

1 **Revision 1**

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3 **The new K, Pb-bearing uranyl-oxide mineral kroupaite: crystal-chemical implications for**  
4 **the structures of uranyl-oxide hydroxy-hydrates**

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19 **ABSTRACT**

20 Kroupaite (IMA2017-031), ideally  $\text{KPb}_{0.5}[(\text{UO}_2)_8\text{O}_4(\text{OH})_{10}] \cdot 10\text{H}_2\text{O}$ , is a new uranyl-oxide  
21 hydroxyl-hydrate mineral found underground in the Svornost mine, Jáchymov, Czechia.  
22 Electron-probe microanalysis (WDS) provided the empirical formula  
23  $(\text{K}_{1.28}\text{Na}_{0.07})_{\Sigma 1.35}(\text{Pb}_{0.23}\text{Cu}_{0.14}\text{Ca}_{0.05}\text{Bi}_{0.03}\text{Co}_{0.02}\text{Al}_{0.01})_{\Sigma 0.48}[(\text{UO}_2)_{7.90}(\text{SO}_4)_{0.04}\text{O}_{4.04}(\text{OH})_{10.00}] \cdot 10\text{H}_2\text{O}$ ,  
24 basis of 40 O atoms apfu. Sheets in the crystal structure of kroupaite adopt the fourmarierite  
25 anion topology, and therefore kroupaite belongs to the schoepite-family of minerals with related  
26 structures differing in the interlayer composition and arrangement, and charge of the sheets.  
27 Uptake of dangerous radionuclides (<sup>90</sup>Sr or <sup>135</sup>Cs) into the structure of kroupaite and other

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28 uranyl-oxide hydroxy-hydrate is evaluated based on crystal-chemical considerations and  
29 Voronoi-Dirichlet polyhedra measures. These calculations show the importance of these phases  
30 for the safe disposal of nuclear waste.

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32 *Keywords:* kroupaite; new mineral species; uranyl-oxide hydroxy-hydrate; crystal structure;  
33 Voronoi-Dirichlet polyhedra;  $^{135}\text{Cs}$ ;  $^{90}\text{Sr}$ ; Jáchymov.

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## INTRODUCTION

36 Uranium dioxide, as nuclear fuel or uraninite (Janeczek et al. 1996),  $\text{UO}_{2+x}$ , readily reacts with  
37 oxygen and water to form a fascinating family of uranyl-oxide hydroxyl-hydrates (UOHs) (Finch  
38 and Ewing 1992; Wronkiewicz et al. 1996; Plášil 2014). These occur in nature as minerals and  
39 are amongst the first alteration products that form during weathering of uraninite in oxidized  
40 zones of U deposit worldwide (Finch et al. 1996a, b; Plášil 2018a). They are of interest in  
41 forensics studies of intercepted illicit nuclear materials as they provide insights into uranium  
42 oxide history. Number of studies has focused on their structure, solubility, and thermodynamic  
43 stability (Casas et al. 1997; Finch and Murakami 1999; Klingensmith et al. 2007; Kubatko et al.  
44 2006a; Gorman-Lewis et al. 2008; Kirkegaard et al. 2019). It is due to their general importance in  
45 nuclear waste disposal and the environmental chemistry of uranium.

46 The onset of oxidation and hydration of uranium oxide often yields phases consisting of  
47 electroneutral sheets of uranyl pentagonal bipyramids with substantial  $\text{H}_2\text{O}$  in the interlayer  
48 region, and typically little, if any, additional metal cations (Burns 2005; Krivovichev and Plášil  
49 2013; Lussier et al. 2016; Plášil 2018a). In some cases, uranium oxide hydrates containing  
50 mixtures of U(IV), U(V) or U(VI) oxidation states occur as well. Continued alteration of uranium

51 oxide, alteration in more chemically diverse aqueous fluids, and alteration of geologically old  
52 uranium oxide that contains substantial radiogenic lead leads to formation of uranyl-oxide  
53 hydroxy-hydrates with anionic sheets of uranyl polyhedra charge-balanced by cations in the  
54 interstitial regions of the structures.

55 Here we describe the new mineral kroupaite that was found underground in the Svornost  
56 (formerly “Einigkeit” in German) mine in Jáchymov, Western Bohemia, Czechia. Details of the  
57 mineralogy, geology and history of the Jáchymov ore district can be found elsewhere (Ondruš et  
58 al. 2003; Hloušek et al. 2014). The specimens studied originate from the Jan Evangelista vein at  
59 the Daniel level of the Svornost mine. Associated minerals include fourmarierite, Na-rich  
60 metaschoepite, uranopilite, liebigite, ewingite and gypsum. The new mineral and its assemblage  
61 are of supergene origin associated with oxidation-hydration alteration of uraninite in old mine  
62 workings. The name honors mining engineer Gustav Kroupa (1857–1935), who was employed by  
63 the state mines in Jáchymov beginning in 1886, and who as head of the mining district, approved  
64 shipment of 10 tons of leachate obtained from processing pitchblende ore to Marie-Curie  
65 Sklodowska and Pierre Curie in 1898. They went on to isolate three grams of the new substance  
66 radium chloride, and subsequently the new element radium. The Commission on New Minerals,  
67 Nomenclature and Classification of the International Mineralogical Association approved the  
68 new mineral and name (IMA2017-031). The description is based upon the holotype specimen  
69 deposited in the mineralogical collection of the National Museum in Prague (catalogue number  
70 no. P1P 16/2017). Crystals used in this study are deposited in the Natural History Museum of Los  
71 Angeles County (catalogue number 66572).

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### **PHYSICAL AND OPTICAL PROPERTIES**

74 Kroupaite forms as radial aggregates of thick platy, orange-yellow crystals up to 1 mm in  
75 diameter (Fig. 1) growing in interstices of gypsum crystals. Tablets are flattened on {100}, with  
76 the prominent crystal forms {100}, {013} and {021} (Fig. 2). Crystals are brittle with at least one  
77 perfect cleavage on {100} and uneven fracture. Crystals are translucent with vitreous luster, have  
78 light yellow streak, and are non-fluorescent under LW and SW ultraviolet radiation. The Mohs  
79 hardness is approximately 2, estimated by scratch tests. The density was not measured due to the  
80 limited availability of material. The calculated density is 5.058 g/cm<sup>3</sup> based on the empirical  
81 formula. Kroupaite is readily soluble in dilute HCl, with no effervescence.

82 Kroupaite is optically biaxial (-), with  $\alpha = 1.691(2)$ ,  $\beta = 1.752(2)$ ,  $\gamma = 1.768(2)$  (measured  
83 with white light). The  $2V$  is 53(1)°, measured directly by conoscopic observation on a spindle  
84 stage; the calculated  $2V$  is 52.7°. Dispersion is strong,  $r > v$ . The mineral is pleochroic with  $X$   
85 colorless,  $Y$  yellow and  $Z$  yellow;  $X < Y \approx Z$ . The optical orientation is  $X = \mathbf{a}$ ,  $Y = \mathbf{c}$ ,  $Z = \mathbf{b}$ . The  
86 Gladstone-Dale compatibility (Mandarino 2007),  $1 - (K_p/K_c)$ , is -0.018 (superior) for the  
87 empirical formula.

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#### 89 **RAMAN SPECTROSCOPY**

90 A Raman spectrum was collected in the range 4500–12 cm<sup>-1</sup> using a DXR dispersive  
91 Raman Spectrometer (Thermo Scientific) mounted on a confocal Olympus microscope. The  
92 Raman signal was excited by a green 532 nm diode-pumped solid-state laser and was collected  
93 by a CCD detector. The experimental parameters were: 50× objective, 10 s exposure time, 100  
94 exposures, 400 lines/mm grating, 50 μm pinhole spectrograph aperture and 1 mW laser power  
95 level. The instrument was set up by a software-controlled calibration procedure using multiple  
96 neon emission lines (wavelength calibration), multiple polystyrene Raman bands (laser frequency

97 calibration) and standardized white-light sources (intensity calibration). Spectral manipulations as  
98 well as band-fitting were performed using the Omnic 9 software (Thermo Scientific).

99 In the Raman spectrum of kroupaite (Fig. 3a) a weak broad band at  $3487\text{ cm}^{-1}$  is assigned  
100 to the  $\nu$  O–H stretching vibrations of hydroxyl and molecular  $\text{H}_2\text{O}$  H-bonded into the structure.  
101 The approximate bond-lengths of H-bonds ( $\text{H}\cdots\textit{Acceptor}$ ) lie in the range  $1.8\text{--}2.0\text{ \AA}$  (Libowitzky  
102 1999). The strong band centered at  $833\text{ cm}^{-1}$ , with a shoulder at  $812\text{ cm}^{-1}$  (Figure 3b), is  
103 attributed to the  $\nu_1$  symmetric stretching vibration of uranyl U–O. The splitting of the  $\nu_1$  of  
104  $(\text{UO}_2)^{2+}$  is concomitant with four unique U sites observed in the crystal structure. Based on recent  
105 theoretical and experimental studies (Colmenero et al. 2018; Kirkegaard et al. 2019), the  
106 assignment of the vibration bands directly to  $\nu_1 (\text{UO}_2)^{2+}$  is not straightforward: the component  
107 bands comprise both symmetric stretching  $\nu_1 (\text{UO}_2)^{2+}$  and  $\delta (\text{U–OH})$ , as well as libration  
108 vibration of ( $\text{H}_2\text{O}$ ). Nevertheless, using an empirical relationship to derive the approximate U–O  
109 bond lengths from the band positions assigned to the  $(\text{UO}_2)^{2+}$  stretching vibrations gives  $\sim 1.78\text{ \AA}$   
110 ( $833\text{ cm}^{-1}$ ) and  $\sim 1.80\text{ \AA}$  ( $812\text{ cm}^{-1}$ ) (Fig. 3b). These values are in line with U–O bond-lengths  
111 obtained from the crystal structure data (see Table 2). There is a series of weak bands in the  $580\text{--}$   
112  $280\text{ cm}^{-1}$  range ( $570, 542, 500, 450, 400, 328, 298\text{ cm}^{-1}$ ). Those at  $570\text{--}500\text{ cm}^{-1}$  are attributable  
113 to librations of  $\text{H}_2\text{O}$ . Those at  $450\text{--}328\text{ cm}^{-1}$  can be assigned to  $\delta (\text{O–U–O}_{\text{eq}})$  vibrations.  
114 According to a theoretical study of schoepite (Colmenero et al. 2018, 2019), these bands also  
115 have a significant contribution of the  $\nu (\text{U–O}_{\text{eq}})$ ,  $\delta (\text{U–OH})$  and libration of  $\text{H}_2\text{O}$ . The band at  $298$   
116  $\text{cm}^{-1}$  is attributed to  $\nu_2 (\delta) (\text{UO}_2)^{2+}$ , but there may be contributions from  $\delta (\text{O–U–O}_{\text{eq}})$ ,  $\delta (\text{U–OH})$   
117 and water librations. Remaining bands located below  $200\text{ cm}^{-1}$  ( $190, 155, 116, 63, 40\text{ cm}^{-1}$ ) are  
118 assigned to molecular deformations and lattice modes.

