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Experimental Determination of Solubility Constant of Kurnakovite, $MgB_3O_3(OH)_5 \bullet 5H_2O$

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ABSTRACT

In this study, I present experimental results on the equilibrium between boracite [$Mg_3B_7O_{13}Cl$(cr)] and kurnakovite [chemical formula, $Mg_2B_6O_{11}$•$15H_2O$(cr); structural formula, $MgB_3O_3(OH)_5$•$5H_2O$(cr);] at 22.5 ± 0.5°C from a long-term experiment up to 1,629 days, approaching equilibrium from the direction of supersaturation,

$$Mg_3B_7O_{13}Cl(cr) + H^+ + 2B(OH)_4^- + 18H_2O(l) \rightleftharpoons 3MgB_3O_3(OH)_5•5H_2O(cr) + Cl^-$$

Based on solubility measurements, the 10-based logarithm of the equilibrium constant for the above reaction at 25°C is determined to be 12.83 ± 0.08 (2σ).

Based on the equilibrium constant for dissolution of boracite,

$$Mg_3B_7O_{13}Cl(cr) + 15H_2O(l) = 3Mg^{2+} + 7B(OH)_4^- + Cl^- + 2H^+$$

at 25°C measured previously (Xiong et al., 2018) and that for the reaction between boracite and kurnakovite determined here, the equilibrium constant for dissolution of kurnakovite,

$$MgB_3O_3(OH)_5•5H_2O(cr) = Mg^{2+} + 3B(OH)_4^- + H^+ + H_2O(l)$$

is derived as -14.11 ± 0.40 (2σ).

Using the equilibrium constant for dissolution of kurnakovite obtained in this study and the experimental enthalpy of formation for kurnakovite from the literature, a set of thermodynamic properties for kurnakovite at 25°C and 1 bar is recommended as follows: $\Delta H_f^0 = -4813.24 \pm 4.92$ kJ•mol^{-1}, $\Delta G_f^0 = -4232.0 \pm 2.3$ kJ•mol^{-1}, and $S^0 = 414.3 \pm 0.9$ J•mol^{-1}•K^{-1}. Among them, the Gibbs energy of formation is based on the equilibrium constant for kurnakovite determined in this study; the enthalpy of formation is from the literature, and the standard entropy is calculated internally with the Gibbs-Helmholtz equation in this work. The thermodynamic properties of kurnakovite estimated using the group contribution method for borate minerals based on the sum of contributions from the cations, the borate polyanions, and the structural water to the thermodynamic properties from the literature, are consistent, within its uncertainty, with the values listed above.

Since kurnakovite usually forms in salt lakes rich in sulfate, studying the interactions of borate with sulfate is important to modeling kurnakovite in salt lakes. For this purpose, I have re-calibrated our previous model (Xiong et al., 2013) describing the interactions of borate with sulfate based on the new solubility data for borate in Na_2SO_4 solutions presented here.

INTRODUCTION

Kurnakovite, which has a structural formula of $MgB_3O_3(OH)_5$•$5H_2O$(cr)("cr" refers to "crystalline", thereafter), is a magnesium borate mineral of triclinic symmetry in the space group of $P\bar{1}$. In kurnakovite, there are the following structural units: triangularly-coordinated [BO_2(OH)]-groups, tetrahedrally-coordinated [$BO_2(OH)_2$]-

55 groups, and $Mg(OH)_2(H_2O)_4$ octahedra, connected into neutral $Mg(H_2O)_4B_3O_3(OH)_5$
56 units forming chains along the [001] direction (Gatta et al., 2019). The mineral that has
57 the same chemical composition but is of monoclinic symmetry is called inderite.
58 Kurnakovite was discovered by Godlevsky (1940) in the borate deposits of west
59 Kazakhstan. Rumanova and Ashirov (1964) determined its densities and refractive
60 indices. Then, Yeh (1965) did some crystal structure determinations for kurnakovite.
61 Razmanova et al. (1970) solved its structure, and Corazza (1974) made a refinement for
62 the structure. Zhou et al. (2012a) refined the hydrogen positions using nuclear magnetic
63 resonance (NMR). Most recently, Gatta et al. (2019) studied the crystal structure and
64 chemistry of a natural kurnakovite from Kramer Deposit, California, using single-crystal
65 neutron diffraction. Kurnakovite was synthesized by Spiryagina (1949) and Yuan et al.
66 (1983). Heinrich (1946) also synthesized kurnakovite, corresponding to the occurrence
67 in USA, but it seems that he mislabeled it as inderite, as Frondel et al. (1956) did
68 (Schaller and Mrose, 1960) (see below).
69 The currently available thermodynamic properties of kurnakovite are inconsistent.
70 Li et al. (1997) measured its enthalpy of formation, and Li et al. (2000) estimated its
71 Gibbs energy of formation as -4249.79 $kJ \cdot mol^{-1}$. By contrast, Anovitz and Hemingway
72 (2002) estimated its Gibbs energy of formation as -4272 $kJ \cdot mol^{-1}$, differing the estimated
73 value from Li et al. (2000) by ~23 $kJ \cdot mol^{-1}$. Therefore, its Gibbs free energy of
74 formation is not well known, leading to the inexact knowledge of its solubility constant.
75 In this work, the solubility constant of kurnakovite is determined to provide a set of its
76 thermodynamic properties.

Given the occurrence of kurnakovite in sulfate-enriched salt lakes in nature, Xiong et al. (2013) developed a model to describe the interactions between sulfate and borate based on literature data on the solubility of sodium tetraborate (borax) in Na_2SO_4 solutions without any pH measurements. In the present work, the previous model has been recalibrated to describe the important interactions between sulfate and borate for modeling the formation of kurnakovite in sulfate-enriched salt lakes in nature, based on our own borax solubility data together with pH measurements in Na_2SO_4 solutions up to 1.8 mol•kg^{-1}.

