

# Revision 1

## Sound wave velocities of Fe<sub>5</sub>Si at high pressure and high temperature conditions: implications to lunar and planetary cores

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### Keywords

Fe-Si alloy, Elastic wave velocity, Lunar and planetary cores, High pressure and temperature

### ABSTRACT

Elastic properties of Fe alloys are critical in constraining the compositions of planetary bodies by comparing to the planetary observations. The sound wave velocities and density of an Fe<sub>5</sub>Si (9 wt% Si) alloy in body centered cubic (bcc) structure were measured by combining an ultrasonic technique with synchrotron X-ray radiography at pressure (P) and temperature (T) conditions of 2.6-7.5 GPa and 300-1173 K, respectively. At room temperature, it is observed that

21 adding Si to bcc-Fe increases the compressional wave velocity ( $V_P$ ) but decreases the shear wave  
22 velocity ( $V_S$ ). At high temperatures, we observed a pronounced effect of pressure on the  $V_S$ -T  
23 relations in the Fe<sub>5</sub>Si alloy. The  $V_P$ -density ( $\rho$ ) relationship of the Fe<sub>5</sub>Si alloy is found to follow  
24 the Birch's law in the P-T range of this study, whereas the  $V_S$ - $\rho$  relation exhibits complex  
25 behavior. Implications of these results to the lunar core and the Mercurian core are discussed.  
26 Our results imply that adding Si to a pure Fe lunar core would be invisible in terms of  $V_P$ , but  
27 exhibit a decreased  $V_S$ . Including Si in a sulfur-rich lunar core would display an increased  $V_P$   
28 and a decreased  $\rho$ . Our density and sound wave velocity model provide lower and upper limit for  
29 a Si-bearing lunar core if 1-3wt% Si content of Enstatite chondrite is taken as compositional  
30 analog. A Si-rich (>9wt %) Mercurian core model is derived to satisfy newly observed moment  
31 of inertia values by MESSENGER spacecraft.

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## 34 **INTRODUCTION**

35 It has been widely accepted that the terrestrial planets (such as the Earth and the Mercury) and  
36 their satellites (such as the Moon, Konopliv et al. 1998) possess Fe-dominated cores. One or  
37 more light elements (such as O, Si, S, C, H) may be present in the cores, based on  
38 cosmochemical and geophysical considerations (e.g., Anderson and Ahrens 1994, Anderson and  
39 Isaak 2002, Badro et al. 2007). Among the potential light elements, Si remains a dominant  
40 candidate, based on several constraints. First, it is experimentally demonstrated that Si has a  
41 significant solubility in liquid Fe (25 wt% Si at the eutectic at 21 GPa, Kuwayama and Hirose,  
42 2004) at high pressure and temperature (high P-T) conditions (Fischer et al., 2013). Because  
43 magma ocean events, which is characterized by the widespread molten Fe and silicate melt,

44 might occur in many inner-solar planetary bodies (such as the Mercury and the Earth) and the  
45 Moon, the high solubility of Si in liquid Fe provides a mechanism for Si entering into those  
46 planetary cores during the silicate-metal differentiation process (Ricolleau et al., 2011, Badro et  
47 al, 2015). Second, the siderophile element partitioning data strongly support that early accretion  
48 of the Earth and the Mercury occurred under highly reduced conditions (Malavergne et al. 2010,  
49 Javoy et al., 2010). Moreover, the Gamma-ray spectrometers of the Mercury's MESSENGER  
50 spacecraft revealed that an amount of 1-4wt% S could be present on the Mercury's surface,  
51 implying that the oxygen fugacity of the Mercury's interior is rather low, with an IW ranging  
52 from -2.6 to -7.3 (Chabot et al., 2014). The extremely low oxygen fugacity is compatible with  
53 the reduced nature of Si. Thus substantial Si could have been incorporated into the cores during  
54 the core-mantle segregation.

55 Pure iron adopts at least three polymorphs at high P-T, including body-centered-cubic (bcc),  
56 face-centered-cubic (fcc), and hexagonal-closed-packing (hcp). The fcc- and hcp-Fe are  
57 commonly viewed to be the dominant phases at terrestrial planetary cores, because of their  
58 stability fields of the related P-T conditions. However, high pressure experimental and  
59 theoretical studies suggested that the addition of Si or Ni in Fe can stabilize the bcc structure at  
60 expanded P-T conditions (Lin et al., 2002, Dubrovinsky et al., 2007, Vocadlo et al., 2008,  
61 Kuwayama et al., 2009). For example, in situ X-ray diffraction experiments on an Fe<sub>5.3</sub>Si alloy  
62 found a stabilized mixture of bcc and hcp phases up to at least 150 GPa and 3000 K (Lin et al.,  
63 2009). Therefore, a bcc structured Fe-Si alloy could be a candidate phase in the cores of  
64 terrestrial planets and their satellites.

65 Sound wave velocity is a critical physical parameter for constraining the planetary core  
66 compositions. In conjunction with the seismological observations of the planetary interior, it

67 provides a direct approach to model the nature of the inaccessible planetary interiors. Multiple  
68 techniques, including ultrasonic techniques, shock compression, high-energy resolution inelastic  
69 X-ray scattering (HERIXS), and nuclear resonant inelastic X-ray scattering (NRIXS), have been  
70 adapted to measure  $V_P$  and  $V_S$  mostly on hcp- and fcc-Fe and their alloys by several groups  
71 (Fiquet et al., 2001, Mao et al., 2001, Lin et al., 2005, Badro et al., 2007, Mao et al., 2012,  
72 Antonangeli et al., 2004, 2015a, b, 2018). HERIXS technique can probe the momentum-resolved  
73 phonon dispersions, from which  $V_P$  is fitted. And  $V_S$  is derived by combining the measured  $V_P$   
74 and equation of state (density and adiabatic bulk modulus). The resultant sound velocity  
75 depends strongly on how well the data sample the linear part of the phonon dispersion and on the  
76 knowledge of sample texture (Antonangeli and Ohtani 2015b). The NRIXS method provides  
77 information of partial phonon density of states (pDOS), through which the Debye sound velocity  
78 can be obtained. Together with information of density and adiabatic bulk modulus,  $V_P$  and  $V_S$   
79 can then be determined (Shen and Mao, 2017). In shock experiments, temperature is not well  
80 determined, and is tied with pressure along a Hugoniot. The ultrasonic method is a direct way to  
81 measure  $V_P$  and  $V_S$  at high P-T conditions (Urlick 1947). This method has been recently  
82 successfully used in conjunction with X-ray synchrotron radiation, providing insightful  
83 information of  $V_P$  and  $V_S$  of several geophysical important materials at high P-T (Higo et al.,  
84 2009, Kono et al., 2010, 2012, Li et al., 2007, 2014).

85 Sound wave velocity measurements on bcc Fe-Si alloys are relatively few. The only available  
86 sound wave velocity data were  $V_P$  of a  $Fe_{5.3}Si$  alloy reported by Lin et al. (2003a) by NRIXS and  
87 Liu et al. (2014) by HERIXS measurements. Notably, there is an approximately 10% difference  
88 between their  $V_P$  results, although the same stoichiometric samples with  $Fe_{5.3}Si$  were used in  
89 these two studies. Moreover, these two measurements were conducted only at room temperature.

90 Temperature effect on sound wave velocities of bcc Fe-Si alloys is still unknown. In this study,  
91 we have conducted ultrasonic measurements on a bcc Fe<sub>5</sub>Si sample at simultaneous high P-T  
92 conditions. We present the effect of Si on V<sub>P</sub> and V<sub>S</sub> of the bcc Fe-Si alloy at high P-T  
93 conditions. The implications of these observations for the planetary core compositions are  
94 discussed.

## 95 **EXPERIMENTS**

96 High P-T ultrasonic velocity measurements were conducted using a Paris-Edinburgh press at  
97 the 16-BMB station at the Advanced Photon Source, Argonne National Laboratory (Kono et al.,  
98 2012). The Fe<sub>5</sub>Si powder, from Goodfellow, was hot-pressed in a piston-cylinder apparatus at 1  
99 GPa and 1073 K for 2hrs. The hot-pressed Fe<sub>5</sub>Si disk size was about 1.5 mm (diameter) ×  
100 0.8~1.2 mm (length). Mirror-finished sample surfaces were produced by carefully polishing  
101 using 1 μm diamond paste. A schematic illustration of the cell assembly is shown in Figure 1.  
102 Pressures were determined by X-ray diffraction of Au using the equation of state by Tsuchiya et  
103 al. (2003). The static pressures were evaluated based on second-order Birch-Murnaghan  
104 Equation of State. And thermal pressures were calculated based on Mie-Grüneisen equation  
105 ( $P_{th} = \frac{r \cdot E_{th}}{v}$ , where P<sub>th</sub> and E<sub>th</sub> are thermal pressure and energy, respectively. r is Grüneisen  
106 parameter and v is volume. E<sub>th</sub> is evaluated based on Debye model). The typical errors in  
107 pressure are 2-8%. The sample was heated in a graphite cylinder, with temperatures estimated  
108 from a previously calibrated power-temperature curve with an identical assembly (Jing et al.,  
109 2014). The temperature uncertainties are about 100 K. The experimental P-T conditions were  
110 2.6-7.5 GPa and 300-1173 K, respectively. For each run, we compressed the sample to a target  
111 pressure and then increased temperature. At any given temperature we waited approximately 1-

112 2mins before collecting ultrasonic, X-ray radiography, and X-ray diffraction data, in order to  
113 reduce the deviatoric stress imposed on the sample during compression.

