

## Revision 3

### Compressibility of two Na-rich clinopyroxenes: A synchrotron single-crystal X-ray diffraction study

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#### Abstract

Synchrotron-based high-pressure single-crystal X-ray diffraction experiments were conducted on synthetic clinopyroxenes at room temperature to a maximum pressure of 40 GPa. We studied two crystals with different composition. A Na-Ti-pyroxene with formula  $(\text{Na}_{0.86}\text{Mg}_{0.14})(\text{Mg}_{0.57}\text{Ti}_{0.43})\text{Si}_2\text{O}_6$  synthesized at  $P = 7$  GPa and  $T = 1700$  °C, and a Na-pyroxene with composition  $(\text{Na}_{0.886}\text{Mg}_{0.085}\text{Fe}_{0.029})(\text{Si}_{0.442}\text{Mg}_{0.390}\text{Fe}_{0.168})\text{Si}_2\text{O}_6$  synthesized at  $P = 15$  GPa and  $T = 1500$  °C. These phases were found to be monoclinic with the space group  $C2/c$  and exhibit  $K_{\text{To}}$  of 106.8(2), 121.8(4) GPa, respectively. Na-Ti-pyroxene is more compressible than Fe-bearing Na-Mg-Si-pyroxene, likely due to the fact that the  $\text{FeO}_6$  octahedron is significantly more rigid than  $\text{MgO}_6$  at high pressure. The formation of Na-rich pyroxenes in the deep mantle is related to crystallization of low-degree alkaline carbonate-silicate melts formed when the crust and mantle interact during the slab descent and its stagnation in the transition zone.

37

38 **Keywords:** pyroxene, single-crystal X-ray diffraction, high-pressure, high-temperature,  
39 phase transitions, equation of state, Earth's mantle

40

## 41 **Introduction**

42 It is well known that pyroxenes may undergo a number of phase transitions with  
43 increasing  $P$  and  $T$  toward at least five different structures (Cameron and Papike 1981;  
44 Yang and Prewitt 2000). These transitions typically affect all the physical properties of  
45 the mineral including density, bulk modulus, and the orientation and dimensions of the  
46 unit-strain ellipsoid. Knowledge of the behavior of mantle materials at high  $P$  is crucial  
47 for understanding of the deep Earth structure and composition. In addition,  
48 thermodynamic parameters of pyroxene end-members are critical for thermo- and  
49 geodynamic modeling of the Earth's upper mantle (Stixrude and Lithgow-Bertelloni  
50 2005).

51 The most common pyroxenes are those that contain the major elements (Ca, Mg,  
52 and Fe) in the M sites (enstatite, ferrosilite, diopside, hedenbergite). Their early HP-  
53 XRD-studies (Hazen and Finger 1977; Levien and Prewitt 1981) formed the basis for  
54 such important scientific interdisciplinary problem as comparative crystal chemistry of  
55 the mantle and core minerals. The results obtained showed that the three polyhedra (M1,  
56 M2 and Si) in pyroxene structures decrease irregularly in size and their compressibilities  
57 depend on their chemical contents. Somewhat less common are pyroxenes that  
58 incorporate larger cations, such as Na. For this reason, Na-rich pyroxenes have been  
59 much less studied.

60 It has long been assumed that clinopyroxenes abundant in the Earth's crust and  
61 upper mantle contain only tetrahedrally coordinated Si. The synthesis of  
62  $\text{Na}(\text{Mg}_{0.5}\text{Si}_{0.5})\text{Si}_2\text{O}_6$  pyroxene and its unit-cell parameters were originally reported based  
63 upon X-ray powder (Gasparik 1988) and single-crystal (Angel et al. 1988) diffraction.  
64 The compound was found to be monoclinic with space group  $P2/n$ . These studies have  
65 shown that clinopyroxenes may accommodate octahedrally-coordinated silicon (Yang  
66 and Konzett 2005) suggesting that the stability of clinopyroxenes may be expanded to  
67 higher pressures than those previously assumed. Later Yang et al. (2009) synthesized five  
68 clinopyroxenes containing various amounts of six-coordinated silicon in the  
69  $\text{Na}(\text{Mg}_{0.5}\text{Si}_{0.5})\text{Si}_2\text{O}_6$ – $\text{NaAlSi}_2\text{O}_6$  system at 15 GPa and 1600°C. These authors showed  
70 that clinopyroxenes with  $^{\text{VI}}\text{Si} \leq 0.33$  atoms per formula unit (apfu) possess  $C2/c$   
71 symmetry, whereas those with  $^{\text{VI}}\text{Si} \geq 0.45$  apfu crystallize with  $P2/n$  symmetry.  
72 Increasing  $^{\text{VI}}\text{Si}$  content from 0.33 to 0.45 apfu results in the formation of the discontinuity  
73 in the unit-cell parameters suggesting that the  $C2/c$ – $P2/n$  transition is first-order in  
74 character (Yang et al. 2009). The  $P$ – $V$ – $T$  equation of state (EoS) was studied for Na-  
75 pyroxene at pressures up to 21 GPa and temperatures up to 1400°C by *in situ* X-ray  
76 diffraction experiments using a Kawai-type multi-anvil apparatus (Dymshits et al. 2015).

77 Another probable high-pressure Na-pyroxene with  $\text{Ti}^{4+}$  in the octahedral site is  
78  $\text{Na}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{Si}_2\text{O}_6$  (Na-Ti-Px). Such Na-Ti-pyroxenes are poorly studied, while the  
79 crystal structure of Na-Ti pyroxene with the composition  $\text{NaTi}^{3+}\text{Si}_2\text{O}_6$  has been deeply  
80 investigated (e.g., Prewitt et al. 1972; Ninomiya et al. 2003; Redhammer et al. 2003). The  
81 synthesis of  $\text{NaTi}^{3+}\text{Si}_2\text{O}_6$  single crystals and the full description of the room-temperature  
82 structure have been first done by Ohashi et al. (1982). At 298 K, the compound has  
83 monoclinic symmetry with space group  $C2/c$ . Ohashi (2003) reported the structural

84 differences in  $(\text{Na,Ca})(\text{Ti}^{3+},\text{Mg})\text{Si}_2\text{O}_6$  clinopyroxenes with various compositions at  
85 ambient conditions. Recently, Ullrich et al. (2010) investigated the influence of the  
86 coupled substitution  $\text{Na}^+\text{Ti}^{3+} \leftrightarrow \text{Ca}^{2+}\text{Mg}^{2+}$  on the structural stability of  $\text{NaTi}^{3+}\text{Si}_2\text{O}_6$  at  
87 high pressures. These authors showed that, in contrast to the composition  
88  $(\text{NaTi}^{3+}\text{Si}_2\text{O}_6)_{0.54}(\text{CaMgSi}_2\text{O}_6)_{0.46}$ , this pyroxene underwent the  $C2/c-P\bar{1}$  phase transition  
89 at a pressure higher than 4.37 GPa.

90 The synthesis of  $(\text{Na}_{0.86}\text{Mg}_{0.14})(\text{Mg}_{0.57}\text{Ti}_{0.43})\text{Si}_2\text{O}_6$  pyroxene with octahedral  
91 titanium and its structural details were originally reported by Sirotkina et al. (2016). This  
92 study has shown that clinopyroxene may accommodate octahedrally-coordinated  $\text{Ti}^{4+}$ .  
93 The isomorphic replacement in this compound with respect to  $\text{Mg}_2\text{Si}_2\text{O}_6$  corresponds to  
94 the scheme:  $\text{Na}^+ + (\text{Ti}^{4+})/2 + (\text{Mg}^{2+})/2 = 2\text{Mg}^{2+}$ . The  $\text{Na}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{Si}_2\text{O}_6$  component has  
95 been sometimes registered as an end-member of natural low-Ca mantle pyroxenes  
96 (Bishop et al. 1978; Rudnick et al. 2004; Aulbach et al. 2004; Sirotkina et al. 2016).

97 Na-rich clinopyroxenes have not been deeply studied at high pressures. Zhao et al.  
98 (1997) performed a synchrotron X-ray powder diffraction study on jadeite up to 8.2 GPa  
99 and 1280 K. They fit their data with a modified Birch-Murnaghan equation of state, with  
100  $K'_0 = 5.0$ , and found the bulk modulus of jadeite to be 125(4) GPa. Nestola et al. (2006)  
101 studied jadeite and aegirine compressibilities, as a function of pressure, and examined  
102 changes in compressional anisotropy with variations in chemistry along the jadeite-  
103 aegirine ( $\text{NaFeSi}_2\text{O}_6$ ) solid solution.

