1   **REVISION 2**

2   **Titanium diffusion profiles and melt inclusion chemistry and morphology in quartz from**

3   **the Tshirege Member of the Bandelier Tuff**

4   **JOSEPH R. BORO[1], JOHN A. WOLFF[1], OWEN K. NEILL[2], ARRON R. STEINER[1],**

5   **AND FRANK C. RAMOS[3]**

6   [1]School of the Environment, Washington State University, Pullman, WA 99163, USA

7   [2]School of Earth and Environmental Sciences, University of Michigan, Ann Arbor, MI 48109, USA

8   [3]Department of Geological Sciences, New Mexico State University, Las Cruces, NM 88003, USA

9

11

12   **ABSTRACT**

13   Many rhyolites contain quartz crystals with relatively Ti-rich rims and Ti-poor cores,

14   with a sharp interface between zones, attributed to partial dissolution followed by overgrowth

15   following a heating event due to mafic recharge of the system. Quartz crystals in the

16   compositionally zoned, high-silica rhyolite Tshirege Member of the Bandelier Tuff, erupted at

17   1.26 Ma from the Valles caldera, New Mexico, show a range in zoning styles with Ti-rich rims

18   becoming more abundant upwards in the ignimbrite sheet among progressively less evolved

19   magma compositions. Here we compare times between quartz overgrowth and eruption obtained

20   by applying Ti diffusion coefficients to Ti concentration profiles in Tshirege Member quartz

21   crystals with those from cathodoluminescence (CL) brightness profiles, and show that

22   panchromatic CL provides only a crude proxy for Ti in quartz in this unit. Titanium

23   concentrations are measured to detection limits of ~1.2 ppm with small analytical errors (<5%)

24   using MAN backgrounds, blank corrections, and oblique corrected transects to resolve diffusion-

25   relaxed zone boundaries as thin as ~10 μm. Timescales derived from Ti profiles using the widely

26   applied Ti-in-quartz diffusion coefficients of Cherniak et al. (2007) range from 60 to 10,000

27   years, suggesting heating and mobilization events at different times prior to the eruption.

28   However, use of the newer Ti diffusivities reported by Jollands et al. (2020) yields timescales up

29   to three orders of magnitude longer, including results that are geologically unreasonable for the

30   Bandelier system. We suggest that assumptions commonly made in diffusion modeling,

31   specifically about the form of the Ti zoning profile prior to diffusive relaxation, may be invalid.

32   Melt inclusions in the Ti-poor cores of late-erupted quartz are chemically akin to early

33   erupted melt compositions, while adhering and groundmass glasses more closely reflect the

34   composition of the host pumice. Heating and mobilization events identified from quartz Ti

35   zoning are thus linked to overall compositional zoning of the tuff, which may have been

36   produced by repeated episodes of melting of a crystal cumulate cognate to the early-erupted,

37   evolved rhyolite. Quartz-hosted melt inclusion faceting suggests the development of a crystal

38   mush over a minimum time frame of 1,000 – 10,000 years prior to recharge events that produced

39   the eruptible Tshirege magma.

40

41   **INTRODUCTION**

42   Diffusion modeling of element concentration profiles in crystals is a fruitful way of

43   extracting timescales of processes occurring at elevated temperatures in geologic systems. The

44   approach relies on some assumptions, such as starting conditions for the diffusion episode and

45   that the concentration profiles being modeled are indeed the result of ionic diffusion. In studies

46   of volcanic systems, diffusion profiles can help determine residence times of crystals in magma

47   based on compositional zoning of the minerals of interest. Diffusion modeling can also be used

48   to determine the time elapsed between an identifiable event in the history of a crystal (e.g.,

49   overgrowth on a resorption surface) and eruption (Costa and Dungan, 2005; Morgan and Blake,

50   2006; Wark et al., 2007; Costa et al., 2008; Till et al., 2015). Timescales deduced from the

51   diffusive blurring of an overgrowth boundary can provide insights on how magma systems

52   respond to disturbance, such as rejuvenation and heating by magmatic recharge, shortly before

53   an eruption. This approach has yielded estimates of short activation timescales (<1 year – 1000

54   years) preceding past catastrophic silicic caldera-forming 'super-eruptions' (Wark et al., 2007;

55   Matthews et al., 2012; Till et al., 2015; Gualda and Sutton, 2016; Cooper et al., 2017). Smaller,

56   much more frequent eruptions may also have activation timescales of < 1 year, for example

57   Calbuco volcano, 2015 (Arzilli et al., 2019).

58   In rhyolitic volcanic systems, quartz is an attractive and widely-used target for diffusion

59   modeling because quartz crystals are usually large and of effectively constant major element

60   composition. Trace element substitutions, particularly that of Ti^{4+} for tetrahedral Si^{4+} in the

61   quartz structure (Götze, 2012; Leeman et al., 2012), result in enhanced cathodoluminescence

62   (CL) brightness that in principle allows easy identification of trace cation concentration zoning,

63   and because the behavior of Ti in quartz is well-studied. Peppard et al. (2001) provided the first

64   detailed description of CL zoning in quartz from a high-silica rhyolite (the Bishop Tuff). Wark

65   and Watson (2006) calibrated Ti-in-quartz as a geothermometer, while Cherniak et al. (2007)

66   reported results for the diffusion coefficient of Ti (D_{Ti}) in quartz. These studies spawned a

67   significant literature linking Ti-in-quartz variations, CL zoning, and magmatic temperature to

68   estimates of crystal residence timescales and the rejuvenation of large stagnant silicic magma

69   bodies to an eruptible state, as well as new calibrations of the Ti-in-quartz (TitaniQ) thermometer

70   (Hayden and Watson, 2007; Wark et al., 2007; Shane et al., 2008; Campbell et al., 2009; Thomas

71   et al., 2010; Gualda et al., 2012; Huang and Audétat, 2012; Matthews et al., 2012; Thomas and

72   Watson, 2012; Wilson et al., 2012; Wilcock et al., 2013; Gualda and Sutton, 2016; Pamukcu et

73   al., 2015; Seitz et al., 2016; Cooper et al., 2017). The temperature sensitivity of D_{Ti} requires

74   accurate knowledge of temperature during the diffusion episode in order to extract timescales

75   from modeled diffusion profiles, placing demands on geothermometry. Also, the application of

76   the Ti-in-quartz geothermometer requires precise knowledge of the activity of Ti in the melt in

77   equilibrium with the quartz, a parameter which is not always well constrained (Huang and

78   Audétat, 2012; Matthews et al., 2012; Thomas and Watson, 2012; Wilson et al., 2012).

79   Much of the interest in using Ti-in-quartz diffusion to estimate silicic magma

80   rejuvenation timescales stems from the geologically short durations that result from applying the

81   diffusivities of Cherniak et al. (2007) to observed Ti zoning profiles, with implications for

82   eruption prediction in regions of silicic volcanism. The estimated durations rely on the

83   assumption of an initial step-function zone boundary separating quartz interiors from rims grown

84   following a heating and resorption event (Wark et al., 2007), and range from hundreds of years

85   down to less than a year (Wark et al., 2007; Gualda et al., 2012; Wilcock et al., 2013; Seitz et al.,

86   2016; Gualda and Sutton, 2016). The shorter durations are supported by cation diffusion

87   estimates from other minerals in some cases, for example feldspar (Till et al., 2015) and

88   pyroxene Chamberlain et al., 2014a). However, U-Th-Pb geochronology of zircon grains from

89   silicic systems typically yields times of $10^4 - 10^5$ years, thought to record a long history of

90   magma body growth and evolution prior to destabilizing events leading to eruption (e.g. Reid

91   and Vasquez, 2017). Now, recent experiments on Ti-in-quartz diffusivity by Jollands et al.

92   (2020) yield much slower diffusion rates than proposed by Cherniak et al. (2007), and lead to

93   timescales for the preservation of Ti zoning profiles in quartz that are more consistent with those

94   derived from geochronology. Thus, the status of Ti zoning in quartz as a recorder of events

95   immediately preceding eruption is thrown into question.

96   In addition to zoning recorded in quartz during crystal growth, melt may become trapped

97   as melt inclusions (MI; Fig. 1); MI are generally thought to record the liquid composition at the

98   time of crystal growth (Lowenstern and Mahood 1991; Dunbar and Hervig 1992; Bacon et al.

99   1992) and are often abundant in quartz phenocrysts from rhyolites. These can then be used to

100   make interpretations about the growth history of the quartz, and petrogenetic relations within the

101   magma body.

102   This study examines measured Ti profiles in quartz phenocrysts from the Bandelier Tuff,

103   Valles caldera, NM, USA, and compares Ti zoning with MI chemistry. Using finite-difference

104   diffusion modeling procedures (Costa et al., 2008), the results are applied to estimating crystal

105   residence times between initiation of overgrowth following a crystal resorption event and

106   eruptive quenching, assuming diffusional relaxation of Ti in quartz crystals from an initial step

107   function distribution. Melt inclusions hosted within those crystals are used to determine the

108   petrogenetic history of the quartz. Wilcock et al. (2013) provide a detailed dataset on the CL and

109   Ti zoning in quartz from the Tshirege Member. This study expands on those data with higher

110   spatial resolution and MI chemistry.

111

112   **GEOLOGICAL AND PETROLOGICAL BACKGROUND**

113   The ~400 km^3 Tshirege (upper) Member of the Bandelier Tuff erupted to form the Valles

114   caldera, Jemez Mountains, NM, USA at 1.26 Ma (Bailey et al., 1969; Phillips et al., 2007;

115   Gardner et al., 2010; Goff et al., 2014) and has been the subject of several petrological and

116   volcanological studies (Smith and Bailey, 1966; Self et al., 1986, 1996; Balsley, 1988; Warshaw

117   and Smith, 1988; Caress, 1996; Stimac, 1996; Warren et al., 2007; Wilcock et al., 2013; Goff et

118   al., 2014; Wolff et al., 2015). It is strongly compositionally zoned from early-erupted high-silica

119   rhyolite to late-erupted low-silica rhyolite, with complex compositional variations in the last-

120   erupted tuff (Smith and Bailey, 1966; Balsley, 1988; Goff et al., 2014; Boro, 2019). The

121   Tshirege Member event was preceded by eruption of the similarly-sized, chemically-zoned high-

122   silica rhyolite Otowi (lower) Member of the Bandelier Tuff at ~1.60 Ma, which formed a caldera

123   now largely overprinted by the later eruption (Goff et al., 2011, 2014; Wolff and Ramos, 2014).

124   During the ~340,000 y interval between the two caldera-forming events, several minor eruptions

125   produced the Valle Toledo Member rhyolite domes and pyroclastic flow and fallout deposits of

126   the Cerro Toledo Formation (Gardner et al., 2010).

127   The Tshirege Member consists of a widespread plinian fallout unit, the Tsankawi Pumice

128   Bed, overlain by non- to densely welded ignimbrite, emplaced by numerous pyroclastic density

129   currents (Bailey et al., 1969; Self et al., 1986, 1996). The ignimbrites are divided into mappable

130   units, recognized over a wide area and designated Qbt1 through Qbt5 in ascending order; some

131   numbered units are additionally subdivided (Warren et al., 2007; Goff et al., 2014). All units

132   contain a range of compositions shown by bulk chemical analysis of single pumices and bulk

133   tuff, representing magmas at different degrees of evolution (Balsley, 1988; Self et al., 1996;

134   Warren et al., 2007; Goff et al., 2014). The Tshirege Member consists of volumetrically

135   dominant high-silica rhyolite (75–79% SiO_2), low-silica rhyolite (73–75% SiO_2), and hornblende

136   dacite with 67–71% SiO_2 (Bailey et al., 1969; Self et al., 1996; Stimac, 1996; Boro, 2019). The

137   dacite occurs as pumice clasts scattered through most of the Tshirege Member, and may

138   represent the recharge event that triggered the Tshirege eruption (Stimac, 1996; Goff et al., 2014;

139   Boro et al., 2020). Goff et al. (2014) also identify an additional component of andesite in late-

140   erupted units. Despite the overall zoned character of the Tshirege Member, there is wide

141   variation in pumice composition at any one stratigraphic level (Self et al., 1996). Several

142   processes, such as overturn driven by gas exsolution or thermal disturbance before eruption

143   (Bachmann and Bergantz, 2006; Burgisser and Bergantz, 2011), extraction effects during

144   eruption (Blake and Ivey, 1986a,b; Trial et al., 1992), or non-sequential deposition of the

145   different magmatic components (Torres et al., 1996; Branney and Kokelaar, 2002) may limit,

146   scramble or obscure the record of zoning in the final deposits. Hence, we find the abundances of

147   incompatible elements in single pumice clasts to be the most useful indicators of degree of

148   magmatic evolution and hence likely vertical position in the pre-eruptive magma body, assuming

149   them as proxies for melt H_2O contents and hence densities. This assumption is supported by H_2O

150   contents of melt inclusions in quartz and feldspar (Dunbar and Hervig, 1992).