114 At each specified P-T conditions, ultrasonic interference and radiographic imaging techniques  
115 allow simultaneous determination of travel time and sample length respectively, from which  
116 sound velocities were yielded. Figure 2 shows an example of the P- and S-wave signals obtained  
117 at 2.6 GPa and 985 K. 30 MHz and 20 MHz electrical sine waves were generated for  $V_P$  and  $V_S$   
118 measurements, respectively. They propagate into sample assembly and reflected at the interfaces,  
119 which were labeled as  $R_0$  (anvil/ $Al_2O_3$ ),  $R_1$  ( $Al_2O_3/Fe_5Si$  sample) and  $R_2$  ( $Fe_5Si$  sample/ $BN$ ).  
120 Then the travel time for the sound velocity can be determined by difference of arrivals of  $R_1$  and  
121  $R_2$ . The uncertainty in the travel time is within  $\pm 0.1$ ns, corresponding to less than 0.1%  
122 uncertainties in  $V_P$  and  $V_S$ , respectively. The sample lengths under high P-T were measured from  
123 an X-ray radiography image using a high-resolution CCD camera (Kono et al., 2012). The pixel  
124 resolution was  $0.948\mu\text{m}/\text{pixel}$ . The error on the measured sample length is less than  $1\mu\text{m}$ . The  
125 resultant uncertainty introduced by sample length measurements for elastic waves is less than  
126 0.03% and 0.18% at 300 K and high T, respectively.

## 127 **RESULTS AND DISCUSSION**

### 128 **Equations of state**

129  $Fe_{5.2}Si$  is considered to adopt the  $D0_3$  crystal structure (cubic, space group:  $Fm\bar{3}m$ , 225) at  
130 ambient conditions (Massalski, 1986) and under compression at 300 K to at least 29 GPa  
131 (Fischer et al., 2013). Our room temperature data show that this alloy maintains a bcc structure  
132 with a different space group ( $Im\bar{3}m$ , 229) at 3.6-7.5 GPa (Figure 3). It may be related to the high  
133 P-T synthesis conditions (1 GPa and 1073 K for 2hrs). Fischer et al. (2013) found that the  $Fe_5Si$   
134 alloy would convert into an fcc+ $B_2$  mixture above 10 GPa and 1000 K. In the P-T range of this

135 study up to 6.1 GPa and 1173 K, we did not observe any diffraction peaks corresponding to  
136 either the fcc or the B<sub>2</sub> phase. Our data show that the Fe<sub>5</sub>Si alloy adopts a bcc structure  
137 throughout our experimental P-T conditions.

138 The unit-cell volumes were obtained simultaneously together with the elastic velocity  
139 measurements, with the results summarized in Table 1. The obtained pressure-volume data at 300  
140 K were fitted into the second-order Birch-Murnaghan equation of state (EOS). The resultant  
141 isothermal bulk modulus ( $K_{T0}$ ) and volume ( $V_0$ ) are 188 (18) GPa and 23.2(2) Å<sup>3</sup>, respectively.  
142 In addition, the thermal expansion coefficient ( $\alpha_T$ ) over a temperature range of 800-1154 K at 2.6  
143 GPa is  $5.27(4.0) \times 10^{-5} \text{ K}^{-1}$ . Our  $\alpha_T$  and  $V_0$  are in general agreement with those by Zhang et al.  
144 (1999) ( $\alpha_T = 4.74 \times 10^{-5} \text{ K}^{-1}$ ,  $V_0 = 23.0 \text{ Å}^3$ ), while  $K_{T0}$  is relatively larger than Zhang's results  
145 ( $K_0 = 161 \text{ GPa}$ ).

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#### 148 **V<sub>P</sub> and V<sub>S</sub> at 300 K**

149 Figure 4 shows  $V_P$  and  $V_S$  of the bcc Fe<sub>5</sub>Si alloy and pure Fe at room temperature as a function  
150 of pressure. Our  $V_P$  results are consistent with those of Liu et al. (2014) by HERIXS, but larger  
151 than those of Lin et al. (2003a) by NRIXS. Similarly, it has been known that the  $V_P$  of bcc-Fe is  
152 also consistent between ultrasonic (Shibazaki et al., 2016, Chigarev et al., 2008, Fiquet et al.,  
153 2001) and HERIXS measurements (Liu et al., 2014). Because NRIXS measures Debye sound  
154 velocity ( $V_D$ ), and calculate  $V_P$  and  $V_S$  based on  $\rho$  and bulk modulus determined in separate  
155 experiments, the inconsistency of the results from the NRIXS measurement may be due to the  
156 indirect approach. Our study, together with the results of Liu et al. (2014), supports that alloying  
157 Si in bcc-Fe increases  $V_P$  at room temperature.

158 The available S-wave data of bcc-Fe and Fe-Si alloys are limited. The only available S-wave  
159 data of a Fe<sub>5.3</sub>Si alloy was the NRIXS results by Lin et al. (2003a). Our obtained V<sub>S</sub> are slightly  
160 larger than that of Lin et al. (2003a), with both data sets displaying lower V<sub>S</sub> than that of bcc-Fe  
161 (Shibazaki et al., 2016, Chigarev et al., 2008). It needs to be pointed out that due to the poor  
162 signal-to-noise ratio, probably arising from small acoustic reflection coefficient between the  
163 Al<sub>2</sub>O<sub>3</sub> buffer rod and the bcc-Fe<sub>5</sub>Si sample, only one data point of V<sub>S</sub> was obtained at room  
164 temperature in this study. At room T, acoustic impedance for V<sub>S</sub> of the Fe<sub>5</sub>Si sample is ~25 at 7.7  
165 GPa, which is similar to that of the buffer rod Al<sub>2</sub>O<sub>3</sub> (~25, e.g., Kung et al., 2000). Nevertheless,  
166 at high temperatures, this situation was improved, because the V<sub>S</sub> of the Fe<sub>5</sub>Si sample decreases  
167 significantly, with reduced acoustic impedances and improved signals in acoustic reflections.

#### 168 **Temperature dependence of V<sub>P</sub> and V<sub>S</sub>**

169 Liu et al. (2014), Shibazaki et al. (2016) and Antonangeli et al. (2015a) have investigated the  
170 effect of temperature on V<sub>P</sub> and V<sub>S</sub> of bcc-Fe under compression, as shown in Figure 5. In bcc-  
171 Fe, both V<sub>P</sub> and V<sub>S</sub> decrease with increasing temperature. The temperature dependences of V<sub>P</sub>  
172 and V<sub>S</sub> under different pressures remain almost the same in a temperature range of 300-700 K.  
173 These results for bcc-Fe are compared with our high temperature results of V<sub>P</sub> and V<sub>S</sub> for the  
174 Fe<sub>5</sub>Si sample at 2.6-6.1 GPa (Figure 5). It shows that in the Fe<sub>5</sub>Si alloy the temperature  
175 dependence of V<sub>S</sub> is much stronger than that of V<sub>P</sub> at a given pressure. For example, at 2.6 GPa  
176 with a temperature decrease of 354 K, ΔV<sub>P</sub> is only 4.9%, compared to a ΔV<sub>S</sub> of 20.4% in the  
177 Fe<sub>5</sub>Si alloy.

178 Meanwhile, the temperature dependence of V<sub>S</sub> in the bcc Fe<sub>5</sub>Si sample weakens as pressure is  
179 increased, which is in contrast to the temperature independence of V<sub>S</sub> in bcc-Fe with varying  
180 pressure. For example, with the same temperature interval (ΔT=350K), ΔV<sub>S</sub> is 5.3% in bcc-Fe at



181 2-2.7 GPa, 4-4.5 GPa and 5.4-5.8 GPa (Shibazaki et al., 2016), while  $\Delta V_S$  in the Fe<sub>5</sub>Si sample is  
182 ~20% and ~10% at 2.6 GPa and 5.5-6.1 GPa, respectively. Temperature dependence of  $V_P$  can  
183 not be assessed since our present data are at one pressure.

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### 186 **Applicability of the Birch's law**

187 The Birch's law suggests that the sound wave velocity of rocks is mainly a function of  $\rho$  and  
188 mean atomic weight:  $V=a(m)+b\times\rho$ , where a and b are Birch's constants and m is the mean  
189 atomic weight (Birch 1960). On the other hand, the validity of the Birch's law for different Fe  
190 phases is still under debate. Antonangeli et al. (2010, 2015a, 2015b) reported that bcc, fcc and  
191 hcp Fe phases follow a linear  $V_P$ - $\rho$  relation over their investigated P-T ranges (0-19 GPa, 300-  
192 1150 K). In contrast, Shibazaki et al. (2016) showed that the  $V_P$ - $\rho$  relation depends on  
193 temperature for bcc-Fe at 2-6.3 GPa and 300-814 K. Figure 6a shows our  $V_P$ - $\rho$  data collected at  
194 2.6-7.5 GPa and 300-1154 K, together with previous reported  $V_P$ - $\rho$  datasets. Our data show a  
195 linear  $V_P$ - $\rho$  relation for bcc Fe<sub>5</sub>Si not only at room temperature condition but also at high  
196 temperature conditions:  $V_P=1.32\times\rho-3.49$  ( $R^2=0.99$ ). Thus our results confirmed the validity of  
197 Birch's law for Fe-Si alloy over the P-T range of this study. The Birch's law seems to hold for  
198 the rest components as shown in figure 6a regardless of the phases and applied experimental  
199 temperatures in a broad density range. The only exception is bcc iron ( $R^2=0.86$ ), discussed by  
200 Shibazaki et al. (2016).