OCCURRENCE OF KURNAKOVITE

Kurnakovite has been reported from about 12 localities worldwide, including the type locality in the gypsum cap of the Inder salt dome, Kazakhstan. In USA, it is present in the Jennifer Mine of the Kramer borate deposit, Kern County (Frondel et al., 1956; Schaller and Mrose, 1960; Pemberton, 1983) (however, Frondel et al. mislabeled kurnakovite as inderite, according to Schaller and Mrose, 1960 and Baysal, 1973), and in the Furnace Creek district, Inyo County (Erd et al., 1970), California. In Turkey, it is present in the Kirka borate deposit (Baysal, 1973; Inan et al., 1973; Helvaci, 1978). In China, it occurs in Da Qaidam Lake and Xiao Qaidam Lake (Qian and Xuan, 1985; Zheng et al., 2005; Li et al., 2012; Li et al., 2013), the Yashatu deposit (Jiang et al., 1996), Qinghai Province; in Zhacang Chaka Salt Lake (Zheng and Liu, 1982; Yang and Zheng, 1985), Nie'er Cuo Salt Lake (Yang and Zheng, 1985; Liu and Zheng, 2010), Chala Ka Salt Lake (Yang and Zheng, 1985), Qag Caca Salt Lake (Yang, 1991), and Jibu

Salt Lake (Li et al., 2004), Xizang (Tibet) Autonomous Region. In Argentina, it occurs in the Tincalayu borax mine, Salta (Hurlbut and Erd, 1974).

At several of these localities, kurnakovite commonly forms in current salt lakes that are rich in sulfate (Sun et al., 1984; Yang, 1989; Yuan et al., 1993; Liu et al., 2003; Zheng and Liu, 2009), and formed in ancient or extinct salt lakes that were also rich in sulfate such as those Neogene salt lakes in the western Turkey (Kistler and Helvacı, 1994) and those Miocene-Pliocene salt lakes in the Death Valley, California, USA (Erd et al., 1970; Tanner, 2002), as evidenced by the occurrence of both kurnakovite and gypsum in those Neogene and Miocene-Pliocene deposits such as the Kirka borate deposit (Helvaci et al, 1993) and the borate deposits in the Furnace Creek Formation in the Death Valley (Erd et al., 1970; Tanner, 2002).

PRACTICAL APPLICATIONS OF KURNAKOVITE

Kurnakovite has several practical applications. In the oil and gas industry, kurnakovite is one of the borate minerals used in the hydrofracturing fluids as cross-linkers for extraction of shale gas (Dobson et al., 2005). This usage is based on the fact that kurnakovite is a sparingly soluble borate mineral. Kurnakovite is used for neutron shielding (Senberber et al., 2017; Gatta et al., 2019), as kurnakovite has the lowest neutron radiation permeability among the common borate minerals (Derun and Kipcak, 2011). Kurnakovite also has interesting luminescence properties with its excitation spectrum at 360 nm and emission spectrum at 420 nm (Yuan et al., 1993). In the field of nuclear waste management, sparingly soluble borate minerals may impact the near-field chemistry of geological repositories, because sparingly soluble borate minerals may have

an impact on aqueous geochemistry of near-field environments as solubility-controlling phase(s) for borate in geological repositories. This is especially true with geological repositories in salt formations. Salt formations are considered to be ideal for nuclear waste isolation (National Academy of Science's Committee on Waste Disposal, 1957), and there are relatively high concentrations of borate present in brines associated with salt formations (e.g., up to 0.18 mol•kg^{-1}, Xiong and Lord, 2008). As borate could potentially form an aqueous complex with Am(III) (Borkowski et al., 2010; Xiong, 2017), the formation of sparingly soluble borate minerals in the near-field of a geological repository could keep borate concentrations low, minimizing the contributions of the aqueous Am(III)-borate complex to the solubility of Am(III).

EXPERIMENTAL METHODS

Solubility measurements were performed from the direction of supersaturation, similar to the approach we used before for the determination of solubility constants of boracite [$Mg_3B_7O_{13}Cl$(cr)] and aksaite [$MgB_6O_7(OH)_6$•$2H_2O$(cr)] (Xiong et al., 2018). The experimental products were not sampled until after the experiment had run for at least 957 days. All chemicals used in our experiment were ACS reagent grade. The solutions used in the experiments were prepared from the degassed deionized (DI) water with resistivity ≥ 18.2 megohm in which any dissolved CO_2 was removed, according to the procedure of Wood et al. (2002).

Our experiments with regard to solubility measurements for borax in Na_2SO_4 solutions from undersaturation are similar to our previous work in NaCl solutions (Xiong et al., 2013).

146 The pH readings were measured with an Orion-Ross combination pH glass
147 electrode, coupled with an Orion Research EA 940 pH meter that was calibrated with
148 three pH buffers (pH values: 4, 7, and 10). Negative logarithms of hydrogen-ion
149 concentrations on molar scale (pcH) were determined from pH readings by using
150 correction factors (Hansen, 2001). Based on the equation in Xiong et al. (2010), pcHs are
151 converted to negative logarithms of hydrogen-ion concentrations on molal scale, pH_m, a
152 notation from Oak Ridge National Laboratory/University of Idaho (e.g., Wood et al.,
153 2002).

154 Solution samples were periodically withdrawn from experimental runs. Before
155 solution samples were taken, pH readings of experimental runs were first measured. The
156 sample size was usually 3 mL. After a solution sample was withdrawn from an
157 experiment and filtered with a 0.2 μm syringe filter, the filtered solution was then
158 weighed, acidified with 0.5 mL of concentrated TraceMetal® grade HNO_3 from Fisher
159 Scientific, and finally diluted to a volume of 10 mL with DI water. If subsequent
160 dilutions were needed, aliquots were taken from the first dilution samples for the second
161 dilution, and aliquots of the second dilution were then taken for the further dilution.

162 Boron, sodium and magnesium concentrations of solutions were analyzed with a
163 Perkin Elmer dual-view inductively coupled plasma-atomic emission spectrometer (ICP-
164 AES) (Perkin Elmer DV 8300). Calibration blanks and standards were precisely matched
165 with experimental matrices. The linear correlation coefficients of calibration curves in all
166 measurements were better than 0.9995. The analytical precision for ICP-AES is better
167 than 1.00% in terms of the relative standard deviation (RSD) based on replicate analyses.

Chloride concentrations were analyzed with a DIONEX ion chromatograph (IC) (DIONEX IC 3000).

The solid phase identification was performed using a Bruker AXS, Inc., D8 Advance X-ray diffractometer (XRD) with a Sol-X detector. XRD patterns were collected using CuKα radiation at a scanning rate of 1.33^{o}/min for a 2θ range of 10–90^{o}.

EXPERIMENTAL RESULTS

Figure 1 shows the XRD patterns of solid phases from my supersaturation experiment with an initial concentration of 1.0 mol•kg^{-1} $MgCl_2$ solution. Figure 1 shows that kurnakovite along with boracite and aksaite crystallized from the solution. Notice that the peaks characteristic of kurnakovite and boracite, are present in the XRD patterns (Figure 1). In our previous work, we determined the thermodynamic properties of boracite and aksaite (Xiong et al., 2018).

