

1 **The effects of shear deformation on planetesimal core segregation: Results from in-situ X-**  
2 **ray micro-tomography**

3 **REVISION 1**

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9  
10 **Abstract**

11 It is well accepted that the Earth formed by the accretion and collision of small (10-  
12 100km), rocky bodies called planetesimals. W-Hf isotopic evidence from meteorites suggest that  
13 the cores of many planetesimals formed within a relatively short time frame of ~3 My. While a  
14 very hot, deep magma ocean is generally thought to have been the driving mechanism for core  
15 formation in large planetary bodies, it inadequately explains differentiation and core formation in  
16 small planetesimals due to temperatures potentially being insufficient for wide-scale silicate  
17 melting to occur. In order for these planetesimals to differentiate within such a relatively short  
18 time without a magma ocean, a critical melt volume of the metallic (core-forming) phase and  
19 sufficient melt connectivity and grain size must have existed in order to attain the required  
20 permeability and lead to efficient core formation. Shear deformation may increase the  
21 connectedness of melt and the permeability, and thus could have been a major contributing factor  
22 in the formation of planetesimal cores. This deformation may have been caused by large impacts  
23 and collisions experienced by the planetesimals in the early solar system. The purpose of this  
24 work is to test the hypothesis that shear deformation enhances the connectivity and permeability  
25 of Fe-S melt within a solid silicate (olivine) matrix, such that rapid core formation is plausible. A  
26 rotational Drickamer apparatus (RDA) was used to heat and torsionally deform a sample of solid  
27 olivine + FeS liquid through six steps of large-strain shear deformation. After each deformation  
28 step, X-ray microtomographs were collected in the RDA to obtain *in-situ* 3-dimensional images  
29 of the sample. The resulting digital volumes were processed and permeability simulations  
30 utilizing the lattice Boltzmann method were performed to determine the effect of shear  
31 deformation on connectivity and permeability within the sample. The resulting permeabilities of  
32 the sample at various steps of deformation are the same within uncertainty and do not exhibit a  
33 change with increasing deformation. Additionally, the migration velocity calculated from the  
34 permeability of the sample is not high enough for segregation to take place within the time frame  
35 of ~3 My. In addition to further constraining the mechanism of core formation in planetesimals,  
36 the image processing techniques developed in this study will be of great benefit to future studies  
37 utilizing similar methods.

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## Introduction

42 Core formation is a significant, yet not completely understood process in the formation of

43 the terrestrial planets and other small, rocky bodies such as large asteroids and satellites.

44 Hafnium-Tungsten isotopic studies of the Earth's mantle and several meteorites indicate that the

45 Earth's core likely formed in ~30-100 My after the formation of the proto-earth, while the parent

46 bodies of iron meteorites differentiated much faster (~1-5 My) (Kleine et al., 2002; Scherstén et

47 al., 2006; Rubie et al., 2007; Burkhardt et al., 2008; Kleine et al., 2009), and perhaps even before

48 1 My (Kruijer et al. 2014). This short timescale of 1-5 My for core formation is in agreement

49 with the theoretical model that accretion in the early solar system took place relatively rapidly

50 (Alexander et al., 2001; Wood et al., 2006; Rubie et al., 2007). The mechanism by which core

51 formation took place in planetesimals is largely dependent upon the thermal history of the body

52 (Rubie et al., 2007). Heat generated from  $^{26}\text{Al}$  decay would have melted the core forming alloy

53 in planetesimals 10-100 km in diameter (Yoshino et al., 2003; Walter and Tronnes, 2004;

54 Bizzarro et al., 2005), but may not have melted the silicate to a significant degree. In the absence

55 of widespread silicate melting, the mechanism by which metal and silicate might have segregated

56 in planetsimals is limited to inter-granular percolation of metallic melt through a solid silicate

57 matrix (Yoshino et al., 2003; Watson and Roberts, 2011).

58 In order for core formation to take place efficiently in an equilibrium setting, the metallic

59 melt must be fully connected within the solid silicate (e.g. Roberts et al., 2007; Watson and

60 Roberts, 2011). Whether or not connectivity is achieved depends on the dihedral (wetting) angle

61 between the liquid and solid grains (von Bagen and Waff, 1986). The dihedral angle ( $\theta$ ) can be

62 expressed as:

63 
$$\frac{\gamma_{ss}}{2\gamma_{sl}} = \cos\left(\frac{\theta}{2}\right)$$

64

65 where  $\gamma_{ss}$  and  $\gamma_{sl}$  refer to the solid-solid and the solid-liquid interfacial energies, respectively  
66 (Bulau and Waff, 1979). A dihedral angle less than  $60^\circ$  leads to a fully interconnected melt  
67 network in which percolation is possible even at extremely small melt volumes; while a dihedral  
68 angle greater than  $60^\circ$  results in isolated pockets of melt and inefficient core formation, unless a  
69 critical volume of melt is present. This critical volume of melt is known as the connectivity  
70 threshold and increases with increasing dihedral angle (von Bargen and Waff, 1986).

71 Experiments performed at conditions relevant to the interiors of planetesimals ( $\sim 1$ -3 GPa)  
72 have determined that for the sulfide/metal melt-solid silicate system the dihedral angle is greater  
73 than  $60^\circ$  (e.g. Ballhaus and Ellis, 1996; Shannon and Agee, 1996; Gaetani and Grove, 1999;  
74 Holzheid et al., 2000; Takafuji et al., 2004; Walte et al., 2007), with an average angle of  $90^\circ \pm 5^\circ$ .  
75 At a dihedral angle greater than  $60^\circ$ , the melt within planetesimals would only have percolated to  
76 the core until the pinch-off threshold was reached, below which the remaining melt would have  
77 become stranded in the solid silicate matrix (von Bargen and Waff, 1986). The pinch-off  
78 threshold, determined to be between 3 and 6 vol% (Yoshino et al., 2003; Roberts et al., 2007;  
79 Watson and Roberts, 2011), is slightly below the percolation threshold. Therefore, being able to  
80 quantify the critical volume of melt (percolation threshold) required in order to maintain  
81 percolative flow becomes essential in understanding the processes that contributed to rapid,  
82 efficient core formation in planetesimals (Watson and Roberts, 2011).

83 Estimates of the connectivity threshold in the olivine + FeS system range from  $\sim 4$  to  
84  $\sim 17\%$ , (Yoshino et al., 2003; Terasaki et al., 2008; Bagdassarov et al., 2009a, 2009b; Watson

85 and Roberts, 2011) with most accepted values being around 5 vol%. Although we don't have  
86 many meteorite samples of differentiated mantle materials, it is commonly thought that it is  
87 unlikely for 5vol% of metal to remain in the mantle. If we assume that core formation efficiently  
88 removes most core material from the mantle, an alternative segregation mechanism is required in  
89 order to lead to efficient core formation. For conditions within planetesimals, deformation  
90 caused by large impacts, and possibly convection, has been suggested as a mechanism that may  
91 have aided in the enhanced permeability and thus the segregation of the remaining melt (Bruhn  
92 et al., 2000; Rushmer et al., 2005; Groebner and Kohlstedt, 2006; Hustoft and Kohlstedt, 2006).  
93 This manner of efficient core formation via deformation would preclude the necessity of  
94 widespread silicate melting (i.e. a magma ocean), particularly in smaller planetesimals that may  
95 have never reached high enough temperatures.

96 Experiments performed on samples of varying compositions and melt volumes indicate  
97 that shear deformation can lead to the enhanced segregation of metallic melt from a solid silicate  
98 matrix (Bruhn et al., 2000; Rushmer et al., 2005; Groebner and Kohlstedt, 2006; Hustoft and  
99 Kohlstedt, 2006). Deformation induced on these samples had varying outcomes, including: the  
100 enhanced interconnection of melt pockets at 4 and 7 vol% sulfide melt (Bruhn et al., 2000) the  
101 migration of melt within a solid silicate matrix (Rushmer et al., 2005; 20-25 vol%), the formation  
102 of a strong melt-preferred orientation of previously isolated melt pockets (Groebner and  
103 Kohlstedt, 2006; 4 vol%), and evidence of grain boundary percolation down to a pinch-off  
104 threshold of ~1 vol% (Hustoft and Kohlstedt, 2006; 3, 5, and 9 vol%). The results of these  
105 experiments support the idea that shear deformation may lead to the more efficient segregation of  
106 metallic melt from a solid silicate matrix at melt volumes close to and above 5 vol%. The main  
107 differences between this previous work and the present study are (1) Some previous studies

108 looked at melt volumes that were already significantly connected (i.e. Rushmer et al. 2005), (2)  
109 In some cases, the experiments were performed at lower pressure (300MPa) and strain rates up to  
110 2 orders of magnitude higher than those here (e.g. Groebner and Kohlstedt, 2006, Hustoft and  
111 Kohlstedt, 2006) and (3) The only other 3-D study (Bruhn et al. 2000) is on a relatively small  
112 volume (~35mm x 35mm x 25mm) that may not be fully representative of connectivity and  
113 permeability of the whole sample. Recent work by Walte et al. (2011) suggests that the behavior  
114 of metallic melt in similar systems (olivine + FeS or Au) is dominated by surface energy at low  
115 strain rates and actually may inhibit elongation of melt particles, and that melt may become  
116 concentrated into larger melt pockets.

