1

2

AMFORM, a new mass-based model for the calculation of the unit formula of amphiboles from

Electron Micro-Probe analyses

- 3 FILIPPO RIDOLFI<sup>1,\*</sup>, ALBERTO ZANETTI<sup>2</sup>, ALBERTO RENZULLI<sup>3</sup>, DIEGO PERUGINI<sup>4</sup>, FRANCOIS
- 4 HOLTZ<sup>1</sup>, ROBERTA OBERTI<sup>2</sup>
- <sup>1</sup>Institut für Mineralogie, Leibniz Universität Hannover, 30167 Hannover, Germany
- <sup>2</sup>CNR-Istituto di Geoscienze e Georisorse, Sede secondaria di Pavia, 27100 Pavia, Italy
- <sup>3</sup>Dipartimento di Scienze Pure e Applicate, Università degli Studi di Urbino "Carlo Bo", 61029 Urbino,
- 8 Italy

10

21

<sup>4</sup>Dipartimento di Fisica e Geologia, Università di Perugia, 06100 Perugia, Italy

ABSTRACT

In this work, we have studied the relationships between mass concentration and unit-formula of 12 amphibole using 114 carefully selected high-quality experimental data, obtained by EMP (Electron 13 Micro-Probe) + SREF (Single-crystal X-ray Structure REFinement) ± SIMS (Secondary-Ion Mass 14 15 Spectrometry) analyses, of natural and synthetic Li-free monoclinic species belonging to the Ca and Na-Ca subgroups, and 75 Li-free and Mn-free C2/m end-members including oxo analogues of Ca 16 amphiboles. Theoretical considerations and crystal-chemical driven regression analysis allowed us to 17 obtain a number of equations which can be used to: (i) calculate from EMP analyses amphibole unit-18 formulae consistent with SREF±SIMS data. (ii) discard unreliable EMP analyses and (iii) estimate 19  $^{W}O^{2-}$  and Fe<sup>3+</sup> contents in Li-free C2/m amphiboles with relatively low Cl contents ( $\leq 1$  wt%). The 20

AMFORM approach mostly relies on the fact that while the cation mass in Cl-poor amphiboles

increases with the content of heavy elements, its anion mass maintains a nearly constant value, i.e., 22 22O + 2(OH, F, O), resulting in a very well-defined polynomial correlation between the molecular 23 mass and the cation mass per gram  $(R^2 = 0.998)$ . 24 The precision of estimating the amphibole formula (e.g., <sup>T</sup>Si±0.02, <sup>C</sup>Al±0.02, <sup>A</sup>(Ca+Na+K)±0.04 apfu) 25 is 2-4 times higher than when using methods published following the last IMA recommended scheme 26 (2012). It is worth noting that most methods using IMA1997 recommendations (e.g., PROBE-AMPH) 27 give errors which are about twice those of IMA2012-based methods. A linear relation between WO2-28 and the sum of <sup>C</sup>(Ti, Fe<sup>3+</sup>) and <sup>A</sup>(Na+K) contents, useful to estimate the iron oxidation state of highly-29 30 oxidized amphiboles typical of post-magmatic processes, is also proposed. A step by step procedure (Appendix 1) and a user-friendly spreadsheet (AMFORM.xlsx, provided as supplementary material) 31 allowing one to calculate amphibole unit-formulae from EMP analyses are presented. This work opens 32 new perspectives on the unit-formula calculation of other minerals containing OH and structural 33 vacancies (e.g., micas). 34 **Keywords:** Li-free amphiboles, oxo component, cation mass, amphibole oxidation, amphibole 35 deprotonation, SREF, SIMS, Mössbauer spectroscopy 36 37 Corresponding author: filippo.ridolfi@uniurb.it 38 39 Introduction 40 Amphiboles are a supergroup of silicate minerals containing, either at the major- or at the trace-element 41 level, most elements of geological/geochemical relevance (for a review, see Hawthorne et al. 2007). It 42 has been largely recognized that the role of amphibole in understanding geological/planetary processes 43

44

45

46

47

48

49

50

51

52

53

54

55

56

57

58

59

60

61

62

63

64

65

66

67

and several health issues is of crucial importance (e.g., Forbes and Starmer 1974; Foley et al. 2002; Gunter et al. 2007; McCanta et al. 2008; Jackson et al. 2013; Smith 2014). Amphibole crystalchemistry has captured the attention of many scientists over the years because of its intrinsic complexity (indeed, the term amphibole derives from the Greek "αμφιβολος", which means ambiguous; Haüy 1801; see also Cipriani et al. 2007) and its ability to record the steps of a wide range of geochemical and petrological processes due to a network of mutual relationships between cation ordering, chemistry of the associated phases (minerals and/or melt) and intrinsic parameters such as pressure, temperature and fugacity of volatile elements (Hammarstrom and Zen 1986; Holland and Blundy 1994; Al'meev et al. 2002; Oberti et al. 2000, 2007a; Ridolfi et al. 2010; Ridolfi and Renzulli 2012; Zhang et al. 2017). However, the prerequisite for using amphiboles as geological markers is the determination of their correct crystal-chemical formula (i.e., composition and site partitioning). In the 70s and 80s, amphibole unit-formula calculation was a hot topic in the geological community (e.g., Stout 1972; Smith 1977; Leake 1978; Laird and Albee 1981; Hawthorne 1983; Rock and Leake 1984; Spear and Kimball 1984; Jacobson and Sorensen 1986) which has led to two major recommended schemes of the International Mineralogical Association (IMA; Leake et al. 1997; Hawthorne et al. 2012). Routine calculations of amphibole unit-formulae from electron microprobe (EMP) data may be seriously affected by inappropriate normalization procedures and/or the lack of accurate information on the oxidation state of iron and the contents of hydrogen and lithium (Leake et al. 1997; Al'meev et al. 2002; Hawthorne et al. 2012; Locock 2014). In particular, most of the published schemes for formula calculation do not account for the occurrence of O<sup>2</sup>- as W anion (e.g., Tindle and Webb 1994; Leake et al. 1997; Al'meev et al. 2002; Esawi 2004; Dale et al. 2005) which allows the number of total negative (and positive) charges to theoretically vary between 46 and 48 (Hawthorne et al. 2012). The spreadsheet of Locock (2014) can only account for a maximum content of O2- in the W- sites (WO2-) equal to 2 times the total content of Ti in C, thus disregarding the

constrained cation contents (mainly cation underestimations) and Fe<sup>3+</sup>/Fe<sub>tot</sub> estimates which, at the best, are averages between the maximum and minimum values (e.g., Leake et al. 1997). Nevertheless, there is a large amount of amphibole literature data reporting H, WO<sup>2-</sup> and Fe<sup>3+</sup>/Fe<sub>tot</sub> measurements and/or accurate estimates (e.g., Robinson et al. 1997; Bottazzi et al. 1999; Oberti et al. 2000; Tiepolo et al. 2003; Adam et al. 2007; Oberti et al. 2007b; Uvarova et al. 2007; Perinelli et al. 2012; Della Ventura et al. 2014) that can be used to improve the existing methods to calculate amphibole unit-formulae.

In this work, we use high-quality literature data and end-member compositions to analyze the relation between elemental concentration (by mass) and stoichiometry in the amphibole supergroup and propose a new mass-based method to be applied only to EMP data, that allows identification of bad analyses and calculation of the correct unit-formula of Li-free (and Mn- and Cl-poor) C2/m amphiboles, with an uncertainty 2-4 times lower than that of recently published procedures (i.e., Hawthorne et al. 2012; Locock 2014). Tests of the most used formula calculation methods (Tindle and Webb 1994; Dale et al. 2005; Locock 2014) are also provided as supplementary material.

#### **ESSENTIAL DEFINITIONS**

Amphibole supergroup has the general formula  $A_{0-1}B_2C_5T_8O_{22}W_2$  (Hawthorne et al. 2012). The amphiboles considered in this work are Li- and Mn<sup>3+</sup>-free C2/m species and their group elements include: A = Na, K, Ca,  $\Box$  (vacancy); B = Ca, Na,  $Mn^{2+}$ ,  $Fe^{2+}$ , Mg; C = Mg, Ti,  $Fe^{2+}$ ,  $Mn^{2+}$ , Cr, Ni, Zn, Al,  $Fe^{3+}$ ; T = Si, Al, Ti;  $W = OH^-$ , F, Cl,  $O^{2-}$  (where Mn, Cr, Ni, Zn and Cl are minor components,  $\leq$  0.2 atoms per formula unit, apfu). Site-assignments and stoichiometric constraints for these amphiboles are provided in Table 1 while Table 2 reports the ideal formula and composition of 75 end-members.

- Definitions needed to follow the text are provided below. Note that most of the calculations needed to obtain the defined parameters are reported in Appendix 1.
- original composition: concentrations expressed as wt% of the oxides (SiO<sub>2</sub>, TiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub>, Cr<sub>2</sub>O<sub>3</sub>,
   FeO<sub>tot</sub>, NiO, ZnO, MnO, MgO, CaO, Na<sub>2</sub>O, K<sub>2</sub>O) and halogens (F, Cl) in the amphibole,
   usually measured by EMP analyses;
  - *TEO*: *Total Elements and Oxides* (also named re-calculated total), wt% sum of oxides (see previous definition) and halogens (F, Cl), minus FeO<sub>tot</sub> (total iron content) and the oxygen atoms balancing F and Cl (i.e., O<sup>F,Cl</sup>), plus Fe<sub>2</sub>O<sub>3</sub>, FeO and H<sub>2</sub>O calculated from the unit-formula (Appendix 1), where calculated H<sub>2</sub>O values correspond to those measured by Secondary-Ion Mass Spectrometry (hereafter SIMS) or estimated by Single-crystal X-ray Structure REFinement (hereafter SREF) by published equations relating the oxo component to the *M*(1)-*M*(2) distance (Oberti et al. 2007a; see following section and Supplement 1 for methods). Note that *TEO* values from original compositions generally deviate from ideality (100 wt%):
    - normalized composition: concentrations expressed as wt% of the oxides and halogens (F, Cl) in amphibole calculated from any unit-formula to obtain a value of TEO equal to 100 wt% (e.g., Table 1 and http://webmineral.com for end-members);
- $M_r$  (g/mol): molecular mass corresponding to the sum of the apfu of all elements (Table 1) previously multiplied by their atomic mass  $(A_r)$ ,;
  - *cmpg*: cation mass per gram, i.e., *cmpg* = 10<sup>-2</sup>(Si + Ti + Al + Cr + Fe + Ni + Zn + Mn + Mg + Ca + Na + K), calculated from the original or normalized compositions, all elements in wt% (see Appendix 1 for calculation). Note that *cmpg* is a mass ratio and it thus corresponds to the total cation mass divided by the sum of the total cation and anion masses for normalized compositions;

#### Revision 1

130

131

132

133

 $X_i$ : mass of element i divided by the total cation mass (see Appendix 1). Note that  $X_i$  values are 114 115 the same in normalized and original compositions; Yi: element or ion i in a generic group-sites Y, where Y can be T, C, B, A and W (Table 1). 116 When superscript is not reported, i refers to the total amount of i in amphibole. To avoid 117 misunderstanding the total amount of iron is expressed as Fe<sub>tot</sub> (e.g., Table 1); 118 CR (apfu·g/mmol): correlation ratio between the sums of the apfu and mmol/g (millimole per 119 gram) of all cation components, i.e.  $CR = \frac{\sum Si \to K \ apfu}{\sum Si \to K \frac{mmol}{a}}$  (Table 1). Note that CR is ideally equal 120 to the apfu·g/mmol value of any cation (e.g.,  $CR^{Si} = \frac{Si \, apfu}{Si \, mmol/g}$ ) or anion (e.g.,  $CR^F =$ 121  $\frac{F \ apfu}{F \ mmol/a}$ ). Once precisely determined (see below), it can be easily used to calculate the apfu of 122 each element multiplying CR by the element concentration in mmol/g (see Appendix 1); 123 Acharge: deviation from electroneutrality in an amphibole unit-formula (i.e., positive – negative 124 charge sums); 125 dC and dB: deviation from 5 apfu and 2 apfu in the C- and B-group cations in the selected unit-126 ormulae, not admitted by the stoichiometric constraints (Table 1; see also section Selection 127 criteria of the calibration dataset): 128 ΔC: the amount of Fe<sup>2+</sup>, Mn and/or Mg exceeding 5 apfu and thus considered as B-group 129

#### DATA SELECTION AND TECHNIQUES

#### Composition and petrogenesis of the investigated amphiboles

cations in the calculated formula (Table 1; Appendix 1).

We have studied the relationships between concentration and unit-formula in Li-free and Mn, Cl-poor monoclinic amphiboles belonging to the Ca, Na-Ca subgroups (and some of their oxo analogues) using a dataset carefully selected from the literature and from the CNR-IGG (Consiglio Nazionale delle Ricerche-Istituto di Geoscienze e Georisorse) amphibole database available in Pavia; selection was done based on the availability of accurate EMP+SREF±SIMS analyses. The dataset contains 114 oxides-formula pairs with the largest possible geochemical and geological variability; the oxoamphiboles considered are kaersutite, ferri-kaersutite, oxo-potassic-chromio-katophorite, oxo-potassictaramite, Ti-rich oxo-sadanagaite, Ti-rich oxo-pargasite and Ti-rich oxo-ferri-pargasite (see AMFORM.xlsx in the supplementary material). Compositions belonging to the sodium amphiboles were excluded because they may contain minor to moderate amounts of Li (e.g., Hawthorne et al. 1993) which cannot be detected and measured by EMP analysis.

The dataset includes published concentration (wt%)-formula (apfu) pairs of both 61 synthetic (Oberti et al. 2000; Bottazzi et al. 1999; Tiepolo et al. 2000; 2003; Adam et al. 2007) and natural amphiboles which are typical of geologically relevant systems (gabbro, peridotite, lherzolite, kyanite-eclogite, marble, metasomatic/skarn-type deposit and several types of metavolcanic amphibolites) and coming from different world-wide localities (Oberti et al. 1995; Vannucci et al. 1995; Robinson et al. 1997; Oberti et al. 2007b; 2015; Uvarova et al. 2007; Perinelli et al. 2012; Della Ventura et al. 2014). 53 unpublished oxides-formula pairs come from the CNR-IGG database and include amphiboles from extrusive rocks, mantle ultramafic rocks (hornblendites, pyroxenites, peridotites), peridotitic and pegmatitic veins (for a list, cf. AMFORM.xlsx).