Experimental results from the direction of precipitation of kurnakovite are tabulated in Table 1. In Figure 2, total boron, chloride, magnesium and sodium concentrations as a function of experimental time are displayed. As shown in Figure 2, the equilibrium was established after about 900 days. The duration of the experiment was up to 1,642 days (Table 1, Figure 2).

In Table 2, solubility data of borax in Na_2SO_4 solutions at 25 ^{o}C are presented. The experimental time was up to 762 days. The experimental duration for these experiments is similar to that for our previous solubility measurements of borax in NaCl solutions, which was 567 days (Xiong et al., 2013), and to that for our previous solubility

191 study of borax in a 0.01 mol•kg^{-1} $MgCl_2$ solutions (Xiong et al., 2017). In our previous
192 studies, we demonstrated that the equilibrium for solubility of borax was attained after
193 ~130 days. Therefore, based on our previous studies, it is assumed that the equilibrium
194 was attained for solubility of borax in Na_2SO_4 solutions in this study.
195
196 THERMODYNAMIC CALCULATIONS AND DISCUSSION
197
198 In our previous work, we determined the thermodynamic properties of boracite
199 and aksaite (Xiong et al., 2018).
200 The equilibrium between boracite and kurnakovite can be represented by the
201 following reactions,
202
203 $Mg_3B_7O_{13}Cl(cr) + H^+ + 2B(OH)_4^- + 18H_2O(l) \rightleftharpoons 3MgB_3O_3(OH)_5 \bullet 5H_2O(cr) + Cl^-$ (1)
204
205 Regarding Reaction (1), its equilibrium constant at infinite dilution can be
206 expressed as follows,
207
208 $$K_1^0 = \frac{(a_{Cl^-})}{(a_{H^+}) \times (a_{B(OH)_4^-})^2 \times (a_{H_2O})^{18}} \quad (2)$$
209
210 In Equation (1), a_i is an activity of the i-th species calculated with a thermodynamic
211 model; a_{H_2O} is the activity of water.

Activities of $B(OH)_4^-$, Cl^-, H^+ and water in the experimental system are calculated using the computer code EQ3/6 Version 8.0a (Wolery et al., 2010; Xiong, 2011a). The database used for calculations was DATA0.FM2 (Domski, 2015; Xiong and Domski, 2016).

Based on the activities calculated using EQ3/6 Version 8.0a, the $\log_{10} K_1^0$ at infinite dilution is calculated in accordance with Equation (2) (Table 3). The equilibrium constant for $\log_{10} K_1^0$ obtained in this study is 12.83 ± 0.08 (2σ).

The dissolution reaction for kurnakovite can be expressed as follows,

$$MgB_3O_3(OH)_5 \bullet 5H_2O(cr) = Mg^{2+} + 3B(OH)_4^- + H^+ + H_2O(l) \qquad (3)$$

The equilibrium constant for Reaction (3) can be derived from $\log_{10} K_1^0$ for Reaction (1) and $\log_{10} K_4^0$ for Reaction (4) regarding dissolution of boracite,

$$Mg_3B_7O_{13}Cl(cr) + 15H_2O(l) = 3Mg^{2+} + 7B(OH)_4^- + Cl^- + 2H^+ \qquad (4)$$

The equilibrium constant for Reaction (4) ($\log_{10} K_4^0$) has been determined as -29.50 ± 0.39 (2σ) by solubility measurements (Xiong et al., 2018). That value is in excellent agreement with a value calculated from the ΔG_f^0 for boracite from the literature (Khodakovsky, Semenov and Aksaenova, unpublished, see citation in Anovitz and Hemingway, 2002, and discussion in Xiong et al., 2018).

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According to $\log_{10} K_1^0$ for Reaction (1) determined in this study and $\log_{10} K_4^0$ for Reaction (4) from Xiong et al. (2018), the equilibrium constant for Reaction (3) ($\log_{10} K_3^0$) is derived as –14.11 ± 0.40 (2σ) (Table 3).

The equilibrium constant for kurnakovite determined by this study provides an opportunity in evaluating the Gibbs free energies of this phase from the estimates in the literature. In the group contribution method, the thermodynamic properties for a borate phase are sum of contributions from the cations in aqueous solution, the borate polyanions, and the structural water to the corresponding thermodynamic properties (Li et al., 2000). Li et al. (2000) calculated the ΔG_f^0 of kurnakovite as –4249.79 kJ•mol^{-1}, according to the group contribution method. Based on this value, $\log_{10} K_3^0$ for Reaction (3) is calculated to be –17.23 (Table 4). Anovitz and Hemingway (2002) estimated the ΔG_f^0 of kurnakovite as –4272 kJ•mol^{-1}, leading to a value of –21.16 for $\log_{10} K_3^0$ for Reaction (3) (Table 4). In comparison with the value determined in this study [–14.11 ± 0.40 (2σ)], the value (–17.23) calculated based on the group contribution method (Li et al., 2000) is off by about three orders of magnitude. This is reasonable considering the accuracy of the group contribution method in estimation of ΔH_f^0 and ΔG_f^0 (see below). In contrast, the value (–21.16) estimated from the method of Anovitz and Hemingway (2002) is off by about seven orders of magnitude. The estimation method of Anovitz and Hemingway (2002) is similar to the methods proposed by Robinson and Haas (1983) and Chermak and Rimstidt (1989) for silicate minerals. Therefore, the group contribution method of Li et al. (2000) performs better than the

254 estimation method of Anovitz and Hemingway (2002). This finding is similar to our
255 previous observation with regard to aksaite (Xiong et al., 2018).

256 According to $\log_{10} K_3^0$ for Reaction (3) from this work, the ΔG_f^0 for kurnakovite
257 is derived as –4231.95 ± 2.29 kJ•mol^{-1} (Table 5). Li et al. (2000) calculated the ΔG_f^0 for
258 kurnakovite as –4249.79 kJ•mol^{-1}, which deviates from my ΔG_f^0 by –17.84 kJ•mol^{-1},
259 indicating that the error associated with the calculation of Li et al. (2000) is 0.42% in
260 terms of ΔG_f^0. This error is within the error range, 0.01-0.60%, for the group
261 contribution method (Li et al., 2000). They also calculated the ΔH_f^0 of kurnakovite as
262 -4831.81 kJ•mol^{-1}. The experimentally determined ΔH_f^0 of kurnakovite is –4813.24
263 kJ•mol^{-1}. Therefore, the calculated ΔH_f^0 deviates from the experimental value by –18.57
264 kJ•mol^{-1}, almost identical to the difference between the calculated and experimental
265 ΔG_f^0's.

