

1

2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27

**Direct and Indirect Evidence for Free Oxygen (O²⁻) in MO-Silicate Glasses
and Melts (M = Mg, Ca, Pb)**

H.Wayne Nesbitt¹, G.Michael Bancroft², Grant S. Henderson³, Ryan Sawyer¹, Richard A. Secco¹

¹Dept. of Earth Sciences, Univ. of Western Ontario, London, Ont., Canada N6A 5B7

²Dept. of Chemistry, Univ. of Western Ontario, London, Ont. Canada N6A 5B7

³ Dept. of Earth Sciences, Univ. of Toronto, Toronto, Ontario Canada M5S 3B1

Corresponding author: hwn@uwo.ca

28

ABSTRACT

29 O 1s XPS spectra of a Pb-silicate glass containing 76.6 mol% PbO provide the first
30 accurate, direct measurement of free oxide ion (O^{2-}) in these glasses. O^{2-} constitutes 35(\pm 3)
31 mol% of total oxygen, with NBO and BO constituting respectively, 52 (\pm 3) and 13(\pm 3) mol%.
32 All ^{29}Si NMR and O 1s XPS results for Pb silicate glasses indicate mol% levels of O^{2-} containing
33 more than \sim 30 mol% PbO. The O^{2-} abundances are consistent with equilibrium thermodynamic
34 considerations where $K \sim 12$ for the mass action equation involving NBO, BO and O^{2-} .

35 Raman and ^{17}O NMR spectra of two CaMg-silicate glasses indicate ~ 10 (\pm 4) mol% O^{2-}
36 in CaMgSiO_4 glass and ~ 18 (\pm 4) mol% O^{2-} in a $\text{Ca}_{0.36}\text{Mg}_{0.36}\text{Si}_{0.28}\text{O}_{1.28}$ glass. Oxygen species
37 abundances are calculated using experimental results from 13 separate ^{29}Si NMR, ^{17}O NMR and
38 Raman measurements of Mg-, Ca- and CaMg-silicate glasses. All reveal mol% levels of O^{2-} with
39 ~ 1 to 2.6 mol% in metasilicate glass and ~ 5 to 10 mol% in orthosilicate glass. Recent Raman
40 experimental results also indicate O^{2-} in CaMg-silicate glasses at levels ranging from about 1 to
41 10 mol%. In all there are 23 separate ^{29}Si NMR, ^{17}O NMR and Raman measurements indicating
42 mol% levels of O^{2-} in alkaline earth silicate glasses. Eight recent MD simulations of Mg, Ca and
43 CaMg-silicate glasses include 21 separate simulations over a wide compositional range. All
44 indicate mol% levels of O^{2-} in the glasses demonstrating that the MD simulations and
45 experimental results on these systems are in accord.

46 There are two fundamentally important implications of these studies. First, free oxygen
47 (O^{2-}) is an *essential constituent* of Pb, Mg, Ca and CaMg binary silicate melts and glasses. It is
48 *not* an ‘accidental’ product associated with glass or melt defects. It is instead, a
49 thermodynamically important constituent of these binary melts (and glasses). Second, where
50 melts are equilibrated, the mass action equation relating BO, NBO and O^{2-} must hold across the

51 *entire* Ca, Mg, CaMg and Pb binary systems, thereby requiring the activities and mole fractions
52 of all three species to be defined and finite in the melts. Free oxygen, however, may be too low
53 to be detected in highly siliceous glasses using conventional spectroscopic techniques.

54 **Keywords:** XPS of glasses, free oxygen in glasses, silicate glasses, Pb-silicate glass, Ca silicate
55 glass, Mg silicate glass, CaMg silicate glass