151

152   **Tshirege Pumice**

153   Whole-pumice chemistry (Fig. 2) shows three distinct rhyolites were present in the

154   Tshirege magma body at the time of eruption (Boro, 2019): two high-silica rhyolites, one

155   enriched in incompatible trace elements (99–173 ppm Nb, 25–41ppm Th: HSR-e) and one

156   relatively depleted in those elements (44–74 ppm Nb, 14–21 ppm Th: HSR-d), and a low-silica

157   rhyolite (26–42 ppm Nb, 10–14 ppm Th: LSR). Quartz grains analyzed in this study were

158   extracted from these three compositional groups of rhyolite pumice. The HSR-e is representative

159   of the Tsankawi Pumice Bed and the lowermost part of Qbt1, and the HSR-d corresponds to the

160   later-erupted Units Qbt2 and Qbt3 of Warren et al (2007). One additional sample, 88-1, is a

161   hornblende dacite pumice containing quartz scavenged from rhyolite, which is texturally

162   identical to the quartz in the rest of the rhyolite and so has been included in this study.

163   Quartz crystals in the Tshirege Member are frequently zoned when viewed in CL (Fig. 1).

164   The style of zoning varies, but is dominantly 'reverse' in character, where crystal cores appear

165   dark (lower Ti, consistent with more evolved melt or lower temperature) and rims appear bright

166   in CL (higher Ti). Wilcock et al. (2013) describe three different CL zoning types in the Tshirege

167   quartz: (1) reverse zoning, with varying sharpness of the boundary between CL-dark core and

168   CL-bright rim; (2) normal zoning with a bright core and dark rim; and (3) crystals that are

169   completely non-zoned. The full range of zoning styles and statistical analyses of their

170   distribution in the Tshirege Member is described by Wilcock et al. (2013) and our study finds a

171   similar distribution (Fig. 1). For the diffusion modeling portion of this study, we focus on

172   crystals with sharp reverse zoning boundaries, which were extracted from whole pumices

173   collected from the sub-unit Qbt3.

174   **DATA ACQUISITION**

175   We analyzed oriented quartz grain separates, cut normal to the c axis, from the Tshirege

176   Member. Grain mounts were made using >500 μm size-fraction crystal separates. Titanium

177   concentrations in quartz were measured by wavelength-dispersive electron probe microanalysis.

178   Measurements were made on a JEOL JXA-8500F field emission electron microprobe located in

179   the Peter Hooper GeoAnalytical Lab at Washington State University, using an accelerating

180   potential of 20kV, a beam current of 400nA, and a spot size of 2-10 μm, following the

181   procedures described by Donovan et al. (2016) for analysis of trace elements in simple matrices

182   such as SiO_2. To summarize, measured peak X-ray intensities were corrected for continuum

183   intensity using the mean atomic number (MAN) method of Donovan and Tingle (1996), and then

184   blank corrected using the procedure of Donovan et al. (2011) to eliminate systematic errors in

185   accuracy resulting from background artifacts. Quartz crystals from Herkimer, NY, with Ti

186   concentrations of <30 ppb (Kohn and Northrup, 2009; Kidder et al., 2013) were used as a blank

187   standard. Several mounts of Herkimer quartz were prepared, so that blank standards and

188   unknowns could be carbon coated together prior to analysis to minimize differences in coating

189   thickness between blank standards and unknowns.

190   We acquired data for a cumulative time of 18 minutes using three spectrometers.

191   Titanium concentration profiles were measured with 4 or 8 μm spacing between analysis spots.

192   Measurement of [Ti] in this manner allows for detection limits of <2 ppm and analytical

193   precision (based on counting statistics) of <5% (2-sigma) for each individual measurement. This

194   combination of spot size and uncertainty is comparable to those obtained using synchotron XRF

195   on similar samples (Matthews et al., 2012; Gualda and Sutton, 2016), but with improved (i.e.,

196   shallower) depth averaging.

197   Measurements were made either on grain mounts, using quartz crystals separated from

198   the rock matrix, or in thin sections on areas far enough from adhering Ti-bearing glass or Ti-rich

199   phases, to avoid artifacts from continuum fluorescence (cf. Fournelle 2007). To minimize effects

200   arising from obliquely or randomly oriented zone boundaries and off-center sections (Shea et al.,

201   2015), crystals were mounted such that profiles were measured normal to the *c* axis across the

202   broadest part of quartz bipyramids (Fig. 1). Titanium concentration profiles ranged in length

203   from 200-400 μm and multiple profiles were acquired on some grains to test for heterogeneity

204   along CL brightness boundaries. Additionally, some profiles oblique to zone boundaries were

205   acquired and then trigonometrically corrected to obtain higher resolution across boundaries with

206   small diffusional relaxation widths. Modeling of the effects of continuum fluorescence across the

207   boundaries between low- and high-Ti zones within the quartz crystal using PENEPMA (Llovet

208   and Salvat, 2016) suggests that any effects of secondary fluorescence of the higher-Ti zone

209   across the boundary are negligible (~1 ppm or less). All profiles, their model times, explanation

210   of oblique profiles, and a comparison of multiple profiles on single crystals can be found in the

211   supplementary data file.

212   Grayscale CL images were obtained using a Gatan MiniCL cathodoluminescence

213   detector mounted on the WSU JEOL JXA-8500F using a 50 nA beam current, 10 kV, and 60

214   second capture time producing images with an effective image resolution of 1 μm, with constant

215   contrast and brightness settings. ImageJ software was used to produce grayscale intensity graphs

216   along EPMA transect lines. Under these conditions the grayscale intensities are considered

217   internally consistent.

218   Titanium concentrations were also measured in a subset of quartz crystals by laser

219   ablation inductively-coupled plasma mass spectrometry (LA-ICP-MS) to confirm the accuracy of

220   EPMA measurements. The LA-ICP-MS measurements were performed on zones in quartz

221   crystals that were uniformly CL-bright or CL-dark, where EPMA measurements yielded uniform

222   Ti concentrations. Data were collected using a Teledyne Analyte Excite Excimer 193 nm laser

223   ablation system attached to a Finnigan Element2 ICP-MS. A 20 μm spot size was used with 7

224   J/cm^2 beam energy, and counts collected for 30 seconds along transects that ran parallel to

225   crystal faces and zone boundaries, staying within the zones defined by CL imaging. Calibration

226   was achieved using NIST-612 and BCR-G glasses, plus a well-characterized internal standard

227   quartz with 9 ppm Ti. Results of LA-ICP-MS and EPMA measurements of Ti are

228   indistinguishable within analytical uncertainty (Table 1).

229   Melt inclusions in quartz and external glasses in the HSR-e, HSR-d, and LSR samples

230 were analyzed for Ti, Zn, Rb, Sr, Y, Zr, Nb, Cs, Ba, REEs, Hf, Ta, Pb, Th, and U using LA-ICP-

231 MS. Some additional thin sections with exposed quartz melt inclusions were also analyzed. A

232 New Wave UP-213 laser was used for ablation with a 20 Hz rep rate and laser power from 3-3.5

233 J/cm^2. Ablations were analyzed using a sampling rate of every ~0.9 sec with an Agilent 7700

234 Series quadrupole mass spectrometer. Laser track widths varied from 12-30 μm depending on

235 available glass and melt inclusion sizes. Inclusions <50 μm in diameter were avoided. Data were

236 normalized to NIST-610 using ^{28}Si or ^{29}Si as an internal reference.

237   Whole-pumice clasts were analyzed for major, minor and trace elements in the Peter

238 Hooper GeoAnalytical Lab at Washington State University by X-ray fluorescence and

239 inductively coupled plasma mass spectrometry (methods and procedures described at

240 https://environment.wsu.edu/facilities/geoanalytical-lab/technical-notes/).

241

242

243

244   **RESULTS**

245 **Cathodoluminescence**

246   CL grayscale images were obtained for >50 quartz crystals. Titanium concentration

247 profiles plus CL grayscale profiles were obtained for 20 quartz crystals from samples taken at

248 several stratigraphic heights within the Tshirege Member. Generally, CL zoning can be split into

249 three types (Fig. 1): 1. Non-zoned; 2. Reversely zoned; 3. Complex. In cases where there were

250 multiple zones (e.g., Fig. 1, panel 1, 3, and 5), the outermost zone boundary was used for

251 diffusion modeling.

252

253   **Glass trace element chemistry and melt inclusion faceting**

254   Trace-element abundances in glasses are somewhat bimodal, similar to the distribution of

255   whole-pumice compositions, but do not always reflect the bulk chemistry of the clast from which

256   they were extracted (Fig. 3; full trace element glass data can be found in the supplementary data

257   file). Melt inclusions in quartz from HSR-e plot with glasses adhering to quartz crystals and

258   groundmass glass remote from crystals in thin section (collectively referred to as "external

259   glasses") from those samples. Melt inclusions from Ti-poor quartz cores in the HSR-d and LSR

260   plot with HSR-e glasses, whereas MIs that plot with HSR-d and LSR external glasses are found

261   in CL-bright rims of crystals or in crystals that show no zoning in the HSR-d or LSR. Some MIs

262   fill a gap between the two groups of data and may have trapped a liquid composition that is not

263   represented by whole-pumice data or groundmass glass data.

264   Melt inclusions occur as faceted and non-faceted forms. Faceting in melt inclusions

265   occurs as an initially round inclusion attempts to acquire a negative crystal form, accomplished

266   through lateral diffusion of silica along the edges of the inclusion (see Fig. 3 in Gualda et al.,

267   2012; supplementary file). The time that an inclusion takes to go from non-faceted to faceted is

268   positively correlated with the size of the inclusion and negatively correlated with temperature.

269   Melt inclusions in the Tshirege quartz vary from almost perfectly round to strongly

270   faceted (Fig. 4). Inclusions have been assigned a faceting strength (FS) value from 0 = unfaceted,

271   spherical inclusion to 2 = strongly faceted, negative bipyramidal crystal shape (Fig. 4d). Facet

272   strength is assigned by visual inspection of facets; the requirements for a melt inclusion to fit into

273   any individual category are outlined in Figure 4e. Although there is some subjectivity around

274   ~FS = 1.0, 0 and 0.5 are very different from 1.5 and 2. In crystals that contain multiple facets

275 with different FS values, higher FS values are found towards the core of the crystal (Fig. 5).

276 Barium and Sr, compatible elements in rhyolite, are correlated with the degree of faceting, where

277 no melt inclusions above FS = 1 have Ba above ~15 ppm; FS = <1 have Ba of 5–66 ppm, with

278 unfaceted HSR-e inclusions having the highest Ba and Sr (Fig. 4a).

