

1 **Revision 3 correction date 08.05.2019**  
2 **Cation ordering, valence states and symmetry breaking in the crystal-**  
3 **chemically complex mineral chevkinite-(Ce). Recrystallization,**  
4 **transformation and metamict states in chevkinite**

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**ABSTRACT**

17 Annealing is commonly used in the recrystallization of metamict minerals in an attempt to  
18 reconstruct the original structure. Annealing at 750 °C of Nb-rich chevkinite-(Ce) from the  
19 Biraya rare-metal deposit, Russia, resulted in the structural transformation  $C2/m \rightarrow P2_1/a$ ,  
20 which defines chevkinite crystal stability in different environments. This transformation  
21 seems to be a rapid version of a naturally occurring process that possibly involves twinning of  
22 the crystals. Nb-rich chevkinite-(Ce) occurs naturally as two polymorphs, one with the  $C2/m$   
23 space group and the other with  $P2_1/a$ . The latter is the stable form under ambient conditions.  
24 There are some distinct differences in the values of the structural parameters, such as the  
25 average  $M-O$  distances or site scattering values of particular sites for both space groups,  
26 which can be associated with the redistribution of some lighter cations, mainly  $Mg^{2+}$ , within  
27 the crystal lattice. The use of complementary experimental techniques (electron probe

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28 microanalysis, X-ray diffraction, and photoelectron spectroscopy) has delivered information  
29 on the structure and transformation of a very complex, highly zoned and partially metamict  
30 solid solution. It should be useful in determining the structure of any mineral where cation  
31 disorder is present.

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33 **Keywords: chevkinite, annealing, crystal structure, metamict, recrystallization**

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## INTRODUCTION

36 Chevkinite-group minerals (CGM), comprising twelve species, are increasingly being  
37 recognised as accessory phases in a wide range of igneous and metamorphic rocks  
38 (Macdonald and Belkin 2002; Vlach and Gualda 2007; Carlier and Lorand 2008; Belkin et al.  
39 2009; Macdonald et al. 2009, 2012). The standard formula of CGM (Ito 1967),  
40  $A_4BC_2D_2(Si_2O_7)_2O_8$ , is often used for determining the sites occupied by particular cations.  
41 Based on structural features CGM can be divided to two subgroups: chevkinite and perrierite.  
42 The chevkinite type structure is shown in summary form in Figure 1. Together  $CO_6$  and  $DO_6$   
43 octahedra form sheets parallel to (001). Between these sheets are  $BO_6$  octahedra, linked to  
44 neighbouring  $BO_6$  and  $CO_6$  octahedra by sharing corners with  $(Si_2O_7)$  disilicate groups, and  $A$   
45 cations arranged in planar arrays with a Si(2)-centred tetrahedron inside each hexagonal array.

46 Due to the occurrence of CGM in chevkinite-type and perrierite-type forms, there are also  
47 discrepancies in the assignment of ions to particular  $B$ ,  $C$  and  $D$  sites. Previous studies of  
48 CGM have shown significant differences in the identification and names of unique sites of the  
49 crystal structure (particularly the  $B$ ,  $C$  and  $D$  sites). To clarify which site in the crystal  
50 structure corresponds to a site from the empirical formula of Nb-rich chevkinite-(Ce)

51 determined by electron microprobe, a short graphical representation of the sites is presented in  
52 Figure 1. An alternative naming of  $M(1)$ ,  $M(2)$ ,  $M(3)$  and  $M(4)$ , consistent with the  
53 nomenclature proposed by Hawthorne et al. (1995) and corresponding to  $B$ ,  $C$ ,  $D(1)$  and  $D(2)$ ,  
54 respectively, is given by Popov et al. (2001) and Sokolova et al. (2004). An exact definition of  
55 the sites in the crystal lattice is essential for a proper comparison with data available in the  
56 literature. An alternative description of the crystal structure of Fe-rich chevkinite-(Ce) was  
57 proposed by (Yang et al. 2002, 2007) with the unit cell origin shifted by the vector  $[0, 0, \frac{1}{2}]$ .  
58 Both descriptions are correct, but care must be taken when comparing the results in the  
59 literature. The coordinates  $(\frac{1}{2}, 0, 0)$  correspond to the  $B$  site in Yang's et al. (2007) crystal  
60 structure and to the  $D(1)$  in our description and those of Popov et al. (2001) and Sokolova et  
61 al. (2004), who name it the  $M(3)$  site.

62 A concentration of radioactive elements often results in full or partial metamictization of  
63 the crystal structure (Hawthorne et al. 1991). This phenomenon has often been recognised for  
64 CGM (Sokolova et al. 2004), for which Th is a significant minor constituent. Annealing is  
65 often used to reconstruct a radiation-damaged crystal structure (Popov et al. 2001). Some  
66 areas of the studied samples of Nb-rich chevkinite-(Ce) are also metamict due to a significant  
67 concentration of Th (Stachowicz et al. 2019).

68 Thermal annealing can also cause the redistribution of metal cations between  
69 crystallographic sites. Rapid redistribution of cations on thermal annealing has been found in  
70 numerous minerals, such as amphibole (Reece et al. 2002; Welch et al. 2008, 2010; Zema et  
71 al. 2011) and olivine (Redfern et al. 1996) using X-ray and neutron diffraction. In these cases,  
72 progressive heating in 20 °C steps from 200-800 °C resulted in rapid redistribution of divalent  
73 cations ( $Mg^{2+}$ ,  $Mn^{2+}$ ,  $Fe^{2+}$ ) within an hour. Consequently, it is likely that some cation  
74 redistribution will occur in chevkinite annealed at  $T > 600$  °C for 24 hours.

75 Chevkinites are known to have vacancies at metal sites in the crystal structure, having  
76 been reported for the *A*, *B*, *C* and *D* sites (Yang et al. 2002), but at the *C* (*M*(2)) site only,  
77 varying from being minor (Popov et al. 2001; Sokolova et al. 2004) to the 50% vacancies at  
78 this site recorded in the crystal structure of delhuyarite-(Ce); this level of vacancy is species-  
79 defining (Holtstam et al. 2017).

80 There is also some uncertainty in the literature as to which space group(s) CGM belong  
81 to.  $P2_1/a$  was determined by Čech et al. (1983), Haggerty and Mariano (1983), Miyawaki et  
82 al. (2002) and Xu et al. (2008). Space group  $C2/m$  was proposed by Gottardi (1960), Yang et  
83 al. (1991), Popov et al. (2001), Yang et al. (2002, 2012) and Liziero (2008), whereas  
84 Miyajima et al. (2002) suggested that the structure of matsubaraite was in the pseudo- $C2/m$   
85 group.