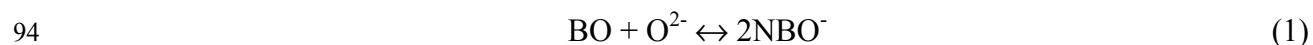
56 INTRODUCTION

57 Over the last two decades dramatic developments have occurred in three techniques
58 relevant to the understanding of distribution of species in silicate glasses and melts. Molecular
59 Dynamics (MD) simulations have improved sufficiently that several hundreds to thousands of
60 atoms may be accommodated using various core-shell interatomic potentials, due primarily to
61 greatly improved computational facilities. From these calculations distributions of Q species,
62 oxygen species, and modifier cation speciation have been evaluated, as have structural properties
63 such as bond angles and lengths (e.g., Mountjoy et al. 2011; Pedone et al. 2010; Mountjoy, 2007;
64 Mead and Mountjoy, 2006; Du and Cormack, 2004). There have been similarly dramatic
65 developments in ^{29}Si NMR spectroscopy. The 2D ^{29}Si MAF NMR and allied 2D spectroscopies
66 generally provide better resolution and clearer demarcation of spectral contributions, than do
67 ^{29}Si MAS NMR spectra. Much greater effort has also been directed toward better quantification
68 of the spectral contributions (Davis et al. 2011; 2010; Zhang et al. 1997;1996; Farnan et al.
69 1992). These advances have revealed spectral contributions in some systems which were
70 impossible to detect by ^{29}Si MAS NMR (e.g., Nesbitt et al. 2015a; Davis et al. 2010). As for the
71 third technique, technical breakthroughs in XPS spectroscopy have made it a useful tool to
72 identify oxygen species in silicate minerals (Zakaznova et al. 2008; 2006; 2005). The most
73 important technical advance was in charge compensation of samples (Nesbitt and Bancroft,

74 2014). With successful charge compensation, linewidths of insulators are commensurate with
75 those of conductors and semi-conductors (Nesbitt et al. 2004). Recent advances in understanding
76 of the contributions to linewidths and lineshapes (Bancroft et al. 2009) also aided greatly in
77 interpretation of Si 2p and O 1s spectra collected from binary silicate glasses (Sawyer et al.
78 2015; 2012; Nesbitt et al. 2015b; 2011; Dalby et al. 2007). Here we assess oxygen speciation in
79 Pb, Mg, Ca and CaMg silicate glasses using information from each of the three techniques. We
80 begin with XPS results followed by contributions from NMR, and finally we address recent MD
81 studies.

82 Determination of the concentration of O^{2-} in silicate glasses is required for
83 thermodynamic modelling of melts and glasses, and to understand the kinetics of reaction of
84 silicate glasses and melts with reagents (e.g., H_2O , CO_2 S-species). Free oxide is highly basic
85 compared with NBO or BO and is likely to be the most reactive oxygen species toward most
86 natural reagents (Sawyer et al., 2015). There is also an exceptionally large reservoir of O^{2-}
87 supplied via the polymerization-depolymerization reaction (Eq. 1). Even at the 0.1% level, its
88 consumption by reaction with reagents will be replaced by conversion of NBO to $BO + O^{2-}$
89 (Eq.1) to maintain equilibrium among the O species (Eq. 2); the polymerization reaction (Eq. 1)
90 is an O^{2-} buffer. With its high reactivity and buffered nature, O^{2-} may be treated as a master
91 variable in silicate melts, much as H^+ (pH) is in aqueous solutions.

92 The oxygen species are related through the polymerization-depolymerization reaction
93 (Fincham and Richardson, 1954):



95 where BO represents “bridging” oxygen (Si-O-Si; O bonded to two Si atoms), NBO represents
96 “non-bridging” oxygen (Si-O-M; O bonded to one Si and a Pb, alkali or alkaline earth atom, M),

97 and O^{2-} is free oxygen (M-O-M; O *not* bonded to Si but but is also referred to as free oxide, non-
98 network oxygen or non-silica bonded O). The associated mass-action equation is:

$$99 \quad K_1 = (NBO^-)^2 / [(BO)(O^{2-})] \quad (2)$$

100 where parentheses indicate activities and K_1 is the equilibrium constant. Early studies
101 demonstrated that K_1 was finite, and that O^{2-} existed in silicate glasses and melts (e.g., Toop and
102 Samis, 1962). Many recent reviews of silicate glasses (e.g., Henderson et al. 2006; Henderson,
103 2005; Mysen, 2003; Stebbins, 1995) do not, however, mention free oxide although many studies
104 published subsequently have reported it in binary silicate glasses (e.g., Al-Hasni and Mountjoy,
105 2014; Sawyer et al. 2015; Nesbitt and Bancroft, 2014; Retsinas et al. 2014; Nasikas et al. 2012;
106 Kohara et al. 2011; 2004; Nesbitt et al. 2011; Davis et al. 2011; Sen et al. 2009; Sen and
107 Tangeman, 2008; Park and Rhee, 2001; Fayon et al. 1998; Zhang et al. 1997). An important
108 objective of this communication is to emphasize the large number of recent studies which
109 indicate O^{2-} in binary silicate glasses.