117 The objective of the present study is to observe the effect of shear deformation on the  
118 permeability of an olivine + FeS sample that is close to the pinch-off threshold of ~3-6 vol%  
119 melt. Previous studies have relied upon methods, such as electrical conductivity (e.g. Yoshino,  
120 2003, 2004), and using theoretical models based on 2-D images of melt geometry (e.g. Hustoft  
121 and Kohlstedt, 2006) that indirectly measure permeability by constraining the connection  
122 threshold. Recently, synchrotron based X-ray micro-tomography (3D) analysis of quenched  
123 samples (Shi et al. 2013) and quenched samples coupled with numerical simulations on both the  
124 olivine-basalt system (Zhu et al. 2011, Miller et al. 2014) and the olivine Fe-S system (Watson  
125 and Roberts 2011, have demonstrated that X-ray tomography is a useful tool in determining the  
126 permeability and melt geometry in a more direct way than previous methods. 2-D X-ray  
127 radiography at high pressure and temperature has recently been employed to observe the  
128 segregation process in-situ (Gotou et al. 2015). Here, we combine the advantages of each of  
129 these techniques. By using *in-situ* high pressure X-ray micro-tomography (HP-XMT) coupled  
130 with numerical simulations to monitor the evolution of the same sample as it is undergoing

131 heating and deformation we evaluate the effect of deformation on the core segregation process.

132

## 133 **Experimental Methods**

### 134 **Sample Synthesis and High Pressure X-ray Microtomography**

135 Starting materials consisted of optically clear San Carlos olivine crystals  
136 ( $[\text{MgO}_{0.91}\text{Fe}_{0.09}]_2\text{SiO}_4$ ) and troilite powder (FeS). After grinding under ethanol using an agate  
137 mortar and pestle, the olivine was sieved to a grain size of 37-74 micrometers. Pure, powdered  
138 FeS (Alfa Aesar) was added to the dried olivine to comprise 4.5 vol% and the mixture was mixed  
139 again under ethanol further to ensure uniformity. The olivine and FeS mixture was packed into a  
140 graphite capsule and sintered in a piston-cylinder apparatus at RPI for 20 hours at 1 GPa and  
141 1250°C. The sample synthesis assembly is shown in Figure 1a. Previous work indicates that  
142 these conditions allow the sample to attain close to complete textural equilibrium (e.g. Gaetani  
143 and Grove, 1999; Yoshino et al., 2003; Roberts et al., 2007; Watson et al., 2010). Once retrieved,  
144 the sintered sample was shaped with a diamond file into several 1x1 mm cylinders and prepared  
145 for high-pressure deformation and imaging experiments. Filing also served to remove the thin  
146 coating of graphite around the edge of the sintered samples.

147 The quenched and equilibrated sample was brought to the Advanced Photon Source (APS)  
148 at Argonne National Laboratory for *in-situ* deformation and tomographic imaging at Sector 13  
149 (GeoSoilEnviroCARS; GSECARS), Beamline 13-BM-D). The sample assembly used in the  
150 Drickamer cell at APS is shown in Figure 1(b). The details of the experimental set-up available  
151 for high pressure X-ray tomography microscopy (HPXTM) are described by Wang (2005) and  
152 Wang et al. (2011). Due to the large X-ray absorption contrast between the olivine and FeS  
153 metal, the two materials can be easily distinguished in the resulting tomographic images at a

154 photon energy of 37 keV (Wang et al., 2011). A major advantage of using HPXTM is that the  
155 sample can be imaged *in-situ* at high pressure and temperature, and so the *evolution* of one  
156 sample can be recorded and observed over time.

157 Tomographic image collection was performed using a 4-inch tube with a 5x objective  
158 lens, resulting in a pixel size of 2  $\mu\text{m}$ . The exposure time was 25 seconds per frame. White field  
159 images were collected before and after each set of tomography images in order to remove  
160 artifacts. The large Si (111) Bragg-Bragg monochromator allows easy switching between  
161 monochromatic and white radiation in seconds (see Wang et al., 2011). Sample pressure was  
162 monitored by energy-dispersive X-ray diffraction of the MgO pressure standard in the sample  
163 assembly and was maintained at 10 tons ( $\sim 1.5\text{GPa} \pm 0.5\text{GPa}$ ) during the experiment (Speziale et  
164 al. 2001). Temperature was estimated through the use of a power curve calibrated at GSECARS  
165 for this experimental assembly. Temperatures were  $1100^\circ\text{C} \pm 100^\circ\text{C}$  during the deformation  
166 process and lowered to  $\sim 850^\circ\text{C}$  during tomographic image collection. Shear strain was applied  
167 to the sample by rotating the upper and lower tungsten carbide anvils at constant speed in  
168 opposite directions, each at  $90^\circ$  steps (**Figure 2**), for a total of  $180^\circ$  of twist. Each step of  
169 deformation lasted for approximately 1.25 hours. Using the total angular rotation ( $840^\circ$ ) and the  
170 total duration of the experiment (6.25 hours), a maximum apparent shear strain rate of  $7.70\text{E-}5\text{ s}^{-1}$   
171 was obtained. However, this is only a rough estimate of the strain rate experienced by the outer  
172 diameter of the sample and is considered an upper bound due to slippage that occurs between the  
173 rotating anvils and the sample during torsion. This strain rate is lower than that reported by  
174 previous workers on a similar system (e.g. Groebner and Kohlstedt, 2006, Hustoft and Kohlstedt,  
175 2006), where strain rates varied from  $10^{-2}$  to  $10^{-4}$ . Walte et al. 2011 report similar strain rates to  
176 our reported maximum ( $7 \times 10^{-6} - 1 \times 10^{-4}$ ).

177 **Electron Microprobe Analysis**

178 Backscattered electron (BSE) imaging, secondary electron (SE) imaging, and  
179 wavelength-dispersive spectroscopy (WDS) were conducted on both an undeformed sample of  
180 the starting material and the deformed sample using the Cameca SX100 electron microprobe at  
181 Rensselaer Polytechnic Institute. All imaging was conducted at 15 kV, with a beam current of  
182 50 nA. The BSE images in **Figure 3** show the basic textures for the undeformed and the  
183 deformed samples. The textures of the two samples are clearly different, with FeS grains in the  
184 deformed sample being much more stretched out and appear to have migrated along olivine grain  
185 boundaries. The deformed texture can be seen in **Figure 3b**, where FeS is present along  
186 individual olivine grain boundaries; while in the undeformed sample, FeS occupies triple-grain  
187 junctions or grain corners as more equi-dimensional blobs (**Figure 3a**). The image of the  
188 deformed sample was taken from the mid-area of the sample, neither at the edge or in the center,  
189 and is broadly characteristic of the texture seen throughout the entire sample. The elongated  
190 blobs are no necessarily co-directional with the direction of shear in the sample, and are not  
191 uniformly aligned throughout the sample.

192 **Table 1** summarizes the electron microprobe composition measurements for sulfide and  
193 olivine in both the undeformed and deformed samples. The FeS grains in the deformed sample  
194 exhibit some quench texture (sulfide immiscibility); however, this internal structure appears to  
195 have had only a slight effect on the resulting Fe and S measurements. The higher standard  
196 deviations in measurements of the deformed sample could also be attributed to the sulfide grains  
197 being thinner and more stretched out, making it more difficult to conduct measurements on a  
198 single bleb due to the beam size of a few microns even in spot mode. We attribute the nickel  
199 measured in the sulfide grains to an impurity in the FeS starting material. The small amount of



200 nickel present in the olivine both before and after the deformation experiment can be attributed  
201 to the fact that nickel is occasionally substituted for iron in the crystal lattice of olivine  
202 (Kohlstedt and Mackwell, 1987).

203

204

## Results and Discussion

### 205 Image Analysis

206 Quantitative permeability measurements were acquired from the resulting HPXTM  
207 images. The individual radiographs collected from the beamline were reconstructed using the  
208 scientific data visualization program Tomo\_Display (Rivers and Gualda, 2009;  
209 <http://cars9.uchicago.edu/software/idl/tomography.html>) and exported as a series of TIFF images.  
210 When these individual images are stacked they create a 3-dimensional volume of the sample.  
211 Six of these image stacks were chosen at increasing degrees of deformation (0°, 180°, 360°, 540°,  
212 720°, and 840°; all at 10 tons of ram load) so that any change in permeability could be observed.  
213 Figure 4a shows a gray-scale XTM image of the sample after reconstruction. These gray-scale  
214 images were then binarized into regions of “melt” and “non-melt” using the program ImageJ  
215 (Rasband, 1997; Figure 4b). The appropriate threshold was determined by finding a value that  
216 would produce the correct proportion of “melt” regions given the expected value from both our  
217 synthetic starting material and initial BSE imaging of the starting material and post-deformation  
218 experiment. The melt volume percent was calculated for each image stack and found to be  
219 within one standard deviation of the starting material. The average melt fraction of the binarized  
220 XTM volumes in the X-direction is  $4.36 \pm 0.11\%$  and an average of  $4.44 \pm 0.07\%$  in the Z-  
221 direction, compared to the actual value of 4.5 vol%. The X- and Z-directions within the sample  
222 can be seen in **Figure 2**, and represent the two directions in which flow was simulated and

223 permeability calculated. These are the two bulk directions that we can measure given the 3-D  
224 data. We performed calculations in both directions because of the potential to observe  
225 anisotropy within the sample due to the shear strain applied to the sample, as well as due to  
226 potential shortening of the sample as the experiment continued. Because the nature of rotational  
227 shear results in a non-uniform strain distribution in the sample, this method we performed  
228 calculations of several subvolumes from different areas of the sample at each degree of  
229 deformation. There was no measurable difference in the resulting permeability in either direction,  
230 however there was a well-defined anisotropy between the two direction (see Figure 6).

