

Revision-1

A spreadsheet for calculating normative mole fractions of end-member species for Na-Ca-Li-Fe²⁺-Mg-Al tourmalines from electron microprobe data

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Abstract

This work presents a spreadsheet that calculates the mole fractions of end-member components for simple Na-Ca-Li-Mg-Fe²⁺-Al tourmalines from electron microprobe data. The input includes the B₂O₃ concentration obtained either from direct analysis or by estimation on the basis of stoichiometry. The concentration of Li₂O can either be input from other analysis or estimated by the spreadsheet. The spreadsheet does not address the mole fractions of Cr, V, oxidized or deprotonated tourmaline species, nor account for species involving tetrahedral boron or aluminum. Therefore, the spreadsheet is not a comprehensive tool that includes all IMA approved tourmaline species, and so is not intended for naming tourmalines according to IMA convention. The present method includes a useful subset of end-member species that can be described simply from electron microprobe data and so, akin to a normative mineralogical analysis for rock composition, the calculations are intended to provide a normative result that serves as simple basis for comparing tourmalines that is more direct than names derived from the most abundant species present.

Keywords: tourmaline, formula, mole fractions, end-members, electron microprobe analysis

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Introduction

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Tourmaline is by far the most important mineral phase in the earth's crust that contains

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boron as an essential structural component. A complex borosilicate, the general formula for

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tourmaline can be expressed as $XY_3Z_6(BO_3)_3(T_6O_{18})V_3W$, where most commonly X = (Na, Ca,

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K, or vacancy), Y = (Mg, Fe²⁺, Al, Li, Mn, Ti, Cr³⁺, V³⁺, Z = Al, Fe³⁺, Cr³⁺, V³⁺, Fe²⁺, Mg, or

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vacancy), T = (Si, Al, or B), B = (B or vacancy), V = (OH, O), and W = (OH, O, F, Cl)

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(Hawthorne and Henry 1999; Filip et al. 2012; Henry et al. 2011; Bosi et al. 2012). Simple, yet

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informative, description of tourmaline composition is hindered by naming the mineral for the

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most abundant end-member species present - with or without other compositional modifiers. A

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more direct approach for tourmaline description would result from presentation of the mole

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fractions of end-member species, similar to methods used for other mineral groups such as the

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feldspars and pyroxenes. Despite considerable previous efforts toward calculating tourmaline

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chemical formula, a mole fraction approach has been hindered by the complexity of tourmaline

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crystal chemistry and resultant lack of a simple tool for calculation.

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Calculating a chemical formula for tourmaline from an electron microprobe analysis

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(EMPA) is complicated by the incorporation of up to three elements (B, H, and Li) that are

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difficult or impossible to analyze using fluorescent X-rays. Moreover, the stoichiometric

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abundance of hydrogen can vary due to several coupled substitutions and, thus, change the total

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charge basis that provides the normalizing factor for calculating the chemical formula. Several

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methods and spreadsheets for recalculating composition and formula from EMPA previously

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have been discussed and distributed (e.g., Henry and Dutrow 2002; Selway and Xiong 2002;

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Yavuz et al. 2006; Clark 2007), and these are useful for naming a tourmaline species and/or

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classifying composition using a series of ternary and quaternary diagrams (e.g., Selway and

50 Xiong 2002; Hawthorne and Henry 1999; Henry et al. 2011). The program of Yavuz et al. (2006)
51 calculates the structural formula, including estimation of oxidized species, and provides the
52 relative percentages (mole fractions) of tourmaline types based on X site speciation (sodic,
53 calcic, and vacancy series), but the program does not estimate mole fractions of any tourmaline
54 end-member species. The TOURCOM program of Pesquera et al. (2008) calculates mole
55 fractions of tourmaline species, albeit using a somewhat outdated list of species, but does so
56 from a tourmaline formula as input rather than from compositional (oxide weight percent) data.
57 Hence, to date none of these approaches easily furnish mole fractions of end-member
58 components from an oxide weight fraction analysis, which is unfortunate because component
59 mole fractions would more instructive for conveyance of tourmaline composition in text than a
60 simple name, and so would be more useful for comparing tourmaline compositions and relating
61 those compositions to chemical environment of formation. For example, consider the
62 hypothetical tourmaline composition shown in Table 1. This composition was calculated from a
63 formula corresponding to 40% schorl, 25% dravite, 20% foitite, and 15% olenite on a molar
64 basis. Use of spreadsheets like that of Selway and Xiong (2002) does a fine job of calculating the
65 atomic formula and assigns the name “schorl” to the phase. Although “schorl” is the correct
66 name for this mineral according to the present rules (e.g., Henry et al. 2011), the name does not
67 convey a compositional difference relative to a mineral that is pure schorl. The use of other
68 descriptive or Schaller modifiers along with species name (cf. Henry et al. 2011) can provide
69 more compositional information, but typically yield convoluted names that provide at best a
70 qualitative description of composition. For example “dravitic-foititic-olenitic- schorl” requires
71 about the same number of characters to print, but provides less direct information than
72 $\text{Shl}(40)\text{Drv}(25)\text{Ftt}(20)\text{Oln}(15)\text{xF}(0)$, where xF represents the mole fraction of F in the W site.

73 To date, the lack of use of tourmaline end-member components likely stems from the
74 complexity of tourmaline crystal chemistry and resultant lack of a simple tool for calculation.
75 This work describes a spreadsheet (Morgan_ProportionalTourmalineFormula_09July2015.xls)
76 that calculates the mole fractions of end-member components for Na-Ca-Li-Mg-Fe²⁺-Al
77 tourmalines from electron microprobe data that includes TiO₂ and MnO. The compositional
78 input also includes the B₂O₃ concentration either obtained by direct analysis (e.g., by SIMS or
79 EMPA) or estimated from stoichiometry. The method utilized is based upon a 31 anion formula
80 calculation as discussed by Clark (2007). Although knowledge or estimation of the actual H (i.e.,
81 H₂O) concentration is commonly helpful for accurate calculation of formulae (e.g., Clark 2007;
82 Henry et al. 2011), it is not necessary for the present purpose as the H₂O concentration is used as
83 a variable in the present spreadsheet to optimize the cation formula based upon either or both
84 filling the Y site at 3 atoms per formula unit and/or estimation of the OH site occupancy. It is re-
85 emphasized here that the calculations in this spreadsheet do not include all IMA approved
86 tourmaline species, and that the spreadsheet is not intended to produce a species name according
87 to IMA conventions. Rather, this spreadsheet contains a subset of what are considered to be
88 useful tourmaline end-members that are easily applicable to electron probe data, intended for the
89 simple purpose of normative comparison of composition.