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## CHEMICAL ANALYSIS

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Kroupaite was analyzed by electron microprobe using a Cameca SX100 electron

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microprobe (Masaryk University, Brno) operating in wavelength dispersive spectroscopy mode

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using an accelerating voltage of 15 kV, beam current of 4 nA and a 10–15  $\mu\text{m}$  beam diameter.

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Concentrations of elements other than those reported in Table S1 were below detection limits (ca

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0.03–0.10 wt. %). The low analytical totals are due to an uneven surface and the porosity of the

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polished section; therefore, we also report normalized data (column “Norm.” in Table 1). A

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matrix correction was applied to the data using the ‘*PAP*’ software (Pouchou and Pichoir 1991).

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The  $\text{H}_2\text{O}$  content was calculated by stoichiometry (obtained from the structure); the paucity of

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pure material precluded a direct determination of the  $\text{H}_2\text{O}$  content. The empirical formula

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calculated on the basis of 40 O atoms per formula unit is:

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$(\text{K}_{1.28}\text{Na}_{0.07})_{\Sigma 1.35}(\text{Pb}_{0.23}\text{Cu}_{0.14}\text{Ca}_{0.05}\text{Bi}_{0.03}\text{Co}_{0.02}\text{Al}_{0.01})_{\Sigma 0.48}[(\text{UO}_2)_{7.90}(\text{SO}_4)_{0.04}\text{O}_{4.04}(\text{OH})_{10.00}] \cdot 10\text{H}_2\text{O}$ .

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The ideal formula is  $\text{KPb}_{0.5}[(\text{UO}_2)_8\text{O}_4(\text{OH})_{10}] \cdot 10\text{H}_2\text{O}$ , which requires:  $\text{K}_2\text{O}$  1.73,  $\text{PbO}$  4.11,  $\text{UO}_3$

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84.21,  $\text{H}_2\text{O}$  9.95, total 100 wt%.

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## X-RAY CRYSTALLOGRAPHY AND STRUCTURE DETERMINATION

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Powder diffraction data were collected using a Rigaku R-Axis Rapid II curved imaging

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plate microdiffractometer with monochromated  $\text{MoK}_\alpha$  radiation. A Gandolfi-like motion on the  $\varphi$

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and  $\omega$  axes was used to randomize the sample. Observed  $d$ -values and intensities were derived by

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profile fitting using the JADE 2010 software (Materials Data, Inc.). Data are given in Table 2.

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Unit-cell parameters refined from the powder data using JADE 2010 with whole pattern fitting

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are:  $a = 14.781(7)$  Å,  $b = 14.095(6)$  Å,  $c = 16.719(7)$  Å,  $V = 3583(3)$  Å<sup>3</sup>,  $Z = 4$  (space group:

142

*Pbca*).

143 Single-crystal X-ray diffraction data were collected at room temperature on a Rigaku  
144 SuperNova diffractometer equipped with a microfocus X-ray source ( $\text{MoK}_\alpha$ ,  $\lambda = 0.71073 \text{ \AA}$ ) and  
145 an Atlas S2 CCD detector. The crystal,  $0.07 \times 0.06 \times 0.03 \text{ mm}$  large, was mounted on a cut  
146 microloop. The raw data reduction was done using CrysAlis software (Rigaku 2019). An  
147 absorption correction combining a Gaussian correction and an empirical scaling was applied to  
148 the data using the Jana2006 software (Petříček et al. 2014). The structure was solved with  
149 SHELXT using charge-flipping (Sheldrick 2015). Full-matrix least squares refinement of the  
150 structure against  $F^2$  was performed with Jana2006 (Petříček et al. 2014); the structure has been  
151 refined to  $R = 0.0447$  for 2587 unique observed reflection. The crystallographic data can be found  
152 in the original cif file (as supplementary file); selected interatomic distances and results of the  
153 bond-valence analysis are given in Tables 3 and 4, respectively..

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#### 155 DESCRIPTION OF THE STRUCTURE

156 Kroupaite crystallizes in orthorhombic space group  $Pbca$  and its structure (Fig. 4)  
157 contains four U sites, one K site, one Pb site and nineteen O sites. Each U site is coordinated by  
158 seven ligands (Table 3), forming pentagonal bipyramids, where the apices of each bipyramid are  
159 comprised of strongly bonded O atoms, forming the approximately linear uranyl ion,  $\text{UO}_2^{2+}$ . In  
160 the equatorial plane, each uranyl ion is bonded to five ligands, either O or  $\text{OH}^-$  (Table 4), and the  
161 polyhedra polymerize by sharing edges and equatorial vertices (Fig. 4) into the well-known  
162 fourmarierite anion sheet topology (Fig. 5) (Burns 2005; Krivovichev and Plášil 2013; Lussier et  
163 al. 2016). In the interlayer, there are two independent cation sites that are occupied by  $\text{K}^+$  and  
164  $\text{Pb}^{2+}$ . Both sites have occupancies lower than unity. Additionally, there are four O sites (O15,  
165 O16, O18, O19) in the interlayer corresponding to  $\text{H}_2\text{O}$  molecules (Table 4) that were identified

166 based on the bond-valence sums incident upon the corresponding O atoms. The K atom is [7]-  
167 fold coordinated (to 3.3 Å) and binds to five distinct  $O_{Ur}$  ( $Ur$  – uranyl) atoms. Site-scattering  
168 refinement revealed that the site is partially occupied ( $\sim 0.47/0.5$ ). The Pb site is [9]-fold  
169 coordinated (to 3.3 Å); six of the ligands are  $O_{Ur}$  atoms from adjacent structural sheets, with three  
170 from each sheet, and thus the Pb cations directly bridge between sheets. There are dimers of Pb  
171 polyhedra; one Pb-polyhedron is linked to its symmetrical equivalent through the pair of  
172 symmetrically related O16( $H_2O$ ) atoms to form  $Pb_2O(O_{Ur})_{10}(H_2O)_3$  dimers.

173         According to the bond-valence analysis and site-scattering refinement the formula,  
174 assuming full metal-cation site occupancy for K (0.94 K from the site-scattering refinement) and  
175 0.5 Pb (0.44 from refinement) and full occupancies of the O( $H_2O$ ) sites, is  
176  $KPb_{0.5}[(UO_2)_8O_4(OH)_{10}] \cdot 8H_2O$ ,  $Z = 4$ , although the  $H_2O$  content is likely somewhat lower.

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## 178                   RELATIONSHIP TO OTHER UOH MINERALS AND COMPOUNDS

179         The structural unit in kroupaite is the well-known fourmarierite-type sheet, which  
180 accommodates various combinations of  $OH^-$  and O in uranyl minerals, and thus has variable  
181 charge. Electroneutral sheets with composition  $[(UO_2)_4O(OH)_6]$  occur in schoepite and  
182 metaschoepite (Plášil 2018b; Weller et al. 2000), whereas anionic sheets with composition  
183  $[(UO_2)_4O_2(OH)_5]^-$  occur in synthetic Na-bearing metaschoepite (Klingensmith et al. 2007) and  
184 leesite (Olds et al. 2018), and with composition  $[(UO_2)_4O_3(OH)_4]^{2-}$  in fourmarierite (Li and  
185 Burns 2000a).

186         Lead cations in the structure of kroupaite occupy the same site as  $Pb^{2+}$  in fourmarierite,  
187 but surprisingly, also the same site as  $K^+$  in leesite (Fig. 5). In the structure of kroupaite, K atoms  
188 occupy the site adjacent to the dimeric Pb polyhedral units. The different behaviors of K and Pb



189 in the structures of kroupaite and leesite are well documented by distinct substitution trends  
190 between kroupaite and fourmarierite (characteristic for the same Pb sites) and leesite (Fig. 6). The  
191 substitution in leesite should take place at the single cationic site for  $\text{Pb}^{2+}$  and  $\text{K}^+$ . The main  
192 structural distinction of kroupaite from leesite is a unique  $\text{K}^+$  site in kroupaite (Fig. 5). It appears  
193 that in the presence of  $\text{Pb}^{2+}$  with a stereoactive lone pair of electrons,  $\text{K}^+$  is favored at a site that  
194 provides more space and, consequently, K atoms shift to a position beneath bounding  $\text{O}_{Ur}$  atoms.  
195 The corresponding Voronoi-Dirichlet polyhedral values that characterize particular coordination  
196 environments of metal cations in the interlayers of kroupaite, leesite, fourmarierite (Fig. 7) and  
197 synthetic Na-metaschoepite are given in Table 5. Comparing Lewis acid (LA) strengths,  $\text{Pb}^{2+}$  is a  
198 much stronger acid (0.22 *vu*) than  $\text{K}^+$  (0.11 *vu*). Both kroupaite and leesite contain similar  
199 amounts of  $\text{H}_2\text{O}$  in their interlayers (kroupaite is slightly more hydrated) and the arrangement of  
200  $(\text{OH})^-$  in the kroupaite sheet is identical to that found both in leesite and synthetic Na-  
201 metaschoepite. The consequence is that Pb adopts a site in the kroupaite structure that is more  
202 compatible with the distribution of higher bond-valence from Lewis acids to Lewis bases; in  
203 kroupaite the average  $\text{Pb}^{2+}\text{-O}$  bond-strength is 0.16 *vu* while that of  $\text{K}^+\text{-O}$  is 0.10 *vu*. Acceptors  
204 of the majority of bonds from  $\text{Pb}^{2+}$  in kroupaite are apical uranyl atoms within the sheets.