279   Highly incompatible elements (e.g., Nb and Th) show positive correlations among all

280 glasses (Fig. 3a). On most bivariate plots, external glasses and MIs from HSR-e pumices plot

281 together while glasses and MIs from the HSR-d and LSR pumices plot together (Fig. 3b, c);

282 some HSR-d and LSR MIs plot with HSR-e external glasses and MIs. Figure 3-d shows Rb/Sr vs

283 Ba/Nb and a field of strongly faceted melt inclusions. This field contains all melt inclusions with

284 a FS ≥ 1 and none with FS < 1. Generally, when faceted and unfaceted inclusions occur together

285 in the same crystal, strongly faceted inclusions occur in the cores of crystals, where weakly or

286 unfaceted inclusions occur in the rims. MIs plotting with external glasses from LSR and HSR-d

287 pumices are only found in CL-bright rims and are unfaceted. The strongly faceted MIs have

288 clearly formed from a move evolved liquid.

289   Faceted inclusions with a FS = 2 are 50-125 μm in radius, suggesting FS = 2 inclusions

290 were trapped and stored in quartz for a time on the order of at least >1,000-10,000 years (Gualda

291 et al., 2012) assuming an average storage temperature of 750 °C. Once an inclusion is strongly

292 faceted, no further changes occur, so these are minimum times. Some of the largest (r = 150 μm)

293 faceted melt inclusions in the Tsankawi pumice (700 °C) may have taken on the order of 10^4

294 years to develop (see supplementary data file for faceting times vs MI radius at different

295 temperatures, Fig. A2).

296

297 **[Ti] vs. CL grayscale intensity**

298   In Figure 6, four representative Ti concentration profiles measured across CL brightness

299   boundaries are plotted with CL grayscale intensity, shown as 3 μm pixel averages, together with

300   estimated times for development of each type of profile assuming an initial step function (next

301   section). The complete set of profiles are given in the supplementary file. Resolution of Ti data at

302   the effective spot size of 2 μm does not allow for accurate modeling of diffusional boundaries

303   thinner than ~ 16 μm (corresponding to ~200 years diffusive relaxation at 750 °C using

304   diffusivity coefficients from Cherniak et al., 2007) because 4-5 points are needed to define a

305   diffusion sigmoid; however in each case the Ti slope is less steep than this limit (Fig. 6). In

306   some cases, oblique corrected profiles allow for resolution of diffusional boundaries <16 μm (see

307   supplementary file, sample 119-4). Usually (Fig. 6, Table 2) the CL grayscale profile is

308   'sharper', i.e. closer to a step function, than the Ti profile; in a few cases they are

309   indistinguishable within uncertainty, and in two cases the Ti profile is steeper than CL grayscale,

310   albeit still overlapping within uncertainty. To illustrate the effects of the different profiles on

311   calculated timescale estimates (see **Modeled diffusion relaxation times** below), in Fig. 6 we

312   compare results from CL grayscale and Ti profiles at a fixed $T = 750$ °C; estimates may differ by

313   more than an order of magnitude. We now attempt to additionally estimate diffusion times from

314   Ti profiles using temperatures derived from thermometry.

315   **Estimation of temperature**

316   Due to the generally high activation energies associated with cation diffusion in silicate

317   minerals, timescales calculated from diffusion profiles are very sensitive to temperature (e.g.,

318   Cherniak et al., 2007). For example, a ΔT of ~50 °C, which is similar to the error range (i.e. ±25

319   °C) arising from calibration and microprobe data uncertainty for many mineral geothermometers,

320   may result in an order of magnitude change in calculated relaxation time. It is therefore

321 necessary to constrain temperature during diffusive relaxation as closely as possible. The

322 Tshirege Member contains magnetite and sporadic ilmenite, but we did not find any pairs that

323 pass the equilibrium test of Bacon and Hirschmann (1988). The first-erupted parts of both the

324 Otowi and Tshirege Members of the Bandelier Tuff (respectively, the Guaje and Tsankawi

325 Pumice Beds) have compositions that are close to haplogranite, are homogeneous, exhibit the

326 least textural evidence for internal disequilibrium within their respective members, and plot very

327 near the minimum in Q–Ab–Or at 2 kb H_2O saturation pressure (Wilcock et al., 2013; Wolff and

328 Ramos, 2014), consistent with a magma temperature close to 700 °C (Tuttle and Bowen, 1958)

329 and the measured H_2O contents of melt inclusions (Dunbar and Hervig, 1992). Warshaw and

330 Smith (1988) give a temperature of 697 °C for the Tsankawi magma, based on an early version

331 of the QUILF thermometer (Andersen and Lindsley, 1988), but do not report uncertainties.

332 Wilcock et al. (2013) review several lines of evidence for storage depth of the Tshirege magma

333 and conclude that a pressure of 200 ± 50 MPa is most appropriate. We concur and assume this

334 pressure and a temperature of 700 °C for the Tsankawi Pumice magma.

335   The TitaniQ thermometer (Wark and Watson, 2006, equation 1 below; Thomas et al.,

336 2010, equation 2 below; Huang and Audétat, 2012, equation 3 below), which relies on the

337 temperature dependence of [Ti] in quartz, can be applied to quartz grains chosen for diffusion

338 modeling, thus avoiding the potential problem in applying temperatures estimated from other

339 mineral phases in high-silica rhyolites that may not be in equilibrium with quartz (Evans and

340 Bachmann, 2013; Evans et al., 2016):

341
$$T(°C) = \frac{-3765 \pm 24}{\log\left(\frac{X_{Ti}^{qtz}}{a_{TiO_2}}\right) - 5.69 \pm 0.02} - 273 \qquad (1)$$

342

$$RT\ln X_{TiO_2}^{\text{quartz}} = -(60952 \pm 3177) + (1.520 \pm 0.39) * T(K) - (1741 \pm 63) * P(kbar) + RT\ln a_{TiO_2}$$

343   (2)

344
$$\log \mathrm{Ti(ppm)} = -0.27943 * \frac{10^4}{T} - 660.53 * \frac{P^{0.35}}{T} + 5.6459 \qquad (3)$$

345   In each case, the thermometer is experimentally calibrated for melts saturated with rutile,

346 hence $a(\mathrm{TiO_2})_{\mathrm{melt}} = 1$; the chief difficulty in its application therefore lies in the estimation of

347 $a(\mathrm{TiO_2})_{\mathrm{melt}}$ because the vast majority of volcanic silicate liquids are not rutile-saturated. Hayden

348 and Watson (2007) provide a method for estimating $a(\mathrm{TiO_2})_{\mathrm{melt}}$ based on rutile saturation as a

349 function of melt composition and temperature; however this is only calibrated at 1 GPa, at which

350 pressure rutile solubility is likely less than at the mid- to upper-crustal storage depths of most

351 rhyolites (Thomas and Watson, 2012). Rhyolite-MELTS (Gualda et al., 2012) calculates

352 $a(\mathrm{TiO_2})_{\mathrm{melt}}$ but the values for the exceptionally Ti-poor glasses of the Tshirege Member are

353 extremely low ($\sim 10^{-5}$), yielding unreasonably high temperatures.

354   Instead, we have calculated $a(\mathrm{TiO_2})_{\mathrm{melt}}$ for the Tshirege Member by 'internally

355 calibrating' to an assumed temperature of 700 °C for the first-erupted Tsankawi pumice, and

356 setting $a(\mathrm{TiO_2})_{\mathrm{melt}}$ to a value of 0.34, which yields 700 °C for the average compositions of

357 Tsankawi quartz (~22.5 ppm Ti) using Eqn. (1). The same result is obtained from the Huang and

358 Audétat (2012) calibration (Eqn. 3) using this $a(\mathrm{TiO_2})_{\mathrm{melt}}$ if P is set to 263 MPa. The high-

359 pressure Thomas et al. (2010) calibration (Eqn. 2) requires a different $a(\mathrm{TiO_2})_{\mathrm{melt}}$ of 0.0775, and

360 was not used here. The Tsankawi-derived $a(\mathrm{TiO_2})_{\mathrm{melt}}$ value is then treated in two ways. In the

361 first approach, $a(\mathrm{TiO_2})$ is assumed constant throughout the Tshirege Member high-silica rhyolite

362 magma. This assumption can be justified on the basis that titanomagnetite is a ubiquitous, if

363 trace, phenocryst phase (Warren et al., 2007) and hence may buffer $a(\mathrm{TiO_2})_{\mathrm{melt}}$. However, it is

364 unclear whether or not quartz and titanomagnetite were co-precipitating phases, or whether

365 titanomagnetite compositions or abundances may have changed during quartz growth, an issue

366   that has led to conflicting interpretations of temperature estimates for the Bishop Tuff, a similar

367   voluminous high-silica rhyolite eruption (Evans and Bachmann, 2013; Gualda and Ghiorso,

368   2013; Evans et al., 2016; Jolles and Lange, 2019). Therefore, when estimating $a(TiO_2)_{melt}$ for the

369   Tshirege Member magmas, buffering cannot be assumed. Instead, the $a(TiO_2)_{melt}$ value of 0.34 is

370   used to calculate an effective TiO_2 activity coefficient for measured TiO_2 in Tsankawi glasses,

371   which is then applied to compositions of glasses in contact with quartz rims throughout the

372   Tshirege Member. The assumption of constant $\gamma(TiO_2)_{melt}$, where γ denotes the activity

373   coefficient, is justified by the essentially constant major-element composition of Tshirege high-

374   silica rhyolite.

375   Modeled diffusion relaxation times (next section) are calculated using three different

376   temperature assumptions: (i) constant temperature of 750 °C (Fig. 6); (ii) temperature estimated

377   using the Wark and Watson (2006) and Huang and Audétat (2012) calibrations at 263 MPa,

378   assuming constant $a(TiO_2)_{melt}$; (iii) temperature estimated using the Wark and Watson (2006)

379   and Huang and Audétat (2012) calibrations at 263 MPa, and applying calculated $\gamma(TiO_2)_{melt}$ to Ti

380   contents of glasses adhering to quartz crystals to estimate $a(TiO_2)_{melt}$. In cases (ii) and (iii), the

381   temperature calculated from the rim composition of the quartz is assumed to apply to diffusion at

382   the inner boundary of the rim.

383

384   **Modeled diffusion relaxation times**

385   We use the 1-D finite difference diffusion method (Costa et al., 2008, equation 4 below),

386   to model Ti diffusion in quartz as a function of time and distance of travel in the lattice:

387
$$C_{i,j+1} = C_{i,j} + \left(\frac{D\Delta t \left(C_{i+1,j} - 2C_{i,j} + C_{i-1,j} \right)}{\Delta x^2} \right) \qquad (4)$$

388   Where: $C_{i,j}$ = the concentration at the current lattice location; $C_{i,j+1}$ = the concentration at the

389   current lattice location one time step forward; $C_{i+1,j}$ = the concentration one lattice step towards

390   the diffusion zone; $C_{i-1,j}$ = the concentration one lattice step away from the diffusion zone; D =

391   diffusion coefficient for the diffusing species in lattice of interest; Δt = change in time for one

392   step in the model; Δx = step size. Boundary conditions for the high and low steps at time = 0

393   were set as the average [Ti] outside of the diffusive relaxation zone, where data formed a plateau,

394   or in cases where data did not form a good plateau, the boundary condition was set to a best fit

395   line through boundary data.

