1   **REVISION 1**

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3   **Crystallographic orientation relationships in host–inclusion systems: new**
4   **insights from large EBSD datasets**

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23   **Abstract**

24   Crystallographic orientation relationships (CORs) between mineral inclusions and their hosts

25   could potentially deliver information about inclusion formation processes and conditions. Most

26   previous studies are based on small numbers of analyses. This paper uses EBSD to study host–

27   inclusion CORs in an inclusion-rich Permian metapegmatite garnet (Koralpe region, Eastern

28   Alps, Austria), demonstrating the importance of large datasets and of EBSD in particular for the

29   analysis of CORs. The distribution of measured orientations reflects host garnet point group

30   symmetry for 89% of inclusions analyzed (total N = 530). Each inclusion phase (rutile,

31   corundum and ilmenite) shows at least three different CORs to host garnet. 'Statistical' CORs

32   are introduced to describe distributions of inclusion orientations that have one or two degrees of

33   freedom with respect to the host, but still reflect host crystal symmetry. Two end member

34   characteristics of statistical CORs are distinguished: rotation and dispersion. Most statistical

35   CORs observed show a mixture of both. Each inclusion phase shows at least one statistical COR.

36   Multiple coexisting CORs and statistical CORs are not restricted to rutile. Re-examination of

37   previous garnet–rutile COR studies in light of the new results indicates that COR information

38   may have been overlooked when using small datasets. Variation in COR parameters correlates

39   with broad differences in assumed metamorphic conditions for new and literature samples,

40   suggesting that petrogenetic information may be available if COR formation can be understood.

41   The favorability of the detected CORs cannot be explained by a simple model involving

42   minimization of misfit between lattice planes, implying that other interface properties or the

43   inclusion formation mechanism are important controls on COR development.

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Introduction

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46   Crystalline mineral inclusions can provide valuable information about the formation and

47   evolution of rocks. The origins of inclusions determine the processes about which they can

48   record petrological information and how this information is encoded, assuming changes in the

49   properties of interest due to re-equilibration can be excluded. In some cases, just determining the

50   origin of a population of inclusions can have important implications for the inferred

51   tectonometamorphic history of a sample (e.g. Green II et al. 1997; Van Roermund et al. 2000; Ye

52   et al. 2000; Mposkos and Kostopoulos 2001; Zhang and Liou 2003; Zhang et al. 2011; Ague and

53   Eckert Jr. 2012; Ruiz-Cruz and Sanz de Galdeano 2013; Gou et al. 2014; Glassley et al. 2014).

54   Many approaches to inferring inclusion origins have been taken. All studies cited in this

55   introduction consider the phases present, their compositions, distributions, shapes and any shape-

56   preferred orientations. Some studies also include inclusion-based microstructures (Burton 1986;

57   Perchuk 2008; Hwang et al. 2011, 2013, 2015), compositional zoning or diffusion profiles in

58   inclusions or hosts (Burton 1986; Ague and Eckert Jr. 2012; Hwang et al. 2013; Khisina et al.

59   2013), and crystallographic orientation relationships (CORs) between inclusion and host

60   crystallographic directions (Brearley and Champness 1986; Hwang et al. 2007, 2011, 2013,

61   2015; Zhang et al. 2011; Proyer et al. 2013, Xu et al. 2015).

62   CORs have mostly been used to try to confirm exsolution origins for inclusions, due to the

63   assumption that 'specific' CORs (where the crystallographic orientation of one phase is fixed

64   relative to another) are a diagnostic criterion for exsolution (e.g. Hwang et al. 2007). However,

65   there is a lack of agreement about criteria to distinguish between host–inclusion CORs of

66   different origins. Combined with other observations, different specific CORs have been

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67   considered evidence both for (Hwang et al. 2011; Zhang et al. 2011) and against (Hwang et al.

68   2011, 2013, 2015) exsolution origins, and other authors have argued absence of a specific COR

69   does not rule out inclusion formation by exsolution (Brearley and Champness 1986; Ague and

70   Eckert Jr. 2012; Proyer et al. 2013; Xu et al. 2015).

71   Identification of inclusion origins in a sample via CORs is based on two assumptions:

72   1) The dataset obtained gives a representative picture of the distribution of inclusion

73   crystallographic orientations. The CORs defined from this distribution (and the relative

74   frequencies thereof) accurately represent the likelihood of finding an inclusion with a

75   given crystallographic orientation relative to the host.

76   2) The number, relative frequencies and characteristics of CORs developed during different

77   inclusion formation processes are known and distinguishable.

78   Assumption 2) requires that assumption 1) was fulfilled for any samples used to develop this

79   knowledge, thus assumption 1) is fundamental to the determination of inclusion origins.

80   However, many studies use only a few tens of inclusion orientations per sample to conclude

81   which - or whether - CORs are present.

82   The ability of electron backscatter diffraction (EBSD) to rapidly acquire large numbers of

83   crystallographic orientations has been exploited to obtain crystallographic orientations of rutile,

84   corundum and ilmenite inclusions (total $N = 530$) in two metapegmatite garnet host grains. Using

85   the new dataset this paper addresses the problem of how to accurately and representatively

86   characterize the distribution of inclusion crystallographic orientations using CORs. It then

87   discusses the potential of well-characterized sets of CORs to reveal the origins of inclusions,

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88   answer wider petrogenetic questions and shed light on the lattice-scale mechanisms controlling

89   COR development.

Geological setting

91   The new dataset originates from metapegmatite garnets from the locality Wirtbartl, in the

92   Koralpe region, Austria (sample number: 04T26K, geographic coordinates: 5177709 N, 504737

93   E; UTM zone 33N, geodetic datum: WGS84). The Wirtbartl metapegmatites are intercalated

94   with metapelitic rocks of the Austroalpine Saualpe-Koralpe crystalline basement complex

95   (Schmid et al. 2004). The complex consists mainly of poly-metamorphic siliciclastic

96   metasediments with minor amphibolites, eclogites and metapegmatites, as well as rare calc-

97   silicates and marbles.

98   The dominant tectono-metamorphic imprint in the Gneiss Unit of the Saualpe-Koralpe complex

99   occurred at eclogite facies conditions in the Cretaceous at around 90 Ma (Thöni 2006).

100 Maximum P-T conditions recorded by eclogites are 600 – 750ºC and 1.8 – 2.4 GPa (Gregurek et

101 al. 1997; Miller and Thöni 1997; Miller et al. 2005, 2007). Similar temperatures but lower

102 pressures are recorded by the metapelites (Gregurek et al. 1997; Tenczer and Stüwe 2003).

103 The Cretaceous tectono-metamorphic event was preceded by Permian low-pressure

104 metamorphism, evident from garnet cores (Thöni and Miller 2009), relict assemblages (Habler

105 and Thöni 2001; Tenczer et al. 2006) and radiometric dating (Thöni and Jagoutz 1992; Thöni et

106 al. 2008). Permian metamorphic conditions in the Saualpe-Koralpe complex have been estimated

107 at 600ºC/0.4 GPa (Habler and Thöni 2001) and 650ºC/0.6 – 0.65 GPa (Tenczer et al. 2006).

108 Widespread Al-rich pegmatites give undisturbed garnet Sm–Nd ages ranging from 285 to 225

109 Ma, indicating multiple melt injections (Thöni et al. 2008; Thöni and Miller 2009). Pegmatites

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110   are interpreted as a product of local melting of siliciclastic (meta)sedimentary protoliths (Thöni

111   and Miller 2000; Habler et al. 2007; Thöni et al. 2008) during long term thinning of the crust

112   (Schuster and Stüwe 2008).

113   The Wirtbartl locality consists predominantly of Al-rich metapelites intercalated with

114   peraluminous metapegmatites (Habler et al. 2007; Bestmann et al. 2008; Thöni et al. 2008).

115   Garnet separates from different pegmatite bodies at the locality give Sm-Nd ages ranging from

116   ca. 255 Ma (Habler et al. 2007) to ca. 230 Ma (Thöni et al. 2008).

117   **Methods**

118   **Thin section preparation**

119   Thin sections were polished mechanically and then chemo-mechanically (the latter using an

120   alkaline colloidal silica suspension and a polyurethane plate) in order to produce a defect-free

121   surface for EBSD analysis. Thin sections were carbon-coated to establish electrical conductivity.

122   A single carbon thread at high vacuum ensured a thin coat for optimal EBSD measurement.

123   **Field emission gun scanning electron microscope (FEG-SEM) and energy dispersive X-ray**

124   **spectroscopy (EDX) analyses**

125   Secondary electron (SE) and backscattered electron (BSE) images as well as EDX and EBSD

126   analyses were collected on an FEI Quanta 3D FEG-SEM with a field emission gun source at the

127   laboratory for scanning electron microscopy and focused ion beam applications of the Faculty of

128   Geosciences, Geography and Astronomy at the University of Vienna (Austria). The microscope

129   is equipped with an Apollo XV Silicon Drift Detector for EDX analysis. EDX data were

130   collected using the TEAM 3.1 software at beam conditions of 15 kV and spot sizes of 4.5 - 5.5

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131   (0.1 - 0.3 nA) in standard mode (30 - 50 μm aperture) or spot size 1.0 (4 nA) in analytic mode

132   (1000 μm aperture).

133   **EBSD analyses**

134   Full crystallographic orientations of host garnet and rutile, ilmenite and corundum inclusions

135   were determined by EBSD in two separate garnet grains. Measurements were carried out using

136   the previously described FEI Quanta 3D FEG-SEM, equipped with an EDAX Digiview IV

137   EBSD camera at an elevation angle of 5º. The OIM DC v6.2.1 EBSD analysis software was used

138   for data acquisition. Beam conditions for all EBSD data were 15 kV accelerating voltage and 4.0

139   nA beam current with a 1000 μm SEM aperture and an incidence angle of 20º to the sample

140   surface. The working distance was 14 mm and EBSD camera binning was 2 x 2, with Hough

141   settings of 1º theta step size and a binned pattern size of 140 pixels. A 9 x 9 convolution mask

142   with a maximum of 16 bands was used for indexing garnet. An 11 x 11 convolution mask with a

143   maximum of 20 bands was used for indexing rutile, ilmenite and corundum. The same

144   background was used throughout, but camera exposure time was increased when measuring

145   corundum to compensate for lower signal intensity. The identity of inclusions was confirmed by

146   EDX after measurement unless identification by EBSD pattern and inclusion habit was

147   unequivocal. The Matlab^{TM} toolbox MTEX (Bachmann et al. 2010; Hielscher et al. 2010) was

148   used for data processing and pole figure plotting.

149   **Microstructural observations**

150   **Thin section description**

151   The original (Permian) pegmatite microstructure of the samples has been affected by Cretaceous

152   deformation and recrystallization (Bestmann et al. 2008; Griffiths et al., 2014). Polycrystalline

153   quartz ribbons (grain size 40 μm – 1 mm), recrystallized feldspar (K-feldspar and albite, grain

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154   size 40 – 150 μm) and acicular kyanite (grain size ~5 μm x 10 – 100 μm) define a mylonitic

155   foliation. Magmatic almandine-spessartine garnet (grain size ~ 0.2 – 1 cm) and K-feldspar

156   (perthitic, grain size up to ~ 1 cm) occur as porphyroclasts. Tourmaline, apatite and zircon are

157   found as accessory minerals in the rock matrix. In less strained samples polycrystalline kyanite

158   forms pseudomorphs completely replacing coarse-grained magmatic andalusite crystals.

159   In plane polarized transmitted light micrographs of thin sections garnet exhibits brownish-grey

160   cores showing concentric and sector zoning (fig. 1), surrounded by clear pinkish rims with

161   euhedral outer facets (fig. 2b+f). Rim garnet is intergrown with anhedral quartz (grain size 50 –

162   500 μm) and rare euhedral zircon (grain size ca. 100 μm). Both cores and rims are of Permian

163   age (Thöni et al. 2008). The source of the dark coloration in cores is abundant submicrometer-

164   sized inclusions (fig. 2), which are scarce or absent in the rims. Griffiths et al. (2014) document

165   that these inclusions are 1 μm – 2 nm in diameter and that there are seven phases present: rutile,

166   ilmenite, corundum, xenotime, zircon, apatite and qingheiite-Fe^{2+} (Hatert et al. 2010), a wyllieite

167   group Fe-Mn phosphate (Moore and Ito 1979).