110 There is good agreement between O 1s XPS and ^{29}Si MAS NMR results, both indicating
111 free oxide (O^{2-}) in Pb silicate glasses (Dalby et al. 2007; Fayon et al. 1998), although it has not
112 been observed directly. We report direct observation of O^{2-} in a glass containing 76.6 mol% PbO.
113 Nasikas et al. (2012) were the first to report direct spectroscopic observation of an O^{2-} signal in
114 binary silicate glasses using ^{17}O NMR spectroscopy. They did not, however, provide fits to these
115 important spectra. The spectra are here deconvoluted using fitting techniques identical to those
116 employed to fit the 76.6 mol% PbO silicate glass, with BO, NBO and O^{2-} abundances evaluated.

117 Zhang et al. (1997) conducted the most exhaustive study of CaSiO_3 glass and it remains
118 the benchmark paper for this system. They used a 2D ^{29}Si MAF NMR technique and
119 demonstrated that the glass contained ~ 1 mol% O^{2-} . Thompson et al. (2012) collected ^{17}O NMR

120 spectra of a glass containing 56.6 mol% CaO. They concluded that there is “no evidence of free
121 oxide in detectable quantities” and also concluded that free oxide cannot be present at levels
122 greater than 1 mol% in glasses containing less than ~ 67 mol% CaO. The issue of O²⁻ abundance
123 in Ca-silicate glasses wants resolution and we address the issue here. Numerous experimental
124 results and MD simulations are reviewed, with O²⁻ contents and uncertainties presented.

125 **EVIDENCE FOR FREE OXIDE FROM EXPERIMENTAL STUDIES**

126 **Pb-Silicate Glasses**

127 **Experimental Methods and Results:** A glass containing nominally 75 mol% PbO was
128 synthesized according to Dalby et al. (2007). After quenching, minor amounts of small crystals
129 were present at the interface with the sample holder but the interior was glassy. The portion
130 containing the crystals was removed and the interior glass was inspected by SEM (Hitachi
131 SU6600) at magnification of 22,000x. The inspection revealed no inhomogeneities (i.e., no
132 crystals). The sample was analysed by XPS as explained in the next paragraph. After XPS
133 analysis the fragment was coated with carbon and analysed again using an Hitachi SU6600. A
134 synthesized glass containing 67 mol% PbO and a natural olivine crystal (forsterite) were used as
135 standards. Energy dispersive and crystal spectrometer analysis of five spots were averaged
136 yielding 76.6 (±1) mol% PbO. The sample is referred to subsequently as the Pb77 sample.

137 Preparation for XPS analyses consisted of fracturing the glass pellet in the introduction
138 chamber of a Kratos Axis Ultra spectrometer (~10⁻⁹ Torr) to expose a pristine surface. It was
139 immediately transferred to the analytical chamber (~10⁻¹⁰ Torr) and a broadscan was collected.
140 The magnetic confinement charge compensation system was employed as describe elsewhere
141 (Dalby et al., 2007; Nesbitt et al., 2011; Sawyer et al., 2012). Details concerning charge
142 compensation are available at ‘<http://www.kratos.com/products/axis-ultra-dld>’ and are discussed

143 by Nesbitt and Bancroft (2014). High resolution O 1s and Si 2p spectra were collected using 10
144 eV pass energy and conditions described previously (Dalby et al. 2007; Bancroft et al. 2009;
145 Nesbitt et al. 2011, Sawyer et al. 2012). The O 1s spectra shown in Figs. 1a and 1b represent
146 glasses containing 50 mol% PbO (PbSiO₃) and 67 mol% PbO (Pb₂SiO₄), and are from Dalby et
147 al. (2007). The O 1s spectrum of the Pb77 glass (contains 76.6 mol% PbO) is illustrated in Fig.
148 1c. These spectra were fit using a Shirley background (Shirley, 1972) and two peaks (30%
149 Lorentian-70% Gaussian peakshapes) representing BO and NBO+O²⁻ signals. The analytical
150 settings for the Pb77 glass were identical to those used by Dalby et al. (2007) and they should be
151 referred to for details.