#### Sample characterization

All the unpublished amphiboles had been analyzed by EMP, SREF and SIMS allowing a complete characterization of their crystal-chemical parameters (AMFORM.xlsx). SREF and SIMS analyses were

158

159

160

161

162

163

164

165

166

167

168

169

170

171

172

173

174

175

176

177

178

179

180

done at CNR-IGG in Pavia, while EMP analyses were mostly done at the University of Manitoba (Winnipeg, Canada). See electronic supplement 1 for a more detailed information on the CNR-IGG analytical methods. The crystal-chemical formulae were calculated by combining SREF, EMP and SIMS results. The number of A-cations was estimated on the basis of the refined site-scattering values at the relevant sites and the K<sub>2</sub>O and Na<sub>2</sub>O contents from EMP analysis. The oxo component was evaluated either by SIMS or by a SIMS-calibrated crystal-chemical relationship (Oberti et al. 2007a; see also electronic supplement 1). Under these constraints, the Fe<sup>3+</sup> content can be derived based on the overall electroneutrality. The Fe<sup>3+</sup> content and its distribution were further constrained through the pattern of refined mean bond-lengths observed at the three M(1-3) octahedra. The presence of the M(4')subsite, indicating the occurrence of small B cations (i.e., Mn<sup>2+</sup>, Fe<sup>2+</sup>, Mg), was checked on the difference Fourier maps. B cations were calculated assigning excess C cations (i.e.,  $\Delta C$ , first Mn<sup>2+</sup> and then Fe<sup>2+</sup> and Mg) trying to minimize the difference between the site scattering calculated (from EMP) for the B and C cations and those obtained by SREF. For further validation, the <sup>T</sup>Al contents obtained by recalculation of EMP analyses was checked to be in close agreement with those calculated from the refined  $\langle T(1)\text{-O}\rangle$  and  $\langle T(2)\text{-O}\rangle$  distances (Oberti et al. 2007a). Many of the amphiboles taken from the literature include EMP, SREF and SIMS data, and their formulae were obtained following the same procedure. The amphibole formula selected from Robinson et al. (1997) was derived from EMP, SREF, Mössbauer spectroscopy (for Fe<sup>3+</sup>/Fe<sub>tot</sub>), wet-chemical (for F) and IR (InfraRed spectroscopy, for H<sub>2</sub>O) analyses. In some cases, the formulae were derived from the only EMP and SREF data (Oberti et al. 1995; Vannucci et al. 1995; Oberti et al. 2007b; Della Ventura et al. 2014), and the oxo component was estimated using the correlation developed at CNR-IGG in Pavia based on SREF results (Oberti et al. 2007a). In other cases, the Fe<sup>3+</sup> content of the amphibole was validated by Mössbauer spectroscopy (Uvarova et al. 2007, Perinelli et al. 2012). For

the oldest selected data (Oberti et al. 1995) the occurrence of <sup>W</sup>O<sup>2-</sup> in amphibole was estimated during this work using the published SREF data (see above).

#### Selection criteria of the calibration dataset

Both literature and unpublished analyses were checked according to a series of criteria aimed at obtaining a high-quality dataset.

Whenever standard deviations (oxide  $\sigma$ ) of the EMP element oxide analyses are available together with averaged compositions, we discarded amphibole data showing oxide  $\sigma$  values higher than 2/3 of the average oxide  $\sigma$  values reported by Ridolfi and Renzulli (2012) for their high-quality experimental amphibole compositions. We also discarded the amphibole compositions with *TEO* values falling outside the range of 100±1.7 wt%, because larger deviations from 100 wt% may derive from analytical problems for some elements, resulting in error propagation to the unit-formula. The amphibole compositions in the dataset have *TEO* values ranging from 98.3 to 100.8 wt%.

Amphibole formulae showing  $\triangle charge$  larger than  $\pm 0.05$ , dC and dB larger than  $\pm 0.01$  and/or total cation apfu (i.e., $\sum Si \rightarrow K$ ; Table 1) higher than 16.005 were also discarded. In addition, formulae calculated without considering the oxo component, i.e., forcing the negative charges to be 46, were not considered. The bijection between the composition and formula of any amphibole was carefully checked comparing the CR values of each of the major elements (e.g.,  $CR^{Si}$ ,  $CR^{Al}$ ,  $CR^{Mg}$ ) with the CR value calculated on the total cation sum ( $\sum Si \rightarrow K$ ; Appendix 1). This procedure allowed us to avoid mismatches between formulae and compositions due to adjustment and/or editing.

The dataset used to calibrate the method contains 114 entries and it is included in the AMFORM.xlsx spreadsheet (provided as supplementary material). The ranges in elemental composition are:  ${}^{T}Si = 5.8\text{-}7.8$  apfu;  ${}^{A}(Ca+Na+K) = 0.1\text{-}1.0$  apfu;  ${}^{W}F \leq 1.3$  apfu;  ${}^{W}Cl \leq 0.2$  apfu;  ${}^{M}g/(Mg+Fe^{2+}) = 0.2\text{-}1.0$ ;  ${}^{E}Fe^{3+}/Fe_{tot} = 0.0\text{-}1.0$ .

It is worth noting that oxides-formula pairs not validated by SREF were not included in this final calibration dataset. This decision was taken to guarantee an independent check of the formulae and a reliable constraint on  $\sum Si \rightarrow K$  values.

Beside the 114 selected amphibole compositions, for calibration we used 75 ideal formulae and (normalized) compositions of Li- and Mn-free *C2/m* end-members of the amphibole supergroup (Hawthorne et al. 2012) (Table 2). The oxides-formula pairs in Table 1 also include kaersutite, ferri-kaersutite, ferro-kaersutite, ferro-ferri-kaersutite and some oxo analogues of the Ca groups as these amphiboles in nature may often have a significant oxo-component.

#### RATIONALE AND DATA ANALYSES

The high-quality dataset described above was used to detect and analyze any possible relation between compositional (e.g., wt% and *mmol/g*) and unit-fomula parameters (apfu) in amphiboles.

For a correct characterization of the amphibole unit-formula, two crucial parameters must be determined:  $\Sigma \text{Si} \rightarrow \text{K}$ , ranging from 15 to 16 apfu and the oxo component ( ${}^{\text{W}}\text{O}^{2-}$ ; 0-2 apfu), which allows the sum of the negative charges to vary between 46 and 48 (Table 1). When these parameters are known and the presence of  $\text{Mn}^{3+}$  can be excluded, the amount of  $\text{Fe}^{3+}$  can be derived under the constraint of electroneutrality (Hawthorne et al. 2012).

### **Development of the** *CR***-equations**

- The correlation ratio (CR) between apfu and mmol/g of any component or sum of components (e.g., Si;
- Fe<sub>tot</sub>, F;  $\sum Si \rightarrow K$ ) must be constant for any normalized and end-member composition-formula pair. If

- *CR* is known with a reasonably good approximation, the apfu content of each element can be calculated multiplying *CR* by its concentration in *mmol/g*.
- Figure 1a shows that the CR of the normalized and end-member compositions is perfectly correlated with their molecular mass,  $M_r$ :

230 
$$CR = 10^{-3} M_r \left( apfu \cdot \frac{g}{mmol} \right)$$
 (R<sup>2</sup> = 1.000)

- Indeed, equation (1) is an identity because CR is mathematically equal to  $M_r$  divided 1000 for the ideal composition of any mineral and compound. The original amphibole compositions only slightly deviate from this linear trend (blue symbols in Fig. 1a). The deviations are due to TEO values usually lower than 100% (see above). However, this simple correlation cannot be used to estimate CR from EMP analysis because  $M_r$  can only be calculated from the formula. Indeed, equation (1) should be used at the end of any formula calculation procedure to calculate CR after Mr has been calculated from the formula, thus validating the final results and the quality of the data (see below).
- Figure 1b shows that the *CR* values of normalized and end-member compositions have a nearly perfect polynomial relation with the cation mass per gram (*cmpg*) which can be directly calculated from EMP data (see above):

$$241 CR = 4.809 cmpg^2 - 3.409 cmpg + 1.276 (apfu \cdot g/mmol) (R^2 = 0.998) (2)$$

Indeed, the anion components in the different amphibole compositions have almost the same mass, because they mostly consist of the same number of ions with similar  $A_r$ , i.e.,  $22O^{2-} + 2(OH^-, F^-, O^{2-})$ . In contrast, the mass of the cation component increases with the amount of heavier cations (e.g.,  $Fe^{2+}$ ,  $Fe^{3+}$ ) resulting in a progressively increasing pattern of CR (and  $M_r$ ) with cmpg. Because cmpg is a mass ratio, Figure 1b has a curvilinear trend. The small scattering observed for some normalized and end-member compositions ( $R^2 = 0.998$ ; Fig. 1b) is due to the occurrence of  $^W(C\Gamma, F^-, O^{2-})$  which have  $A_r$  values different from that of  $OH^-$ , thus affecting the cmpg values. For example, the heaviest end-member ferro-ferri-cannilloite has the same cation mass as its oxo analogue but a higher  $M_r$  value

because it differs (in mass term) by having two more hydrogen atoms (Table 2). Therefore, the mass of W anions is higher than that of its oxo equivalent (because OH is heavier than  $O^{2-}$ ) resulting in a *cmpg* value slightly lower than that of oxo-ferro-ferri-cannilloite (Fig. 1b; Table 1). F-rich amphiboles behave in the opposite way because F has a mass higher than OH. However the effect of F and  $^{W}O^{2-}$  in calculating *CR* is minimal as confirmed by the high determination coefficient (R<sup>2</sup>) of equation 2 (Fig. 1b), so that amphibole compositions with high F and oxo contents can be treated with this method with a sufficient accuracy.

In contrast, amphiboles with high Cl contents (e.g., Léger et al. 1996; Coogan et al. 2001) deviate significantly from equation 2 (towards lower *cmpg*) because the  $A_r$  value of chlorine is about twice that of F, OH and O. However, the maximum Cl content (i.e., 0.20 apfu, corresponding to 0.72 wt%) in the high-quality dataset produces negligible deviations from equation 2. This is because the incorporation of Cl in amphibole is always related to high  $Fe^{2+}$  contents (e.g., Oberti et al. 2007a) which results in relatively low *cmpg* underestimations (e.g., in the two Fe- and Cl-rich amphiboles marked with green triangles in Fig. 1b).

It is worth noting that equation 2 cannot be successfully applied to the original compositions of most of the amphiboles because EMP uncertainties commonly result in incorrect *CR* and *cmpg* values leading to significant deviations from the normalized composition, i.e., from total elements and oxides equal to 100 wt% (Fig. 1b). Therefore, at least a preliminary estimation of  ${}^{W}O^{2-}$ , H<sub>2</sub>O and *TEO*, followed by a normalization calculation of the original composition, is required.

### The oxo component, WO<sup>2</sup>-

- It is commonly accepted that  ${}^{W}O^{2-}$  and  ${}^{W}OH^{-}$  contents in amphibole mostly depend on two substitution mechanisms involving cations occurring at the M(1) and M(3) sites (e.g., King et al. 1999; Popp et al.
- 2006; Oberti et al. 2007a):

274 
$$M(1)(Mg, Fe^{2+}) + 2^WOH^- \rightarrow M(1)Ti^{4+} + 2^WO^{2-}$$
 (a)

275 
$$M^{(1,3)}Fe^{2+} + {}^{W}OH^{-} \rightarrow M^{(1,3)}Fe^{3+} + {}^{W}O^{2-}$$
 (b)

During igneous and metamorphic processes, the OH<sup>-</sup> content of amphibole is mostly ruled by substitution mechanism (a) wherein the amount of OH<sup>-</sup> at the W site is reduced by twice the amount of Ti incorporated at the M(1) site. Substitution (a) mostly occurs at high-T low-fH<sub>2</sub>O conditions, and involves chemical exchange of major components such as Mg, Fe<sup>2+</sup> and Ti with the surrounding environment (i.e., minerals and melt). During magma ascent or hydrothermal alteration, amphibole may undergo a high T-fO<sub>2</sub> process of deprotonation (i.e., dehydrogenation) involving iron oxidation according to substitution mechanism (b).

From a crystal-chemical viewpoint, the occurrence of  ${}^{W}O^{2-}$  induces important changes in the cation-ordering scheme typical of amphiboles, where high-charged C cations are fully ordered at the M(2) site, with the only exception of Al, which may disorder between the M(2) and M(3) sites in high-T Mg-rich pargasites and edenites (Oberti et al. 1995; Della Ventura et al. 2014). The different bond-valence bond-strength requirements of the O(3) oxygen after  ${\rm H}^+$  loss must be satisfied by the presence of high-charged cations at the coordinated M(1) (with multiplicity 2) and M(3) sites. This feature of the amphibole solid-solution system implies complex but strongly related compositional changes that can be empirically discerned using multivariate least-square analysis (e.g., Ridolfi and Renzulli 2012; Ridolfi et al. 2014; Zhang et al. 2017).

Among the 114 amphiboles in the calibration dataset, 87 formulae have  ${}^WO^{2-} \le 2^CTi$  implying that mechanism (b) is almost not or weakly active. Hereafter, for these amphiboles we will use the prefix "poorly-oxidized" to remind that the amount of  ${}^{M(1,3)}Fe^{3+}$  due to post-crystallization oxidation is zero or very low. These amphiboles may contain up to 1.3 apfu  ${}^WO^{2-}$ , which mostly derives from mechanism (a). However, the constraint of all the Ti in C-group cations ( ${}^CTi$ ) as a proxy for the oxo component (Hawthorne et al. 2012; Locock 2014) may be severely misleading because in these

samples a significant amount of  ${}^{C}$ Ti is often ordered at the M(2) site and hence does not contribute to mechanism (a) (Oberti et al. 2007a).

Regression analysis shows that the  ${}^{W}O^{2-}$  content in poorly-oxidized amphiboles (with  ${}^{W}O^{2-} \le 2^{C}$ Ti) can be estimated with reasonably low errors (Fig. 2a) using the following equation:

$$^{W}O^{2-} = -6.684X_{Si} + 11.025X_{Ti} - 0.989X_{Al} - 2.800X_{Fetot} - 20.359X_{Mn} - 0.903X_{Mg} - 0.000X_{Mg} - 0.000X_{$$

303 
$$6.875X_{Ca} - 11.119X_{Na} - 2.553X_K + 5.751X_F + 4.610 \text{ apfu}$$
 (3)

This equation can be applied without any previous calculation of the amphibole formula, as it only depends on the values of the cation fractions  $(X_i)$  calculated from EMP analyses. In addition, the  $X_i$  values are the same in both original and normalized compositions because a generalized overestimation (or underestimation) does not change the mass ratios.

A drawback of equation 3 is that it underestimates  $^{W}O^{2-}$  in highly-oxidized amphiboles (where  $^{W}O^{2-} > 2^{C}$ Ti), which underwent high-T, high- $fO_2$  post-magmatic and/or hydrothermal alteration according to the mechanism (b). However, this issue may even turn out to be an advantage when studying the processes of magmatic crystallization from amphibole crystals which underwent post-magmatic oxidation-deprotonation.  $fO_2$  in high-T magmatic environments (up to  $\sim 10^{-7}$  bar, corresponding to a  $\log fO_2$  of 3-4 units above the Ni-NiO buffer, hereafter NNO; Ridolfi and Renzulli 2012) is several orders of magnitude lower than in air ( $\sim 0.21$  bar, i.e.,  $\sim 0.68 \log fO_2$ ; Namur et al. 2012) where high-T post-magmatic oxidation most probably occurs. It is worth noting that the highly-oxidized amphiboles in our calibration dataset are Ca-dominant megacrysts (rapidly ejected to the surface from high T-P conditions) or mantle amphiboles crystallized from hydrothermal fluids (e.g. late-stage veins in peridotites, metasomatic deposits).