231 In order to approximate the true texture of the sample, the binarized XTM images were  
232 compared to the higher resolution BSE images of the deformed sample. In **Figure 5**, the  
233 binarized deformed sample is compared to a binarized XTM image, illustrating the similarities in  
234 texture and melt distribution between the two images. After the binarization process, the six  
235 image stacks, all with dimensions of 450x450x150 pixels, were each divided into nine  
236 150x150x150 pixel sub-volumes and converted into digital volume input files in MATLAB<sup>®</sup>.

237

### 238 **Lattice Boltzmann Simulations**

239 The lattice-Boltzmann method applied to 3-D digital rock samples has been shown to be  
240 a fast and accurate method of quantifying permeability of complex geometries found in natural  
241 porous systems (e.g. White et al. 2006). Here, quantitative permeability calculations were  
242 performed on the digital volumes using the open-source program Palabos (Latt, 2009), which  
243 utilizes the lattice Boltzmann method (LBM) to simulate flow of a viscous fluid through a matrix  
244 while representing the physics of a real system (Chen and Doolen, 1998; Latt, 2008). Palabos  
245 and the LBM have been used and validated by several previous studies (e.g. Bosl et al., 1998;

246 Roberts et al., 2007; Degruyter et al., 2010). Palabos uses Darcy's law to obtain the permeability  
247 of the sub-volumes in non-dimensional lattice units from the average velocity distribution  
248 throughout the 3-D volume, along with an applied pressure gradient and fluid viscosity. This  
249 non-dimensional value is then converted into physical units ( $\text{m}^2$ ) by multiplying it with the pixel  
250 size of the XTM image.

251 The calculated permeabilities for various steps of shear strain for sample R1288 can be  
252 found in **Table 2**. The final measurements are all within one standard deviation of one another  
253 and do not increase with increasing deformation. Figure 6 plots the permeability results from  
254 two experiments against the steps of shear strain. The experiment labeled R1288 is the  
255 experiment shown in the images in this paper. The experiment labeled R1350 is a second  
256 experiment that was repeated using identical methods. The second experiment (R1350) was  
257 deformed to a significantly higher degree, although the final textures appeared to be similar. Also,  
258 the calculated permeabilities on both samples are consistent within uncertainty, and both sample  
259 show the sample anisotropy between the X and Z directions. This anisotropy may be a result of  
260 initial shortening of the sample due to compression at the initiation of the experiment. The one  
261 point at the highest degree of deformation in R1350 may indicate a slight shift upwards in  
262 permeability at very high degrees of deformation, but more work and experiments will need to be  
263 done to confirm this result. The quantitative analysis performed on the digital volumes allows  
264 for a more direct means to calculate the permeability of the sample than previous work that relied  
265 on models such as the Kozeny-Carman relationship relating permeability to grain size and model  
266 dependant geometric factors. The permeabilities obtained in this study are comparable to the  
267 range of values from previous workers' studies, particularly those of Roberts et al. (2007) and  
268 Watson and Roberts (2011). These studies both describe the olivine/sulfide system as well as

269 utilize XTM images to quantitatively determine permeability via lattice Boltzmann simulations.  
270 **Figure 7** compares these three studies to one another, where it can be seen that the permeabilities  
271 in this study are within one standard deviation of the permeabilities obtained for samples with  
272 higher melt fractions. It can also be seen that the results in this study have higher permeabilities  
273 than those of Watson and Roberts for the same melt fraction and the pre-deformation  
274 measurements are consistent with previous studies which state that the pinch-off threshold in the  
275 FeS-silicate system is between 3 and 6 vol% (Yoshino et al., 2003; Roberts et al., 2007; Watson  
276 and Roberts, 2011).

### 277 **Comparison to Previous Studies**

278 Several previous studies address the question of permeability and connectivity in similar  
279 samples with and without the complicating factor of deformation. The present work differs from  
280 these previous studies in a few important ways, as described below. In some previous work, the  
281 presence of an electrically conductive pathway has been interpreted as evidence for a melt that  
282 was sufficiently connected to allow for permeable flow (i.e. Yoshino et al., 2003, 2004).  
283 However, it has recently been shown (e.g. Watson and Roberts 2011, Watson et al. 2010) that  
284 small, disconnected, blebs of sulfide can create electrically conductive pathways. This is thought  
285 to be due to very thin (~nm) films along grain boundaries and edges even when the melt fraction  
286 is well below the percolation threshold (~1 vol% as opposed to 5 vol%). Because the difference  
287 in electrical conductivity is so drastic between the silicate and the sulfide melt, even a miniscule  
288 volume that is connected will produce significantly higher bulk conductivity. In these cases, the  
289 connected volume is such a small percentage of the total melt in the sample that it is unlikely to  
290 add any substantial permeability to the system. A more thorough discussion comparing estimates  
291 of permeability from electrical conductivity and x-ray micro-tomography measurements is

292 available in Watson and Roberts, (2011).

293         There have also been previous studies of the effect of deformation on connectivity and  
294 permeability in olivine + iron sulfide systems (e.g. Bruhn et al. 2000, Groebner and Kohlstedt,  
295 2006, Hustoft et al. 2007, and Walte et al. 2011). Bruhn et al. (2000) performed experiments  
296 with a comparable volume fraction of Fe-S melt in an olivine matrix and deformed the samples  
297 at a higher strain rate of between  $10^{-4}\text{s}^{-1}$  and  $10^{-3}\text{s}^{-1}$  at 1250°C and 300MPa. In backscattered  
298 electron images they observed similar (but more pronounced) changes in the shape of the Fe-S  
299 melt blobs. The pockets became larger, more elongated, and were aligned at an angle of  $\sim 20^\circ$   
300 with the shear plane. Bruhn et al. performed a 3-D reconstruction on a small portion of their  
301 sample ( $\sim 35\text{mm} \times 35\text{mm} \times 25\text{mm}$ ) by serial sectioning, and repeated BSE imaging. They interpret  
302 the changes in the melt pocket texture as evidence that melt can become interconnected and thus  
303 allow permeable flow even in systems with high dihedral angles, as a result of shear deformation.  
304 The benefit of this technique is enhanced spatial resolution of the shape of the Fe-S blob, but that  
305 comes at a cost of not being able to image as much of the sample (thousands to millions of grains  
306 and pockets), and therefore, perhaps not being able to assess the change in connectivity across  
307 the whole sample. Groebner and Kohlstedt (2006) expanded on the earlier work with more  
308 experiments on an analog system with an even higher dihedral angle of  $\sim 150^\circ$  (olivine +4% Au).  
309 Again, they found a change in texture associated with deformation of the samples, and that the  
310 molten gold formed well connected melt bands at an angle of  $\sim 15^\circ$  to the shear plane. They took  
311 these results as evidence that deformation may induce more efficient percolative flow with non-  
312 wetting melts than previously believed. Again, the strain rates of these experiments were at least  
313 2-3 orders of magnitude higher than the maximum strain rate measured here. The theory behind  
314 these results and similar results relating to the effect of shear on silicate melt extraction in the

315 Earth is summarized in Kohlstedt and Holtzmann (2009).

316 Walte et al. (2011) performed a series of similar experiments on olivine + FeS, and  
317 Olivine + Au across a broader range of strain rates ( $\sim 10^{-4} \text{ s}^{-1}$  -  $10^{-6} \text{ s}^{-1}$ ). They analyzed the  
318 resulting textures in 2-D sections of the samples, and found that the changes in textures could be  
319 categorized into different types depending on the strain rate. They show that at high strain rates  
320 (the stress dominated regime, above  $\sim 10^{-4} \text{ s}^{-1}$ ) the samples show linear zones of elongated melt  
321 pockets, and that the degree of elongation increases with increased strain rate. At lower strain  
322 rates (the surface tension dominated regime, below  $\sim 10^{-5} \text{ s}^{-1}$ ), liquid pockets are not linearly  
323 aligned or significantly elongated. The textures seen in our experiments are consistent with an  
324 intermediate texture between what was observed for the high and low strain rate samples. This is  
325 also consistent with our measured maximum strain rate of  $7.7 \times 10^{-5} \text{ s}^{-1}$ . Walte's et al. (2011)  
326 experiments show that only a very small amount of melt is lost during the low strain rate  
327 experiments, indicating that there is limited connectivity of the melt within the sample. All of the  
328 experiments by Walte et al. (2011) show that at best, the melt segregation is inefficient, and at  
329 least a 2-3vol% of the metallic melt is left behind in the sample, which is consistent with our  
330 present results.