152 **Interpretation of O 1s Spectra:** The fits to the O 1s XPS spectra of Pb-metasilicate (50
153 mol% PbO) and Pb-orthosilicate (67 mol% PbO) glasses (Figs. 1a, 1b) were obtained using the
154 peak fit parameters of Dalby et al. (2007). As for other suites of glasses, all peaks migrate to
155 lower BE with increased metal oxide content as explained by Nesbitt and Bancroft (2014). Two
156 of their findings are very important with respect to this study: (1) the BO linewidths are constant
157 at ~1.22 eV regardless of glass composition; (2) the more intense NBO+O²⁻ peak is composite
158 (Dalby et al. 2007) but its linewidth changes little between 50 and 67 mol% PbO (i.e., 1.17 eV to
159 1.22 eV, Dalby et al. 2007, their Table 2). The effectively constant linewidth of the BO peak
160 (1.22 eV) is expected in that individual peaks contributing to the O 1s spectrum should have a
161 linewidth of ~ 1.25 ±0.1 eV (Bancroft et al. 2009; Nesbitt et al. 2004). It is nevertheless
162 surprising that the composite NBO+O²⁻ peak is just as narrow. As explained by Dalby et al.
163 (2007), the two contributions are effectively superimposed. To summarize, the BO and NBO+O²⁻
164 peaks are of similar width (~1.22 eV) and are effectively independent of glass composition. This
165 circumstance aids greatly in fitting the O 1s XPS spectrum of the Pb77 glass, as now discussed.

166 **BO% in Pb77 Glass.** The O 1s XPS spectrum of the Pb77 glass (Fig. 1c) is similar to the
167 orthosilicate glass (Fig. 1b). Both consist of an intense low binding energy (BE) peak with a
168 distinctive shoulder on its high BE side. Using Fig. 1b as guide, the Pb77 glass was fit with a BO
169 and a NBO+O²⁻ peak. As previously discussed the BO linewidth of the Pb77 glass spectrum was
170 constrained to 1.22 eV (Fig. 1c). A second, entirely unconstrained peak was introduced to
171 represent the NBO+O²⁻ contribution and the resulting least squares best fit is shown in Fig. 1c.
172 Fit parameters are listed in Table 1. The fit indicates 10.8 mol% BO with the remainder being
173 NBO+O²⁻. To evaluate uncertainties, different backgrounds were selected and the BO peakwidth
174 was adjusted by 0.2 eV (i.e., 1.02 and 1.42 eV). No BO value was greater than 2 mol% different
175 from 10.8 mol% and we conclude that BO = 10.8 (±2) mol%. If the polymerization reaction (Eq.
176 1) had gone to completion, all BO would have been consumed. Clearly the reaction did not go to
177 completion leaving some BO and O²⁻ unconsumed. Knowing the glass composition, the BO
178 abundance (10.8%) and the stoichiometry of reaction (1), then following Sawyer et al. (2015, see
179 their section entitled ‘Constraints on Oxygen Speciation’) the abundances of the three oxygen
180 species can be calculated and these are BO = 10.8 mol%, NBO = 54.2 mol% and O²⁻ = 35.0
181 mol%. A 2 mol% uncertainty is assigned to these values.

182 **Deciphering the NBO+O²⁻ Signal.** The full width at half maximum (FWHM) of the NBO+O²⁻
183 peak (Fig. 1c) is much broader (1.60 eV) than any other NBO+O²⁻ peak fitted to the Pb-silicate
184 glasses of Dalby et al. (2007). The explanation may relate to the increased intensity of the O²⁻
185 contribution relative to the NBO contribution and to a shift of the O²⁻ peak to lower BE relative
186 to the NBO peak (with increased PbO content). The hypothesis is now tested. It is evident from
187 Fig. 1c that introduction of separate, unconstrained NBO and O²⁻ peaks will not provide a
188 meaningful fit because there are no features with which to ‘fix’ the positions, linewidths or

189 intensities of the two peaks. Constraints must be used if the NBO and O²⁻ contributions are to be
190 separated. We have consequently fit the spectrum using three peaks and *two* distinct constraints.

191 By the first method, both BO *and* NBO peaks were constrained at 1.22 eV, as observed in
192 the 67 mol% PbO glass (Fig. 1b). The third (O²⁻) peak was introduced and was entirely
193 unconstrained. The resulting least squares fit is shown in Fig. 2a with fit parameters listed in
194 Table 1. The fit indicates that the unusual breadth of the NBO+O²⁻ peak is the result of an intense
195 O²⁻ contribution which overlaps the NBO peak. The O-species proportions derived from the fit
196 are BO = 14.7 mol%, NBO = 51.0 mol% and O²⁻ = 34.3 mol%. These compare favourably with
197 the results derived from Fig. 1c where BO = 10.8 mol%, NBO = 54.2 mol% and O²⁻ = 35.0
198 mol%. As evidence for a reasonable fit, an O 1s spectrum of PbO collected by Dr. Mark
199 Biesinger (Surface Science Western, pers. comm.) indicates that its O²⁻ peak is centered at 529.0
200 eV compared with 529.04 eV (for the O²⁻ peak of Fig. 2a (Table 1)).