396   The diffusion coefficient of Ti in quartz parallel to the c axis is not well established and

397   we use the two current published values given by (Cherniak et al., 2007, equation 5; Jollands et

398   al., 2020, equation 6):

399                          $D_{\mathrm{Ti}} = 7 \times 10^{-8}\exp(-273\pm12 \text{ kJ mol}^{-1} /RT) \text{ m}^2 \text{ sec}^{-1}$ (5)

400

401                          $log_{10}D_{\mathrm{Ti}} = -8.3\pm 0.4 - [311\pm 12 \text{ kJ mol}^{-1} /(2.303RT)] \text{ m}^2 \text{ sec}^{-1}$ (6)

402   Where: D_{Ti} = diffusion coefficient of Ti in quartz, R is the universal gas constant and T is

403   absolute temperature. Cherniak et al. (2007) provide seven additional experiments measuring Ti

404   diffusion in quartz normal to c, with little anisotropy apparent. Regression of those experiments

405   over the temperature range 750 – 1101 °C gives an Arrhenius relation that yields results

406   indistinguishable from Eqn (5), which we use here and suggests that Ti-diffusion parallel or

407   perpendicular to c-axes is similar. Errors for the CL and Ti profiles at constant temperatures are

408   calculated from the inherent error in the D_{Ti} which, when applied to these data, lead to large (40-

409   60%) errors of modeled times. In Table 2, uncertainties of diffusion times for the Ti profiles

410   calculated using temperatures from TitaniQ that arise from fitting sigmoids to the data are

411   reported separately. The very different diffusivities from Cherniak et al. (2007) and Jollands et

412   al. (2020) result in diffusion timescales that are systematically offset by an average of two orders

413   of magnitude (Figure 6; Tables 2 and 3); the implications of these results are outlined in the

414   **Discussion** section below.

415   In most cases, Ti diffusive relaxation times calculated from CL grayscale profiles are

416   shorter than those calculated from Ti data using the same D_{Ti}, by up to an order of magnitude

417   (Table 2, Fig. 6). In some cases the two profiles yield identical results within error. Previous

418   authors have presented discrepant CL grayscale and Ti concentration data, consistent with our

419   findings (e.g., Fig. 9 of Matthews et al., 2012), but have discounted the significance for

420   calculated timescales. We also note that, overall, grayscale profiles are smoother than those for

421   Ti concentrations from the same crystal (Fig. 6), resulting in many cases in decreased, but

422   perhaps less realistic, calculated uncertainties associated with timescales (Table 2). Furthermore,

423   while spectroscopic measurements of quartz CL emissions at specific wavelengths, such as ~454

424   nm, are very well correlated with Ti contents (MacRae et al., 2013, 2018), greyscale CL is not a

425   reliable proxy for Ti concentration. For many panchromatic CL detectors, the collection optics

426   accept light from a wide variety of angles, and therefore light from adjacent areas, which are still

427   emitting from the initial electron bombardment, or light transmitted through the sample and

428   scattered off of microcracks in the sample, which may be included in a CL measurement that is

429   supposed to represent only the CL emitted from an individual pixel (MacRae et al., 2013). Also,

430   as described by Leeman et al. (2012) and MacRae et al. (2018), greyscale intensities include not

431   only CL from Ti dopants, but also from the intrinsic CL produced by quartz, by crystallographic

432   defects, by aluminum dopants, and by non-bridging oxygen holes in the crystal structure. In fact,

433   certain CL emissions from quartz, such as those from non-bridging oxygen holes, are actually

434   *inversely* correlated with Ti contents (see Fig. 4 of Leeman et al., 2012). Therefore, the diffusion

435   profiles used for the modeling presented here are based on the Ti concentrations measured by

436   EPMA; profiles based on CL intensity are not considered.

437

438   **DISCUSSION**

439   Titanium concentrations in rims of zoned quartz are invariably higher than those in

440   Tsankawi quartz, hence estimated temperatures are always higher. Assuming 700 °C for the

441   Tsankawi, the average temperature (excluding dacite 88-1) for quartz rims in pumice clasts with

442   64 – 73 ppm Nb is 774 ± 14 °C (a(TiO$_2$) method) or 740 ± 17 °C (γ(TiO$_2$) method). This

443   reinforces the qualitative value of the TitaniQ thermometer, but the difficulties associated with

444   a(TiO$_2$) estimation somewhat negate its quantitative value as a thermometer applicable to

445   rhyolites (see also Wilson et al., 2012). The majority of rhyolites with high magmatic H$_2$O

446   contents erupt at temperatures between 700 and 800 °C, so the temperature estimates in Table 2

447   are reasonable but hardly surprising.

448   Sample 88-1 is a hornblende dacite pumice containing quartz texturally indistinguishable

449   from that in the high-silica rhyolite (Fig. 1); the quartz is thought to have been incorporated as

450   dacite mixed with rhyolite immediately prior to the eruption (Stimac, 1996; Boro et al., 2020).

451   The quartz rim compositions yield temperatures of 799–825 °C, consistent with 797 ± 17 °C

452   from amphibole thermometry (Boro et al., 2020). Despite the higher temperature, this quartz

453   crystal produces one of the longest modeled Ti diffusion times (see 750 °C Ti model-time

454   column, Table 2), and hosts a FS = 2 melt inclusion in the CL-dark core, supporting a long

455   storage time for this crystal.

456   There is a large discrepancy between the widely-used values of D_{Ti} in quartz of Cherniak

457   et al. (2007), and the recent estimate of Jollands et al. (2020); compare eqns (5) and (6). Use of

458   eqn. (5) has produced estimates of short timescales for quartz regrowth (Matthews et al., 2012;

459   Till et al., 2015; Gualda and Sutton, 2016; Cooper et al., 2017), although in some cases these

460   timescales are supported by other methods (e.g., Chamberlain et al., 2014a). In the case of the

461   Tshirege Member, the Jollands et al. (2020) diffusivities yield modeled diffusion times of

462   chemical relaxation across growth boundaries in quartz up to 10^7 years (Table 3), which is

463   geologically unreasonable for this system; we take the 360 k.y. time between the Otowi and

464   Tshirege eruptions as the maximum geologically reasonable timescale for crystal growth likely

465   to be recorded in the Tshirege Member. Most of the estimates in Table 3 are longer.

466   Therefore, if the Jollands et al. (2020) diffusion coefficients (Eqn. 6) are preferred, the

467   assumption of an initial step-function Ti concentration profile may be invalid, and the profiles in

468   Fig. 6 are partly inherited from crystal growth. In this case the initial condition is not

469   constrained. Although diffusion sigmoids can be fit to all cases, in detail both the CL and Ti

470   concentration profiles show numerous minor reversals and irregularities on either side of the

471   zone boundary. Commonly, a thin peak in Ti or Cl brightness occurs of the high-Ti side of the

472   boundary (Fig. 6; supplemental data). These variations may be due to changes in crystal growth

473   rate (Huang and Audétat, 2012). However, the major CL dark core – CL light rim boundary

474   often truncates earlier zoning in the crystal core, so is not solely a result of changes in growth

475   rate but is the product of an episode of resorption followed by regrowth. The presence of

476   unfaceted melt inclusions in many crystals, including some of the CL-bright crystal rims, limits

477   their residence at magmatic temperature to less than $\sim2 \times 10^4$ years (supplementary data), using

478   the faceting time estimation of Gualda et al. (2012; their eqn. 9). In addition to the overall

479 chronology of the Bandelier system, this also militates against the timescales estimated using

480 Eqn. (6), and assuming an initial step function, having any geological meaning.

481 If the Cherniak et al. (2007) diffusion coefficients (eqn. 5) are preferred, the results

482 suggest that an event or events involving reheating of the system occurred over a range between

483 <100 and >1,000 years (order of magnitude) prior to eruption, generally consistent with melt

484 inclusion faceting times. These events preceded recharge by the dacite, which may have acted as

485 the trigger for the eruption (Stimac, 1996; Goff et al., 2014; Boro et al., 2020) on a shorter

486 timescale. Some quartz crystals (Fig. 1) have rounded edges and appear to have gone through an

487 additional resorption event, truncating existing zoning patterns, without subsequent growth of

488 new quartz prior to the eruption, so the calculated times in Table 2 may reflect a sequence of

489 events cascading towards the caldera-forming eruption.

490 The reasons for the large contrast between fast and slow diffusivities estimated by

491 Cherniak et al. (2007) and Jollands et al. (2020) respectively is unclear. Each study uses a

492 experimentally similar method of exposing quartz to a powdered source of TiO_2 followed by

493 depth profiling, with the major differences being that Cherniak et al. (2007) used a 99.9% pure

494 TiO_2 source for Ti and Jollands et al. (2020) used a Ti-doped SiO_2 powder with [Ti] of ~100

495 ppm. Jollands et al. (2020) were unable to reproduce the results of Cherniak et al. (2007) using a

496 pure TiO_2 source due to degradation of the quartz crystal surface during a one-hour annealing

497 with a pure rutile powder, making subsequent depth profiling using SIMS unfeasible. Jollands et

498 al. (2020) speculate that Ti may have more than one diffusion mechanism in quartz, with the

499 faster mechanism effectively absent at the low Ti concentrations of their experiments (see their

500 supplemental file p. 10), and therefore, by implication, in the majority of natural cases. The

501   question of which diffusivities are more correct has significant implications for understanding

502   the dynamics and timescales for silicic magma systems. Our study does not resolve this question.

503

504   **IMPLICATIONS**

505   **Compositional zoning of the Tshirege Member magma**

506   Most quartz cores from HSR-d pumice have near-constant and low Ti contents,

507   indistinguishable from non-zoned quartz in HSR-e Tsankawi pumice. The MIs hosted by these

508   cores are typically faceted and have trace element abundances similar to HSR-e pumice, whereas

509   the occasional MIs in the Ti-rich rims of quartz from HSR-d pumice have HSR-d chemistry and

510   are non- or weakly faceted (Fig. 5). These observations link overall bulk zoning in the Tshirege

511   Member to melt inclusion chemistry (Figs. 2, 3), quartz growth, and quartz residence time. The

512   most evolved, first-erupted melt compositions (HSR-e chemistry) and low-Ti quartz existed

513   *before* the less evolved, late-erupted melt (HSR-d and LSR chemistries) and high-Ti quartz

514   developed in the erupted portion of the system. This is consistent with a simple model of

515   crystallization, cumulate formation, and subsequent melting and remobilization of the cumulate

516   to create a compositionally zoned magma body (Wolff et al., 2015, 2020). In this model, which

517   is an extension of the 'mush model' (Bachmann and Berganz, 2004; Hildreth, 2004), the quartz-

518   feldspar cumulate pile beneath a cognate crystal-poor melt lens is heated and remobilized by

519   recharge, with little mass contribution from the recharge magma (Wark et al., 2007; Wolff and

520   Ramos, 2014). The result is a relatively water-poor rhyolite, of higher density and with lower

521   incompatible element concentrations than the initial rhyolite melt lens. The new melt, with a

522   cargo of crystals inherited from the cumulate pile, pools beneath the initial melt lens to form a

523   thicker, compositionally zoned body of eruptible magma. The lack of quartz zoning in HSR-e

524   samples suggests an enriched liquid lens that was shut off from the thermal and chemical effects

525   of invading recharge magmas, likely shielded by a crystal mush that was melted and mobilized to

526   form the HSR-d magma.

527   Figure 7 depicts four stages in the development of zoning in the Tshirege system:

528   a. Initial state of the system is an accumulating crystal mush overlain by a lens of

529   magma, which is highly enriched in incompatible trace elements, and depleted in

530   compatible trace elements – especially those which strongly partition into sanidine

531   (i.e., Sr and Ba). This system is producing quartz crystals that trap melt from the

532   evolved body and settle to contribute to the mush.

533   b.   The mush is around 70% crystallinity with correspondingly lower bulk water content

534   then the melt and consists of crystals with melt inclusions. Storage for 1,000-10,000

535   years allows for faceting of melt inclusions.

536   c. Recharge magma, underplating and intruding the crystal mush column, acts as a

537   heating element and may also add H_2O to the system from second boiling, loosening

538   the mechanically locked mush (Boro, 2019), causing quartz crystals to partially

539   resorb. Simultaneous melting of feldspar adds Ba and Sr to the melt. Crystals resume

540   growing.

541   d.   Quartz crystals regrow as they find a new equilibrium at higher temperatures forming

542   CL-bright rims with higher Ti concentrations, and capture the recharge event with

543   unfaceted melt inclusions enriched in Ba and Sr. Continued recharge of the system

544   mobilizes the mush and overpressure triggers the eruption.