86 A sample of Nb-rich chevkinite-(Ce) from the Biraya rare-metal deposit, Russia, was  
87 studied by Stachowicz et al. (2019) to determine its crystal structure and to evaluate the role  
88 of Nb in the chevkinite group. Chevkinite from this locality is the most Nb-rich yet known.  
89 Stachowicz et al. (2019) identified a new substitution mechanism,  $2^D\text{Ti}^{4+} \rightarrow ^D\text{Nb}^{5+} + ^D\text{Ti}^{3+}$ ,  
90 which, together with the substitution  $^C\text{Fe}^{3+} + ^D\text{Ti}^{4+} \rightarrow ^C\text{Fe}^{2+} + ^D\text{Nb}^{5+}$  leads to substantial Nb  
91 enrichment. The present paper focuses on the nature of the  $P2_1/a$  phase in Nb-rich chevkinite-  
92 (Ce) from the same locality. On the basis of our new data, a possible relationship between the  
93  $P2_1/a$  and  $C2/m$  space groups is proposed.

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## 95 **SAMPLE AND ANALYTICAL METHODS**

96 The Nb-rich chevkinite-(Ce) analysed here is from the Biraya rare-metal deposit, located in  
97 the north of the Irkutsk district, Transbaikalia, Russia ( $57^\circ52'51''\text{N}$ ,  $116^\circ42'30''\text{E}$ ). Nine single  
98 crystals were examined by single-crystal X-ray diffraction. Mineral compositions in crystal 1

99 were determined by electron microprobe at the Inter-Institute Analytical Complex at IGMiP  
100 Faculty of Geology, University of Warsaw, using a Cameca SX-100 microprobe equipped  
101 with four wavelength analysers. The detailed results are given in a companion article  
102 (Stachowicz et al., 2019). There is considerable compositional variation related to textural  
103 variations. Variation in the oscillatory zoned area is modest, e.g. 8.04-10.09 wt% Nb<sub>2</sub>O<sub>5</sub>. In  
104 that zone, the average analytical total is 98.03 wt%; however, a notable feature of the other  
105 zones is the low oxide totals, down to 88.41 wt%. Such low totals are commonly associated  
106 with hydrothermal alteration, consistent in this case with the textural evidence that the low-  
107 total zones appear to be replacing the oscillatory zones. The partial metamictization of the Nb-  
108 rich chevkinite-(Ce) crystals was confirmed by the results of series of X-ray experiments on  
109 natural and annealed crystals. The experimental section contains details of the annealing  
110 procedure. An analysis of the valences of Ce, Ti and Fe, investigated by X-ray photoelectron  
111 spectroscopy (XPS) was also presented (Stachowicz et al., 2019). Cerium is present as Ce<sup>3+</sup>  
112 only, and iron as Fe<sup>2+</sup> and Fe<sup>3+</sup> in the ratio 1:1.84. Titanium is present in three valence states,  
113 +4, +3, +2, with ratios of 5:5:2, respectively. The EPMA analysis of unaltered parts of crystal  
114 1 gave the following empirical formula:



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## 117 **CRYSTAL STRUCTURE DETERMINATION**

### 118 **Experimental**

119 A full Ewald sphere of reflections was collected to  $\theta = 30^\circ$  for two crystals (1 and 6) using a  
120 KUMA KM4CCD  $\kappa$ -axis diffractometer equipped with Opal CCD detector and graphite-  
121 monochromated MoK $\alpha$  radiation. Another six crystals (2-5, 7, 8) from the same sample were  
122 analysed on an Agilent SuperNova diffractometer, equipped with a Mo K $\alpha$  micro-focus X-ray

123 source and an EOS CCD detector. Finally, a series of single-crystal XRD experiments on  
124 crystal 9 was carried out with an Agilent XcaliburE diffractometer equipped with an EOS  
125 detector and MoK $\alpha$  radiation source.

126 Details of investigation of natural crystals 1 and 2 are given in the complementary paper  
127 (Stachowicz et al., 2019). Here, we present the results of the structural analysis of five  
128 additional natural crystals (3, 6, 7, 8, 9) and four annealed crystals (1, 4, 5, 9). The annealing  
129 of crystals 1, 4 and 5 was performed in a vacuum furnace at 750 °C, for 24 hours. The crystals  
130 were cooled to room temperature within three hours. A series of single-crystal XRD  
131 experiments on crystal 9 was carried out (i) on a natural, unheated crystal; (ii) after annealing  
132 at 500 °C for 24 h; (iii) after annealing at 600 °C for 18 h; (iv) after annealing at 600 °C for a  
133 further 24 h; (v) after annealing at 650 °C for 24 hours. Before each annealing cycle the  
134 crystal was enclosed in an evacuated borax glass capsule.

135 All data sets were corrected for Lorentz and polarization effects. A numerical absorption  
136 correction was applied in each case based upon crystal shape. Data reduction and analysis  
137 were carried out with the program CrysAlisPro® (Rigaku-Oxford Diffraction).

138 Crystal structures were solved by direct methods and refined using SHELXL (Sheldrick  
139 2008) as implemented in Olex2 (Dolomanov et al. 2009) and WinGX (Farrugia 2012). The  
140 refinements were based on  $F^2$  for all reflections, except those with negative intensities.  
141 Weighted  $R$  factors ( $wR$ ) and all goodness-of-fit ( $S$ ) values are based on  $F^2$ . Conventional  $R$   
142 factors are based on  $F$  with  $F$  set to zero for negative  $F^2$ .  $R$  factors based on  $F^2$  are about twice  
143 as large as those based on  $F$ . Scattering factors for neutral atoms were taken from the  
144 International Tables for Crystallography Vol. C (Wilson 1992).

145 In order to obtain better geometry and ADPs (Sanjuan-Szklarz et al. 2016), higher-  
146 resolution datasets were collected than recommended by the International Union of  
147 Crystallography (IUCr). The highest residual electron density maxima (even up to 9.4 eÅ<sup>-3</sup> for

148 crystal 2) are located *c.a.* 0.6-0.7 Å from the heavy *REE* atoms for all crystal structures. These  
149 values can be reduced ( $4.8 \text{ e}\text{\AA}^{-3}$  for crystal 2) when the resolution is decreased to  $0.6 \text{ \AA}^{-1}$ , (as  
150 recommended by IUCr), consistent with the cause of the high residual being associated with  
151 termination ripples in the Fourier synthesis, rather than being due to incomplete modelling of  
152 a contribution from non-bonded electrons or a split site.

153 In this study, the origin of the unit cell for all crystal structures was chosen such that the  
154 *B* site corresponds to the Wyckoff *2d* unique position for space group *C2/m* and to the *2b*  
155 position for space group *P2<sub>1</sub>/a*. The unique site *C* refers to position *4e* for both space groups.  
156 The *D* site refers to two independent Wyckoff positions: *2a*, *2b* for *C2/m* and *2a*, *2c* for *P2<sub>1</sub>/a*.  
157 Our choice is analogous to that used by Sokolova et al. (2004).