168   Inclusions define both concentric and sector zones in the garnet cores (fig. 1). Different zones are

169   defined by variation in the abundances, grain sizes, habits or colors of the different inclusion

170   phases. Transitions between concentric zones can be abrupt or gradual, and sometimes zoning is

171   oscillatory (fig. 1a). Lateral transitions between sectors are always abrupt (e.g. fig. 1b). The outer

172   boundaries of sector zones and all concentric zones are parallel to garnet crystal faces, primarily

173   {112} and {110}.

174   Almost all inclusions that can be resolved optically are equant or slightly oblate, with no shape

175   preferred orientation (fig. 2). The only exception is the intermittently developed outermost zone,

176   which consists of elongate (0.2 – 0.5 x 10 – 100 μm) rutile needles with their long axes oriented

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177 parallel to garnet <111> directions (not shown). Corundum inclusions are almost invisible in

178 transmitted light micrographs as they have a similar refractive index to garnet. SEM images (fig.

179 2d+h) reveal that they are tabular with a large aspect ratio (0.1 – 0.5 x 1 – 10 μm). Inclusions

180 large enough to be resolved in the SEM exhibit crystal facets; apatite and wyllieite group

181 phosphates have many facets, thus appearing rounded. Occasional multiphase inclusions can be

182 observed.

183 During Cretaceous eclogite facies metamorphism garnet underwent both crystal plastic and

184 brittle deformation. These processes locally promoted microstructural and compositional re-

185 equilibration of inclusions and garnet, resulting in two microstructures crosscutting the inclusion

186 zoning: recrystallization zones (Bestmann et al. 2008) and inclusion trails (Griffiths et al. 2014).

187 Both microstructures are surrounded by garnet where sub-micrometer inclusions are absent.

188 **EBSD measurement domains**

189 To study possible CORs between inclusions and garnet two domains were selected (fig. 2),

190 situated in the cores of separate but adjacent pegmatite garnets. Both have similar distributions of

191 inclusions, though inclusions in domain A are smaller and more abundant than inclusions in

192 domain B (fig. 2). SEM imaging and EDX measurements show that the most abundant phases in

193 both domains are rutile, corundum and wyllieite group phosphate. No ilmenite could be detected

194 in domain A, but ilmenite is present in domain B, where it is rarer and smaller than rutile and

195 corundum. These differences reflect the fact that the domains are at different positions in the

196 zoning succession. Domains were selected to avoid the areas of optically visible re-equilibration

197 associated with inclusion trails and recrystallization zones.

198 **Crystallographic orientation data**

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199   EBSD point analyses determined the crystallographic orientation of host garnet, corundum, rutile

200   and ilmenite. Indexing of xenotime and zircon EBSD patterns generated multiple orientation

201   solutions for single inclusion crystals. No reference pattern was available for wyllieite group

202   phosphates and both wyllieite and apatite inclusions were sensitive to beam damage. In light of

203   these methodological obstacles and their relative scarcity in the selected domains, EBSD data

204   was not collected for zircon or any phosphate phases.

205   **Representativeness and precision of the EBSD single point dataset**

206   Emphasis was placed on collecting a large number of measurements for each inclusion phase; the

207   total number of inclusions analyzed does not reflect the relative abundance of each phase.

208   However, the relative frequency of different CORs within each phase is expected to be

209   representative for the grainsizes that could be measured (minimum ca. 400 nm parallel to the

210   long axis of the EBSD interaction volume) because the only selection criterion was sufficient

211   pattern quality for indexing. All rutile and corundum CORs with N>3 inclusions were found in

212   both garnets. Some CORs are up 2.5 times more frequent in one garnet domain compared to the

213   other (table S1).

214   A rough estimate of the precision of orientation determination was obtained by calculating the

215   average misorientation angle between five garnet orientations measured on the same crystal and

216   the mean orientation of the five measurements. The measurements differed from the mean

217   orientation by an average of 0.7º, and a similar value was obtained for three repeat measurements

218   on a second garnet crystal. The estimated precision in misorientation angle between two

219   independent measurements is thus 1.4º.

220   **Pole figure plot construction**

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221   All pole figures were plotted with antipodal symmetry. To enable comparison between garnets

222   all inclusion orientations were plotted relative to a fixed host garnet orientation (x ‖ $[100]_{garnet}$

223   and z ‖ $[001]_{garnet}$). No garnet direction was strongly preferred over any of its symmetrical

224   equivalents for any COR in either garnet. This allowed the combination of data from separate

225   garnets and meant that a partial symmetrization of the dataset could be carried out to make CORs

226   clearer in pole figures without introducing spurious symmetries. Four copies of the dataset were

227   overlapped, each rotated by 90º around garnet [001] relative to each other, forcing the dataset to

228   conform to the fourfold symmetry of the garnet [001] axis. A single quadrant of the resulting

229   pole figure contains the orientation relationship information of the whole dataset, combining

230   inclusions that have CORs with symmetrically equivalent garnet axes. Symmetrized plots are

231   indicated in figure captions.

232   **Rutile crystallographic orientations**

233   The crystallographic orientation of rutile inclusions relative to the host garnet reflects the

234   symmetry of the garnet structure (fig. 3). Rutile inclusions were divided into groups based on the

235   alignment of their <001> directions (*c*-axes) with different directions in garnet (fig. 3). Groups

236   were divided into subgroups according to the relationships of other rutile directions with garnet.

237   The suggested CORs of undivided rutile inclusion groups and the most abundant subgroups are

238   listed in table 1.

239   **Group R1 (fig. 4a).** This group comprises rutile inclusions with their *c*-axes parallel to garnet

240   <110> with ≤ 5º misorientation, corresponding to maxima in the *c*-axis ODF plot (fig. 3). Only

241   30% of inclusions in group R1 have *c*-axes that lie within 1.4º of garnet <110>. The distribution

242   of misorientation angles between rutile *c*-axes and garnet <110> is shown in figure 4b. Subgroup

243   R1a comprises the majority of group R1. One of the two symmetrically equivalent rutile *a*-axes

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244   is parallel to a garnet <111> direction and the second is parallel to a garnet <112> direction (both

245   with up to 5º misorientation, fig. 4a). In the small subgroup R1b (fig. S1a), *a*-axes appear to

246   follow one set of higher-order symmetrically equivalent directions in garnet. Given the 5º

247   orientation spread it is difficult to specify these, but the garnet <144> and <118> directions are a

248   good approximation.

249   **Group R2 (fig. S1b).** This group comprises the four rutile inclusions with a *c*-axis parallel to

250   garnet <111> with ≤ 5º misorientation. The mean misorientation angle between rutile *c*-axes and

251   garnet <111> is 0.7º. In subgroup R2a one of the rutile *a*-axes is parallel to a garnet <110>

252   direction and the second is parallel to a garnet <112> direction, with no significant

253   misorientation. The *a*-axes of one inclusion lie within a garnet {111} plane but not parallel to

254   any low-indexed garnet directions, it is assigned to subgroup R2b.

255   **Group R3 (fig. 5).** This group comprises rutile inclusions with a *c*-axis lying in a cone inclined

256   to the garnet <111> directions. The angle which the rutile *c*-axis makes to the nearest garnet

257   <111> direction will be referred to as the 'inclination angle'. This relationship was previously

258   described by Proyer et al. (2013), who recorded inclination angles from 26º - 29º (mean 27.6º).

259   Group R3 encompasses all rutile inclusions with inclination angles of 26º - 31º (mean 28.1º).

260   Rutile *c*-axes are not evenly distributed around garnet <111>. Six maxima form three pairs

261   flanking each garnet <110> direction, conforming to the threefold symmetry axis along garnet

262   <111> (fig. 3). These diffuse maxima coincide with garnet <135> directions. Three weaker

263   maxima occur between these pairs, centered on garnet <113> directions. Group R3 was divided

264   into 3 subgroups.

265   Subgroup R3a (fig. 5a), the largest, corresponds to the orientation relationship seen by Proyer et

266   al. One rutile *a*-axis lies in or near to the {111} plane perpendicular to the <111> direction

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267   around which the rutile *c*-axis cone lies (fig. 5ai). The second *a*-axis is forced by symmetry to lie

268   on a small circle at ± the inclination angle from the {111} plane, i.e. rutile orientations are tilted

269   around the *a*-axis in the garnet {111} plane by the inclination angle. The *a*-axes in garnet {111}

270   planes never occur within ca. 10º of a garnet <110> direction but otherwise no direction within

271   the plane is avoided. The inclined *a*-axes show a preference for garnet <112> directions. The

272   low-indexed rutile direction aligned closest to garnet <111> is one of the rutile <103> directions

273   (fig. 5aii). 56% of inclusions in subgroup R3a have a rutile <103> direction within 1.4º of garnet

274   <111>. No low-indexed garnet directions coincide with other rutile <103> directions, which lie

275   in two cones ca. 38º and 55º inclined to garnet <111>. One small circle of {101} poles is inclined

276   only 5º to garnet <111> and a second small circle lies at the *c*-axis inclination angle from the

277   {111} plane, coinciding with the rutile *a*-axis small circle (fig. S2a). Rutile {101} poles show no

278   preference for a garnet direction. All other orientation relationships described by Proyer et al.

279   follow by symmetry from the relationships described here.

280   Subgroup R3b (fig. 5b) comprises group R3 inclusions where one rutile {101} plane pole is

281   parallel to a garnet <110> direction (fig. 5bii). The *c*-axes of these inclusions cluster near to

282   garnet <113> directions (within the previously defined cone around garnet <111>), but do not

283   follow the <113> directions strictly. In contrast to subgroup R3a, rutile *a*-axes are not

284   perpendicular to the garnet <111> direction around which the *c*-axis cone is located (fig. 5bi).

285   One *a*-axis appears concentrated near to garnet <112> directions that do not lie perpendicular to

286   garnet <111> and some rutile <103> directions seem to cluster near garnet <135> directions (fig.

287   S2b), but there are not enough data to be confident about these potential relationships.

288   Subgroup R3c (fig. S2c) comprises the nine group R3 inclusions with *c*-axes that lie within the

289   cone around a garnet <111> direction, but for which no other relationships with garnet could be

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290   found. Rutile *c*-axes cluster near to garnet <135> directions (though this was not the criteria used

291   to define the subgroup). It is possible that there are other alignments between garnet and rutile

292   directions but sampling statistics for this subgroup are too poor to make them obvious.

293   **Group R1* (fig. 4c).** This group represents a broad spread of *c*-axis orientations. Of all

294   inclusions not belonging to groups R1, R2 or R3, over 80% are oriented with their *c*-axes

295   between 5º and 22º from a garnet <110> direction (fig. 3), and are assigned to this group. The

296   distribution of misorientation angles between rutile *c*-axes and garnet <110> is shown in figure

297   4b. Inclusions satisfying the *c*-axis criterion for group R3 have been excluded from group R1*.

298   The orientation relationships of rutile directions other than <001> with garnet are as diffuse as

299   the *c*-axis distribution. One of the two rutile *a*-axes tends to cluster parallel or near to a garnet

300   <111> direction. However, almost no rutile *a*-axes are found aligned with a garnet <112>

301   direction, and the remaining *a*-axes define a broad girdle around the {110} plane.

302   **Group RX (fig S3a).** This group comprises rutile inclusions where no orientation relationship

303   with the garnet could be observed.

304   **Corundum crystallographic orientations**

305   The crystallographic orientation of corundum inclusions relative to the host garnet also reflects

306   the symmetry of the garnet. Multiple groups can be identified based on the alignment of

307   corundum <0001> directions (*c*-axes) with different garnet directions. Groups were divided into

308   subgroups according to the relationships of other corundum directions with garnet. The CORs of

309   undivided corundum inclusion groups and the most abundant subgroups are listed in table 2. The

310   tabular habit of corundum inclusions is defined by their crystallography, with tablets parallel to

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311   corundum {0001} planes. All corundum CORs therefore imply corresponding shape-preferred

312   orientation relationships.