545

546   **Eruption forecasting**

547   An important application of petrologic study of past eruptions is to draw links between

548   events recorded in crystals and melts, particularly those interpreted as destabilizing to the

549   system, and monitoring signals that might be detected at the surface in the run-up to a future

550   eruption (Blundy and Cashman, 2008). Studies using the Cherniak et al. (2007) Ti-in-quartz

551   diffusion coefficients (e.g., Gualda and Sutton, 2016; Cooper et al., 2017) have emphasized short

552   timescales of crystal regrowth and residence following recharge events prior to a supereruption.

553   In the case of the Tshirege Member, the events recorded in quartz would imply multiple

554   disturbances over $\sim 10^3$ years prior to eruption, culminating in the intrusion of dacite magma into

555   the system, the probable immediate trigger for the eruption (Goff et al., 2014; Boro et al., 2020).

556   If recharge events can be detected at the surface (e.g., inflation, seismicity, increased gas flux), it

557   is unclear how the critical eruption trigger could be identified, but a series of events over a long

558   term might indicate destabilization of a static magma body. The new diffusion coefficients of

559   Jollands et al. (2020) immediately throw all the short timescale estimates derived by previous

560   workers from Ti (or CL) profiles in quartz into question. Jollands et al. (2020) note that the

561   longer timescales of $10^{5\pm1}$ y they calculate for quartz residence and growth in the Bishop Tuff are

562   consistent with the durations of magma reservoir assembly derived from zircon U-Th-Pb dating

563   and other methods. We may note that both short and long timescales for the Bishop Tuff - Long

564   Valley system are currently supported by other methods: short times ($<10^2$ years, Wark et al.,

565   2007, using the Cherniak et al., 2007 diffusivities) are supported by diffusion-based estimates

566   from other phases (Chamberlain et al., 2014a) and long times ($\sim 10^5$ years, Jollands et al., 2020,

567   using their diffusivities) by radioisotope studies of zircon (Coath and Reid, 2000; Simon and

568   Reid, 2005; Chamberlain et al., 2014b). Regardless of which Ti diffusivities are correct, an

569   overall picture of silicic systems being established over $\sim 10^5$ years or longer, and subject to

570   multiple disturbances such as recharge which ultimately lead to eruption, seems robust; the

571   question that remains is what exactly quartz is telling us about this history.

572   Our results from the Tshirege Member suggest that the longer Ti-in-quartz duration

573   estimates may be incorrect, not necessarily because the diffusivity experiments are flawed, but

574   more probably because the assumption of an initial sharp Ti-zone boundary in quartz is invalid.

575   The agreement of shorter times obtained using the diffusivity value published by Cherniak et al.

576   (2007) with melt-faceting times is also notable. We conclude that, without constraints on initial

577   conditions, Ti profiles in quartz shed no light on the timescales for destabilization and

578   mobilization of rhyolitic magma bodies preparatory to eruption until this current discrepancy is

579   sufficiently addressed.

580

587

588   **REFERENCES CITED**

589   Anderson, D.J., Lindsley, D.H. (1988) Internally consistent solution models for Fe-Mg-Mn-Ti

590   oxides; Fe-Ti oxides. American Mineralogist 73, 714-726.

591   Arzilli et al. 2019. The unexpected explosive sub-Plinian eruption of Calbuco volcano

592   (22–23 April 2015; southern Chile): Triggering mechanism implications. Journal of

593   Volcanology and Geothermal Research 378 (2019): 35-50.

594   Bachmann, O., Bergantz, G.W. (2004) On the Origin of Crystal-poor Rhyolites: Extracted from

595   Batholithic Crystal Mushes. Journal of Petrology 45-8, 1565-1582.

596   Bachmann, O., Bergantz, G.W. (2006) Gas percolation in upper-crustal silicic crystal mushes as

597   a mechanism for upward heat advection and rejuvenation of near-solidus magma bodies.

598   Journal of Volcanology and Geothermal Research, 149, 85-102.

599   Bacon, C.R. and Hirschmann, M.M. (1988) Mg/Mn partitioning as a test for equilibrium between

600   coexisting Fe-Ti oxides. American Mineralogist, 73, 57–61.

601   Bacon, C.R., Newman, S., Stopler, E.M. (1992) Water, CO2, Cl, and F in melt inclusions in

602   phenocrysts from three Holocene explosive eruptions, Crater Lake, Oregon. American

603   Mineralogist, 77(9-10), 1021-1030.

604   Bailey, R.A., Smith, R.L. and Ross, C.S. (1969) Stratigraphic nomenclature of volcanic rocks in

605   the Jemez Mountains, New Mexico. U.S. Geological Survey Bulletin, 1274-P, 1–19.

606   Balsley, S.D. (1988) The petrology and geochemistry of the Tshirege Member of the Bandelier

607   Tuff, Jemez Mountains volcanic field, New Mexico, U.S.A. M.S. thesis, University of Texas

608   at Arlington, 188 p.

609   Blake, S., Ivey, G.N. (1986a) Magma-mixing and the dynamics of withdrawal from stratified

610   reservoirs. Journal of Volcanology and Geothermal Research, 27, 153-178.

611   Blake, S., Ivey, G.N. (1986b) Density and viscosity gradients in zoned magma chambers, and

612   their influence withdrawal dynamics. Journal of Volcanology and Geothermal Research, 30,

613   201-230.

614   Blundy, J., Cashman, K. (2008) Petrologic Reconstruction of Magmatic System Variables and

615   Processes. Reviews in Mineralogy and Geochemistry 69, 179-239.

616   Boro, J.R. (2019) Recharge and mobilization of crystal mush to produce and erupt a zoned

617   magma chamber – the Tshirege Member of the Bandelier Tuff, Valles caldera, New Mexico,

618   USA: Ph.D. dissertation, Washington State University.

619   Boro, J.R., Wolff, J.A. and Neill, O.K. (2020) Anatomy of a recharge magma: Hornblende dacite

620   pumice from the rhyolitic Tshirege Member of the Bandelier Tuff, Valles caldera, New

621   Mexico, USA. Submitted to Contributions to Mineralogy and Petrology.

622   Branney, M.J. and Kokelaar, P. (2002) Pyroclastic Density Currents and the Sedimentation of

623   Ignimbrites. Geological Society. Geological Society Memoir, 27, 143 pp.

624   Burgisser, A., Bergantz, G.W. (2011). A rapid mechanism to remobilize and homogenize highly

625   crystalline magma bodies. Nature, 471, 212-215.

626   Campbell, M.E., Hanson, J.B., Minarik, W.G., and Stix, J. (2009) Thermal history of the

627   Bandelier magmatic system: evidence for magmatic injection and recharge at 1.61 Ma as

628   revealed by cathodoluminescence and titanium geothermometry. Journal of Geology, 117,

629   469–485.

630   Caress, M.E. (1996) Zonation of alkali feldspar compositions in the Tshirege Member of the

631   Bandelier Tuff in Pueblo Canyon, near Los Alamos, New Mexico. New Mexico Geological

632   Society, 47th Field Conference Guidebook, 275–283.

633   Chamberlain, K.J., Morgan, D.J., and Wilson, C.J.N. (2014a) Timescales of mixing and

634   mobilisation in the Bishop Tuff magma body: perspectives from diffusion chronometry.

635   Contributions to Mineralogy and Petrology, 168:1034, 24 pp.

636   Chamberlain, K.J., Wilson, C.J.N., Wooden, J.L., Charlier, B.L.A., and Ireland, T.R. (2014b)

637   New perspectives on the Bishop Tuff from zircon textures, ages and trace elements. Journal

638   of Petrology, 55, 395–426.

639   Cherniak, D.J., Watson, E.B, and Wark., D.A. (2007) Ti diffusion in quartz. Chemical Geology,

640   236, 65–74.

641   Cooper, G.F., Morgan, D.J., and Wilson, C.J.N. (2017) Rapid assembly and rejuvenation of a

642   large silicic magmatic system: insights from mineral diffusive profiles in the Kidnappers and

643   Rocky Hill deposits, New Zealand. Earth and Planetary Science Letters, 473, 1–13.

644   Costa, F. and Dungan M.A. (2005) Short timescales of magmatic assimilation from diffusion

645   modelling of multiple elements in olivine. Geology, 33, 837–840.

646   Costa, F., Dohmen, R., and Chakraborty, S. (2008) Time scales of magmatic processes from
647   modeling the zoning patterns of crystals. Reviews in Mineralogy and Geochemistry, 69, 545–
648   594.

649   Donovan, J.J., Lowers, H.A., and Rusk, B.G. (2011) Improved electron probe microanalysis of
650   trace elements in quartz. American Mineralogist, 96, 274–282.

651   Donovan, J.J., Singer, J.W. and Armstrong, J.T. (2016). A new EPMA method for fast trace
652   element analysis in simple matrices. American Mineralogist, 101, 1839–1853.

653   Donovan, J.J., Tingle, T.N., 1996. An improved mean atomic number background correction for
654   quantitative microanalysis. J. Microsc. Soc. Am. 2, 1-7.

655   Dunbar, N.W and Hervig, R.L. (1992) Volatile and trace element composition of melt inclusions
656   from the lower Bandelier Tuff; implications for magma chamber processes and eruptive
657   style. Journal of Geophysical Research, 97, 15,151-15,170.

658   Evans, B.W. and Bachmann, O. (2013) Implications of equilibrium and disequilibrium among
659   crystal phases in the Bishop Tuff. American Mineralogist, 98, 271–274.

660   Evans, B.W., Hildreth, W., Bachmann, O., and Scaillet, B. (2016) In defense of magnetite-
661   ilmenite thermometry in the Bishop Tuff and its implication for gradients in silicic magma
662   reservoirs. American Mineralogist, 101, 469–482.

663   Fournelle, J.F. (2007) The Problem of Secondary Fluorescence in EPMA in the Application of
664   the Ti-in-Zircon Geothermometer and the Utility of PENEPMA Monte Carlo Program.
665   Microscopy and Microanalysis, 13(S02), 1390-1391. doi: 10.1017/S1431927607079354

666   Gardner, J.N., Goff, F., Kelley, S.A. and Jacobs, E. (2010) Rhyolites and associated deposits of
667   the Valles-Toledo caldera complex. New Mexico Geology, 32, 3–18.

668   Goff, F., Gardner, J.N., Reneau, S.L., Kelley, S.A., Kempter, K.A., and Lawrence, J.R. (2011)
669   Geologic map of the Valles caldera, Jemez Mountains, New Mexico. New Mexico Bureau of
670   Geology and Mineral Resources Geologic Map, 79, scale 1:50,000.

671   Goff, F., Warren, R.G., Goff, C.J., and Dunbar, N. (2014) Eruption of reverse-zoned upper
672   Tshirege member, Bandelier Tuff from centralized vents within Valles caldera, New Mexico.
673   Journal of Volcanology and Geothermal Research, 276, 82–104.

674   Götze, J. (2012) Application of cathodoluminescence microscopy and spectroscopy in
675   geosciences. Microscopy and Microanalysis, 18, 1270–1284.

676   Gualda, A.R.G, Sutton, S.R. (2016) The Year Leading to a Supereruption. PLoS ONE 11, 18pp.

677   Gualda, G.A.R, Pamukcu, A.S., Ghiorso, M.S., Anderson, A.T Jr., Sutton, S.R., Rivers, M.L.

678   (2012) Timescales of Quartz Crystallization and the Longevity of the Bishop Giant Magma

679   Body. PLoS ONE 7(5).

680   Gualda, G.A.R. and Ghiorso, M.S. (2013) The Bishop Tuff giant magma body: an alternative to

681   the standard model. Contributions to Mineralogy and Petrology, 166, 755–775.

682   Hayden, L.A. and Watson, E.B. (2007) Rutile saturation in hydrous siliceous melts and its

683   bearing on Ti-thermometry of quartz and zircon. Earth and Planetary Science Letters, 258,

684   561–568.