201 On the other hand,  $V_S$ - $\rho$  data for bcc-Fe and Fe-Si alloys are few and appear to be more  
202 complex (Figure 6b). It shows that our 300 K point is consistent with Lin's (2003a) room T data  
203 but far from the rest high temperature  $V_S$  data. The possible reason for the large derivation is that

204 temperature might have a fundamentally important effect on  $V_S$ . Similar observation has been  
205 made by Shibazaki et al. (2016) that in bcc-Fe  $V_S$  strongly depend not only on density but also  
206 on temperature. Therefore, cautions must be taken when applying the Birch's law for  $V_S$ .

## 207 **IMPLICATIONS TO THE SOUND WAVE VELOCITY MODELS OF THE LUNAR** 208 **AND MERCURIAN CORES**

209 Growing evidence suggests that the terrestrial planets and their satellites, such as the Mercury,  
210 the Earth and the Moon, share lots of similarities in many ways, such as the layered structures  
211 and the elements variety (Brown and Elkins-Tanton 2009, Lin et al., 2016). Si is suggested to be  
212 a highly potential light element at the P-T conditions of the cores of the Earth (125-350 GPa,  
213 3000-6000 K, Wänke and Dreibus 1997) and the Mercury (8-40 GPa, 1700-2200 K, Chabot et  
214 al., 2014) based on geophysical and geochemical constraints. There is no direct evidence yet that  
215 Si may exist in the lunar core (5-6GPa, 1300-1900 K, Wieczorek 2006). However, according to  
216 giant impact theory, the Moon might form from similar building blocks to that of the Earth, as  
217 demonstrated by isotopic evidences including oxygen, chromium and titanium (Dauphas 2017).  
218 Enstatite chondrite meteorites may represent possible building blocks of the Earth-Moon system  
219 as they have almost indistinguishable isotopic compositions (Qin et al., 2010, Javoy et al., 2010,  
220 Warren et al., 2011, Zhang et al., 2012, Young et al., 2016). Fe-Ni is an abundant mineral in  
221 Enstatite chondrite and 1-3wt% Si is being found in Fe-Ni metal solution (Mason 1966).  
222 Therefore, Si might be an important light element in lunar core, as suggested for the Earth  
223 (Antonangeli et al., 2010).

224 Here we calculated  $V_P$  and  $V_S$  of our 9 wt% Si and 91 wt% Fe sample under the P-T  
225 conditions of the Mercury and Lunar cores. The high P-T sound wave velocity is calculated as:

$$226 \quad V = V_{(P,300K)} + \left(\frac{dV}{dT}\right)_P \times \Delta T ,$$

227 where  $V_{(P,300K)}$  and  $(\frac{dV}{dT})_P$  are the elastic wave at high pressure and 300 K and temperature  
228 dependence of elastic wave, respectively. First, we extrapolated the sound wave velocity to the  
229 target pressure using  $V_{(P\text{-wave},300K)} = 0.04(1) \times P + 6.34(1) (R^2 = 0.98)$  and  
230  $V_{(S\text{-wave},300K)} = 0.032(1) \times P + 2.99(2) (R^2 = 0.91)$ , which were derived by fitting our datasets  
231 (Figure 1). As only one data point of  $V_S$  is available at 300 K, the slope of  $V_S$ -P relation from  
232 Lin et al. (2003) was used to construct  $V_{(S\text{-wave},300K)} - P$  relations, i.e.  
233  $V_{(S\text{-wave},300K)} = 0.032(1) \times P + 2.99(2) (R^2 = 0.91)$ . Secondly, temperature effect was evaluated  
234 through  $(\frac{dV_P}{dT})_{2.6\text{GPa}} = -0.0008(1) \text{ km/s} (R^2 = 0.89)$  and  $(\frac{dV_S}{dT})_{5.5\text{GPa}} = -0.00097 \text{ km/s}$ ,  
235 which were derived by fitting our high temperature  $V_P$  and  $V_S$  data at temperature ranges of 800-  
236 1154 K and 854-1173 K, respectively. Based on our sound wave velocity data, the estimated  $V_P$   
237 and  $V_S$  profiles, together with  $\rho$  profiles for the interiors of the Moon and the Mercury are shown  
238 in Figures 7-8.

239 Due to the paucity of seismic waves that penetrate the deepest 500 km of the Moon  
240 identified in the Apollo seismic data, the composition and status constraints on deep lunar  
241 interior are insufficiently known at present. At present most the lunar interior density and sound  
242 wave velocity models only consider S as a light element in the solid inner core or a pure fcc Fe  
243 core. The density and sound wave velocity models of a Si constituent solid inner core have not  
244 been developed yet. For example, Weber et al. (2011) assumed  $V_P$  and  $V_S$  to be 4.2 km/s and 2.2  
245 km/s for a S-rich solid inner core based on high pressure elasticity measurements of iron alloys  
246 (Sanloup et al., 2000, Williams 2009, Balog et al., 2003). In contrast, based on an fcc Fe lunar  
247 inner core model, Antonangeli et al. (2015a) proposed that  $V_P$  and  $V_S$  should be 4.7-5.7 km/s and

248 2.1-3.4 km/s, respectively. Based on the experimental results of this study, a Si-rich lunar inner  
249 core would possess following characteristics compared to a pure Fe or a S-rich lunar core (Figure  
250 7):  $V_P$  and  $\rho$  of a Si-rich core is comparable and slightly smaller than their counterparts in a pure  
251 Fe core, respectively. A Si-rich core has much higher  $V_P$  and moderately smaller  $\rho$  than those of  
252 a S-rich core.  $V_S$  of a Si-rich core are relatively smaller than those of a pure Fe and S-rich cores  
253 (Figure 7). It has been established in the Fe-rich Fe-Si alloy the density and sound wave velocity  
254 decrease and increase respectively with increasing Si content at 300 K (Lin et al., 2003b). Our  
255 proposed models were built based on the assumption that lunar core contains 9 wt% Si. If Fe-Ni  
256 metal alloy in Enstatite chondrite, which contains 1-3wt% Si, is taken as composition analogy of  
257 the lunar core. Then our present model (Figure 7) provides lower and upper values for density  
258 and sound wave velocity respectively in a 1-3wt% Si-bearing core, assuming thermal expansion  
259 and  $(dV/dT)$  at lower Si content (1-3wt%) are comparable to their counterparts at 9 wt% Si  
260 content. It should be note that moon might form under relatively more oxidized condition (IW-1,  
261 Jones and Palme, 2000) compared to  $fO_2$  values of Enstatite chondrite(IW-3 to -8, McCoy et al.,  
262 1999), which indicates less Si (<1-3wt%) entered into lunar core during core-mantle segregation.  
263 However, reducing Si concentration in Fe-Si alloy will result in larger density and smaller sound  
264 velocity. Therefore, the constraints of lowers values for density and upper values for sound wave  
265 velocity are still valid in a less Si-bearing (<1-3wt%) lunar core.

266 As the innermost and the second densest planet of the solar system, the Mercury holds a  
267 crucial position in understanding the formation and the evolution of the terrestrial planets.  
268 Constraints on the composition and interior structure of the Mercury mainly come from  
269 observations of MARINER 10 and MESSENGER spacecrafts. An intrinsic magnetic field in the  
270 Mercury is among major accomplishments of these two missions, and it brought up the idea that

271 the Mercury should have a core which might be partially molten (our experimental data were  
272 collected in solid phase zone, hereafter discussions and models are specifically for Mercurian  
273 solid inner core only). Knibbe and Westrenen (2015, 2018) conducted a series of studies to  
274 investigate the thermal and magnetic field evolution of a Fe-Si alloy Mercurian core. Their  
275 results indicate that a Si dominated Mercurian core is highly possible. In such a Fe-Si core, no  
276 compositional convection is generated upon core solidification, in agreement with magnetic field  
277 indications of a stable layer at the top of the Mercury. Moreover, a Si-bearing core has the  
278 advantage to explain the highly reduced nature in the Mercury, as opposed by a Fe-S core. We  
279 calculated density and sound wave velocity of the Fe<sub>5</sub>Si alloy at pressure and temperature  
280 conditions corresponding to the interior of the Mercury (Figure 8). By comparing our  
281 measured  $\rho$  between 300 K and 1700 K (estimated T at the Mercury's CMB) together with EOS  
282 measurements of 16wt% Si (Fischer et al., 2013), it clearly shows that the Si content has a much  
283 stronger effect on  $\rho$  than temperature. To our best knowledge, only two literatures, which were  
284 both published by Knibbe and Westrenen (2015, 2018), specifically studied and yielded the  
285 interior density models for a Si-bearing Mercurian core. Polar moment of inertia ( $C/MR^2$ ) and  
286 fraction of polar moment of outer solid shell ( $C_m/C$ ) are two important parameters to constrain  
287 the density distribution of the Mercury's interior in particular. Knibbe and Westrenen (2015,  
288 2018) calculated a large number of Mercury's density profiles as a function of Si content using  
289 Monte Carlo approach. And corresponding  $C/MR^2$  and  $C_m/C$  were calculated for each density  
290 profiles. To satisfy the newly updated  $C/MR^2$  and  $C_m/C$  values by radio tracking data from the  
291 MESSENGER spacecraft (Mazarico et al., 2014, Stark et al., 2015), Knibbe and Westrenen  
292 estimated the average density to be 6.5~7.5g/cm<sup>3</sup> in a Si-bearing Mercurian core. And they  
293 proposed the corresponding Si content, respectively, to be 20 wt% and 7 wt%. Figure 8a shows