#### 205 **URANYL-OXIDE HYDROXY-HYDRATES WITH VARIOUS INTERLAYER CATIONS**

206 The interstitial complexes of uranyl-oxide hydrates incorporate various elements with  
207 distinct stereochemistry. Uranyl minerals form in complex multiphase chemical conditions  
208 arising from their geological settings (and geochemistry), and are also expected to form in  
209 complex environments such as underground repositories for long-term storage of nuclear (Maher  
210 et al. 2013; Ewing 2015).

211 The structures and compositions of uranyl-oxide hydrates have recently been reviewed  
212 (Plášil 2018a). Crystal structures of uranyl-oxide hydrates sometimes contain U(V) or U(IV),  
213 with U(V) observed in structures containing  $\beta$ -U<sub>3</sub>O<sub>8</sub> (Burns and Finch 1999) and  $\alpha$ -U<sub>3</sub>O<sub>8</sub> (Plášil  
214 2017a) types of uranyl-oxide layers. In nollmotzite, Mg[U<sup>V</sup>(U<sup>VI</sup>O<sub>2</sub>)<sub>2</sub>O<sub>4</sub>F<sub>3</sub>] $\cdot$ 4H<sub>2</sub>O, the  $\beta$ -U<sub>3</sub>O<sub>8</sub> type  
215 of sheet contains fluorine as well as oxygen (Plášil et al. 2018).

216 The interstitial complexes of uranyl oxide hydrates incorporate various alkali and alkaline  
217 earth cations as well as lanthanides (Zhang et al. 2018, 2019; Hill and Burns 1999; Burns and  
218 Hill 2000a, b; Cahill and Burns 2000). The capacity of uranyl-oxide hydrates to accommodate  
219 cations of various Lewis-acid strengths arises in part from the heterogeneous distribution of  
220 different types of anions within the sheets: uranyl O atoms, which are somewhat undersaturated  
221 with respect to their bond-valence requirements, and OH<sup>-</sup> groups within the uranyl-oxide layers  
222 that are bond-valence donors. These sheets readily accommodate cations of distinct charges and  
223 radii (Zhang et al. 2016), and also of different stereochemistry (Olds et al. 2017). In comparison,  
224 kamitugaite, PbAl[(UO<sub>2</sub>)<sub>5</sub>(PO<sub>4</sub>)<sub>2.38</sub>(AsO<sub>4</sub>)<sub>0.62</sub>O<sub>2</sub>(OH)<sub>2</sub>](H<sub>2</sub>O)<sub>11.5</sub> (Plášil 2017b) combines divalent  
225 and trivalent cations in its interstitial complexes, and the Pb<sup>2+</sup> is electron lone-pair stereoactive.  
226 The distribution of anions appears to preclude occurrence of both Pb<sup>2+</sup> and Al<sup>3+</sup> in the same  
227 interlayer. Thus, there are two distinct interlayers in kamitugaite, giving a large unit cell.

228 Voronoi-Dirichlet polyhedra (VDP) calculations (Blatov et al. 2004) were used to  
229 evaluate and quantify bonding environments in the interlayer regions of UOHs. The VDP  
230 calculations are summarized in Table 5 and selected aspects are displayed in Figure 8. Generally,  
231 Pb<sup>2+</sup> occupies sites with VDP volume ( $V_{\text{VDP}}$ )  $\sim$ 18 Å<sup>3</sup>. If there is an additional cation with a larger  
232 ionic radius, as K<sup>+</sup> in gauthierite and kroupaite, it occupies sites with  $V_{\text{VDP}} > 20$  Å<sup>3</sup>. In leesite, the  
233 K<sup>+</sup> occupies a site with  $V_{\text{VDP}} > 19.66$  Å<sup>3</sup> that is populated by Pb<sup>2+</sup> in other uranyl-oxide-hydrate

234 structures. The structure of gauthierite is particularly interesting as it contains four symmetrically  
235 independent partially occupied K sites. Site K2 has  $V_{\text{VDP}} \sim 27 \text{ \AA}^3$ .

### 236 POTENTIAL $\text{Cs}^+$ AND $\text{Sr}^{2+}$ INCORPORATION

237 Voronoi-Dirichlet polyhedra calculations for uranyl-oxide-hydrate structures can help in  
238 predicting incorporation of radionuclides of concern for nuclear waste disposal, such as  $^{135}\text{Cs}$  ( $t^{1/2}$   
239 = 2.3 MY) or  $^{90}\text{Sr}$  ( $t^{1/2} = 28.8 \text{ Y}$ ) that are important for long-term disposal and shorter-term heat  
240 generation, respectively (Maher et al. 2013; Ewing 2015). VDP calculations are sensitive to the  
241 size of the corresponding cation and can be employed to determine characteristic volumes of  
242 corresponding cation polyhedra in uranyl-oxide-hydrate structures. Results of the analysis are  
243 given in Table 5 and Figure 8, where bonding properties of interlayer cations in most uranyl-  
244 oxide-hydrate structures based on VDP volume and corresponding ionic radii (after Shannon  
245 1976) are listed. The ionic radii of  $\text{Cs}^+$  and  $\text{Sr}^{2+}$  are 1.81 and 1.36  $\text{\AA}$ , respectively, and  $\text{Sr}^{2+}$   
246 readily substitutes for  $\text{Pb}^{2+}$  and  $\text{Ca}^{2+}$ , as in agrinierite (Cahill and Burns 2000). Substitutions of  
247  $\text{Sr}^{2+}$  for  $\text{Pb}^{2+}$  and  $\text{Ca}^{2+}$  has been documented for synthetic UOHs related to curite and becquerelite  
248 (Burns and Hill 2000a; Burns and Li 2002). Cesium is less likely to be incorporated into the  
249 interlayers of UOHs structures, although a synthetic uranyl oxide hydrate containing Cs has been  
250 reported (Hill and Burns 1999) as well as uptake of  $\text{Cs}^+$  by a uranyl oxide hydrate during  
251 crystallization (Giammar and Hering 2004). It is plausible that  $\text{Cs}^+$  can be incorporated in K-  
252 bearing UOHs, as the  $V_{\text{VDP}}$  of  $\text{K}^+$  sites reaches  $\sim 24 \text{ \AA}^3$  (with an extreme value of  $\sim 27 \text{ \AA}^3$  in case  
253 of K2 in gauthierite; Tables 7).

### 254 CHARGE-DENSITY MATCH IN URANYL-OXIDE-HYDRATE STRUCTURES

255 We used charge density calculations to identify mis-matches in UOHs by modifying an  
256 approach used earlier for uranyl germanates and uranyl silicates (Li et al. 2018). The charge  
257 density  $\rho$  associated with the anionic structural units was calculated as  $\rho = q_e \times Z/V$ . Here  $q_e$  is the  
258 effective charge of the structural unit, which is the formal charge  $q_f$  of the structural units  
259 modified by the number of hydrogen bonds,  $q_f + h \times 0.2$  (where  $h$  is the number of hydrogen  
260 atoms in the structural unit and  $0.2 \nu u$  is the assumed bond-strength of the corresponding H  
261 bond).  $Z$  is the number of formula units in each unit cell,  $V$  is the unit-cell volume ( $\text{\AA}^3$ ), and  $\rho$  is  
262 then the charge density associated with the structural unit. The charge density of the interlayer  
263 complex is calculated in the same way, taking into account the formal charge of the interlayer  
264 complex modified by the H-bonds emanating from it (Table 6). The majority of UOHs structures  
265 exhibit an excess of charge density associated with the interlayer complex (Fig. 9). Exceptions  
266 are the denser (polymerized) dehydrogenated structures such as for curite and spriggite. The  
267 outlying value of the synthetic PbUOH phase (Li and Burns 2000b) is due to the density of the  
268 bond-valence acceptors within the framework as compared to the relatively simple complex  
269 occupying the channels. The high charge density of the  $REE^{\text{III}}$ -containing UOHs is associated  
270 with structural units of the  $\alpha$ - $\text{U}_3\text{O}_8$  topology that are highly versatile. The variation of the charge  
271 densities for the  $\alpha$ - $\text{U}_3\text{O}_8$  type sheet is the largest within the most common topological types  
272 (Table 7).

273

### IMPLICATIONS

274 The new K,Pb-bearing uranyl-oxide hydroxy-hydrate kroupaite is particularly interesting  
275 due to ordering of monovalent and divalent cations of different stereochemistry in the interlayer  
276 region. Minerals provide unique insights into crystal chemical features that may be difficult to  
277 study *via* laboratory synthesis. Recent observations of natural samples, including kroupaite,

278 leesite and gauthierite from several localities demonstrate that uranyl-oxide-hydrate sheet anion  
279 topologies readily accommodate a range of heterovalent cations *via* unique configurations of their  
280 interlayers. Some uranyl-oxide-hydrate structures investigated here were found, based on analysis  
281 of their corresponding Voronoi-Dirichlet polyhedra, to be suitable for incorporation of large  
282 monovalent cations such as Cs<sup>+</sup>.

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497

498

## FIGURE CAPTIONS

499 Figure 1. Orange yellow aggregates of kroupaite on the surface of strongly altered uraninite.

500 Horizontal field of view is 2.5 mm (photo P. Škácha).

501

502 Figure 2. Crystal drawing of kroupaite in clinographic projection.

503

504 Figure 3a. Raman spectrum of kroupaite in the full-range ( $4500\text{--}12\text{ cm}^{-1}$ , split at  $2000\text{ cm}^{-1}$ ).

505 Figure 3b). Band decomposition in the Raman spectrum of kroupaite for  $\nu_1(\text{UO}_2)^{2+}$  in the region

506 from  $950\text{--}700\text{ cm}^{-1}$ .

507

508 Figure 4. Crystal structure of kroupaite viewed down  $[001]$ . The uranyl-oxide hydroxide sheets

509 (in yellow) alternate with the interlayer containing water oxygen (red), potassium (lavender) and

510 lead (orange). Unit-cell edges are outlined by black-solid lines.

511

512 Figure 5. Comparative view of the anion sheet topologies and  $\text{OH}^-$  distributions for uranyl-oxide

513 hydroxide-hydrate minerals with the fourmarierite topology. Black circles highlight vertices

514 containing  $\text{OH}^-$ , and bare vertices represent  $\text{O}^{2-}$ ; orange spheres represent  $\text{Pb}^{2+}$ , blue  $\text{K}^+$ , and

515 green  $\text{Na}^+$  atoms, respectively. Figure adapted from Klingensmith et al. (2007).