685   Hildreth, W. (2004) Volcanological perspectives on Long Valley, Mammoth Mountain, and

686   Mono Craters: several contiguous but discrete systems. Journal of Volcanology and

687   Geothermal Research 136, 169-198.

688   Huang, R. and Audétat, A. (2012) The titanium-in-quartz (TitaniQ) thermombarometer: a critical

689   examination and re-calibration. Geochimica et Cosmochimica Acta, 84, 75–89.

690   Jollands, M.C., Bloch, E., and Müntener, O. (2020) New Ti-in-quartz diffusivities reconcile

691   natural Ti zoning with time scales and temperatures of upper crustal magma reservoirs.

692   Geology 48, doi:10.1130/G47238.1

693   Jolles, J.S.R. and Lange, R.A. (2019) High-resolution Fe-Ti oxide thermometry applied to

694   single-clast pumices from the Bishop Tuff: a re-examination of compositional variations in

695   phenocryst phases with temperature. Contributions to Mineralogy and Petrology 174:70, 43

696   pp.

697   Kidder, S., J.-P. Avouac and Y.-C. Chan (2013), Application of titanium-in-quartz

698   thermobarometry to greenschist facies veins and recrystal-lized quartzites in the Hsuehshan

699   range, Taiwan, Solid Earth, 4(1), 1–21, doi:10.5194/se-4-1-2013

700   Kohn MJ, Northrup CJ. 2009. Taking mylonites' temperature. Geology 37(1), 47–50

701   Leeman, W.P., MacRae, C.M., Wilson, N.C., Torpy, A., Lee, C.-T.A., Student, J.J., Thomas,

702   J.B., and Vicenzi, E/P. (2012) A study of cathodoluminescence and trace element

703   compositional zoning in natural quartz from volcanic rocks: mapping titanium content in

704   quartz. Microscopy and Microanalysis, 18, 1322–1341.

705   Llovet, X., and Salvat, F. (2016) PENEPMA: a Monte Carlo programme for the simulation of X-

706   ray emission in EPMA. IOP Conf. Ser.: Mater. Sci. Eng.109012009

707   Lowenstern, J.B., Mahood, G.A. (1991) New data on magmatic H2O contents of pantellerites,

708   with implications for petrogenesis and eruptive dynamics at Pantelleria. Bulletin of Volc. 57-

709   1, 78-83.

710   MacRae, C.M., Wilson, N.C., Torpy, A. (2013) Hyperspectral cathodoluminescence. Mineralogy

711   & Petrology 107, 429-440. Doi: 10.1007/s00710-013-0272-8

712   MacRae, C.M., Wilson, N.C., Torpy, A., and Delle Piane, C. (2018) Soft X-ray and

713   cathodoluminescence measurement, optimization and analysis at liquid nitrogen

714   temperatures. IOP Conference Series: Materials Science and Engineering, Volume 304, Issue

715   1, pp. 012010 (2018).

716   Matthews, N.E., Huber, C., Pyle, D.M., and Smith, V.V. (2012) Timescales of magma recharge

717   of large silicic systems from Ti diffusion in quartz. Journal of Petrology, 53, 1385–1416.

718   Morgan, D.J. and Blake, S. (2006) Magmatic residence times of zoned phenocrysts: introduction

719   and application of the binary element diffusion modeling (BEDM) technique. Contributions

720   to Mineralogy and Petrology, 151, 58–70.

721   Pamukcu, A.S., Ghiorso, M.S., Gualda, G.A. (2016) High-Ti, bright-CL rims in volcanic quartz:

722   a result of very rapid growth. Contributions to Mineralogy and Petrology 172, 9pp.

723   Peppard, B.T, Steele, I.M., Davis, A.M., Wallace, P.J., Anderson, A.T. (2001) Zoned quartz

724   phenocrysts from the rhyolitic Bishop Tuff. American Mineralogist 86(9), 1034-1052.

725   Phillips, E.H., Goff, F., Kyle, P.R., McIntosh, W.C., Dunbar, N.W., and Gardner, J.N. (2007)

726   The $^{40}Ar/^{39}Ar$ age contraints on the duration of resurgence at the Valles caldera, New

727   Mexico. Journal of Geophysical Research, 112, B08201, 15 p.

728   Reid, M.R. and Vasquez, J.A. (2017) Fitful and protracted assembly leading to a giant eruption,

729   Youngest Toba Tuff, Indonesia. Geochemistry, Geophysics, Geosystems 18, 156–177.

730   Seitz, S., Putlitz, B., Baumgartner, L.P., Escrig, S., Meibom, A., and Bouvier, A.-S. (2016) Short

731   magmatic residence times of quartz phenocrysts in Patagonian rhyolites associate dwith

732   Gondwana breakup. Geology, 44, 67–70.

733   Self, S., Goff, F., Gardner, J.N., Wright, J.V. and Kite, W. (1986) Explosive rhyolitic volcanism

734   in the Jemez Mountains: Vent locations, caldera development and relation to regional

735   structure. Journal of Geophysical Research, 91, 1779–1798.

736 Self, S., Heiken, G., Sykes, M.L., Wohletz, K., Fisher, R.V., and Dethier, D.P. (1996) Field
737   excursions to the Jemez Mountains, New Mexico. Bulletin of the New Mexico Bureau of
738   Geology and Mineral Resources, 134, 72 pp.
739 Shane, P., Smith, V.C., Narin, I. (2008) Millennial timescale resolution of rhyolite magma
740   recharge at Tarawera volcano: insights from quartz chemistry and melt inclusions.
741   Contributions to Mineralogy and Petrology 156, 397-411.
742 Shea, T., Costa, F., Krimer, D., and Hammer, J.E. (2015) Accuracy of timescales retrieved from
743   diffusion modeling in olivine: a 3D perspective. American Mineralogist, 100, 2026–2042.
744 Simon, J.L. and Reid, M.R. (2005) The pace of rhyolite differentiation and storage in an
745   'archetypa' silicic magma system, Long Valley, California. Earth and Planetary Science
746   Letters, 235, 123–140.
747 Smith, R.L. and Bailey, R.A. (1966) The Bandelier Tuff - a study of ash-flow eruption cycles
748   from zoned magma chambers. Bulletin Volcanologique, 29, 83–104.
749 Stimac, J.A. (1996) Hornblende-dacite pumice in the Tshirege member of the the Bandelier Tuff:
750   Implications for magma chamber and eruptive processes. New Mexico Geological Society,
751   47th Field Conference Guidebook, 269–274.
752 Thomas, J.B. and Watson, E.B. (2012) Application of the Ti-in-quartz thermobarometer to rutile-
753   free systems. Reply to: a comment on: 'TitaniQ under pressure: the effect of pressure and
754   temperature on the solubility of Ti in quartz' by Thomas et al. Contributions to Mineralogy
755   and Petrology, 164, 369–374.
756 Thomas, J.B., Watson, E.B., Spear, F.S., Shemella, P.T., Nayak, S.K., and Lanzirotti, A. (2010)
757   TitaniQ under pressure: the effect of pressure and temperature on the solubility of Ti in
758   quartz. Contributions to Mineralogy and Petrology, 160, 743–759.
759 Till, C.B., Vasqez, J.A. and Boyce, J.W. (2015) Months between rejuvenation and volcanic
760   eruption at Yellowstone caldera, Wyoming. Geology, 43, 695–698.
761 Torres, R.C., Self, S. and Martinez, M.M.L. (1996) Secondary pyroclastic flows from the June
762   15, 1991, ignimbrite of Mount Pinatubo. In C.G. Newhall, R.S. Punongbayan, eds., Fire and
763   Mud: eruptions and lahars of Mount Pinatubo, Philippines. Philippine Institute of
764   Volcanology and Seismology and University of Washington Press, pp. 665–678.
765 Trial, A.F., Spera, F.J., Greer, J. and Yuen, D.A. (1992) Simulations of magma withdrawal from
766   compositionally zoned bodies. Journal of Geophysical Research, 97, 6713–6733.

767   Tuttle, O.F. and Bowen, N.L. (1958) Origin of granite in the light of experimental studies in the

768   system $NaAlSi_3O_8$-$KAlSi_3O_8$-SiO_2-H_2O. Geological Society of America Memoir, 74, 153 pp.

769   Wark, D.A. and Watson, E.B. (2006) TitaniQ: a titanium-in-quartz geothermometer.

770   Contributions to Mineralogy and Petrology, 152, 743–754.

771   Wark, D.A., Hildreth, W., Spear, F.S., Cherniak, D.J., and Watson, E.B. (2007) Pre-eruption

772   recharge of the Bishop magma system. Geology, 35, 235–238.

773   Warren, R.G., Goff, F., Kluk, E.C., and Budahn, J.R. (2007) Petrography, chemistry, and mineral

774   compositions for subunits of the Tshirege Member, Bandelier Tuff, within the Valles caldera

775   and Pajarito Plateau: New Mexico Geological Society, 58th Field Conference Guidebook,

776   316–332.

777   Warshaw, C.M. and Smith, R.L. (1988) Pyroxenes and fayalites in the Bandelier Tuff, New

778   Mexico: temperatures and comparison with other rhyolites. American Mineralogist, 73,

779   1025–1037.

780   Wilcock, J., Goff, F., Minarik, W.G., and Stix, J. (2013) Magmatic rewcharge during the

781   formation and resurgence of the Valles calderam New Mexico, USA: evidence from quartz

782   compositional zoning and geothermometry. Journal of Petrology, 54, 635–664.

783   Wilson, C.J.N., Seward, T.M., Allan, A.S.R., Charlier, B.L.A. and Bello, L. (2012) A comment

784   on: 'TitaniQ under pressure: the effect of pressure and temperature on the siolubility of Ti in

785   quartz', by Jay B. Thomas, E. Bruce Watson, Frank S. Spear, Philip Shemella, Saroj K.

786   Nayak and Antonio Lanzirotti. Contributions to Mineralogy and Petrology, 164, 359–368.

787   Wolff, J.A. and Ramos, F.C. (2014) Processes in caldera-forming high-silica rhyolite magma:

788   Rb-Sr and Pb isotope systematics of the Otowi Member of the Bandelier Tuff, Valles

789   Caldera, New Mexico, USA. Journal of Petrology, 55, 345–375.

790   Wolff, J.A., Ellis, B.S., Ramos, F.C., Starkel, W.A., Boroughs, S., Olin, P.H. and Bachmann, O.

791   (2015) Remelting of cumulates as a process for producing chemical zoing in silicic tuffs: a

792   comparison of cool, wet and hot, dry rhyolitic magma systems. Lithos, 236–237, 275–286.

793   Wolff, J.A., Forni, F., Ellis, B.S. and Szymanowski, D. (2020) Europium and barium

794   enrichments in compostionally zoned felsic tuffs: A smoking gun for the origin of chemical

795   and physical gradients by cumulate melting. Earth and Planetary Science Letters 540:116251,

796   12 pp.

797

798   **FIGURE CAPTIONS**

799   **FIGURE 1.** Cathodoluminescence grayscale images of representative quartz crystals from four

800   different samples of the Tshirege Member, Bandelier Tuff, arranged in stratigraphic order. Note

801   increasing complexity of CL-zoning upwards through the Tshirege Member. Crystallized melt

802   inclusions appear bright; glassy inclusions are near-black.

803   **FIGURE 2.** Concentrations of Th and Nb in whole pumices plotted for the Tshirege Member.

804   Notice the bimodal distribution of the high-silica rhyolite magmas, allowing distinction of three

805   magma types (enriched high-silica rhyolite, HSR-e; depleted high-silica rhyolite HSR-d, and

806   low-silica rhyolite, LSR; see also Table 4).

807   **FIGURE 3.** Trace element variations among Tshirege glasses; EG = external glass, MI = melt

808   inclusion. **a.** Th vs. Nb; **b.** La vs. Hf; **c.** Hf/La vs Rb. **d.** Rb/Sr vs Ba/La, with faceted inclusions

809   identified – see text.

