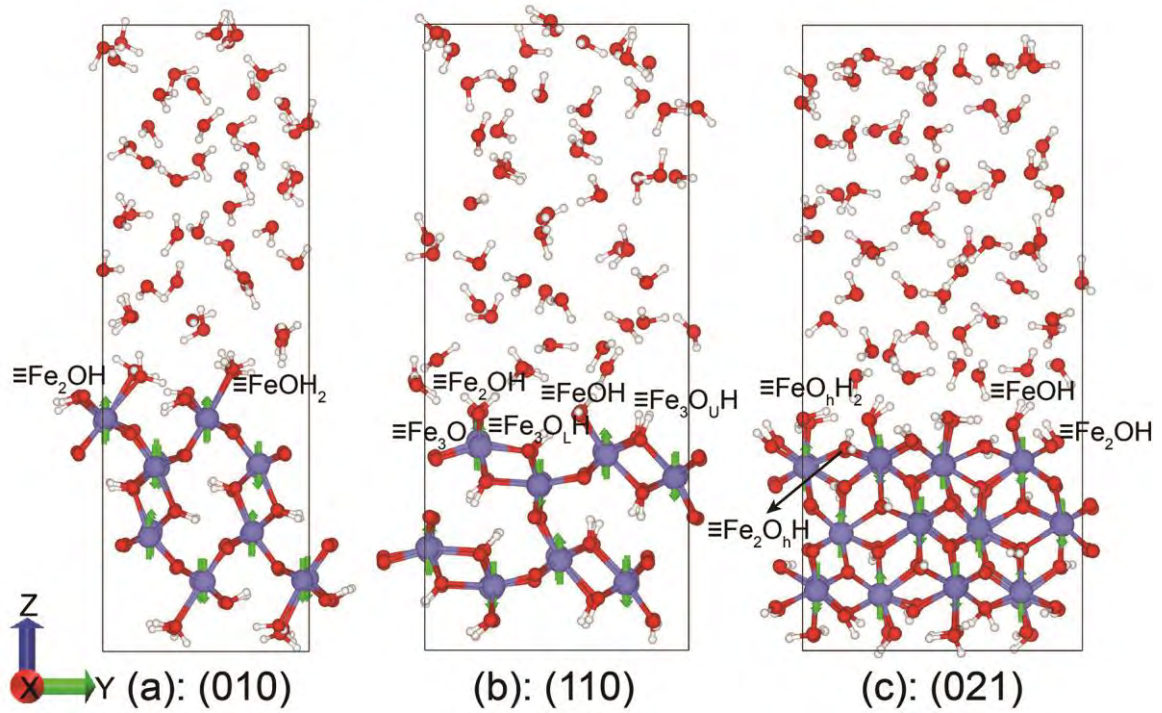
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635 **Endnote:**

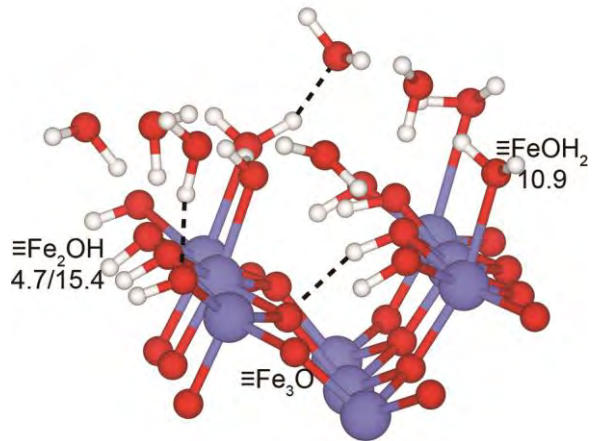
636 <sup>1</sup>Supplemental Material.

637





**FIGURE 1.** The surface models used in the study. O = red, H = white, Fe = blue-violet. Green arrows indicate the electron spin orientations.