### 331 **Implications**

332 The permeabilities obtained in this study can be used to calculate the migration velocity  
333 of a sulfide melt through an olivine matrix in order to determine if shear deformation can lead to  
334 core formation in small (100 km) planetesimals within the 1-5 My time frame. The rate of  
335 migration can be calculated using the relationship:

$$336 \quad v = k\Delta\rho g/\eta$$

337 where  $k$  is the permeability,  $\Delta\rho$  is the density difference between sulfide and olivine ( $2.0\text{E}+03$

338  $\text{kg/m}^3$ ),  $g$  is the gravitational acceleration ( $0.1 \text{ m/s}^2$ ), and  $\eta$  is sulfide melt viscosity ( $0.01 \text{ kg/m}\cdot\text{s}$ ),  
339 after Roberts et al. 2007 and Watson et al. 2011. Using the average of the permeabilities (X-  
340 direction;  $6.31\text{E-}15 \text{ m}^2$ ), the migration velocity is calculated to be  $0.4 \text{ cm/year}$ . A migration  
341 velocity of  $\sim 3.3 \text{ cm/year}$  is necessary in order to fully segregate a metallic melt into the core of a  
342 small planetesimal within 3 My (Watson and Roberts, 2011).

343 However, migration velocity is highly dependent on grain size. Figure 8 shows that for a  
344 melt volume of 4.5%, and the conditions above, a grain size of approximately  $230 \mu\text{m}$  is needed  
345 in order to reach a migration velocity of  $3.3 \text{ cm/year}$ . These grain sizes are reasonable for small  
346 planetesimals (Watson and Roberts, 2011). To obtain the migration velocities in Figure 6, the  
347 Kozeny-Carman relationship was used to calculate the permeabilities at increasing grain sizes:

348 
$$k = (1/C) \cdot d^2 \phi^n$$

349 with  $C = 2000$  (geometric constant),  $\phi = 4.5 \text{ vol\%}$  (porosity), and  $n = 2$ , with  $n$  being a scaling  
350 exponent representing how close to the percolation threshold a system is. The actual grain sizes  
351 in this study were between  $40$  and  $80 \mu\text{m}$ , and so these small sizes could be a contributing factor  
352 in the low permeabilities, and thus low migration velocities, observed in this sample. As  
353 mentioned above, caution needs to be applied when we are using the Kozeny-Carman  
354 relationship, as it is not uniquely determined for this system. The geometric terms chosen are  
355 roughly similar to those that have been used with some success to describe the olivine/basalt  
356 system at equilibrium, but it is unclear that these terms will apply equally well here. The main  
357 purpose of this calculation is to illustrate that the permeabilities measured in this olivine/FeS  
358 system are low compared to what is required for rapid core formation in planetesimals. It should  
359 be noted that increasing the exponent  $n$  from  $n=2$  to  $n=3$  (the value used for fully connected melt  
360 well above the percolation threshold by Faul, 1997 and Bourbie and Zinszer, 1985) decreases the

361 permeability of the system even further. Furthermore, the migration velocity is also highly  
362 dependent on viscosity. The values calculated here can essentially be considered an upper bound,  
363 as they represent viscosities at the relatively high temperatures of 1300°C, where some silicate  
364 melting would be expected. The viscosity of FeS melt at these high temperatures and pressures  
365 between 1 and 2 GPa is around 0.005 kg/m·s (Kono et al. 2015). But, LeBlanc and Secco (1996)  
366 showed that the viscosity of Fe<sub>73</sub>S<sub>27</sub> melts increases by nearly an order of magnitude as the  
367 temperature is lowered to ~1100°C (the conditions of these experiments, and reasonable  
368 conditions for this model of percolative core formation in the absence of silicate melt). Studies  
369 that obtain permeability indirectly through methods such as electrical conductivity yield  
370 migration velocities that differ by several orders of magnitude from this study and others that use  
371 HPXTM. From their electrical conductivity experiments, Yoshino et al. (2003) estimate a  
372 migration velocity of ~1-100 m/year. This significantly higher value may be attributed to thin  
373 layers of sulfide melt between olivine grains that were unable to be imaged via XTM due to the  
374 *in-situ* nature of the experiment and thus the decreased resolution. However, overall, the  
375 possible contribution that these narrow connections may have to the calculated permeability is  
376 likely insignificant (Roberts et al., 2007; Watson and Roberts, 2011). Instead, this great  
377 difference likely stems from the fact that a direct measurement of permeability was not possible  
378 and so the Kozeny-Carman relationship was relied upon to infer permeability. In this study, the  
379 permeability was directly measured, thus the migration velocity calculated likely represents a  
380 more realistic scenario for core formation.

381         The main perceived drawback to the tomography method presented here is that the spatial  
382 resolution of the imaging is not able to capture the smallest threads of melt that could potentially  
383 be connected, and create high permeability pathways. Given our measured voxel size, we



384 estimate that we can reliably image a feature that about 2-4 micrometers in diameter, especially  
385 considering the large contrast between the two phases in our tomographic reconstructions. First,  
386 we note that the sulfide melt that is contributing to the permeability of the sample is a small  
387 fraction of the total melt in the sample (ie. most of the melt is not connected). We can calculate  
388 the expected permeability of the sample given different fractions of melt that is well connected  
389 (Figure 9). Here the data symbols represent lattice Boltzmann simulations run on artificial (ideal)  
390 volumes with a cylindrical tubules of varying diameters along grain edges of cubic grains (150  
391 micrometer edge length). The solid gray curve is the analytical solution to Darcy's law for the  
392 same geometry (Turcotte, 2002). Here we can see that our observed permeability ( $\sim 10^{-15} \text{ m}^2$ )  
393 corresponds to tubules approximately 2-3 micrometers in diameter. This is admittedly close to  
394 the expected resolution of what we could measure. However, in order to achieve an order of  
395 magnitude higher permeability, tubules of approximately 5.5 micrometers in diameter are  
396 predicted which we would expect to see clearly, but we do not. Secondly, we can compare 2-D  
397 images of the sample at different spatial resolution. Figure 10 shows an example of the  
398 differences we can expect to see in thresholding a 2-D backscattered electron image of the  
399 deformed sample. The first panel shows the original image, the second shows that high  
400 resolution image thresholded directly, the fourth shows the thresholding results of an image that  
401 was artificially reduced in resolution to mimic the resolution that we would achieve by  
402 tomography ( $\sim 2$  micrometers per pixel). In both cases the images were thresholded to result in  
403 4.6 vol% melt. Although there are some noticeable differences, the main difference tends to be  
404 around the perimeter of the larger melt blobs, which is unlikely to add significantly to the  
405 permeability. The lower resolution image does miss a few stand-alone pixels that appear in the  
406 higher resolution image, but again, these few pixels are unlikely to make a large difference in the

407 measured permeability.

408         The permeabilities obtained here from the X-ray microtomographic images via lattice  
409 Boltzmann simulations indicate that the migration velocity is probably not high enough for  
410 complete core formation to take place in planetesimals within the 1-5 My time frame. However,  
411 there is still much work that can be done in order to increase our understanding of the effects of  
412 certain parameters such as strain rate, temperature, and metal/silicate composition on the melt  
413 connectivity, permeability, and migration velocity. These new results indicate that permeabilities  
414 obtained via XTM and the LBM are reliable and accurate; further work utilizing these methods is  
415 promising and will bring us even closer to understanding the complex and significant event of  
416 core formation in planetesimals. The development of in-situ high pressure x-ray tomography  
417 techniques allows for novel experiments to be conducted, including those that monitor the  
418 evolution of a system undergoing deformation and reaction. These new techniques greatly  
419 enhance the array of tools to investigate dynamic processes at high temperatures and pressures in  
420 more detail and with more accuracy than previously available.

421

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## Figure Captions

**Figure 1.** (a)  $\frac{3}{4}$  “ piston cylinder cell assembly used to synthesize the olivine + FeS starting material in a graphite capsule. (b) the assembly used for deformation experiments in the Drickamer cell.

**Figure 2:** Schematic illustration of the sample with the two directions of flow that permeability measurements were obtained from. The X-direction of flow is parallel to the axis of rotation, while the Z-direction is perpendicular.

**Figure 3.** BSE images of an undeformed sample and the deformed sample. (a) An undeformed sample and (b) the deformed sample, both sectioned parallel to the axis of rotation. The image of the deformed sample is from a location in the midpart of the sample (neither at the edge or at the center).

**Figure 4.** XTM image before and after binarization. (a) A gray-scale XTM image slice and (b) the same slice binarized. Melt is represented as the white areas, while non-melt (i.e. silicate matrix) is represented by black.