810   **FIGURE 4.** **a.** Faceting strength (FS) vs Ba concentration; explanation of FS given in text. **b.**

811   Crystal containing melt inclusions with FS = 0 and 0.5. **c.** FS = 1 and 1.5. **d.** FS = 2. Note that

812   not all crystals exhibit all FS values. **e.** Sketch comparison of FS categories and qualifications for

813   any given FS value.

814   **FIGURE 5.** Back-scatter electron image of a quartz crystal from HSR-d pumice hosting four

815   melt inclusions (light gray). White numbers indicate FS rating; each inclusion is labeled with Ba

816   and Sr concentrations. Gray dashed line shows interpreted original crystal boundary, before

817   regrowth event. Note elevated Ba and Sr in the low FS inclusions in the interpreted rim. This

818   crystal has no CL zoning.

819   **FIGURE 6.** Titanium concentration and CL grayscale intensity profiles of four representative

820   quartz crystals from the Tshirege (158-3, 88-1, 151-3, and 90-1) with modeled diffusion curves

821   ([Ti]: solid black lines; CL: dashed grey lines), calculated from eqns. (4) – (6). Error bars for [Ti]

822   points are smaller than symbol size. Transect data are cropped to the diffusional relaxation zone;

823   full transects can be found in supplementary data. CL grayscale images and transect locations are

824   included for each sample *OC = oblique corrected transect; explanation in supplementary data

825   file. C = diffusion times calculated using D_{Ti} from Cherniak et al. (2007); J = diffusion times

826   calculated using D_{Ti} from Jollands et al. (2020).

827

828   **FIGURE 7.** A simplified four stage model showing the development of the CL zoning and melt

829   inclusion chemistry for the Tshirege magmas. **a.** Initial stage: accumulation of crystals, some

830   with melt inclusions depleted in compatible trace elements. **b.** Mature high-crystallinity mush;

831   ongoing faceting of melt inclusions on a ~1,000-10,000 year timescale. **c.** More primitive

832   magma starts to recharge the system with heating and possible release of volatiles, causing

833   resorption of quartz and feldspar. **d.** Quartz grows at higher temperatures trapping melt

834   inclusions with higher concentrations of compatible trace elements (i.e., Ba and Sr). Eventually,

835   the system overpressurizes to the point of eruption.

836

837   **TABLES**

838   **Table 1.** LA-ICP-MS and EPMA data for selected samples.

839   **Table 2.** Data from diffusion modeling results and titanium in quartz thermometry results using

840   D_{Ti} from Cherniak et al. (2007) "Nb (ppm)" is the concentration of Nb in the host pumice.

841   **Table 3.** Data from diffusion modeling results and titanium in quartz thermometry results using

842   D_{Ti} from Jollands et al. (2020).

843   **Table 4.** XRF analyses of whole pumice clasts from which quartz crystals were sampled and

844   analyzed (Table 2). Sample 9 is from the Tsankawi Pumice and quartz-glass data from this

845   sample were used to calibrate a_{TiO_2} for TitaniQ.

Table 1: LA-ICPMS vs WDS-EMPA for [Ti] in quartz

Sample:	LA-ICPMS (ppm)		WDS average (ppm)	
Cores:				
158-3	26.8	± 1.3	24.7	± 1.5
151-1	28.7	± 2.5	29.5	± 1.0
104-5	30.8	± 2.4	32.7	± 1.1
151-3	35.8	± 2.8	34.5	± 0.9
Rims:				
158-3	44.4	± 2.2	42.4	± 1.1
151-1	44.7	± 3.1	48.4	± 0.7
104-5	48.2	± 2.8	51.1	± 1.7
151-3	45.7	± 3.6	46.3	± 1.3

Errors reported in 1σ

Table 2: Diffusion Modeling Results

Sample	CL Model time			[Ti] model time			Model times a(TiO$_2$)			Model times γ(TiO$_2$)			Nb (ppm)
	time (years)	error[a]		time (years)	error[a]		time (years)	error[b]	T used (°C)	time (years)	error[b]	T used (°C)	
Tshirege													
88-1	2060	+824	-1236	10400	+4160	-6000	980	± 95	825	2200	± 275	799	37
151-3[c]	520	+208	-312	<520	+208	-312	<525	± 90	748	<780	± 140	727	64
151-1[c]	300	+120	-180	920	+368	-552	930	± 180	748	2300	±300	727	64
104-4-2	180	+72	-108	240	+96	-144	<155	± 60	778	<490	± 220	731	65
104-5-1	160	+64	-96	<190	+76	-114	<185	± 80	752	<780	± 600	703	65
104-5-2	—	—	—	<270	+108	-162	<265	± 120	752	<900	± 600	703	65
141-1-1	400	+160	-240	2000	+800	-1200	1150	± 250	786	2000	± 550	748	68
141-2-1	—	—	—	<400	+160	-240	<150	± 60	786	<300	± 100	758	68
141-2-2	120	+48	-72	<180	+72	-108	<90	± 60	786	<160	± 90	758	68
119-3	600	+240	-360	900	+360	-560	250	±40	783	480	± 90	762	69
119-4-OC	—	—	—	150	+60	-90	60	±15	783	105	± 20	762	69
158-3	120	+48	-72	1200	+480	-180	610	± 120	778	2300	± 300	724	68
90-1	55	+22	-33	<280	+120	-45	<140	± 40	773	<265	± 55	753	73
90-1-OC	—	—	—	210	+88	-132	115	± 20	773	170	± 25	753	73
90-3	100	+40	-60	<1100	+440	-660	<650	± 105	783	<1050	± 215	753	73
90-3-OC	—	—	—	180	+72	-108	150	± 20	783	175	± 15	753	73
90-4	640	+248	-372	800	+96	-36	410	± 75	775	980	± 115	742	73

First two columns are calculated using 750°C to allow for comparison of the two profiles.
[a]Errors arising from the error on the diffusion coefficient (Cherniak et al., 2007), calculated at a fixed T = 750 °C.
[b]Errors from fitting diffusion sigmoid to data; errors from uncertainty of diffusion coefficient not included.
[c]No glass Ti contents measured; average Tshirege glass Ti concentration used for temperature estimation.
OC = oblique corrected transect. See supplemental data for explanation of oblique correction

Table 3: Diffusion modeling results

Sample	Model times a(TiO$_2$)			Model times γ(TiO$_2$)		
	Model Time (years)	error	T used (°C)	Model Time (years)	error	T used (°C)
88-1	1.1E+06	± 9.9E+03	825	5.65E+06	± 8.5E+04	799
151-3	<3.1E+05	± 9.9E+03	748	<6.95E+05	± 2.2E+04	727
151-1	9.9E+05	± 8.9E+03	748	6.18E+06	± 1.0E+05	727
104-4-2	<2.66E+04	± 3.6E+04	778	<2.72E+05	± 5.4E+04	731
104-5-1	<3.80E+04	± 3.9E+03	752	6.95E+05	± 4.1E+05	703
104-5-2	<7.85E+04	± 7.0E+03	752	<9.28E+05	± 4.1E+05	703
141-1-1	1.52E+06	± 1.6E+04	786	4.66E+06	± 3.4E+05	748
141-2-1	<2.49E+04	± 7.0E+04	786	<1.01E+05	± 1.1E+04	758
141-2-2	<8.86E+03	± 3.9E+03	786	<2.83E+04	± 8.9E+03	758
119-3	6.98E+04	± 3.9E+03	783	2.61E+05	± 8.9E+03	762
119-4-OC	3.91E+03	± 7.3E+02	783	1.21E+04	± 4.2E+02	762
158-3	4.23E+05	± 2.4E+02	778	6.18E+06	± 1.0E+05	724
90-1	<2.16E+04	± 1.6E+04	773	<7.85E+04	± 3.3E+03	753
90-1-OC	1.45E+04	± 1.7E+03	773	3.20E+04	± 6.7E+02	753
90-3	<4.81E+05	± 4.2E+02	783	<1.27E+06	± 1.0E+05	753
90-3-OC	2.48E+05	± 2.2E+03	783	3.40E+05	± 2.4E+02	753
90-4	1.90E+05	± 4.2E+02	775	1.10E+06	± 2.4E+02	742

Diffusional relaxation times calculated using D$_{Ti}$ of Jollands et al. (2020).
Errors listed are from fitting of the diffusion sigmoid to data.

Table 4: Whole Pumice Analyses

Major and minor elements (wt%)

Sample	88	90	104	119	141	151	158	9
SiO_2	69.58	78.57	74.69	78.44	78.96	79.07	79.82	75.70
TiO_2	0.42	0.08	0.08	0.07	0.08	0.07	0.09	0.09
Al_2O_3	15.87	12.21	11.83	11.70	11.40	11.45	11.44	13.53
FeO*	3.30	1.36	1.33	1.19	1.26	1.18	1.38	1.85
MnO	0.06	0.05	0.04	0.05	0.05	0.05	0.05	0.09
MgO	0.98	0.01	0.15	0.13	0.05	0.16	0.02	0.11
CaO	2.44	0.37	1.23	0.77	0.41	0.70	0.26	0.36
Na_2O	3.59	2.67	3.18	2.90	2.96	2.87	2.58	3.07
K_2O	3.64	4.67	7.43	4.71	4.82	4.43	4.34	5.18
P_2O_5	0.13	0.01	0.03	0.04	0.02	0.03	0.02	0.02
Trace elements (ppm)								
Zn	109	77	74	74	73	76	72	152
Ga	24	24	21	22	22	22	22	29
Rb	112	158	133	151	147	142	144	273
Sr	323	9	40	19	21	28	7	30
Y	53	72	91	65	70	60	58	183
Zr	268	213	198	204	213	199	223	289
Nb	37	73	65	69	68	64	68	153
Ba	559	93	70	67	49	52	52	64
La	63	69	62	61	69	63	62	67
Ce	101	118	112	112	117	118	118	120
Nd	46	53	53	49	49	48	45	54
Pb	463	43	111	28	50	38	92	63
Th	15	22	20	22	21	20	22	38

[a]FeO = Fe_{Total}
Major oxides normalized to a volatile-free basis
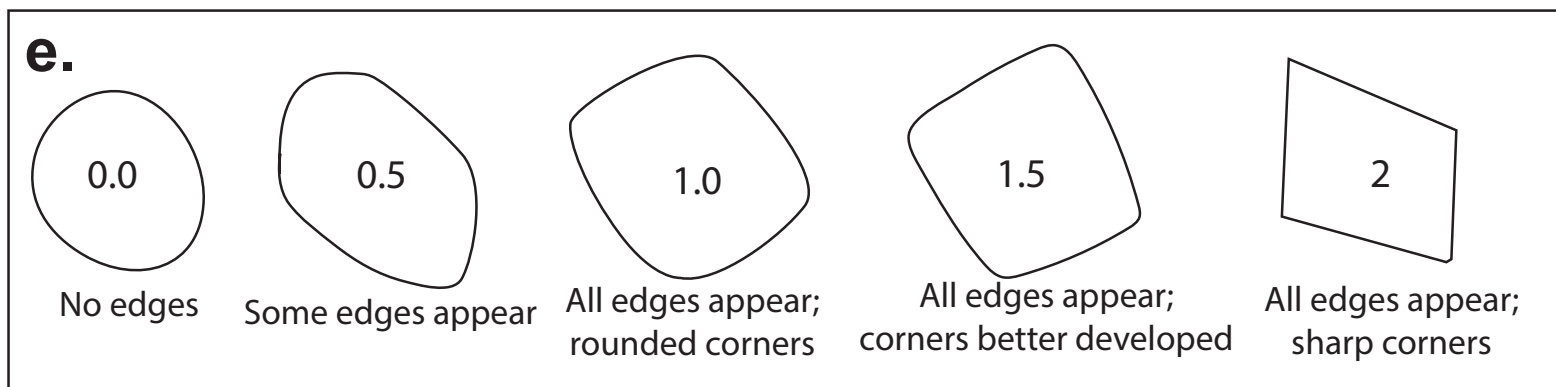
Relative stratigraphic position