104 To shed light on the high-pressure behavior of Na-rich clinopyroxenes, here we  
105 report the single-crystal X-ray diffraction study of two pyroxenes with composition  
106  $(\text{Na}_{0.86}\text{Mg}_{0.14})(\text{Mg}_{0.57}\text{Ti}_{0.43})\text{Si}_2\text{O}_6$  and  $(\text{Na}_{0.884}\text{Fe}^{2+}_{0.116})(\text{Mg}_{0.475}\text{Si}_{0.442}\text{Fe}^{2+}_{0.083})\text{Si}_2\text{O}_6$  up to a  
107 pressure of 40 GPa. Furthermore, in an effort to understand the variation in Na-rich

108 pyroxene compressibilities, a series of Na-clinopyroxenes from the literature is also  
109 examined.

110

## 111 **Experimental methods**

112         Synthesis of a new Na-Ti-pyroxene with formula  $(\text{Na}_{0.86}\text{Mg}_{0.14})(\text{Mg}_{0.57}\text{Ti}_{0.43})\text{Si}_2\text{O}_6$   
113 was performed at the Vernadsky Institute of Geochemistry and Analytical Chemistry,  
114 Russian Academy of Sciences, Moscow, Russia, using the high-pressure toroidal ‘anvil-  
115 with-hole’ apparatus at 7 GPa and 1700 °C. The starting mixture was chemically pure  
116 oxides of Mg,  $\text{Ti}^{4+}$  and Si and sodium silicate  $\text{Na}_2\text{SiO}_3$  corresponding to the formula  
117  $\text{Na}_2\text{MgTi}_2\text{Si}_3\text{O}_{12}$ . Solid-state cells of a 30-mm outer diameter were manufactured from  
118 pressed mixture of MgO and BN in equal parts (with a small amount of  $\text{Cr}_2\text{O}_3$ ). They  
119 contained an ultrapure graphite heater with an outer diameter of 7 mm and a length of 7.5  
120 mm, which had a hole with a diameter of 2.5 mm and a depth of 2.5 mm. This hole was  
121 the container for starting materials. The temperature measurement accuracy was  $\pm 10$  °C.  
122 Run pressure was controlled to  $\pm 0.5$  GPa. Details of the experimental techniques and cell  
123 calibration were described by Bobrov and Litvin (2009). Colorless transparent crystals of  
124 Na-Ti-Px,  $\sim 150$   $\mu\text{m}$  in size, were observed in the quenched groundmass of elongated  
125 rutile and pyroxene crystals in the run carried out at  $P = 7$  GPa and  $T = 1700$  °C (Fig. 1a).

126         The Fe-bearing Na-Mg-Si pyroxene with the composition  
127  $(\text{Na}_{0.886}\text{Mg}_{0.085}\text{Fe}_{0.029})(\text{Si}_{0.442}\text{Mg}_{0.390}\text{Fe}_{0.168})\text{Si}_2\text{O}_6$  was synthesized on a 2000-t Kawai-type  
128 high-pressure multi-anvil apparatus at the Bayerisches Geoinstitut, Bayreuth, Germany,  
129 at 14 GPa and 1500 °C. The details of experimental assembly and procedures were  
130 described elsewhere (Frost et al. 2004). The starting material (90 mol %  
131  $\text{Na}(\text{Mg}_{0.5}\text{Si}_{0.5})\text{Si}_2\text{O}_6 + 10$  mol %  $\text{Fe}_2\text{Si}_2\text{O}_6$ ) was prepared from chemically pure oxides

132 (MgO, FeO, and SiO<sub>2</sub>) and sodium silicate Na<sub>2</sub>SiO<sub>3</sub>, homogenized at room temperature  
133 using ethanol and then dried in the stove at 100 °C. A starting mixture was placed into a  
134 capsule of 3.5 mm in height and 2 mm in diameter made of a rhenium foil. The high  
135 temperature was generated using a LaCrO<sub>3</sub> heater. The capsule was isolated from the  
136 heater by a MgO cylinder. The cell assembly with the sample was compressed between  
137 eight cubic tungsten carbide anvils with corners truncated to 5.0 mm edge lengths. The  
138 accuracy in determination of pressure and temperature was estimated to be ±0.5 GPa and  
139 ±50 °C, respectively. The run duration was 2 h. Then, the sample was rapidly quenched  
140 to ambient temperature by switching off a power supply with a quench rate of 200 °C/s.  
141 Fig. 1b shows the secondary electron image of Na-pyroxene aggregates in a groundmass  
142 composed of very small pyroxene and stishovite grains.

143 After runs, sample with Na-Ti pyroxene was embedded in epoxy and polished to  
144 study texture and phase compositions. The compositions of the run products were  
145 analyzed by means of a JEOL JSM-6480LV scanning electron microscope equipped with  
146 an Oxford X-MaxN energy-dispersive analytical setup at the Department of Petrology,  
147 Geological Faculty, Moscow State University. The following standards were used: NaCl  
148 for Na, TiO<sub>2</sub> for Ti, diopside for Si and Mg, and synthetic Fe<sub>2</sub>SiO<sub>4</sub> for Fe. Compositions  
149 of the phases were determined from the average of 4–6 analyses performed at an  
150 accelerating voltage of 20 kV and beam current of 10 nA.

151 Pre-selected isometric crystals of ~ 15 μm were loaded in diamond anvil cells  
152 (DACs) into holes drilled through Re gaskets indented to 20-35 μm thickness. After the  
153 study at ambient conditions, DACs were loaded with Ne to achieve quasi-hydrostatic  
154 conditions. Neon was also used as a pressure standard using the equation of state (Fei et  
155 al. 2007). For pressure measurements below 15 GPa, the fluorescence emission of a ruby

156 chip was used. Two separate synchrotron-based X-ray diffraction experiments were  
157 performed at the ESRF, Grenoble, France, at the beamline ID09A and at the DESY of  
158 PETRA III, Hamburg, Germany, at the extreme conditions beamline P02.2. At the ESRF  
159 on beamline ID09, we used a mar555 flat panel detector and an X-ray wavelength of  
160 0.415 Å with a beam spot size of  $\sim 10 \times 10 \mu\text{m}^2$ . At the extreme conditions beamline  
161 P02.2 at PETRA III, we used X-ray wavelength of 0.2903 Å and a Perkin Almer detector,  
162 and the beam-size was  $3 \times 8 \mu\text{m}^2$ . The positions of the detectors were calibrated using Si  
163 or CeO<sub>2</sub> standards.

164 Single-crystal diffraction data were collected at various pressures in two modes.  
165 Wide scans were collected during  $\omega$  rotation scans of  $\pm 20^\circ$  with 40 s per frame and step  
166 scans were collected with rotation of the cell of  $\pm 38^\circ$  with a typical exposure time of 0.5-  
167 2 s per frame.

168 The indexing of Bragg reflections, the intensity data reduction, and the empirical  
169 absorption correction were performed using the Agilent CrysAlisPro software (Oxford  
170 Diffraction 2006). Crystal structures were refined using Jana 2006 (Petricek et al. 2014).  
171 Polyhedral volumes were calculated using VESTA software (Momma and Izumi 2011).  
172 The Birch-Murnaghan and Vinet equations of state coefficients were refined using the  
173 program EoSFit-7c (Angel et al. 2014).

## 174 **Results**

175  
176 *In situ* X-ray diffraction experiments were performed up to 40 GPa for Na-Ti Px  
177 and up to 30 GPa for Fe-bearing Na-Mg-Si Px; the pressure-volume (*P-V*) data are given  
178 in Table S1 (Supplementary Information).