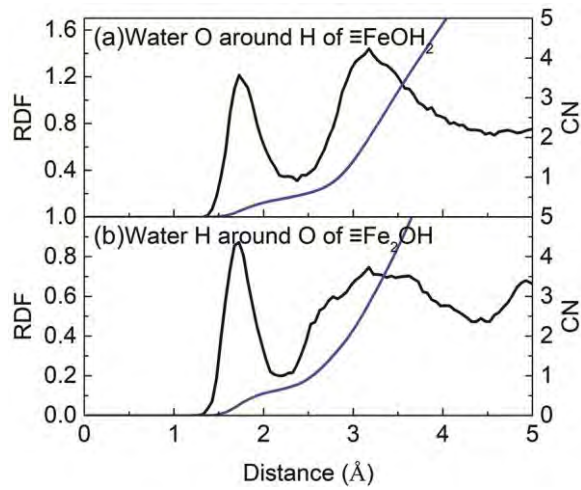
643

644 **FIGURE 2.** Snapshot of the (010) surface. Atoms are color-coded by element as

645 described in Figure 1. Only the water molecules that hydrogen-bonded with surface

646 groups are depicted and the others are removed for clarity.

647



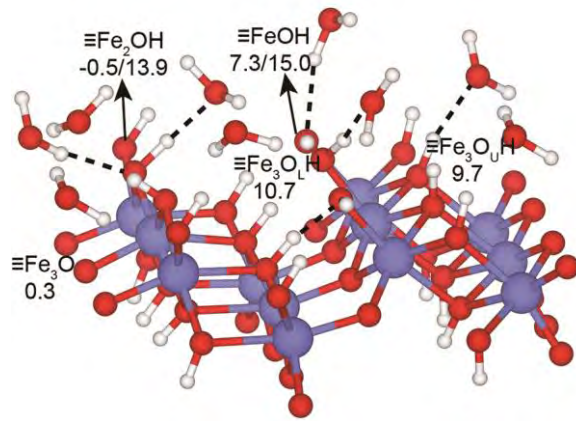
648

649 **FIGURE 3.** Radial distribution function (RDF) and coordination number (CN) for

650 **(a)** water O around H of  $\equiv\text{FeOH}_2$  and **(b)** water H around O of  $\equiv\text{Fe}_2\text{OH}$  on (010)

651 surface.

652



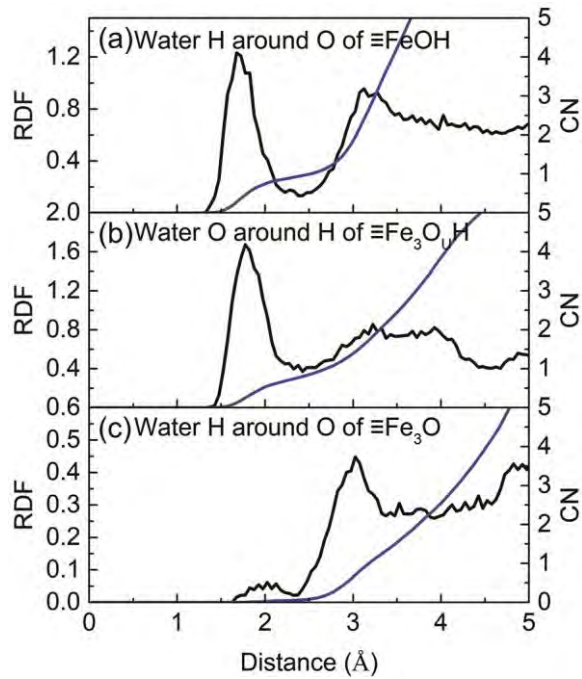
653

654 **FIGURE 4.** Snapshot of the (110) surface. Atoms are color-coded by element as

655 described in Figure 1. Only the water molecules that hydrogen-bonded with surface

656 groups are depicted and the others are removed for clarity.

657

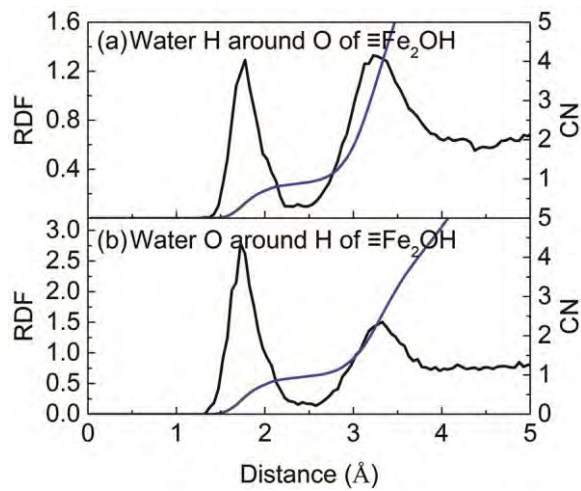


658

659 **FIGURE 5.** RDF and CN for (a) water H around O of  $\equiv\text{FeOH}$ , (b) water O

660 around H of  $\equiv\text{Fe}_3\text{O}_4\text{H}$ , and (c) water H around O of  $\equiv\text{Fe}_3\text{O}$  on (110) surface.