313   **Group C1 (fig. 6a).** This group comprises corundum inclusions with a c-axis parallel to the

314   garnet <112> direction with ≤ 5º misorientation. 78% of these inclusions have a c-axis within

315   1.4º of garnet <112>. Most inclusions belong to subgroup C1a. One corundum a-axis (parallel to

316   the poles of corundum {11-20} planes) is aligned with a garnet <111> direction (fig 6ai). By

317   symmetry the other two a-axes align close to garnet <113> directions. Correspondingly,

318   corundum {10-10} poles are aligned at 30º to the a-axes, one {10-10} pole is fixed parallel to

319   garnet <110> and the other two lie near to garnet <135> directions (fig 6aii). The small subgroup

320   C1b is identical to C1a except that inclusions are rotated 30º around their c-axes. Two inclusions

321   have a-axes in garnet {112} planes that are not parallel to any of the important garnet directions

322   seen in the other subgroups, these are assigned to subgroup C1c.

323   **Group C2 (fig. 6b).** This group comprises corundum inclusions with a c-axis parallel to the

324   garnet <111> direction with ≤ 5º misorientation. 84% of the group has a c-axis within 1.4º of

325   garnet <111>. Almost all inclusions are assigned to subgroup C2a, where all corundum a-axes

326   (fig 6bi) are parallel to garnet <112> directions and all {10-10} poles (fig. 6bii) are parallel to

327   garnet <110> directions. Subgroup C2b comprises the 3 inclusions where corundum a-axes are

328   merely located within a garnet {111} plane and are not systematically parallel to a low-indexed

329   garnet direction.

330   **Group C3 (fig. S4).** This group comprises the small number of corundum inclusions with a c-

331   axis parallel to the garnet <100> direction with ≤ 5º misorientation. The mean misorientation

332   angle between group C3 corundum c-axes and garnet <100> is 1.47º. One corundum a-axis is

333   always parallel to a garnet <110> direction, as by symmetry is one {10-10} pole.

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334   **Group C4 (fig. 6c).** This group comprises corundum inclusions without a c-axis within $\leq 5^{\circ}$

335   misorientation angle of either garnet <111> or <112> directions, but with one a-axis (fig. 6ci)

336   parallel to a garnet <111> direction (with $\leq 5^{\circ}$ misorientation). 38% of inclusions in the group

337   have one a-axis within 1.4° of garnet <111>. The corundum c-axes lie in {111} garnet planes, as

338   does one of the {10-10} poles (fig. 6cii). This group has not been divided into subgroups as there

339   are no symmetrically repeated concentrations of corundum {10-10} poles, c- or a-axes parallel to

340   low indexed garnet directions. Nonetheless group C4 corundum c-axes do not appear randomly

341   distributed around one a-axis, but this may be an artifact of the small number of grains

342   comprising this group.

343   **Group CX (fig S3b).** This group comprises corundum inclusions where no orientation

344   relationship with the garnet could be observed.

345   **Ilmenite crystallographic orientations**

346   The crystallographic orientation of ilmenite inclusions relative to the host garnet also reflects

347   garnet symmetry. Groups were defined based on the alignment of ilmenite <0001> directions (c-

348   axes) with different garnet directions and divided into subgroups using the relationships of other

349   ilmenite directions with garnet. The CORs of undivided ilmenite inclusion groups and the most

350   abundant subgroups are listed in table 3.

351   **Group I1 (fig. 7a).** This group comprises ilmenite inclusions with a c-axis parallel to the garnet

352   <112> direction with $\leq 5^{\circ}$ misorientation. 86% of the group has their c-axis within 1.4° of garnet

353   <112>. In the largest subgroup, I1a, one ilmenite a-axis (equivalent to one ilmenite {11-20}

354   plane pole) is aligned with a garnet <111> direction (fig. 7ai). The other a-axes align close to

355   garnet <113> directions. One ilmenite {10-10} pole is fixed parallel to garnet <110> and the

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356   other two lie near to garnet <135> directions (fig. 7aii). The small subgroup I1b is identical to

357   I1a except that inclusions are rotated 30º around their c-axes. Six inclusions have a-axes in

358   garnet {112} planes that are not parallel to any of the important garnet directions seen in the

359   other subgroups, these are assigned to subgroup I1c.

360   **Group I2 (fig. 7b).** This group comprises ilmenite inclusions with a c-axis parallel to the garnet

361   <111> direction with ≤ 5º misorientation. 95% of the group has a c-axis within 1.4º of garnet

362   <111>. All but one inclusion are assigned to subgroup I2a, where all ilmenite a-axes are parallel

363   to garnet <112> directions (fig. 7bi) and all {10-10} poles are parallel to garnet <110> directions

364   (fig. 7bii). A single inclusion has a-axes located within a garnet {111} plane but not parallel to a

365   low-indexed garnet direction, assigned to subgroup I2b.

366   **Group I3 (fig. 7c).** This group comprises ilmenite inclusions without a c-axis within ≤ 5º

367   misorientation angle of either garnet <111> or <112> directions, but with one a-axis (fig. 7ci)

368   parallel to a garnet <111> direction (with ≤ 5º misorientation). 65% of inclusions in the group

369   have one a-axis within 1.4º of garnet <111>. The ilmenite c-axes lie in {111} garnet planes, as

370   does one of the {10-10} poles (fig. 7cii). This group has not been divided into subgroups as there

371   are no symmetrically repeated concentrations of ilmenite {10-10} poles, c- or a-axes parallel to

372   low indexed garnet directions.

373   **Group IX (fig S3c).** This group comprises ilmenite inclusions where no orientation relationship

374   with the garnet could be observed.

375   **Discussion**

376   89% of the 530 inclusions analyzed by EBSD have crystallographic orientations that can be

377   related to the crystal symmetry of the host garnet. Each of the three inclusion phases examined

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378   can be divided among at least three different groups (most with several subgroups) on the basis

379   of orientation relationships between host and inclusion crystallographic directions. The Wirtbartl

380   host–inclusion system displays exceptional variety in the number and type of CORs present.

381   The origin of the Wirtbartl inclusions is not discussed here. This would require a full picture of

382   the CORs present in host–inclusion systems with different known inclusion origins, something

383   this paper suggests is not yet available.

384   **Types of COR**

385   Nomenclature is required to discuss the diverse characteristics of the observed CORs. The

386   proposed terminology for COR types does not carry any genetic implications. In this discussion,

387   the term 'specific COR' refers to a crystallographic orientation relationship where the

388   orientations of inclusion and host are fixed with respect to one another, with zero degrees of

389   freedom. It makes no reference to the coherency of the two lattices or the interface geometry and

390   structure.

391   About half the COR groups described do not show a specific COR to the host garnet.

392   Nonetheless, the distribution of inclusion crystallographic orientations in these groups reflects

393   the symmetry of the garnet (e.g. fig. 3). The term 'statistical COR' is introduced to describe the

394   relationships between host and inclusion directions that are not specific but non-random. A

395   statistical COR is defined by a population of inclusions. The crystallographic orientations of

396   individual inclusions with a particular statistical COR have one or more degrees of freedom

397   relative to the crystallographic orientation of the host, although there may be limits to the range

398   of misorientation angles over which this freedom exists. EBSD measurement of increasing

399   numbers of inclusions with the same statistical COR reveals an orientation distribution that

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400 increasingly accurately approximates conformity to the centrosymmetric point group symmetry

401 of the host crystal.

402 The inclusion orientation distributions of statistical CORs display two end member

403 characteristics. A statistical COR usually exhibits a mixture of both. In some groups, one

404 inclusion crystallographic direction is fixed to the host and the others are free to assume any

405 direction rotated around this common axis, i.e. inclusion crystallographic orientations have one

406 degree of freedom (subgroup R3a, fig. 5a; group C4, fig. 6c; subgroup I1c, fig. 7a; group I3, fig.

407 7c; Proyer et al. 2013; Xu et al. 2015). This characteristic of a statistical COR will be referred to

408 as 'rotation'. 'Rotational' statistical CORs are those where rotation is the strongest element of the

409 inclusion orientation distribution. In most examples the single degree of freedom is limited, so

410 that not every orientation distributed around a certain direction is equally favored (e.g. subgroup

411 R3a, fig. 5a; Xu et al. 2015).

412 Other groups show inclusion crystallographic directions concentrated within a certain

413 misorientation angle of particular host crystallographic directions, but not fixed exactly parallel

414 to them (groups R1 and R1*, fig. 4; subgroups R3b and R3c, figs. 5b & S2c). Such groups allow

415 two degrees of freedom between host and inclusion crystallographic orientations, but only within

416 strict limits. This characteristic of a statistical COR will be referred to as 'dispersion'.

417 'Dispersional' statistical CORs are those where dispersion is the strongest element of the

418 inclusion orientation distribution; if one crystallographic direction were less dispersed then the

419 statistical COR would be rotational in character. Rotational CORs often show subordinate

420 dispersion (all rotational CORs listed in the previous paragraph; Xu et al. 2015).

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421 Due to the complexity inherent in precisely determining the error of lattice orientations derived

422 from SEM-EBSD analyses (e.g. Ram et al. 2015), a generalized criterion to differentiate specific

423 CORs from statistical CORs at very small dispersions is beyond the scope of this paper. In the

424 Wirtbartl dataset the two predominantly dispersional statistical CORs (groups R1 and R1*) can

425 nonetheless be reliably classified because the observed dispersion greatly exceeds the expected

426 angular error of Hough-transform-based EBSD (fig. 4).

427 An indication of the amount of dispersion of an axis relationship can be obtained by calculating

428 the fraction of inclusions in a group that fulfill the chosen relationship with a misorientation

429 angle below a set value. This has been carried out for the Wirtbartl dataset for groups containing

430 > 10 inclusions, using an angle of 1.4°, twice the approximate angular precision of the garnet

431 orientation measurements. For axis relationships that are considered specific (groups C1, C2, I1

432 and I2) > 75% of all inclusions have misorientation angles of less than 1.4°, whereas in groups

433 with minor or major dispersional character, < 65% of all inclusions fulfill this criterion. It is not

434 considered useful to subdivide groups depending on whether each inclusion exceeds the angular

435 cutoff or not as there is no evidence that there would be a physical or genetic distinction between

436 the resulting subgroups.

437 Table S2 summarizes how the CORs of all (sub)groups listed in tables 1 – 3 have been classified,

438 according to the criteria discussed above.

439 **Why use the statistical COR concept?**

440 **General considerations.** Currently, studies of host–inclusion systems often look for evidence of

441 specific CORs, rather than fully describing the distribution of inclusion orientations present. The

442 statistical COR concept encourages a less binary approach, in accordance with the wide variety

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443   of CORs observed in this and other studies (Proyer et al. 2013; Xu et al. 2015) that are not

444   specific. It also highlights the need for larger numbers of orientation measurements when

445   studying CORs.

446   Once inclusion directions are separated by less than twice the angular error of the EBSD

447   measurement from each other, the distribution of directions is indistinguishable from continuous.

448   Below this limit (e.g. subgroup R3a, fig. 5a; group C4, fig. 6c) it is inappropriate to represent the

449   distribution of orientations as a large number of different specific CORs.

450   **Illustrative case study: re-examination of Hwang et al. (2007, 2015).** Re-examining some

451   previous results provides an example of how the concept of statistical CORs can capture details

452   of host–inclusion crystallographic relationships that are otherwise obscured.

453   Hwang et al. (2015) present TEM data on the interfaces and CORs of rutile needles in garnet

454   from multiple sources: detrital Idaho 'star garnet' most likely originally from polymetamorphic

455   amphibolite facies metapelitic schist (West et al. 2005; Lang et al. 2014) and garnets from two

456   ultra-high-pressure (UHP) localities: an eclogite from the Sulu UHP terrane in China and a

457   microdiamond-bearing rock from the Erzgebirge, Germany. The Idaho garnets are the main

458   focus of the study, whereas the UHP sample measurements are an expansion of a smaller dataset

459   presented in Hwang et al. (2007).