At this point, we analyzed correlations between the measured values of  ${}^{W}O^{2-}$  and cation compositional parameters in both poorly and highly oxidized amphiboles, starting from the assumption that the fractions of Ti and Fe<sup>3+</sup> occurring at the M(1) and M(3) sites are directly involved in the

process of deprotonation. The best correlation we found for the 114 amphiboles in the dataset is

reported in Figure 2b: i.e.,  ${}^{W}O^{2-} = 0.963[4/3{}^{C}Ti + 2/3{}^{C}Fe^{3+} + 2/3{}^{A}(Na+K)] - 0.624$ . The overall

324 correlation shows a reasonably good  $R^2$  value (0.927) and closely approaches the equation:

$${}^{W}O^{2-} = 4/3{}^{C}Ti + 2/3{}^{C}Fe^{3+} + 2/3{}^{A}(Na+K) - 2/3 \text{ apfu}$$
(4a)

- Equation 4a works well both for poorly ( ${}^{W}O^{2-} \le 2{}^{C}Ti$ ) and highly ( ${}^{W}O^{2-} > 2{}^{C}Ti$ ) oxidized amphiboles
- when  $4/3^{\rm C}$ Ti +  $2/3^{\rm C}$ Fe<sup>3+</sup> +  $2/3^{\rm A}$ (Na+K) is  $\geq 2/3$ . At those values, the only two samples significantly
- deviating from equation 4a (giving a WO<sup>2</sup>- overestimation up to 0.49 apfu) are rare Na-Ca amphiboles,
- i.e., alumino-taramite K22-2 and fluoro-alumino-magnesio-taramite DJ102-23, which are characterized
- by high <sup>C</sup>Fe<sup>3+</sup> and A-cation contents but, according to their crystal-chemical characterization do not
- contain oxo component (Oberti et al. 2007b; Fig. 2b ). In Figure 2b, amphiboles with  $4/3^{\circ}$ Ti +  $2/3^{\circ}$ Fe<sup>3+</sup>
- $+ 2/3^{A}(Na+K) \le 2/3$  have zero or negligible  $^{W}O^{2-}$  contents, providing the constraint:

333 
$$^{W}O^{2-} = 0$$
 apfu, if  $4/3^{C}Ti + 2/3^{C}Fe^{3+} + 2/3^{A}(Na+K) \le 2/3$  apfu (4b)

- When applying equations 4a and constraint 4b we obtain a  $\sigma_{est} = 0.12$  apfu for the whole dataset (Fig.
- 335 2b). When the two major outliers alumino-taramite K22-2 and fluoro-alumino-magnesio-taramite
- DJ102-23 are not considered, the maximum error decreases from 0.49 to 0.3 apfu which is even lower
- than that indicated by equation 3 for only the poorly-oxidized amphiboles (0.4 apfu; Fig. 2a).
- Equation (4a) and constraint (4b) can be easily applied to any amphibole unit-formula anytime
- an independent measurement of  $Fe^{3+}/Fe_{tot}$  is available. When this is not the case,  $^WO^{2-}$  and  $Fe^{3+}$
- contents can be estimated using a system of two linear equations including (4a) and the charge balance
- 341 equation:

$$342 4(Si+Ti) + 3(Al+Cr+Fe^{3+}) + 2[Mg+(Fe_{tot}-Fe^{3+})+Mn+Ni+Zn+Ca] + Na+K = 46 + {}^{W}O^{2-}$$
 (4c)

- 343 where the uncertainty of the  ${}^{W}O^{2-}$  and  $Fe^{3+}$  estimates depends on the errors of cation estimation
- multiplied by their ionic charge.

#### Revision 1

345

346

347

348

349

350

351

352

353

354

355

356

357

358

359

360

361

362

363

364

365

366

367

The presence of A-cations in equations (4a,b) may be explained by their capability to help in achieving local electroneutrality around the O(3) site, where deprotonation occurs. Recent *in operando* studies combining SREF and FTIR (Fourier Transform Infrared Spectroscopy) showed that deprotonation preferentially occurs close to an occupied *A* site, so that it is faster in amphibole compositions with fully occupied A-sites (Susta et al. 2016; Della Ventura et al. 2017; Oberti et al. 2018).

#### TOTAL COEFFICIENT AND CALCULATION PROCEDURE

In the previous section, we have stressed that the application of equation 2 is biased by the inevitable EMP errors of the 114 high-quality amphibole data (Fig. 1). In order to overcome this problem, obtaining an adjusted composition approaching a normalized one, we first calculated deviated compositions which are the concentrations (wt%) of the oxides and halogens (F, Cl) calculated from a normalized amphibole composition to have a TEO deviating from 100 wt% by a specific value, namely 98.2 and 101.8 wt%; e.g., normalized SiO<sub>2</sub>·0.982 (wt%), normalized F·1.018 (wt%). The opposites of 0.982 and 1.018 represent the corresponding total coefficients (TC) which, in general, can be calculated by dividing the sum of the oxides of a normalized composition by that of its original or deviated compositions. The TC values are 1 for normalized compositions, < 1 for overestimated compositions and > 1 for underestimated compositions. Then we used equations 2 and 3 to calculate preliminary formulas for both normalized and deviated compositions. The values of Fe<sub>2</sub>O<sub>3</sub> and FeO concentrations,  $O^{F,Cl}$ , and  $\triangle charge$  can also be calculated from these preliminary unit-formulae (Appendix 1). Multivariate least-square analysis using all of these 342 (114 normalized and 114.2 deviated) data provided the following equation to be used to calculate *TC*:

384

385

386

387

388

368 
$$TC = -7.9 * 10^{-4}SiO_2 + 6 * 10^{-4}TiO_2 - 6.6 * 10^{-4}Al_2O_3 + 8.75 * 10^{-5}Fe_2O_3 - 9.4 * 10^{-4}FeO -$$
369  $8.5 * 10^{-4}MgO - 1.1 * 10^{-3}CaO - 1.48 * 10^{-3}Na_2O - 8.6 * 10^{-4}K_2O - 9.62 * 10^{-3}O^{F,Cl} +$ 
370  $6.41 * 10^{-3}H_2O - 9.57 * 10^{-3}TEO + 4.13 * 10^{-4}\Delta charge + 2.024$  (5)

- where  $SiO_2$  to  $K_2O$  are the original, normalized or the deviated oxides (wt%). The calculated regression parameters are  $R^2 = 0.992$  and  $\sigma_{est} = 0.001$  (Fig. 3).
- If the TC values are applied to the original EMP analyses (i.e., original SiO<sub>2</sub>·TC, original TiO<sub>2</sub>·TC, etc.), the resulting adjusted compositions closely approach the normalized concentrations (wt%). These adjusted compositions can then be used to obtain amphibole formulae using again equations (2) and (3). Using the 114 amphiboles in our high-quality dataset, this second stage of calculations produces a statistic error ( $\sigma_{est}$ ) of 0.055 apfu for  $\Sigma Si \rightarrow K$ . The resulting formulae should be refined further using the series of stoichiometric constraints reported in Table 1 (see Appendix 1 for calculation).
- When applying these constraints to the apfu calculated from the calibration dataset, only sporadic and very minor adjustments are observed (a few calculated formulae indicate  $\sum$ Si-K slightly higher than 16 apfu). In this dataset, the calculated *TEO* span from 99.6 to 100.5 wt%, and the final  $\sigma_{est}$  values for  $^{A}$ (Ca+Na+K) and Si contents are 0.042 and 0.017 apfu, respectively (Table 3). The amount of Fe<sup>3+</sup> (and Fe<sup>2+</sup>) can then be calculated by charge balance (eq. 4c).
  - Optionally, the  ${}^WO^{2-}$  and  ${}^Fe^{3+}$  contents can be independently estimated using a system of two linear equations, i.e., 4a and 4c. The total amount of  ${}^Fe^{2+}$  is finally calculated by the constraint  ${}^Fe^{3+}$  +  ${}^Fe^{2+}$  (Table 1, Appendix 1). The condition expressed in the constraint 4b should be respected and the priority in adjusting  ${}^WO^{2-}$  and  ${}^Fe^{3+}$  values should be given to charge balance (i.e., eq. 4c) considering that  $\Delta charge$  can be as high as 0.1 due to error propagation in the solutions of this system.
- Finally, the calculated amphibole formula (AMFORM) can be used to calculate the molecular mass  $(M_r)$ , hereafter  $M_r^{AMFORM}$  (see section Essential Definitions for  $M_r$  calculation from a generic formula).

 $M_r^{AMFORM}$  should closely approach the molecular mass calculated with equation 1 using the CR value obtained after the application of equation 1 to the adjusted compositions (hereafter  $M_r^{CR} = 10^3 \cdot CR$  g/mol). In our database, the deviation among these molecular masses ( $\Delta MM\% = 200 \frac{M_r^{AMFORM} - M_r^{CR}}{M_r^{AMFORM} + M_r^{CR}}$ ) ranges between -0.60 and 0.74% ( $\sigma_{est} = 0.18$ ; Table 3).

A flowchart and a step by step procedure to calculate amphibole unit-formulae are reported in Appendix 1. The whole procedure is included in a user-friendly Excel spreadsheet (provided as supplementary material) called AMFORM.xlsx. By default, this spreadsheet gives the WO<sup>2-</sup> and Fe<sup>3+</sup> values calculated according to equations 3 and 4c, but it also gives the results of the optional method (eqs. 4a-c). We strongly recommend the use of this spreadsheet to avoid errors due to typing or unavoidable approximations of the coefficients reported in this article.

AMFORM.xlsx also provides warnings for bad analyses and deviations from the correct stoichiometry such as recalculated initial TEO < 98.2 and > 101.8 wt%, sum of C and B cations < 5 and 2 apfu, respectively (i.e., negative  $\Delta$ C and Ca in A-group) and  $\Delta$ MM% < -0.60 and > 0.74%, which are not included in Appendix 1.

#### TESTING THE AMFORM APPROACH

To allow for an independent validation of the AMFORM approach, a test was made using an additional 51 amphibole compositions belonging to the Ca, Na-Ca, Na and oxo groups, taken from the literature (King et al. 2000; Tiepolo et al. 2001; Oberti et al. 2000, 2003, 2010, 2015, 2016, 2017; Uvarova et al. 2007; Satoh et al. 2004; Della Ventura et al. 2014; Gentili et al. 2015; Gatta et al. 2017) or still unpublished (CNR-IGG Pavia), which have been analyzed with EMP±SREF±SIMS and other techniques for Fe<sup>3+</sup>/Fe<sub>tot</sub> measurements (KMnO<sub>4</sub> titration, SXRF, XANES, Mössbauer spectroscopy). It is worth noting that the analyses of these amphiboles generally have higher uncertainties (e.g., *TEO* of

#### Revision 1

97-102 wt%; dC from -0.07 to 0.01 apfu;  $\Delta charge$  from -0.09 to 0.07) than the 114 analyses selected for the calibration of the AMFORM procedure (see the AMFORM spreadsheet for these lower-quality data). This second test dataset also includes 10 amphibole composition-formula pairs recently published by Dyar et al. (2016) respecting the quality criteria of the calibration data (AMFORM.xlsx).

Table 3 and Figure 4 compare the capability of AMFORM to estimate the amphibole formula parameters for both the calibration and the test data. The generally higher  $\sigma_{est}$  values of the lower-quality test data confirm the validity of our approach while the higher  $\Delta MM\%$  values indicate that this parameter is useful for detecting large analytical uncertainties (Table 3). The reliability of AMFORM is further confirmed by the homogeneous distribution around the 1:1 line observed for both calibration and test data and by the absence of outliers (Fig. 4). The few Li-free Na amphibole used to test AMFORM suggest that the method is reliable also in the case of Na amphiboles (e.g., Fig. 4c), for which the calibration was based solely on end-member compositions (Table 2; Fig. 1b). A test performed using 28 Fe-Mg-Mn C2/m species (cummingtonite-grunerite; Hirschmann et al. 1994) also suggest that AMFORM.xlsx can be used for these amphiboles with reasonably low uncertainties ( $\sigma_{est} \leq 0.040$  apfu for the main cations). However, this test is not reliable because Hirschmann et al. (1994) calculated the formula under the constraint that  $\Sigma Si \rightarrow K = 15$ .

### A comparison between the AMFORM and the Locock (2014) spreadsheets

As a final step, we tested the capability of the most used methods to calculate the amphibole unit-formula (i.e., Tindle and Webb 1994; Dale et al. 2005; Locock 2014) using our calibration and test datasets (electronic supplement 1). For most compositions, the PROBE-AMPH spreadsheet (Tindle and Webb 1994) and the model of Dale et al. (2005) (which is an improvement of that of Holland and Blundy 1994) give errors which are about twice those of Locock (2014) and will be not discussed further.

438

439

440

441

442

443

444

445

446

447

448

449

450

451

452

453

454

455

456

457

458

459

460

461

When calculating the amphibole unit-formula, the most difficult parameters to quantify are the <sup>C</sup>Al and Fe<sup>3+</sup>contents and the amount of cations in A, i.e., A(Ca + Na + K) (e.g., Leake et al. 1997; Al'meev et al. 2002; Ridolfi et al. 2010). Figure 5, compares the AMFORM results obtained for these parameters with those calculated by the spreadsheet published by Locock (2014), which is based on the procedures suggested in the IMA 2012 classification scheme (Hawthorne et al. 2012). When the Fe<sup>3+</sup>/Fe<sub>tot</sub> ratio, and/or the H<sub>2</sub>O and Li contents are unknown (i.e., when only EMP analyses are available), the Locock (2014) spreadsheet provides two automatic procedures, depending on the presence or absence of WO<sup>2</sup>-. The Fe<sup>3+</sup> contents resulting from AMFORM are those of the default WO<sup>2-</sup> method (eq. 3 and 4c). As a matter of fact, considering the unit-formulae of the high-quality amphibole compositions as reference data (i.e., those cation contents that for their high-quality better approach the effective unit formulae), the errors of the AMFORM procedure are, on average, 2 to 4 times lower that those obtained with the spreadsheet proposed by Locock (2014) (Fig. 5). Locock (2014) tends to underestimate <sup>C</sup>Al and <sup>A</sup>(Ca + Na + K) in amphiboles with total cation contents close to 16 apfu, and to slightly overestimate the same parameters when the  $\Sigma$ Si-K is close to 15 apfu. As far as the Fe<sup>3+</sup> content is concerned, Locock (2014) methods with and without WO<sup>2-</sup> estimates, behaves similarly to the 13- and 15-cations methods by IMA-1997 (Leake et al. 1997) as they generally produce large overestimations and large underestimations, respectively (Fig. 5). For an independent validation of the AMFORM approach and Locock (2014)'s methods, we tested a subset of 19 published compositions of poorly-oxidized amphiboles (yellow squares in Fig. 5c; AMFORM spreadsheet). These data were not included in our high-quality calibration dataset because they were recently published, have not been examined by SREF and/or or because they have high  $\triangle charge$  values (up to  $\pm 0.13$ ). However, the Fe<sup>3+</sup> content (and Fe<sup>3+</sup>/Fe<sub>tot</sub>) of these amphiboles should be valuable as it was estimated by SREF and Mössbauer spectroscopic analyses (Dyar et al. 2016), Synchroton X-ray Fluorescence (SXRF; King et al. 2000), KMnO<sub>4</sub> titration (Satoh et al. 2004) or X-ray

Absorption Near Edge Structure (XANES) spectroscopy (Bonadiman et al. 2014). In the AMFORM (default method) and Locock (2014) diagrams (Figs. 5c,f,i), these 19 amphiboles with  $^{W}O^{2-}$  < 2Ti have the same behavior as the poorly-oxidized calibration amphiboles. When the reference Fe<sup>3+</sup> values of these amphiboles are compared to those obtained by AMFORM, they approach the 1:1 line and have deviations (from -0.14 to +0.27 apfu) well within the maximum-minimum Fe<sup>3+</sup> error range of the AMFORM default procedure (Fig. 5c).