#### 158 **Crystal structure data**

159 Emphasis is given to the transformations of crystal 1 for which complementary X-ray  
160 datasets before and after annealing, and numerous electron probe microanalyzer (EPMA)  
161 analyses were obtained. Subsequent X-ray experiments on the remaining crystals (2-9)  
162 corroborate a general trend. The exact allocation of cations to crystallographic sites for  
163 compositions determined by EPMA is hindered for several reasons. The empirical formula for  
164 Nb-rich chevkinite-(Ce) crystal 1 given by Stachowicz et al. (2019)  
165  $^A(\text{Ca}_{0.18}\text{Sr}_{0.13}\text{Na}_{0.16}\text{La}_{1.2}\text{Ce}_{2.02}\text{Pr}_{0.16}\text{Nd}_{0.42})^{BCD}(\text{Fe}_{1.91}\text{Mg}_{0.16}\text{Al}_{0.13}\text{Ti}_{1.22}\text{Nb}_{1.11})(\text{Si}_{1.99}\text{O}_7)_2\text{O}_8$ , is the  
166 average of all microprobe analyses, and is not representative because the crystal is partially  
167 metamict, due to its significant Th content. Partial recrystallization occurred during the  
168 annealing process, after which stronger scattering of X-rays by crystals 1 and 9 was observed.  
169 Moreover, the refined site scattering values (ssv= electrons per site) of the *A*, *B*, *C* and *D* sites  
170 changed. The transformation *C2/m* → *P2<sub>1</sub>/a* was also observed. As described in the

171 Introduction, it is also likely that thermal annealing at 600-700 °C is involved in redistribution  
172 of some cations.

173 Initially, ssv were refined on the basis of the X-ray diffraction data. We found that an  
174 identical allocation of cations in both the  $P2_1/a$  and  $C2/m$  crystal structures is inconsistent  
175 with the refined site occupancies:  $A$ ,  $B$ ,  $C$  and  $D$  ssv sum to different values in the natural  
176  $C2/m$  and transformed, annealed  $P2_1/a$  crystal 1. We carried out several X-ray experiments on  
177 both annealed and untreated natural crystals of Nb-rich chevkinite-(Ce) and found a clear  
178 correlation between the changes in the refined X-ray crystal structure parameters (Table 1)  
179 and the temperature of annealing.

180 The structural parameters for natural crystals 1, 6, 7, 8 and 9 listed in Table 1 are very  
181 consistent. Volumes of the first coordination spheres of cations at the  $B$ ,  $C$  and  $D$  sites are  
182 similar for these ( $C2/m$ ) crystals.  $BO_6$  octahedra all have volumes of  $\sim 12 \text{ \AA}^3$ .  $D(1)$  and  $D(2)$   
183 octahedra have equal volumes of  $\sim 11 \text{ \AA}^3$ . After annealing, the volume of the  $BO_6$  octahedron  
184 increases markedly to  $12.6 \text{ \AA}^3$ , whereas the volumes of  $CO_6$ ,  $D(1)O_6$  and  $D(2)O_6$  octahedra  
185 remain unchanged. However, ssv values change for all  $A$ ,  $B$ ,  $C$  and  $D$ , being least for the  $C$   
186 site. Crystals 2 and 3 are also natural, but their crystal structure parameters are comparable to  
187 those obtained for the annealed and transformed samples. The analysis of reflections (Figure  
188 S1) also proved that the space group for this case is rather  $P2_1/a$ .

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## DETERMINATION OF SPACE GROUPS

### 191 Consequences of crystal annealing; decrease of symmetry

192 In order to determine the space group(s) in which CGM crystallize the same single crystal  
193 fragment of Nb-rich chevkinite-(Ce) which was investigated using X-ray radiation  
194 (Stachowicz et al., 2019) was annealed at 750 °C for 24 hours, and then cooled to room



195 temperature within 3 hours. A new set of XRD data was then collected on our single crystal  
196 X-ray diffractometer. Quasi-precession images of the  $(1kl)$  reciprocal lattice layer (Figure 2)  
197 reconstructed from the full data collection prove the presence of the transformation from  
198  $C2/m$  space group to  $P2_1/a$ . Reflections violating  $C2/m$  symmetry ( $h + k = 2n + 1$  for  $hkl$ ) are  
199 shown inside the red rectangles in Figure 2. The reconstructed diffraction patterns for the  
200 fourteen X-ray experiments on Nb-rich chevkinite-(Ce) crystals are given in Supplementary  
201 Figure S1, together with information on  $\langle I/\sigma(I) \rangle$  for all violators.

202 The natural crystals 2 and 3 also transformed to  $P2_1/a$  symmetry and only these two  
203 crystals exhibit a significant twinning out of all tested samples (1-9). It is, therefore, possible  
204 that the mechanism of natural transformation involves twinning of the crystals.

205 Annealing of the Nb-rich chevkinite-(Ce) at  $750^\circ\text{C}$  caused a transition from space group  
206  $C2/m$  to  $P2_1/a$  and we have suggested that this transformation seems to be a rapid version of a  
207 naturally occurring process (Stachowicz et al. 2019). Evidence from the natural rocks is  
208 equivocal. Perrierite, which generally forms at higher temperatures than chevkinite  
209 (Macdonald and Belkin 2002; Macdonald et al. 2019), commonly but not invariably  
210 crystallizes in space group  $P2_1/a$ ; Sr-Zr perrierite-(Ce), for example, has a  $C2/m$  symmetry  
211 (Stachowicz et al. 2014). Attempting to relate CGM space group type to temperature of  
212 formation is hindered by the difficulties in estimating temperatures of the common host rocks,  
213 such as metasomatites, skarns and pegmatites. Such information would be better sought using  
214 phenocrysts in extrusive rocks for which temperatures have been estimated. A further  
215 complication is that we have observed the reverse transformation from  $P2_1/a$  to  $C2/m$  in a  
216 compositionally simpler perrierite from Nettuno, Italy, induced by pressures up to 6 GPa.

217 The Bärnighausen tree (Figure 3) served as a test, validating the transition by means of  
218 Group Theory. It summarises a transition pathway and was constructed using the  
219 WYCKSPLIT (Kroumova et al. 1998) software implemented into the Bilbao Crystallographic

220 Server (Aroyo et al. 2006a, 2006b). The largest shift of atoms is expected for light atoms that  
221 are released from a symmetry element (O(3) and O(4)). The rotation of the SiO<sub>4</sub> tetrahedron,  
222 that contains O(3) and O(4) oxygen atoms, results in a change of the coordination of the A(2)  
223 site (see Table 1). A detailed discussion of the Bärnighausen tree and the symmetry relations  
224 in Nb-chevkinite-(Ce) is given in the Supplementary Data.