516

517 Figure 6. Ternary compositional plot for chemical analyses of kroupaite and related minerals.  
518 Analyses from additional set of kroupaite samples (labelled as JACH) are displayed to illustrate  
519 chemical substitutional trends.  $M^+ \leftrightarrow$  vacancy (with black dashed line): variability in composition  
520 between leesite (end-member) and schoepite;  $M^+ \leftrightarrow M^{2+}$  (black solid line): variability between  
521 leesite (end-member) and fourmarierite; the grey arrow points towards the substitution  
522 characteristic for intermediate series members and schoepite.

523

524 Figure 7. Voronoi-Dirichlet polyhedra (VDP) for interlayer cations in selected structures with  
525 corresponding VDP volumes ( $V_{VDP}$ ): a) kroupaite, K1 atom (lavender); Pb1 atom (orange); b)  
526 leesite; K1 atom (lavender); c) fourmarierite.

527

528 Figure 8. The size of cation polyhedra in the interlayers of uranyl-oxide hydroxy-hydrate  
529 structures: the volume ( $V_{VDP}$ ) of Voronoi-Dirichlet polyhedra versus the ionic radius. Outliers are  
530 labelled.

531

532 Figure 9. Charge-density matches in uranyl-oxide hydrate structures. The black solid line  
533 represents a linear fit to the data (equation and regression statistics given), and the dashed line  
534 represent an ideal match;  $a = -1$ ,  $b = 0$ .

535

536



Table 1. Analytical data for kroupaite (in wt. %), average of 6 analyses.

Constituent	Mean	Range	Stand. Dev.	Probe Standard	Normalised
Na <sub>2</sub> O	0.08	0.00–0.20	0.08	albite	0.08
K <sub>2</sub> O	2.14	1.99–2.32	0.10	sanidine	2.25
CaO	0.10	0.08–0.14	0.03	fluorapatite	0.10
PbO	1.84	1.64–2.46	0.31	vanadinite	1.93
CuO	0.41	0.00–0.72	0.28	lammerite	0.43
CoO	0.05	0.00–0.33	0.12	Co metal	0.05
Al <sub>2</sub> O <sub>3</sub>	0.02	0.00–0.12	0.04	sanidine	0.02
Bi <sub>2</sub> O <sub>3</sub>	0.25	0.00–0.51	0.19	Bi metal	0.26
UO <sub>3</sub>	80.67	78.80–82.24	1.15	uranophane	84.64
SO <sub>3</sub>	0.11	0.00–0.38	0.18	SrSO <sub>4</sub>	0.12
H <sub>2</sub> O*	9.65				10.12
Total	95.23				100.00

\*calculated as determined from the structure.

Table 2. Powder X-ray data ( $d$  in Å) for kroupaite.

$I_{\text{obs}}$	$d_{\text{obs}}$	$d_{\text{calc}}$	$I_{\text{calc}}$	$hkl$	$I_{\text{obs}}$	$d_{\text{obs}}$	$d_{\text{calc}}$	$I_{\text{calc}}$	$hkl$
<b>100</b>	<b>7.407</b>	7.4101	100	2 0 0	<b>21</b>	<b>2.0348</b>	2.0493	8	0 6 4
		6.4972	2	0 2 1			2.0372	11	6 2 4
		4.4916	3	3 1 1			2.0226	5	6 4 0
		3.7050	21	4 0 0			2.0166	5	2 0 8
<b>59</b>	<b>3.602</b>	3.6025	35	0 2 4	<b>11</b>	<b>1.9777</b>	1.9752	10	2 6 4
		3.5240	16	0 4 0			1.8525	3	8 0 0
<b>78</b>	<b>3.224</b>	3.2399	53	2 2 4	<b>10</b>	<b>1.7984</b>	1.8241	4	4 0 8
		3.1824	23	2 4 0			1.8012	4	0 4 8
		2.8581	2	5 1 1			1.7933	7	4 6 4
<b>16</b>	<b>2.572</b>	2.7655	3	2 4 3	<b>7</b>	<b>1.7474</b>	1.7503	5	2 4 8
		2.5828	15	4 2 4			1.7142	3	2 8 0
		2.5534	7	4 4 0			1.6475	5	8 2 4
		2.4700	4	6 0 0			1.6397	2	8 4 0
		2.3266	2	0 6 1			1.6388	3	2 8 3
<b>6</b>	<b>2.0886</b>	2.1660	2	1 4 6	<b>7</b>	<b>1.6471</b>	1.6358	2	2 6 7
		2.0957	4	0 0 8			1.6199	4	4 4 8
		2.0775	2	7 1 1			1.5980	2	6 0 8
							1.5929	2	2 2 10
					<b>5</b>	<b>1.5864</b>	1.5772	3	6 6 4

Table 3. Selected interatomic distances (Å) for kroupaite.

U1–O2	1.805(10)	U2–O11	1.789(11)	U3–O4	1.765(10)
U1–O7	1.799(11)	U2–O14	1.799(12)	U3–O8	1.800(10)
U1–O1 <sup>i</sup>	2.231(9)	U2–O1	2.222(8)	U3–O6	2.413(9)
U1–O6	2.693(10)	U2–O10 <sup>iii</sup>	2.548(9)	U3–O9	2.451(9)
U1–O10 <sup>ii</sup>	2.460(8)	U2–O12 <sup>iii</sup>	2.428(10)	U3–O11	2.533(9)
U1–O13	2.254(8)	U2–O18 <sup>ii</sup>	2.312(9)	U3–O12	2.224(9)
U1–O22	2.434(9)	U2–O22	2.445(9)	U3–O16	2.313(9)
<U1–O <sub>Ur</sub> >	1.80	<U2–O <sub>Ur</sub> >	1.79	<U3–O <sub>Ur</sub> >	1.78
<U1–O <sub>eq</sub> >	2.41	<U2–O <sub>eq</sub> >	2.39	<U3–O <sub>eq</sub> >	2.39
U4–O3	1.791(12)	Pb1–O4 <sup>iii</sup>	2.971(11)	K1–O4 <sup>vii</sup>	3.201(18)
U4–O5	1.797(10)	Pb1–O5 <sup>v</sup>	2.804(11)	K1–O6 <sup>vii</sup>	2.902(18)
U4–O1	2.252(8)	Pb1–O7 <sup>v</sup>	3.025(11)	K1–O8 <sup>xi</sup>	3.201(18)
U4–O6 <sup>iv</sup>	2.410(9)	Pb1–O7 <sup>iv</sup>	3.102(11)	K1–O15	2.86(2)
U4–O11	2.471(10)	Pb1–O8 <sup>v</sup>	2.803(11)	K1–O16 <sup>xi</sup>	3.28(2)
U4–O12	2.253(9)	Pb1–O10	2.732(11)	K1–O17	2.86(2)
U4–O19	2.538(9)	Pb1–O14	2.462(14)	K1–O18	2.69(3)
<U4–O <sub>Ur</sub> >	1.79	Pb1–O14 <sup>vi</sup>	3.036(14)	<K1–O>	3.00
<U4–O <sub>eq</sub> >	2.39	Pb1–O18 <sup>vii</sup>	3.006(16)		
		<Pb1–O>	2.88		

Symmetry codes: (i)  $-x+3/2, y-1/2, z$ ; (ii)  $-x+3/2, -y+1, z-1/2$ ; (iii)  $x, -y+3/2, z-1/2$ ; (iv)  $-x+3/2, y+1/2, z$ ; (v)  $x-1/2, -y+3/2, -z+1$ ; (vi)  $-x+1, -y+2, -z+1$ ; (vii)  $-x+1, -y+1, -z+1$ ; (viii)  $-x+1, y+1/2, -z+3/2$ ; (ix)  $x, -y+3/2, z+1/2$ ; (x)  $x+1/2, -y+3/2, -z+1$ ; (xi)  $x+1/2, y, -z+3/2$ ; (xii)  $-x+3/2, -y+1, z+1/2$ .

Table 4. The bond-valence analysis for krouapite.\*

	U1	U2	U3	U4	Pb1#	K1#	$\Sigma BV_{\text{anions}}$	Assignment
O1	0.68	0.69		0.65			2.01	O
O2	1.66						1.66	O
O3				1.71			1.71	O
O4			1.81		0.12	0.06	1.99	O
O5				1.69	0.17		1.87	O
O6	0.25		0.46	0.46		0.12	1.29	OH
O7	1.69				0.19		1.88	O
O8			1.68		0.17	0.06	1.91	O
O9	0.42	0.35	0.42				1.19	OH
O10		1.72			0.21		1.93	O
O11		0.45	0.36	0.41			1.21	OH
O12	0.64		0.69	0.65			1.98	O
O13		1.69					1.69	O
O14					0.48		0.48	H <sub>2</sub> O
O15						0.13	0.13	H <sub>2</sub> O
O16		0.57	0.57			0.05	1.18	OH
O17						0.13	0.13	H <sub>2</sub> O
O18					0.11	0.20	0.31	H <sub>2</sub> O
O19	0.44	0.43		0.35			1.22	OH
$\Sigma BV_{\text{cations}}$	5.78	5.89	5.99	5.92	1.46	0.73		

\*All values are in valence units (*vu*); # – site with a reduced occupancy;  $\Sigma BV$  – sum of the bond-valences; bond–valence parameters were taken from Gagné & Hawthorne (2015) and from Burns et al. (1997).

Table 5. Crystal-chemical characteristics for metal cations and their coordination environment in structures of selected minerals and compounds.