460   Hwang et al. (2015) define seven major garnet–rutile CORs, all exclusively specific. Their COR-

461   1, COR-5 and COR-6 are not found in the Wirtbartl garnets, and their COR-4 (corresponding to

462   subgroup R2a) is present but rare in both datasets. Comparison of the three remaining Hwang et

463   al. CORs with the rotational statistical COR of group R3a provides evidence of statistical CORs

464   in the older datasets. Rutile inclusions with crystallographic orientations corresponding to

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465   Hwang et al.'s COR-2 & COR-2' ([103]$_{Rt}$ ‖ [111]$_{Grt}$ & (0±10)$_{Rt}$ ‖ (4-3-1)$_{Grt}$, COR-2 and COR-

466   2' are indistinguishable by EBSD) are common in the Wirtbartl garnets. The same is true for

467   their COR-3 ([103]$_{Rt}$ ‖ [111]$_{Grt}$ & (010)$_{Rt}$ ‖ (2-1-1)$_{Grt}$). For the Wirtbartl dataset it is

468   immediately obvious that the <010> directions (*a*-axes) of inclusions with <103>$_{Rt}$ ‖ <111>$_{Grt}$

469   are not *limited* to being parallel to either <4-3-1>$_{Grt}$ or <2-1-1>$_{Grt}$. Rutile *a*-axes can lie anywhere

470   in the {111} plane, with the exception of positions within ca. 10º of a garnet <110> direction

471   (group R3a, fig. 5ai).

472   Hwang et al. (2015) document rutile inclusions with small misorientations from their specific

473   CORs, describing these as 'angular misfits of xº' or 'xº off' from a particular axis relationship.

474   Multiple angular misfits are explicitly described in the Hwang et al. (2015) measurements from

475   the Sulu UHP garnet sample. For inclusions close to COR-2/2', the reported range of angular

476   misfits is greater (0 - 6º) for rutile *a*-axes than for the perpendicular rutile <103> directions (0 -

477   2º), i.e. these inclusions are misoriented around a rotation axis close to garnet <111> from the

478   ideal COR. Inclusions close to COR-3 reportedly do not show any angular misfit for rutile

479   <103> directions but show angular misfits of 0 - 3º for their *a*-axes, corresponding to a pure

480   rotation around garnet <111>. Taking the extremes of both ranges implies that only 7º of the

481   16.1º angle between neighboring <2-1-1>$_{Grt}$ and <4-3-1>$_{Grt}$ directions remains unoccupied by

482   rutile *a*-axes in the reported dataset. Given that the Sulu garnet dataset presented in Hwang et al.

483   (2015) consists of only 19 rutile inclusion orientations, 17 with COR-2/2' or COR-3 orientations,

484   there is a strong possibility that further measurements might reveal a continuous distribution of

485   rutile *a*-axes in the garnet {111} plane, similar to that of the Wirtbartl garnets. This possibility is

486   supported by the 5 Sulu rutile needles plotted by Hwang et al. (2007) that have *c*-axes in a cone

487   around a garnet <111> direction and *a*-axes in a garnet {111} plane (implying one <103>$_{Rt}$ is

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488   approximately parallel to $<111>_{Grt}$). None of these inclusions have a-axes that coincide with <2-

489   1-$1>_{Grt}$, <4-3-$1>_{Grt}$, or <1-$10>_{Grt}$, and one particular a-axis (a_6) is approximately halfway

490   between a <2-1-$1>_{Grt}$ and a <4-3-$1>_{Grt}$ direction (fig. 8).

491   Hwang et al. (2015) do not explicitly give the percentage of inclusions with angular misfits for

492   every sample, but in contrast to the Sulu garnets, the Idaho star garnets appear to mostly show

493   inclusions without angular misfits. Of 58 inclusions measured in one sample (a 6-ray star garnet

494   showing 6 different CORs), only one is called out as having any angular misfit. The distribution

495   of rutile inclusion crystallographic orientations in the 6-ray Idaho star garnet is therefore best

496   described by multiple specific CORs, even using the stricter definition preferred in this paper.

497   The existence of a range of rutile inclusion crystallographic orientations arrayed around a

498   common host garnet axis (a rotational statistical COR) is a reproducible and important

499   characteristic of the Sulu garnet samples that is obscured by describing the distribution as a

500   number of specific CORs with 'angular misfit[s]'. The Sulu orientation distribution appears

501   distinguishable from that in the Idaho star garnets, where the large majority of rutile inclusions

502   *do* have completely specific CORs (assuming that all instances of angular misfit have been

503   explicitly reported). This fact may be of petrological significance, but previous terminology has

504   not allowed for such distinctions to be unambiguously stated.

505   A final judgment on the continuity of rutile a-axis distributions in garnet {111} planes in the

506   Sulu samples must await measurement of a larger number of rutile crystallographic orientations.

507   However, even if further measurements were to confirm the current angular misfit ranges for

508   COR-2/2' and COR-3 as the maximum variation present in the Sulu sample, the description of

509   these CORs as specific would remain misleading. If the current ranges describe the true

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510   maximum variation, the individual groupings COR-2, COR-2' and COR-3 can be retained.

511   However, they should then be described as rotational statistical CORs to denote the nature of the

512   angular variation within each population. Should further measurements instead reveal a

513   continuous distribution, a single rotational statistical COR would most correctly describe the

514   systematic distribution of inclusion orientations with $<103>_{Rt}$ ∥ $<111>_{Grt}$.

515   The uncertainty about the rotational statistical COR(s) in the Sulu sample stems directly from the

516   limited number of rutile crystallographic orientations reported so far. However, no matter how

517   large the dataset, small groups of inclusions from which the full particulars of a COR cannot be

518   reliably determined will almost always be found (e.g. subgroup R2b, fig. S1b; subgroups C1c &

519   C2b, fig. 6a+b; subgroups I1c & I2b, fig. 7a+b). The most general description for a group of

520   inclusions with one axis fixed relative to the host is a single rotational statistical COR, and in the

521   absence of sufficient measurements to reveal greater detail, this is the recommended description.

522   The inclusions in the Sulu sample with $<103>_{Rt}$ ∥ $<111>_{Grt}$ should be described as belonging to

523   a single rotational statistical COR until further data becomes available.

524   **Comparison of Wirtbartl COR data with literature CORs**

525   Existing literature data on CORs between garnet and corundum are restricted to intergrowths

526   between corundum and yttrium aluminium garnet. Sugiyama et al. (2009) found the same COR

527   as the commonest COR in this study (subgroup C1a, fig. 6a), $<0001>_{corundum\ (Crn)}$ ∥ $<112>_{garnet\ (Grt)}$

528   & $\{11\text{-}20\}_{Crn}$ ∥ $\{111\}_{Grt}$. Frazer et al. (2001) detected the COR $<0001>_{Crn}$ ∥ $<112>_{Grt}$ & {10-

529   10}$_{Crn}$ ∥ $\{111\}_{Grt}$, observed only rarely in this study (subgroup C1b, fig. 6a). No literature could

530   be located on CORs between garnet and ilmenite. However, in the Wirtbartl data there is great

531   similarity between the CORs of the two different trigonal phases with garnet. All COR groups

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532 identified for ilmenite are also shown by corundum. This similarity extends to broader similarity

533 with literature data for CORs between trigonal and cubic crystals. The hematite-magnetite

534 system shows condition-dependent variation between the axis relationships $<0001>_{\text{hematite (Hem)}}$

535 $\parallel <111>_{\text{magnetite (Mag)}}$ and $<0001>_{\text{Hem}} \parallel <112>_{\text{Mag}}$ (Bursill & Withers 1979), and for the axis

536 relationship $<0001>_{\text{Hem}} \parallel <111>_{\text{Mag}}$ both the relationships $\{10\text{-}10\}_{\text{Hem}} \parallel \{110\}_{\text{Mag}}$ (e.g. Bursill &

537 Withers 1979) and the relationship $\{11\text{-}20\}_{\text{Hem}} \parallel \{110\}_{\text{Mag}}$ (Amouric et al. 1986) have been

538 found to exist. The range of possible CORs between two phases can seemingly be estimated

539 knowing only their respective crystal systems, suggesting that the role of conserved symmetry

540 elements in controlling CORs is large. Despite the existence of a range of *possible* CORs, the

541 simultaneous occurrence of so many of these in one system does appear to be an unusual feature

542 of the Wirtbartl garnets.

543 At present, the host–inclusion system for which the most varied COR data is available is the

544 garnet–rutile system. Despite uncertainties concerning inclusion formation mechanisms and the

545 conditions and timing of COR formation, an overview of reported garnet–rutile CORs gives an

546 indication of distinguishable characteristic features and possible trends. Rutile–garnet CORs

547 have been described from five garnet localities: detrital 'star garnets' most likely from

548 polymetamorphic amphibolite facies metapelitic schists (West et al. 2005; Lang et al. 2014) in

549 Idaho (Guinel & Norton 2006; Hwang et al. 2015); garnets from eclogite layers in an ultramafic

550 complex in the Sulu UHP terrane, China (Hwang et. al 2007, 2015); garnets containing

551 microdiamonds from the Erzgebirge, Germany (Hwang et. al 2007, 2015); granulite facies garnet

552 rims on UHP garnets from a kyanite-garnet mica-schist in the Kimi complex, Rhodope Massif,

553 Greece (Proyer et al. 2013); and low pressure pegmatite garnets from the locality Wirtbartl,

554 Koralpe, Eastern alps (this study). The Erzgebirge garnet–rutile CORs are not described in

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555   sufficient detail to judge whether they are statistical or specific, so are not included in the

556   discussion below.

557   The axis relationship $<103>_{\text{rutile (Rt)}} \parallel <111>_{\text{Grt}}$ is found at every locality, but there are

558   differences in the arrangement of rutile *a*-axes in {111} garnet planes between the localities. In

559   Idaho star garnet there are reportedly multiple specific CORs involving $<103>_{\text{Rt}} \parallel <111>_{\text{Grt}}$,

560   with COR-2/2' rutile *a*-axes parallel to $<4\text{-}3\text{-}1>_{\text{Grt}}$ (the sole COR present in one garnet analyzed),

561   COR-3 rutile *a*-axes parallel to $<2\text{-}1\text{-}1>_{\text{Grt}}$ and COR-1 rutile *a*-axes parallel to $<1\text{-}10>_{\text{Grt}}$

562   (Hwang et al. 2015). This last axis relationship is found *only* in the Idaho garnets. In contrast,

563   there is a single rotational statistical COR around $<103>_{\text{Rt}} \parallel <111>_{\text{Grt}}$ reported for rutile needles

564   in garnet from the Rhodope and from equant rutile inclusions in this study (subgroup R3a), with

565   rutile *a*-axes found at all points in the garnet {111} plane apart from close to garnet $<1\text{-}10>$

566   directions (this study fig. 5; Proyer et al. 2013). The dataset is of limited size, but the same

567   rotational statistical COR also seems to be shared by inclusions with $<103>_{\text{Rt}} \parallel <111>_{\text{Grt}}$ in the

568   Sulu garnets (Hwang et al. 2007, 2015). Rutile inclusions with *c*-axes concentrated on

569   dispersional statistical CORs around garnet $<110>$ directions comprise ca. 50% of the 250

570   inclusions measured in the Wirtbartl samples, but are not observed at any of the other localities.

571   The COR $<001>_{\text{Rt}} \parallel <111>_{\text{Grt}} \& <010>_{\text{Rt}} \parallel <1\text{-}10>_{\text{Grt}}$ is found in the Idaho garnets (where it is

572   designated COR-4), the Rhodope garnets, and in this study (corresponding to subgroup R2a), but

573   is very rare in all cases. CORs involving $<001>_{\text{Rt}} \parallel <001>_{\text{Grt}}$ are found occasionally in the Sulu

574   garnets and commonly in certain Idaho garnets (11 of 58 inclusions measured in one garnet have

575   Hwang et al.'s COR-5; $[001]_{\text{Rt}} \parallel [001]_{\text{Grt}} \& (010)_{\text{Rt}} \parallel (1\text{-}10)_{\text{Grt}}$), such CORs are not found

576   elsewhere.