179 As shown in Figure 2, the Birch's normalized stress (FE)—Eulerian strain ( $fE$ )  
180 plots for both pyroxenes can be clearly fitted with horizontal straight lines. Therefore, the  
181 data can be fitted with a 2nd-order BM EoS. From this fitting, the bulk modulus obtained  
182 at room temperature is  $K_0 = 106.8(2)$  GPa for Na-Ti Px and  $K_0 = 121.8(4)$  GPa for Fe-  
183 bearing Na-Mg-Si Px. This is in a good agreement with the  $P$ - $V$  data on the initial volume  
184  $V_0$  and room temperature bulk modulus  $K_0$  for studied pyroxenes (Table 1). The  
185 normalized unit-cell parameters for pyroxenes calculated as  $X_P/X_0$  ( $X_P$  are the  
186 experimentally determined parameters  $a$ ,  $a\sin\beta$ ,  $b$ ,  $c$  at pressure point  $P$ ;  $X_0$  = EoS values  
187 at ambient pressure) are shown in Figure 3. For a monoclinic mineral, in which the beta  
188 angle changes significantly with pressure, the  $a$ - and  $c$ -crystal axes are not the principal  
189 axes of the strain tensor, and, therefore, are not the directions of minimum and maximum  
190 compression in the crystal structure. Strain tensor of the mineral and the minimum and  
191 maximum compression direction in the  $a$ - $c$  plane (Table S2 in Supplementary  
192 Information) were simulated with the cell-parameter data between room and pressure  
193 conditions using the win\_strain software ([http://www.rossangel.com/text\\_strain.htm](http://www.rossangel.com/text_strain.htm)).  
194 The unit strain ellipsoid is significantly anisotropic, as is demonstrated by the axial ratios  
195  $\epsilon_1:\epsilon_2:\epsilon_3 = 1:3.07:1.64$  (computed between 0–40.3 GPa), where  $\epsilon_2$  is parallel to the  $b$   
196 axis,  $\epsilon_1$  and  $\epsilon_3$  lie in the  $ac$ -plane perpendicular to each other and  $\epsilon_1$  divides  $\beta$ . Neither  
197 the crystallographic  $a$  nor  $c$  axes are principal axes of the strain ellipsoids. The stiffest  
198 direction lies between  $+a$  and  $+c$ , since the  $\beta$  angle is changing as  $P$  increases, thus,  
199 contributing an expansion to directions between  $+a$  and  $+c$ . The stiffest direction in the  
200 structure of the studied pyroxenes lies close to the bisector of the obtuse angle  $\beta$  not  
201 along  $[101]$ , but along  $[u0w]$  in the  $(010)$  plane at low pressures (Table S2 in  
202 Supplementary Information). As a function of pressure, we can see the change in the



203 value of the unit strain parallel to the stiffest direction and a significant change in its  
204 orientation, which is rotated counterclockwise. Thus, with increasing pressure, the stiffest  
205 direction lies close to [405]. As it was noted above, the *b* direction or [010] is the most  
206 compressible direction in studied pyroxenes. The kinking of the tetrahedral chains  
207 accounts for most of the anisotropy of compression observed in the *a-c* plane in particular  
208 along the  $\epsilon_1$  (Thompson and Downs 2008).

209 Results of the structural refinements for studied pyroxenes are given in CIFs in  
210 Supplementary Information. The crystal structures of Fe-bearing Na-Mg-Si pyroxene and  
211 Na-Ti pyroxene are quite similar and based on three types of polyhedra: one octahedra  
212 ( $M1O_6$ ), one eight-fold coordinated site ( $M2O_8$ ) and one tetrahedron ( $SiO_4$ ) (Fig. 4).

213 Within a coordination sphere of 2.6 Å, the M2 site is surrounded by six O atoms  
214 with two O3 atoms at a distance of 2.9 Å from the M2 cation. Since this value is  
215 significantly reduced to 2.32 Å for Na-Ti Px and to 2.39 Å for Fe-bearing Na-Mg-Si Px  
216 with increasing pressure, the coordination of the M2 site appears to become eightfold at *P*  
217 > 20 GPa, whereas other Na-bearing pyroxenes still exhibit an octahedrally-coordinated  
218 M2 site (e.g., Prewitt and Burnham 1966; Clark et al. 1969; Ohashi et al. 1982). Fig. 5  
219 shows that the effective coordination number changes as a function of pressure. In order  
220 to compare the effective coordination number in the *P*-range investigated it was fixed to  
221 the dodecahedral shape. M2 sites are distorted and occupied by Na with a small  
222 admixture of Mg and  $Fe^{2+}$ . The M1 sites are smaller and almost regular octahedral. The  
223 M1 site is occupied by Ti and Mg in Na-Ti Px, whereas this site for Fe-bearing Na-Mg-Si  
224 pyroxene is occupied by  $Si^{4+}$ ,  $Fe^{2+}$  and  $Mg^{2+}$ . The  $SiO_4$  tetrahedra are connected via  
225 bridging O3 atoms to form chains running along the *c* axis. The  $SiO_4$  tetrahedra are  
226 distorted: the Si–O bond distances range broadly from 1.53 to 1.66 Å with the Si–O3

227 bond being the longest one (Figs. 6c and 7c). The quadratic elongation and angular  
228 variation parameters (Robinson et al. 1971) have been used to determine the non-ideality  
229 of the coordination polyhedra.

230 With increasing pressure, all structural units show an anisotropic distortion. Figure  
231 8 illustrates the normalized polyhedral volume for  $M1O_6$ ,  $M2O_8$ , and  $SiO_4$  polyhedra in  
232 studied pyroxenes.

233 The polyhedral volumes show clear changes with increasing pressure as well. A  
234 third-order Birch-Murnaghan EoS was used for the fitting of polyhedral volumes. For  
235 Na-Ti Px, between 3 and 40 GPa, the volume of  $M1O_6$  decreases slightly from 10.9 to  
236  $8.97 \text{ \AA}^3$  (Fig. 8a, Table s3) with a bulk modulus of 102(2) GPa. The evolution of the  
237 individual M1–O bonds is anisotropic (Fig. 8) with the following compressibility  
238 scheme:  $\beta(M1-O1) = 2.9 \times 10^{-3} \text{ GPa}^{-1} > \beta(M1-O2) = 2.4 \times 10^{-3} \text{ GPa}^{-1} \gg \beta(M1-O3) =$   
239  $1.67 \times 10^{-3} \text{ GPa}^{-1}$ . The Fe-bearing Na-Mg-Si Px is characterized by the similar  
240 compressibility scheme. In the pressure range from 4–30 GPa, the  $M1O_6$  volume  
241 decreases from 10.27 to  $9.111 \text{ \AA}^3$  (Fig. 8b, Table s6) with a bulk modulus of 156(19) GPa  
242 indicating the following compressibility scheme:  $\beta(M1-O1) = 3.46 \times 10^{-3} \text{ GPa}^{-1} > \beta(M1-$   
243  $O2) = 2.4 \times 10^{-3} \text{ GPa}^{-1} \gg \beta(M1-O3) = 1.11 \times 10^{-3} \text{ GPa}^{-1}$ .

244 The  $M2O_8$  polyhedron with the bulk modulus of 73(1) GPa is much softer than  
245 M1. The studied pyroxenes are characterized by the following compressibility scheme:  
246  $\beta(M2-O3) \gg \beta(M2-O1) \approx \beta(M2-O2) > \beta(M2-O4)$ .

247 The Si-tetrahedron is the most rigid structural unit of the pyroxene structure (e.g.  
248 Yang and Prewitt, 2000). For Na-Ti Px in the pressure range from 3 to 40 GPa, its  
249 volume decreases from 2.137 to  $2.028 \text{ \AA}^3$  with a bulk modulus of 901(495) GPa.  
250 However, Fe-bearing Na-Mg-Si Px shows greater decrease in the Si-tetrahedron volume.

251 Between 4 and 30 GPa, its volume decreases from 2.13 to 1.90 Å<sup>3</sup> with a bulk modulus  
252 of 236(134) GPa. The Si-O1, Si-O2 and Si-O3 bonds show compressibilities of  $\sim 1 \times 10^{-3}$   
253 GPa<sup>-1</sup>.

254 The characteristic feature of Na- pyroxenes is the decrease of the O3-O3-O3 angle  
255 from 171.9° at 3 GPa to 153.61° at 40 GPa for Na-Ti Px and from 172.2° at 4 GPa to  
256 166° at 30 GPa for Fe-bearing Na-Mg-Si Px, which indicates a strong compression of  
257 tetrahedral chains (Table s5). It should be noted that most likely we observe an  
258 isostructural (isosymmetric) phase transition at around 22 GPa due to the rotation of the  
259 tetrahedral chains. The main change associated with the tetrahedral chains is the change  
260 in kinking, due to the decrease in the O3-O3-O3 angle from 22 GPa. Such rotation  
261 provokes the rapid increase in coordination of the M2 cations (Fig. 6b) from 6 to 8. The  
262 second-order isosymmetric phase transition has been also observed in aegirine at 24 GPa  
263 by Xu et al. (2017) with an evident discontinuity in the O3-O3-O3 angle at that pressure.  
264 Figure 6b shows the sympathetic M2–O3 bonds, which positioned to favor the tetrahedral  
265 rotation upon compression, and antipathetic M2–O3 bonds positioned to resist the  
266 rotation (McCarthy et al. 2008). The antipathetic M2–O3 bonds decrease much more  
267 slowly than the other M2–O3 bonds, since tetrahedral rotation provides a component of  
268 the O3 displacement away from M2. The antipathetic M2–O3 bonds have the smallest  
269 decrease with pressure while the sympathetic M2–O3 bonds have the greatest decrease.