Structure	Atom	CN	Ionic radius (Å)	$V_{\text{VDP}}$ (Å <sup>3</sup> )
Kroupaite (this work)	K	9	1.55	23.331
	Pb	9	1.35	19.0646
Leesite (Olds et al. 2018)	K	9	1.55	19.6591
	Fourmarierite (Li and Burns 2000a)	Pb1	7	1.23
Gauthierite (Olds et al. 2017)	Pb2	9	1.35	18.3776
	Pb1	9	1.35	15.432
	Pb2	10	1.4	19.095
	Pb3	10	1.4	22.429
	Pb4	11	1.45	18.342
	K1	12	1.64	22.905
	K2	10	1.59	27.398
	K3	10	1.59	22.451
Na-metaschoepite (Klingensmith et al. 2007)	Na	5	1	9.987
CsUOH (Hill and Burns 1999)	Cs	10	1.81	29.668
CsUSi (Huang et al. 2003)	Cs	10	1.81	27.183
	Cs	9	1.78	28.804
	Cs	10	1.81	25.721
	Cs		1.88	30.621
	Wölsendorite (Burns 1999)	Pb1	8	1.29
	Pb2	11	1.45	17.354
	Pb3	11	1.45	16.974
	Pb4	9	1.35	16.971
	Pb5	11	1.45	17.055
	Pb6	11	1.45	18.604
	Pb7	7	1.23	14.645
	Pb8	10	1.4	22.77
	Vandendriesscheite (Burns 1997)	Pb1	9	1.35
	Pb2	10	1.4	18.035
	Sr-curite (Burns and Hill 2000a)	Sr1	10	1.36
	Sr2	11	1.4	15.927
	Sr-becquerelite (Burns and Li 2002)	Sr1	11	1.4
	Sr2	11	1.4	14.875
	Agrinierite (Cahill and Burns 2000)	Ca/Sr	9	1.31
Spriggite (Brugger et al. 2004)	Pb1	11	1.45	14.439
	Pb2	8	1.29	16.073
	Pb3	10	1.4	16.973
	Pb4	10	1.4	17.377
	Pb5	9	1.35	16.805
	Pb6	9	1.35	16.909
	Pb7	8	1.29	13.25

Rameauite (Plášil et al. 2016)	K1	12	1.64	20.283
	K2	12	1.64	19.433
	Ca	10	1.23	13.658
Richetite (Plášil 2017a)	Pb1	10	1.4	18.172
	Pb2	10	1.4	16.689
	Pb3	11	1.45	16.76
	Pb4	11	1.45	16.811
	Pb5	10	1.4	15.754
	Fe/Mg	6	0.74	8.867
	Pb6	10	1.4	16.253
	Pb7	9	1.35	16.763
KUOH (Burns and Hill 2000b)	Pb8	11	1.45	16.9
	K1	8	1.51	21.516
	K2	11	1.61	21.165
	K3	9	1.55	19.698
	K4	10	1.59	22.164
	K5	10	1.59	18.619
	K6	11	1.61	19.045
	K7	11	1.61	20.121
	K8	12	1.64	19.871
	K9	11	1.61	20.287
Becquerelite (Burns and Li 2002)	K10	10	1.59	21.009
	Ca	8	1.12	13.066
Billietite (Finch et al. 2006)	Ba	10	1.52	18.199
Compreignacite (Burns 1998)	K	7	1.46	11.198
Curite (Ghazisaeed et al. 2019)	Pb1	9	1.35	13.015
	Pb2	10	1.4	16.142
Masuyite (Burns and Hanchar 1999)	Pb1	10	1.4	16.135
	Pb2	12	1.49	16.577
Protasite (Pagoaga et al. 1987)	Ba	10	1.52	17.171
Sayrite (Plášil 2019)	Pb	9	1.35	16.682
Wyartite (Burns and Finch 1999)	Ca	7	1.06	17.746
Nollmotzite (Plášil et al. 2018)	Mg	6	0.72	8.657
PbUOH (Li and Burns 2000b)	Pb	8	1.29	14.733
K <sub>2</sub> CoUOH (Zhang et al. 2016)	Co	6	0.75	8.772
	K1	12	1.64	19.417
	K2	10	1.59	19.729
K <sub>2</sub> NiUOH (Zhang et al. 2016)	Ni	6	0.69	8.464
	K1	12	1.64	19.484
	K2	10	1.59	19.719
CsUOH (Kubatko et al. 2006b)	Cs	12	1.88	24.082
CsUV (Obbade et al. 2004)	Cs2	12	1.88	26.135
	Cs1	12	1.88	27.807
	Cs3	12	1.88	27.284

CsUMo (Krivovichev and Burns 2001)	Cs2	12	1.88	28.63
	Cs1	12	1.88	24.171
CsCoUSe (Wylie and Burns 2012)	Cs	9	1.78	15.689
CsAsU (Locock and Burns 2003)	Cs2	12	1.88	32.097
	Cs1	12	1.88	31.874
CsUFO (Dao 1972)	Cs1	11	1.85	26.894
	Cs2	10	1.81	26.166

CN – coordination number;  $V_{\text{VDP}}$  – volume of the corresponding Voronoi-Dirichlet polyhedron.

Table 6. Charge-densities of structural units and interlayer complexes in selected UOHs.

Structure	$q$	$q_{\text{effective}}$	$Z$	$V$	$\rho^-$	$\rho^+$
Schoepite (Plášil 2018b)	0	-1.2	8	3528.22	0	-0.00272
Metaschoepite (Weller et al. 2000)	0	-1.2	8	3429.97	0	-0.0028
Kroupaite (this work)	-2	-4	4	3502.3	-0.00228	-0.00457
Leesite (Olds et al. 2018)	-1	-2	8	3522	-0.00227	-0.00454
Fourmarierite (Li and Burns 2000a)	-2	-2.8	8	3280	-0.00488	-0.00683
Na-metaschoepite (Klingensmith et al. 2007)	-1	-2	8	3452.96	-0.00232	-0.00463
Gauthierite (Olds et al. 2017)	-3	-4.4	8	5917.8	-0.00406	-0.00595
Vandendriesscheite (Burns 1997)	-3	-5.2	8	8490	-0.00283	-0.0049
Curite (Ghazisaeed et al. 2019)	-6	-7.2	2	1367.78	-0.00877	-0.01053
Sr-curite (Burns and Hill 2000a)	-5.64	-6.912	2	1341.5	-0.00841	-0.0103
CsUOH (Hill and Burns 1999)	-3	-5.6	3	3871.16	-0.00232	-0.00434
KUOH (Burns and Hill 2000b)	-5	-6.8	4	3549.5	-0.00563	-0.00766
Compreignacite (Burns 1998)	-2	-3.2	2	1299.3	-0.00308	-0.00493
Wölsendorfitite (Burns 1999)	-14	-14.8	8	10982	-0.0102	-0.01078
Masuyite (Burns and Hanchar 1999)	-2	-2.4	2	599	-0.00668	-0.00801
Agrinierite (Cahill and Burns 2000)	-4	-4.8	8	4799.6	-0.00667	-0.008
PbUOH (Li and Burns 2000b)	-5	-7	4	3450	-0.0058	-0.00812
NaUOH (Li and Burns 2001)	-2	-2.4	4	967.33	-0.00827	-0.00992
NH <sub>4</sub> UOH (Li et al. 2001)	-3	-4	4	3512	-0.00342	-0.00456
NaUOH (Burns and Deely 2002)	-1	-2	2	715.97	-0.00279	-0.00559
Sr-becquerelite (Burns and Li 2002)	-2.54	-2.832	1	298.4	-0.00851	-0.00949
Becquerelite (Burns and Li 2002)	-2	-3.2	4	2563.1	-0.00312	-0.00499
CaUOH (Glatz et al. 2002)	-2	-2.8	2	649.6	-0.00616	-0.00862
Uranosphaerite (Colmenero et al. 2019)	0	-0.2	4	453.6	0	-0.00176
Billietite (Finch et al. 2006)	-2	-3.2	4	2614.7	-0.00306	-0.0049
Rameauite (Plášil et al. 2016)	-4	-4.8	4	2437.7	-0.00656	-0.00788
Nollmotzite (Plášil et al. 2018)	-2	-2.6	2	676.98	-0.00591	-0.00768
Sayrite (Plášil 2019)	-4	-4.4	2	964.46	-0.00829	-0.00912
Spriggite (Brugger et al. 2004)	-6	-6.4	8	4616	-0.0104	-0.01109
Richetite (Plášil 2017a)	-11	-13.8	2	3600.68	-0.00611	-0.00767
Protasite (Pagoaga et al. 1987)	-2	-2.4	2	617.497	-0.00648	-0.00777
Vandenbrandeite (Rosenzweig and Ryan 1977)	0	-0.8	2	254.929	0	-0.00628
K <sub>2</sub> CoUOH (Zhang et al. 2016)	-3	-5.6	1	2509.2	-0.0012	-0.00223
K <sub>2</sub> NiUOH (Zhang et al. 2016)	-3	-5.6	1	2500.3	-0.0012	-0.00224
La <sub>3</sub> UOH (Zhang et al. 2019)	-9	-10	2	1124	-0.01601	-0.01779
Nd <sub>3</sub> UOH (Zhang et al. 2019)	-9	-10	2	1097	-0.01641	-0.01823
U <sup>V</sup> UOH (Belai et al. 2008)	0	-1	4	1254	0	-0.00319
Ianthinite (Burns et al. 1997)	0	-2.4	4	2502.7	0	-0.00384