**Figure 5.** A binarized XTM image compared to a binarized BSE image. (a) Binarized XTM image of the sample deformed to  $360^\circ$  and (b) a binarized BSE image of the fully deformed sample. The texture and melt distribution in both images are very similar, indicating that the binarization process is successful in reproducing the sample texture.

Figure 6: Permeability vs. degrees of deformation for two experiments. The images depicting texture in this paper are all from the first experiment (labeled R1288). The second experiment was performed in an analogous manner, but experienced significantly more deformation. The resulting final textures are very similar between both experiments, and the permeability results are consistent within uncertainty.

**Figure 7.** Plot of melt fraction vs. permeability comparing the results of this work to previous work. The closed circle is permeability in the X-direction for this work (4.5 vol% melt) and the open circle is for the Z-direction, with each point being an average of the full volumes in each respective direction of flow. One permeability result is shown from Roberts et al. (2007) and six results are shown from Watson and Roberts (2011). The average of the nine permeabilities is represented by the horizontal dashed lines and the gray area represents one standard deviation from this average. The sample from Roberts et al. is 10 vol%, and the results from Watson and Roberts are ~4, ~6, and ~10 vol%. The uncertainties on the data point from Roberts et al. were not available.



**Figure 8.** Migration velocity plotted as a function of grain size at a melt volume of 4.5%. The vertical gray dashed line represents the minimum grain size necessary (~230  $\mu\text{m}$ ) to attain the minimum migration velocity needed (3.3 cm/yr) in order for a small (100 km) planetesimal to fully differentiate within 3 My.

**Figure 9:** Permeability versus tubule diameter for an idealized geometry of cubic grains of different sizes with melt tubes along grain edges. Symbols represent results from lattice Boltzmann simulations run on idealized artificial volumes, and curves are calculations of the permeability from Darcy's law for this simplified geometry.

**Figure 10:** (a) BSE image of post-run sample (b) thresholded high resolution BSE image (c). Original BSE image again. (d) thresholding of the same image that has been artificially reduced in resolution to approximate the tomography results .

**Tables**

**Table 1.**

**Electron Microprobe Results.**

<b>Olivine (wt%) - Deformed</b>							
	<b>SiO<sub>2</sub></b>	<b>FeO</b>	<b>MgO</b>	<b>NiO</b>	<b>SO</b>	<b>Total</b>	<b>No. of Analyses</b>
Average	40.10±0.28	10.55±0.26	50.28±0.24	0.04±0.01	0.04±0.03	101.02±0.16	54
<b>Sulfide (wt%) - Deformed</b>							
	<b>Fe</b>	<b>S</b>	<b>Si</b>	<b>Mg</b>	<b>Ni</b>	<b>Total</b>	<b>No. of Analyses</b>
	62.31±1.45	32.01±3.73	0.43±0.42	0.59±0.79	2.70±2.36	98.04±0.87	20
<b>Olivine (wt%) - Undeformed</b>							
	<b>SiO<sub>2</sub></b>	<b>FeO</b>	<b>MgO</b>	<b>NiO</b>	<b>SO</b>	<b>Total</b>	<b>No. of Analyses</b>
Average	40.25±0.20	10.70±0.08	50.58±0.09	0.05±0.01	0.03±0.05	101.61±0.21	44
<b>Sulfide (wt%) - Undeformed</b>							
	<b>Fe</b>	<b>S</b>	<b>Si</b>	<b>Mg</b>	<b>Ni</b>	<b>Total</b>	<b>No. of Analyses</b>
	59.21±0.45	35.62±0.45	0.17±0.16	0.04±0.04	3.54±0.22	98.58±0.55	21

$\sigma$  = one standard deviation

**Table 2.**

Final Permeability Results for the Sample R1288 in the X- and Z-Directions.

<b>X-Direction</b>				
<b>Angle</b>	<b>Melt Fraction</b>	<b><math>\sigma</math>MF</b>	<b>Log(k)</b>	<b><math>\sigma</math>log(k)</b>
0	4.39	0.56	-14.04	0.05
180	4.53	0.89	-14.24	0.05
360	4.34	0.54	-14.21	0.04
540	4.37	0.48	-14.19	0.04
720	4.34	0.53	-14.24	0.08
840	4.20	0.61	-14.27	0.06

<b>Z-Direction</b>				
<b>Angle</b>	<b>Melt Fraction</b>	<b><math>\sigma</math>MF</b>	<b>Log(k)</b>	<b><math>\sigma</math>log(k)</b>
0	4.32	0.85	-14.52	0.08
180	4.52	1.03	-14.74	0.09
360	4.42	0.68	-14.68	0.05
540	4.45	1.00	-14.78	0.07
720	4.46	1.02	-14.83	0.05
840	4.44	0.80	-14.69	0.11

$\sigma$  = one standard deviation.

## Figures

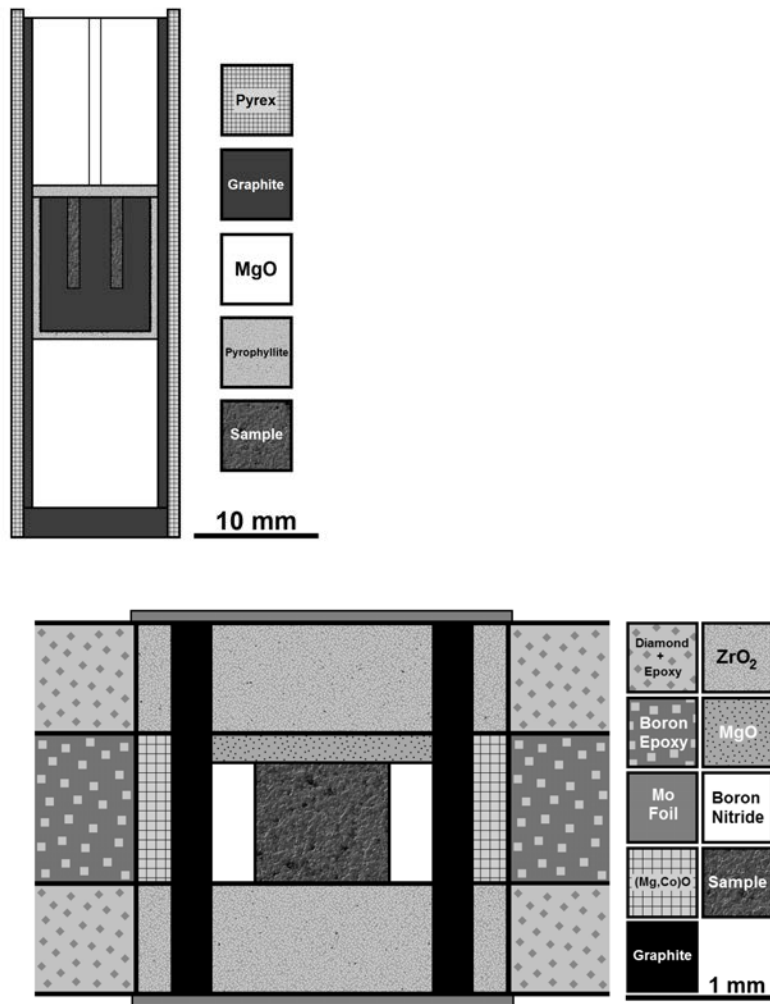


Figure 1.