270

## 271 **DISCUSSION**

272 It is worthy to note that in contrast to Na-Ti Px, Fe-bearing Na-Mg-Si Px, as well  
273 as the starting material Na(Mg<sub>0.5</sub>Si<sub>0.5</sub>)Si<sub>2</sub>O<sub>6</sub> used for its synthesis, are the phases which  
274 contain both tetrahedrally and octahedrally coordinated silicon. A systematic survey of

275 these high-pressure structures (Finger and Hazen 2000; Pushcharovsky 2004) showed  
276 that besides pyroxenes, the silicates of the titanite, garnet (majorite), wadeite, benitoite  
277 and spinel structural types belong to this group. In addition, there are Na- and Mg-  
278 silicates with silicon in mixed four- and six-fold coordination. In experiments, all of them  
279 crystallize at pressures between about 5 and 20 GPa.

280         Based on the foregoing, it follows that the compressibility of Na-Ti Px (106.8(2)  
281 GPa) is significantly higher than that of Fe-bearing Na-Mg-Si Px (121.8(4) GPa). Fig. 13  
282 shows comparison of unit cell volumes with increasing pressure for the two pyroxenes  
283 studied.

284         Dymshits et al. (2015) conducted a study of the compressibility of Na-rich  
285 pyroxene. In connection with the findings of Tribaudino et al. (2001), who showed that  
286 the M2 site chemistry has a little effect on the bulk modulus of pyroxenes, the  
287 relationship between the ambient unit-cell volume and M1 cation radius suggests that  
288 bulk compressibility in *C2/c* silicate pyroxenes may be controlled by the compressibility  
289 of the M1 octahedron. Thus, we should compare our results not only with high-Na  
290 pyroxenes, but also with other pyroxenes with similar structural characteristics. The  
291 compressibility systematics of clinopyroxenes has been a subject of intensive research.  
292 Several factors responsible for the bulk moduli variation have been proposed: volume-  
293 bulk modulus systematic at ambient conditions (Bridgman 1923), cation size and  
294 occupancy of the M1 site (Thompson and Downs 2004), type (sympathetic or  
295 antipathetic) of the M2-O3 bonds (McCarthy et al. 2008).

296         Thompson et al. (2005) showed that the unit cell volume is largely a function of  
297 M1, and the bulk modulus of *C2/c* pyroxenes depends primarily on the occupancy of the  
298 M1 site. The bulk moduli values of Na-Ti- and Na-Mg-Si Px (106.8(2) and 121.8(4) GPa,

299 respectively) indicate that the substitution of  $\text{Mg}^{2+}$  cation ( $r(\text{Mg}^{2+})=0.72 \text{ \AA}$ ) with the  
300 slightly larger  $\text{Fe}^{2+}$  cation ( $r(\text{Fe}^{2+})=0.78 \text{ \AA}$ ) at the M1 site causes softening of the  $C2/c$   
301 structure. Such behavior was observed for olivine (Zhang et al. 1997), and the Fe-Mg  
302 spinel solid solution (Hazen 1993) as well. In addition, we can see the effect of  $\text{Fe}^{2+}$  on  
303 pyroxene compressibility by comparing the  $C2/c$  Fe-bearing Na-Mg-Si Px (this study)  
304 and  $P2/n$  pyroxene with the composition  $\text{NaMg}_{0.5}\text{Si}_{2.5}\text{O}_6$  (Dymshits et al. 2015). The bulk  
305 moduli of  $\text{NaMg}_{0.5}\text{Si}_{2.5}\text{O}_6$  pyroxene is 103(2), which is significantly lower than that of  
306 Fe-bearing Na-Mg-Si Px (121.8(4) GPa). The stiffer structure is typical of pyroxenes  
307 with Mg substitution with  $\text{Fe}^{3+}$  in the octahedral M1 site ( $r(\text{Fe}^{3+})=0.64 \text{ \AA}$ ),  $\text{Al}^{3+}$   
308 ( $r(\text{Al}^{3+})=0.535 \text{ \AA}$ ) and  $\text{Cr}^{3+}$  ( $r(\text{Cr}^{3+})=0.615 \text{ \AA}$ ); their bulk moduli are 117.9(4), 136.5(14),  
309 136.7(6), respectively. The increased stiffness of such pyroxenes may indicate their lower  
310 transition pressures in comparison with  $\text{NaMg}_{0.5}\text{Si}_{2.5}\text{O}_6$  or  $\text{Na}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{Si}_2\text{O}_6$ .  
311 Incorporation of  $\text{Ti}^{4+}$  in the M1 site does not influence on the bulk modulus of pyroxene.

312 It is shown that the type of the M2-O3 bonds (sympathetic or antipathetic) is very  
313 important as well. The M2-O3 bonds display one of two behavior modes as pyroxene  
314 structures are compressed and  $\text{SiO}_4$  tetrahedra rotate, which results in change of the O3-  
315 O3-O3 angles and decrease in M2-O3 distances (Downs 2003). The M2-O3 bonds with  
316 decreasing length are inhibited by the pressure-induced tetrahedral rotation, which tends  
317 to resist rotation, and are, thus, termed “antipathetic” bonds typical of diopside and other  
318 Ca-rich pyroxenes. “Antipathetic” bonds are positioned to resist the tetrahedral rotation.  
319 In contrast, the M2-O3 bonds that are further shortened by tetrahedral rotation would  
320 either assist or have no effect on tetrahedral rotation, and are thus termed “sympathetic”  
321 bonds.

322 M2 in the structures of our *C2/c* Na-rich pyroxenes and *P2/n* Na-pyroxene  
323 described by Dymshits et al. (2015) has two (topologically identical) antipathetic and two  
324 sympathetic M2-O3 bonds; this is characteristic of all *C2/c* pyroxenes, in which the M2  
325 site is eight-fold and bonded to all bridging O atoms. The group of monovalent-M2 *C2/c*  
326 pyroxenes ( $\text{LiAlSi}_2\text{O}_6$ ,  $\text{NaAlSi}_2\text{O}_6$ ,  $\text{NaCrSi}_2\text{O}_6$ , and  $\text{NaFeSi}_2\text{O}_6$ ), in which M2 is six-fold  
327 and bonded to two bridging O atoms, is characterised by the presence of antipathetic M2-  
328 O3 bonds. Figures 6b and 10b shows the change in M2-O distances in our Na-rich  
329 pyroxenes as a function of pressure. It was found that the antipathetic M2-O3 bonds  
330 decreased in length much more slowly than the other M2-O bonds, since tetrahedral  
331 rotation provided a component of O3 displacement away from M2. The antipathetic M2-  
332 O3 distance shows the smallest decrease with pressure, while the sympathetic M2-O3  
333 distance has the greatest decrease. This can be interpreted by coupling of the common  
334 compression of the structure with pressure and rotation of the silicate tetrahedra, which  
335 leads to shortening or lengthening of some interatomic distances. Thus, pyroxenes with  
336 only antipathetic M2-O3 bonds are much stiffer in comparison with phases containing  
337 two types of bonds.

338 McCarthy et al. (2008) predicted that the bulk moduli of silicate clinopyroxenes  
339 with antipathetic M2-O3 bonds should follow  $K_0^{\text{ant}}$  (GPa) =  $-0.5051V_0$  ( $\text{\AA}^3$ ) + 339.37,  
340 whereas clinopyroxenes without antipathetic M2-O3 bonds should follow  $K_0^{\text{sym}}$  (GPa) =  
341  $-0.7784V_0$  ( $\text{\AA}^3$ ) + 419.14. At the same time, it was suggested that the effect of  
342 temperature should not be significant. Thus, Cameron et al. (1973) found that the  
343 expansion of the jadeite structure from ambient temperature to 800°C resulted in increase  
344 in the unit cell volume by 1.9% only, and increase in pressure up to 9 GPa reduced the  
345 unit cell volume by 5.9%. In this study, we show that the unit cell volume of Na-Ti-Px

346 decreases by 20.9% with increasing pressure up to 40 GPa, and the unit cell volume of  
347 Na-Mg-Si Px decreases by 15.8% with increasing pressure within the range of 0–30 GPa.  
348 Our Na-rich pyroxenes and  $P2/n$   $\text{NaMg}_{0.5}\text{Si}_{2.5}\text{O}_6$  pyroxene (Dymshits et al., 2015) are in  
349 an intermediate position between pyroxenes with two antipathetic M2–O3 bonds (upper  
350 trend) and pyroxenes with only sympathetic M2–O3 bonds (lower trend) (Fig. 14). This  
351 fact indicates that the bulk modulus of such pyroxenes with different compositions can be  
352 calculated, and these values can vary within the  $K_0^{\text{ant}} - K_0^{\text{sym}}$  range.