### An evaluation of the two methods used by AMFORM to calculate WO2- and Fe3+

Figure 6 reports plots and statistics obtained by using the AMFORM default (eq. 3, 4c) and the optional (eq. 4a-c) methods to calculate the  $^{W}O^{2-}$  and  $Fe^{3+}$  contents for 137 amphibole compositions (114 high-quality compositions used for calibration plus 23 among lower-quality compositions and recently published data, both poorly and highly oxidized) where  $Fe^{3+}/Fe_{tot}$  values were measured as discussed in the previous paragraph and in Figure 5c.

The default method in AMFORM is particularly useful to estimate the amount of  $^WO^{2-}$  and  $Fe^{3+}$  in poorly-oxidized amphiboles, those in equilibrium with the melt and/or other minerals (e.g., at 800–1,130 C, 130–2,200 MPa and in between NNO-2.1 and NNO+3.6; Ridolfi and Renzulli 2012). Indeed, these amphiboles fall very close to (and are distributed homogeneously around) the 1:1 line in Figures 6a,b; their  $^WO^{2-}$  and  $Fe^{3+}$  contents can be estimated with a reasonably low uncertainty ( $\pm 0.1$  apfu; Table 3; Figs. 2a and 4c). In contrast, in the case of highly-oxidized amphiboles, i.e., those which underwent hydrothermal and post-crystallization oxidation, the default method may provide significant underestimation (up to 1.1 apfu,  $\sigma_{est} = 0.45$  apfu; Fig. 6a,b), and therefore cannot be used to study metasomatic and oxidation processes during magma ascent (Dyar et al. 1993; King et al. 1999; Popp et al. 2006; Oberti et al. 2007a). Hence, we suggest to use the optional method for these amphiboles, because it provides a roughly homogeneous distribution around the 1:1 line in the plots in Figures 6d,e.

486

487

488

489

490

491

492

493

494

495

496

497

498

499

500

501

502

503

504

505

507

508

The large observed uncertainties when estimating WO<sup>2-</sup> and Fe<sup>3+</sup> values by this method (up to 1.1 apfu,  $\sigma_{\rm est} = 0.3$  apfu; Table 3) occur because of the substantial propagation of errors from the system of two linear equations (eq. 4a and 4c) and two variables (WO<sup>2</sup>- and Fe<sup>3+</sup>). Indeed, Table 3 also reports the estimated Fe<sup>3+</sup> error due to uncertainty propagation (according to the probability theory), for both default and optional calculations. When calculated using the uncertainties of the calibration higherquality dataset, the propagation of Fe<sup>3+</sup> errors in the optional method are about twice of those in the default calculation and almost double when the quality of the data is lowered (i.e. when using the errors of the lower-quality test dataset). However, Figures 6c,f show that the error in Fe<sup>3+</sup>/Fe<sub>tot</sub> determination tends to decrease regularly with increasing total iron content (Fe<sub>tot</sub>) for both the default (only considering the poorly-oxidized amphiboles) and the optional method. In other words, the tested amphiboles show a homogeneous and decreasing distribution around the zero-error line (Figs 6c,f). It is worth noting that the most used methods for unit-formula calculation (Tindle and Webb 1994; Dale et al. 2005; Locock 2014) result in much more scattered distributions of the Fe<sup>3+</sup>/Fe<sub>tot</sub> errors and higher  $\sigma_{\rm est}$  values (electronic supplement 1). For Fe-Mg-Mn amphiboles such as cummingtonite and grunerite, we recommend the use of the optional method. We have tested AMFORM against the data of Hirschmann et al. (1994) indicating an Fe<sup>3+</sup>/Fe<sub>tot</sub> ≤ 1% for heat-treated Fe-Mg-Mn amphiboles, as measured by Mössbauer spectroscopy (see above). For these amphiboles, the optional method shows  $Fe^{3+}/Fe_{tot} < 5\%$  ( $\leq 1\%$  for most of them, 71%) whereas the default method indicates higher  $Fe^{3+}/Fe_{tot}$ values (up to 17%).

506 **IMPLICATIONS** 

Figure 4 and Table 3 demonstrate the capability of the AMFORM approach to quantify, based solely on EMP data, the most critical parameters in the unit formula of amphiboles with a satisfactory

reliability. It is worth noting that the proposed approach has been calibrated and is consistent with crystal-chemical formulae obtained by combining high-quality structure refinement and analytical data.

The AMFORM procedure has been calibrated and validated for some petrologically-relevant C2/m amphibole compositions (oxo, Ca, Na-Ca, Na, Fe-Mg-Mn amphiboles), considering only Li- and Mn<sup>3+</sup>-free end-member compositions. The presence of significant Li and Cl contents would strongly affect the results because their lower cation mass and higher anion mass, respectively, would largely affect the behavior of the CR-cmpg relationship. Indeed, AMFORM should be applied only to amphiboles with Cl < 0.2 apfu (<1 wt%). In addition, AMFORM only accounts for Mn<sup>2+</sup> and hence cannot be used to constrain the formula of Mn<sup>3+</sup>-rich amphiboles (e.g., dellaventuraite, ungarettiite; Hawthorne et al. 1995; Hawthorne et al. 2012).

However, AMFORM.xlsx automatically provides warnings anytime the composition proposed deviates too much from the calibration dataset and the calculated *TEO* values (both initial and adjusted) deviate too much from those shown by the calibration amphiboles.

The default AMFORM procedure to estimate <sup>W</sup>O<sup>2-</sup> and Fe<sup>3+</sup> contents is particularly recommended to study the stability of amphibole and develop (or refine) thermobarometric equations aiming at constraining the magma pre-eruptive conditions and storage from the amphibole composition of volcanic rocks (e.g., Ridolfi et al. 2010; Ridolfi and Renzulli 2012; Erdmann et al. 2014; Putirka 2016; Ridolfi et al. 2016). For this purpose, the difficulty of estimating the Fe<sup>3+</sup> content related to hydrothermal or post-magmatic oxidizing processes may even be considered as an advantage (see above). In any case, this Fe<sup>3+</sup> component can be roughly estimated using the optional <sup>W</sup>O<sup>2-</sup> and Fe<sup>3+</sup> results in AMFORM.xlsx.

The mass-based method proposed in this work may also open a new perspective in the calculation of the unit-formula of other minerals. It may be particularly useful for OH-bearing phases characterized by structural vacancies, where the total number of cation is not known (e.g., micas).

533

534

535

536

537

538

539

540

541

542

543

544

545

546

547

548

549

550

551

552

553

While equation 1 is valid for any type of chemical compound and mineral, equation 2 must be adapted to other phases with different proportions of anion and cation sites in order to allow a reliable estimate of CR, and thus, of the total cation apfu contents. Acknowledgments This work was supported by a fellowship of the Alexander Von Humboldt Foundation and a research grant ("assegno di ricerca") co-funded by University of Perugia and University of Urbino through the Consolidator Grant ERC-2013- CoG Proposal No. 612776 CHRONOS (P.I. Diego Perugini), both awarded to the first author. AZ and RO acknowledge support by the Italian PRIN 2015 grant code 20158 A9CBM. We are grateful to R.R. Al'meev and O. Namur (Leibniz Universität Hannover) for their critical readings of the manuscript. Careful and helpful reviews of the manuscript done by two anonymous referees greatly improved the quality of the manuscript. We thank them very much for all their suggestions. References Adam J., Oberti R., Cámara F., and Green T.H. (2007) An electron microprobe, LAM-ICP-MS and single-crystal X-ray structure refinement study of the effect of pressure, melt-H<sub>2</sub>O concentration and fO<sub>2</sub> on experimentally produced basaltic amphiboles. European Journal of Mineralogy, 19, 641-655. Al'meev R.R., Ariskin A.A., Ozerov A.Yu., and Kononkova N.N. (2002) Problems of the Stoichiometry and Thermobarometry of Magmatic Amphiboles: An Example of Hornblende

| 554 | from the Andesites of Nezymyannyi Volcano, Eastern Kamchatka. Geochemistry International,  |
|-----|--|
| 555 | 40, 723-738.   |
| 556 | Bonadiman C., Nazzareni S., Coltorti M., Comodi P., Giuli G., and Faccini B. (2014) Crystal chemistry  |
| 557 | of amphiboles: implications for oxygen fugacity and water activity in lithospheric mantle  |
| 558 | beneath Victoria Land, Antarctica. Contributions to Mineralogy and Petrology, 167, 984.  |
| 559 | Bottazzi P., Tiepolo M., Vannucci R., Zanetti A., Brumm R., Foley S.F., and Oberti R. (1999) Distinct  |
| 560 | site preferences for heavy and light REE in amphibole and the prediction of $^{Amph/L}D_{REE}$ .   |
| 561 | Contributions to Mineralogy and Petrology, 137, 36-45.   |
| 562 | Cipriani C. (2007) Amphiboles: Historical Perspective. Reviews in Mineralogy and Geochemitry, 67,  |
| 563 | 517-546.   |
| 564 | Coogan L.A., Wilson R.N., Gillis K.M., and MacLeod C.J. (2001) Near-solidus evolution of oceanic   |
| 565 | gabbros: insights from amphibole geochemistry. Geochimica et Cosmochimica Acta, 65, 4339-  |
| 566 | 4357.  |
| 567 | Dale J., Powel R., White R.W., Elmer F.L., and Holland T.J.B. (2005) A thermodynamic model for   |
| 568 | $Ca-Na  clinoamphiboles  in  Na_2O-CaO-FeO-MgO-Al_2O_3-SiO_2-H_2O-O  for  petrological  although the contraction of the $ |
| 569 | calculations. Journal of Metamorphic Geology, 23, 771–791.   |
| 570 | Della Ventura G., Bellatreccia F., Cámara F., and Oberti R. (2014) Crystal-chemistry and short-range   |
| 571 | order of fluoro-edenite and fluoro-pargasite: a combined X-ray diffraction and FTIR  |
| 572 | spectroscopic approach. Mineralogical Magazine, 78, 293-310.   |

| 573 | Della Ventura G., Susta U., Bellatreccia F., Marcelli A., Redhammer G.J., and Oberti R. (2017)                         |
|-----|--|
| 574 | Deprotonation of Fe-dominant amphiboles: Single-crystal HT-FTIR spectroscopic studies of                               |
| 575 | synthetic potassic-ferro-richterite. American Mineralogist, 102, 117-125.  |
| 576 | Dyar M.D., Mackwell S.J., McGuire A.V., Cross L.R., and Robertson J.D. (1993) Crystal chemistry of                     |
| 577 | Fe <sup>3+</sup> and H <sup>+</sup> in mantle kaersutite: Implications for mantle metasomatism. American Mineralogist, |
| 578 | 78, 968-979.   |
| 579 | Dyar M.D., Breves E.A., Gunter M.E., Lanzirotti A., Tucker J.M., Carey C.J., Peel S.E., Brown E.B.,                    |
| 580 | Oberti R., Lerotic M., and Delaney J.S. (2016) Use of multivariate analysis for synchrotron                            |
| 581 | micro-XANES analysis of iron valence state in amphiboles. American Mineralogist, 101, 1171-                            |
| 582 | 1189.  |
| 583 | Erdmann S., Martel C., Pichavant M., and Kushnir A. (2014) Amphibole as an archivist of magmatic                       |
| 584 | crystallization conditions: problems, potential, and implications for inferring magma storage                          |
| 585 | prior to the paroxysmal 2010 eruption of Mount Merapi, Indonesia. Contributions to Mineralogy                          |
| 586 | and Petrology, 167, 1016.  |
| 587 | Esawi E.K. (2004) AMPH-CLASS: An Excel spreadsheet for the classification and nomenclature of                          |
| 588 | amphiboles based on the 1997 recommendations of the International Mineralogical Association.                           |
| 589 | Computers & Geosciences 30, 753–760.   |
| 590 | Foley S., Tiepolo M., and Vannucci R. (2002) Growth of early continental crust controlled by melting                   |
| 591 | of amphibolite in subduction zones. Nature, 417, 837-840.  |
| 592 | Forbes W.C., and Starmer R.J. (1974) Kaersutite is a possible source of alkali olivine basalts. Nature,                |
| 593 | 250, 209-210.  |

| Gatta G.D., McIntyre G.J., Oberti R., and Hawthorne F.C. (2017) Order of <sup>[6]</sup> Ti <sup>4+</sup> in a Ti-rich calcium   |
|---|
| amphibole from Kaersut, Greenland: a combined X-ray and neutron diffraction study. Physics  |
| and Chemistry of Minerals, 44, 83-94.   |
| Gentili S., Bonadiman C., Biagioni C., Comodi P., Coltorti M., Zucchini A., and Ottolini L. (2015)  |
| Oxo-amphiboles in mantle xenoliths: evidence for H <sub>2</sub> O-rich melt interacting with the  |
| lithospheric mantle of Harrow Peaks (Northern Victoria Land, Antarctica). Minerogy and  |
| Petrology, 109, 741-759.  |
| Gunter M.E., Belluso E., and Mottana A. (2007) Amphiboles: Environmental and health concerns.   |
| Reviews in Mineralogy and Geochemitry, 67, 453-516.   |
| Hammarstrom J.M., and Zen E. (1986) Aluminum in hornblende: an empirical igneous geobarometer.  |
| American Mineralogist, 71, 1297-1313.   |
|   |
| Haüy R.J. (1822) Traité de Minéralogie. II ed. Bachelier-Huzard, Paris, pp. 597.  |
|   |
| Haüy R.J. (1822) Traité de Minéralogie. II ed. Bachelier-Huzard, Paris, pp. 597.  |
| Haüy R.J. (1822) Traité de Minéralogie. II ed. Bachelier-Huzard, Paris, pp. 597.  Hawthorne F.C., Ungaretti L., Oberti R., Bottazzi P., and Czamanske G.K. (1993) Li: An important  |
| <ul> <li>Haüy R.J. (1822) Traité de Minéralogie. II ed. Bachelier-Huzard, Paris, pp. 597.</li> <li>Hawthorne F.C., Ungaretti L., Oberti R., Bottazzi P., and Czamanske G.K. (1993) Li: An important component in igneous alkali amphiboles. American Mineralogist, 78, 733-745.</li> </ul>  |
| <ul> <li>Haüy R.J. (1822) Traité de Minéralogie. II ed. Bachelier-Huzard, Paris, pp. 597.</li> <li>Hawthorne F.C., Ungaretti L., Oberti R., Bottazzi P., and Czamanske G.K. (1993) Li: An important component in igneous alkali amphiboles. American Mineralogist, 78, 733-745.</li> <li>Hawthorne F.C. (1983) The crystal chemistry of the amphiboles. The Canadian Mineralogist, 21, 173-</li> </ul>  |
| <ul> <li>Haüy R.J. (1822) Traité de Minéralogie. II ed. Bachelier-Huzard, Paris, pp. 597.</li> <li>Hawthorne F.C., Ungaretti L., Oberti R., Bottazzi P., and Czamanske G.K. (1993) Li: An important component in igneous alkali amphiboles. American Mineralogist, 78, 733-745.</li> <li>Hawthorne F.C. (1983) The crystal chemistry of the amphiboles. The Canadian Mineralogist, 21, 173-480.</li> </ul>  |
| <ul> <li>Haüy R.J. (1822) Traité de Minéralogie. II ed. Bachelier-Huzard, Paris, pp. 597.</li> <li>Hawthorne F.C., Ungaretti L., Oberti R., Bottazzi P., and Czamanske G.K. (1993) Li: An important component in igneous alkali amphiboles. American Mineralogist, 78, 733-745.</li> <li>Hawthorne F.C. (1983) The crystal chemistry of the amphiboles. The Canadian Mineralogist, 21, 173-480.</li> <li>Hawthorne F.C., Oberti R., Cannillo E., Sardone N., Zanetti A., Grice J.D., and Ashley P.M. (1995). A</li> </ul> |