266 If we use the calculated values as the benchmarks, the above identical differences
267 in comparing the calculated and experimental values demonstrate that our experimentally
268 derived ΔG_f^0 is highly consistent with the experimental ΔH_f^0 from Li et al. (1997). To
269 state in a different way, the difference between the calculated ΔH_f^0 and ΔG_f^0 is –582.02
270 kJ•mol^{-1}. Interestingly, the difference between the experimental ΔH_f^0 of Li et al. (1997)
271 and my experimentally derived ΔG_f^0 is –581.29 kJ•mol^{-1}, which is almost identical to the
272 above difference for the calculated ΔH_f^0 and ΔG_f^0.

Regarding the entropy of kurnakovite, the value derived by this study from the experimental ΔG_f^0 and ΔH_f^0 is 414.31 J•mol^{-1}•K^{-1}, which carries an uncertainty of ~1 J•mol^{-1}•K^{-1}. The entropy calculated internally with the Gibbs-Helmholtz equation by this study based on the estimated ΔG_f^0 and ΔH_f^0 from Li et al. (2000) is 411.85 J•mol^{-1}•K^{-1}. As the calculated ΔG_f^0 and ΔH_f^0 from Li et al. (2000) do not have error estimates, there is no error estimate on the entropy calculated here. Taking into consideration the uncertainties associated with the experimentally-derived entropy, and with the estimated entropy, the difference between these two entropies would be similar to those between experimentally-derived and estimated ΔG_f^0, and between experimentally-derived and estimated ΔH_f^0, and be within the error range for the group contribution method (i.e., to 0.6%).

It is noted that Birsoy and Özbas (2012) used a value of –4366.90 kJ•mol^{-1} for the Gibbs free energy of formation for kurnakovite in their calculations of activity diagrams of borates. They cited Anovitz and Hemingway (2002) as the source. In fact, the primary source for that value is from Huang et al. (1988). However, the enthalpy value (–4856 kJ•mol^{-1}) measured by Huang et al. (1988) is more negative than the valued (-4813.24 kJ•mol^{-1}) determined by Li et al. (1997). In addition, the entropy value (361. 7 J•mol^{-1}•K^{-1}) obtained by Huang et al. (1988) seems too low in comparison with the recent values (e.g., 405 J•mol^{-1}•K^{-1} from Anovitz and Hemingway, 2002; and 414.31 J•mol^{-1}•K^{-1} from this work).

In natural salt lakes such as those in the Qinghai-Xizhang (Tibet) Plateau, China, kurnakovite occurs in those lakes which are rich in borate and sulfate. Therefore, the

295 interactions of borate with sulfate are important to modeling the formation of kurnakovite
296 in salt lakes in nature. In our previous work (Xiong et al., 2013), we developed a model
297 to describe the interactions between sulfate and borate based on the solubility data of
298 borax in Na_2SO_4 solutions from the literature. However, the solubility data from the
299 literature, used for development of our model, lacked pH measurements. In this work, we
300 re-calibrate our model based on our solubility measurements on borax in Na_2SO_4
301 solutions with pH_m measurements (Table 2).

302 The parameters for the re-calibrated model are tabulated in Table 6. As indicated
303 in Table 6, there are changes in the Pitzer parameters for the interactions of $B(OH)_4^-$—
304 SO_4^{2-} and $B_4O_5(OH)_4^{2-}$—SO_4^{2-}—Na^+ in the re-calibrated model. The $\log_{10} K_{sp}^0$ for borax
305 (sodium tetraborate decahydrate) from the re-calibrated model agrees with the previous
306 value within the quoted uncertainties (Table 6).

307 In Figure 3, our experimental data in Na_2SO_4 solutions are compared with the
308 values predicted by the re-calibrated model, by our previous model (Xiong et al., 2013),
309 and by the model of Felmy and Weare (1986). Figure 3 indicates that our re-calibrated
310 model performs well. Our previous model based on the literature data without pH
311 measurements performs reasonably well. The model of Felmy and Weare (1986) seems
312 to overpredict total boron concentrations as a function of ionic strength.

313 In Table 7, the predicted values for elemental concentrations using the previous
314 model of Xiong et al. (2013), the recalibrated model presented in this work, and the
315 Felmy and Weare (1986) model are compared with the experimental values for borax
316 solubilities in the assemblage of halite+borax+nahcolite. Table 7 shows that the values
317 predicted by the model of Xiong et al. (2013) and the re-calibrated model are in better

agreement with the experimental values taken from Teeple (1929) than the Felmy and Weare (1986) model. Notice that the B(III) elemental concentration changes by using the re-calibrated model in this work with respect to the previous model by Xiong et al. (2013). The B(III) concentration predicted by the re-calibrated model is in excellent agreement with the experimental value.

Similarly, in Table 8, the values predicted by the previous model of Xiong et al. (2013), the recalibrated model presented in this work and the Felmy and Weare (1986) model are compared with the experimental values with the experimental values from Teeple (1929) for borax solubilities in the assemblage of borax+sodium pentaborate. Table 8 shows that the values predicted by the model of Xiong et al. (2013) and the re-calibrated model are in excellent agreement with the experimental values, whereas those predicted by the Felmy and Weare (1986) model are off.

In our model developed in 2013 (Xiong et al., 2013), we first introduced $NaB(OH)_4(aq)$ into the borate model to accurately describe the interaction between borate and sodium, as various techniques including the vapor pressure method, conductivity measurements, and dielectric spectroscopy indicate the presence of $NaB(OH)_4(aq)$ (Rowe and Atkinson, 1990; Weres, 1995; Buchner et al., 1999). The advances in borate chemistry since then have further supported our addition of $NaB(OH)_4(aq)$ into the borate chemistry model. First, Zhou et al. (2012b) provided the clear structural evidence for the existence of $NaB(OH)_4(aq)$. Zhou et al. (2012b) used a rapid liquid X-ray diffractometry with a highly effective *X'celerator*® detector to investigate the diffusion structure of aqueous sodium borate solutions at 25 ^{o}C. They found out that the free Na^+ and $B(OH)_4^-$ ions combine to form contact ion pair (CIP), $NaB(OH)_4(aq)$. Zhou et al. (2017) further

341 studied the association of $B(OH)_4^-$ with Na^+ via the X-ray diffraction technique with the
342 empirical potential structure refinement (EPSR) modeling. In addition, Zhou et al.
343 (2017) performed Density Function Theory (DFT) calculations for the structure and
344 stability of $NaB(OH)_4(aq)$. Their work further demonstrates that Na^+ and B forms
345 contact ion pair. Second, the most recent conductivity measurements by Arcis et al.
346 (2016) also confirm the existence of $NaB(OH)_4(aq)$.