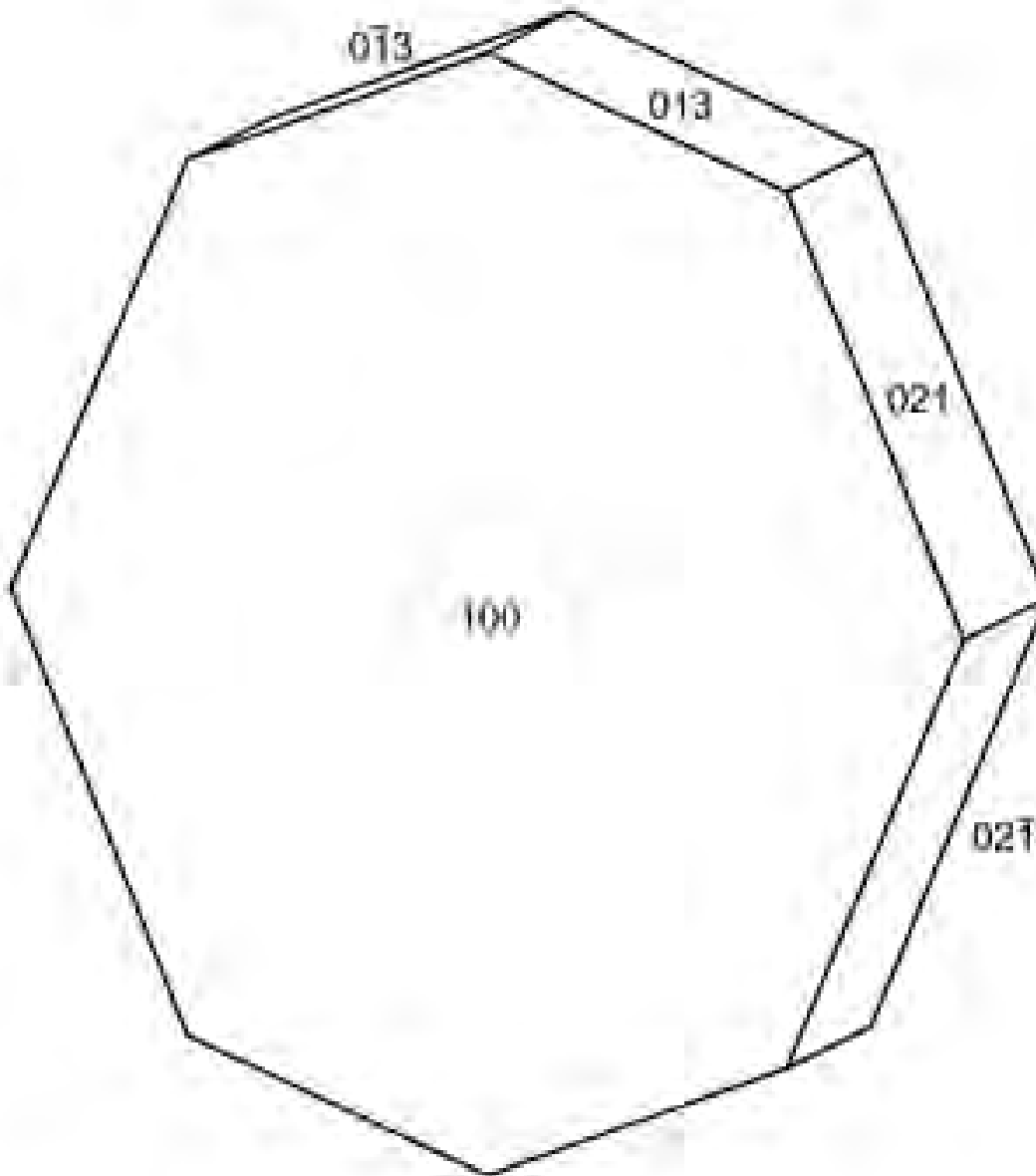
$q$  – charge;  $q_{\text{effective}}$  – effective charge (charge modified by the number and strength of H bonds);  $Z$  – formula units;  $V$  – unit-cell volume ( $\text{\AA}^3$ );  $\rho^-$  – charge-density of structural units ( $e \text{\AA}^{-3}$ );  $\rho^+$  – charge-density of interlayer complex ( $e \text{\AA}^{-3}$ ).

Table 7. Ranges in charge-densities for most common topological types of UOH structural units.

Topology	Charge density range ( $e\text{\AA}^{-3}$ )	Range in Lewis basicity ( $\nu$ )
$\alpha$ - $\text{U}_3\text{O}_8$	$2.23 \times 10^{-3}$ – $18.23 \times 10^{-3}$	0.14–0.23
$\beta$ - $\text{U}_3\text{O}_8$	$3.84 \times 10^{-3}$ – $11.09 \times 10^{-3}$	0.12–0.24
fourmarierite	$2.72 \times 10^{-3}$ – $6.83 \times 10^{-3}$	0.11–0.23