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Methods

92 **Calculational Approach**

93 The approach to calculation was to first develop a spreadsheet (in Microsoft Excel) that
94 calculates a chemical formula based upon a 31 anion normalization (default 62⁻ total anionic
95 charge) from electron microprobe data that includes wt% B₂O₃ (e.g., Clark 2007). The decision
96 to include B₂O₃ concentration in the input was based on several factors: (1) addition of boron

97 reduces unconstrained components to two (Li, H); (2) boron can be analyzed directly by EMPA
98 or SIMS; (3) in cases where boron cannot, or is not, analyzed directly, the B₂O₃ concentration
99 can be estimated by the assumption of stoichiometric abundance (Selway and Xiong 2002; Clark
100 2007); and (4) the desire to accommodate tourmaline compositions that contain boron at the T
101 site. The latter desire partly stems from application to experimental tourmaline synthesis at the
102 University of Oklahoma, of which some products have been shown by both EMPA and other
103 methods (e.g., SIMS, ¹¹B NMR) to contain tetrahedrally-coordinated boron in excess of that
104 required to fill the trigonally-coordinated boron site, along with a concomitant Si deficiency
105 (e.g., London 2011; Guttery 2012).

106 Once a chemical formula is derived from the compositional data, atoms are assigned to
107 structural sites according to current tourmaline nomenclature (e.g., Henry et al. 2011). The moles
108 and subsequent mole fractions of components are then derived using a series of simple “IF” or
109 “IF/AND” logical statements that progressively calculate the moles of end-member species and
110 subtract the associated number of atoms associated with each from the starting stoichiometry,
111 ideally to arrive at a zero residual sum for all elements in the formula. Because they were
112 developed separately, but from a common root file, calculations for lithium-free and lithium-
113 bearing tourmalines are performed on separate sheets that draw their compositions by link to the
114 “front-end” sheet (Sheet 1) on which the user enters the composition and sample name for
115 calculation. Following entry of the composition, the user simply adjusts the water content of the
116 phase to optimize the sums of the Y site and OH site in the field (Li-free or Li-bearing) that is
117 appropriate for the mineral being considered; if necessary, the oxygen (anion) basis also can be
118 adjusted to provide an optimization of ΣYZTB cations (ideal = 18.000) but this is typically only
119 needed in the case of complex, oxidized (deprotonated) compositions. If the Li₂O content is

120 initially unknown, as is usually the case for minerals analyzed by electron probe, the Li-bearing
121 sub-sheet will calculate the approximate Li apfu allowing the user to refine the formula by
122 adjusting the Li_2O concentration on the front-end sheet; in such cases several subtle adjustments
123 of Li_2O and H_2O concentrations may be necessary to optimize the Y and OH site totals. The
124 atoms of Ti in the formula are added to Fe for the mole fraction calculations, and thus are added
125 to the schorl component. This does not produce a large error because Ti typically is present only
126 at trace levels (<0.5 wt%) in reduced tourmalines. A concentration of 0.5 wt% TiO_2 corresponds
127 to only a 2 mol% fictive schorl component in dravite, the Li-free tourmaline for which
128 stoichiometry would be most strongly affected by Ti(Y) substitution because of its low average
129 atomic number. All Ca in lithium tourmaline is calculated as a “hydroxy-liddicoatite” component
130 (not an IMA approved species). The calculations do not distinguish between “fluor-“ or
131 “hydroxy-“ end-members of relevant species, but do provide the mole fractions of F and Cl in
132 the W site (cells K32 & K33) for comparison; because F and Cl are believed not to enter the V
133 site (e.g., Henry et al. 2011), this value is not allowed to exceed 1.00.

134 Performing a normalization series that identifies the dominant species, based upon the
135 most abundant component (cation or vacancy) in the X site and most abundant cation in the Y
136 site (e.g., Henry et al. 2011), and then subtracts its associated cations from the bulk formula
137 would be most in line with the convention used for naming tourmalines (e.g., Henry et al. 2011).
138 Because ratios among Na, Ca, and vacancy in the X site, and among Fe, Mg, Al, and Li in the Y
139 site vary among different tourmaline species, however, such an approach would require a
140 procedure in which the order of calculation of the amounts of different tourmaline species is
141 variable dependent upon bulk composition. Moreover, attempts at such a simple, directly
142 “subtractive” approach commonly run into calculational difficulties involving balance of Mg and

143 Fe with Al in the Y site for tourmalines with significant X site vacancy. A way found to
144 circumvent these issues is to perform calculations for group based upon X site components
145 (sodic, calcic, and vacancy series), and to derive the abundances of Fe and Mg species within
146 these groups according to the Fe/Mg ratio of the bulk composition. Although this approach tends
147 to slightly reduce the calculated norm for the more abundant Fe or Mg species in each group
148 (e.g., schorl versus dravite, foitite versus magnesio-foitite), it typically does not decrease the
149 dominant species enough to affect naming the tourmaline for the most abundant species as
150 derived from simple consideration of chemical formula.

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152 **End-Members Included**

153 The end-member components included in the calculations are listed in Table 2. End-
154 members represented among the common tourmaline species include all except Cr-rich, V-rich,
155 and Fe³⁺-bearing compositions. Although Cr- and V-rich members should be easy enough to
156 accommodate, they are comparatively rare and were not considered a high priority for the
157 present spreadsheet. Calculation of ferric iron species was neglected because of multiple
158 substitution mechanisms that accommodate trivalent cations at the Y crystallographic site, and so
159 results would not be conclusive without direct analysis of Fe³⁺ and/or Li and H that are not
160 amenable to analysis by electron probe. Lithium-rich tourmaline species included in the
161 calculations are elbaite, rossmanite, and (hydroxy-) liddicoatite. Although darrellhenryite,
162 Na(LiAl₂)Al₆(BO₃)₃Si₆O₁₈(OH)₃O, has recently been accepted as a tourmaline species (Novak et
163 al. 2013), it was not included in the present calculations because it would be impossible to
164 resolve from a combination of elbaite and olenite using electron microprobe data.

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Results

167 **Example of calculation for a nominally Li-Free tourmaline**

168 As a starting point, consider calculating the end member mole fractions for the
169 tourmaline composition shown in Table 1. The user enters the known, and/or estimated,
170 concentrations of oxide components and the name of the sample in the blue cells of Sheet 1 of
171 the spreadsheet (Fig. 1a: name in cell C3, oxides in cells B7-B20). After data entry (Fig 1a), note
172 an analytical total less than 100 wt%, calculated sums at the Y crystallographic site (red cells) for
173 both Li-free and Li-bearing tourmalines significantly in excess of 3, and a poor match to the
174 ideal stoichiometry of the phase (40-25-0-0-0-20-0-15, listed in the mole percent sequence
175 schorl-dravite-tsilaisite-uvite-feruvite-foitite-magnesio-foitite-olenite that is used by convention
176 for Li-free tourmalines hereafter). Excesses at the Y site and errors in the end-member
177 components at this stage are due to an incorrect number of cations to charge balance the oxygen
178 (anion) basis of the calculation, so is due to the absence of hydrogen. The easiest logical
179 adjustment to make at this point is to add water by difference, in the amount of 100-(Total),
180 which is 3.18 wt%. The Li-free calculations show that addition of this concentration of water
181 (Fig. 1b) yields a 3.00 apfu sum at the Y site and a sum of YZBT cations of 18.0005, indicating
182 that the calculations are complete. Note that whereas calculation of the mole fractions of species
183 by the Li-free sheet does not exactly reproduce the theoretical stoichiometry used for calculating
184 the tourmaline composition, the Li-bearing sheet does. This is because the Li sheet performs a
185 strictly progressive subtractive calculation routines whereas the Li-free sheet uses a proportional
186 normalization based upon the bulk Mg/Fe ratio for each of the tourmaline groups based upon X
187 site occupancy. Although the Li-bearing sheet performs well for this particular sodium-dominant

188 composition, the simple subtractive method fails for tourmalines with dominant X site vacancy,
189 as discussed above.