201 For the second deconvolution method, the linewidth of the BO peak is constrained to 1.22
202 eV (as for the first method). The second constraint has the BO, NBO and O²⁻ proportions equal
203 to the values from the two peak fit of Fig. 1c. With BO linewidth constrained to 1.22 eV and
204 with the three peak areas constrained (i.e., BO:NBO:O²⁻ = 10.8%:54.2%:35%), the fit shown in
205 Fig. 2b is obtained. The fit parameters are listed in Table 1. The NBO linewidth is 1.52 which is
206 somewhat greater than 1.25 ±0.1 eV (the value expected from theory, Bancroft et al. 2009;
207 Nesbitt et al. 2004). The O²⁻ peak maximum (529.22 eV) is, however, still close to that expected
208 for O of PbO (529.0 eV, see previous paragraph). Moreover, the fit is similar to the fit of Fig. 2a
209 although different constraints were used, thus providing confidence that deconvolution of the
210 oxygen signals are reasonable.

211 The O²⁻ peak are not evident in Figs. 1a or 1b so that its BE must be < 0.5 eV of the

212 respective NBO peak as emphasized by Nesbitt and Bancroft (2014, see their Fig. 13). For the
213 Pb77 glass (Fig. 2), the O^{2-} peak is at 0.5 to 0.7 eV lower BE than the NBO peak in the Pb77
214 glass (Fig. 2). As explanation, all peaks shift to lower BE (and at different rates) with increased
215 counter oxide content (e.g., Nesbitt and Bancroft, 2014, their Fig. 20). The O^{2-} peak of Fig. 2,
216 apparently shifts slightly more than the NBO (Fig. 2), although the energy splitting remains
217 small (0.5 to 0.7 eV). The explanation for this small differential shift is uncertain, but
218 undoubtedly relates to electron density over the NBO and O^{2-} moieties. As PbO increases beyond
219 67 mol%, NBO abundance decreases leaving O^{2-} to take on ever greater electron density and
220 approach the BE of O^{2-} observed in PbO. This aspect, however, needs further study.

221 We conclude that: (1) these types of constraints yield reasonable fits to the Pb77 glass O
222 1s XPS spectrum; (2) the breadth of the NBO+ O^{2-} peak of Fig. 1c is indeed the result of an
223 intense O^{2-} peak split from the NBO peak by about 0.5 to 0.7 eV; (3) there is a large amount of
224 O^{2-} in the Pb silicate glasses studied (~35 mol% in Pb77 glass).

225 **Other Experimental Evidence.** Furukawa et al. (1978) and Iwamoto et al. (1979) conducted
226 Raman spectroscopic studies of Pb-silicate glasses and detected BO, NBO and O^{2-} in the high-
227 PbO glasses but amounts are uncertain due to ambiguity in sensitivity factors. Smets and
228 Lommen (1982) conducted an O 1s XPS study of Pb-silicate glasses ranging in composition
229 from 30 to 70 mol% PbO. Their spectra are poorly resolved but their estimates of X_{BO} are similar
230 to those of Dalby et al. (2007), although they display greater variability. The MD and EXAFS
231 study of Rybicki et al. (2001) demonstrated the presence of PbO_4 and possibly PbO_3 groups (i.e.,
232 O^{2-}) in a wide compositional range of Pb-silicate glasses. Takaishi et al. (2005) identified O^{2-} in
233 Pb-silicate glasses using X-ray and neutron diffraction techniques where O is bonded to three Pb
234 atoms. Fayon et al. (1998) observed Q^2 and Q^1 species in invert Pb-silicate glasses (i.e., $MO > 50$

235 mol%). The presence of these Q-species necessitates the presence of O^{2-} in all glasses they
236 reported. Very recently, Lee and Kim (2015) reported O^{2-} in their ^{17}O NMR spectrum of Pb-
237 silicates but they provide neither fits to their spectra nor other support for their quoted O^{2-}
238 abundances. In summary, free oxygen has been detected in Pb-silicate glasses using a wide range
239 of experimental and simulation techniques and there is excellent agreement among the various
240 techniques and laboratories.