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577   The data available show that multiple rutile–garnet CORs are common in single localities and

578   that similarities exist between CORs over a wide range of conditions. This suggests strong

579   favorability of certain axis relationships. Whether this is a consequence of energetically

580   favorable lattice-scale interactions or common inclusion formation processes (or both) is

581   unknown. Alongside broad similarities there are variations between (and in the case of the Idaho

582   garnets even within) localities. The two localities with at least one unique COR (Idaho and

583   Wirtbartl) are the two with very different implied conditions of formation to the UHP and

584   granulite garnets. The Wirtbartl data are the only results from equant rutile inclusions rather than

585   needles, this may also contribute to the observed differences. The literature comparison

586   corroborates the impression given by the corundum and ilmenite data that the Wirtbartl garnets

587   exhibit an unusually high number of different CORs for a single locality.

588   **Lattice-based explanations for the Wirtbartl CORs?**

589   A lattice matching (or coherency) model (e.g. Howe 1997; Balluffi et al. 2005) predicts

590   orientation relationships well for phases with similar crystal symmetries and structures.

591   However, the Wirtbartl inclusions have heterophase interfaces, separating different crystal

592   systems and oxygen sublattices. Calculated lattice strain was used to compare parallel sets of

593   planes from observed CORs to examine whether lattice matching can explain their favorability.

594   Physically, lattice mismatches may be accommodated by elastic strain, misfit dislocations or an

595   incoherent interface (Howe 1997).

596   Tables 1 – 3 list the sets of parallel garnet and inclusion plane poles or directions that define the

597   largest COR (sub)groups. Whenever directions are listed, the indices of the direction are

598   identical to the pole of a plane with equivalent indices. A pair of parallel related planes was

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599   designated *(hkl)* for garnet and *(mno)* for inclusions. The d-spacings of sets of garnet planes

600   *(HKL)* = x*(hkl) and inclusion planes *(MNO)* = y*(mno) were used to calculate lattice strains.

601   The variables *x* and *y* are positive scalar integers. Calculated lattice strains depend on the size of

602   *x* and *y*, referred to here as the 'order' of the *(HKL)* and *(MNO)* planes. In this work low-order

603   planes are preferred, as these are more likely to correspond to layers of atoms in the crystal. The

604   lowest-order pair of planes that could achieve a strain of between -0.04 and +0.04 (an arbitrary

605   target) was determined for each planar relationship in tables 1 – 3. Lattice strain was calculated

606   as $\frac{d_{(MNO)\ inclusion} - d_{(HKL)\ garnet}}{d_{(HKL)\ garnet}}$, where $d_{(MNO)}$ represents the d-spacing of *(MNO)* planes. If only

607   very high order planes met the target, the strain for a 1:*x* or *y*:1 ratio of orders was calculated for

608   comparison purposes, with *x* (or *y*) chosen to minimize the lattice strain. The results are given in

609   tables 4 – 6. Bolded relationships are those where the target lattice strain can be achieved using

610   orders ≤ 3, assumed to indicate the best matches.

611   Using $d_{inclusion}$ as the denominator instead has negligible effect for small lattice strains. For lattice

612   strains > 0.1 there is a difference of ≥ 20%. The effect of pressure has been neglected as the

613   pegmatites formed at no more than 0.3 GPa (Habler et al. 2007). Calculations used lattice

614   constants measured at room pressure and at room temperature and 600ºC (table S3). Room

615   temperature values are discussed here; lattice strains calculated using cell parameters at 600ºC

616   differ by ≤ 0.01 (tables S4-S6).

617   The lattice-matching hypothesis posits that common, specific CORs should have multiple good

618   d-spacing fits between inclusion and host, with rotational CORs occurring where one set of

619   planes has a much better fit than the planes oriented at a high angle to them.

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620   **Rutile CORs (table 4).** A good low-indexed fit was not found for the relationship $\{001\}_{\text{rutile (Rt)}}$

621    $\|$ $\{110\}_{\text{garnet (Grt)}}$, which fits with the observation that although rutile c-axes are concentrated near

622   garnet <110> directions there is significant dispersion (subgroup R1a, group R1*, fig. 4). The

623   calculated fits for the rutile $\{100\}$ plane relationships of subgroup R1a are good, including a 1:1

624   correspondence between $\{100\}_{\text{Rt}}$ and $\{112\}_{\text{Grt}}$ with only 3% misfit. Despite this, rutile a-axes

625   show similar amounts of dispersion to the c-axes for subgroup R1a, and the relationship

626    $\{100\}_{\text{Rt}}\|$ $\{112\}_{\text{Grt}}$ is absent in group R1*.

627   Only one of the three sets of planes examined for each COR in subgroups R2a and R3b shows a

628   good calculated fit with garnet. Despite this, neither COR shows a rotational component,

629   although both are rare as would be expected for poorly fitting CORs.

630   In subgroup R3a a single rutile <103> direction (pole to a $\{405\}$ rutile plane) is aligned

631   (sub)parallel to garnet <111>. There is a poor fit between rutile $\{405\}$ planes and garnet, the

632   most plausible relationship being $\{405\}_{\text{Rt}}\|$ $\{12\ 12\ 12\}_{\text{Grt}}$ (lattice strain 0.06). However, the

633   <103> rutile vector is almost exactly equal to half the <111> garnet vector (misfit strain only

634   0.004). Despite poor agreement between $\{405\}$ rutile planes and garnet plane families parallel to

635    $\{111\}$, the similarity between crystal vector lengths somehow favors this axial orientation

636   relationship. Rutile inclusions can rotate around the fixed <103> direction despite the good fits

637   exhibited by rutile $\{100\}$ planes.

638   **Corundum CORs (table 5).** Despite only one set of planes having a low-indexed, low lattice

639   strain fit with garnet, subgroup C1a is specific and also the commonest corundum COR.

640   Subgroup C2a is slightly less common than subgroup C1a, despite being the *only* COR for which

641   three perpendicular sets of well-fitting planar relationships are calculated. No good low index fit

642   exists for the only fixed set of planes of the group C4 rotational statistical COR. No rotational

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643   statistical COR is developed around the much better fitting pair of $\{10\text{-}10\}_{\text{corundum}} \| \{220\}_{\text{Grt}}$

644   planes (lattice strain -0.01).

645   **Ilmenite CORs (table 6).** Ilmenite subgroups I1a and I2a share the same COR as corundum

646   subgroups C1a and C2a. But whereas in subgroup C1a the $\{10\text{-}10\}$ planes achieve the lowest

647   lattice strains with garnet, in subgroup I1a the best fits were achieved by planes parallel to

648    $\{0001\}$. This does fit with the greater number of inclusions rotated around their c-axes for

649   ilmenite as compared to corundum (compare subgroup C1c, 1% of all corundum orientations,

650   with subgroup I1c, 7% of all ilmenite orientations).

651   In group I3, the only good alignment is $\{33\text{-}60\}_{\text{Ilm}} \| \{888\}_{\text{Grt}}$ (lattice strain -0.01). The fact that

652   these are the only fixed planes of a rotational statistical COR may suggest that this high-indexed

653   planar relationship is actually favorable.

654   **Evaluation.** The calculated lattice strains and plane indices are not very effective at explaining

655   the CORs observed. Although at least one set of low-indexed inclusion planes usually fits well

656   with garnet for each group/subgroup, the results do not reflect the observed relative frequencies

657   of each COR and cannot explain why a particular COR is specific or statistical. An interface-

658   scale factor not addressed here is the nature of bonding across the host–inclusion interface.

659   Strong (and thus energetically favorable) bonds between atoms preferentially exposed at certain

660   orientations of interface planes could encourage specific relationships that appear unfavorable

661   due to lattice strain alone.

662   It appears that the continuation of symmetry elements between host and inclusion has a strong

663   influence on CORs. Many CORs with only a single set of well-fitting planes are nonetheless

664   specific rather than rotational statistical, and the same direction (the $\{11\text{-}20\}$ pole) is the axis of a

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665   rotational statistical COR for both trigonal phases, despite the fact that for corundum in

666   particular, other planes would theoretically have better fits. One possible factor which could

667   favor continuation of symmetry elements is the minimization of elastic strain energy between

668   host and inclusion at a larger scale than individual lattice planes, controlling CORs by the

669   interaction of host and inclusion elastic properties. These do have several characteristics similar

670   to statistical CORs. The {111} planes in garnet, populated by rutile a-axes of the subgroup R3a

671   rotational statistical COR, are planes of constant garnet stiffness. Regions of shallow gradients in

672   elastic properties exist around low-indexed garnet crystallographic directions, coinciding with

673   axis relationships where dispersion of rutile directions is seen. This explanation has difficulty

674   explaining the importance of the rutile <103> direction however, as this is a direction of neither

675   minimum nor maximum stiffness in rutile, and the resulting conical distribution of the stiff

676   (relative to garnet) rutile c-axis does not follow contours of constant garnet stiffness.

677   **Implications**

678   This work shows that multiple coexisting CORs and statistical CORs between host and

679   inclusions are not an isolated quirk of rutile inclusions in garnet. Studies based on relatively

680   small numbers of inclusion orientations have likely overlooked statistical CORs and

681   underestimated the true variety of CORs present, with implications for interpretations of

682   inclusion origins.

683   It is essential to test the above hypothesis and discover how widespread the features of CORs

684   identified in the Wirtbartl garnets are. Future studies of host–inclusion systems should involve

685   large numbers of measurements in order to accommodate the concept of statistical CORs and

686   obtain a representative picture of the frequency of the different CORs detected. EBSD is the

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687   optimum method to achieve COR characterization within a reasonable timeframe. Context from

688   EBSD measurements greatly increases the value of any TEM data obtained on individual

689   inclusions and avoids unrepresentative conclusions.

690   The CORs defined for a given sample should be guided by the amount of data available, the

691   limitations of the methods employed, the aims of the study, and prior knowledge of the system.

692   As decisions about how to describe a distribution of inclusion orientations can influence the way

693   a dataset is presented, future studies should explicitly discuss their reasons for defining each

694   COR reported. Failure to do this could obscure important aspects of the data.

695   Sufficiently large numbers of measurements of inclusion orientations provide information on

696   many different parameters: which - and how many - CORs each inclusion phase assumes, the

697   relative frequencies of these CORs, whether these CORs are specific or statistical, and the

698   amount of rotation and dispersion of each statistical COR. A survey of rutile inclusion CORs in

699   garnet from multiple localities suggests these parameters are likely affected by processes of

700   inclusion formation / incorporation and/or variables such as pressure, temperature, cooling rate,

701   composition, interface geometry, nucleation rate, or growth rate. An improved understanding of

702   the small and large scale processes controlling the development of the full range of host-

703   inclusion CORs could deliver information not only about the origins of the inclusions involved

704   but also the conditions at the time of formation.

705   It is currently not possible to predict the favorability of particular CORs from knowledge of host

706   and inclusion crystal lattices. A simple model involving the minimization of misfits between

707   parallel sets of host and inclusion lattice planes could not fully explain the frequency or

708   characteristics of the CORs observed in the Wirtbartl samples, implying that unaccounted for

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709   interface-scale factors (e.g. atomic bonding), long range interactions such as elastic strain and/or

710   the formation mechanisms of the inclusions may be important factors. Combined EBSD and

711   TEM studies of systems where the origin of inclusions is independently known are necessary to

712   determine the influence of inclusion formation processes on the resulting CORs. Improved

713   computer models of the 3D atomic structure of interfaces will make it possible to probe the

714   influence of other variables on the favorability of different CORs. An ultimate goal would be to

715   be able to divide inclusions into COR groups based on physical characteristics of their interfaces

716   and genetic considerations.