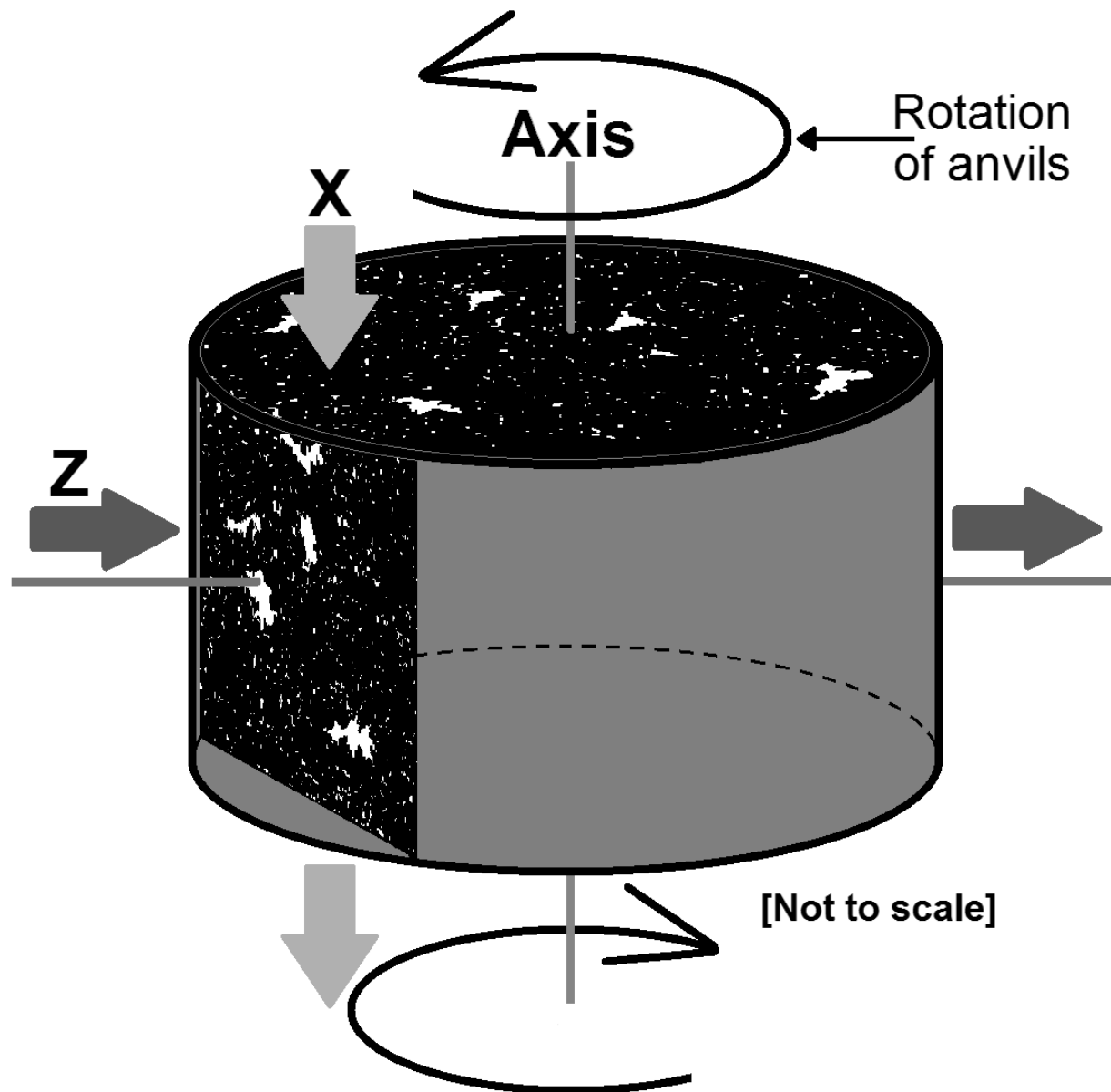
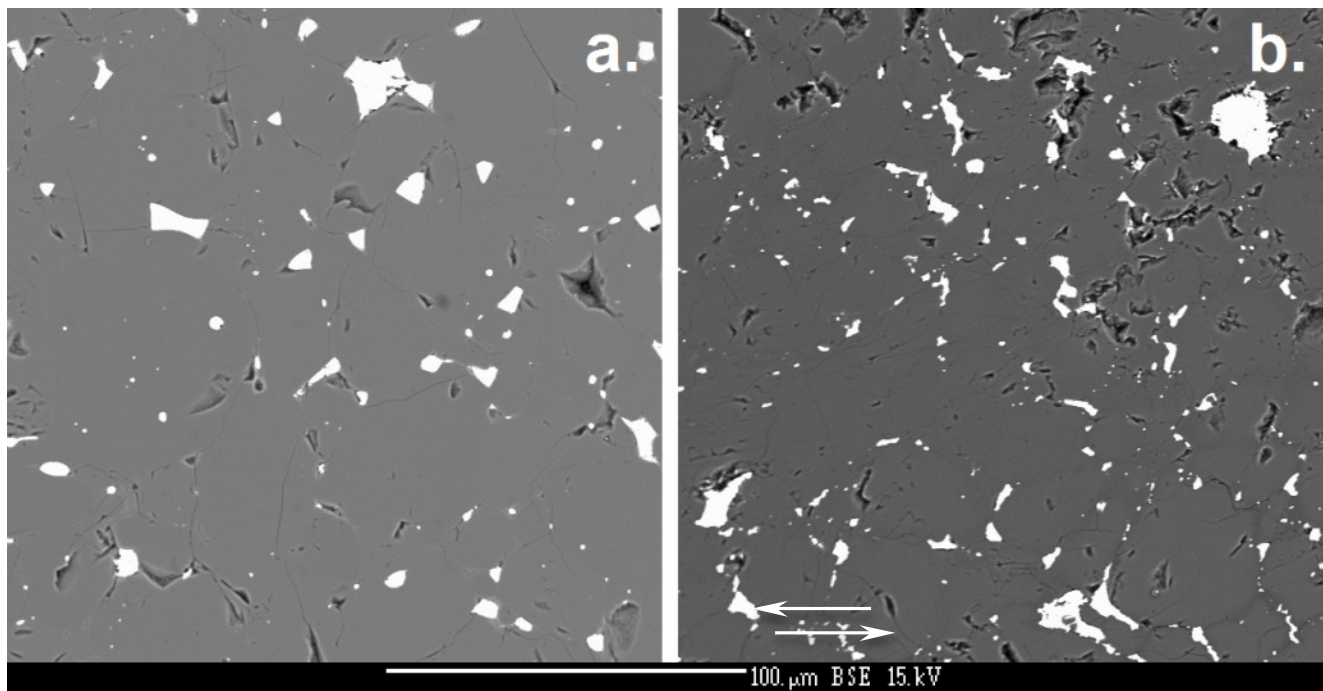
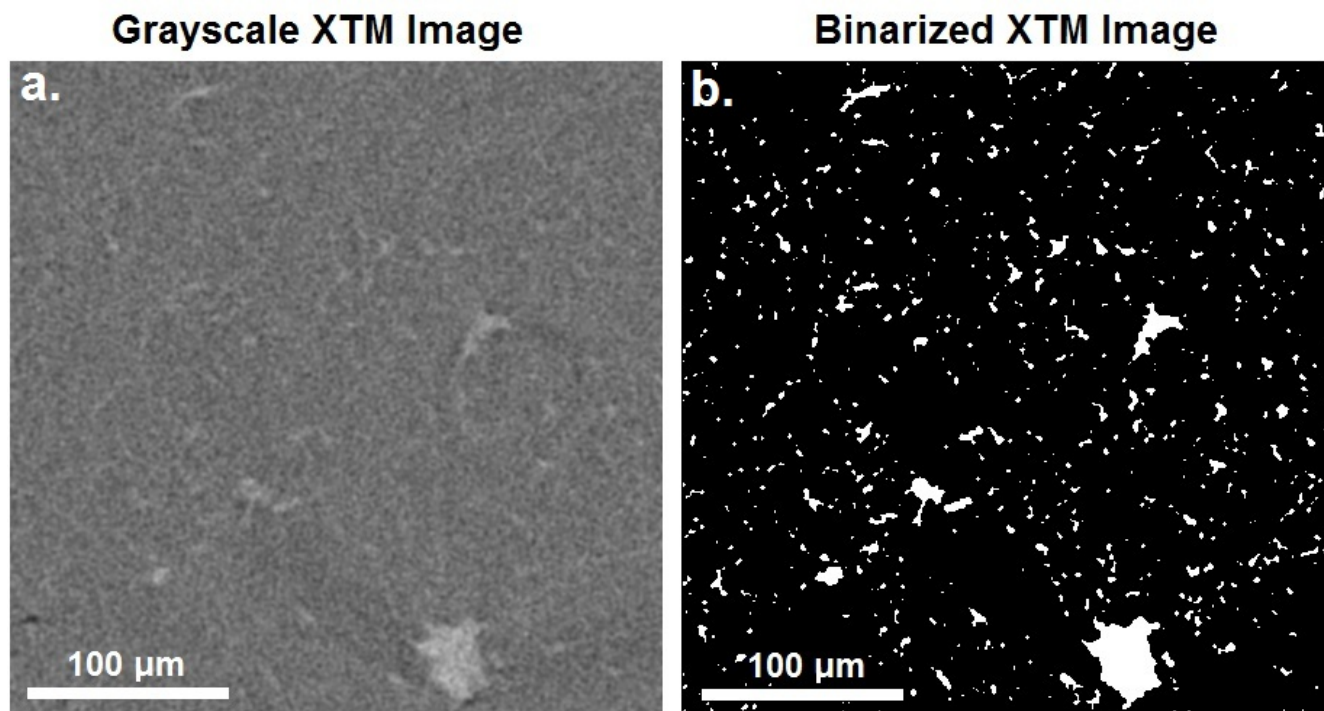