294 that their density profiles of 7 wt% and 20 wt% Si are systematically lower than those from  
295 Fisher et al. (2013) and the results of this work. Two possible sources may contribute to this  
296 discrepancy. First, the density profiles in Knibbe and Westrenen (2018) were interpolated and  
297 extrapolated linearly based on EOS parameters of pure fcc Fe (Komabayashi and Fei, 2010) and  
298 Fe<sub>71</sub>Si<sub>29</sub> (~17 wt% Si) (Lin et al., 2003b). The effect of temperature on EOS of Fe<sub>71</sub>Si<sub>29</sub> was not  
299 taken into account. Secondly, Fe<sub>71</sub>Si<sub>29</sub> is in B2 phase in Lin's (2003b) studied P-T range, which  
300 will make it difficult to inter/extrapolate with a phase in different structure (fcc-Fe). In order to  
301 satisfy density constraints of 6.5~7.5g/cm<sup>3</sup>, our results suggest a Si content in the Mercurian core  
302 higher than 9 wt%. In Figure 8a, density profiles of Fe<sub>2.6</sub>Si (16 wt% Si, Fischer et al., 2013) at  
303 300 K and 1700 K ( $\alpha_T$  of Fe<sub>2.6</sub>Si sample is unknown, we used  $\alpha_T$  of Fe<sub>5</sub>Si sample instead to  
304 correct the density of Fe<sub>2.6</sub>Si sample to high T) were shown as well. A Si abundant (>16 wt%)  
305 Mercurian core could even be possible given the EOS measurements and high-T density  
306 corrections were correct. Presently, direct observation on Mercurian core composition is not  
307 possible. Sound wave velocity models for Mercurian core are quite few and mostly from elastic  
308 wave measurements and thermodynamic calculations. Figure 8b compared the sound wave  
309 velocity models of a Fe-Ni (10% Ni by weight) alloy core (thermodynamic model by Lv et al.,  
310 2011), a pure fcc Fe core (High P-T measurements by Antonangelia et al., 2015a) and a Fe-Si  
311 alloy core (9% Si by weight) (this work). It shows that incorporating Ni in pure Fe results in an  
312 increased sound wave velocity while adding Si has the opposite effect. Moreover, even the  
313 similar amount of light element influence the sound wave velocity to quite different extent. For  
314 example, additional 10 wt% Ni in pure fcc Fe result in 18~19% increment in both  $V_P$  and  $V_S$ .  
315 While  $V_P$  and  $V_S$  with additional 9 wt% Si are about 6.4 % and 43 % smaller than that of a pure  
316 fcc Fe, respectively.

317 Comparing laboratory measured density and sound wave velocity values with planetary  
318 observation data is a direct approach to constrain the deep interior status and compositions. For  
319 the moon, our study shown that a Si-rich lunar core exhibits comparable  $V_P$  and different  $V_S$  in  
320 contrast to pure Fe core or S-rich core. This observation stresses the importance of simultaneous  
321 match of  $V_P$  and  $V_S$  when constraining lunar core composition use seismograms data and high  
322 pressure elastic data. Present seismic data of lunar core are from Apollo mission and far less than  
323 that required to constrain the interiors. However, international community has shown long term  
324 ambitions to explore outer space and great achievements have been made. For example,  
325 China's series of Chang'e Moon missions have sent spacecraft to lunar orbit and the lunar surface.  
326 Seismometer deployment on the lunar surface is also being planned around 2025. Laboratory  
327 proposed sound wave velocity models, including ours, are likely to be testable by the upcoming  
328 missions.

329 For the Mercurian core, our study suggests a large amount ( $>9$  wt% or even higher than 16  
330 wt%) of Si might be in it to best satisfy moment of inertia constraints. As mentioned before,  
331 there is no direct seismic observation of Mercurian core. Highly reduced Aubrite meteorites is a  
332 potentially relevant analog given Mercurian highly reduced nature (i.e. IW-3 to IW-7). It  
333 contains an average of 0.1-2.4 wt% Si (Mt. Egerton has the largest amount of Si in the metal of 4  
334 wt%). High P-T experimental studies has well established that Si become more siderophile under  
335 more reducing conditions (i.e. Si changes from lithophile to siderophile at IW-3.5, Corgne et al.,  
336 2008). Therefore, a large amount of Si could enter the Mercurian core during magma ocean  
337 process, which is consistent with our suggested Si-bearing model. It should be note that our  
338 proposed Si content in Mercurian core composition is derived based on extrapolation of  
339 relatively low experimental pressures in contrast to Mercurian core. At characteristic Mercurian

340 core pressure condition, Fe<sub>5</sub>Si sample of bcc phase might convert into more complex phases (i.e.  
341 fcc+B2 or hcp+B2) as suggested by Fischer et al. (2013). However, either fcc or hcp phases are  
342 denser than bcc. Therefore, even more Si is required in the Mercurian core to satisfy density  
343 constraints.

344 Systematic elastic data, especially sound wave velocity, at characteristic lunar and planetary  
345 core P-T conditions for a broader selective light element (such as C, S, O, H) are quite scarce.  
346 We still need further experimental work on high P-T EOS and elastic property measurements for  
347 Fe-multiple light elements system. In all, density and sound wave velocity data, combined with  
348 spacecraft observations, are critical for further refining the elastic property of core materials,  
349 which will provide tight constraints on the composition and evolution of the planetary and lunar  
350 interiors.

#### 351 **ACKNOWLEDGMENTS**

352 This work was supported by the National Natural Science Foundation of China (41374096,  
353 41174071), the Strategic Priority Research Program (B) of the Chinese Academy of Sciences  
354 (XDB18000000) and the Major Program of National Natural Science Foundation of China  
355 (41490630). This work was performed at HPCAT (Sector 16), Advanced Photon Source (APS),  
356 Argonne National Laboratory. GS and YK acknowledge the support by DOE-BES, Division of  
357 Materials Sciences and Engineering under Award No. DEFG02-99ER45775. HPCAT operation  
358 is supported by DOE-NNSA under Award No. DE-NA0001974, with partial instrumentation  
359 funding by NSF. The Advanced Photon Source is a U.S. Department of Energy (DOE) Office of  
360 Science User Facility operated for the DOE Office of Science by Argonne National Laboratory  
361 under Contract No. DE-AC02-06CH11357.