717   **Acknowledgements**

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864   **Figure Captions**

865   FIGURE 1. Transmitted plane polarized light micrographs of thin sections show concentric (**a**)

866   and sector (**b**) zoning in Wirtbartl metapegmatite garnets, defined by variations in inclusion

867   abundances, grain sizes and habits. Inclusion trails with bleaching zones (Griffiths et al. 2014)

868   crosscut the zoning. Oscillatory zoning visible at bottom right of (**a**).

869   FIGURE 2. Inclusion EBSD measurement domains A (**a-d**) and B (**e-h**). Optical overviews of

870   each domain [(**a**) and (**e**)] show the regions from which inclusion orientations were obtained

871   (black dashed lines), the number of measurements made, and the positions of optical close-ups

872   [(**c**) and (**g**), pink rectangles] and BSE images [(**d**) and (**h**), orange rectangles]. (**b**) and (**f**)

873   provide optical context, the areas shown in (**a**) and (**e**) are indicated by yellow polygons.

874   FIGURE 3. The orientation distribution function (ODF) of all measured rutile inclusion <001>

875   directions, plotted relative to a fixed garnet orientation (antipodal, equal angle, upper hemisphere

876   pole figure). The halfwidth (HW) and intensity of the ODF are indicated to the right of the pole

877   figure, and the ODF color scale is shown below. Garnet crystallographic directions are indicated

878   by colored squares and triangles, see legend above the pole figure. Colored small circles indicate

879   rutile *c*-axis criteria used to define the groups of rutile inclusions set out in table 1: R1 = dark

880   grey, R1* = light blue, R3 = red. Group R2 *c*-axis maxima are hidden by overlying garnet <111>

881   symbols.

882   FIGURE 4. EBSD data from rutile inclusions in groups R1 and R1* plotted relative to a fixed

883   garnet orientation. Both plots are antipodal, equal angle, upper hemisphere pole figures. Garnet

884   directions are indicated by colored squares and triangles, see legend in figure 3. (**a**) Orientation

885   of rutile <001> (red) and <100> (blue) directions for group R1. Dark grey small circles have a

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886   radius of 5°. (**b**) Histogram showing the distribution of misorientation angles (in degrees)

887   between rutile *c*-axes and garnet <110> directions for groups R1 and R1*. Bins are 1° wide. (**c**)

888   Orientation of rutile <001> directions for groups R1 (red) and R1* (light blue). Also plotted is an

889   ODF of group R1* <100> directions (color scale as in fig. 3). The halfwidth (HW), minimum

890   and maximum intensity of the ODF are indicated to the right of the pole figure. Small circles of

891   5° (dark grey) and 22° (light blue) are drawn around the garnet [0-11] direction. A fourfold

892   rotation was used to combine symmetrically equivalent inclusion data into a single pole figure

893   quadrant (see section 'pole figure plot construction').

894   FIGURE 5. EBSD data from rutile inclusions in subgroups R3a and R3b plotted relative to a

895   fixed garnet orientation. All plots are antipodal, equal angle, upper hemisphere pole figures.

896   Garnet directions are indicated by colored squares and triangles, see legend in figure 3. A

897   fourfold rotation was used to combine inclusion data from symmetrically equivalent garnet

898   directions into a single pole figure quadrant for all plots (see section 'pole figure plot

899   construction'). Red small circles are at inclination angles of 26° and 31° from garnet [111]. (**a**)

900   The orientation of rutile <001> (red, **i**+**ii**), <100> (blue, **i**) and <103> (blue, **ii**) directions for

901   subgroup R3a (legend above each figure). Black small circles are at inclination angles of 62° and

902   90° to garnet [111] for (**i**) and 38° and 55° to garnet [111] for (**ii**). (**b**) The orientation of rutile

903   <001> (red, **i**+**ii**) and <100> (blue, **i**) directions and {101} (blue, **ii**) plane poles for subgroup

904   R3b (legend above each figure). Black small circles are at inclination angles of 62° and 90° to

905   garnet [111] for (**i**).

906   FIGURE 6. EBSD data from corundum inclusions in groups C1 (**a**), C2 (**b**) and C4 (**c**) plotted

907   relative to a fixed garnet orientation. Poles to corundum {0001} planes are indicated in all plots

908   as red circles. In addition, the left column of plots (**i**) shows corundum {11-20} plane poles

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909   (blue) and the right column (**ii**) shows {10-10} poles (blue) for each group. All plots are

910   antipodal, equal angle, upper hemisphere pole figures. Garnet directions are indicated by colored

911   squares and triangles, see legend in figure 3. A fourfold rotation was used to combine inclusion

912   data from symmetrically equivalent garnet directions into a single pole figure quadrant for all

913   plots (see section 'pole figure plot construction'). Black small circles indicate (**a**) garnet {112}

914   planes (**b**) a garnet {111} plane (**ci**) a garnet {111} plane and a cone inclined at 60° to garnet

915   [111] and (**cii**) a garnet {111} plane and a cone inclined at 30° to garnet [111].

916   FIGURE 7. EBSD data from ilmenite inclusions in groups I1 (**a**), I2 (**b**) and I3 (**c**) plotted

917   relative to a fixed garnet orientation. Poles to ilmenite {0001} planes are indicated in all plots as

918   red circles. In addition, the left column of plots (**i**) shows ilmenite {11-20} plane poles (blue) and

919   the right column (**ii**) shows {10-10} poles (blue). All plots are antipodal, equal angle, upper

920   hemisphere pole figures. Garnet directions are indicated by colored squares and triangles, see

921   legend in figure 3. A fourfold rotation was used to combine inclusion data from symmetrically

922   equivalent garnet directions into a single pole figure quadrant for all plots (see section 'pole

923   figure plot construction'). Black small circles indicate (**a**) garnet {112} planes (**b**) a garnet {111}

924   plane (**ci**) a garnet {111} plane and a cone inclined at 60° to garnet [111] and (**cii**) a garnet {111}

925   plane and a cone inclined at 30° to garnet [111].

926   FIGURE 8. Equal angle projection plot of rutile orientation data adapted from Hwang et al.

927   (2007). The original plot is underlain by small circles at 28° and 33° to one garnet <111>

928   direction (red continuous lines) and small circles at 57° and 90° to the same direction (blue

929   dotted lines, dots 2° apart). Garnet <134> (orange triangles) and <112> (green triangles)

930   directions in the (-11-1) garnet plane are plotted, and do not coincide with rutile a-axes a_1 or $a_3 -$

931   a_6, which belong to rutile inclusions with c-axes (c_1 & $c_3 - c_6$) inclined on cones to garnet [-11-1]

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932   (red small circles). Figure used by permission of John Wiley and Sons, from Hwang et al.

933   (2007), Journal of Metamorphic Petrology, vol. 25, Fig. 3, p. 354.

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Tables

TABLE 1. Relationships between crystallographic directions of rutile inclusions and host garnet

Group	rt c-axis ∥ grt <uvw>	N (gp.)	Largest subgroup(s)	(sub)group rt a-axis ∥ grt <uvw>	(sub)group rt {101} ∥ grt <uvw>	(sub)group rt <103> ∥ grt <uvw>	N (sgp.)
R1	grt <110> (±5°)	43	R1a	grt <111> (±5°) (1ax) grt <112> (±5°) (1ax)	-	-	39
R1*	grt <110> (>5°, <22°)	84	-	concentrated at grt <111> (1ax)	n.o.	n.o.	-
R2	grt <111>	4	R2a	grt <110> (1ax) grt <112> (1ax)	-	-	3
R3	Cone around grt <111> (28.5° ± 2.5)	103	R3a	1ax in grt {111} plane (±5°), avoid grt <110>	n.o.	grt <111> (±5°) (1ax)	80
			R3b	Never in grt {111} plane 1ax near grt <112>	grt <110> (1ax)	n.o.	14
RX	n.o.	16	-	n.o.	n.o.	n.o.	-

Notes: rt = rutile; grt = garnet; gp. = group; sgp = subgroup; n.o. = not observed. The largest subgroup in each group is detailed in this table. Additional subgroups with N ≥10 are also included. Where two orientation relationships are enough to define a specific COR, the other columns are left blank (-).The number of symmetrically equivalent crystallographic directions which follow each relationship is indicated (1ax = one direction, 2ax = 2 directions, no comment = all equivalent directions share the relationship).

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TABLE 2. Relationships between crystallographic directions of corundum inclusions and host garnet

Group	crn c-axis ∥ grt <uvw>	N (gp.)	Largest subgroup	(sub)group crn a-axis ∥ grt <uvw>	(sub)group crn {10-10} pole ∥ grt <uvw>	N (sgp.)
C1	grt <112>	69	C1a	grt <111> (1ax) near grt <113> (2ax)	grt <110> (1ax) near grt <135> (2ax)	62
C2	grt <111>	56	C2a	grt <112>	grt <110>	53
C3	grt <100>	3	-	grt <110> (1ax)	grt <110> (1ax)	-
C4	in grt {111}	28	-	grt <111> (±5°)	1ax in grt {111} plane (±5°)	-
CX	n.o.	24	-	n.o.	n.o.	-

Notes: crn = corundum; grt = garnet; gp. = group; sgp = subgroup; n.o. = not observed. The largest subgroup in each group is detailed in this table. No additional subgroups with N ≥ 10 were found. The number of symmetrically equivalent crystallographic directions which follow each relationship is indicated (1ax = one direction, 2ax = 2 directions, no comment = all equivalent directions share the relationship).

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TABLE 3. Relationships between crystallographic directions of ilmenite inclusions and host garnet

Group	ilm c-axis $\parallel$ grt <uvw>	N (gp.)	Largest subgroup	(sub)group ilm a-axis $\parallel$ grt <uvw>	(sub)group ilm {10-10} pole $\parallel$ grt <uvw>	N (sgp.)
I1	grt <112>	28	I1a	grt <111> (1ax) near grt <113> (2ax)	grt <110> (1ax) near grt <135> (2ax)	21
I2	grt <111>	21	I2a	grt <112>	grt <110>	20
I3	in grt {111}	35	-	grt <111> (±5°)	1ax in grt {111} plane (±5°)	-
IX	n.o.	16	-	n.o.	n.o.	-

Notes: ilm = ilmenite; grt = garnet; gp. = group; sgp = subgroup; n.o. = not observed. The largest subgroup in each group is detailed in this table. No additional subgroups with N ≥ 10 were found. The number of symmetrically equivalent crystallographic directions which follow each relationship is indicated (1ax = one direction, 2ax = 2 directions, no comment = all equivalent directions share the relationship).

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TABLE 4. Calculation of lattice strains for parallel sets of rutile and garnet planes determined using EBSD.

(Sub)group	CORs from EBSD (format: rt $\parallel$ grt)	Lowest index planes (-0.04 ≤ ε ≤ 0.04) (format: rt $\parallel$ grt)	ε	Best fit 1 : x d-spacing ratio (format: rt $\parallel$ grt)	ε (1 : x d-spacing ratio)
R1a	{001} $\parallel$ {110}	{003} $\parallel$ {880}	0.04	{001} $\parallel$ {330}	-0.08
	{100} $\parallel$ {112} *(1ax)*	**{100} $\parallel$ {112}**	**0.03**	-	-
R1a / R1*	**{100} $\parallel$ {111} *(1ax)***	**{200} $\parallel$ {333}**	**-0.03**	-	-
R2a	{001} $\parallel$ {111}	{003} $\parallel$ {777}	-0.03	{001} $\parallel$ {222}	0.12
	{100} $\parallel$ {112} *(1ax)*	**{100} $\parallel$ {112}**	**0.03**	-	-
	{100} $\parallel$ {110} *(1ax)*	{004} $\parallel$ {777}	0.02	{100} $\parallel$ {220}	-0.12
R3a	**<103> $\parallel$ <111>**	**<206> $\parallel$ <111>**	**0.00**	-	-
	{405} $\parallel$ {111}	{405} $\parallel$ {13 13 13}	-0.02	{405} $\parallel$ {12 12 12}	0.06
R3b	{001} $\parallel$ {113}	{005} $\parallel$ {6 6 18}	-0.02	{001} $\parallel$ {113}	0.15
	{100} $\parallel$ {112} *(1ax)*	**{100} $\parallel$ {112}**	**0.03**	-	-
	{101} $\parallel$ {110}	{303} $\parallel$ {10 10 0}	-0.01	{101} $\parallel$ {330}	0.09

Notes: rt = rutile; grt = garnet; ε = calculated lattice strain. Lattice strains given to 2 decimal places, at this degree of precision errors in lattice constants used for the calculation are too small to affect the result. Bolded relationships are those where the target lattice strain can be achieved with a simple 1:x or 2:x d-spacing ratio. The number of symmetrically equivalent crystallographic directions which follow each relationship is indicated (1ax = one direction, no comment = all equivalent directions share the relationship).