| 614   | Hawthorne F.C., Oberti R., Della Ventura G., and Mottana A. (2007) Amphiboles: Crystal Chemistry,   |
|---|---|
| 615   | Occurrence, and Health Issues. Reviews in Mineralogy and Geochemitry, 67, 545 pp  |
| 616   | Hawthorne F.C., Oberti R., Harlow G.E., Maresch W.V., Martin R.F., Schumacher J.C., and Welch   |
| 617   | M.D. (2012) IMA report Nomenclature of the amphibole supergroup. American Mineralogist,   |
| 618   | 97, 2031-2048.  |
| 619   | Hawthorne F.C., Oberti R., Cannillo E., Ottolini L., Roelofsen J.N., and Martin R.F. (2001) Li-bearing  |
| 620   | arfvedsonitic amphiboles from the Strange Lake peralkaline granite, Quebec. The Canadian  |
| 621   | Mineralogist, 39, 1161-1170.  |
| 622   | Hirschmann M., Evans B.W., and Yang H. (1994) Composition and temperature dependence of Fe-Mg   |
| 623   | ordering in cummingtonite-grunerite as determined by X-ray diffraction. American Mineralogist   |
| 624   | 79, 862-877.  |
|   |   |
| 625   | Holland T.J.B., and Blundy J.D. (1994) Non-ideal interactions in calcic amphiboles and their bearing  |
| 625<br>626  | Holland T.J.B., and Blundy J.D. (1994) Non-ideal interactions in calcic amphiboles and their bearing on amphibole-plagioclase thermometry. Contributions to Mineralogy and Petrology, 116, 433-   |
|   |   |
| 626   | on amphibole-plagioclase thermometry. Contributions to Mineralogy and Petrology, 116, 433-  |
| 626<br>627  | on amphibole-plagioclase thermometry. Contributions to Mineralogy and Petrology, 116, 433-447.  |
| 626<br>627<br>628   | on amphibole-plagioclase thermometry. Contributions to Mineralogy and Petrology, 116, 433-447.  Jackson C.R.M., Parman S.W., Kelley S.P., and Cooper R.F. (2013) Noble gas transport into the   |
| <ul><li>626</li><li>627</li><li>628</li><li>629</li></ul>                         | on amphibole-plagioclase thermometry. Contributions to Mineralogy and Petrology, 116, 433-447.  Jackson C.R.M., Parman S.W., Kelley S.P., and Cooper R.F. (2013) Noble gas transport into the mantle facilitated by high solubility in amphibole. Nature Geoscience, 6, 562-565.  |
| <ul><li>626</li><li>627</li><li>628</li><li>629</li><li>630</li></ul>             | on amphibole-plagioclase thermometry. Contributions to Mineralogy and Petrology, 116, 433-447.  Jackson C.R.M., Parman S.W., Kelley S.P., and Cooper R.F. (2013) Noble gas transport into the mantle facilitated by high solubility in amphibole. Nature Geoscience, 6, 562-565.  Jacobson C.E., and Sorensen S.S. (1986) Amphibole compositions and metamorphic history of the   |
| <ul><li>626</li><li>627</li><li>628</li><li>629</li><li>630</li><li>631</li></ul> | on amphibole-plagioclase thermometry. Contributions to Mineralogy and Petrology, 116, 433-447.  Jackson C.R.M., Parman S.W., Kelley S.P., and Cooper R.F. (2013) Noble gas transport into the mantle facilitated by high solubility in amphibole. Nature Geoscience, 6, 562-565.  Jacobson C.E., and Sorensen S.S. (1986) Amphibole compositions and metamorphic history of the Rand Schist and the greenschist unit of the Catalina Schist, Southern California. Contributions to  |
| 626<br>627<br>628<br>629<br>630<br>631<br>632                                     | on amphibole-plagioclase thermometry. Contributions to Mineralogy and Petrology, 116, 433-447.  Jackson C.R.M., Parman S.W., Kelley S.P., and Cooper R.F. (2013) Noble gas transport into the mantle facilitated by high solubility in amphibole. Nature Geoscience, 6, 562-565.  Jacobson C.E., and Sorensen S.S. (1986) Amphibole compositions and metamorphic history of the Rand Schist and the greenschist unit of the Catalina Schist, Southern California. Contributions to Mineralogy and Petrology, 92, 308-315. |

637

638

639

640

641

642

643

644

645

646

647

648

649

650

651

652

653

654

655

656

657

King P.L., Hervig R.L., Holloway J.R., Delaney J.S., and Dyar M.D. (2000) Partitioning of Fe<sup>3+</sup>/Fe<sub>total</sub> between amphibole and basanitic melt as a function of oxygen fugacity. Earth and Planetary Science Letters, 178, 97-112. Laird J.O., and Albee A.L. (1981) High-pressure metamorphism in mafic schist from Northern Vermont. American Journal of Science, 281, 97-126. Léger A., Rebbert C., and Webster J. (1996) Cl-rich biotite and amphibole from Black Rock Forest, Cornwall, New York. American Mineralogist, 81, 495–504. Leake B.E. (1978) Nomenclature of amphiboles. The Canadian Mineralogist, 16, 501-520. Leake B.E., Woolley A.R., Arps C.E.S., Birch W.D., Gilbert M.C., Grice J.D., Hawthorne F.C., Kato A., Kisch H.J., Krivovichev V.G., Linthout K., Laird J., Mandarino J., Maresch W.V., Nickel E.H., Schumaker J.C., Smith D.C., Stephenson N.C.N., Ungaretti L., Whittaker E.J.W., and Youzhi G. (1997) Nomenclature of amphiboles: report of the subcommittee on amphiboles of the International Mineralogical Association Commission on New Minerals and Mineral Names. Mineralogical Magazine, 61, 295-321. Locock A.J. (2014) An Excel spreadsheet to classify chemical analyses of amphiboles following the IMA2012 recommendations. Computer and Geosciences, 62, 1–11. McCanta M.C., Treiman A.H., Dyar M.D., Alexander C.M.O.'D., Rumble III D., and Essene E.J. (2008) The LaPaz Icefield 04840 meteorite: Mineralogy, metamorphism, and origin of an amphibole-and biotite-bearing R chondrite. Geochimica et Cosmochimica Acta, 72, 5757-5780. Oberti R., Ungaretti L., Cannillo E., Hawthorne F.C., and Memmi I. (1995) Temperature-dependent Al order-disorder in the tetrahedral double chain of C2/m amphiboles. European Journal of Mineralogy, 7, 1049-1063.

| 3   | Oberti R., Vannucci R., Zanetti A., Tiepolo M., and Brumm R.C. (2000) A crystal chemical re-        |
|---|---|
| )   | evaluation of amphibole/melt and amphibole/clinopyroxene $D_{Ti}$ values in petrogenetic studies.   |
| )   | American Mineralogist, 85, 407-419.   |
| _   | Oberti R., Boiocchi M., and Smith D.C. (2003) Fluoronyböite from Jianchang (Su-Lu, China) and       |
| <u>,                                     </u> | nybo«ite from Nybö (Nordfjord, Norway): a petrological and crystal-chemical comparison of           |
| 3   | these two high-pressure amphiboles. Mineralogical Magazine, 67, 769–782.                            |
| ļ   | Oberti R., Hawthorne F.C., Cannillo E., and Cámara F. (2007a) Long-range order in amphiboles.       |
| ,   | Reviews in Mineralogy and Geochemistry, 67, 125-171.  |
| <u>,                                    </u>  | Oberti R., Boiocchi M., Smith D.C., and Medenbach O. (2007b) Aluminotaramite, alumino-              |
| ,   | magnesiotaramite, and fuoro-alumino-magnesiotaramite: Mineral data and crystal chemistry.           |
| 3   | American Mineralogist, 92, 1428-1435.   |
| )   | Oberti R., Boiocchi M., Hawthorne F.C., and Robinson P. (2010) Crystal structure and crystal        |
| )   | chemistry of fluoro-potassic-magnesio-arfvedsonite from Monte Metocha, Xixano region,               |
| _   | Mozambique, and discussion of the holotype from Quebec, Canada. Mineralogical Magazine,             |
| <u> </u>                                      | 74, 951-960.  |
| 3   | Oberti R., Boiocchi M., Hawthorne F.C., Ball N.A., and Harlow G.E. (2015) Katophorite from the Jade |
| ļ   | Mine Tract, Myanmar: mineral description of a rare (grandfathered) endmember of the                 |
| <u>,</u>                                      | amphibole supergroup. Mineralogical Magazine, 79, 355–363.  |
| ò   | Oberti R., Boiocchi M., Hawthorne F.C., Ball N.A., Cámara F., Pagano R., and Pagano A. (2016)       |
| ,   | Ferro-ferri-hornblende from the Traversella Mine (Ivrea, Italy): occurrence, mineral description    |
| 3   | and crystal-chemistry. Mineralogical Magazine, 80, 1233-1242.                                       |

Oberti R., Boiocchi M., Hawthorne F.C., Ball N.A., and Blass G. (2017) Ferri-obertite from the 679 680 Rothenberg quarry, Eifel volcanic complex, Germany: mineral data and crystal chemistry of a new amphibole end-member. Mineralogical Magazine, press. DOI: 10.1127/ejm/2018/0030-681 2712. 682 Oberti R., Boiocchi M., Zema M., Hawthorne F.C., Redhammer G., Susta U., and Della Ventura G. 683 (2018) The HT behaviour of riebeckite: Expansivity, deprotonation, selective Fe oxidation and a 684 novel cation disordering scheme for amphiboles. European Journal of Mineralogy, press. DOI: 685 10.1127/ejm/2018/0030-2712. 686 Ottolini L., Bottazzi P., Zanetti A., and Vannucci R. (1995) Determination of hydrogen in silicates by 687 Second Ion Mass Spectrometry. The Analist, 120, 1309-1314. 688 689 Namur O., Charlier B., Toplis M.J., and Auwera J.V. (2012) Prediction of plagioclase-melt equilibria in anhydrous silicate melts at 1 atm. Contributions to Mineralogy and Petrology, 163, 133-150. 690 Perinelli C., Andreozzi G.B., Conte A.M., Oberti R., and Armienti P. (2012) Redox state of 691 692 subcontinental lithospheric mantle and relationships with metasomatism: insights from spinel peridotites from northern Victoria Land (Antarctica). Contributions to Mineralogy and 693 Petrology, 164, 1053-1067. 694 Popp R.K., Hibbert H.A., and Lamb W.M. (2006) Oxy-amphibole equilibria in Ti-bearing calcic 695 amphiboles: Experimental investigation and petrologic implications for mantle-derived 696 amphiboles. American Mineralogist, 91, 54-66. 697 698 Putirka K. (2016) Amphibole thermometers and barometers for igneous systems and some implications for eruption mechanisms of felsic magmas at arc volcanoes. American Mineralogist, 101, 841-699 858. 700

Ridolfi F., Renzulli A., and Puerini M. (2010) Stability and chemical equilibrium of amphibole in calc-701 702 alkaline magmas: an overview, new thermobarometric formulations and application to subduction-related volcanoes. Contributions to Mineralogy and Petrology, 160, 45-66. 703 704 Ridolfi F., and Renzulli A. (2012) Calcic amphiboles in calc-alkaline and alkaline magmas: thermobarometric and chemometric empirical equations valid up to 1,130°C and 2.2 GPa. 705 Contributions to Mineralogy and Petrology, 163, 877-895. 706 Ridolfi F., Renzulli A., and Acosta-Vigil A. (2014) On the stability of magmatic cordierite and new 707 708 thermobarometric equations for cordierite-saturated liquids. Contributions to Mineralogy and Petrology, 167, 996. 709 710 Ridolfi F., Braga R., Cesare B., Renzulli A., Perugini D., and Del Moro S. (2016) Unravelling the complex interaction between mantle and crustal magmas encoded in the lavas of San Vincenzo 711 (Tuscany, Italy). Part I: Petrography and Thermobarometry. Lithos, 244, 218-232. 712 Robinson G.W., Grief J.D., Gault R.A., and Lalonde A.E. (1997) Potassic pargasite, a new member of 713 714 the amphibole group from Pargas, Turku-Pori, Finland. The Canadian Mineralogist, 35, 1535-1540. 715 Rock N.M.S., and Leake B.E. (1984) The International Mineralogical Association amphibole 716 nomenclature scheme: computerization and its consequences. Mineralogical Magazine, 48, 211-717 227. 718 Satoh H., Ymaguchi Y., and Makino K. (2004) Ti-substitution mechanism in plutonic oxy-kaersutite 719 720 from the Larvik alkaline complex, Oslo rift, Norway. Mineralogical Magazine, 68, 687–697.