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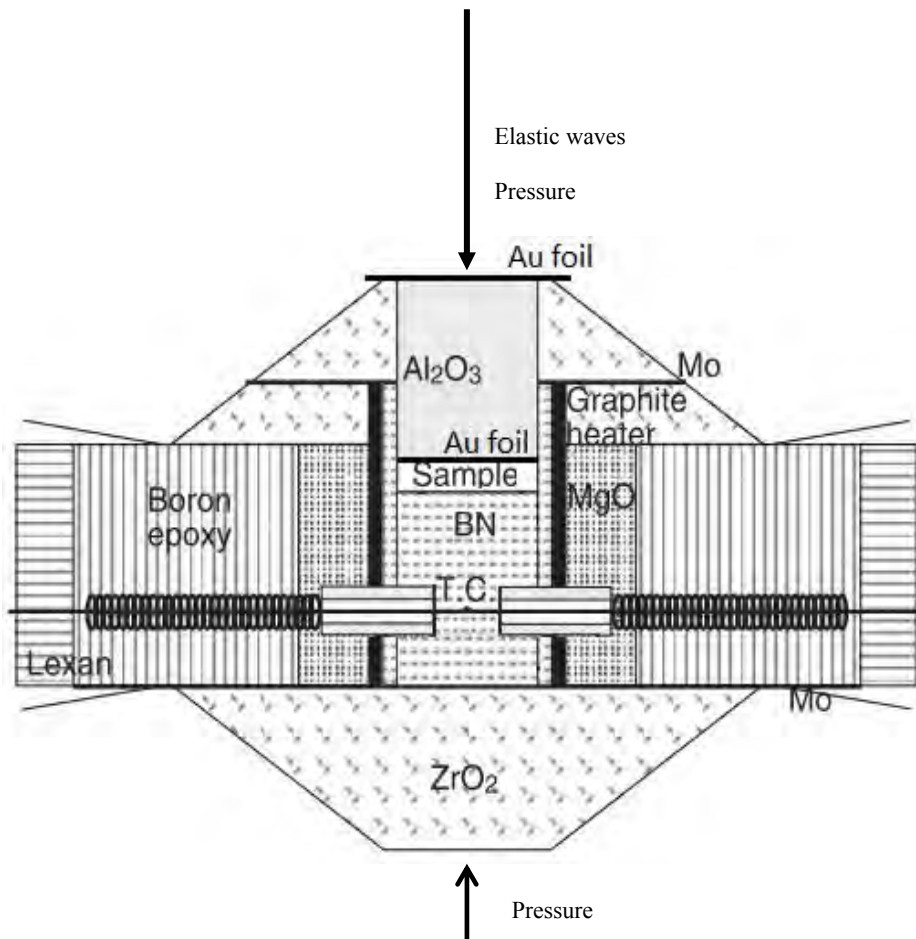
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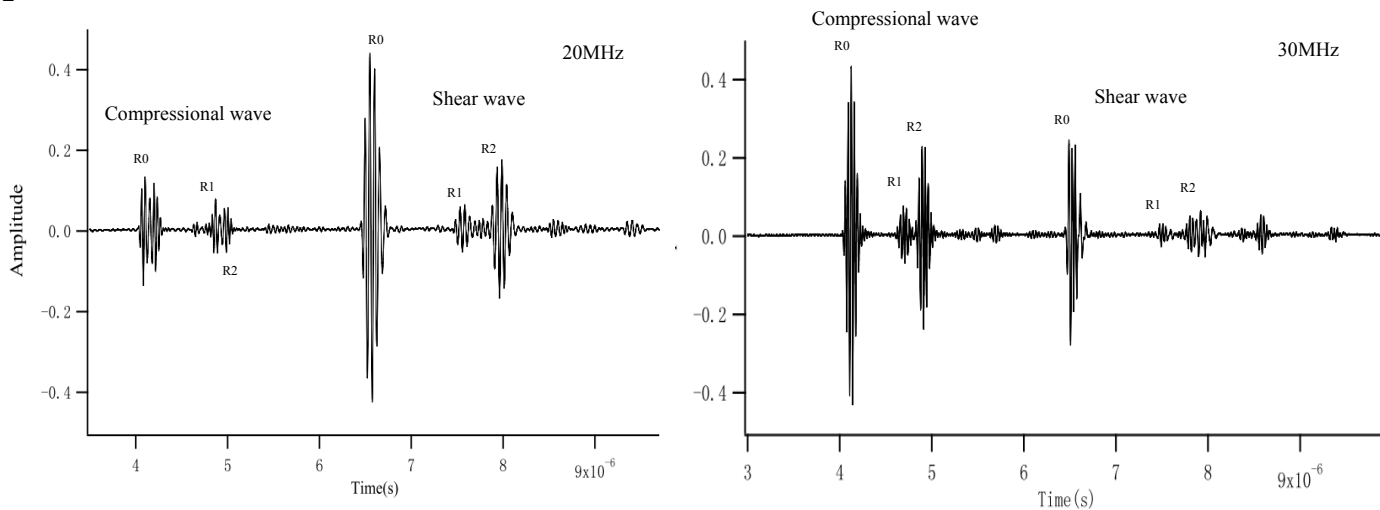
**FIGURE 1.** Schematic illustration of the cell assembly used in our high pressure and high temperature sound velocity measurements (modified from Kono et al., 2012). The top tungsten carbide (WC) anvil was used to generate 30MHz (for  $V_P$ ) and 20MHz (for  $V_S$ ) ultrasonic signals and to receive the reflected signals. Elastic waves passed through the WC anvil and propagated into an  $Al_2O_3$  rod, the  $Fe_5Si$  sample and a BN rod. Reflected signals at the anvil/ $Al_2O_3$  ( $R_0$ ),  $Al_2O_3/Fe_5Si$  sample ( $R_1$ ) and  $Fe_5Si$  sample/ $BN$  ( $R_2$ ) boundaries were recorded to calculate the travel time of  $V_P$  and  $V_S$ .

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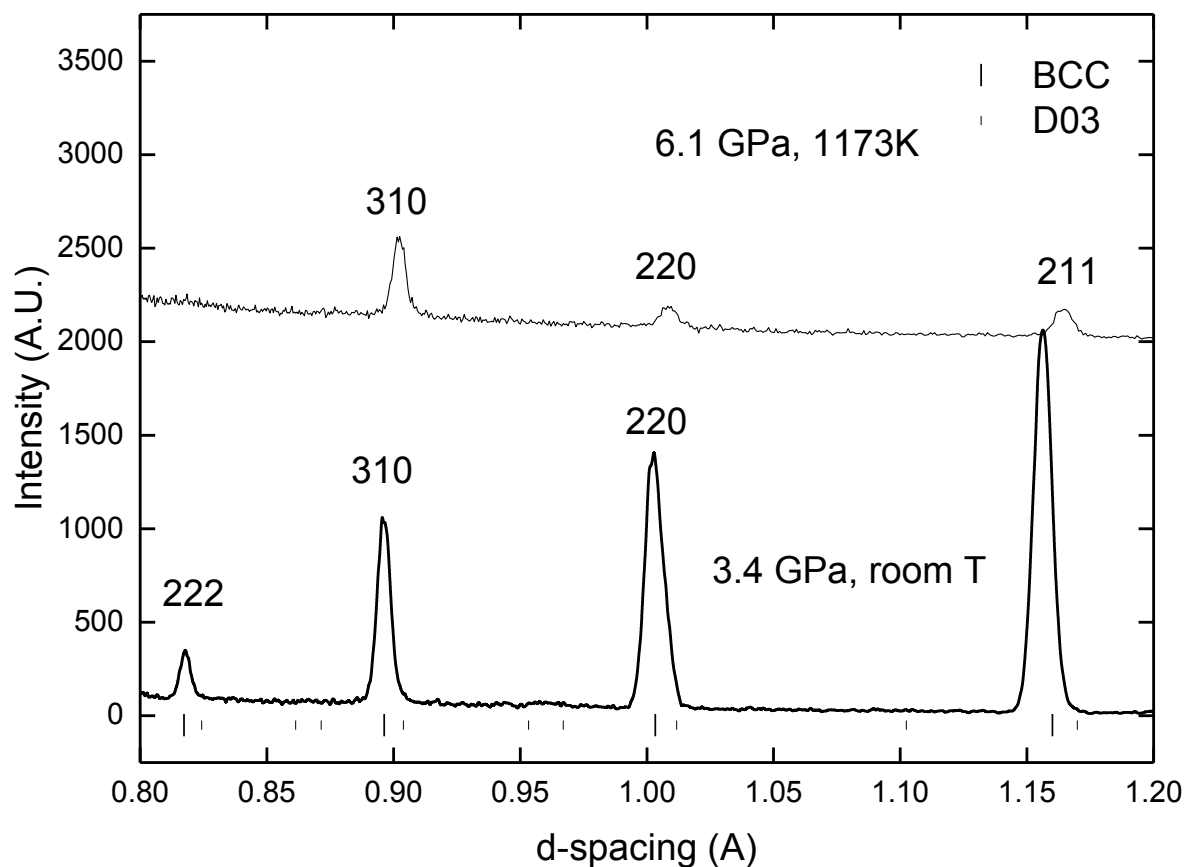


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602 **FIGURE 2.** Examples of P- and S-wave signals obtained at 2.6 GPa and 985 K. The echoes  
603 from the  $R_1$  and  $R_2$  interfaces were clearly observed. The elastic wave travel time was  
604 determined by the pulse echo overlap method using the reflected signals from the  $R_1$  and  $R_2$   
605 interfaces. This allowed us to precisely determine the travel time for both P- and S- waves ( $R_2$ - $R_1$   
606 is travel time duration). The sample length under high P-T was measured from an X-ray  
607 radiography image using a high-resolution CCD camera. The pixel resolution was 0.948  
608  $\mu\text{m}/\text{pixel}$ .  $V_P$  and  $V_S$  were calculated by dividing the sample length by the travel time. Travel  
609 time durations and sample lengths were extracted using Igor software. More details can be found  
610 in Kono et al. (2012).