190 Discrimination of the Table-1 tourmaline composition from a Li-bearing tourmaline is
191 indicated by the 100 wt% analytical total obtained with added water and a zero estimated Li
192 content from the Li-bearing calculation routine. Note that the OH site total, $=\Sigma V+W$, is 3.55 (Fig
193 1b); this value is correct given the presence of 15 mol% olenite, each mole of which removes 3
194 moles of H. Calculated residuals from the sheet making the Li-Free calculations (Table 5) are
195 very low and essentially represent rounding errors in the calculations.

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197 **Example of calculation for a Li-bearing tourmaline**

198 For a lithium-bearing tourmaline, consider calculation for a 50-50 molar mixture of
199 elbaite and rossmanite. As in the example above, the weight percent values for known oxide
200 components (excluding Li_2O) are entered in the blue cells (Fig. 2a: name in cell C3, oxides in
201 cells B7-B20). Note that in this example, a MgO concentration of 0.001 wt% was added to avoid
202 a division by zero error in the Li-Free sheet (sum of $\text{FeO}+\text{MgO}=0$); this addition is not necessary
203 for calculation of Li-bearing tourmalines. After data entry, again the analytical total is
204 significantly less than 100 wt% and the Y site sum for Li-free calculation is significantly
205 different than 3.00 (Fig. 2a). Identification as a Li-rich tourmaline is apparent from the
206 aluminous nature of the tourmaline, the positive estimated Li content from the Li-bearing
207 calculation, and the Y site sum for the Li-free calculation being much less than 3.00. Among the
208 remaining calculations, the addition of water to the analysis would only decrease the Y site sum
209 further and, hence, the calculations fail for a Li-absent composition. Note at this point that the Y
210 site sum for the Li-bearing calculation is 3.00 because Li is calculated by difference at this site,

211 but that the amount of Li calculated is underestimated. Similar to the previous example, the
212 easiest second step is to add water to obtain the proper OH site total (full at ~3.79 wt% H₂O for
213 this case: Fig. 2b). With the addition of water, note that the cations of Li calculated by the
214 spreadsheet increases, but is less than the ideal value, and that analytical total is still significantly
215 less than 100 wt%. The next step will be to add Li to the analysis. An initial estimate based on
216 difference of the analytical total from 100 wt%, =2.08 wt% Li₂O yields the correct mole
217 fractions of end-members, but provides slightly more Li to the formula (1.29 apfu) than is
218 calculated by the Li-bearing sheet (1.25 apfu), and yields a slightly deficient OH site sum as well
219 (Fig. 2c). Therefore, slight iterative adjustments to both Li₂O and H₂O (Fig. 2d) eventually
220 provide agreement between added and calculated Li, and better sums at the OH site (3.996) and
221 total of YZBT sites (18.002). Upon conclusion of calculation, the sheet performing the Li-
222 bearing calculations again shows zero or near-zero residuals for all components except
223 cumulative Li (which is correct) (Table 5).

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225 **Compositions tested**

226 To test the spreadsheet, the chemical formulae of selected tourmaline stoichiometries
227 were converted to weight percent oxides using a spreadsheet that derives the oxide (and
228 elemental) weight fractions for a phase based upon the numbers of cations and anions in its
229 chemical formula unit. The compositions of Li-absent tourmalines tested include all of the end-
230 members in the calculation (tsilaisite not shown in table), 50-50 molar mixtures of dravite-schorl,
231 dravite-uvite, uvite-foitite, and schorl-foitite, a limited number of ternary compositions, and a
232 variety of more complicated 4- and 5-component theoretical phases plus some natural complex
233 compositions. The compositions and results from calculation for the simple Li-absent phases are
234 provided in Table 4, and those for the more complex Li-absent compositions in Table 5. The

235 residuals resulting from all Li-absent calculations are provided in Table 6. As can be seen, the
236 spreadsheet exactly reproduced the mole fractions of simple unary and binary compositions. As
237 compositions become more complex, there is slightly poorer agreement between theoretical and
238 calculated mole fractions due primarily to the effect of Fe/Mg proportionation among members
239 of the various X-site compositional groups. For example, note that the 50-30-0-20-0-0-0
240 composition yielded 40-40-0-10-10-0-0 because Na and Fe from the schorl component are re-
241 distributed toward dravite and feruvite components. Note that the solution obtained, 40-40-0-10-
242 10-0-0, represents a schorl-dravite that is just as consistent with the stoichiometry of the mineral
243 as the formula used to calculate the composition. This demonstrates a complication with
244 calculating tourmaline mole fractions: a single composition may be described algebraically by
245 more than one combination of accepted tourmaline species. Among the compositions tested
246 (Tables 3 and 4), however, this is one of only two cases noted where the mole fraction
247 calculations made naming the tourmaline for the most abundant species ambiguous or inaccurate
248 in comparison to the mole fractions used to calculate it.

249 Compositions input for Li-bearing tourmalines were calculated in the same manner as for
250 Li-free tourmalines. The compositions tested included elbaite, rossmanite, liddicoatite, a 50-50
251 molar mixture of elbaite-rossmanite, an elbaite(50)foitite(25)olenite(25) molar mixture, and
252 natural elbaitic tourmalines from the Little Three pegmatite (Morgan and London 1999) and
253 Elba, Italy. The results, residuals, and calculated Li atoms per formula unit are shown in Table 6.
254 Again, the spreadsheet faithfully reproduced the ideal mole fractions, and independently
255 calculated the cations of Li present to within 0.01 apfu of the ideal mineral formulae for the
256 calculated compositions. Calculations from the natural “elbaite” shows olenitic, rossmanitic,
257 and even tsilaisite –dominated results, consistent with the observation of Guttery (2012) that no

258 reported natural elbaite has been found to contain more than about 67 mole% of the elbaite end-
259 member.