Fig. 1



**Fig. 2**

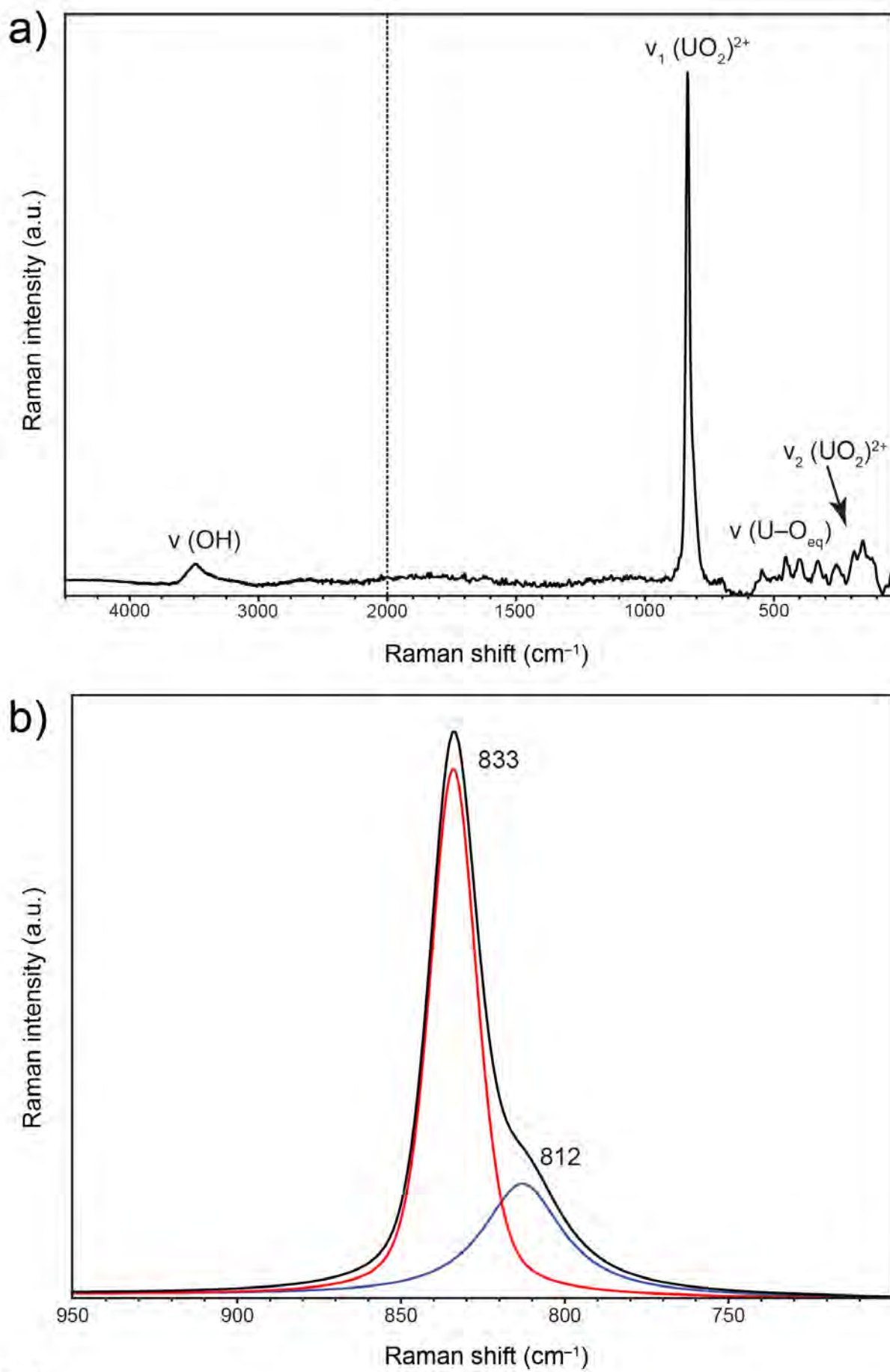


Fig. 3

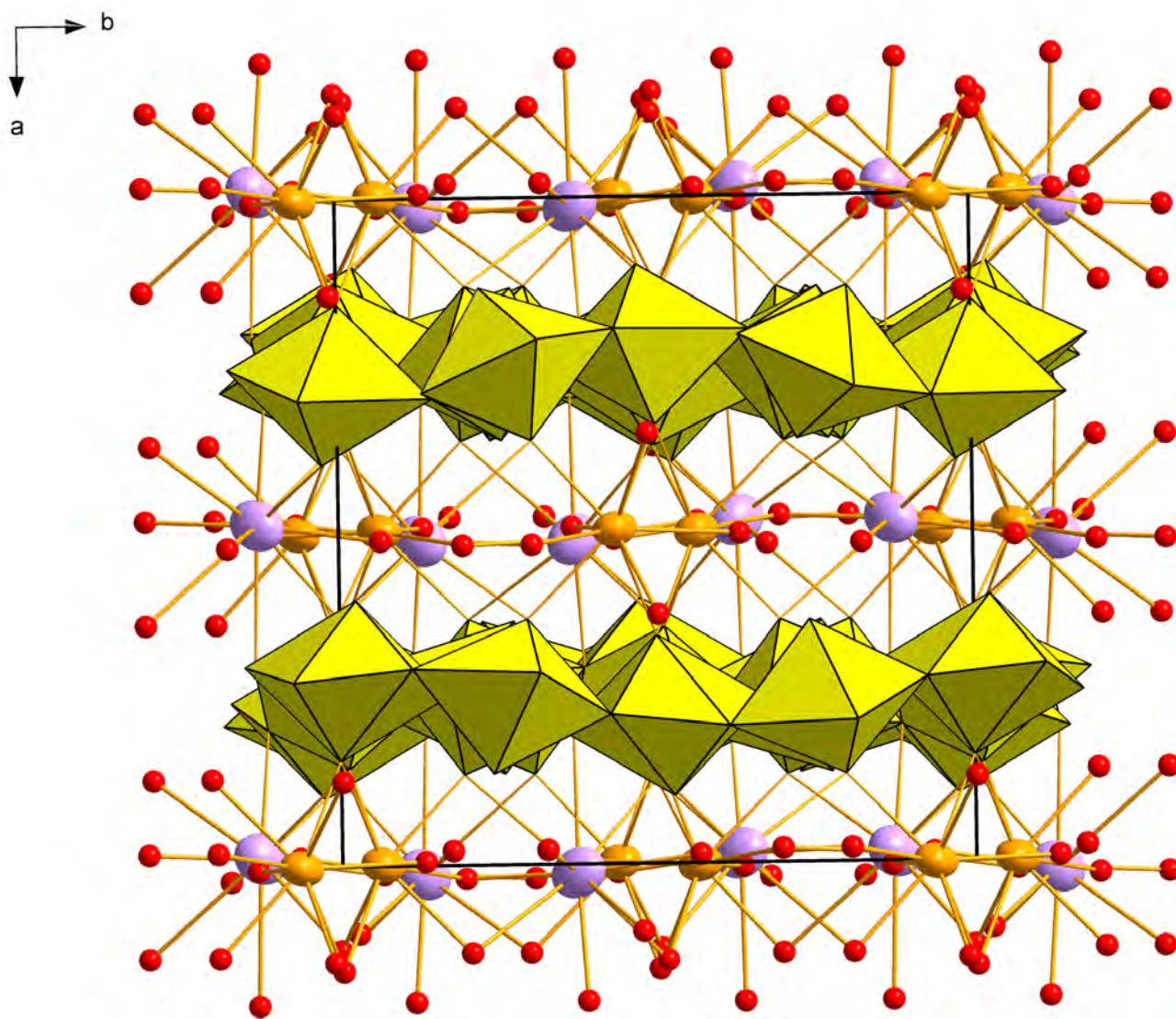


Fig. 4

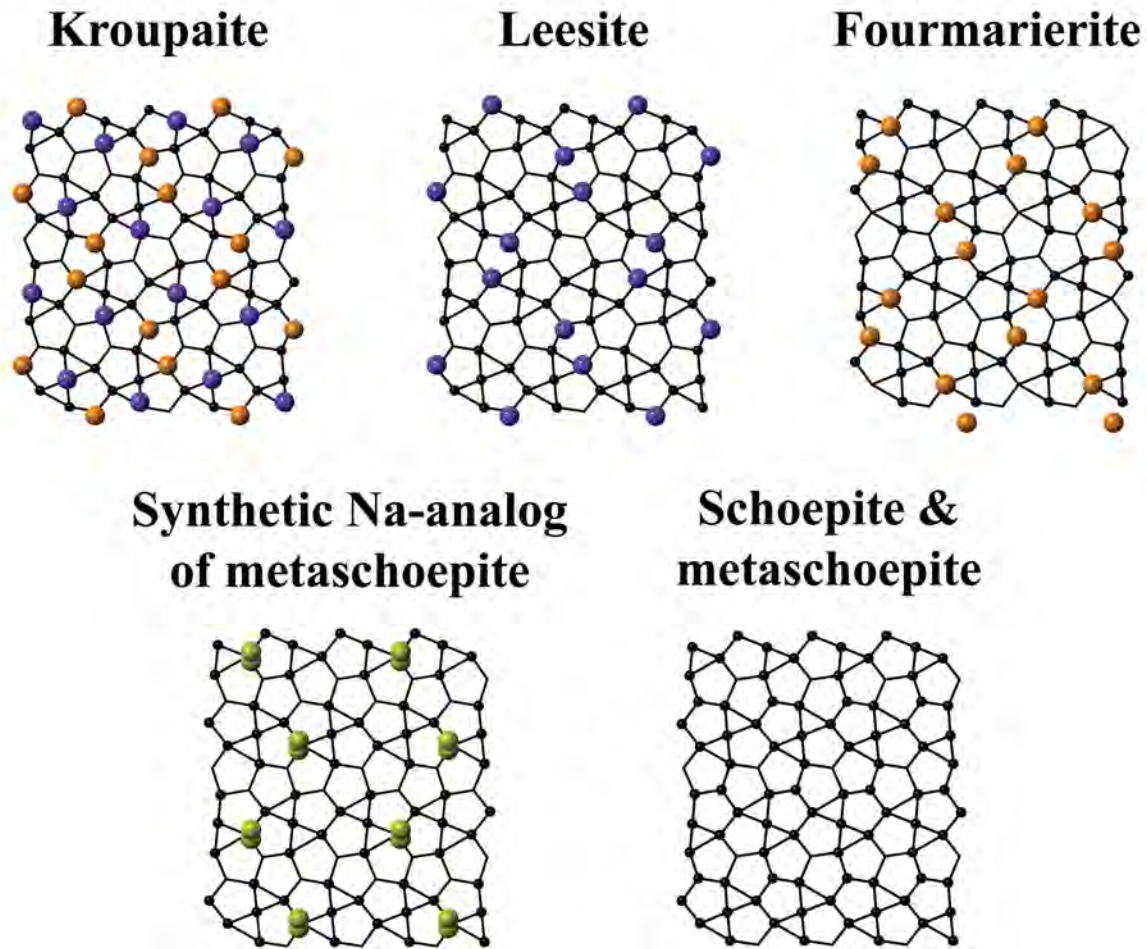


Fig. 5

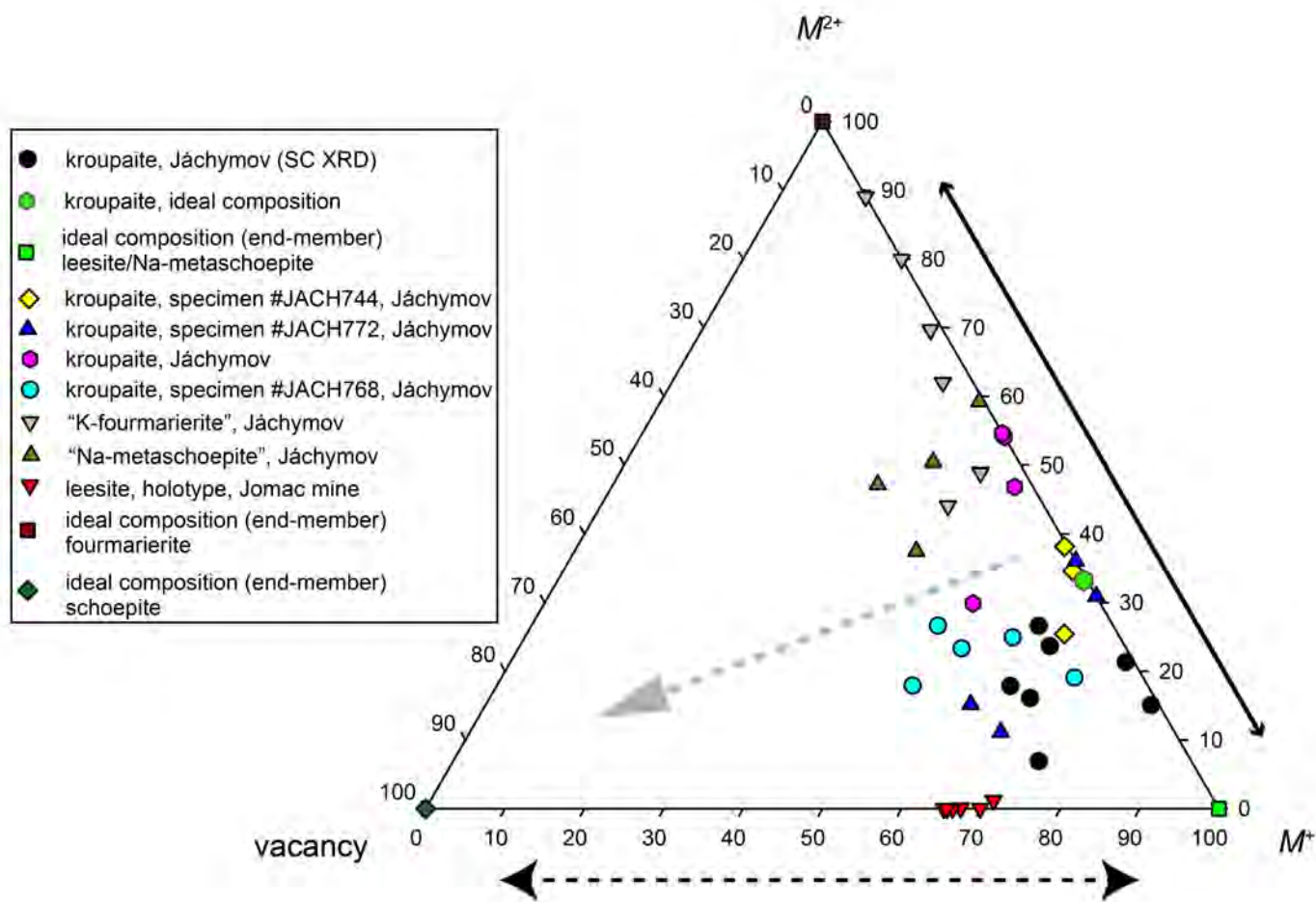