353

## 354 **Implications**

355

356 Despite significant interest of experimentalists to the study of geophysically  
357 important phase equilibria in the Earth's mantle and the need to increase the experimental  
358 database related to multicomponent systems, incorporation of Si and  $\text{Ti}^{4+}$  in the  
359 octahedral sites of minerals is very important for understanding the processes in the deep  
360 Earth and in obtaining the data on the composition and structure of deep Earth  
361 geospheres. The influence of these elements on structural peculiarities of high-pressure  
362 phases may have a certain impact on the  $PT$ -parameters and phase transformations.

363 Si-rich Na-pyroxene and Na-majorite (Dymshits et al. 2010; Bindi et al. 2011)  
364 have the same chemical compositions and should be considered as potential hosts for  
365 sodium in the Earth's upper mantle areas characterized by an excess of Na with respect to  
366 Al in the bulk. Generally, this is not typical of peridotitic lithologies in the upper mantle  
367 regularly sampled by mantle xenoliths. However, the probability to find a Na-rich  
368 substrate in the deep mantle is confirmed by an inclusion in diamond with the  
369 composition of  $(\text{Na}_{0.16}\text{Mg}_{0.84})(\text{Mg}_{0.92}\text{Si}_{0.08})\text{Si}_2\text{O}_6$  found in a kimberlite from China (Wang

370 and Sueno 1996). As this phase has been found to have the garnet structure (Wang and  
371 Gasparik, 2000), the appropriate compositions should exist in the mantle to stabilize Na-  
372 pyroxene as a component in pyroxene below the pyroxene–garnet transition pressure,  
373 which is approximately 16.5 GPa (Gasparik 1989). Our studies have shown that  
374 incorporation of small amount of Fe<sup>3+</sup> to Na-pyroxene significantly increases both the  
375 bulk modulus and the pressure of the Na-Px/Na-Grt transformation. Previously, the  
376 pyroxene/garnet phase transition in the Na<sub>2</sub>MgSi<sub>5</sub>O<sub>12</sub> was studied in a wide range of *P–T*  
377 parameters (14–18 GPa, 1500–2100°C; Dymshits et al. 2010; 2013). These authors have  
378 shown that at 15 GPa and 1500 °C (which corresponds to the synthesis conditions of Fe-  
379 bearing Na-Mg-Si pyroxene in this study) Na-Maj is stable.

380         The formation of most of Na-rich minerals and phase assemblages in the Earth’s  
381 mantle is related to crystallization of alkaline carbonate-silicate melts (Bobrov et al.  
382 2008). Such melts (Klein-BenDavid et al. 2006) are known from inclusions in diamonds  
383 and are considered to be the most active agents of mantle magmatism and metasomatism,  
384 as well as diamond formation. Walter et al. (2008) suggested that melting occurred due to  
385 the crust-mantle interaction as slabs descended to the mantle and stagnated in the  
386 transition zone being heated up to the carbonated eclogite solidus where they released a  
387 low-degree melt.

388         Similarly, titanium-rich lithologies in the Earth’s mantle are caused by the crust-  
389 mantle interaction and subduction of the oceanic crust containing MORB with ~2 wt%  
390 TiO<sub>2</sub> to different depths (Sours-Page et al. 1999). The new Na-Ti-pyroxene was  
391 synthesized at the upper mantle pressure (7 GPa) (Sirotkina et al. 2016). Unfortunately,  
392 there is still no data on Na-Ti pyroxene/Na-Ti garnet or Na-Ti pyroxene/Ti-bridgmanite  
393 phase transitions. It has also been shown that Ti stabilizes the bridgmanite structure to



394 lower pressure regions, so that Ti-bearing bridgmanite may be stable at pressures above  
395 18 GPa (Bindi et al. 2017). Inclusions in some superdeep natural diamonds provide  
396 evidence for Ti-rich domains at transition zone depths that are likely related to  
397 metasomatism by low-degree melts (e.g., Thomson et al. 2016). The Ti-rich phases are  
398 potentially stable in such Ti-rich environments, where the high content of titanium and  
399 presence of high-Ti phases could have important geochemical effects or act as a tracer for  
400 metasomatic processes.

401 Further work is needed to determine the *PT*-parameters of stability of these  
402 titanium-rich phases, and to determine their thermo-physical and chemical properties.

403

404

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413

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- 578



579 **Table 1.** EoS coefficients resulting from the fits using a third-order Birch-Murnaghan  
580 EoS for unit-cell parameters and volume for Na-Ti Px and Fe-bearing Na-Mg-Si Px

Composition	Birch-Murnaghan	
	$V_0$ ( $\text{\AA}^3$ )	$K_0$ (GPa)
Na-Ti pyroxene	428.57(20)	106.8(2)
Fe-bearing Na-Mg-Si pyroxene	413.20(4)	121.8(4)

581

582 **Table 2.** Equation of state coefficients for unit-cell volumes for Na-bearing pyroxenes

Composition	Birch-Murnaghan			Ref.
	$V_0$ ( $\text{\AA}^3$ )	K (GPa)	K'	
Na-Ti	428.57(20)	106.8(2)	-	This study
Fe-bearing Na-Mg-Si	413.20(4)	121.8(4)	-	This study
$\text{NaMg}_{0.5}\text{Si}_{2.5}\text{O}_6$	407.2	103(2)	6.2(7)	Dymshits et al. 2015
$\text{NaAlSi}_2\text{O}_6$ (Jd)	402.03(2)	136.5(14)	3.4(4)	McCarthy et al. 2008
$\text{NaAlSi}_2\text{O}_6$ (Jd)	402.26(2)	134.0(7)	3.7(6)	Nestola et al. 2006
$\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ (Aeg)	429.25(3)	116.1(5)	4.4(1)	Nestola et al., 2006
$\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ (Aeg)	429.40(9)	117(1)	3.2(2)	McCarthy et al. 2008
$\text{NaFe}^{3+}\text{Si}_2\text{O}_6$ (Aeg)	431.5(1)	126(2)	3.4(10)	Xu et al., 2017

583

584

FIGURE CAPTIONS

585 **Fig. 1.** (a) BSE image of an aggregate of euhedral Na–Ti-pyroxene crystals (light gray)  
586 and in the quenched groundmass of elongate rutile (white) and pyroxene (light gray)  
587 crystals (7 GPa, 1700°C); (b) SE image of Na-Mg-Si pyroxene aggregates in a  
588 groundmass composed of very small pyroxene and stishovite grains (14 GPa, 1500°C)

589 **Fig. 2** Normalized pressure  $F_E$  (GPa) – Eulerian strain  $f_E$  plot for studied pyroxenes.

590 **Fig. 3.** Normalized unit cell parameters of studied pyroxenes.

591 **Fig 4.** The crystal structure of Na-Ti pyroxene at 3 GPa. Shown the configuration of O-  
592 rotated tetrahedral chain with O3-O3-O3 angle of 171.9(8). Given are M1O6 octahedra  
593 and SiO4 tetrahedra. The O3 atoms that can be bonded to M2 are labelled O3<sub>2</sub> and O3<sub>3</sub>,  
594 which are sympathetic and O3<sub>1</sub> and O3<sub>4</sub> which are antipathetic.

595 **Fig 5.** Effective coordination number for M2 site as a function of pressure for studied  
596 pyroxenes

597 **Fig. 6.** Pressure dependence of the selected interatomic distances for Na-Ti Px. Pressure  
598 measurement errors are less than symbol sizes.

599 **Fig. 7.** Pressure dependence of selected interatomic distances in Fe-bearing Na-Mg-Si  
600 pyroxene. Pressure measurement errors are less than symbol sizes.

601 **Fig. 8.** Normalized polyhedral volume of studied pyroxenes

602 **Fig. 9.** Volume – pressure dependence for Na-rich pyroxenes. Errors are less than symbol  
603 sizes. The results of fits using a 2<sup>nd</sup>-order Birch-Murnaghan equation of state are shown  
604 by solid line.

605 **Fig. 10.** Dependence of the bulk modulus on the unit cell volume for  $C2/c$  and  $P2_1/c$   
606 pyroxenes (Arlt and Angel 2000; Gatta et al. 2005; McCarthy et al. 2008). Bulk modulus

607 for Na-rich pyroxenes and  $P2/n$   $\text{NaMg}_{0.5}\text{Si}_{2.5}\text{O}_6$  pyroxene (Dymshits et al. 2015) vary  
608 within the  $K_0^{\text{ant}} - K_0^{\text{sym}}$  range.