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Discussion

263 The present spreadsheet faithfully reproduces the formulae and mole fractions of the ideal
264 Li-absent end-members and their simple solid solutions tested here (Table 3). Reproduction of
265 mole fractions for more complex, quaternary and higher, calculated compositions (Table 4)
266 shows less perfect agreement with norms used to calculate the compositions for two reasons: (1)
267 not all compositions have a unique solution (e.g., a mixture of schorl and magnesio-foitite can
268 have an identical composition to a mixture of dravite and foitite); and (2) calculation of Fe and
269 Mg species among the different X site groups according to bulk Fe/Mg ratio can yield a
270 decrease in the mole fraction of the dominant component versus increase in that of the less
271 dominant one (e.g., schorl versus dravite; foitite versus magnesio-foitite). Both of these factors
272 are exacerbated for compositions with intermediate proportions of X site vacancy, and such
273 compositions can result in a dominant species mole fraction that is inconsistent with the species
274 name based upon simple consideration of the most abundant components in the X and Y sites.
275 An example of this is the 50-30-0-20-0-0-0-0 composition in Table 3 that yielded a 40-40-0-10-
276 10-0-0-0 norm, so would be named schorl-dravite even though the formula used for calculating
277 composition was schorl-dominant. As mentioned above, the solution obtained is correct for the
278 atomic proportions obtained from the composition, and highlights the problem that all
279 compositions may not have a unique solution with respect to mole fractions. This apparently
280 indicates that at least some of the accepted tourmaline species do not represent algebraically

281 discrete end-members. Such cases appear to be rare, however, and in some cases the calculated
282 mole fraction of the dominant species is greater than that of the theoretical formula used to
283 calculate the composition (e.g., the 40-25-0-0-0-20-0-15 composition yielded 44-21-0-0-0-14-6-
284 15, and the 40-30-0-0-10-0-10 composition yielded 46-27-0-4-6-6-4-7: Table 4).

285 Among the admittedly few calculated Li tourmaline compositions tested, the spreadsheet
286 accurately reproduced the ideal mole fractions and calculated cations of Li to within 0.01 apfu of
287 the ideal mineral formulae. Because the Li content is calculated by difference at the Y site, Li
288 can be slightly overestimated for crystals having significant vacancy at that site. There is,
289 however, no way to determine such vacancy from electron probe data: other methods are needed
290 (e.g., Filip et al. 2012). Because such vacancy cannot be evaluated from microprobe data, and
291 because tourmalines that contain appreciable Li commonly are Li-rich (i.e., elbaite-rossmanite-
292 liddicoatite solid solutions), this uncertainty is not considered an important (or addressable)
293 source of error for the mole fraction calculations presented here.

294 Noting reproduction of the mole fractions for calculated compositions within the limits
295 discussed, application can be turned to natural compositions. A dravite-uvite composition taken
296 from Deer, Howie, and Zussman (1982), DHZ, was indicated in its reference to have 4.40 wt%
297 H₂O, but the Li-free calculations yielded both an analytical total in excess of 100 wt% and
298 significantly more than four OH radicals per formula unit using that concentration. Lowering the
299 water content to 3.72 wt% (Table 4) yields 4.005 OH per formula unit, consistent with zero
300 olenite and ferric iron components, and lowers the analytical total to slightly less than 100 wt%.
301 Calculation by the Li-absent spreadsheet yields the result of 0-53-0-40-2-0-0-0 identifying this
302 tourmaline as dravite (dravite-uvite), consistent with Na>Ca and Mg>Fe. The DHZ composition
303 is notable in having 3.288 Mg apfu – a number greater than can be accommodated by the Y site

304 in tourmaline. The spreadsheet handles this by allocating Mg to the Z site, in agreement with
305 formulae for uvite and feruvite in which Mg^{2+} at the Z site provides charge compensation for
306 Ca^{2+} at the univalent X site (e.g., Hawthorne and Henry, 1999), although the presence of Mg in
307 the Z site led to slightly larger negative residuals at the T and Y sites than other compositions
308 tested (Table 5).

309 The mole fraction calculations for the L35f, HGTR40, BMR-CT, and India Dravite
310 tourmalines analyzed in our lab at Oklahoma (Table 4) all produce low residuals (Table 5) and
311 would yield names based on most abundant component consistent with the convention based
312 upon bulk X site occupancy and Mg/Fe ratio. The discussed uncertainties in formulae and
313 naming for tourmalines having intermediate values of X site occupancy, however, are
314 particularly notable for the Bačik -1 and Bačik -2 compositions (from Bačik et al. 2015) in Table
315 4. For the Bačik-1 composition, Na has slightly greater abundance than both vacancy and
316 calcium in the X site, and $Fe > Mg$ in the Y site; by convention this species would be named
317 “schorl”. The most abundant species calculated by the spreadsheet, however, is foitite at 22% as
318 compared to schorl at 19%. The result is similar, but slightly better, for the Bačik-2 composition
319 for which the two most abundant calculated species are schorl (22%) and foitite (19%). These
320 results show the uncertainty for naming tourmaline species with intermediate X site occupancies
321 from mole fraction calculations. Given that both tourmalines contain <0.44 apfu Na and have
322 $Fe/(Fe+Mg) \sim 0.6$, it is suggested here that the name “schorl” is perhaps no less misleading than
323 “foitite” or “schorl-foitite-feruvite”. Regardless of species name derived, however, the relative
324 fractions of sodic, calcic, and vacancy species produced by the spreadsheet are correct. In these
325 latter cases, the relative fractions of sodic species (schorl, dravite, olenite) are greater than that of
326 the other X-site groups (calcic, vacancy). Hence, although such compositions provide the

327 greatest uncertainty for naming a tourmaline species from mole fractions, the conveyance of
328 mole fractions provides more information about the true chemical nature of the mineral than
329 naming for the dominant species.

330 As discussed above, the spreadsheet does not address the abundances of oxidized species
331 containing trivalent cations in the Y crystallographic site. Although reasons have been presented
332 for not considering the abundances of oxidized atoms of Fe or other multivalent transition
333 metals, there is an additional complicating factor that is not yet well addressed by present
334 tourmaline nomenclature - namely the coupled substitution of trivalent cations in the Y and T
335 crystallographic sites. Boron can substitute for Si in the T site with charge balance mostly
336 maintained by the substitution of Al at the Y site (e.g., Hughes et al. 2009; Lussier et al. 2009).
337 Because significant tetrahedral boron is rare in natural tourmaline, and because there is no end-
338 member species named for this substitution, it does not affect mole fraction calculations (or
339 naming). Perhaps the most common trivalent ion substituting in the T site of tourmaline is
340 aluminum (e.g., Lussier et al. 2009), yielding a net substitution of the form: $M^{3+}(Y) + Al^{3+}(T) =$
341 $M^{2+}(Y) + Si^{4+}(T)$. Tourmaline is commonly formed in aluminous schists and in association with
342 highly-fractionated peraluminous granitic magmas, the latter of which become more aluminous
343 and transition metal-depleted with fractionation (London 2011). Tourmalines produced in both
344 environments often are more aluminous than ideal formulae, and often appear to involve the
345 operation of a "Tschermak"-like substitution of the form $Al(Y)Al(T) = M^{2+}(Y)Si(T)$ that could
346 progress toward a hypothetical hyper-aluminous tourmaline similar to
347 $NaAl_3Al_6(BO_3)_3(Si_3Al_3)O_{18}(OH)_4$. This substitution (with lesser $Al(Y)B(T)$) appears to lie at the
348 heart of hyper-aluminous, but Li-poor, tourmalines produced by experimental synthesis at the
349 University of Oklahoma (e.g., Guttery 2012; London 2011). Even though aluminum in the T site