963

46

964

TABLE 5. Calculation of lattice strains for parallel sets of corundum and garnet planes determined using EBSD.

(Sub)group	CORs from EBSD (format: crn ‖ grt)	Lowest index planes (-0.04 ≤ ε ≤ 0.04) (format: crn ‖ grt)	ε	Best fit 1 : x d-spacing ratio (format: crn ‖ grt)	ε (1 : x d-spacing ratio)
C1a	{0001} ‖ {112}	{0008} ‖ {336}	-0.03	{0003} ‖ {112}	0.08
	{11-20} ‖ {111} *(1ax)*	{4 4 -8 0} ‖ {11 11 11}	0.02	{11-20} ‖ {333}	-0.07
	{10-10} ‖ {110} *(1ax)*	**{10-10} ‖ {220}**	**-0.01**	-	-
C2a	**{0001} ‖ {111}**	**{0002} ‖ {111}**	**0.03**	-	-
	{11-20} ‖ {112}	**{11-20} ‖ {224}**	**-0.01**	-	-
	{10-10} ‖ {110}	**{10-10} ‖ {220}**	**-0.01**	-	-
C3	{0001} ‖ {001}	{0007} ‖ {006}	0.04	{0001} ‖ {001}	-0.12
	{11-20} ‖ {110} *(1ax)*	{22-40} ‖ {770}	-0.02	{11-20} ‖ {330}	0.13
	{10-10} ‖ {110} *(1ax)*	**{10-10} ‖ {220}**	**-0.01**	-	-
C4	{11-20} ‖ {111} *(1ax)*	{4 4 -8 0} ‖ {11 11 11}	0.02	{11-20} ‖ {333}	-0.07

Notes: crn = corundum; grt = garnet; ε = calculated lattice strain. Lattice strains given to 2 decimal places, at this degree of precision errors in lattice constants used for the calculation are too small to affect the result. Bolded relationships are those where the target lattice strain can be achieved with a simple 1:x or 2:x d-spacing ratio. The number of symmetrically equivalent crystallographic directions which follow each relationship is indicated (1ax = one direction, no comment = all equivalent directions share the relationship).

965

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TABLE 6. Calculation of lattice strains for parallel sets of ilmenite and garnet planes determined using EBSD.

(Sub)group	CORs from EBSD (format: ilm ‖ grt)	Lowest index planes (-0.04 ≤ ε ≤ 0.04) (format: ilm ‖ grt)	ε	Best fit 1 : x d-spacing ratio (format: ilm ‖ grt)	ε (1 : x d-spacing ratio)
I1a	**{0001} ‖ {112}**	**{0003} ‖ {112}**	**0.01**	-	-
	{11-20} ‖ {111} *(1ax)*	{33-60} ‖ {888}	-0.01	{11-20} ‖ {333}	-0.14
	{10-10} ‖ {110} *(1ax)*	{50-50} ‖ {990}	-0.01	{10-10} ‖ {220}	-0.08
I2a	{0001} ‖ {111}	{0 0 0 13} ‖ {6 6 6}	0.03	{0002} ‖ {111}	-0.05
	{11-20} ‖ {112}	{5 5 -10 0} ‖ {9 9 18}	0.03	{11-20} ‖ {224}	-0.08
	{10-10} ‖ {110}	{50-50} ‖ {990}	-0.01	{10-10} ‖ {220}	-0.08
I3	{11-20} ‖ {111}	{33-60} ‖ {888}	-0.01	{11-20} ‖ {333}	-0.14