225

## 226 **ASSIGNMENT OF POSITIONS FOR CATIONS**

227 In order to determine which atoms occupy *A*, *B*, *C* and *D* sites, one can relate the values of the  
228 ionic radii (Shannon 1976) to the volumes of the first coordination polyhedra of each site,  
229 which can be calculated from the X-ray crystal structure using the algorithm introduced by  
230 Robinson et al. (1971). This approach may be useful especially in cases of a high variability  
231 of elements occupying the same crystallographic sites in a mineral, which is the case for Nb-  
232 rich chevkinite-(Ce). The volumes of octahedra were calculated in Platon software (Spek  
233 2009) and the volumes of other polyhedra in Vesta software (Momma and Izumi 2011). The  
234 refined (against the X-ray data) *A*, *B*, *C* and *D* site scattering values sum to significantly  
235 different values for *C2/m* and *P2<sub>1</sub>/a* crystal structures. The MO<sub>6</sub> first coordination sphere  
236 octahedra (especially the BO<sub>6</sub> octahedra) also differ significantly in volume (Table 1).

237 The *A* sites are occupied by *REE*, Ca and Na atoms. As is common in CGM, there is an  
238 excess of elements in the *A* site. Sokolova et al. (2004) suggested the presence of small  
239 amounts of Ca (0.05 atoms per formula unit; apfu) in the *B* site of chevkinite-(Ce) from the  
240 Khaldzan Buragtag alkali granite, Mongolia.

241 The BO<sub>6</sub> octahedron is the largest of all MO<sub>6</sub> octahedra in CGM. The ions having the  
242 largest radii (except larger *REE* cations from the *A* sites) should be considered to occupy the *B*  
243 site. The ssv values of 26 electrons for natural (*C2/m*) crystals 1, 7, 8 suggest the predominant  
244 occupancy of Fe<sup>2+</sup> (ionic radius (i.r.) of 0.78 Å), which is in agreement with the literature. The

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245 ssv values for crystals 6 and 9 suggest the possible occupation of elements heavier than Iron.  
246 Following the suggestion of Sokolova et al. (2004), due to the excess of cations commonly  
247 assigned to the *A* site, some can occupy also the *B* site of Nb-rich chevkinite-(Ce). Among  
248 heavier elements, only Th could fit in to this site: Th-O bond length varies between 2.15-2.62  
249 Å for crystal structures with Th-O<sub>6</sub> coordination octahedra (Serezhkina et al. 2017). Figure 4  
250 presents the BO<sub>6</sub> coordination with atoms shown as thermal ellipsoids. Mixed occupancy can  
251 be registered as a larger  $U_{iso}$  value and prolate/oblate anisotropic displacement ellipsoid.  
252 However, a positional disorder of a single atom species must also be considered. To reach the  
253 ssv of 29 for crystal 9, 0.08 *apfu* of Th<sup>4+</sup> in the *B* site is needed and 0.04 *apfu* to reach an ssv  
254 of 27.6 for crystal 6. Crystal 9 was also much more metamict than other crystals (see  
255 Supplementary Figure S1 with the weakest scattering of X-ray reflections, despite the longest  
256 exposure time), so a larger concentration of Th is expected here. The mechanism of Th  
257 incorporation into the *B* site may be the substitution:  ${}^B\text{Fe}^{2+} + {}^A\text{Ce}^{3+} \rightarrow {}^B\text{Th}^{4+} + {}^A\text{Na}^+$ .

258 With the transformation to a lower symmetry space group the volume of BO<sub>6</sub> increases on  
259 the average by 0.6 Å<sup>3</sup> and the ssv value drops by *ca.* 2 electrons. These results show that  
260 heating induces a reorganisation or substitution of cations. The lighter Mg<sup>2+</sup> (i.r. = 0.72Å) ions  
261 substitute for Th<sup>4+</sup> or part of the Fe<sup>2+</sup>.

262 The *C* site has the smallest volume of all MO<sub>6</sub> coordination octahedra (Table 1) for Nb-rich  
263 chevkinite-(Ce) (for both structure types). It is occupied by Fe<sup>3+</sup> (i.r. = 0.65 Å), Nb<sup>5+</sup> (i.r. =  
264 0.64 Å) and Al<sup>3+</sup> (i.r. = 0.54 Å) ions. This site shows the smallest changes due to  
265 transformation, both in CO<sub>6</sub> volume and ssv values.

266 The two *D*(1) and *D*(2) sites have identical DO<sub>6</sub> volumes, yet differ with ssv values of 20.7  
267 and 24.2 in average, respectively, for crystals of *C2/m* symmetry. We assigned Ti<sup>3+</sup> (i.r. = 0.67  
268 Å), Ti<sup>4+</sup> (i.r. = 0.60 Å), Nb<sup>5+</sup> and Mg<sup>2+</sup> into these sites. In the transformed crystals (*P2<sub>1</sub>/a*  
269 symmetry), Mg<sup>2+</sup> is absent from these sites which is reflected in the increase of ssv to 24.7

270 and 26.8 in average, for  $D(1)$  and  $D(2)$  respectively. The  $DO_6$  octahedra have the largest  
271 volumes (our calculations) among all chevkinites of known crystal structure. We interpret this  
272 as a structural indication of the presence of  $Ti^{3+}$  ( $C2/m$  and  $P2_1/a$ ) and  $Mg^{2+}$  ( $C2/m$ ) at the  $D$   
273 sites of the Nb-rich chevkinite-(Ce). The mechanism of  $Ti^{4+}$  substitution in the  $D$  sites is also  
274 proposed as:  $2Ti^{4+} \rightarrow Nb^{5+} + Ti^{3+}$ ;  $2Ti^{4+} + O^{2-} \rightarrow Nb^{5+} + Mg^{2+} + OH^- + vac.$

275 Niobium is distributed among the  $C$  and  $D$  sites. Its presence is shown in larger values of  
276  $ssv$  because it is masked by the presence of vacancies and lighter elements,  $Al^{3+}$  at the  $C$  and  
277  $Mg^{2+}$  at the  $D$  site. With the migration of Magnesium to the  $B$  site in the  $P2_1/a$  crystal  
278 structure the presence of Nb is revealed in the increasing values of  $ssv$  of the  $D$  sites.

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## IMPLICATIONS

281 The recognition that the analysis of the systematic extinction of reflections forbidden in a  
282 certain space group can be equivocal demands testing. Such a test, proposed here, is the  
283 values of the volumes of  $BO_6$  octahedra and atomic displacement parameters  $U_{eq}$ . A  
284 convenient tool in the evaluation of indicators of the crystal symmetry is construction of the  
285 Bärnighausen tree. The multidisciplinary crystal-chemical approach used here should be of  
286 value in determining the structure of all minerals with cation disorder. This may be  
287 particularly relevant to REE-bearing phases due to the increased use of REE in technological  
288 applications and the accompanying interest in REE exploitation.