347 The contributions of $NaB(OH)_4(aq)$ to total borate concentrations are expected to
348 be significant in Na-rich solutions. As illustrated by Table 9, the predicted
349 concentrations of $NaB(OH)_4(aq)$ to the total borate concentrations for the assemblage of
350 borax and mirabilite ($Na_2SO_4 \cdot 10H_2O$) at 25°C are 16 % (based on the model of
351 Xiong et al., 2013) or 11% (based on the recalibrated model in this work).
352
353

IMPLICATIONS

As borate can form an aqueous complex with actinides(III), an immediate implication is that the formation of magnesium-bearing borates such as kurnakovite will minimize the concentrations of the aqueous actinides(III)-borate complex to the solubility of actinides(III), by sequestrating soluble borate. This is because the brines in salt formations commonly contain high concentrations of magnesium. For instance, the magnesium concentration in the Generic Weep Brine (GWB) at the Waste Isolation Pilot Plant (WIPP), a geological repository for transuranic waste in the southeastern New Mexico, USA, is 1.16 mol•kg^{-1} (Xiong and Lord, 2008).

Another important implication from this study is that our thermodynamic model can accurately describe the interactions between borate and sulfate. Therefore, our model can be applied to salt lakes with high concentrations of sulfate for efficient recovery of borate.

Finally, as kurnakovite has important industrial applications, the thermodynamic model presented in this study for kurnakovite could increase its usefulness, because the model can be applied to optimize crystallization of kurnakovite from natural brines and its synthesis on an industrial scale.

It is of interest to note that the *ab-initio* calculations have been attempted for assessment of thermodynamic properties of the aqueous species of some heavy metals (Vetuschi Zuccolini et al., 2011). Therefore, it will be valuable to apply *ab-initio* calculations to the borate system including solid boron phases and aqueous borate species in the future. When that happens, it will be possible to compare the *ab-initio* calculations with the empirical estimation methods such as the group contribution method for borates

377 from Li et al. (2000) and the method of Anovitz and Hemingway (2002) for borates,
378 which adopted the methodology for silicates, against the bench-mark experimental
379 values. It would also provide new insights into the speciation scheme of aqueous borate
380 species.
381
382

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Table 1. Experimental results of indirect precipitation of kurnakovite from 1.0 mol•kg^{-1} $MgCl_2$ + 1.0 mol•kg^{-1} NaCl solutions at 22.5 ± 0.5 ^{o}C.

Experimental No.	Experimental Duration (day)	pH_m*	Total magnesium molality, $m_{\Sigma Mg}$, mol•kg^{-1}	Total boron molality, $m_{\Sigma B}$, mol•kg^{-1}	Total sodium molality, $m_{\Sigma Na}$, mol•kg^{-1}	Total chloride molality, $m_{\Sigma Cl}$, mol•kg^{-1}
SYN-Boracite-2	957	8.15	1.112	1.199	1.14	3.083
	1204	8.25	1.125	1.220	1.00	3.054
	1266	8.16	1.130	1.180	1.13	3.016
	1289	8.18	1.138	1.233	1.14	3.072
	1322	8.14	1.130	1.197	N/A	3.055
	1470	8.16	1.146	1.191	N/A	3.137
	1582	8.25	1.167	1.091	1.09	3.094
	1629	8.15	1.049	1.030	1.18	3.028

*pcH values are first calculated based on pH readings and correction factors for $MgCl_2$ solutions from Hansen (2001), and are then converted to pH_m based on the equation from Xiong et al. (2010). As the experimental solutions contain significant amounts of sodium and borate as well as the supporting medium, $MgCl_2$, the pH_m's calculated based on the correction factor for pure $MgCl_2$ might have additional experimental uncertainties. The uncertainties for pH_m by using the correction factor for pure $MgCl_2$ are estimated to be less than ± 0.08 according to the comparison with the correction factors for NaCl used in Xiong (2008) at the ionic strengths of the experiments in this work. In the thermodynamic calculations, the uncertainties include those for pH_m.

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623 Table 2. Experimental results for solubility of borax in Na_2SO_4 solutions at 25 ± 0.5 °C.
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Experimental No.	Supporting Medium Na_2SO_4 (molal)	Experimental time (day)	pH_m	Molal total boron concentrations, $m_{\Sigma B}$, in equilibrium with sodium tetraborate
$Nd(OH)_3$-B-0.01SO_4-1	0.010	454	9.21	0.529
$Nd(OH)_3$-B-0.01SO_4-2	0.010	454	9.22	0.518
$Nd(OH)_3$-B-0.1SO_4-1	0.10	454	9.08	0.420
$Nd(OH)_3$-B-0.1SO_4-2	0.10	454	9.07	0.407
$Nd(OH)_3$-B-0.5SO_4-1	0.5	454	8.73	0.226
$Nd(OH)_3$-B-0.5SO_4-2	0.5	454	8.73	0.273
$Nd(OH)_3$-B-1.0SO_4-1	1.0	454	8.55	0.232
$Nd(OH)_3$-B-1.0SO_4-2	1.0	454	8.55	0.230
$Nd(OH)_3$-B-1.5SO_4-1	1.5	454	8.55	0.254
$Nd(OH)_3$-B-1.5SO_4-2	1.5	454	8.55	0.222
$Nd(OH)_3$-B-1.8SO_4-1	1.8	454	8.66	0.231
$Nd(OH)_3$-B-1.8SO_4-2	1.8	454	8.66	0.231
$Nd(OH)_3$-B-0.01SO_4-1	0.010	762	9.22	0.527
$Nd(OH)_3$-B-0.01SO_4-2	0.010	762	9.19	0.536
$Nd(OH)_3$-B-0.1SO_4-1	0.10	762	9.04	0.447
$Nd(OH)_3$-B-0.1SO_4-2	0.10	762	9.04	0.455
$Nd(OH)_3$-B-0.5SO_4-1	0.5	762	8.71	0.253
$Nd(OH)_3$-B-0.5SO_4-2	0.5	762	8.71	0.258
$Nd(OH)_3$-B-1.8SO_4-1	1.8	762	8.63	0.212
$Nd(OH)_3$-B-1.8SO_4-2	1.8	762	8.63	0.208
$Nd(OH)_3$-B-0.5SO_4-1	0.5	791	8.74	0.261
$Nd(OH)_3$-B-0.5SO_4-2	0.5	791	8.73	0.267