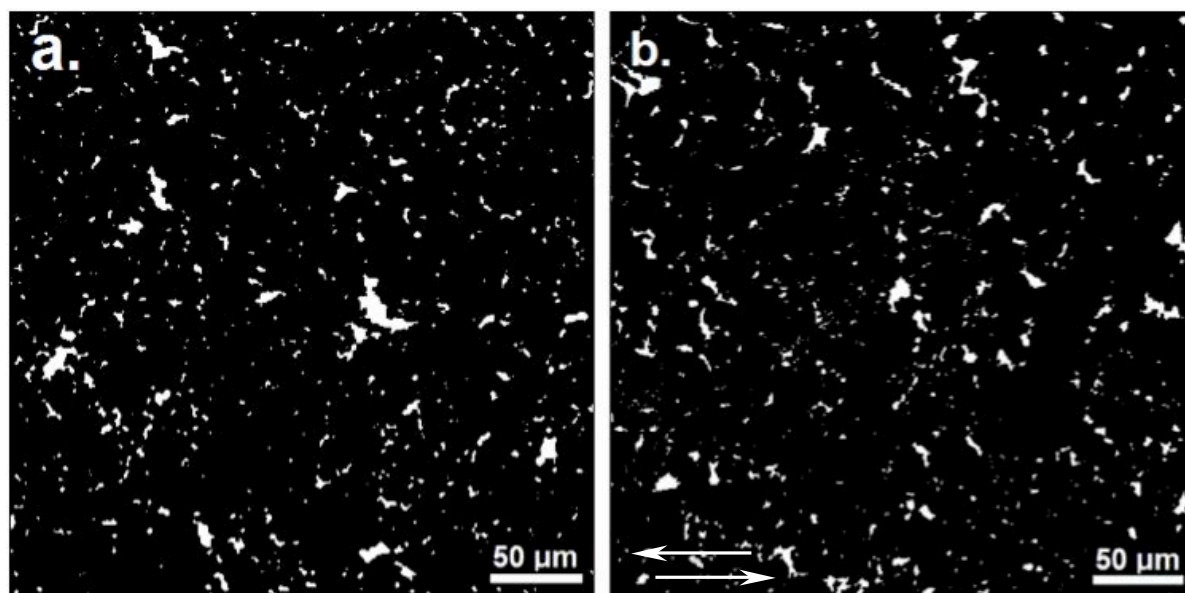
Figure 2.



**Figure 3.**



**Figure 4.**



**Figure 5.**



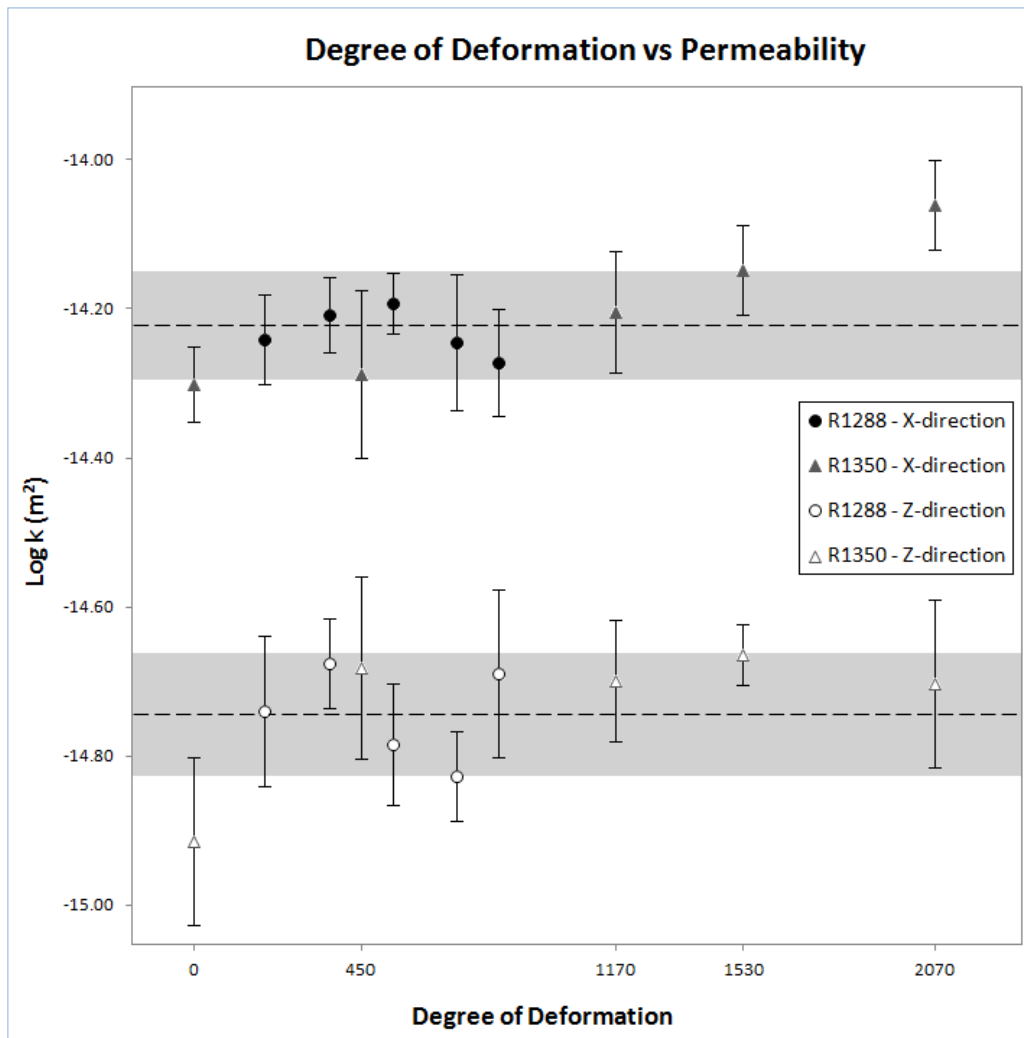


Figure 6

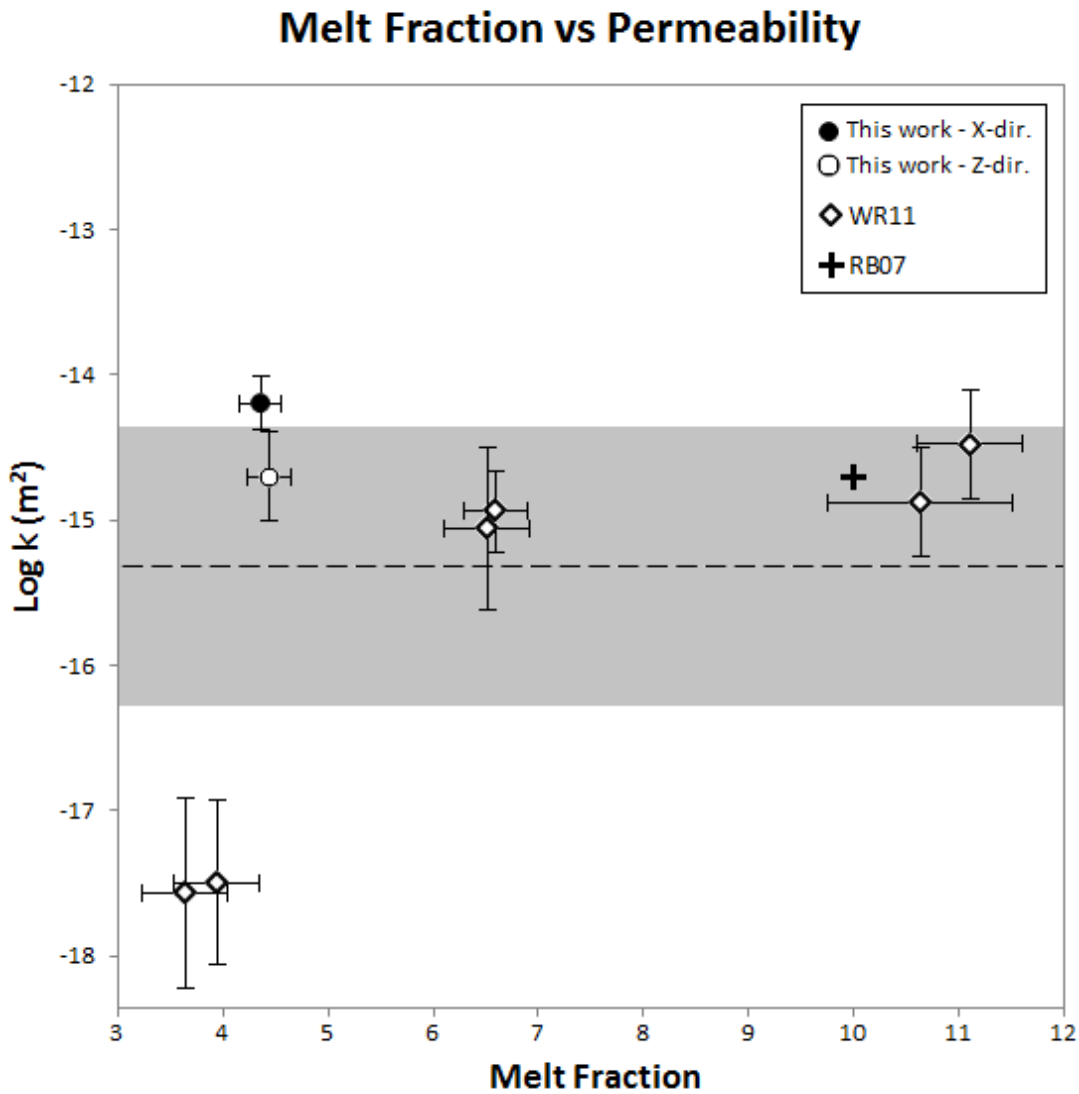


Figure 7.