Figure 1

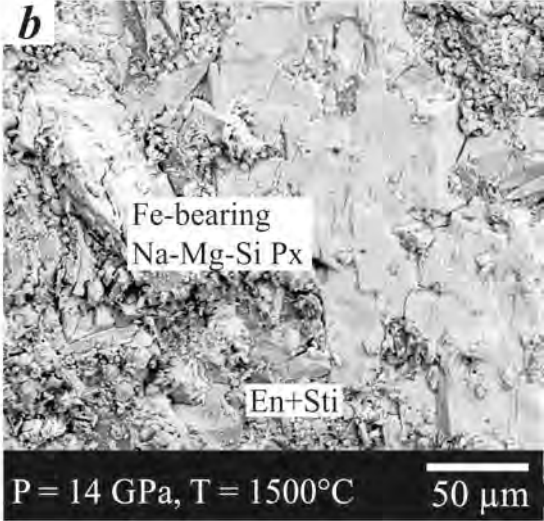
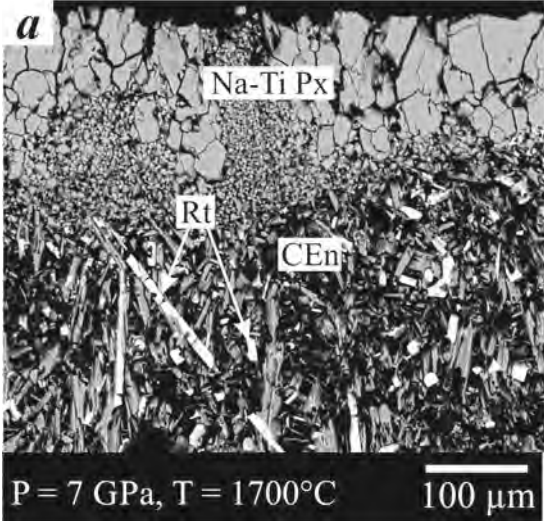


Figure 2

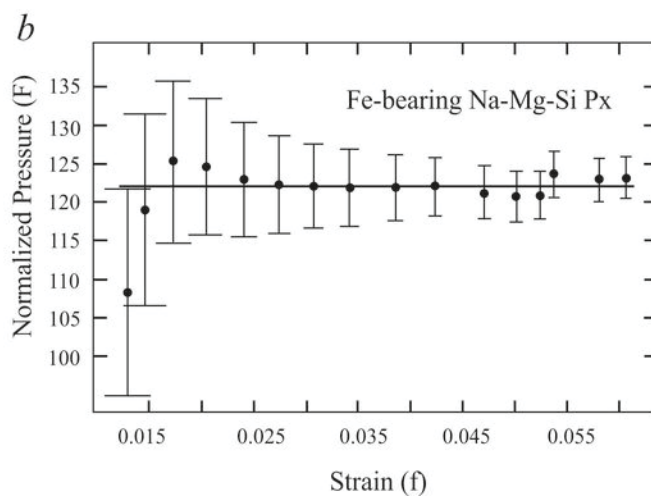
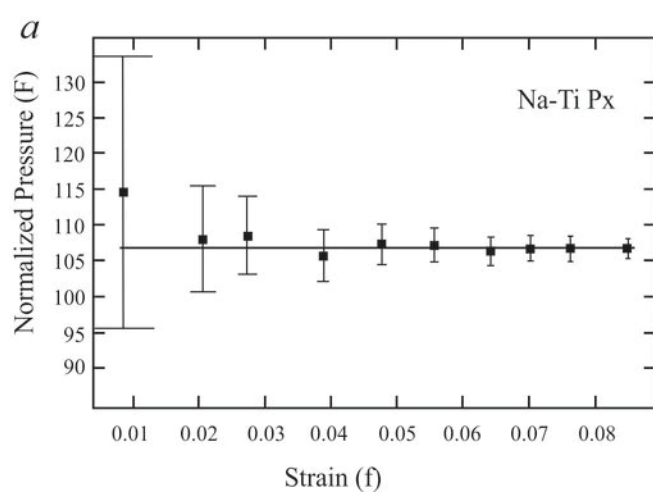
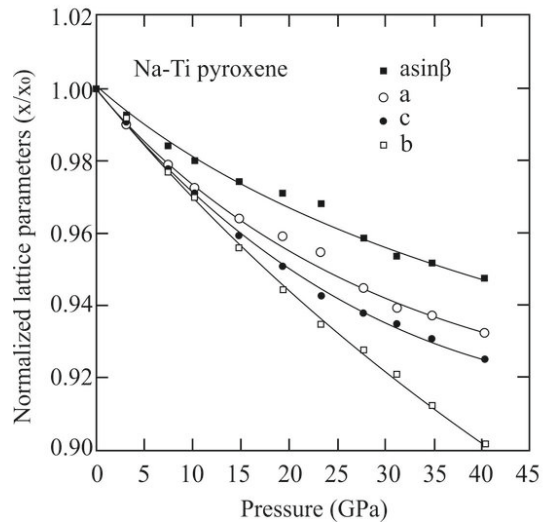


Figure 3

*a*



*b*

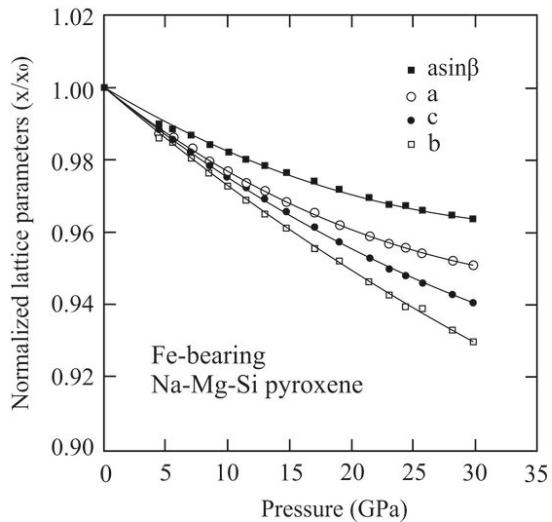


Figure 4

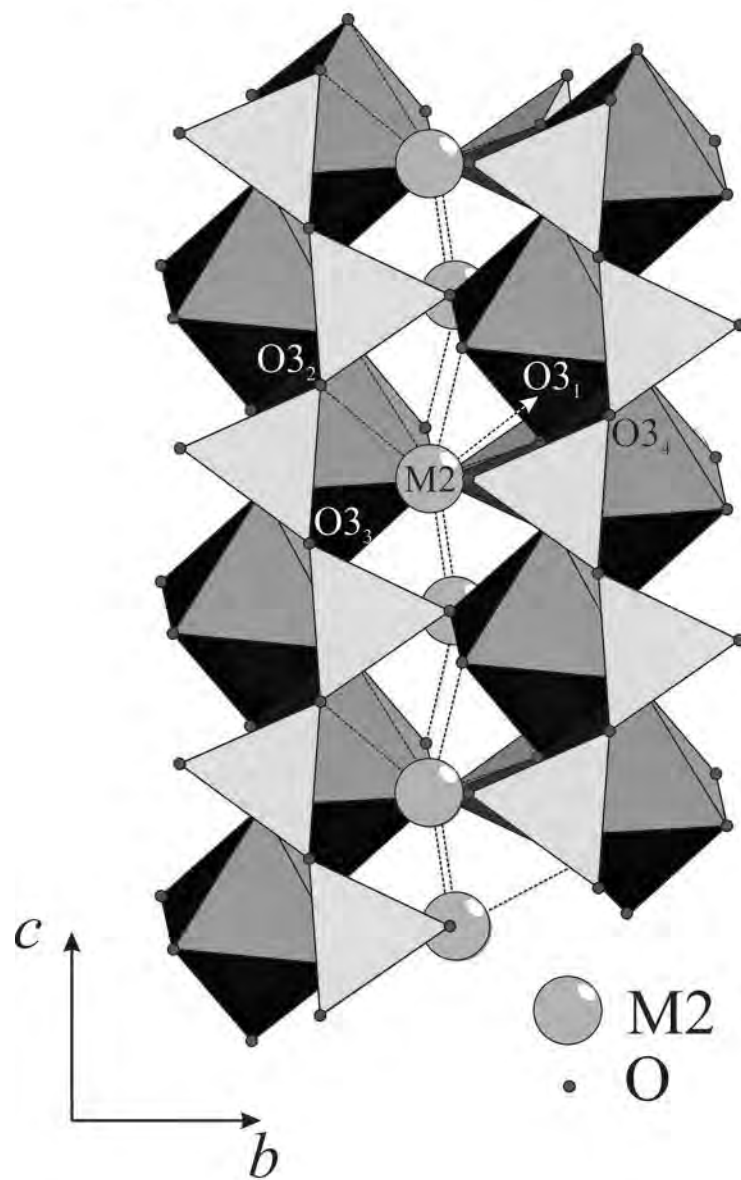
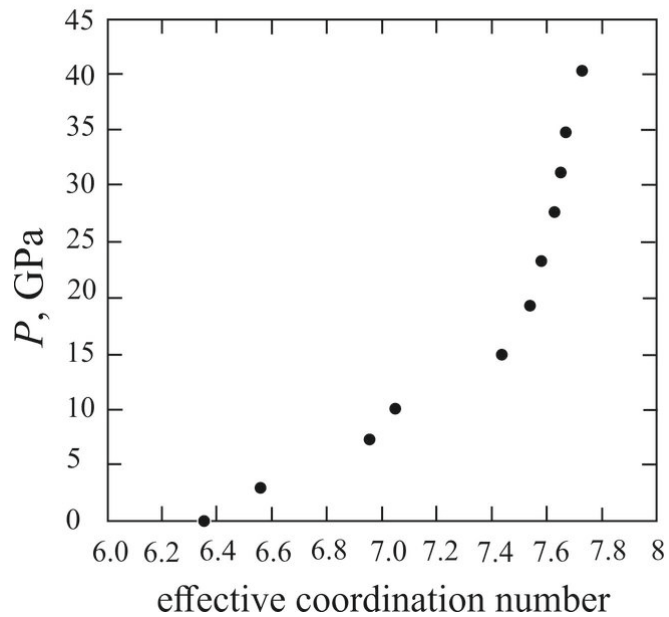