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$Nd(OH)_3$-B-1.0SO_4-1	1.0	791	8.56	0.224
$Nd(OH)_3$-B-1.0SO_4-2	1.0	791	8.56	0.233
$Nd(OH)_3$-B-1.5SO_4-2	1.5	791	8.56	0.207
$Nd(OH)_3$-B-1.8SO_4-2	1.8	791	8.65	0.203
$Nd(OH)_3$-B-0.01SO_4-1	0.010	811	9.33	0.551
$Nd(OH)_3$-B-0.01SO_4-2	0.010	811	9.23	0.553
$Nd(OH)_3$-B-0.1SO_4-1	0.10	811	9.09	0.463
$Nd(OH)_3$-B-0.1SO_4-2	0.10	811	9.09	0.467
$Nd(OH)_3$-B-0.5SO_4-1	0.5	811	8.74	0.303
$Nd(OH)_3$-B-0.5SO_4-2	0.5	811	8.75	0.296
$Nd(OH)_3$-B-1.0SO_4-1	1.0	811	8.56	0.254
$Nd(OH)_3$-B-1.0SO_4-2	1.0	811	8.57	0.247
$Nd(OH)_3$-B-1.5SO_4-1	1.5	811	8.56	0.227
$Nd(OH)_3$-B-1.5SO_4-2	1.5	811	8.56	0.218
$Nd(OH)_3$-B-1.8SO_4-1	1.8	811	8.65	0.205
$Nd(OH)_3$-B-1.8SO_4-2	1.8	811	8.65	0.215

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Table 3. Equilibrium constants at infinite dilution for the equilibrium between boracite and kurnakovite and for the dissolution reaction of kurnakovite at 25°C and 1 bar.

Reaction	$\log_{10} K^0$ [A]
$Mg_3B_7O_{13}Cl(cr) + H^+ + 2B(OH)_4^- + 18H_2O(l) \rightleftharpoons 3MgB_3O_3(OH)_5{\bullet}5H_2O(cr) + Cl^-$	12.83 ± 0.08 (2σ)
$MgB_3O_3(OH)_5{\bullet}5H_2O(cr) = Mg^{2+} + 3B(OH)_4^- + H^+ + H_2O(l)$	–14.11 ± 0.40 (2σ)

[A] The equilibrium constants were calculated based on all of the experimental data tabulated in Table 1. The uncertainty in terms of 2σ includes that for the small extrapolation from 22.5°C to the standard temperature of 25°C.

Table 4. Equilibrium constants at infinite dilution for kurnakovite dissolution at 25°C and 1 bar calculated from the Gibbs free energies from the literature.

Reaction	$\log_{10} K^0$
$MgB_3O_3(OH)_5{\bullet}5H_2O(cr) = Mg^{2+} + 3B(OH)_4^- + H^+ + H_2O(l)$	–17.23 [A]
	–21.16 [B]

Note: Calculated using the estimated ΔG_f^0 values from Li et al. (2000) [A] and Anovitz and Hemingway (2002) [B], consistent with the NBS Thermodynamic Tables (Wagman et al., 1982).

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Table 5. Thermodynamic properties of kurnakovite, $MgB_3O_3(OH)_5 \bullet 5H_2O$(cr), at 25°C and 1 bar. The values recommended by this study are in bold.

Species	ΔH_f^0, kJ•mol^{-1}	ΔG_f^0, kJ•mol^{-1}	S^0 J•mol^{-1}•K^{-1}	References and Remarks
Kurnakovite	–4856	–4272	405	Anovitz and Hemingway (2002) [A]
Kurnakovite	–4813.24 ± 2.46			Li et al. (1997) [B]
Kurnakovite	–4831.81	–4249.79	411.85	Li et al. (2000); Entropy calculated in this work [C]
Kurnakovite	**–4813.24 ± 2.46**	**–4231.95 ± 2.29**	**414.31 ± 0.9**	This work [D]

[A] All parameters were estimated.
[B] Enthalpy was experimentally determined.
[C] All parameters were estimated. Gibbs free energy of formation and enthalpy of formation were calculated using the group contribution method of Li et al. (2000). Entropy was calculated internally with the Gibbs-Helmholtz equation by this work from the estimated enthalpy and Gibbs free energy.
[D] Enthalpy is the experimental value of Li et al. (1997) determined using the calorimetric method. Gibbs free energy was computed from the experimentally determined equilibrium constant from this work. Entropy was calculated from the experimental enthalpy of Li et al. (1997) and the derived Gibbs free energy from the experimental equilibrium constant of this work.

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672 Table 6. The revision of the thermodynamic model for the Na–$B(OH)_3$–SO_4 system in
673 Xiong et al. (2013) based on experimental solubility data of borax in Na_2SO_4 solutions at
674 25°C presented in this work

Pitzer Mixing Parameters and Interaction Parameters Involving Neutral Species				
Species, *i*	Species, *j*	Species, *k*	θ_{ij} or λ_{ij}	Ψ_{ijk} or ζ_{ijk}
$B(OH)_4^-$	SO_4^{2-}		0.17 ± 0.03 (Xiong et al. 2013)	
$B(OH)_4^-$	SO_4^{2-}		–0.00562 ± 0.0026 (P.W.)	
$NaB(OH)_4(aq)$	Na^+		0.093 ± 0.005	
$B_4O_5(OH)_4^{2-}$	SO_4^{2-}	Na^+		0.1 ± 0.2 (Xiong et al., 2013)
$B_4O_5(OH)_4^{2-}$	SO_4^{2-}	Na^+		0.00174 ± 0.0012 (P.W.)
Equilibrium Constants for Solubility and Complex Formation Reactions				
Reaction			log *K* or log β_1 at 25 °C unless otherwise noted	
$Na_2B_4O_7•10H_2O^A \rightleftharpoons 2Na^+ + 4B(OH)_4^- + 2H^+ + H_2O$			–24.80 ± 0.10 (2σ) (Xiong et al., 2013)	
$Na^+ + B(OH)_4^- \rightleftharpoons NaB(OH)_4(aq)$			0.25 ± 0.01	

675 P.W.: present work.
676 [A]: The structural formula for borax is $Na_2B_4O_5(OH)_4•8H_2O$, which is same as its
677 chemical formula that was used in Xiong et al. (2013), $Na_2B_4O_7•10H_2O$.
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Table 7. A comparison of the experimental invariant solution compositions for the assemblage of Halite (NaCl) + Nahcolite ($NaHCO_3$) + Borax ($Na_2B_4O_7•10H_2O$ or $Na_2B_4O_5(OH)_4•8H_2O$ as its structural formula) with the values predicted by various models at 25°C.