1.
400 μm

2.
400 μm

3.
400 μm

4.
400 μm

5.
400 μm

6.
400 μm

7.
400 μm

8.
400 μm

9.
400 μm

10.
400 μm

11.
400 μm

12.
400 μm
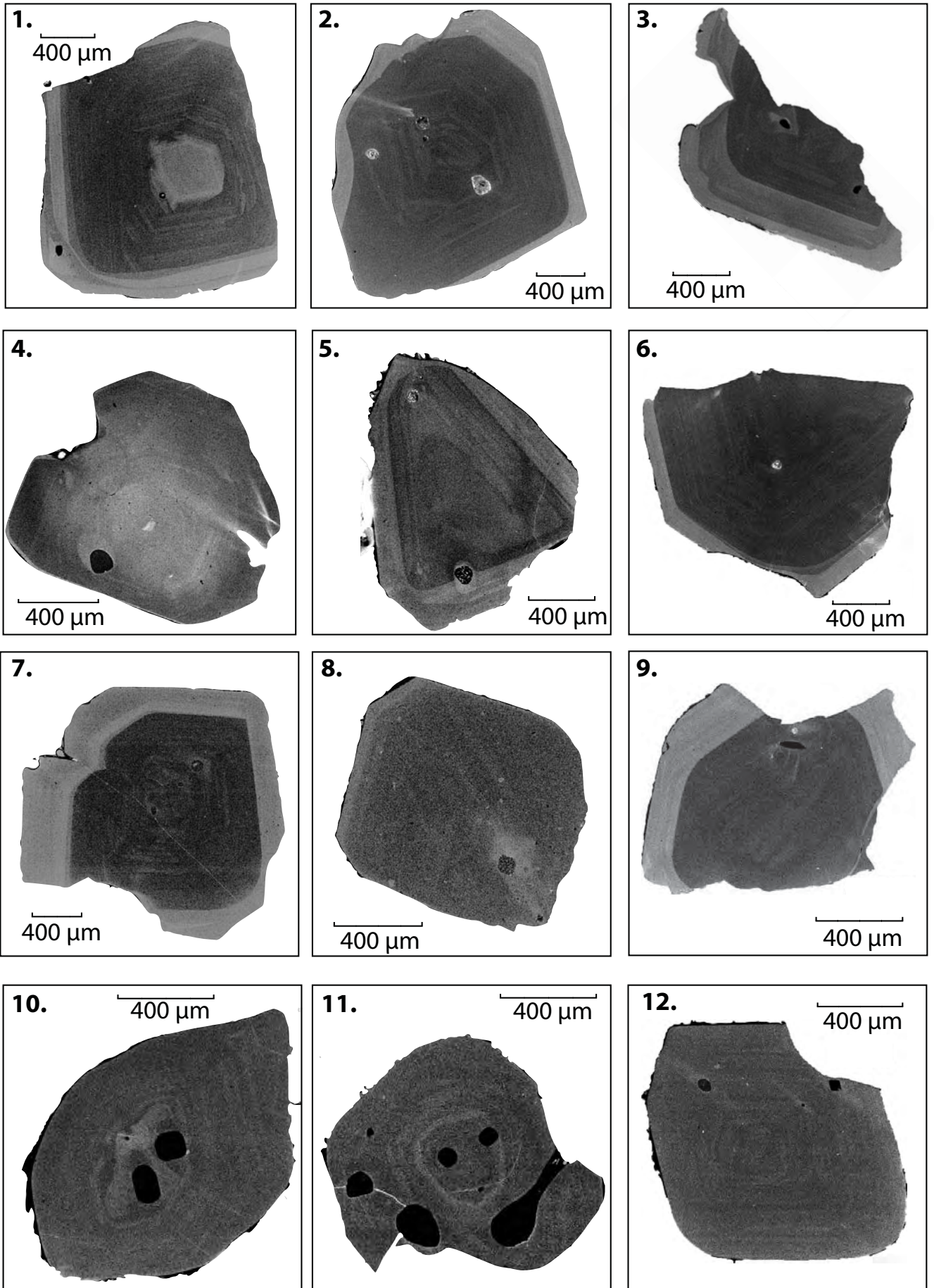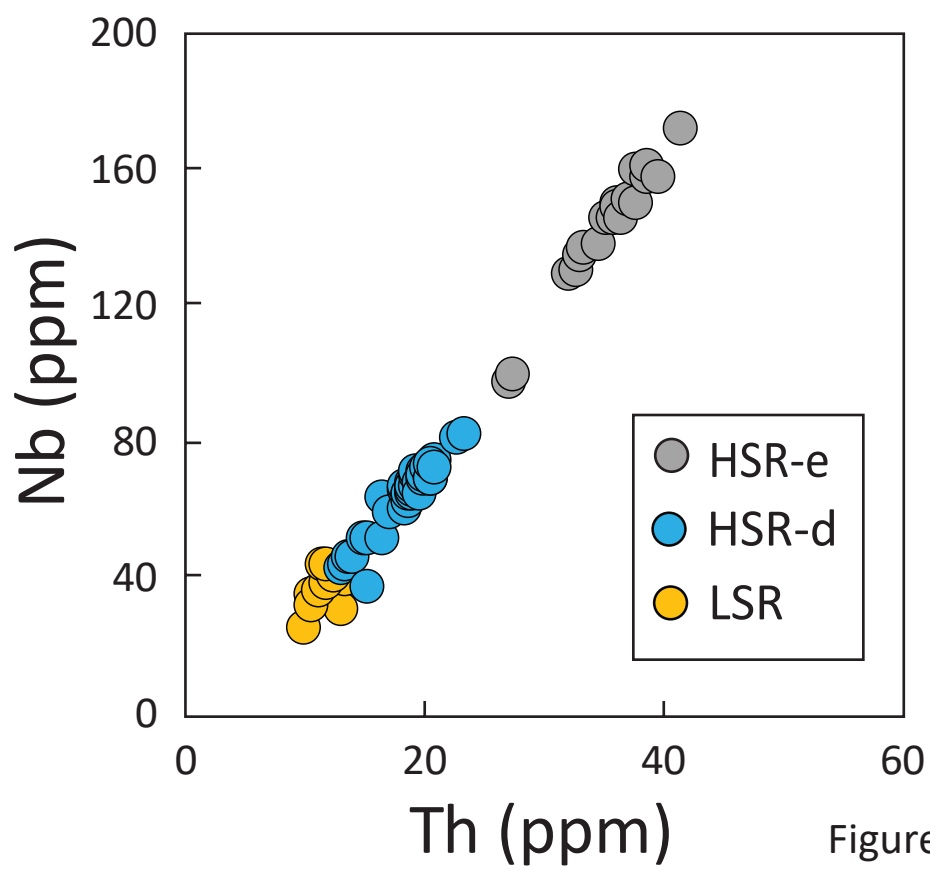
Figure 1

Figure 2

Figure 3

Figure 4

a. Quartz-hosted Melt Inclusions

HSR-e
HSR-d
LSR

Ba (ppm)

Facet strength

b.

0.5   0

a.

500 μm

c.

1.5
1

d.

2

e.

0.0
No edges

0.5
Some edges appear

1.0
All edges appear;
rounded corners

1.5
All edges appear;
corners better developed

2
All edges appear;
sharp corners

Ba = 3.2 ppm
Sr = 0.74 ppm

Ba = 2.8 ppm
Sr = 0.69 ppm

Ba = 68 ppm
Sr = 19 ppm

1.5

0.5

1

0

Ba = 66 ppm
Sr = 18 ppm

500 μm

Figure 5

Figure 6

T= 750 °C ● = [Ti]

[Ti] model time
C 1.2E3 ± 1.5E1 y
J 1.6E6 ± 3.9E3 y

T= 750 °C
C 1.0E3 ± 1.0E2 y
J 1.2E6 ± 3.1E5 y

T= 750 °C
C 5.2E2 ± 9.0E1 y
J 3.2E5 ± 7.4E4 y

T= 750 °C   OC*
bump
dip
C 2.1E3 ± 1.5E1 y
J 5.1E6 ± 1.3E6 y

[Ti] (ppm)

× = CL (raw)
○ = CL (avg.)

CL model time
C1.2E2 ± 2.5E1 y
J 1.7E4 ±3.9E3 y

C 5.2E2 ± 5.0E1 y
J 3.0E5 ± 7.5E4 y

C 5.2E2 ± 7.5E1 y
J 3.2E5 ± 1.0E4 y

C 5.5E1 ± 1.5E1 y
J 3.3E3 ± 8.2E2 y

CL Greyscale (out of 255)

Relative distance (µm)

CL Photos of samples from above

Transect line
400 µm
158-3

Transect line
400 µm
88-1

Transect line
400 µm
151-3

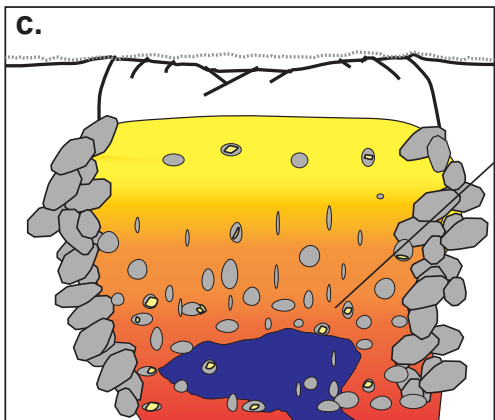Transect line
400 µm
90-1

a. T = 0

Melt inclusion trapped
during fractionation

Fractional Crystalization

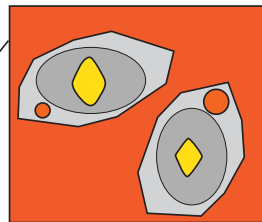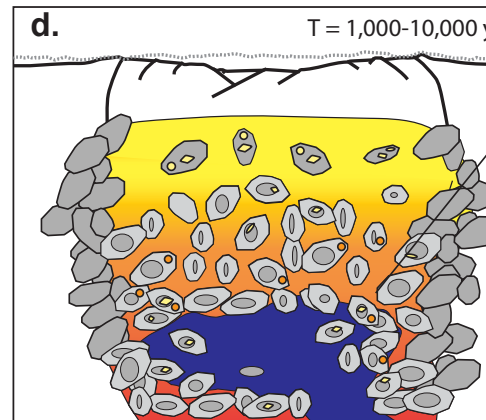**b.**
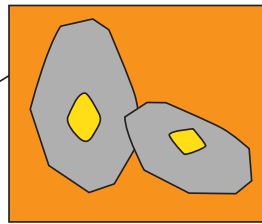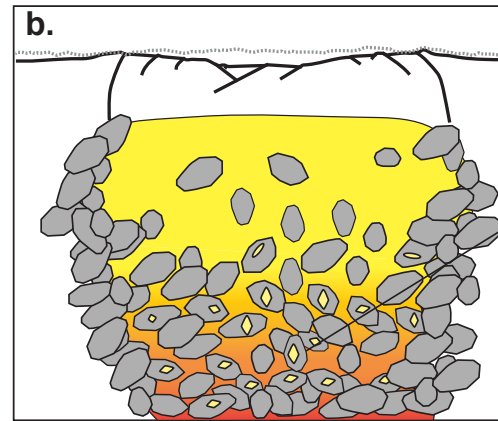
Inclusions become faceted
during storage.

Storage

c.
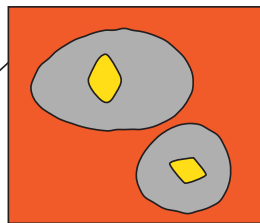
Crystals resorb during
recharge event

Recharge

For simplicity, this diagram only draws quartz phenocrysts; crystals not to scale.

d. T = 1,000-10,000 y

Unfaceted inclusions become
trapped during regrowth of
CL-bright rims; diffusion starts.

Regrowth and diffusional relaxation

Figure 7