Notes: ilm = ilmenite; grt = garnet; ε = calculated lattice strain. Lattice strains given to 2 decimal places, at this degree of precision errors in lattice constants used for the calculation are too small to affect the result. Bolded relationships are those where the target lattice strain can be achieved with a simple 1:x or 2:x d-spacing ratio. The number of symmetrically equivalent crystallographic directions which follow each relationship is indicated (1ax = one direction, no comment = all equivalent directions share the relationship).
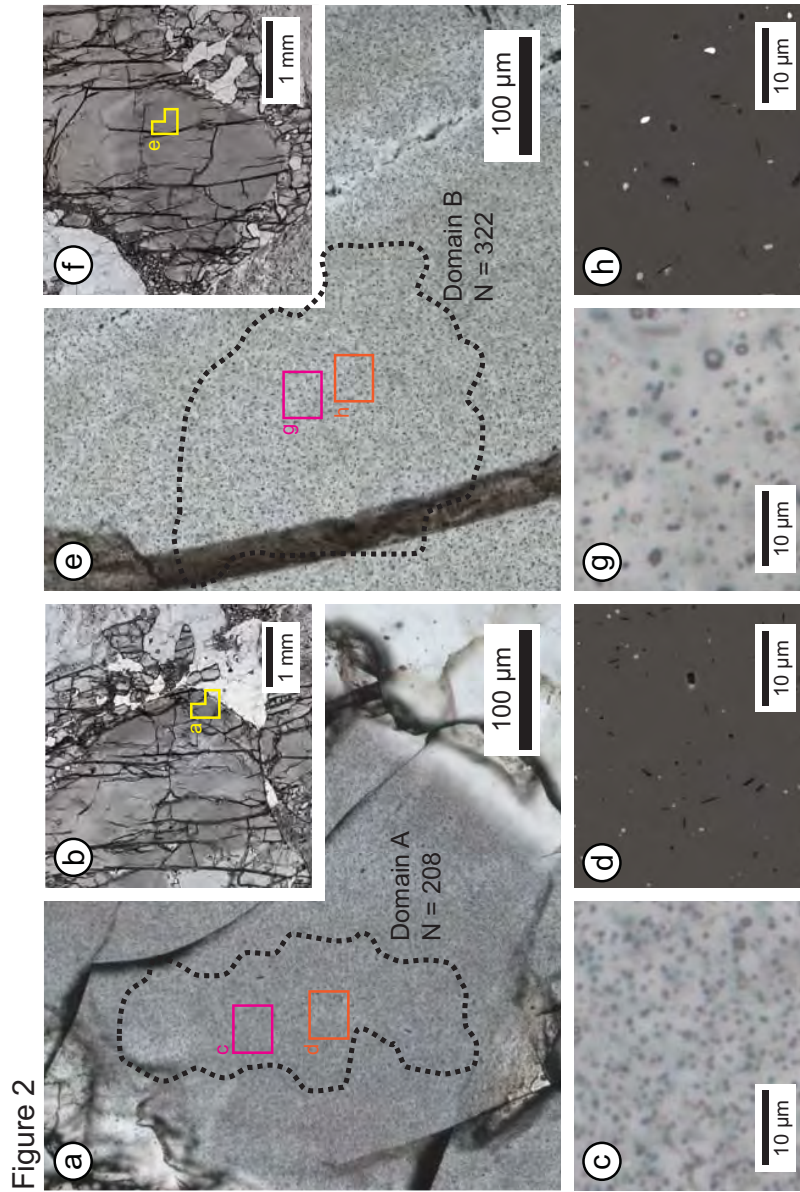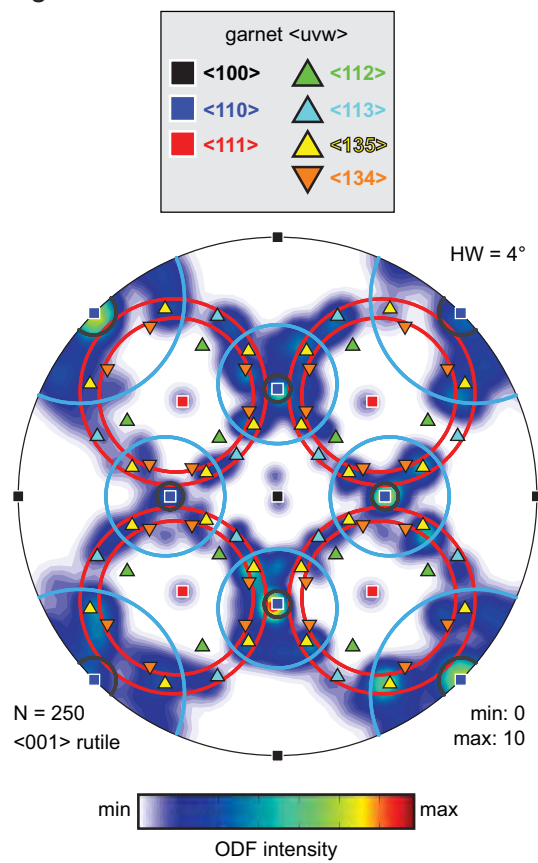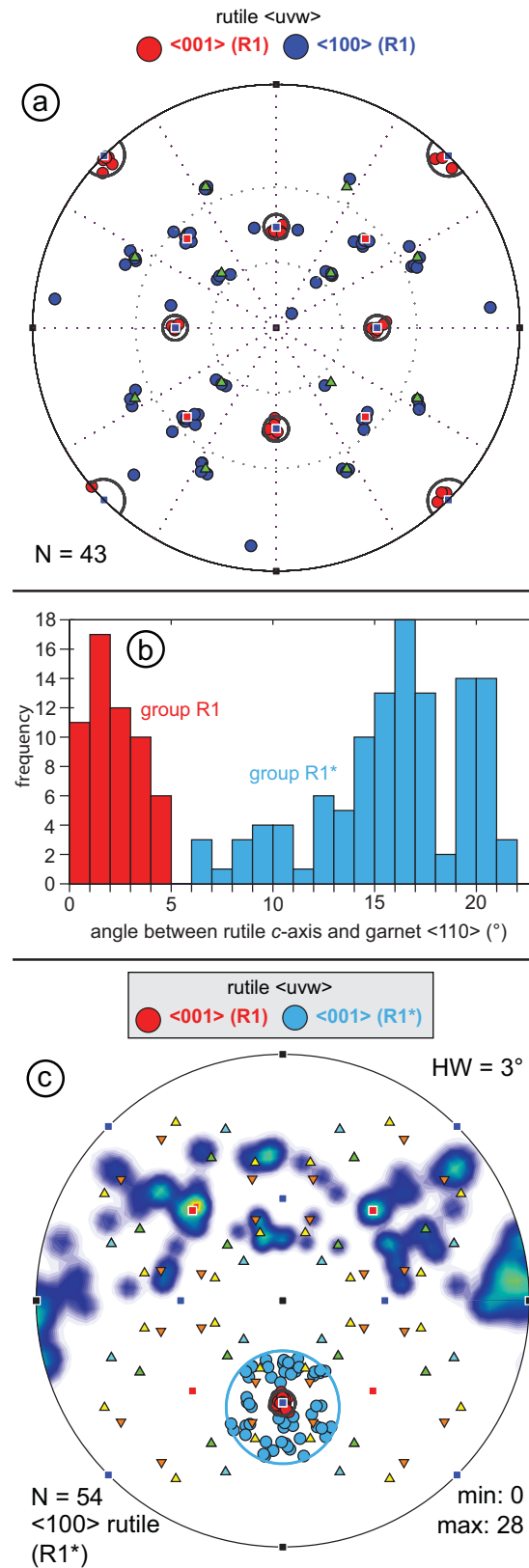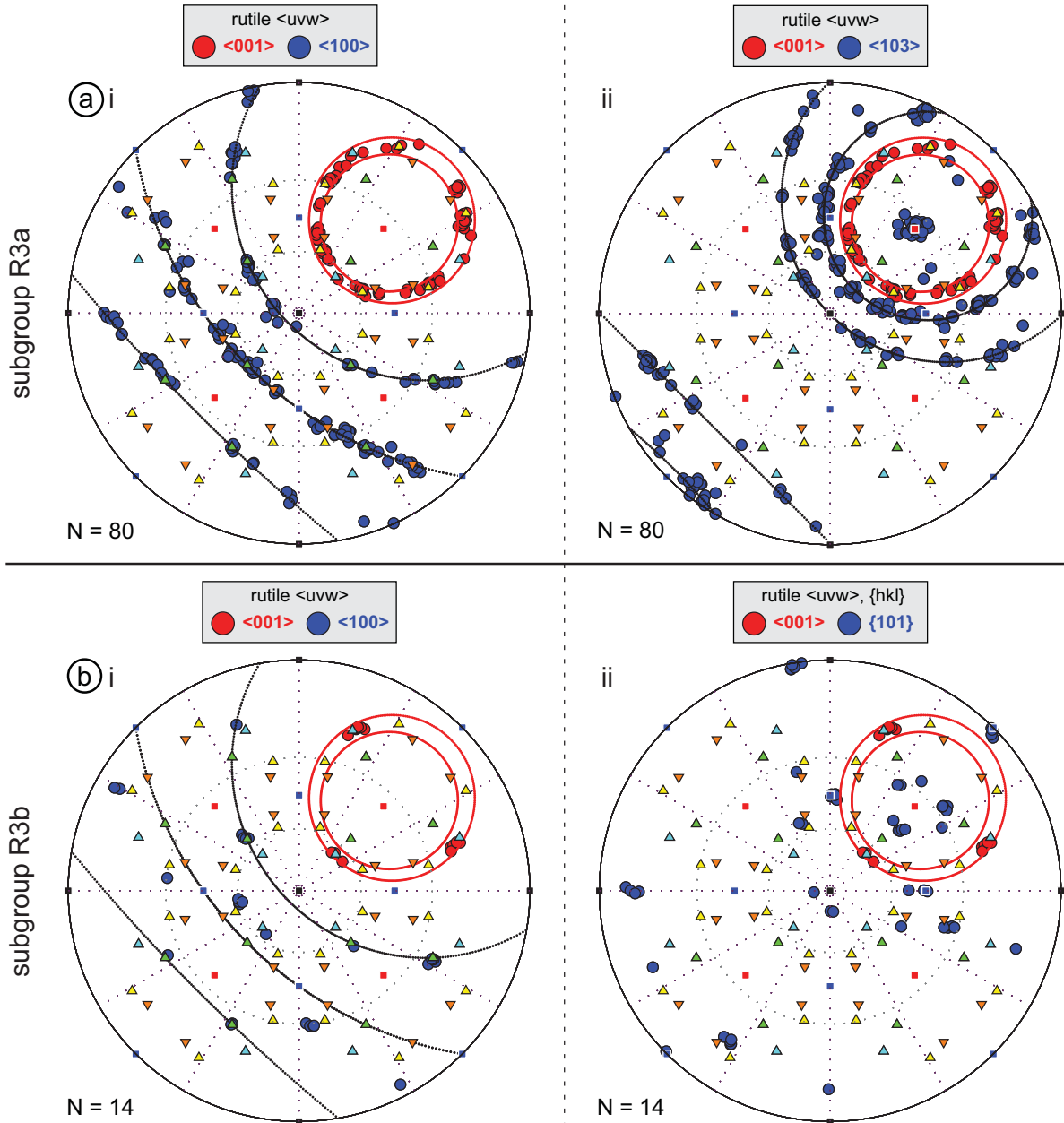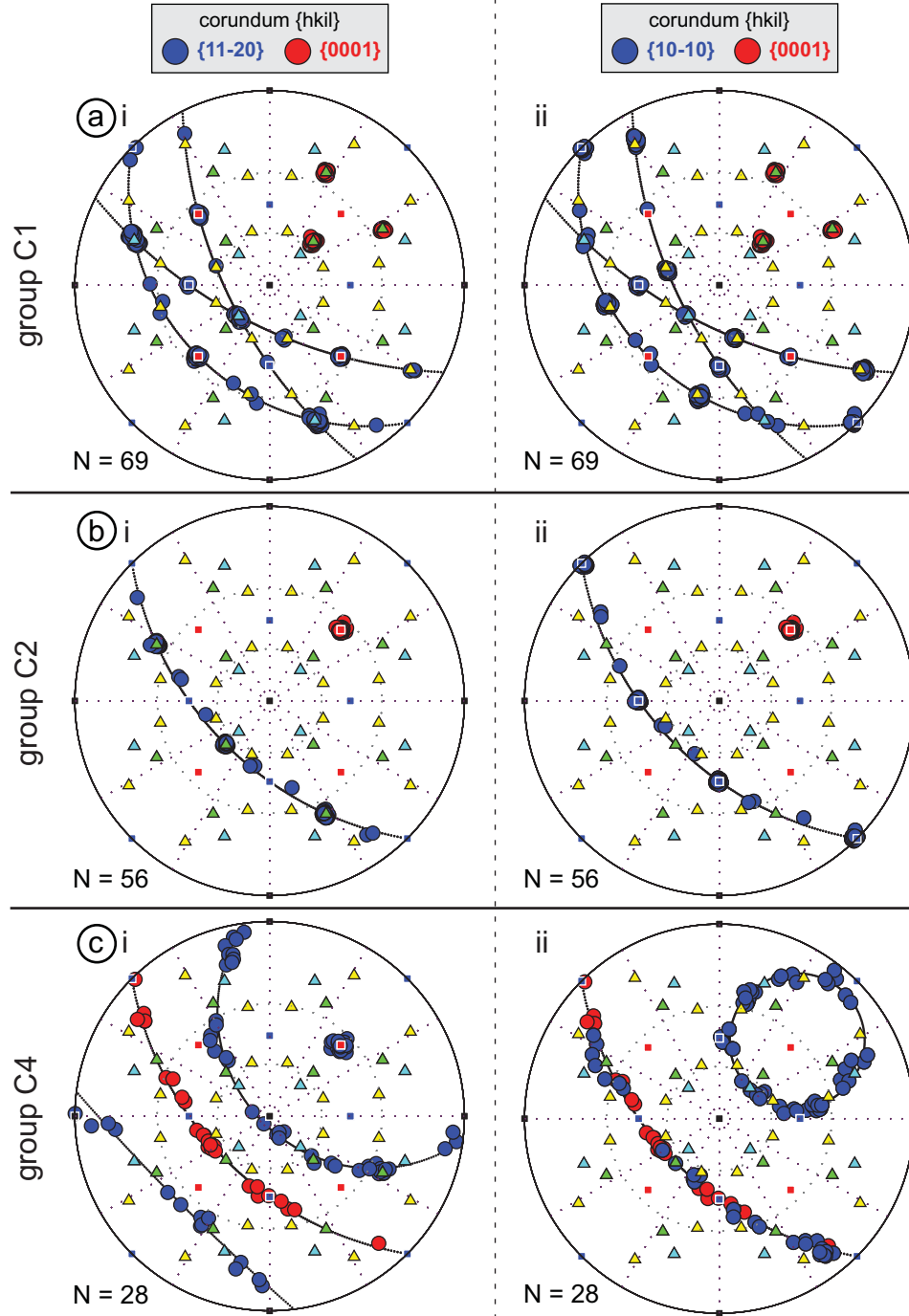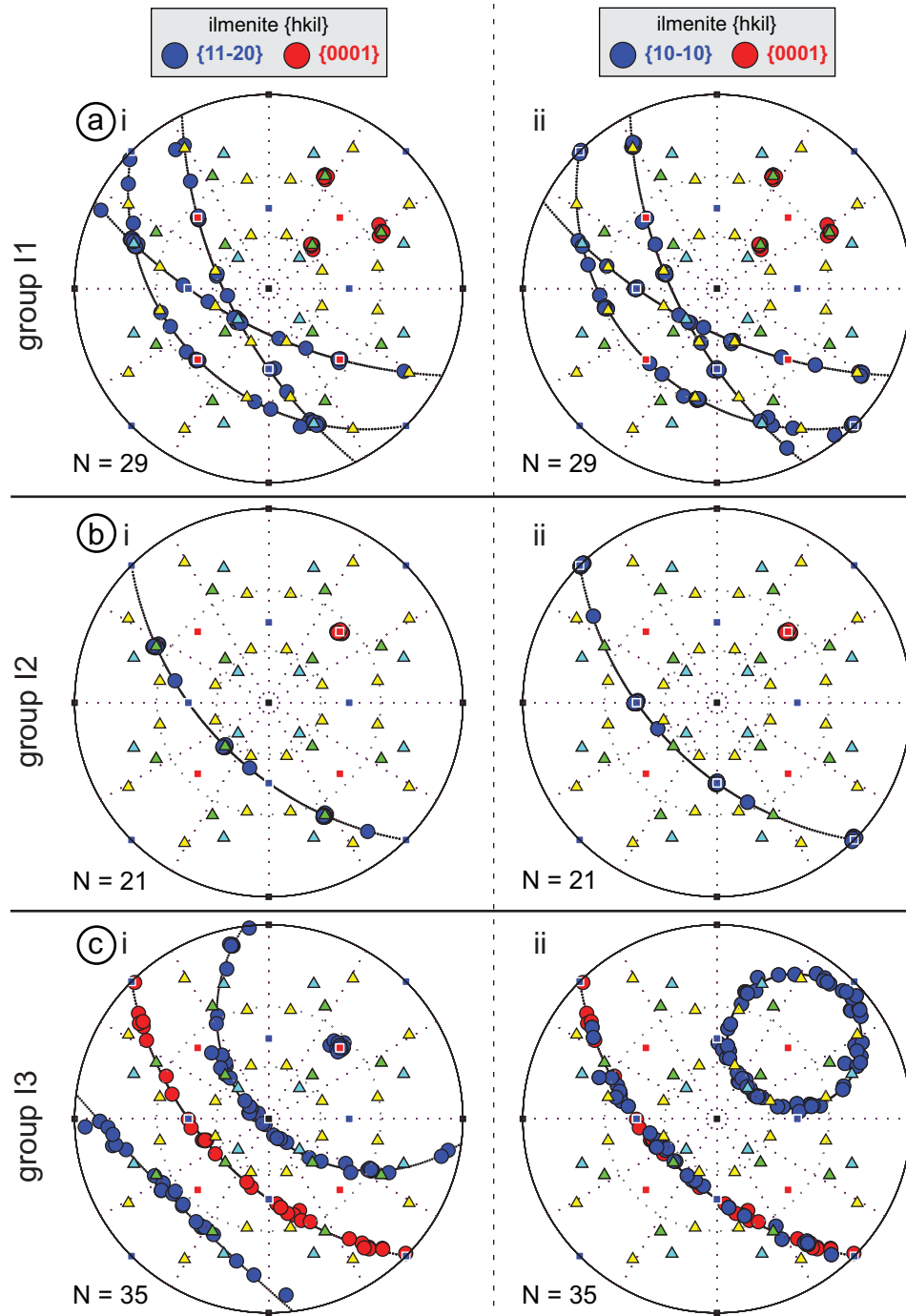
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47

Figure 1
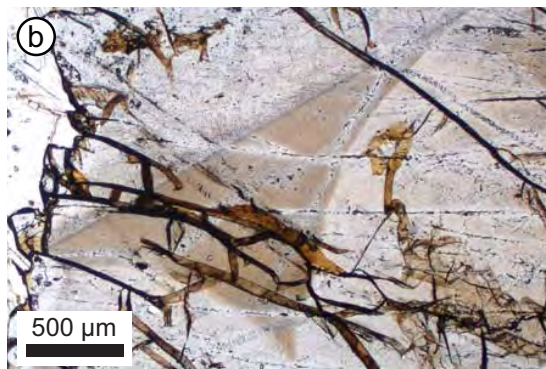
Figure 2

Figure 3

Figure 4

Figure 5

Figure 6

Figure 7

Figure 8