350 is recognized to be common in natural tourmaline (Lussier et al. 2009), to date only one species
351 has been named that is distinctive for T-site Al: adachiite, $\text{CaFe}_3\text{Al}_6(\text{Si}_5\text{Al})\text{O}_{18}(\text{BO}_3)_3(\text{OH})_3(\text{OH})$
352 (Nishio-Hamane et al. 2013). At present, however, there is no Mg-analog of this mineral, and
353 definition as a Ca- and Fe-rich tourmaline makes it of little application to hyper-aluminous
354 tourmalines from evolved pegmatite systems that tend to be depleted in both Ca and Fe and, as
355 discussed above, could potentially contain more than one Al in the T site. Therefore, even though
356 an approved species, adachiite was not considered an algebraically useful end-member for the
357 present calculations, and T site substitution of Al is omitted from the present calculation of end-
358 member mole fractions. Fortunately this is not a significant concern for mole fraction
359 calculations (or naming) for most natural tourmaline compositions, but it does complicate
360 estimating the abundances of other trivalent cations and lithium at the Y site as well as the
361 abundance of “oxy”-tourmaline species including olenite. With respect to “oxy-“ tourmalines,
362 oxy-dravite $[\text{Na}(\text{Al}_2\text{Mg})(\text{Al}_5\text{Mg})(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}]$ (Bosi and Skogby 2013) and oxy-schorl
363 $[\text{Na}(\text{Fe}_2\text{Al})(\text{Al}_6)(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}]$ (Bačík et al. 2013) are both approved tourmaline species
364 that are not addressed in the present calculations. Not only is the deprotonation in these minerals
365 not determinable from microprobe data, but at least algebraically both of these minerals represent
366 a combination of the root minerals (dravite and schorl) with olenite. Comparing the formula for
367 oxy-dravite, above, with that of olenitic-dravite, $\text{Na}(\text{Mg}_2\text{Al})\text{Al}_6(\text{Si}_6\text{O}_{18})(\text{BO}_3)_3(\text{OH})_3\text{O}$, shows
368 the main distinction between phases to be disordering of Mg between the Y and Z sites in oxy-
369 dravite. Such disorder cannot be evaluated from electron probe data. Because of a lack of
370 algebraic uniqueness and inability to discern from electron probe data, the “oxy-“ tourmaline
371 species are not addressed in the present spreadsheet; oxidized species in the present calculations
372 will at least partly be reflected by the olenite mole fraction, which represents a discrete

373 calculable component. If, however, a true Tschermak-like tourmaline end-member is ever
374 adopted as an approved end-member, then the present spreadsheet likely should be revised to
375 include that species – perhaps at the expense olenite. In that way, the aluminous component
376 reflected by Al(Y) would be treated in an equal manner to other tourmaline species without
377 regard to oxidation state or water activity.

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Implications

380 Potential users should bear in mind that this spreadsheet is directed at simple normative
381 calculations from electron probe data for Na-Ca-Li-Fe²⁺-Mg-Al tourmalines. For reasons
382 outlined previously, it does not address the mole fractions of Cr-rich, V-rich, or Fe³⁺-rich
383 tourmalines, does not include calculation for K-rich tourmaline (although K is included in
384 calculating X site occupancy), and does not include deprotonated “oxy”-tourmalines other than
385 olenite. Some of these components, such as Cr and V, should be comparatively easy to address in
386 calculation whereas some, especially Fe³⁺ and deprotonated species, may be impractical unless
387 analyses in addition to EMPA are performed. The incorporation of Fe³⁺ species likely would
388 require a significant re-working of the spreadsheet which was deemed unnecessary given its
389 primary application for calculating tourmaline formula from EMPA data. Because not all IMA
390 approved tourmaline species are included, nor can even be distinguished on the basis of electron
391 probe data alone, this spreadsheet cannot be used to definitively name or classify a tourmaline
392 according to IMA rules and accepted species. Rather, this spreadsheet is intended to fill a niche
393 similar to that of a mineralogical norm for rock composition by providing a tool for direct
394 comparison of tourmalines from different deposits according to a common standard. Even if this
395 particular spreadsheet does not prove to be the accepted tool for such comparison, it is my hope

396 that other researchers will either improve upon this work or develop and distribute a more
397 comprehensive and user-friendly tool for calculating tourmaline mole fractions. In this way we
398 can move past the vague “(species)-itic” procedure of describing tourmaline towards a method
399 with more chemical specificity.

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Table 1. Hypothetical tourmaline composition

Oxide	Wt. %
SiO ₂	35.84
B ₂ O ₃	10.38
Al ₂ O ₃	33.70
FeO*	11.43
MgO	3.01
Na ₂ O	2.46
H ₂ O	3.18
Total	100.00

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Table 2. Tourmaline end-members included in the calculations; □ denotes a site vacancy.

Phase	Abbreviation	Formula
Common tourmalines		
Schorl	Shl	NaFe ₃ Al ₆ (BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Dravite	Drv	NaMg ₃ Al ₆ (BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Tsilaisite	Tsl	NaMn ₃ Al ₆ (BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Feruvite	Fuv	CaFe ₃ (Al ₅ Mg)(BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Uvite	Uvt	CaMg ₃ (Al ₅ Mg)(BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Olenite	Oln	NaAl ₃ Al ₆ (BO ₃) ₃ Si ₆ O ₁₈ ((OH)O ₂)O
Foitite	Ftt	□(Fe ₂ Al)Al ₆ Si ₆ (BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Magnesio-foitite	Mft	□(Mg ₂ Al)Al ₆ Si ₆ (BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Lithium tourmalines		
Elbaite	Elb	Na(Li _{1.5} Al _{1.5})Al ₆ (BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Rossmannite	Rss	□(LiAl ₂)Al ₆ (BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH
Liddicoatite-OH	Ldd	Ca(Li ₂ Al ₁)Al ₆ (BO ₃) ₃ Si ₆ O ₁₈ (OH) ₃ OH

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497 Table 3. Simple theoretical Li-free compositions tested