Figure 5

*a*



*b*

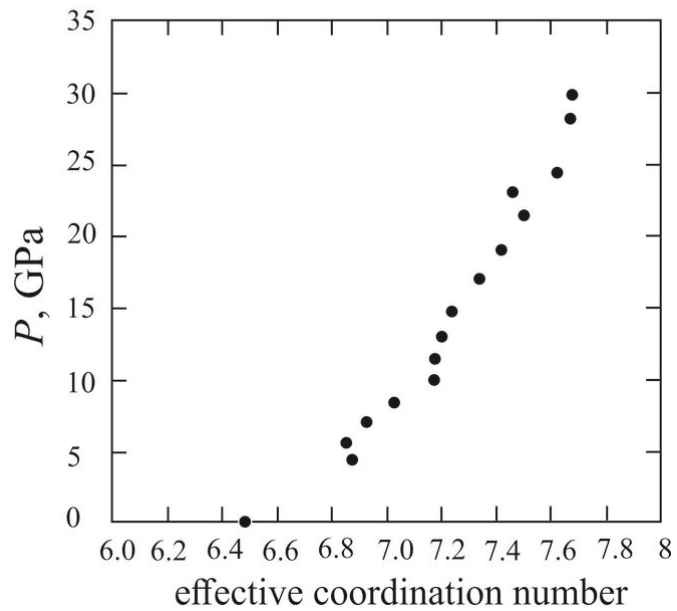


Figure 6a

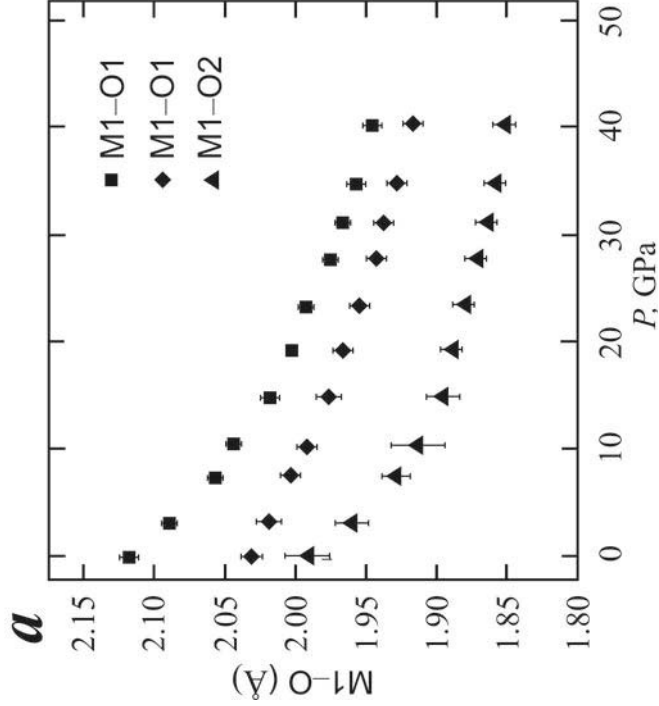


Figure 6b

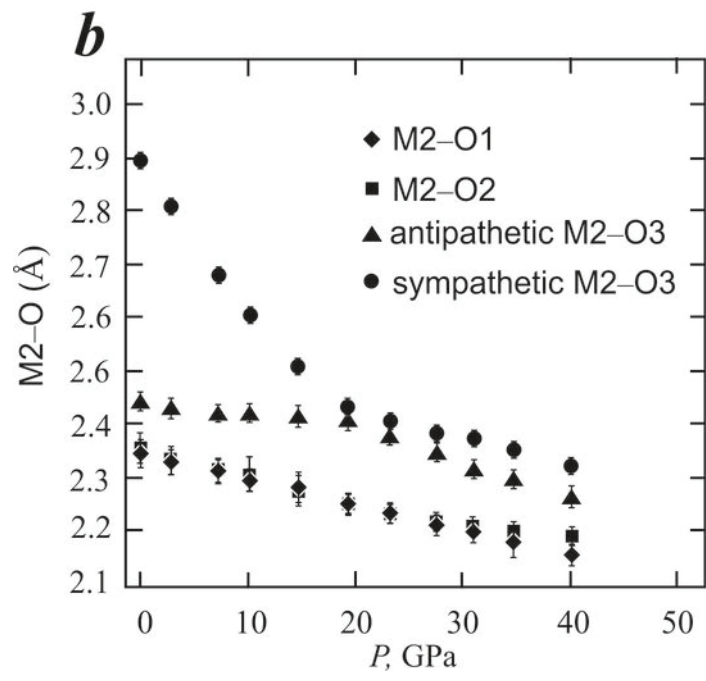


Figure 6c

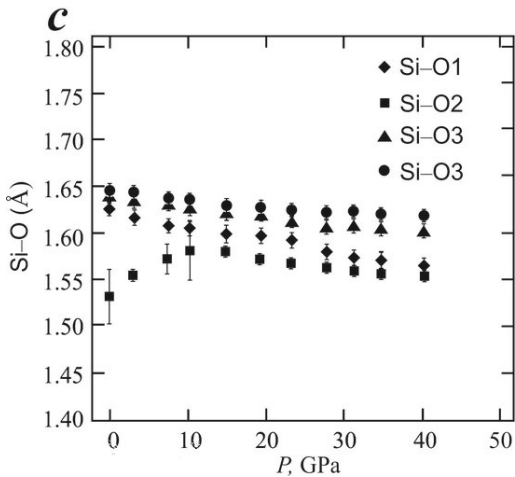


Figure 7a

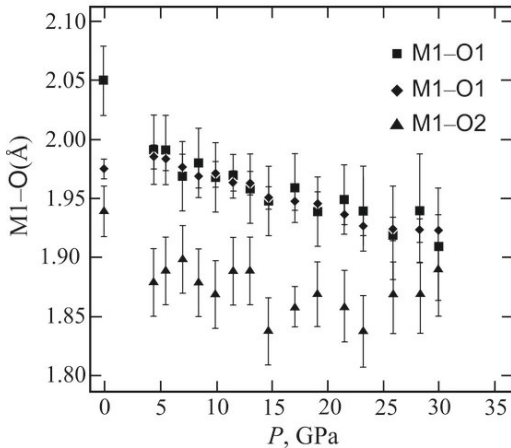


Figure 7b