Elemental Concentrations, mol•kg^{-1}	Experimental data [B]	FW86	Xiong et al. (2013)	Re-calibrated Model (Present Work)
B(III)	0.199	0.237	0.176	0.195
Na(I)	6.11	6.33	6.30	6.30
Cl(-I)	5.90	6.00	6.01	6.01
C(IV), TDIC [A]	0.107	0.214	0.208	0.209

[A] TDIC, total dissolved inorganic carbon, as HCO_3^-/CO_3^{2-}
[B] 20°C; from Teeple (1929).

Table 8. A comparison of the experimental solution compositions for the assemblage of Borax ($Na_2B_4O_7•10H_2O$ or $Na_2B_4O_5(OH)_4•8H_2O$ as its structural formula) + Sodium Pentaborate ($NaB_5O_8•5H_2O$) with the values predicted by various models at 25°C.

Elemental Concentrations, mol•kg^{-1}	Experimental data [A]	FW86	Xiong et al. (2013)	Re-calibrated Model (Present Work)
B(III)	4.20	5.33	4.21	4.21
Na(I)	1.03	1.36	0.972	0.972

[A] 24°C; from Teeple (1929).

Table 9. Predicted distributions of borate species for the assemblage of borax and mirabilite by using the model in Xiong et al. (2013) and the re-calibrated model in this work

Borate species	Model in Xiong et al. (2013)		Re-calibrated model	
	molality	log a_i	molality	log a_i
$B(OH)_3(aq)$	0.04588	-1.4905	0.050379	-1.4482
$B(OH)_4^-$	0.032386	-1.8985	0.039938	-1.9443
$NaB(OH)_4(aq)$	0.020311	-1.3760	0.018332	-1.4180
$B_3O_3(OH)_4^-$	0.0071235	-3.0793	0.0079010	-3.0398
$B_4O_5(OH)_4^{2-}$	0.0016022	-4.2857	0.0080894	-4.2917
ΣB	0.12606		0.16471	

Figure Captions

Figure 1. XRD patterns of the solid phases from the experiments. The vertical lines in pink, green and blue are the reference peaks of boracite, kurnakovite, and borax, respectively. All of the reference peaks are from the database of the International Centre for Diffraction Data, ICDD. a. The XRD pattern in comparison with those of boracite and borax; b. the XRD pattern in comparison with those of kurnakovite and borax.

Figure 2. Variations of the total boron, chloride, magnesium and sodium concentrations as a function of run duration.

Figure 3. A comparison of experimental solubility data of borax in Na_2SO_4 solutions at 25^{o}C with the values predicted by using various models.

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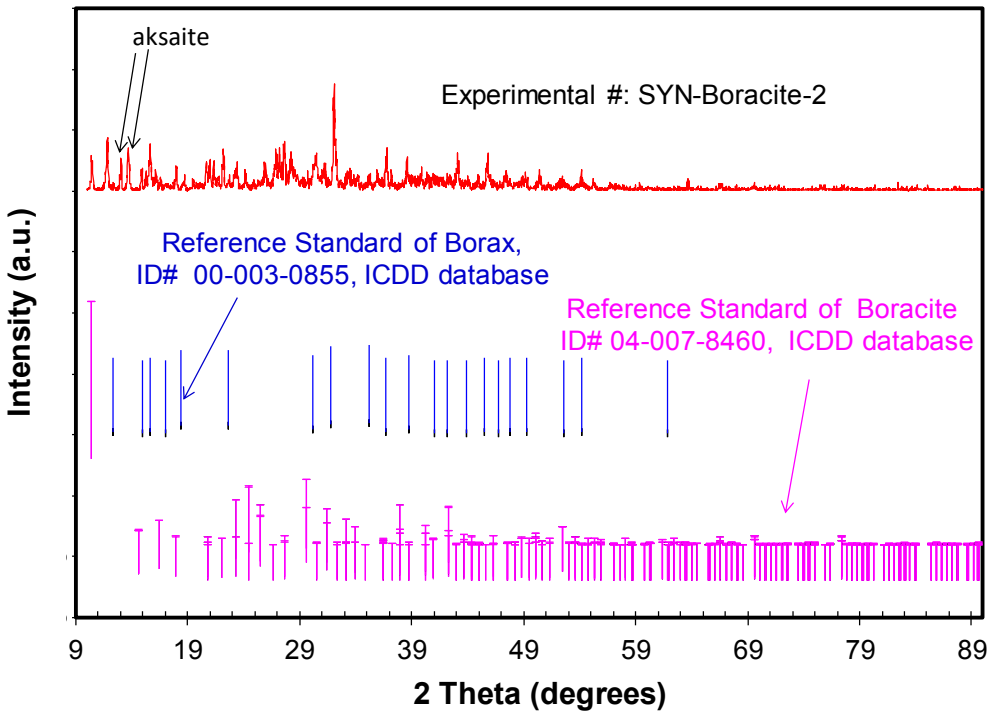

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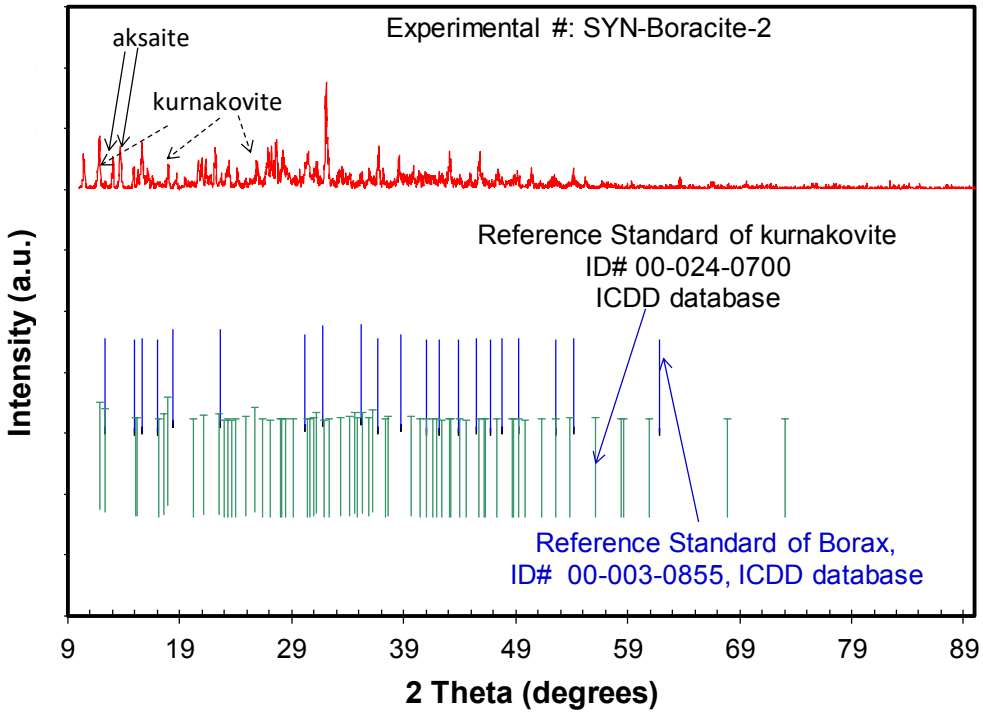