Smith P.P.K. (1977) An Electron Microscopic Study of Amphibole Lamellae in Augite. Contributions 721 722 to Mineralogy and Petrology, 59, 317-322. Smith D.J. (2014) Clinopyroxene precursors to amphibole sponge in arc crust. Nature 723 724 Communications, 5, 4329. Spear F.S., and Kimball K.L. (1984). RECAMP—A FORTRAN IV program for estimating Fe<sup>3+</sup> 725 contents in amphiboles. Computer and Geosciences, 10, 317-325. 726 Susta U. (2016) Dehydration and deprotonation processes in minerals: development of new 727 spectroscopic techniques. Unpublished PhD Thesis, University of Roma Tre. 728 Stout J.H. (1972) Phase Petrology and Mineral Chemistry of Coexisting Amphiboles from Telemark, 729 Norway. Journal of Petrology, 13, 99-145. 730 Tiepolo M., Vannucci R., Oberti R., Foley S., Bottazzi P., and Zanetti A. (2000) Nb and Ta 731 732 incorporation and fractionation in titanian pargasite and kaersutite: crystal-chemical constraints and implications for natural systems. Earth and Planetary Science Letters, 176, 185-201. 733 Tiepolo M., Bottazzi P., Foley S.F., Oberti R., Vannucci R., and Zanetti A. (2001) Fractionation of Nb 734 735 and Ta from Zr and Hf at Mantle Depths: the Role of Titanian Pargasite and Kaersutite. Journal of Petrology, 42, 221-232. 736 Tiepolo M., Zanetti A., Oberti R., Brumm R., Foley S., and Vannucci R. (2003) Trace-element 737 partitioning between synthetic potassic-richterites and silicate melts, and contrasts with the 738 partitioning behaviour of pargasites and kaersutites. European Journal of Mineralogy, 15, 329-739 340. 740 Tindle A.G., and Webb P.C. (1994) PROBE-AMPH—a spreadsheet program to classify microprobe-741

derived amphibole analyses. Computer and Geosciences, 20, 1201-1228.

| 743               | Ungaretti L. (1980) Recent developments in X-ray single crystal diffractometry applied to the crystal-   |
|-------------------|--|
| 744               | chemical study of amphiboles. Godisnjak Jugoslavenskog Centra za Kristalografiju, 15, 29-65.   |
| 745               | Ungaretti L., Smith D.C., and Rossi G. (1981) Crystal-chemistry by X-ray structure refinement and  |
| 746               | electron microprobe analysis of a series of sodic-calcic to alkali amphiboles from the NybO  |
| 747               | eclogite pod, Norway. Bulletin de Minéralogie, 104, 400-412.   |
| 748               | Uvarova Y., Sokolova E., Hawthorne F.C., McCammon C.A., Kazansky V.I., and Lobanov K.V.  |
| 749               | (2007) Amphiboles from the Kola Superdeep Borehole: Fe <sup>3+</sup> contents from crystal-chemical  |
|                   |  |
| 750               | analysis and Mössbauer spectroscopy. Mineralogical Magazine, 71, 651-669.  |
| 750<br>751        | analysis and Mössbauer spectroscopy. Mineralogical Magazine, 71, 651-669.  Vannucci R., Piccardo G.B., Rivalenti G., Zanetti A., Rampone E., Ottolini L., Oberti R., Mazzucchelli  |
|                   |  |
| 751               | Vannucci R., Piccardo G.B., Rivalenti G., Zanetti A., Rampone E., Ottolini L., Oberti R., Mazzucchelli   |
| 751<br>752        | Vannucci R., Piccardo G.B., Rivalenti G., Zanetti A., Rampone E., Ottolini L., Oberti R., Mazzucchelli M., and Bottazzi P. (1995) Origin of LREE-depleted amphiboles in the subcontinental mantle.   |
| 751<br>752<br>753 | Vannucci R., Piccardo G.B., Rivalenti G., Zanetti A., Rampone E., Ottolini L., Oberti R., Mazzucchelli M., and Bottazzi P. (1995) Origin of LREE-depleted amphiboles in the subcontinental mantle. Geochimica et Cosmochimica Acta, 59, 1763-1771. |

#### Revision 1

757

758

759

760

761

762

763

764

765

766

767

768

769

770

771

772

773

774

775

776

**Table captions** Table 1. Summary of the preferred site-assignments and stoichiometric constraints for Li- and Mn<sup>3+</sup>-free C2/m amphiboles, according to Hawthorne et al. (2012). Table 2. Formula and normalized composition (wt%) of the selected Li- and Mn-free monoclinic amphibole end-members and the oxo counterparts for the Ca amphiboles considered in this work. As the composition is normalized, all total elements and oxides close to ideality (100 wt%). The end-embers are ordered by increasing Mr. Values of cmpg are also reported for comparison. Table 3. Statistic errors ( $\sigma_{est}$ ) of the AMFORM procedure calculated using the calibration and test data. The errors of uncertainty propagation in the calculation of the parameters are also reported. See AMFORM.xlsx for references and data. Figure captions Figure 1. Plots of CR vs. (a)  $M_r$ , molecular mass, and (b) cmpg, cation mass per gram. The equations (and their statistic values) obtained using normalized and end-member (Table 2) compositions are also reported. The end-member sample with the lowest  $M_r$  is cummingtonite,  $\Box Mg_2Mg_5Si_8O_{22}(OH)_2$ ,

#### Revision 1

whereas that with the highest  $M_r$  is ferro-ferri-cannilloite,  $CaCa_2(Fe^{2+}_4Fe^{3+})(Si_5Al_3)O_{22}(OH)_2$ . Because of EMP analytical errors, the original amphibole compositions show TEO (Total Elements and Oxides) varying from 98.3 to 100.8 wt%. Underestimated (< 100 wt%) and overestimated (> 100 wt%) compositions are located above and below the ideal relations, respectively. See the text for additional details.

783 Figure 2.

782

784

785

786

787

788

789

- (a) Correlation between the measured (reference)  $^WO^{2-}$  values and those calculated with equation 3 for 87 amphiboles with  $^WO^{2-} \le 2^CTi$  (i.e., poorly-oxidized amphiboles); the 1:1 line is reported together with the standard ( $\sigma_{est}$ ) and maximum (Max) errors. (b) The best correlation found between the reference  $^WO^{2-}$  values and cation composition for all the 114 high-quality amphibole compositions. The red dashed lines describe the proposed relations; related equations and statistic errors are also reported in red. See text for additional details.
- 790 Figure 3.
- The correlation between *TC* (Total Coefficient) values and those calculated with equation 5 for the 342 calculated compositions (either normalized or deviated) and the 114 original compositions. Normalized and deviated *TEO* data are also shown. Maximum and minimum uncertainties of the equation are +0.005 and -0.004.
- 795 Figure 4.
- The correlation between the reference <sup>T</sup>Si (a), <sup>C</sup>Al (b), <sup>B</sup>Na (c) and <sup>A</sup>(Ca + Na + K) (d) values and those calculated with the AMFORM spreadsheet for the amphibole compositions used to calibrate the

#### Revision 1

procedure (blue diamonds) and for those used for testing (yellow triangles). The 1:1 lines are reported in all diagrams (see Table 3 for statistics).

Figure 5.

Correlations between the reference  $^{C}$ Al,  $^{A}$ (Na + K + Ca) and Fe<sup>3+</sup> values (from EMP+SREF±SIMS data) and those calculated solely from the high-quality EMP analysis in our dataset; (a-c): AMFORM; (d-f): Locock (2014) without  $^{W}O^{2-}$  estimates; (g-i): Locock (2014) with  $^{W}O^{2-}$  estimates. The statistics in diagrams (c), (f), (i) for Fe<sup>3+</sup> refer to the 87 amphiboles with  $^{W}O^{2-} \le 2^{C}$ Ti, whereas all the other diagrams refer to all the 114 amphiboles of the dataset; max and min errors are the maximum and minimum (calculated – reference) values. Symbols are reported in (a) and (f). In (c), (f), (i), highly-oxidized Ca amphiboles ( $^{W}O^{2-} > 2^{C}$ Ti) are distinguished by orange empty squares while yellow squares are additional Ca and Na-Ca amphiboles (poorly-oxidized;  $^{W}O^{2-} \le 2^{C}$ Ti) the Fe<sup>3+</sup>/Fe<sub>tot</sub> value of which was measured using independent techniques (King et al. 2000; Satoh et al. 2004; Bonadiman et al. 2014; Dyar et al. 2016; see AMFORM.xlsx). The 1:1 line is reported in all diagrams.

811 Figure 6.

Correlations between the reference  ${}^WO^{2-}$  and  $Fe^{3+}$  values and those calculated with the default (a-b) and the optional (d-e) procedures in AMFORM for the 114 compositions used for calibration and the 23 compositions with  $Fe^{3+}$  measured by independent techniques. In these diagrams the 1:1 line is also shown. (c) and (f) report the errors of  $Fe^{3+}/Fe_{tot}$  calculations versus the reference total iron content (apfu); the line represent the 0 error reference. In (a) and (b), statistics refer only to highly-oxidized Ca amphiboles (with  ${}^WO^{2-} > {}^CTi$ ) and ferri-kaersutites, symbols have the same color of statistic values; see Fig. 4c for the statistics of poorly-oxidized amphiboles. In (c), (d), (e) and (f) statistics refer to all the 137 amphiboles considered. See the text for additional explanations.

Fig 1.

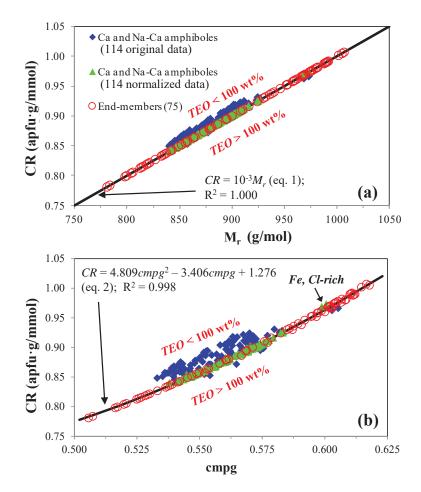


Fig 2.

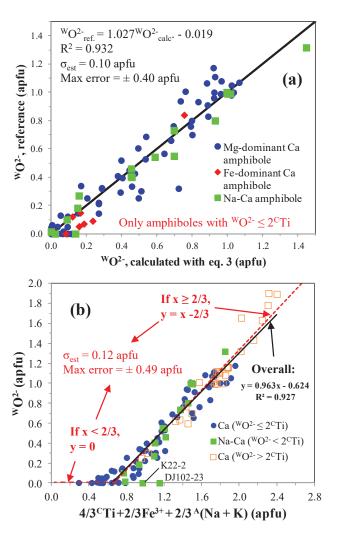


Fig 3.

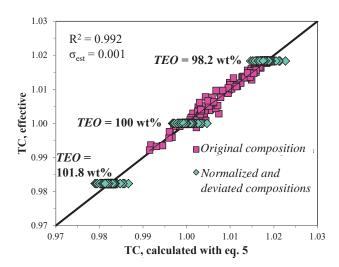


Fig 4.

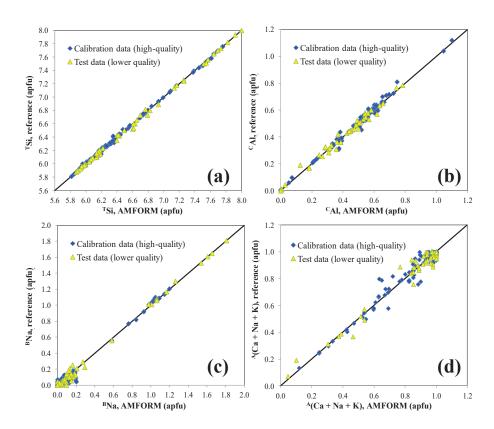


Fig 5.

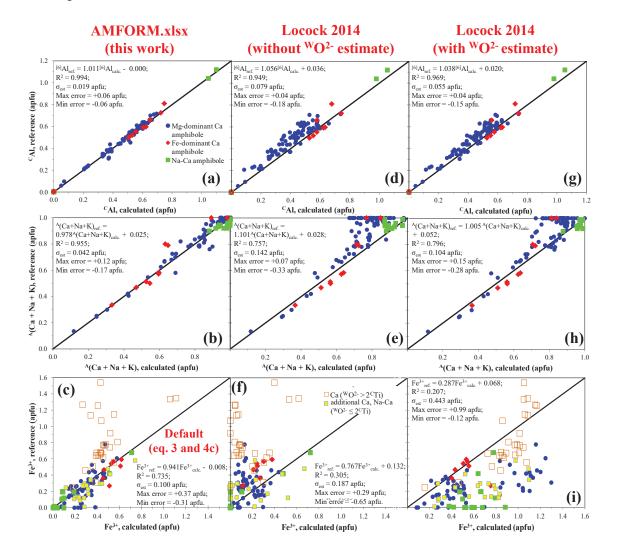


Fig 6.

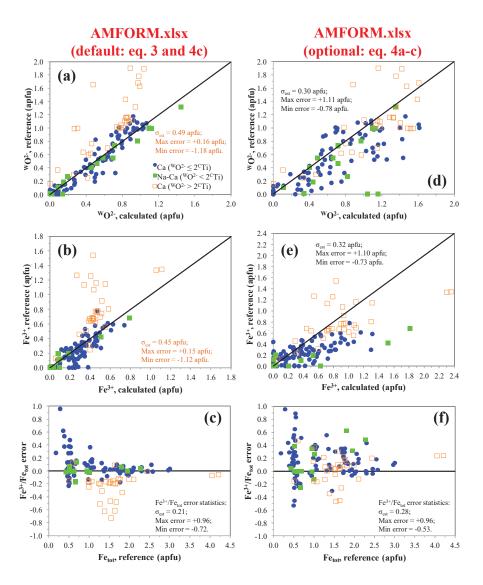


Table 1.

|             | os and total<br>apancy | Elements          | Stoichiometric constraints (apfu)     |  |  |  |  |
|-------------|------------------------|-------------------|---------------------------------------|--|--|--|--|
|             | Cations (15-1          | 6 apfu)           |                                       |  |  |  |  |
|             |                        | Si                | $Si \le 8$                            |  |  |  |  |
| T (8 apfu)  |                        | Al                |                                       |  |  |  |  |
|             |                        | Ti                | $\sum Si \rightarrow Ti \ge 8$        |  |  |  |  |
|             |                        | Cr                |                                       |  |  |  |  |
|             | C (5 apfu)             | Ni                |                                       |  |  |  |  |
|             | c (5 upiu)             | Zn                |                                       |  |  |  |  |
|             |                        | Fe <sub>tot</sub> |                                       |  |  |  |  |
|             |                        | Mn                |                                       |  |  |  |  |
| B (2 apfu)  |                        | Mg                | $\sum Si \rightarrow Mg \ge 13$       |  |  |  |  |
|             |                        | Ca                |                                       |  |  |  |  |
|             | A (0-1 apfu)           | Na                |                                       |  |  |  |  |
|             |                        | K                 | $15 \le \sum Si \rightarrow K \le 16$ |  |  |  |  |
|             | Anions                 | s (24 apfu)       |                                       |  |  |  |  |
| O (22 apfu) |                        | O                 | $\Sigma O \ge 22$                     |  |  |  |  |
|             |                        | ОН                |                                       |  |  |  |  |
|             | W (2 apfu)             | F                 |                                       |  |  |  |  |
|             |                        |                   |                                       |  |  |  |  |
|             |                        | Cl                |                                       |  |  |  |  |

ap fu: atoms per formula units;  $\Delta C = \sum Si \rightarrow Mg - 13$  (Mn, Fe<sup>2+</sup> and Mg occurring as B cations). Notes: Fe<sub>tot</sub> = Fe<sup>3+</sup> + Fe<sup>2+</sup> (only Fe<sup>2+</sup> is assigned to the B sites)

Table 2.