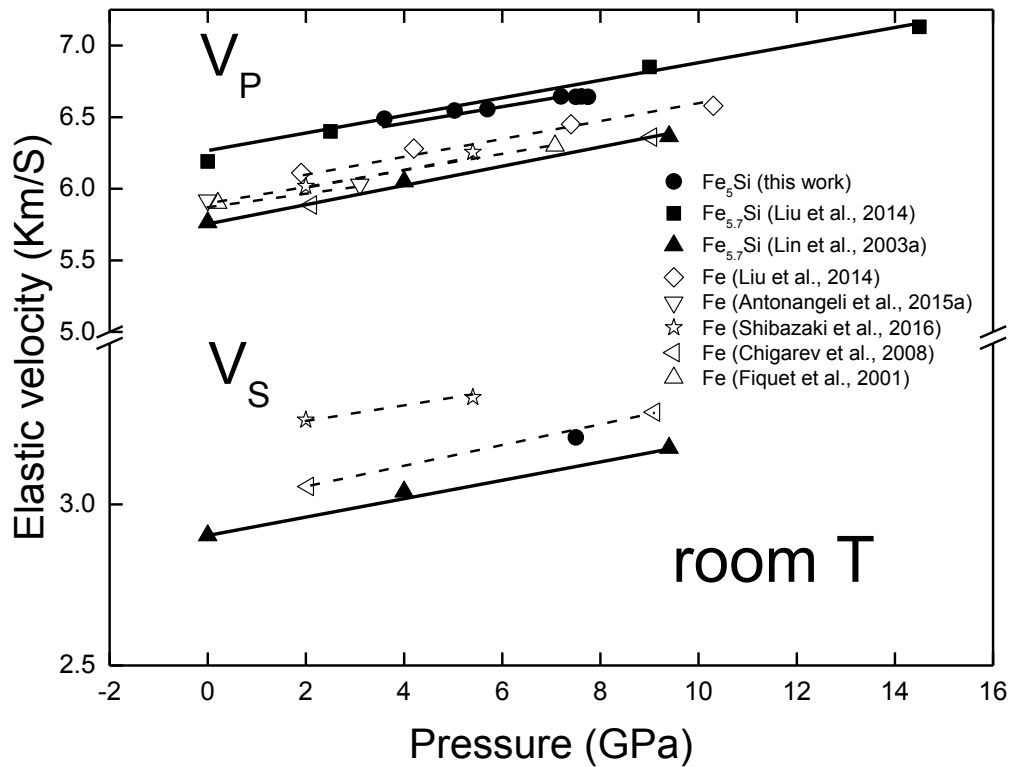
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614 **FIGURE 3.** Diffraction patterns obtained from the bcc Fe<sub>5</sub>Si sample at room temperature and  
615 3.6 GPa and at 1173 K and 6.1 GPa. Structure measurements were carried out by energy-  
616 dispersive x-ray diffraction with energy up to 150 keV. Diffracted x-rays were collimated to 0.5  
617 mm × 0.2 mm (vertical × horizontal) with  $2\theta = 15^\circ$  (Yamada et al., 2011). Standard bcc Fe and  
618 D0<sub>3</sub> Fe<sub>3</sub>Al structures at ambient condition are indicated. An obvious offset at high T pattern was  
619 observed, which may due to crystal structure's relaxation upon heating.

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623 **FIGURE 4.** The effect of Si on  $V_P$  and  $V_S$  of bcc Fe at room temperature. Solid and empty  
 624 symbols represent  $Fe_5Si$  alloy and pure Fe, respectively. HERIXS was employed by Liu et al.  
 625 (2014) and Antonangeli et al. (2015a). NRIXS was employed by Lin et al. (2003). Ultrasonic  
 626 interferometry was adopted by Shibazaki et al. (2016) and this work. Laser ultrasonics was used  
 627 by Chigarev et al. (2008) and Fiquet et al. (2014). Lines are for vision guide only.

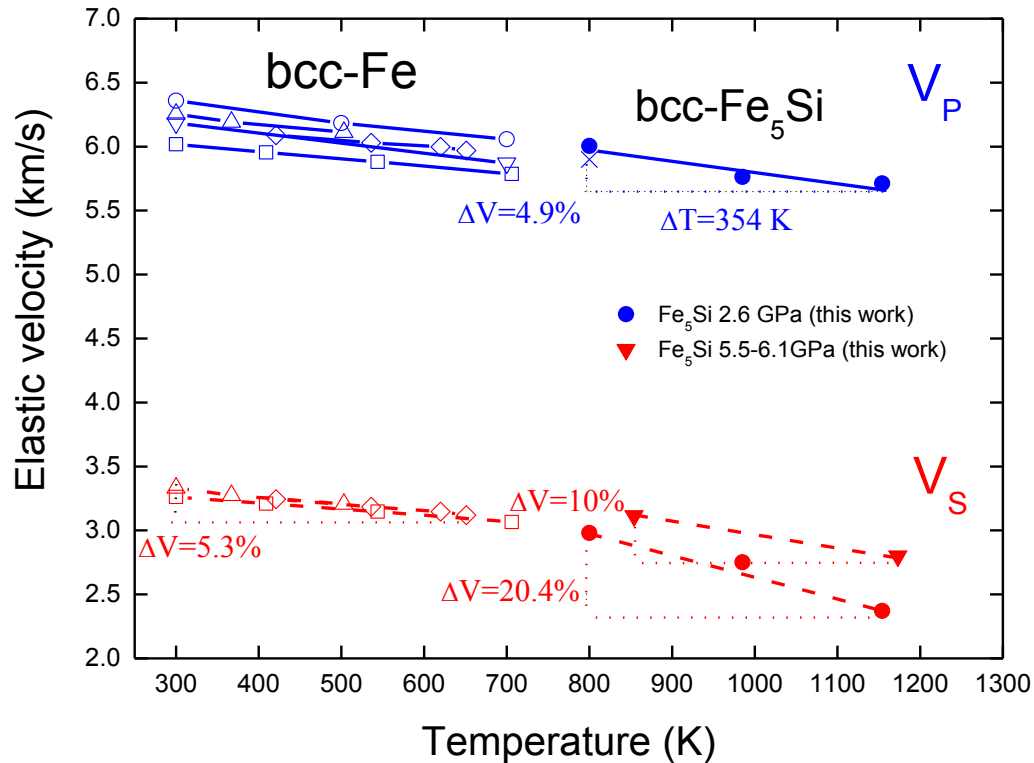
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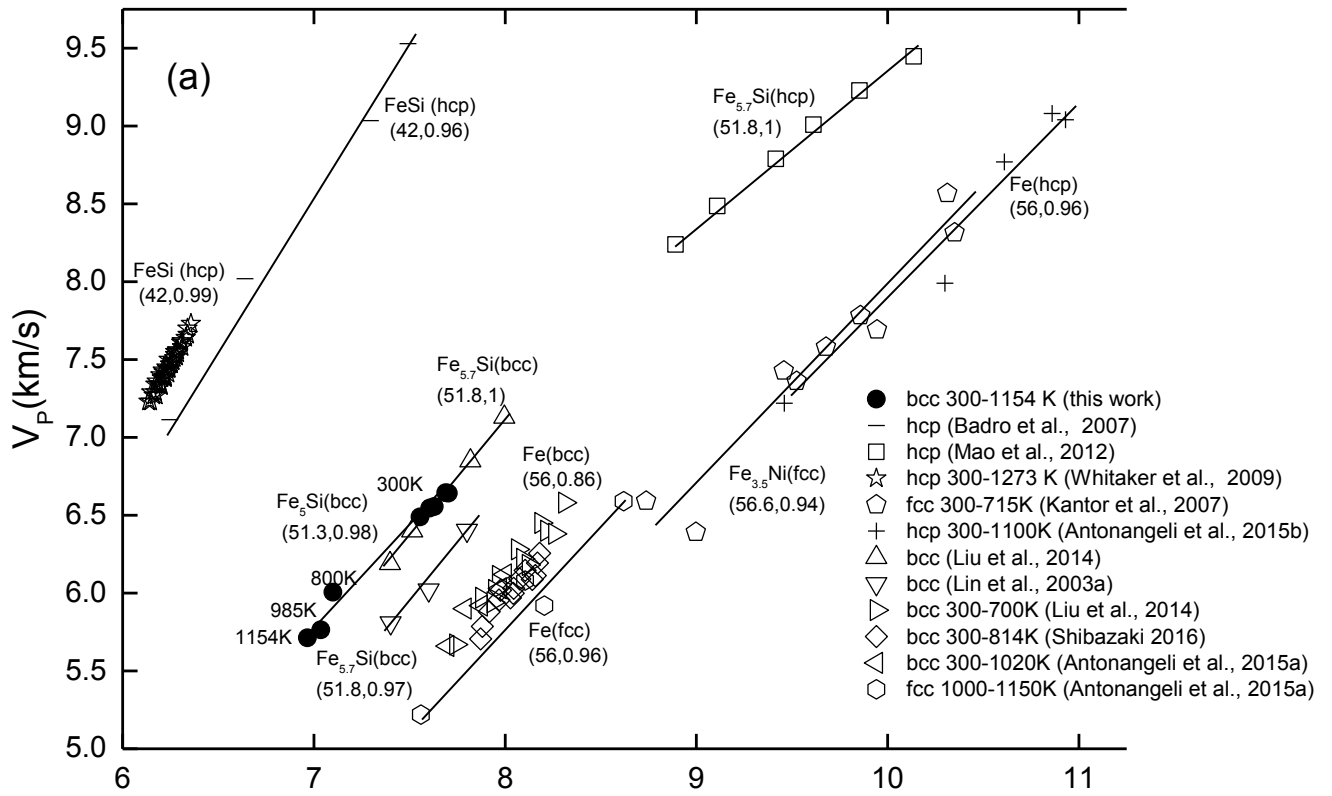
635 **FIGURE 5.** High P-T sound velocity of bcc Fe<sub>5</sub>Si and Fe. Solid and empty symbols represent  
636 bcc Fe<sub>5</sub>Si and Fe, respectively.  $V_P$  and  $V_S$  are represented by blue and red symbols, respectively.  
637 Empty down triangles and circles are HERIXS results at 3 GPa and 6 GPa, respectively (Liu et al., 2014). Cross is inelastic x-ray scattering data at 2.5 GPa (Antonangeli et al., 2015a). Empty  
638 squares, diamonds and upper triangles represent ultrasonic results at 2-2.7 GPa, 4-4.5 GPa and  
639 5.4-5.8 GPa, respectively (Shibazaki et al., 2016).