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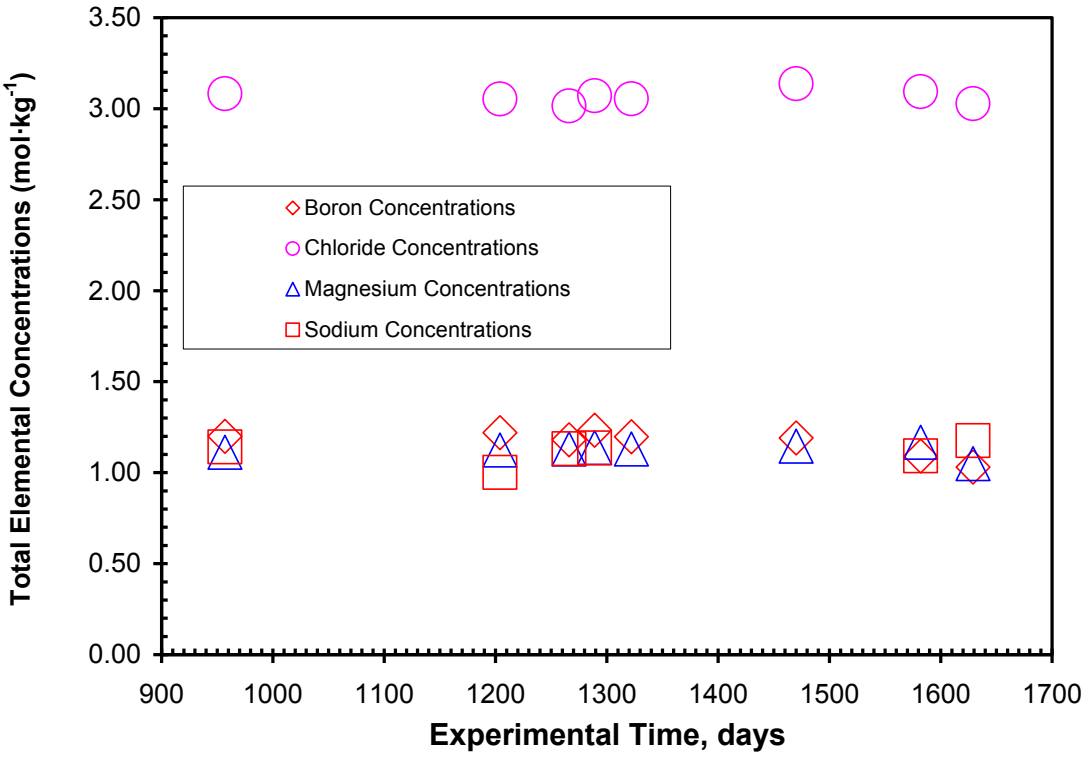

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736 Figure 2.
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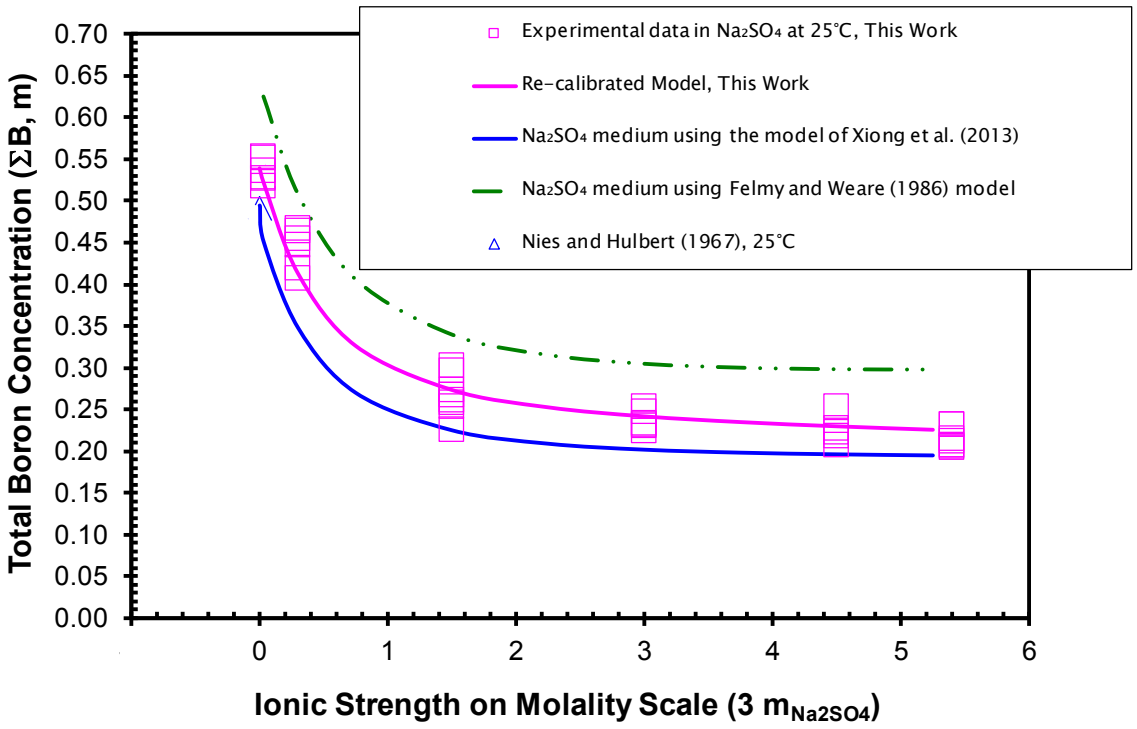

Figure 3.