	Schorl	Dravite	Uvite	Feruvite	Foite	Mg-Foite	Olenite	Shl(50)-Drv(50)	Drv(50)-Uv(50)	Uv(50)-Mft(50)	Shl(50)-Oln(50)	Shl(50)-Ftt(50)	50,30,0,20,0,0,0	0,20,0,40,40,0,0,0	0,0,0,30,40,0,0,30
Wt%															
SiO ₂	34.23	37.60	37.04	33.76	36.00	38.42	37.41	35.83	37.32	37.68	35.75	35.09	35.73	35.76	35.76
B ₂ O ₃	9.92	10.89	10.73	9.78	10.43	11.13	10.84	10.38	10.81	10.92	10.36	10.17	10.35	10.36	10.35
Al ₂ O ₃	29.04	31.90	26.19	23.87	35.63	38.02	47.60	30.40	29.02	34.64	37.91	32.25	29.30	26.29	31.35
FeO	20.46			20.19	14.35			10.71			10.69	17.48	10.68	8.55	8.55
MgO		12.62	16.57	3.78		8.59		6.01	14.61	10.54			6.79	10.40	6.40
CaO			5.76	5.25					2.90	2.93			1.11	4.45	3.89
Na ₂ O	2.94	3.23					3.22	3.08	1.60		3.07	1.51	2.46	0.62	0.92
H ₂ O	3.42	3.76	3.70	3.37	3.60	3.84	0.93	3.58	3.73	3.30	2.23	3.51	3.57	3.57	2.77
Total	100.00	100.00	99.99	100.00	100.01	100.00	100.00	99.99	99.99	100.01	100.01	100.01	99.99	100.00	100.01
Results															
APFU (#Ox)	31	31	31	31	31	31	31	31	31	31	31	31	31	31	31
Si	6.000	6.000	6.000	6.000	6.000	6.001	6.001	6.000	6.001	5.999	6.000	5.999	6.001	6.001	6.000
Ti															
B	3.001	2.999	3.000	3.000	3.000	3.000	3.001	3.000	3.000	3.000	3.001	3.001	3.000	3.000	3.000
Al	6.000	6.000	5.000	5.001	6.999	6.999	9.000	6.001	5.500	6.500	7.500	6.499	5.800	5.200	6.200
Fe	2.999		0.000	3.001	2.000			1.500			1.501	2.500	1.500	1.200	1.200
Mg		3.001	4.000	1.001		2.000		1.500	3.501	2.501			1.700	2.601	1.600
Ca			1.000	1.000					0.500	0.500			0.200	0.800	0.699
Na	0.999	0.999					1.001	1.000	0.499		0.999	0.501	0.801	0.202	0.299
[] _x	0.000	0.000	0.000	0.000	1.000	1.000	0.000	0.000	0.000	0.000	0.001	0.499	0.000	0.000	0.000
OH	3.999	4.002	3.998	3.995	4.002	4.001	0.995	3.999	4.000	3.504	2.497	4.003	3.999	3.996	3.100
Mole Fraction															
Schorl	1.00	0.00	0.00	0.00	0.00	0.00	0.00	0.50	0.00	0.00	0.50	0.50	0.40	0.08	0.10
Dravite	0.00	1.00	0.00	0.00	0.00	0.00	0.00	0.50	0.50	0.00	0.00	0.00	0.40	0.12	0.13
Tsilaisite	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
Uvite	0.00	0.00	1.00	0.00	0.00	0.00	0.00	0.00	0.50	0.50	0.00	0.00	0.10	0.48	0.40
Feruvite	0.00	0.00	0.00	1.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.10	0.32	0.30
Foite	0.00	0.00	0.00	0.00	1.00	0.00	0.00	0.00	0.00	0.00	0.00	0.50	0.00	0.00	0.00
Mg-Foite	0.00	0.00	0.00	0.00	0.00	1.00	0.00	0.00	0.00	0.50	0.00	0.00	0.00	0.00	0.00
Olenite	0.00	0.00	0.00	0.00	0.00	0.00	1.00	0.00	0.00	0.00	0.50	0.00	0.00	0.00	0.07

498 Table 4. Complex theoretical and natural Li-free compositions tested (*-value calculated for microprobe analysis)

	40,25,0, 0,0, 20,0,15	30,10,0, 10,10, 30,10,0	40,30,0, 0,10, 10,0,10	10,40,0, 20,20, 0,0,10	DHZ ¹	Báčik -1 ²	Báčik -2 ²	L35f	HGTR- 40	BMR- CT	India Dravite	Uvite C5212 ³	Feruvite ⁴
Wt. %													
SiO ₂	35.84	35.64	35.61	36.05	35.96	34.77	35.45	35.61	35.39	37.73	36.64	35.96	32.33
TiO ₂					0.14	0.30	0.20	0.24	0.20	0.45	0.42	0.62	2.19
B ₂ O ₃	10.38	10.33	10.32	10.45	10.73	10.37	10.31	*10.53	*10.61	*10.97	10.84	11.49	11.25
Al ₂ O ₃	33.70	32.25	31.73	31.09	30.85	34.08	32.81	34.64	35.18	33.27	34.28	26.80	23.38
FeO	11.43	12.79	12.07	7.90	0.76	10.26	10.56	13.57	6.96	5.79	0.74	0.41	13.56
MnO						0.02	0.01	0.18	0.06	0.03	0.30		0.07
MgO	3.01	3.19	3.98	7.26	13.67	3.70	3.82	1.62	5.76	8.64	10.30	15.20	7.80
CaO		1.11	0.55	2.24	2.41	1.41	1.46	0.21	0.14	0.86	0.32	5.50	3.30
Na ₂ O	2.46	1.23	2.45	1.86	1.63	1.16	1.32	1.72	1.68	2.22	2.47	0.13	1.16
K ₂ O					0.09	0.03	0.00	0.05	0.07	0.01	0.00	0.00	0.05
H ₂ O	3.18	3.47	3.29	3.15	3.72	3.21	3.45	*3.56	*3.56	*3.49	*3.57	2.74	3.48
F						0.00	0.00	0.13	0.18	0.65		1.49	
Cl						0.11	0.05						
Total	100.00	100.01	100.00	100.00	99.96	99.37	99.43	102.01	99.71	103.85	99.88	99.71	99.57
Results													
APFU (#Ox)	31	31	31	31	31	31	31.2	31.13	31	31.08	31	31.13	30.98
Si	6.000	6.000	6.000	6.000	5.803	5.840	5.986	5.896	5.799	5.957	5.872	5.877	5.745
Ti					0.017	0.038	0.025	0.030	0.025	0.053	0.051	0.076	0.284
B	2.999	3.000	3.001	3.002	2.988	3.006	3.004	3.009	3.000	2.989	2.998	3.240	3.346
Al	6.650	6.400	6.301	6.100	5.869	6.747	6.530	6.671	6.795	6.192	6.475	5.162	4.750
Fe	1.600	1.800	1.701	1.100	0.103	1.441	1.491	1.879	0.954	0.765	0.099	0.056	1.955
Mn						0.003	0.001	0.025	0.008	0.004	0.041	0.000	0.010
Mg	0.751	0.800	0.999	1.801	3.288	0.926	0.961	0.400	1.407	2.033	2.460	3.702	2.004
Ca		0.200	0.099	0.400	0.417	0.254	0.264	0.037	0.025	0.146	0.055	0.963	0.610
Na	0.799	0.400	0.800	0.600	0.510	0.378	0.432	0.552	0.534	0.680	0.768	0.041	0.388
K					0.019	0.006	0.000	0.011	0.015	0.002	0.000	0.000	0.011
[] _x	0.201	0.400	0.100	0.000	0.055	0.362	0.304	0.400	0.427	0.173	0.178	0.000	0.000
OH	3.551	3.900	3.697	3.497	4.005	3.596	3.886	3.932	3.891	3.676	3.816	2.987	4.001
F								0.068	0.093	0.324		0.770	
Cl						0.020	0.009						
Mole Fraction													
Schorl	0.44	0.28	0.46	0.22	0.00	0.19	0.22	0.39	0.20	0.19	0.04	0.00	0.29
Dravite	0.21	0.12	0.27	0.35	0.53	0.12	0.14	0.08	0.29	0.49	0.66	0.04	0.10
Tsilaisite	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.01	0.00	0.00
Uvite	0.00	0.06	0.04	0.25	0.40	0.10	0.10	0.01	0.01	0.10	0.05	0.92	0.15
Feruvite	0.00	0.14	0.06	0.15	0.02	0.16	0.16	0.03	0.01	0.04	0.00	0.04	0.45
Foite	0.14	0.28	0.06	0.00	0.00	0.22	0.19	0.33	0.18	0.05	0.01	0.00	0.00
Mg-Foite	0.06	0.12	0.04	0.00	0.00	0.14	0.12	0.07	0.25	0.12	0.17	0.00	0.00
Olenite	0.15	0.00	0.07	0.03	0.00	0.08	0.07	0.09	0.06	0.00	0.06	0.00	0.00