289 The possible existence of a new end member in CGM has been identified with the substitution  
290 mechanism given for  $Ti^{3+}$  and  $Nb^{5+}$  in the  $D$  sites:  ${}^A Ce_4 {}^B Fe^{2+} {}^C (Fe^{3+})_2 {}^D Nb^{5+} {}^E Ti^{3+} (Si_2O_7)_2 O_8$ .

### 291 **Geological significance**

292 Nb-rich chevkinite-(Ce) is of igneous/hydrothermal origin. We can speculate that the  
293 mineral was formed at relatively high temperature and then rapidly cooled. The cooling froze  
294 the structure in space group  $C2/m$  which is stable at high temperature but remains metastable

295 at room temperature. It can be assumed that the metastable phase at room temperature would,  
296 after a sufficiently long time, reorganise to a lower symmetry. Laboratory heating of the  
297 sample delivered enough energy to overcome the kinetic barrier of the transition and enabled  
298 the ordering of most of the atoms in the general positions of the unit cell. The energy supplied  
299 to the system was not large enough to match the natural conditions for the formation of Nb-  
300 rich chevkinite-(Ce) and that is why we were able to recognise the crystal structure  
301 transformation.

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### ACKNOWLEDGMENTS

304 We are very grateful to David Brown, an anonymous reviewer and Associate Editor  
305 Alejandro Fernandez-Martinez for their very helpful comments on the manuscript, which  
306 much improved its quality. The research for this paper was in part supported by the Polish  
307 Ministry of Science and Higher Education within the Mobility Plus Fund award number  
308 1301/MOB/IV/2015/0. Financial support was provided by Polish National Science Centre  
309 NCN grant decision DEC-2011/03/B/ST10/05491. We thank the Department of Earth  
310 Sciences, Natural History Museum, London, for hosting MS's year-long visit to work with  
311 MDW.

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## FIGURE CAPTIONS

443 **Figure 1.** Unit cell oriented along the **b** direction. The positions of the  $MO_6$  coordination  
444 octahedra of *B*, *C* and *D* sites are in green, yellow and orange, respectively. *M*(1)-*M*(4) is an  
445 alternative naming of sites first proposed by Popov et al. (2001).

446 **Figure 2.** Comparison of precession images of (1kl) layers for (a) untreated crystal 1 in  $C2/m$   
447 symmetry and (b) in  $P2_1/a$  symmetry, after annealing at 750 °C. The reflection extinction rule  
448 for *C* centring of the unit cell,  $h+k = 2n+1$  for all (hkl) reflections, does not hold for the  
449 annealed crystal (b).

450 **Figure 3.** The Bärnighausen tree indicates a transition from aristotype  $C2/m$  to a hettotype  
451  $P2_1/a$ . Above the arrows are given the shifts of atoms in Å. Below the diagram are given the  
452 three oxygen atoms that with the transformation symmetry in aristotype correspond to the  
453 O(1A), O(5A) and O(8A) atoms from the hettotype.

454 **Figure 4.** The *B*-O bonds in  $BO_6$  coordination. The broken-off bond of 2.16 Å corresponds to  
455 the extremal position of an O(3) atom.

456

457

## TABLES

**Table 1. The M-O bond distances and site scattering values (ssv) for A,B,C and D sites in Nb-rich chevkinite-(Ce), for crystals 1-9 – distances in Å, together with volumes (V in Å<sup>3</sup>) of the MO<sub>x</sub> first coordination spheres. Crystal numbers are given in the second row with temperature of annealing as superscript.**

<i>C2/m</i>	1	6	7	8	9	<i>P2<sub>1</sub>/a</i>	9 <sub>an</sub> <sup>600</sup>	9 <sub>an2</sub> <sup>600</sup>	9 <sub>an3</sub> <sup>650</sup>	2	3	4 <sub>an</sub> <sup>750</sup>	5 <sub>an</sub> <sup>750</sup>	1 <sub>an</sub> <sup>750</sup>
<i>A(1)</i>						<i>A(1)</i>								
<b>O(8)</b> <sub>x2</sub>	2.491(5)	2.487(4)	2.495(3)	2.495(4)	2.489(5)	<b>O(8A)</b>	2.471(4)	2.467(4)	2.465(3)	2.472(6)	2.472(7)	2.441(2)	2.441(2)	2.463(3)
						<b>O(8)</b>	2.490(4)	2.490(4)	2.500(3)	2.512(6)	2.524(7)	2.513(2)	2.515(2)	2.517(3)
<b>O(2)</b>	2.496(6)	2.496(6)	2.499(5)	2.500(6)	2.517(9)	<b>O(2)</b>	2.496(4)	2.493(4)	2.489(3)	2.505(7)	2.503(8)	2.469(2)	2.481(2)	2.482(3)
						<b>O(1A)</b>	2.500(4)	2.499(4)	2.483(4)	2.481(7)	2.471(7)	2.427(2)	2.454(2)	2.462(4)
<b>O(1)</b> <sub>x2</sub>	2.542(7)	2.553(5)	2.549(5)	2.544(6)	2.551(7)	<b>O(1)</b>	2.545(4)	2.546(4)	2.557(4)	2.553(7)	2.565(7)	2.564(2)	2.590(2)	2.563(4)
<b>O(5)</b> <sub>x2</sub>	2.560(6)	2.559(4)	2.560(4)	2.558(4)	2.560(5)	<b>O(5)</b>	2.573(4)	2.575(4)	2.578(3)	2.572(6)	2.575(6)	2.566(2)	2.574(2)	2.581(3)
						<b>O(5A)</b>	2.574(4)	2.572(4)	2.580(4)	2.574(6)	2.574(7)	2.575(2)	2.585(2)	2.582(3)
<b>O(7)</b>	2.810(6)	2.806(4)	2.813(4)	2.811(4)	2.800(7)	<b>O(7)</b>	2.817(3)	2.819(3)	2.828(3)	2.826(7)	2.834(7)	2.854(2)	2.839(2)	2.846(3)
< <b>M-O</b> >	2.56(2)	2.56(2)	2.57(2)	2.56(2)	2.56(2)	< <b>M-O</b> >	2.56(2)	2.56(2)	2.56(1)	2.56(2)	2.56(2)	2.55(2)	2.56(6)	2.56(1)
<u>V AO<sub>8</sub></u>	28.1	28.1	28.2	28.1	28.3	<u>V AO<sub>8</sub></u>	28.3	28.0	28.0	28.1	28.2	27.6	27.9	28.0
<b>O(4)</b> <sub>x2</sub>	3.189(3)	3.189(4)	3.197(3)	3.196(4)	3.199(5)	<b>O(4)</b>	3.144(6)	3.131(5)	3.092(5)	3.057(7)	3.018(8)	2.948(2)	2.919(3)	3.011(4)
						< <b>M-O</b> >	2.62(2)	2.62(2)	2.62(1)	2.62(2)	2.62(2)	2.595(5)	2.600(6)	2.61(1)
						V AO <sub>9</sub>	32.7	32.6	32.6	32.6	32.6	31.8	32.2	32.4
						<b>O(3)*</b>	3.315(4)	3.313(4)	3.310(3)	3.32(1)	3.318(7)	3.251(2)	3.301(3)	3.319(3)
< <b>M-O</b> >	2.69(2)	2.69(2)	2.69(2)	2.69(2)	2.69(2)	< <b>M-O</b> >	2.69(2)	2.69(2)	2.69(2)	2.69(2)	2.69(2)	2.66(2)	2.67(8)	2.68(2)
V AO <sub>10</sub>	37.8	37.8	37.9	37.8	38.0	V AO <sub>10</sub>	38.0	38.4	38.4	38.4	38.4	37.5	37.9	38.3
ssv	52.5	52.7	51.9	52.1	52.2	ssv	54.7	55.2	55.8	52.2	53.7	52.7	55.7	55.2
<i>A(2)</i>						<i>A(2)</i>								
<b>O(2)</b>	2.454(7)	2.456(6)	2.450(5)	2.445(6)	2.469(9)	<b>O(2)</b>	2.438(4)	2.435(4)	2.434(3)	2.420(7)	2.423(8)	2.407(2)	2.435(2)	2.431(3)
<b>O(8)</b> <sub>x2</sub>	2.499(5)	2.493(4)	2.499(3)	2.502(4)	2.492(5)	<b>O(8)</b>	2.485(4)	2.485(4)	2.477(3)	2.484(6)	2.482(7)	2.457(2)	2.454(2)	2.475(3)
						<b>O(8A)</b>	2.526(4)	2.529(4)	2.545(3)	2.557(6)	2.565(7)	2.576(2)	2.571(2)	2.571(3)
<b>O(1)</b> <sub>x2</sub>	2.703(7)	2.693(5)	2.682(5)	2.683(6)	2.698(7)	<b>O(1)</b>	2.626(4)	2.624(4)	2.612(4)	2.615(7)	2.599(7)	2.549(2)	2.576(2)	2.589(4)
<b>O(6)</b>	2.632(6)	2.627(4)	2.637(4)	2.631(5)	2.634(7)	<b>O(1A)</b>	2.662(4)	2.658(4)	2.661(4)	2.663(7)	2.669(7)	2.673(2)	2.696(2)	2.663(4)