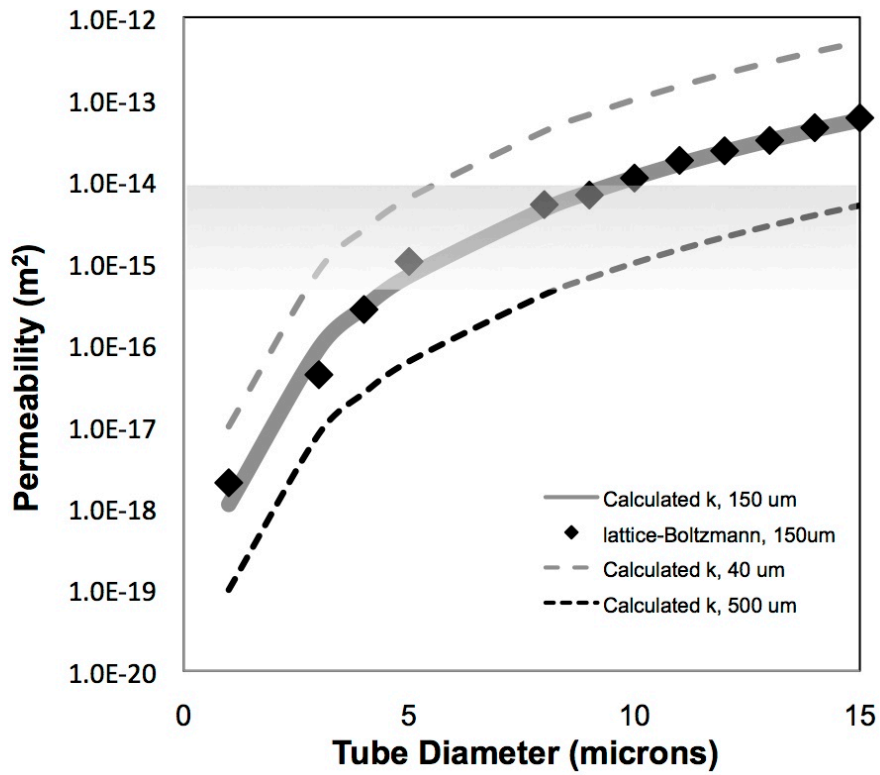


Figure 8.

# Migration Velocity vs Grain Size at 4.5 vol% Melt

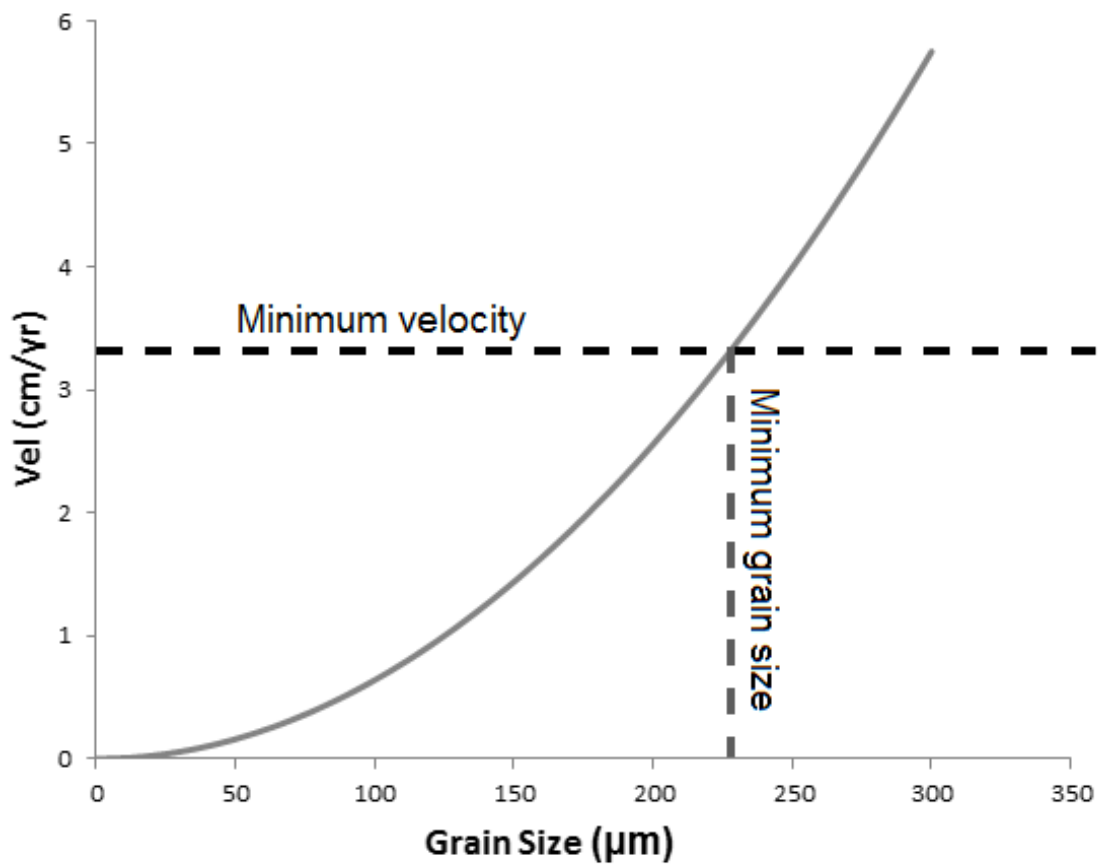
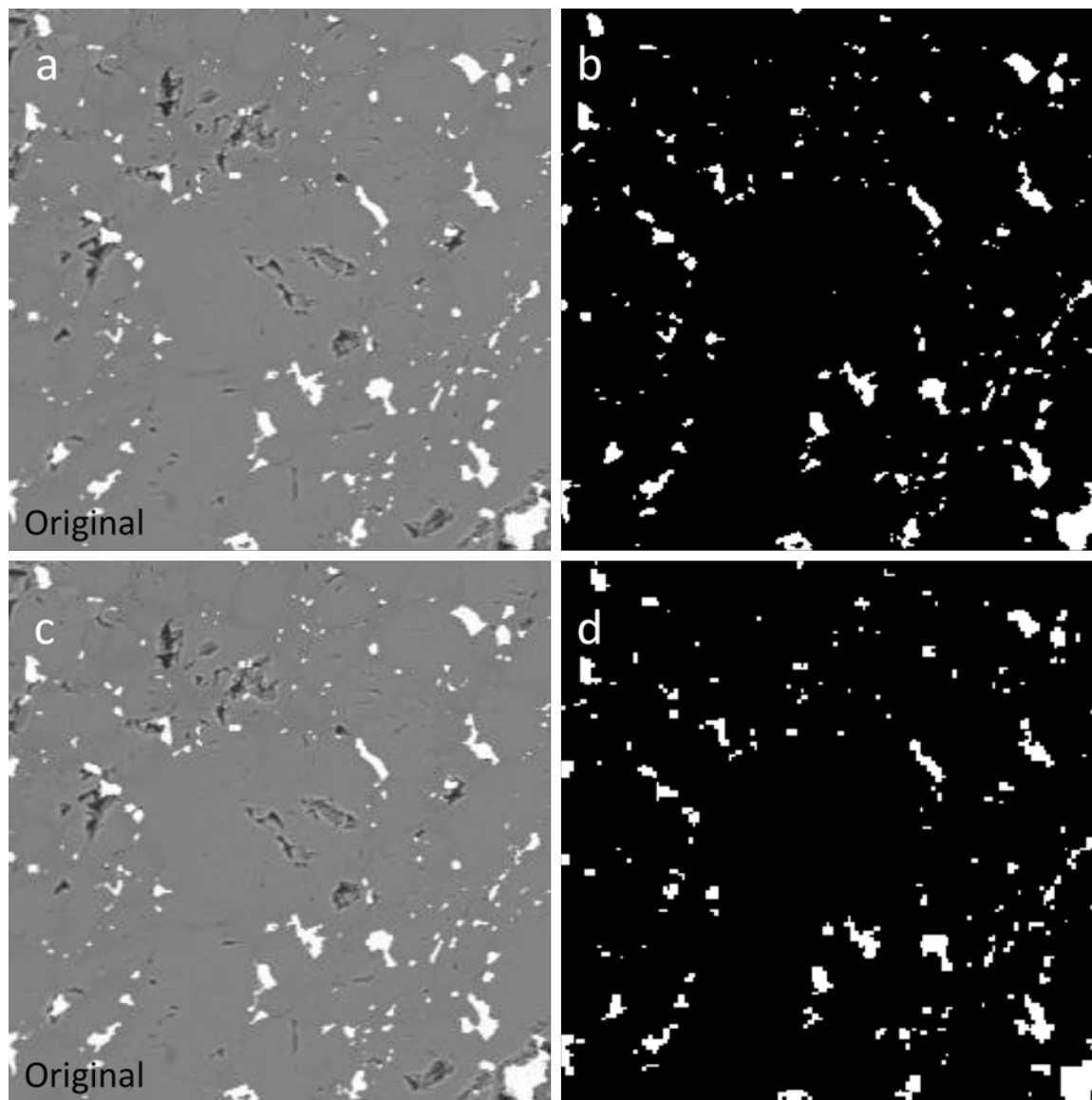


Figure 9



**Figure 10**