Fig. 6

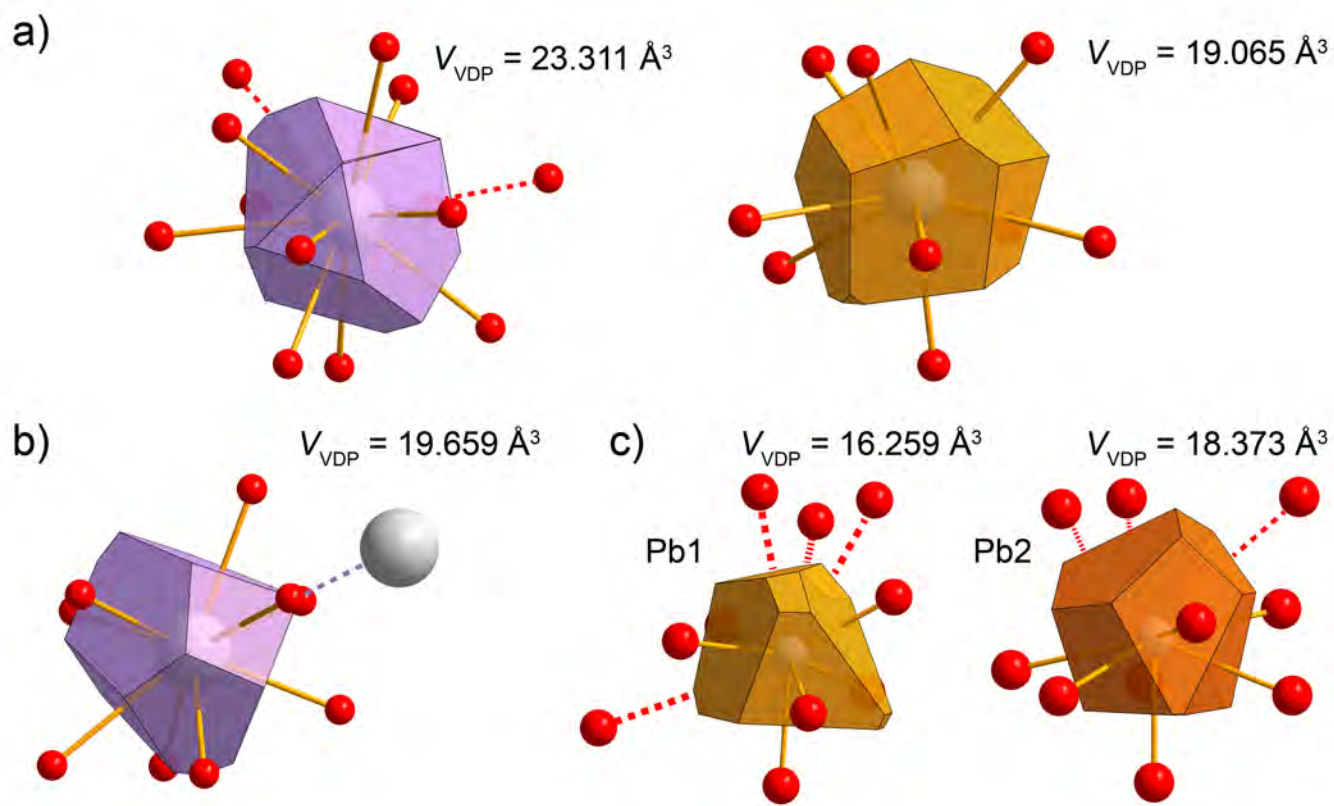


Fig. 7



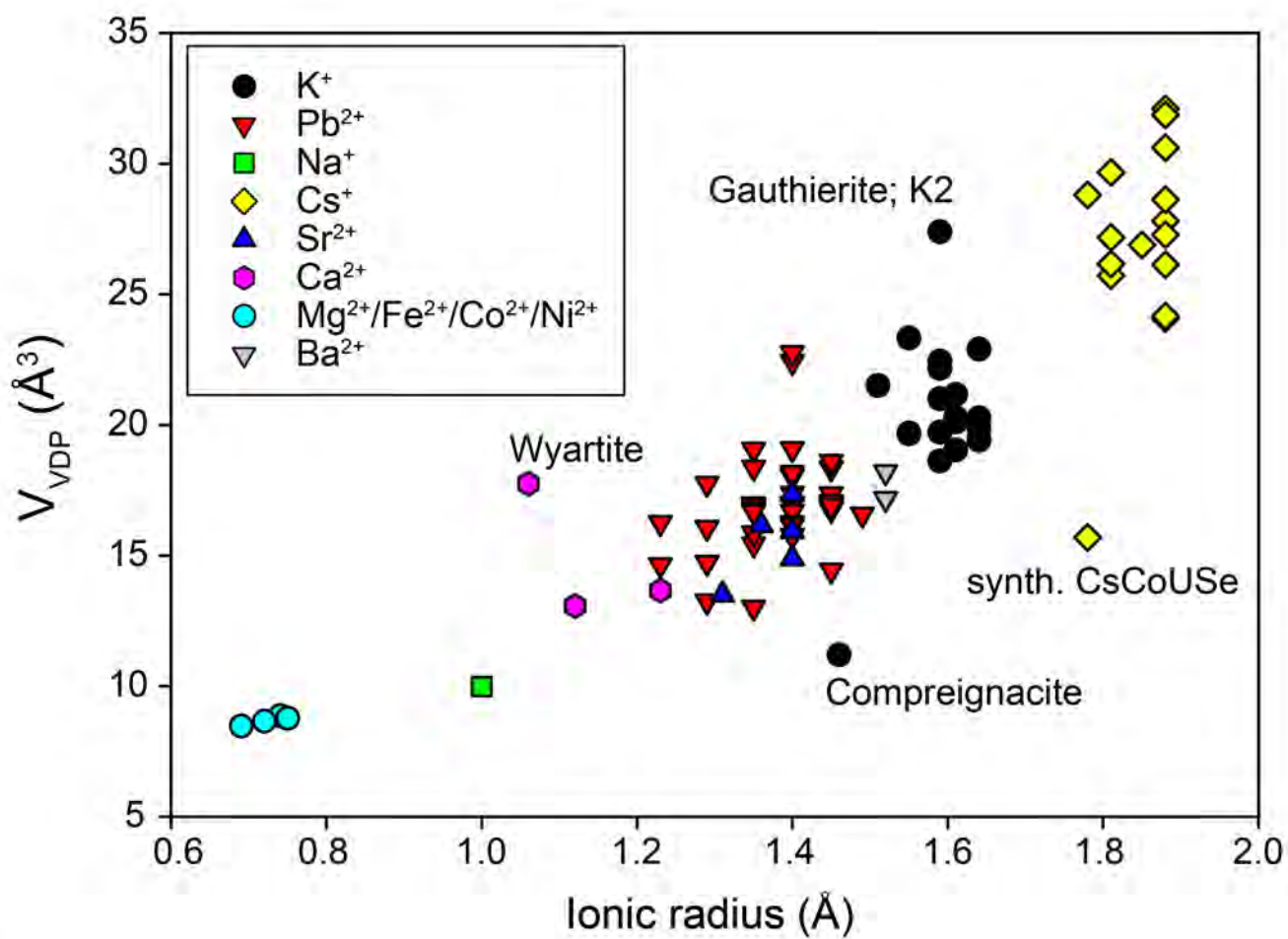


Fig. 8

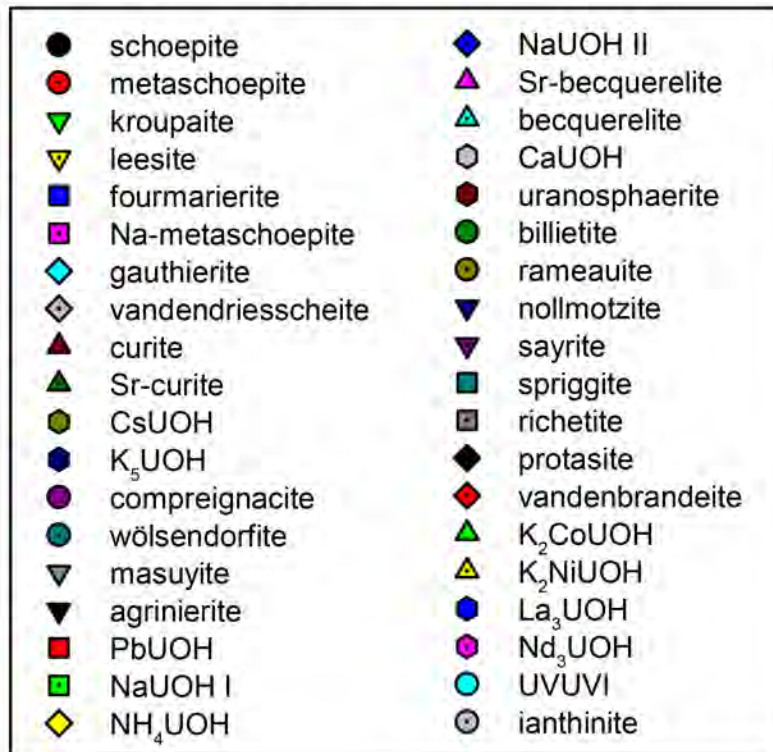
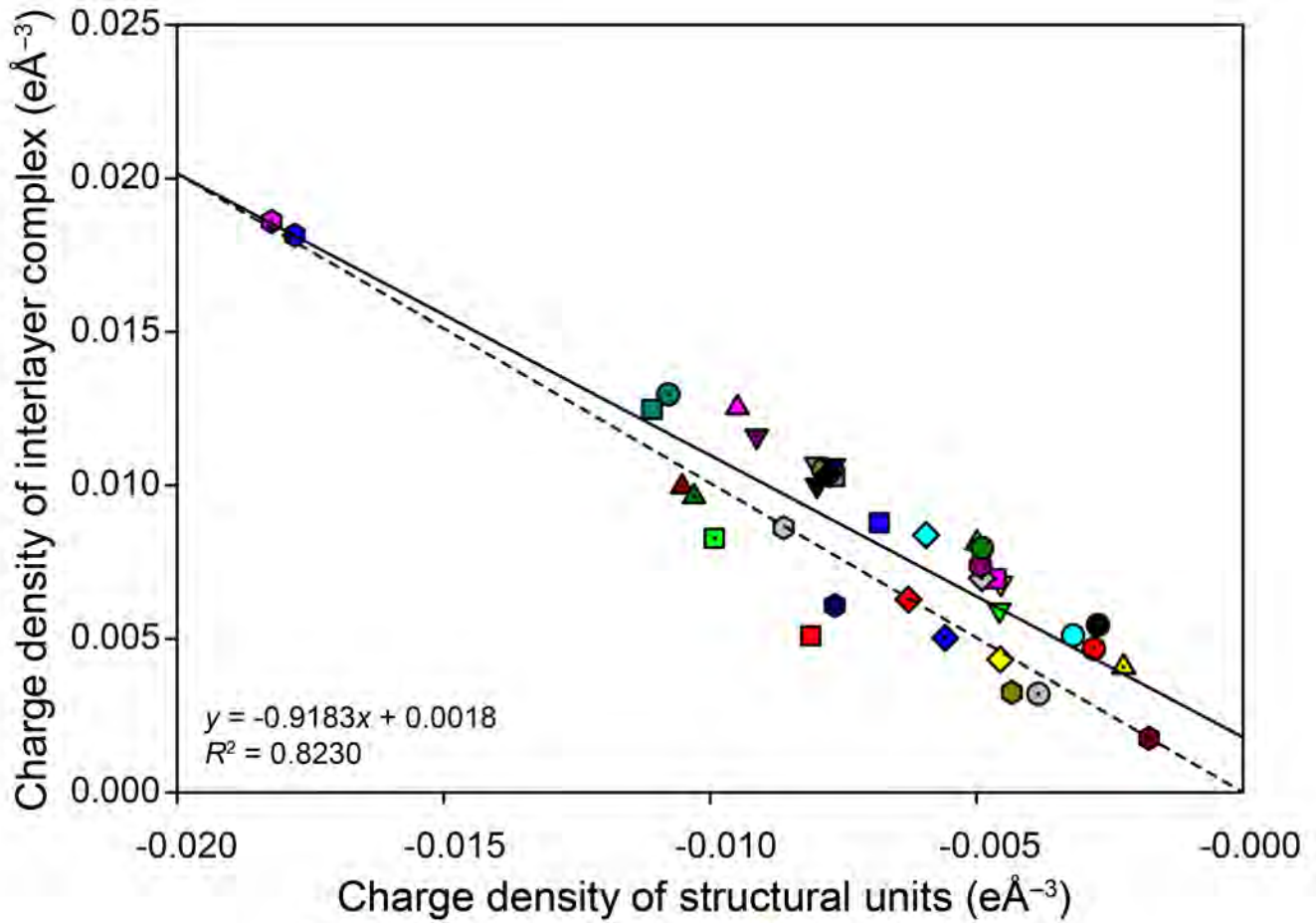


Fig. 9