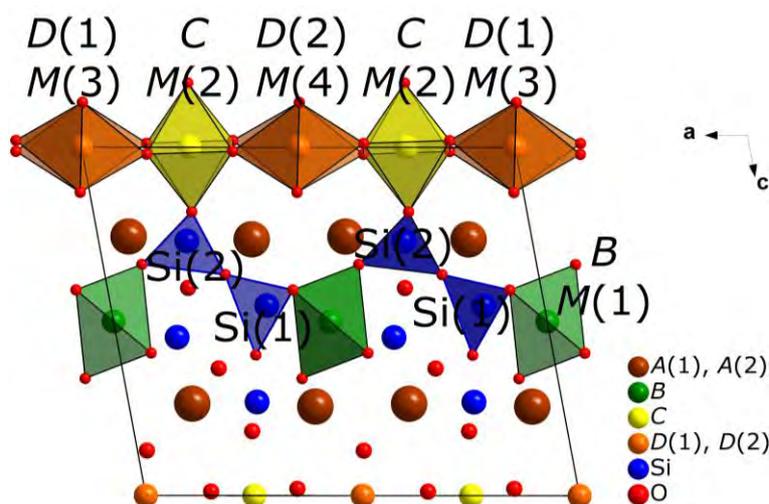
<b>O(5)<sub>x2</sub></b>	2.605(5)	2.601(4)	2.605(4)	2.606(4)	2.611(5)	<b>O(5A)</b>	2.619(4)	2.615(4)	2.623(4)	2.628(6)	2.629(7)	2.613(2)	2.603(2)	2.636(3)
						<b>O(5)</b>	2.615(4)	2.610(4)	2.616(3)	2.613(6)	2.617(6)	2.620(2)	2.613(2)	2.625(3)
						<b>O(6)</b>	2.627(3)	2.624(3)	2.630(3)	2.624(7)	2.631(8)	2.624(2)	2.627(2)	2.637(3)
<b>&lt;M-O&gt;</b>	2.59(2)	2.58(2)	2.58(2)	2.58(2)	2.59(2)	<b>&lt;M-O&gt;</b>	2.57(2)	2.57(2)	2.57(1)	2.58(3)	2.58(3)	2.56(3)	2.57(6)	2.58(1)
<b><u>VAO<sub>8</sub></u></b>	28.2	28.5	28.5	28.5	28.8	<b>VAO<sub>8</sub></b>	28.1	28.1	28.1	28.2	28.2	27.7	27.9	28.2
<b>O(3)<sub>x2</sub></b>	3.034(3)	3.030(2)	3.028(2)	3.027(2)	3.032(3)	<b>O(3)</b>	2.890(6)	2.871(5)	2.816(5)	2.803(7)	2.745(7)	2.644(2)	2.652(2)	2.716(4)
						<b>&lt;M-O&gt;</b>	2.61(3)	2.61(2)	2.60(2)	2.60(2)	2.60(2)	2.574(5)	2.580(6)	2.60(1)
						<b><u>VAO<sub>9</sub></u></b>	33.0	32.8	32.8	32.9	32.8	32.1	32.4	32.7
						<b>O(3)*</b>	3.117(6)	3.135(5)	3.185(5)	3.211(9)	3.263(7)	3.308(2)	3.336(2)	3.275(4)
<b>&lt;M-O&gt;</b>	2.68(2)	2.67(2)	2.67(2)	2.67(2)	2.68(2)	<b>&lt;M-O&gt;</b>	2.66(2)	2.66(2)	2.66(2)	2.66(3)	2.66(3)	2.65(3)	2.66(7)	2.66(1)
<b>VAO<sub>10</sub></b>	38.8	38.6	38.6	38.6	38.8	<b>VAO<sub>10</sub></b>	38.2	38.1	38.2	38.3	38.3	37.5	37.9	38.2
<b>ssv</b>	50.2	51.0	50.2	50.4	51.3	<b>ssv</b>	53.5	53.9	54.8	51.6	52.9	50.8	55.2	54.1
<b>B</b>						<b>B</b>								
<b>O(3)<sub>x2</sub></b>	1.988(8)	1.982(7)	1.989(6)	1.988(7)	2.004(11)	<b>O(3)<sub>x2</sub></b>	2.015(4)	2.012(3)	2.019(3)	2.010(8)	2.006(8)	2.016(2)	2.010(2)	2.026(3)
<b>O(1)<sub>x4</sub></b>	2.156(6)	2.151(6)	2.165(5)	2.167(6)	2.164(7)	<b>O(1)<sub>x2</sub></b>	2.214(4)	2.212(4)	2.213(4)	2.212(7)	2.213(7)	2.194(2)	2.184(2)	2.217(4)
						<b>O(1A)<sub>x2</sub></b>	2.223(4)	2.216(4)	2.228(4)	2.233(7)	2.229(7)	2.219(2)	2.211(2)	2.238(4)
<b>&lt;M-O&gt;</b>	2.10(2)	2.10(2)	2.11(2)	2.11(2)	2.11(3)	<b>&lt;M-O&gt;</b>	2.15(1)	2.15(1)	2.15(1)	2.15(2)	2.15(2)	2.143(5)	2.135(5)	2.16(1)
<b>VBO<sub>6</sub></b>	12.0	11.9	12.0	12.0	12.1	<b>VBO<sub>6</sub></b>	12.6	12.6	12.7	12.6	12.6	12.4	12.4	12.8
<b>ssv</b>	25.9	27.6	26.0	26.2	29.0	<b>ssv</b>	25.2	25.2	25.1	24.6	24.4	25.5	23.5	25.0
<b>C</b>						<b>C</b>								
<b>O(7)<sub>x2</sub></b>	1.969(4)	1.968(3)	1.971(3)	1.972(4)	1.976(5)	<b>O(7)<sup>#</sup></b>	1.974(4)	1.975(3)	1.976(3)	1.981(7)	1.972(6)	1.941(2)	1.949(2)	1.977(3)
<b>O(6)<sub>x2</sub></b>	1.978(4)	1.979(4)	1.980(3)	1.979(4)	1.989(5)	<b>O(6)<sup>\$</sup></b>	1.987(4)	1.986(3)	1.987(3)	1.977(6)	1.983(6)	1.961(2)	1.962(2)	1.988(3)
						<b>O(7)<sup>*</sup></b>	1.980(4)	1.981(3)	1.983(3)	1.979(7)	1.980(6)	1.964(2)	1.975(2)	1.985(3)
						<b>O(6)<sup>*</sup></b>	1.993(4)	1.995(3)	2.000(3)	1.994(6)	2.003(6)	1.985(2)	1.993(2)	2.005(3)
<b>O(5)<sub>x2</sub></b>	2.017(4)	2.019(3)	2.019(3)	2.019(3)	2.036(4)	<b>O(5)</b>	2.031(4)	2.034(3)	2.034(3)	2.020(6)	2.028(6)	2.015(2)	2.028(2)	2.032(3)
						<b>O(5A)</b>	2.026(3)	2.029(3)	2.029(3)	2.020(6)	2.032(6)	2.009(2)	2.022(2)	2.029(3)
<b>&lt;M-O&gt;</b>	1.99(1)	1.999(9)	1.990(7)	1.990(9)	2.00(2)	<b>&lt;M-O&gt;</b>	2.00(1)	2.000(8)	2.002(8)	1.99(2)	2.00(2)	1.979(5)	1.988(5)	2.003(8)