1 – Deer et al. (1982); 2 – Báčik et al. (2015); 3 – Dunn et al. (1977); 4 – Grice et al. (1989)

502 Table 5. Residuals from calculation of Li-absent tourmalines
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Composition Tested:	504											
	Shl	Drv	Uvt	Fuv	Ftt	Mft	Oln	Drv50 -Shl50	Drv50 -Uv50	Uvt50- Mft50	Shl50- Oln50	Shl50- Ftt50
Ca	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Mg(Y)	0.0000	0.0017	0.0013	0.0000	0.0000	-0.0005	0.0000	0.0000	0.0022	0.0009	0.0000	0.0000
Fe+Ti	0.0001	0.0000	0.0000	0.0029	0.0002	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Mn	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Na	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0016	0.0000	0.0000	0.0000	0.0000	0.0004
□x	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Al(Y)	-0.0007	-0.0006	-0.0002	-0.0002	-0.0007	-0.0007	0.0000	0.0001	-0.0016	-0.0015	0.0004	-0.0002
T	0.0001	0.0000	0.0002	0.0001	0.0000	0.0007	0.0015	-0.0005	0.0005	0.0000	0.0003	0.0024
Y	-0.0006	0.0011	0.0011	0.0027	-0.0005	-0.0012	0.0000	0.0001	0.0007	-0.0006	0.0003	-0.0002
Z	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0008	-0.0006	0.0000	0.0000	0.0000	0.0023
X	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0016	0.0000	0.0000	0.0000	0.0000	0.0004

Composition Tested:	50,30,0	0,20,0,	0,0,0,	40,25,0,	30,10,0	40,30,0	10,40,0				Little 3	BMR
	20,0, 0,0,0	40,40, 0,0,0	30,40, 0,0,30	0,0, 20,0,15	10,10, 30,10,0	0,10, 10,0,10	20,20, 0,0,10	Báčik -1	Báčik -2	DHZ	5f	CT
Ca	0.0002	0.0015	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Mg(Y)	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0672	0.0000	0.0000
Fe+Ti	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0668	0.0000	0.0279
Mn	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Na	0.0008	0.0002	0.0000	0.0000	-0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
□x	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Al(Y)	0.0000	0.0000	0.0005	0.0014	0.0000	0.0012	-0.0003	0.0014	0.0006	-0.0546	0.0002	-0.0241
T	0.0015	-0.0002	0.0002	0.0001	0.0003	0.0001	0.0001	0.0000	0.0000	0.0000	0.0000	0.0000
Y	0.0000	0.0000	0.0000	0.0014	0.0000	0.0012	-0.0003	0.0014	0.0006	0.0794	0.0002	0.0037
Z	0.0010	-0.0007	0.0002	0.0000	-0.0004	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
X	0.0010	0.0017	0.0000	0.0000	-0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000

505 Table 6. Li-bearing compositions tested

506	Composition	Elb	Rss	LDD	Elb50-	Elb50-	Little 3	Elbaite
507	Tested:				Rss50	Ftt25-	059B	Elba
508						Oln25	Pocket	
509	Wt%							
510	SiO ₂	38.49	39.03	38.57	38.76	37.57	37.55	37.89
511	B ₂ O ₃	11.15	11.31	11.17	11.23	10.88	*10.83	10.28
512	TiO ₂						0.07	0.04
513	Al ₂ O ₃	40.82	44.15	38.17	42.47	41.17	39.50	43.85
514	FeO					3.74	0.02	0.11
515	MnO						6.68	0.11
516	MgO						0.00	
517	Li ₂ O	2.39	1.61	3.20	2.00	1.17	*0.99	1.66
518	CaO			6.00			0.05	0.07
519	Na ₂ O	3.31	0.00	0.00	1.67	2.42	2.38	2.43
520	H ₂ O	3.84	3.90	2.89	3.87	3.05	*2.70	3.47
521	F						1.11	0.10
522	Cl							
523	Total	100.00	100.00	100.00	100.00	100.00	101.41	99.97
524	RESULTS							
525	APFU							
526	Si	6.001	6.000	6.001	6.000	6.001	6.004	5.942
527	B	3.000	3.001	2.999	3.000	2.999	2.989	2.782
528	Ti							
529	Al	7.501	8.001	7.000	7.750	7.751	7.445	8.106
530	Fe					0.500	0.003	0.014
531	Mn						0.905	0.014
532	Mg						0.000	
533	Ca			1.000			0.009	0.012
534	Li*	1.499	0.996	2.000	1.252	0.752	0.637	1.047
535	Na	1.001	0.000	0.000	0.501	0.750	0.738	0.739
536	OH	3.993	3.999	2.999	3.996	3.249	2.989	3.680
537	F						0.561	0.050
538	Mole Fractions							
539	Liddicoatite	0.00	0.00	1.00	0.00	0.00	0.01	0.01
540	Elbaite	1.00	0.00	0.00	0.50	0.50	0.25	0.44
541	Rossmannite	0.00	1.00	0.00	0.50	0.00	0.25	0.24
542	Tsilaisite	0.00	0.00	0.00	0.00	0.00	0.30	0.00
543	Schorl	0.00	0.00	0.00	0.00	0.00	0.00	0.00
544	Dravite	0.00	0.00	0.00	0.00	0.00	0.00	0.00
545	Foitite	0.00	0.00	0.00	0.00	0.25	0.01	0.01
546	Mg-foitite	0.00	0.00	0.00	0.00	0.00	0.00	0.00
547	Olenite	0.00	0.00	0.00	0.00	0.25	0.19	0.30
548	Residuals							
549	Ca	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
550	Mg	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
551	FeTi	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
552	Mn	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
553	Na	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
554	□x	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
555	Al(Y)	-0.0019	0.0005	-0.0007	0.0000	0.0000	0.0000	0.0000
556	T	-0.0029	0.0004	-0.0007	0.0003	0.0006	0.0044	0.0000
557	Li apfu [#]	1.4987	1.0000	2.0004	1.2502	0.7499	0.6392	0.9180

*- Li calculated by manual refinement from microprobe data; # - Li calculated by spreadsheet

555

Figure Captions

556 Figure 1. Li-free tourmaline calculations for the Li-absent tourmaline of Table 1: (a) initial data
557 entry into blue cells (B7-B20) of Sheet1; (b) addition of water concentration (cell B18).