661

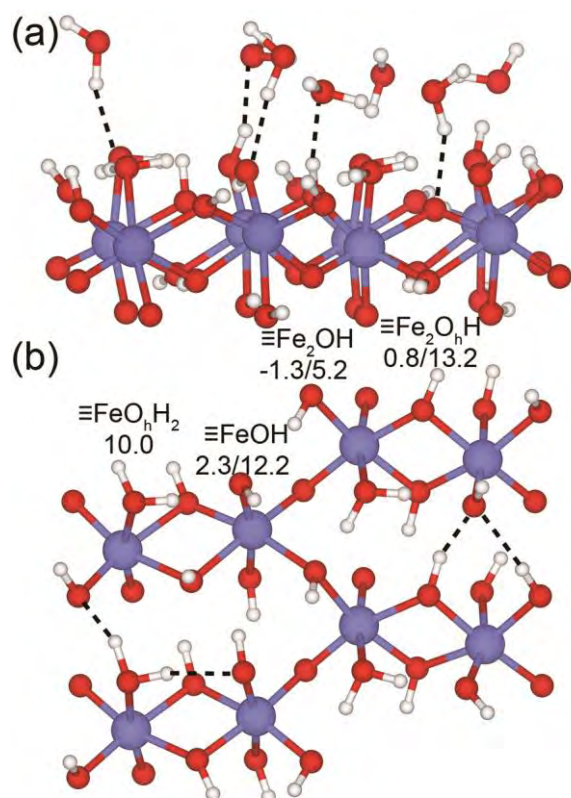


662

663 **FIGURE 6.** RDF and CN for (a) water H around O of  $\equiv\text{Fe}_2\text{OH}$  and (b) water O

664 around H of  $\equiv\text{Fe}_2\text{OH}$  on (110) surface.

665



666

667 **FIGURE 7.** Snapshot of the (021) surface. **(a)** side view showing the hydrogen

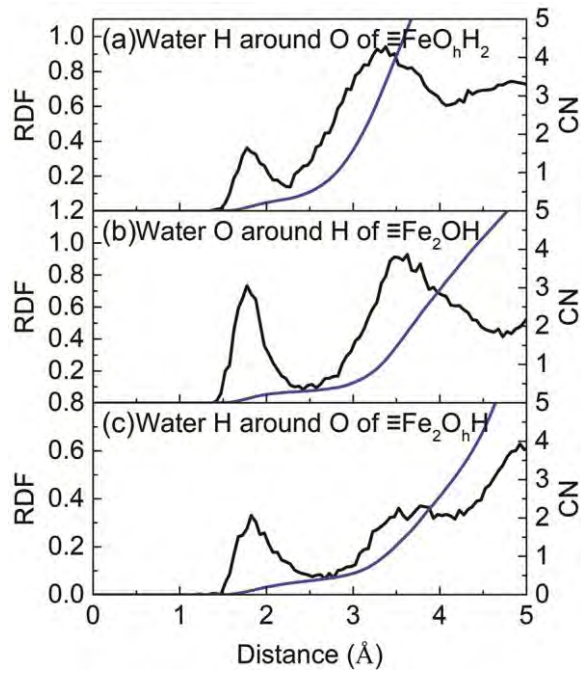
668 bonds between surface groups and water molecules; **(b)** top view showing the

669 hydrogen bonds between surface groups. Atoms are color-coded by element as

670 described in Figure 1. Only the water molecules that hydrogen-bonded with surface

671 groups are depicted and the others are removed for clarity.

672



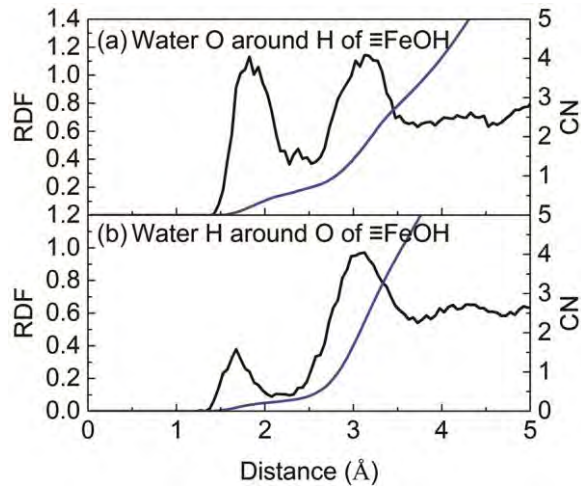
673

674 **FIGURE 8.** RDF and CN for (a) water H around O of  $\equiv\text{FeO}_h\text{H}_2$ , (b) water O

675 around H of  $\equiv\text{Fe}_2\text{OH}$ , and (c) water H around O of  $\equiv\text{Fe}_2\text{O}_h\text{H}$  on (021) surface.