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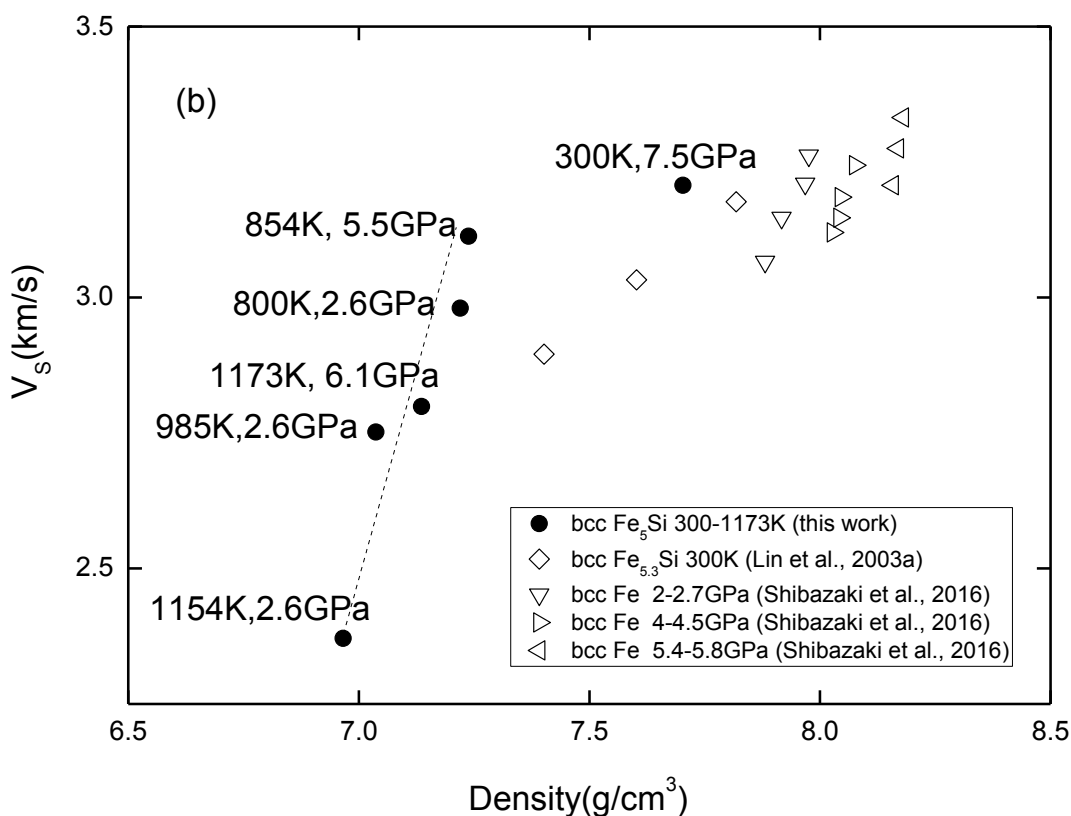
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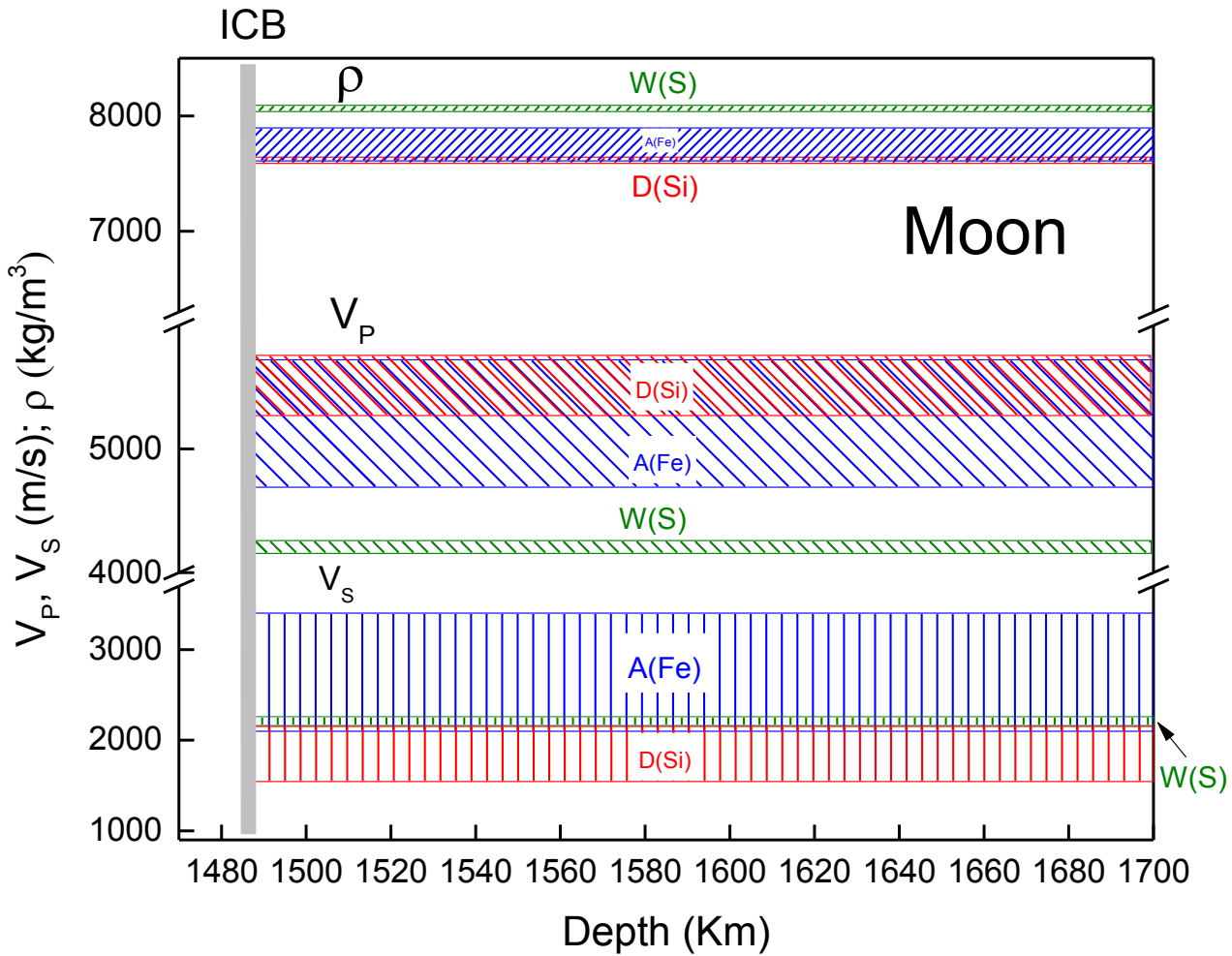
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652 **FIGURE 6.**  $V$ - $\rho$  relations of Fe and its alloys. Experimental conditions are given in the  
 653 legend. The experimental techniques employed in previous literatures are indicated as following.  
 654 Ultrasonic measurement: Whitaker et al. (2009) and Shibazaki et al. (2016). Inelastic x-ray  
 655 scattering: Badro et al. (2007), Kantor et al. (2007) and Antonangeli et al. (2010, 2015a, b).  
 656 HERIXS: Mao et al. (2012) and Liu et al. (2014). NRIXS: Lin et al. (2003). Our experimental  
 657 temperatures are labeled next to the symbols. (a)  $V_P$ - $\rho$  relations. Numerical values in the brackets  
 658 are mean atomic weight and  $R^2$  in linear regression, respectively. Except for three high  
 659 temperature data, our rest data were collected at ambient temperature. Unless specified otherwise  
 660 the  $V_P$  from previous literatures are at 300 K. (b)  $V_S$ - $\rho$  relations. Our results are solid symbols  
 661 and empty ones are for previous literatures.  $V_S$  from Shibazaki et al. (2016) are at 300-814 K.  
 662 Our  $V_S$ - $T$  data seems to follow a linear relation except for the 300 K. The dash lines are for eye  
 663 guide only.