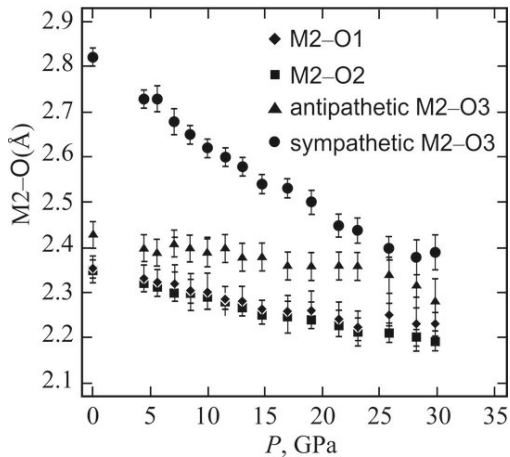


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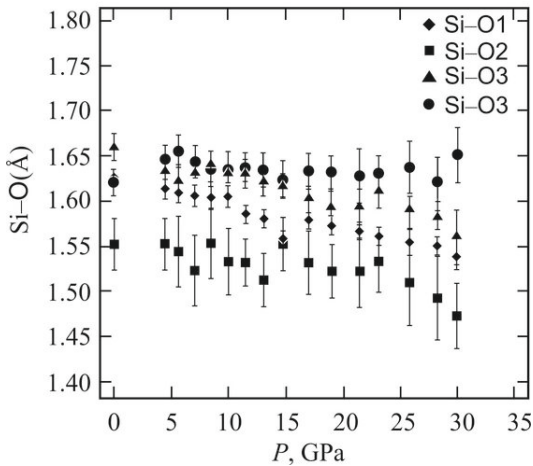


Figure 8

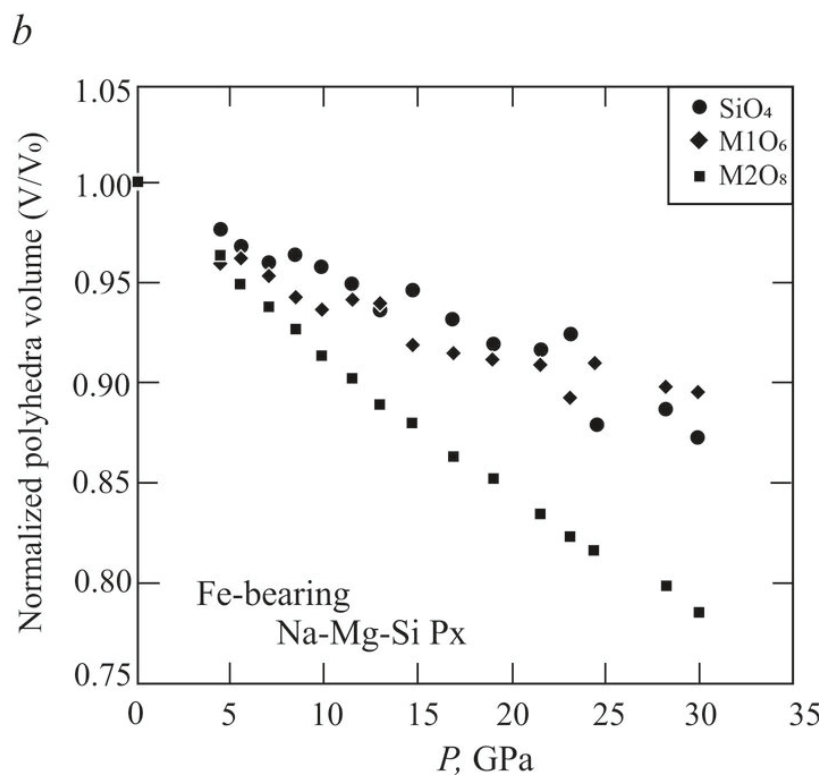
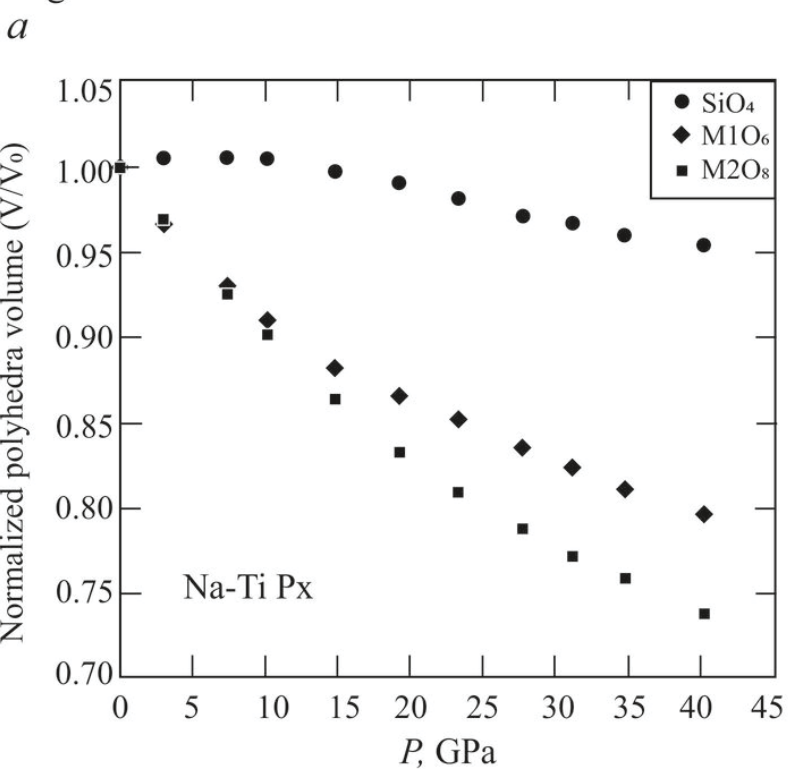




Figure 9

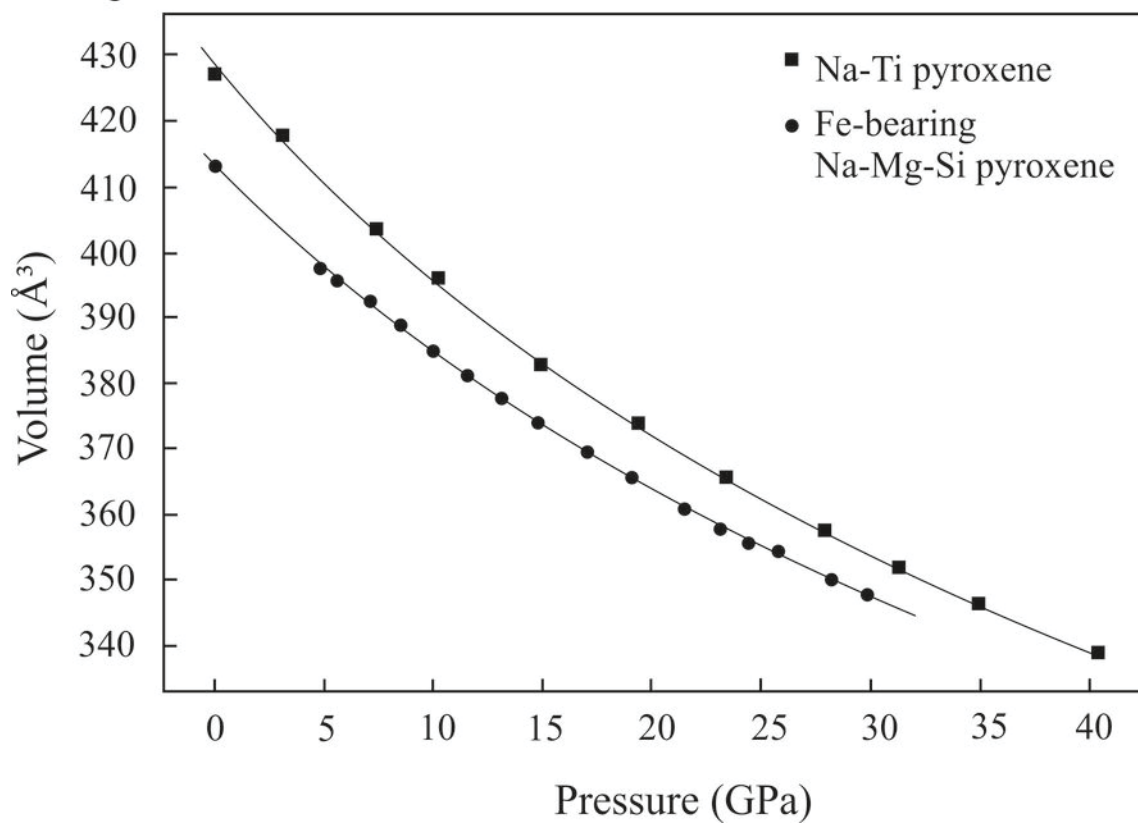


Figure 10