558

559 Figure 2. Li-bearing tourmaline calculations for Elb(50)Rss(50) composition: (a) initial data
560 entry into blue cells (B7-B20) of Sheet1; (b) first addition of water concentration (cell B18) in
561 Sheet1; (c) first addition of Li₂O concentration by difference (cell B14); (d) final calculation
562 after optimizing H₂O (cell B18) and Li₂O (cell B14).

563

564

Figure 1. Li-Free calculation

565

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
1	Tourmaline Normative Calculation Sheet													
2	user inputs Sample name, Wt% values in blue cells, then adjust H ₂ O content (and #O, if necessary) to yield 3 apfu in Y site													
3	Sample: Table 1: 40,25,0,0,0,20,0,15													
4	# Oxyge	31.0000	=	62.0000	negative charge									
5														
6		Wt.% Ox	gpfu	mol prp	Ox prp	#anions	IPFU	Li-Free Mole Fractions						
7	SiO ₂	35.84	60.09	0.5964	1.1929	12.7294	6.3647	Schorl:	0.50	0.85	Σ Sodium Species			
8	TiO ₂	79.90	0.0000	0.0000	0.0000	0.0000	0.0000	Dravite:	0.23	0.15	Σ Vacancy Species			
9	Al ₂ O ₃	33.70	101.96	0.3305	0.9916	10.5812	7.0541	Tsilaisite:	0.00	0.00	Σ Calcium Species			
10	FeO	11.43	71.85	0.1591	0.1591	1.6976	1.6976	Uvite	0.00					
11	MnO	70.94	0.0000	0.0000	0.0000	0.0000	0.0000	Feruvite	0.00					
12	MgO	3.01	40.32	0.0747	0.0747	0.7966	0.7966	Foiteite:	0.10					
13	CaO	56.08	0.0000	0.0000	0.0000	0.0000	0.0000	Mg-Foiteite:	0.05					
14	Li ₂ O	29.88	0.0000	0.0000	0.0000	0.0000	0.0000	Olenite:	0.12					
15	Na ₂ O	2.46	61.98	0.0397	0.0397	0.4235	0.8471	sum	1.00					
16	K ₂ O	94.20	0.0000	0.0000	0.0000	0.0000	0.0000	sum	1.00					
17	B ₂ O ₃	10.38	69.64	0.1491	0.4472	4.7717	3.1811	OH Sum	0.0000					
18	H ₂ O	18.02	0.0000	0.0000	0.0000	0.0000	0.0000							
19	F	19.00	0.0000	0.0000	0.0000	0.0000	0.0000	Li-Bearing Mole Fractions						
20	Cl	35.45	0.0000	0.0000	0.0000	0.0000	0.0000	Liddicoatite:	0.00	0.85	Σ Sodium Species			
21	----	----						Elbaitite:	0.00	0.15	Σ Vacancy Species			
22	sub				2.9050			Rossmannite:	0.00	0.00	Σ Calcium Species			
23	O=F	0.00			0.0000			Tsilaisite:	0.00					
24	O=Cl	0.00			0.0000			Schorl:	0.46					
25	Total	96.82			2.9050		19.0941	Dravite:	0.27					
26							ΣYZBT	Foiteite:	0.15					
27			norm=	10.6712										
28														
29														
30					SITE Calculations									
31					B(T)	0.0000								
32					Al(T)	0.0000								
33					Al(Y)	1.0541								
34				assumes Ti is Vl:	[]X	0.1529								
35								Fraction F/W:	0.00					
								Fraction Cl/W:	0.00					

a

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
1	Tourmaline Normative Calculation Sheet													
2	user inputs Sample name, Wt% values in blue cells, then adjust H ₂ O content (and #O, if necessary) to yield 3 apfu in Y site													
3	Sample: Table 1: 40,25,0,0,0,20,0,15													
4	# Oxyge	31.0000	=	62.0000	negative charge									
5														
6		Wt.% Ox	gpfu	mol prp	Ox prp	#anions	IPFU	Li-Free Mole Fractions						
7	SiO ₂	35.84	60.09	0.5964	1.1929	12.0003	6.0001	Schorl:	0.44	0.80	Σ Sodium Species			
8	TiO ₂	79.90	0.0000	0.0000	0.0000	0.0000	0.0000	Dravite:	0.21	0.20	Σ Vacancy Species			
9	Al ₂ O ₃	33.70	101.96	0.3305	0.9916	9.9751	6.6501	Tsilaisite:	0.00	0.00	Σ Calcium Species			
10	FeO	11.43	71.85	0.1591	0.1591	1.6004	1.6004	Uvite	0.00					
11	MnO	70.94	0.0000	0.0000	0.0000	0.0000	0.0000	Feruvite	0.00					
12	MgO	3.01	40.32	0.0747	0.0747	0.7510	0.7510	Foiteite:	0.14					
13	CaO	56.08	0.0000	0.0000	0.0000	0.0000	0.0000	Mg-Foiteite:	0.06					
14	Li ₂ O	29.88	0.0000	0.0000	0.0000	0.0000	0.0000	Olenite:	0.15					
15	Na ₂ O	2.46	61.98	0.0397	0.0397	0.3993	0.7986	sum	1.00					
16	K ₂ O	94.20	0.0000	0.0000	0.0000	0.0000	0.0000	sum	1.00					
17	B ₂ O ₃	10.38	69.64	0.1491	0.4472	4.4984	2.9989	OH Sum	3.5512					
18	H ₂ O	3.18	18.02	0.1765	0.1765	1.7756	3.5512							
19	F	19.00	0.0000	0.0000	0.0000	0.0000	0.0000	Li-Bearing Mole Fractions						
20	Cl	35.45	0.0000	0.0000	0.0000	0.0000	0.0000	Liddicoatite:	0.00	0.80	Σ Sodium Species			
21	----	----						Elbaitite:	0.00	0.20	Σ Vacancy Species			
22	sub				3.0815			Rossmannite:	0.00	0.00	Σ Calcium Species			
23	O=F	0.00			0.0000			Tsilaisite:	0.00					
24	O=Cl	0.00			0.0000			Schorl:	0.40					
25	Total	100.00			3.0815		18.0005	Dravite:	0.25					
26							ΣYZBT	Foiteite:	0.20					
27			norm=	10.0600										
28														
29														
30					SITE Calculations									
31					B(T)	0.0000								
32					Al(T)	0.0000								
33					Al(Y)	0.6501								
34				assumes Ti is Vl:	[]X	0.2014								
35								Fraction F/W:	0.00					
								Fraction Cl/W:	0.00					

b

566

Figure 2. Li-bearing calculation

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