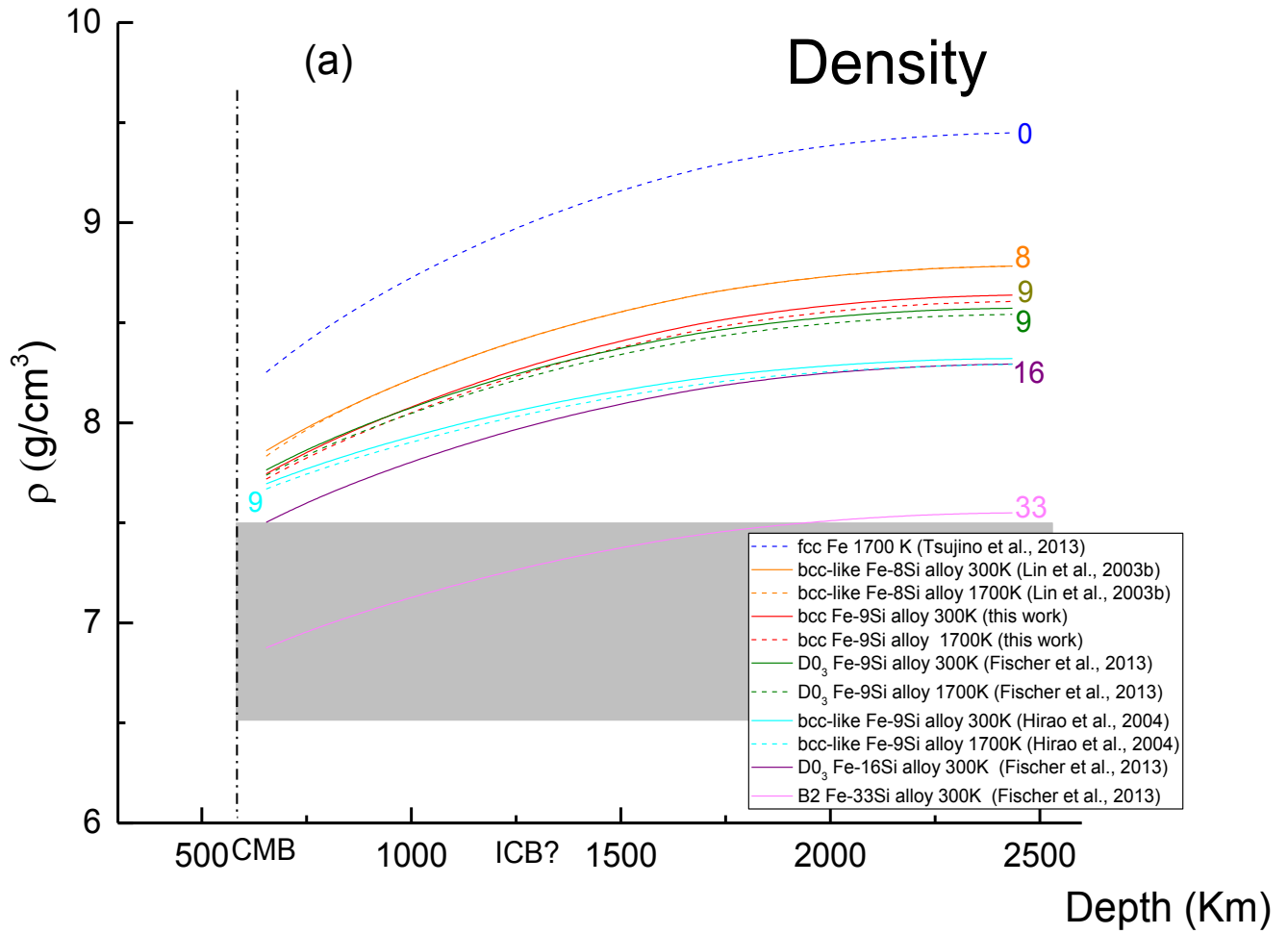


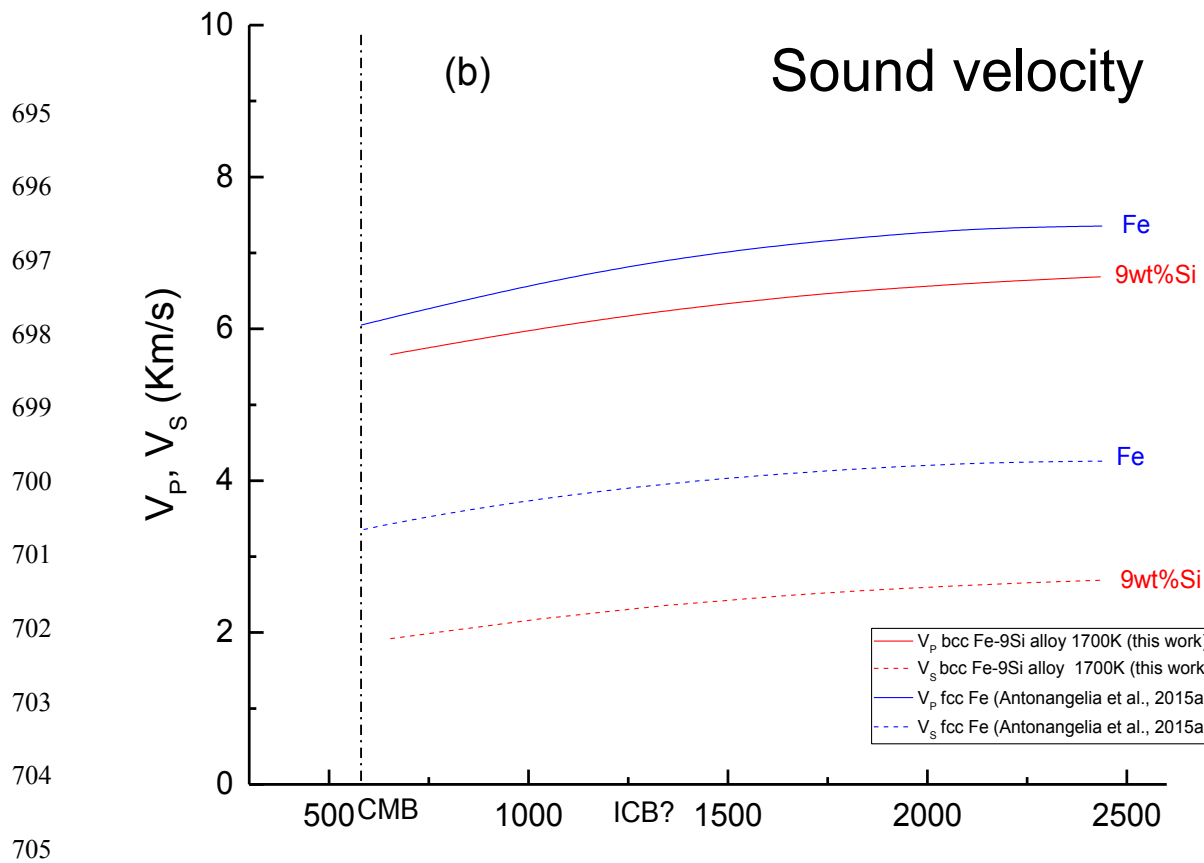
664 **FIGURE 7.**  $V_P$ ,  $V_S$  and  $\rho$  model for lunar inner core. Vertical axis is divided into three  
 665 sections, which represent results of  $\rho$ ,  $V_P$  and  $V_S$ , respectively. Left- and right-hand diagonals  
 666 are  $V_P$  and  $\rho$ , respectively. Vertical lines are  $V_S$ . Blue, green and red represent results from  
 667 Antonangeli et al., (2015a) (A), Weber et al., (2011) (W) and this work (D). Our profiles were  
 668 calculated at 5 GPa, 1300 K and 1900 K. Elements in the bracket represent studied light element  
 669 in literatures. Grey line marks the solid inner core boundary.

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706 **FIGURE 8.** Density (a) and sound velocity (b) profiles at Mercury's core conditions. Pressure-  
 707 depth relation of Mercurian core is from seismic structure model reported by Lv. (2011). CMB  
 708 marks the core-mantle boundary. Mercurian core might be partially molten. However, ICB depth  
 709 has not been well defined yet. In (a), the shade area shows the densities range of a Si-bearing  
 710 Mercurian core which satisfies observed  $C/MR^2$  and  $C_m/C$  values by radio tracking data from the  
 711 MESSENGER spacecraft (Knibbe and Westrenen 2018). The numbers labeled besides the  
 712 symbols represent Si content in Fe-Si alloy applied in literatures. The  $D0_3$  structure is an ordered  
 713 version of the B2 structure, which is an ordered version of the bcc structure. In (b), Lv's sound  
 714 velocity profiles were calculated based on mineral physics data assuming temperature is 1825 K  
 715 at CMB. Sound velocities profiles of fcc iron are from linear sound velocity-density relation  
 716 reported by Antonangeli et al. (2015a). It clearly shows incorporating Ni in pure Fe results in an  
 717 increased sound velocity while adding Si has the opposite effect.

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720 **TABLE 1.** Experimental conditions and results of sound velocity measurements.

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Run No.	P (GPa)	T (K)	V <sub>P</sub> (km/s)	V <sub>S</sub> (km/s)	ρ (g/cm <sup>3</sup> )
1	3.6(3)	300	6.49(1)		7.56(2)
1	5.0(3)	300	6.55(1)		7.61(1)
1	5.7(3)	300	6.56(1)		7.63(1)
1	7.2(3)	300	6.64(1)		7.69(0)
1	7.5(6)	300	6.64(1)	3.21(3)	7.70(0)
2	2.6(1)	800	6.01(2)	2.98(4)	7.10(1)
2	2.6(2)	985	5.76(2)	2.75(4)	7.04(2)
2	2.6(2)	1154	5.71(2)	2.37(3)	6.97(1)
2	5.5(5)	854		3.11(4)	7.24(0)
2	6.1(1)	1173		2.80(4)	7.14(2)