| Name                      | Group Sub-grou     | Formula   | SiO <sub>2</sub> TiO <sub>2</sub> Al <sub>2</sub> C | <sub>3</sub> FeO <sub>tot</sub> | MgO CaO     | Na <sub>2</sub> O Sum    | Fe <sub>2</sub> O <sub>3</sub> FeO | H <sub>2</sub> O | $M_r$ | cmpg  |
|---------------------------|--------------------|---|---|---------------------------------|-------------|--------------------------|------------------------------------|------------------|-------|-------|
| Cummingtonite             | W(OH,F,Cl) Mg-Fe-M | In □Mg <sub>2</sub> Mg <sub>5</sub> Si <sub>8</sub> O <sub>22</sub> (OH) <sub>2</sub>   | 61.56 0.00 0.00                                     |                                 | 36.13 0.00  | 0.00 97.69               |                                    | 2.31             | 781   | 0.506 |
| Glaucophane               | W(OH,F,Cl) Na      | $\square Na_2(Mg_3Al_2)Si_8O_{22}(OH)_2$  | 61.35 0.00 13.0                                     | 1 0.00                          | 15.43 0.00  | 7.91 97.70               |                                    | 2.30             | 784   | 0.507 |
| Winchite                  | W(OH,F,Cl) Na-Ca   | □(NaCa)(Mg <sub>4</sub> Al)Si <sub>8</sub> O <sub>22</sub> (OH) <sub>2</sub>  | 60.24 0.00 6.39                                     | 0.00                            | 20.20 7.03  | 3.88 97.74               |                                    | 2.26             | 798   | 0.516 |
| Barroisite                | W(OH,F,Cl) Na-Ca   | $\square$ (NaCa)(Mg <sub>3</sub> Al <sub>2</sub> )(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>   | 52.60 0.00 19.1                                     | 3 0.00                          | 15.12 7.01  | 3.88 97.75               |                                    | 2.25             | 800   | 0.517 |
| Eckermannite              | W(OH,F,Cl) Na      | NaNa <sub>2</sub> (Mg <sub>4</sub> Al)Si <sub>8</sub> O <sub>22</sub> (OH) <sub>2</sub>   | 59.80 0.00 6.34                                     | 0.00                            | 20.06 0.00  | 11.57 97.76              |                                    | 2.24             | 804   | 0.520 |
| Nybøite                   | W(OH,F,Cl) Na      | NaNa <sub>2</sub> (Mg <sub>3</sub> Al <sub>2</sub> )(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>   | 52.22 0.00 18.9                                     | 9 0.00                          | 15.01 0.00  | 11.54 97.76              |                                    | 2.24             | 805   | 0.521 |
| Tremolite                 | W(OH,F,Cl) Ca      | □Ca <sub>2</sub> Mg <sub>5</sub> Si <sub>8</sub> O <sub>22</sub> (OH) <sub>2</sub>  | 59.17 0.00 0.00                                     | 0.00                            | 24.81 13.81 | 0.00 97.78               |                                    | 2.22             | 812   | 0.525 |
| Magnesio-hornblende       | W(OH,F,Cl) Ca      | □Ca <sub>2</sub> (Mg <sub>4</sub> Al)(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>  | 51.67 0.00 12.5                                     | 3 0.00                          | 19.81 13.78 | 0.00 97.79               |                                    | 2.21             | 814   | 0.526 |
| Tschermakite              | W(OH,F,Cl) Ca      | $\Box Ca_2(Mg_3Al_2)(Si_6Al_2)O_{22}(OH)_2$   | 44.21 0.00 25.0                                     |                                 | 14.83 13.75 | 0.00 97.79               |                                    | 2.21             | 815   | 0.527 |
| Richterite                | W(OH,F,Cl) Na-Ca   | Na(NaCa)Mg <sub>5</sub> Si <sub>8</sub> O <sub>22</sub> (OH) <sub>2</sub>   | 58.74 0.00 0.00                                     | 0.00                            | 24.63 6.85  | 7.57 97.80               |                                    | 2.20             | 818   | 0.528 |
| Katophorite               | W(OH,F,Cl) Na-Ca   | Na(NaCa)(Mg <sub>4</sub> Al)(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>   | 51.30 0.00 12.4                                     | 4 0.00                          | 19.66 6.84  | 7.56 97.80               |                                    | 2.20             | 820   | 0.529 |
| Taramite                  | W(OH,F,Cl) Na-Ca   | Na(NaCa)(Mg <sub>3</sub> Al <sub>2</sub> )(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> (OH) <sub>2</sub>   | 43.89 0.00 24.8                                     | 3 0.00                          | 14.72 6.83  | 7.55 97.81               |                                    | 2.19             | 821   | 0.530 |
| Ferri-winchite            | W(OH,F,Cl) Na-Ca   | $\square(NaCa)(Mg_4Fe^{3+})Si_8O_{22}(OH)_2$  | 58.14 0.00 0.00                                     |                                 | 19.50 6.78  | 3.75 96.85               | 9.66 0.00                          | 2.18             | 827   | 0.533 |
| Magnesio-arfvedsonite     | W(OH,F,Cl) Na      | NaNa <sub>2</sub> (Mg <sub>4</sub> Fe <sup>3+</sup> )Si <sub>8</sub> O <sub>22</sub> (OH) <sub>2</sub>  | 57.72 0.00 0.00                                     |                                 | 19.36 0.00  | 11.16 96.88              |                                    | 2.16             | 833   | 0.536 |
| Edenite                   | W(OH,F,Cl) Ca      | NaCa <sub>2</sub> Mg <sub>5</sub> (Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>   | 50.41 0.00 6.11                                     |                                 | 24.16 13.44 |                          |                                    | 2.16             | 834   | 0.537 |
| Pargasite                 | W(OH,F,Cl) Ca      | NaCa <sub>2</sub> (Mg <sub>4</sub> Al)(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> (OH) <sub>2</sub>   | 43.13 0.00 18.3                                     |                                 | 19.29 13.42 |                          |                                    | 2.16             | 836   | 0.538 |
| Sadanagaite               | W(OH,F,Cl) Ca      | NaCa <sub>2</sub> (Mg <sub>3</sub> Al <sub>2</sub> )(Si <sub>5</sub> Al <sub>3</sub> )O <sub>22</sub> (OH) <sub>2</sub>   | 35.88 0.00 30.4                                     |                                 | 14.44 13.39 |                          |                                    | 2.15             | 837   | 0.539 |
| Magnesio-riebeckite       | W(OH,F,Cl) Na      | $\square \text{Na}_2(\text{Mg}_3\text{Fe}^{3+}_2)\text{Si}_8\text{O}_{22}(\text{OH})_2$   | 57.14 0.00 0.00                                     |                                 | 14.37 0.00  | 7.37 95.96               | 18.98 0.00                         |                  | 841   | 0.541 |
| Magnesio-ferri-hornblende | W(OH,F,Cl) Ca      | $\Box Ca_2(Mg_4Fe^{3+})(Si_7Al)O_{22}(OH)_2$  | 49.90 0.00 6.05                                     |                                 | 19.13 13.31 |                          | 9.47 0.00                          | 2.14             | 843   | 0.542 |
| Ferri-katophorite         | W(OH,F,Cl) Na-Ca   | Na(NaCa)(Mg <sub>4</sub> Fe <sup>3+</sup> )(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>  | 49.56 0.00 6.01                                     |                                 |             | 7.30 96.93               |                                    |                  | 849   | 0.545 |
| Cannilloite               | W(OH,F,Cl) Ca      | CaCa <sub>2</sub> (Mg <sub>4</sub> Al)(Si <sub>5</sub> Al <sub>3</sub> )O <sub>22</sub> (OH) <sub>2</sub>   | 35.27 0.00 23.9                                     |                                 | 18.93 19.75 |                          |                                    | 2.11             | 852   | 0.547 |
| Rootname 4                | W(OH,F,Cl) Ca      | NaCa <sub>2</sub> (Mg <sub>4</sub> Ti)(Si <sub>5</sub> Al <sub>3</sub> )O <sub>22</sub> (OH) <sub>2</sub>   | 35.11 9.33 17.8                                     |                                 | 18.84 13.11 |                          |                                    | 2.11             | 856   | 0.549 |
| Kaersutite                | w <sub>O</sub> -   | NaCa <sub>2</sub> (Mg <sub>3</sub> TiAl)(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> O <sub>2</sub>  | 42.05 9.32 17.8                                     |                                 | 14.10 13.08 |                          | 0                                  | 0.00             | 857   | 0.552 |
| Ferri-barroisite          | W(OH,F,Cl) Na-Ca   | Na(NaCa)(Mg <sub>3</sub> Fe <sup>3+</sup> 2)(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>   | 49.06 0.00 5.95                                     |                                 | 14.10 6.54  | 3.61 96.03               |                                    | 2.10             | 857   | 0.550 |
| Ferri-nybøite             | W(OH,F,Cl) Na      | NaNa <sub>2</sub> (Mg <sub>3</sub> Fe <sup>3+</sup> <sub>2</sub> )(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>   | 48.73 0.00 5.91                                     |                                 | 14.01 0.00  | 10.77 96.06              |                                    | 2.09             | 863   | 0.553 |
| Magnesio-hastingsite      | W(OH,F,Cl) Ca      | $NaCa_2(Mg_4Fe^{3+})(Si_6Al_2)O_{22}(OH)_2$   | 41.69 0.00 11.7                                     |                                 | 18.64 12.97 |                          |                                    | 2.08             | 865   | 0.554 |
| Ferri-tschermakite        | W(OH,F,Cl) Ca      | $\Box Ca_2(Mg_3Fe^{3+}_2)(Si_6Al_2)O_{22}(OH)_2$  | 41.28 0.00 11.6                                     |                                 | 13.85 12.84 |                          |                                    |                  | 873   | 0.558 |
| Ferro-glaucophane         | W(OH,F,Cl) Na      | $\square \text{Na}_2(\text{Fe}^{2+}_3\text{Al}_2)\text{Si}_8\text{O}_{22}(\text{OH})_2$   | 54.74 0.00 11.6                                     |                                 | 0.00 0.00   | 7.06 97.95               |                                    | 4 2.05           | 878   | 0.560 |
| Ferri-taramite            | W(OH,F,Cl) Na-Ca   | Na(NaCa)(Mg <sub>3</sub> Fe3+ <sub>2</sub> )(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> (OH) <sub>2</sub>   | 41.01 0.00 11.6                                     |                                 | 13.75 6.38  | 7.05 96.13               | 18.16 0.00                         |                  | 879   | 0.561 |
| Ferri-cannilloite         | W(OH,F,Cl) Ca      | $CaCa_2(Mg_4Fe^{3+})(Si_5Al_3)O_{22}(OH)_2$   | 34.11 0.00 17.3                                     |                                 | 18.31 19.10 |                          |                                    |                  | 881   | 0.562 |
| Ferri-kaersutite          | w <sub>O</sub> -   | NaCa <sub>2</sub> (Mg <sub>3</sub> TiFe <sup>3+</sup> )(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> O <sub>2</sub>   | 40.68 9.01 11.5                                     |                                 | 13.64 12.66 |                          |                                    |                  | 886   | 0.567 |
| Ferro-barroisite          | W(OH,F,Cl) Na-Ca   | $\square(\text{NaCa})(\text{Fe}^{2+}_{3}\text{Al}_{2})(\text{Si}_{7}\text{Al})\text{O}_{22}(\text{OH})_{2}$   |   | 0 24.11                         | 0.00 6.27   | 3.47 97.99               |                                    | 1 2.01           | 894   | 0.568 |
| Ferri-sadanagaite         | W(OH,F,Cl) Ca      | NaCa <sub>2</sub> (Mg <sub>3</sub> Fe <sup>3+</sup> <sub>2</sub> )(Si <sub>5</sub> Al <sub>3</sub> )O <sub>22</sub> (OH) <sub>2</sub>   |   | 9 16.05                         | 13.51 12.53 |                          |                                    |                  | 895   | 0.569 |
| Ferro-nybøite             | W(OH,F,Cl) Na      | NaNa <sub>2</sub> (Fe <sup>2+</sup> <sub>3</sub> Ab <sub>2</sub> )(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>   | 46.73 0.00 16.9                                     |                                 | 0.00 0.00   | 10.33 98.00              |                                    | 5 2.00           | 900   | 0.571 |
| oxo Ferro-tschermakite    | WO Ca              | $\Box \text{Ca}_{2}(\text{Fe}^{2+}\text{Fe}^{3+}_{2}\text{Al}_{2})(\text{Si}_{6}\text{Al}_{2})\text{O}_{22}\text{O}_{2}$  | 39.70 0.00 22.4                                     |                                 |             | 0.00 98.24               |                                    |                  | 908   | 0.577 |
| Ferro-tschermakite        | W(OH,F,Cl) Ca      | $\Box Ca_2(Fe^{2+}_3Al_2)(Si_6Al_2)O_{22}(OH)_2$  | 39.61 0.00 22.4                                     |                                 |             | 0.00 98.02               |                                    | 8 1.98           | 910   | 0.576 |
| Ferro-taramite            | W(OH,F,Cl) Na-Ca   | $Na(NaCa)(Fe^{2+}_{3}Al_{2})(Si_{6}Al_{2})O_{22}(OH)_{2}$   | 39.35 0.00 22.2                                     |                                 |             | 6.77 98.03               |                                    | 3 1.97           | 916   | 0.579 |
| Ferro-winchite            | W(OH,F,Cl) Na-Ca   | □(NaCa)(Fe2+4Al)Si8O22(OH)2   | 52.01 0.00 5.52                                     |                                 | 0.00 6.07   | 3.35 98.05               |                                    | 1.95             | 924   | 0.582 |
| oxo Ferro-sadanagaite     | WO Ca              | $NaCa_2(Fe^{2+}Fe^{3+}_2Al_2)(Si_5Al_3)O_{22}O_2$   | 32.30 0.00 27.4                                     |                                 |             | 3.33 98.28               |                                    |                  | 930   | 0.587 |
| Ferro-eckermannite        | W(OH,F,Cl) Na      | NaNa <sub>2</sub> (Fe <sup>2+</sup> <sub>4</sub> Al)Si <sub>8</sub> O <sub>22</sub> (OH) <sub>2</sub>   | 51.68 0.00 5.48                                     |                                 |             | 10.00 98.06              |                                    | 1.94             | 930   | 0.585 |
| Ferro-sadanagaite         | W(OH,F,Cl) Ca      | $NaCa_2(Fe^{2+}_3Al_2)(Si_5Al_3)O_{22}(OH)_2$   | 32.23 0.00 27.3                                     |                                 |             | 3.33 98.07               |                                    | 3 1.93           | 932   | 0.586 |
| Riebeckite                | W(OH,F,Cl) Na      | $\square \text{Na}_2(\text{Fe}^{2+}_{3}\text{Fe}^{3+}_{2})\text{Si}_8\text{O}_{22}(\text{OH})_2$  | 51.36 0.00 0.00                                     |                                 |             | 6.62 96.37               |                                    |                  | 936   | 0.588 |
| oxo Ferro-hornblende      | WO Ca              | $\Box \text{Ca}_2(\text{Fe}^{2+}_{3}\text{Fe}^{3+}_{2}\text{Al})(\text{Si}_7\text{Al})\text{O}_{22}\text{O}_2$  | 44.83 0.00 10.8                                     |                                 |             | 0.02 98.29               |                                    |                  | 938   | 0.591 |
| Ferro-hornblende          | W(OH,F,Cl) Ca      | $\Box Ca_2(Fe^{2+}_{4}Al)(Si_7Al)O_{22}(OH)_2$  | 44.74 0.00 10.8                                     |                                 |             |                          |                                    | 7 1.92           |       | 0.589 |
| Ferro-katophorite         | W(OH,F,Cl) Na-Ca   | Na(NaCa)(Fe <sup>2+</sup> <sub>4</sub> Al)(Si <sub>7</sub> Al)O <sub>22</sub> (OH) <sub>2</sub>   | 44.46 0.00 10.7                                     |                                 |             | 6.55 98.10               |                                    | 8 1.90           | 946   |       |
| Ferro-ferri-barroisite    | W(OH,F,Cl) Na-Ca   | $\square(\text{NaCa})(\text{Fe}^{2+}_{4}\text{Fe}^{3+}_{2})(\text{Si}_{7}\text{Al})\text{O}_{22}(\text{OH})_{2}$  | 44.19 0.00 5.36                                     |                                 |             |                          |                                    |                  | 952   |       |
| Ferro-kaersutite          | WO -               | NaCa <sub>2</sub> (Fe <sup>2+</sup> <sub>3</sub> TiAl)(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> O <sub>2</sub>  | 37.87 8.39 16.0                                     |                                 |             |                          |                                    | 4 0.00           |       | 0.597 |
| Ferro-ferri-winchite      | W(OH,F,Cl) Na-Ca   | $\square(\text{NaCa}_2(\text{Fe}^{-3}\text{HA})(\text{Si}_6\text{Ai}_2)\text{O}_{22}\text{O}_2)$<br>$\square(\text{NaCa})(\text{Fe}^{2+}_4\text{Fe}^{3+})\text{Si}_8\text{O}_{22}(\text{OH})_2$ | 50.44 0.00 0.00                                     |                                 |             |                          |                                    | 5 1.89           | 953   |       |
| Ferro-ferri-nybøite       | W(OH,F,Cl) Na      | NaNa2(Fe2+3Fe3+2)(Si7Al)O22(OH)2  | 43.91 0.00 5.32                                     |                                 |             | 9.71 96.45               |                                    | 0 1.88           | 958   | 0.597 |
| Arfvedsonite              | W(OH,F,Cl) Na      | NaNa <sub>2</sub> (Fe <sup>2+</sup> <sub>4</sub> Fe <sup>3+</sup> )Si <sub>8</sub> O <sub>22</sub> (OH) <sub>2</sub>  | 50.13 0.00 0.00                                     |                                 |             | 9.71 90.43               |                                    | 7 1.88           | 959   |       |
| oxo Ferro-pargasite       | WO Ca              | NaCa <sub>2</sub> (Fe <sup>2+</sup> <sub>2</sub> Fe <sup>3+</sup> <sub>2</sub> Al)(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> O <sub>2</sub>  | 37.55 0.00 15.9                                     |                                 |             | 3.23 98.33               |                                    |                  | 960   |       |
| Ferro-pargasite           | W(OH,F,Cl) Ca      | NaCa <sub>2</sub> (Fe <sup>2+</sup> <sub>4</sub> Al)(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> (OH) <sub>2</sub>   | 37.47 0.00 15.9                                     |                                 |             | 3.23 98.33<br>3.22 98.13 |                                    | 7 1.87           | 962   |       |
| 1 ciro purgusac           | (,-,, Ca           |   | J1.71 0.00 1J.7                                     | · 27.07                         | J.00 11.00  | . J.22 70.13             | 0.00 27.0                          | , 1.07           | 702   | 3.377 |