<b>V CO<sub>6</sub></b>	10.4	10.4	10.4	10.4	10.6	<b>V CO<sub>6</sub></b>	10.6	10.6	10.6	10.5	10.6	10.3	10.4	10.6
<b>ssv</b>	24.4	24.2	24.2	24.4	24.1	<b>ssv</b>	23.8	24.0	24.1	22.7	23.2	21.4	22.6	23.7
<b>D(1)</b>						<b>D(1)</b>								
<b>O(8)<sub>x4</sub></b>	2.013(4)	2.015(4)	2.008(3)	2.006(4)	2.028(5)	<b>O(8)<sub>x2</sub></b>	2.020(4)	2.020(3)	2.023(3)	2.017(6)	2.009(7)	1.986(2)	2.003(2)	2.022(3)
						<b>O(8A)<sub>x2</sub></b>	2.004(4)	2.005(3)	2.005(3)	1.995(6)	1.984(7)	1.964(2)	1.978(2)	2.002(3)
<b>O(6)<sub>x2</sub></b>	2.043(5)	2.040(5)	2.038(4)	2.039(5)	2.039(7)	<b>O(6)<sub>x2</sub></b>	2.027(3)	2.026(3)	2.026(3)	2.038(7)	2.021(7)	2.017(2)	2.028(2)	2.024(3)
<b>&lt;M-O&gt;</b>	2.02(2)	2.02(2)	2.018(9)	2.02(1)	2.03(2)	<b>&lt;M-O&gt;</b>	2.02(1)	2.017(8)	2.018(8)	2.02(2)	2.02(2)	1.989(5)	2.003(5)	2.016(8)
<b>V DO<sub>6</sub></b>	11.0	11.0	10.9	10.9	11.1	<b>V DO<sub>6</sub></b>	10.9	10.9	10.9	10.9	10.7	10.4	10.7	10.9
<b>ssv</b>	20.8	20.6	20.9	21.2	20.0	<b>ssv</b>	25.6	26.5	27.4	22.7	23.1	23.8	24.6	23.7
<b>D(2)</b>						<b>D(2)</b>								
<b>O(7)<sub>x2</sub></b>	2.039(5)	2.035(4)	2.032(4)	2.029(5)	2.041(7)	<b>O(7)<sub>x2</sub></b>	2.021(3)	2.018(3)	2.019(3)	2.020(6)	2.019(7)	1.984(2)	2.022(2)	2.017(3)
<b>O(8)<sub>x4</sub></b>	2.011(4)	2.013(4)	2.012(3)	2.008(4)	2.021(5)	<b>O(8)<sub>x2</sub></b>	2.017(4)	2.016(3)	2.019(3)	1.999(6)	1.985(7)	2.012(2)	1.991(2)	2.016(3)
						<b>O(8A)<sub>x2</sub></b>	2.030(4)	2.033(3)	2.036(3)	2.023(6)	2.026(7)	2.016(2)	2.029(2)	2.044(3)
<b>&lt;M-O&gt;</b>	2.02(2)	2.02(1)	2.019(9)	2.02(2)	2.03(2)	<b>&lt;M-O&gt;</b>	2.02(1)	2.022(8)	2.025(8)	2.01(2)	2.01(2)	2.003(5)	2.014(5)	2.026(8)
<b>V DO<sub>6</sub></b>	11.0	11.0	10.9	10.9	11.1	<b>V DO<sub>6</sub></b>	11.0	11.0	11.0	10.8	10.8	10.7	10.8	11.0
<b>ssv</b>	24.5	24.3	24.1	24.3	23.7	<b>ssv</b>	27.0	27.9	28.5	26.0	25.6	24.4	24.9	30.4

<sup>#</sup><sub>x,y,z</sub>; <sup>\$</sup><sub>x,y,1+z</sub>; <sup>\*</sup><sub>3/2-x,-1/2+y,1-z</sub>