676





677

678 **FIGURE 9.** RDF and CN for (a) water O around H of  $\equiv\text{FeOH}$  and (b) water H

679 around O of  $\equiv\text{FeOH}$  on (021) surface.

680

681 **TABLE 1.** Calculated pKa values of groups on (010) surface in comparison with

682 MUSIC results

Groups	This study	MUSIC <sup>a</sup>
$\equiv\text{FeOH}_2$	10.9±1.8	
$\equiv\text{Fe}_2\text{OH}_2/\equiv\text{Fe}_2\text{OH}$	4.7±0.8/15.4±0.7	4.3/-

<sup>a</sup>(Boily, 2012).

683

684

685 **TABLE 2.** Calculated pKa values of surface groups on (110) surface in comparison  
 686 with literature results

Groups	This study	MUSIC <sup>a</sup>			FPMD <sup>b</sup>
		I	II	III	
$\equiv\text{FeOH}_2/\equiv\text{FeOH}$	7.3±0.5/15.0±0.7	11.7/23.6	7.7/19.6	3.7/15.6	7.0/-
$\equiv\text{Fe}_2\text{OH}_2/\equiv\text{Fe}_2\text{OH}$	-0.5±1.3/13.9±0.7	0.4/12.3			
$\equiv\text{Fe}_3\text{O}_L\text{H}$	10.7±0.5	11.7			
$\equiv\text{Fe}_3\text{O}_U\text{H}$	9.7±0.7	11.7			
$\equiv\text{Fe}_3\text{OH}$	0.3±0.8	-0.2			

<sup>a</sup>(Venema et al., 1998; Gaboriaud and Ehrhardt, 2003): I, II, and III mean that 1, 2, and 3 hydrogen bonds are presumed between surface groups and water, respectively. <sup>b</sup>(Leung and Criscenti, 2012).

687

688

689 **TABLE 3.** Calculated pKa values of surface groups on (021) surface in comparison  
690 with MUSIC results

Groups	This study	MUSIC <sup>a</sup>
$\equiv\text{FeO}_h\text{H}_2$	10.0±1.5	11.9
$\equiv\text{FeOH}_2/\equiv\text{FeOH}$	2.3±1.2/12.2±1.7	8.1/20.0
$\equiv\text{Fe}_2\text{OH}_2/\equiv\text{Fe}_2\text{OH}$	-1.3±2.0/5.2±1.3	0.0/11.9
$\equiv\text{Fe}_2\text{O}_h\text{H}_2/\equiv\text{Fe}_2\text{O}_h\text{H}$	0.8±1.7/13.2±1.0	7.7/19.6

<sup>a</sup>(Venema et al., 1998).

691

692

693 **TABLE 4.** Calculated pKa values of surface groups and PZC of individual surfaces

Surface	Groups	pKa	PZC
(010)	$\equiv\text{FeOH}_2$	10.9	7.8
	$\equiv\text{Fe}_2\text{OH}_2/\equiv\text{Fe}_2\text{OH}$	4.7/15.4	
(110)	$\equiv\text{FeOH}_2/\equiv\text{FeOH}$	7.3/15.0	8.5
	$\equiv\text{Fe}_2\text{OH}_2/\equiv\text{Fe}_2\text{OH}$	-0.5/13.9	
	$\equiv\text{Fe}_3\text{O}_L\text{H}$	10.7	
	$\equiv\text{Fe}_3\text{O}_U\text{H}$	9.7	
	$\equiv\text{Fe}_3\text{O}$	0.3	
(021)	$\equiv\text{FeO}_h\text{H}_2$	10.0	3.8
	$\equiv\text{FeOH}_2/\equiv\text{FeOH}$	2.3/12.2	
	$\equiv\text{Fe}_2\text{OH}_2/\equiv\text{Fe}_2\text{OH}$	-1.3/5.2	
	$\equiv\text{Fe}_2\text{O}_h\text{H}_2/\equiv\text{Fe}_2\text{O}_h\text{H}$	0.8/13.2	

694

695

696