Table 2. Continue.

| Name                         | Group          | Sub-group | Formula   | SiO <sub>2</sub> Ti | O <sub>2</sub> Al <sub>2</sub> | O <sub>3</sub> FeC | o <sub>tot</sub> MgO | CaO   | Na <sub>2</sub> O | Sum   | Fe <sub>2</sub> O <sub>3</sub> | FeO   | H <sub>2</sub> O | M <sub>r</sub> | cmpg  |
|------------------------------|----------------|-----------|---|---------------------|--------------------------------|--------------------|----------------------|-------|-------------------|-------|--------------------------------|-------|------------------|----------------|-------|
| oxo Ferro-ferri-hornblende   | w <sub>O</sub> | Ca        | $\Box Ca_{2}(Fe^{2+}_{2}Fe^{3+}_{3})(Si_{7}Al)O_{22}O_{2}$  | 43.50 0.0           | 00 5.2                         | 27 37.             | 15 0.00              | 11.60 | 0.00              | 97.52 | 24.77                          | 14.86 | 0.00             | 967            | 0.603 |
| oxo Ferro-cannilloite        | $^{W}O$        | Ca        | $CaCa_{2}(Fe^{2+}_{2}Fe^{3+}_{2}Al)(Si_{5}Al_{3})O_{22}O_{2}$   | 30.78 0.            | 00 20                          | .89 29.4           | 15 0.00              | 17.24 | 0.00              | 98.36 | 16.36                          | 14.72 | 0.00             | 976            | 0.607 |
| oxo Ferro-ferri-tschermakite | w <sub>O</sub> | Ca        | $\Box Ca_{2}(Fe^{2+}Fe^{3+}_{4})(Si_{6}Al_{2})O_{22}O_{2}$  | 37.33 0.0           | 00 10                          | .56 37.            | 0.00                 | 11.61 | 0.00              | 96.69 | 33.07                          | 7.44  | 0.00             | 966            | 0.602 |
| Ferro-ferri-tschermakite     | W(OH,F,Cl)     | Ca        | $\Box Ca_{2}(Fe^{2+}{}_{3}Fe^{3+}{}_{2})(Si_{6}Al_{2})O_{22}(OH)_{2}$   | 37.25 0.            | 00 10                          | .53 37.            | 0.00                 | 11.59 | 0.00              | 96.49 | 16.50                          | 22.27 | 1.86             | 968            | 0.601 |
| oxo Ferro-actinolite         | $^{W}O$        | Ca        | $\Box Ca_{2}(Fe^{2+}{}_{3}Fe^{3+}{}_{2})Si_{8}O_{22}O_{2}$  | 49.65 0.            | 0.0                            | 00 37.             | 1 0.00               | 11.59 | 0.00              | 98.35 | 16.50                          | 22.26 | 0.00             | 968            | 0.603 |
| Ferro-ferri-hornblende       | W(OH,F,Cl)     | Ca        | $\Box Ca_{2}(Fe_{4}^{2+}Fe_{4}^{3+})(Si_{7}Al)O_{22}(OH)_{2}$   | 43.41 0.            | 00 5.2                         | 26 37.0            | 0.00                 | 11.57 | 0.00              | 97.32 | 8.24                           | 29.66 | 1.86             | 969            | 0.602 |
| Ferro-actinolite             | W(OH,F,Cl)     | Ca        | $\Box Ca_{2}Fe^{2+}{}_{5}Si_{8}O_{22}(OH)_{2}$  | 49.55 0.0           | 0.0                            | 00 37.0            | 0.00                 | 11.56 | 0.00              | 98.14 | 0.00                           | 37.03 | 1.86             | 970            | 0.602 |
| Ferro-ferri-taramite         | W(OH,F,Cl)     | Na-Ca     | Na(NaCa)(Fe <sup>2+</sup> <sub>3</sub> Fe <sup>3+</sup> <sub>2</sub> )(Si <sub>6</sub> Al <sub>2</sub> )O <sub>22</sub> (OH) <sub>2</sub> | 37.02 0.0           | 00 10                          | .47 36.8           | 39 0.00              | 5.76  | 6.36              | 96.51 | 16.40                          | 22.13 | 1.85             | 974            | 0.604 |
| Ferro-ferri-katophorite      | W(OH,F,Cl)     | Na-Ca     | Na(NaCa)(Fe2+4Fe3+)(Si7Al)O22(OH)2  | 43.14 0.0           | 00 5.2                         | 23 36.8            | 35 0.00              | 5.75  | 6.36              | 97.33 | 8.19                           | 29.48 | 1.85             | 975            | 0.604 |
| Ferro-richterite             | W(OH,F,Cl)     | Na-Ca     | Na(NaCa)Fe <sup>2+</sup> <sub>5</sub> Si8O <sub>22</sub> (OH) <sub>2</sub>  | 49.25 0.            | 0.0                            | 00 36.8            | 31 0.00              | 5.75  | 6.35              | 98.15 | 0.00                           | 36.81 | 1.85             | 976            | 0.604 |
| Ferro-cannilloite            | W(OH,F,Cl)     | Ca        | $CaCa_{2}(Fe^{2+}_{4}Al)(Si_{5}Al_{3})O_{22}(OH)_{2}$   | 30.72 0.            | 00 20                          | .85 29.3           | 9 0.00               | 17.20 | 0.00              | 98.16 | 0.00                           | 29.39 | 1.84             | 978            | 0.605 |
| oxo Ferro-rootname 4         | $^{W}O$        | Ca        | $NaCa_{2}(Fe^{2+}_{2}Fe^{3+}_{2}Ti)(Si_{5}Al_{3})O_{22}O_{2}$   | 30.66 8.            | 15 15                          | .61 29.3           | 3 0.00               | 11.45 | 3.16              | 98.37 | 16.30                          | 14.67 | 0.00             | 980            | 0.608 |
| Ferro-ferri-kaersutite       | w <sub>O</sub> | -         | $NaCa_{2}(Fe^{2+}_{3}TiFe^{3+})(Si_{6}Al_{2})O_{22}O_{2}$   | 36.75 8.            | 14 10                          | .40 29.3           | 0.00                 | 11.43 | 3.16              | 99.18 | 8.14                           | 21.97 | 0.00             | 981            | 0.609 |
| Ferro-rootname 4             | W(OH,F,Cl)     | Ca        | $NaCa_{2}(Fe^{2+}_{4}Ti)(Si_{5}Al_{3})O_{22}(OH)_{2}$   | 30.60 8.            | 13 15                          | .58 29.2           | 27 0.00              | 11.42 | 3.16              | 98.17 | 0.00                           | 29.27 | 1.83             | 982            | 0.607 |
| oxo Ferro-ferri-sadanagaite  | $^{W}O$        | Ca        | $NaCa_{2}(Fe^{2+}Fe^{3+}_{4})(Si_{5}Al_{3})O_{22}O_{2}$   | 30.42 0.            | 00 15                          | .48 36.3           | 37 0.00              | 11.35 | 3.14              | 96.76 | 32.33                          | 7.27  | 0.00             | 988            | 0.611 |
| oxo Hastingsite              | $^{W}O$        | Ca        | $NaCa_{2}(Fe^{2+}_{2}Fe^{3+}_{3})(Si_{6}Al_{2})O_{22}O_{2}$   | 36.46 0.            | 00 10                          | .31 36.3           | 3 0.00               | 11.34 | 3.13              | 97.57 | 24.22                          | 14.53 | 0.00             | 989            | 0.612 |
| Ferro-ferri-sadanagaite      | W(OH,F,Cl)     | Ca        | $NaCa_{2}(Fe^{2+}_{3}Fe^{3+}_{2})(Si_{5}Al_{3})O_{22}(OH)_{2}$  | 30.35 0.            | 00 15                          | .45 36.2           | 29 0.00              | 11.33 | 3.13              | 96.56 | 16.13                          | 21.78 | 1.82             | 990            | 0.610 |
| oxo Ferro-edenite            | $^{W}O$        | Ca        | $NaCa_{2}(Fe^{2+}_{3}Fe^{3+}_{2})(Si_{7}Al)O_{22}O_{2}$   | 42.49 0.            | 00 5.1                         | 5 36.2             | 29 0.00              | 11.33 | 3.13              | 98.38 | 16.13                          | 21.77 | 0.00             | 990            | 0.612 |
| Hastingsite                  | W(OH,F,Cl)     | Ca        | $NaCa_{2}(Fe^{2+}_{4}Fe^{3+})(Si_{6}Al_{2})O_{22}(OH)_{2}$  | 36.38 0.            | 00 10                          | .29 36.2           | 25 0.00              | 11.32 | 3.13              | 97.37 | 8.06                           | 29.00 | 1.82             | 991            | 0.610 |
| Ferro-edenite                | W(OH,F,Cl)     | Ca        | $NaCa_{2}Fe^{2+}_{5}(Si_{7}Al)O_{22}(OH)_{2}$   | 42.40 0.            | 00 5.1                         | 4 36.2             | 21 0.00              | 11.31 | 3.12              | 98.18 | 0.00                           | 36.21 | 1.82             | 992            | 0.611 |
| Grunerite                    | W(OH,F,Cl)     | Mg-Fe-Mn  | $\Box Fe_{2}^{2+}Fe_{5}^{2+}Si_{8}O_{22}(OH)_{2}$   | 47.99 0.0           | 0.0                            | 00 50.2            | 21 0.00              | 0.00  | 0.00              | 98.20 | 0.00                           | 50.21 | 1.80             | 1002           | 0.615 |
| oxo Ferro-ferri-cannilloite  | $^{W}O$        | Ca        | $CaCa_{2}(Fe^{2+}_{2}Fe^{3+}_{3})(Si_{5}Al_{3})O_{22}O_{2}$   | 29.90 0.            | 00 15                          | .22 35.7           | 75 0.00              | 16.74 | 0.00              | 97.61 | 23.84                          | 14.30 | 0.00             | 1005           | 0.618 |
| Ferro-ferri-cannilloite      | W(OH,F,Cl)     | Ca        | $CaCa_{2}(Fe^{2+}_{4}Fe^{3+})(Si_{5}Al_{3})O_{22}(OH)_{2}$  | 29.84 0.            | 00 15                          | .19 35.0           | 68 0.00              | 16.71 | 0.00              | 97.42 | 7.93                           | 28.54 | 1.79             | 1007           | 0.617 |

Table 3.

| Amphibole                   | Calibration high        |                              | Test lower-quality data $N = 51$ |           |  |  |  |
|-----------------------------|-------------------------|------------------------------|----------------------------------|-----------|--|--|--|
| parameter                   | $\sigma_{\mathrm{est}}$ | $\sigma_{\rm est}$ max error |                                  | max error |  |  |  |
| $^{\mathrm{T}}\mathrm{Si}$  | 0.017                   | 0.068                        | 0.026                            | 0.081     |  |  |  |
| Ti                          | 0.002                   | 0.008                        | 0.002                            | 0.006     |  |  |  |
| $Al_{tot}$                  | 0.006                   | 0.018                        | 0.021                            | 0.077     |  |  |  |
| Fe <sub>tot</sub>           | 0.007                   | 0.045                        | 0.024                            | 0.121     |  |  |  |
| Mg                          | 0.008                   | 0.028                        | 0.015                            | 0.045     |  |  |  |
| Ca                          | 0.005                   | 0.019                        | 0.005                            | 0.016     |  |  |  |
| Na                          | 0.003                   | 0.010                        | 0.006                            | 0.035     |  |  |  |
| K                           | 0.002                   | 0.007                        | 0.002                            | 0.005     |  |  |  |
| F                           | 0.004                   | 0.016                        | 0.013                            | 0.060     |  |  |  |
| <sup>C</sup> Ti             | 0.012 (0.017)           | 0.087                        | 0.007 (0.026)                    | 0.039     |  |  |  |
| <sup>C</sup> Al             | 0.019 (0.018)           | 0.065                        | 0.023 (0.034)                    | 0.066     |  |  |  |
| $\Delta C$                  | 0.035 (0.021)           | 0.140                        | 0.035 (0.044)                    | 0.101     |  |  |  |
| <sup>B</sup> Na             | 0.036 (0.022)           | 0.159                        | 0.036 (0.044)                    | 0.095     |  |  |  |
| $^{A}(Ca + Na + K)$         | 0.042 (0.022)           | 0.168                        | 0.044 (0.045)                    | 0.124     |  |  |  |
| Fe <sup>3+</sup> , default* | 0.100 (0.126)           | 0.373                        | 0.151 (0.169)                    | 0.620     |  |  |  |
| Fe <sup>3+</sup> , optional | 0.303 (0.248)           | 1.104                        | 0.361 (0.419)                    | 1.001     |  |  |  |
| $\Delta MM\%$               | 0.18                    | 0.74                         | 0.29                             | 0.87      |  |  |  |

N: sample number;  $\sigma_{\text{est}}$ : standard error of the estimate; max error: maximum error;

<sup>\*:</sup> N = 87 and 40 for calibration quality and test data (only amphiboles with  ${}^WO^{2-} \le 2^CTi$ ); brackets report errors due to the uncertainty propagation in the calculation of the parameters.