463

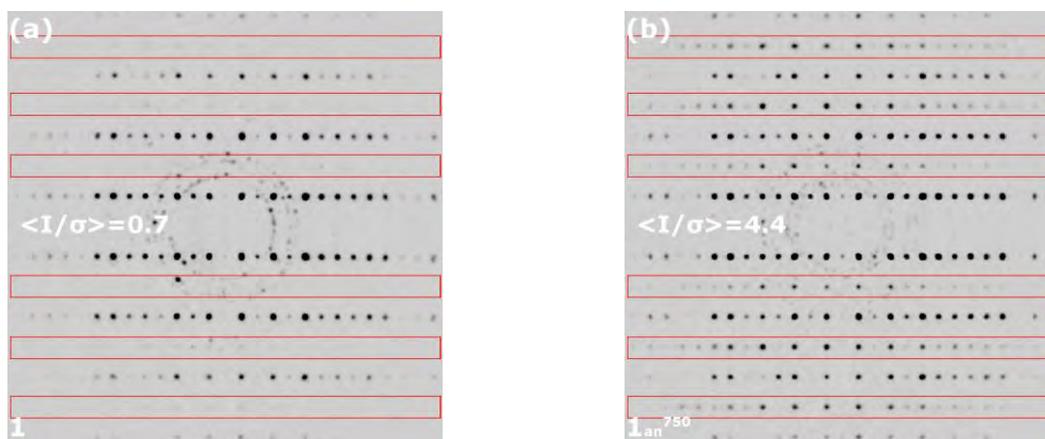
FIGURES



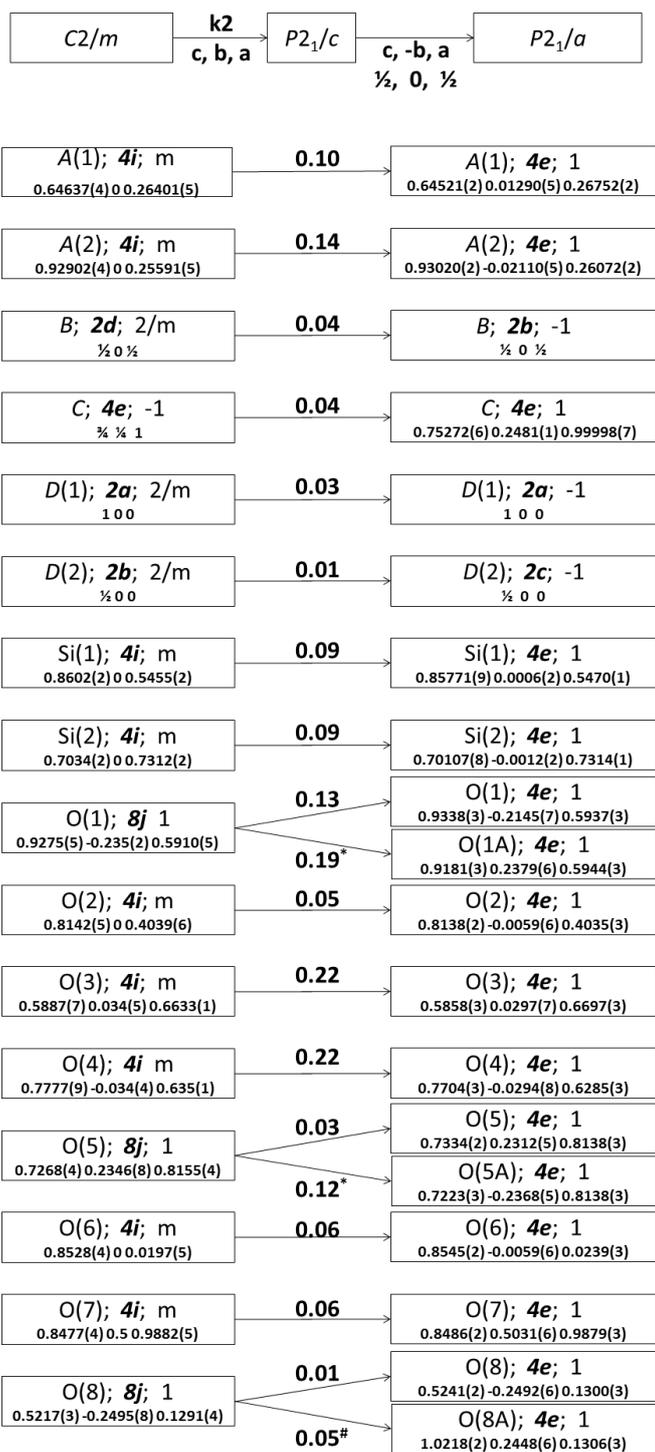
464

465 **Figure 1.** Unit cell oriented along the *b* direction. The positions of the  $MO_6$  coordination octahedra of *B*, *C*  
 466 and *D* sites are in green, yellow and orange, respectively. *M*(1)-*M*(4) is an alternative naming of sites first  
 467 proposed by Popov et al. (2001).

468



469 **Figure 2.** Comparison of precession images of (1kl) layers for (a) untreated crystal 1 in  $C2/m$  symmetry and  
 470 (b) in  $P2_1/a$  symmetry, after annealing at 750 °C. The reflection extinction rule for *C* centring of the unit  
 471 cell,  $h+k = 2n+1$  for all (hkl) reflections, does not hold for the annealed crystal (b).



\* $O(1)^{x, -y, z}$ ; \* $O(5)^{x, -y, z}$ ; \* $O(8)^{1/2+x, 1/2+y, z}$

472

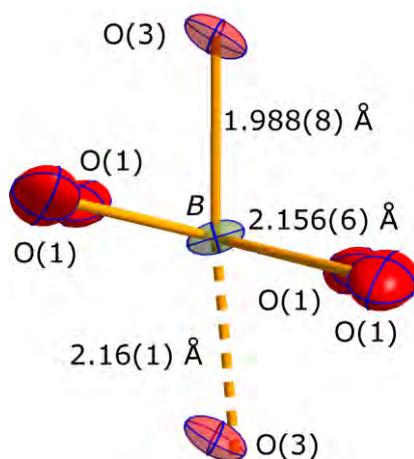
473 **Figure 3.** The Bärnighausen (family) tree indicates a transition from aristoctype  $C2/m$  to a hettotype  $P2_1/a$ .

474 Above the arrows are given the shifts of atoms in Å. Below the diagram are given the three oxygen atoms

475 that with the transformation symmetry in aristoctype correspond to the O(1A), O(5A) and O(8A) atoms from

476 the hettotype.





477

478 **Figure 4.** The *B*-O bonds in *BO*<sub>6</sub> coordination. The broken-off bond of 2.16 Å corresponds to the extremal  
479 position of an O(3) atom.

480