241 **Thermodynamic Analysis.** A melt at equilibrium necessarily requires adherence to the mass
242 action equation (Eq. 2) and substitution of mole fractions (X_{NBO} , X_{BO} , X_{O2-}) for activities makes
243 K_1 (Eq. 2) a 'conditional equilibrium constant'. Dalby et al. (2007) report atomic % of oxygen
244 species from which X_{BO} , X_{NBO} and X_{O2-} were calculated. X_{BO} is plotted as a function of glass
245 composition on Fig. 3 (large shaded circles). The large shaded squares (Fig. 3) represent X_{BO}
246 values derived from ^{29}Si NMR Q-species distributions reported by Fayon et al. (1998) and
247 calculated according to Sawyer et al. (2015, see their Appendix A). The large solid circle of Fig.
248 3 represents X_{BO} obtained from the fit to the O 1s XPS spectrum of the Pb77 glass (Fig. 1c). The
249 horizontal error bar represents the uncertainty in the glass composition. The NMR and XPS
250 agreement is reasonable. Both sets of results indicate that the polymerization reaction (Eq. 1)
251 does not go to completion and that $K_1 \sim 12$ (Eq. 2). Values for X_{O2-} of Pb-silicate glasses are, for
252 the first time, presented in Fig. 3 (small symbols). They were calculated from these results for
253 Pb77 glass, the XPS and NMR results of Dalby et al. (2007) and Fayon et al. (1998) using the
254 approach of Sawyer et al. (2015, p. 2). X_{O2-} increases systematically with increasing PbO content
255 and they straddle the X_{O2-} curve calculated for $K_1 = 12.0$. We emphasize that with $K_1 \sim 12.0$,
256 equilibrium (Eq. 2) requires the Pb77 glass to contain about 33 mol% O^{2-} (i.e., $X_{O2-} \sim 0.33$). The
257 two peak fit to the Pb77 glass (Fig. 1c) yields $X_{BO} = 0.108$ and $X_{O2-} = 0.35$. The two fits using

258 constraints (Figs. 2a and 2b) also yield oxygen species abundances consistent with $K_1 \sim 12$. The
259 concentration of O^{2-} is reasonably known as a function of composition in the Pb-silicate binary
260 system.

261 **Mg-Ca-Silicate Glasses**

262 **Introduction.** Nasikas et al. (2012; 2011) were the first to report direct experimental evidence
263 for O^{2-} in Ca-Mg silicate glasses of composition $Ca_{1.0}Mg_{1.0}Si_{1.0}O_4$ (i.e., CMS33; $SiO_2 = 33$
264 mol%) and $Ca_{1.44}Mg_{1.44}Si_{0.56}O_4$ (CMS28; $SiO_2 = 28$ mol%). The measurement at the orthosilicate
265 composition (CMS33) is particularly instructive because a stoichiometric constraint unique to
266 this composition permits determination of the abundance of all oxygen species provided the
267 concentration of any one species is known. Consider, for example, addition of CaO to SiO_2 melt.
268 Progressive addition of CaO results in BO and O^{2-} being converted to NBO according to Eq. (1)
269 where the BO is derived from SiO_2 and O^{2-} from CaO. If, *at the orthosilicate is composition* the
270 polymerization reaction (Eq. 1) goes to completion, all BO and O^{2-} will be consumed
271 simultaneously and only NBO will be present in the glass. If, however, the reaction does not go
272 to completion, then some BO *and an equal amount of O^{2-}* will remain (unreacted) in the glass
273 (i.e., $X_{BO} = X_{O^{2-}}$). If the amount of unreacted BO is ' x ' then the concentration of O^{2-} in the glass
274 is also ' x ' and the amount of NBO is the total oxygen in the glass is ' $O_T - 2x$ ' where $O_T =$
275 $X_{CaO} + 2X_{SiO_2}$. Converting to mole fractions and substitution into Eq. (2) yields:

$$276 \quad K_1 = X_{NBO}^2 / (X_{BO} X_{O^{2-}}) = (1 - 2x) / x^2 \quad (3)$$

277 If, at the orthosilicate composition, *either X_{BO} or $X_{O^{2-}}$* is known, K_1 can be calculated and the
278 concentrations of all oxygen species can be evaluated. These types of calculations were
279 performed on Ca-Mg-silicate glasses to obtain BO, NBO and O^{2-} abundances for numerous
280 experimental studies discussed subsequently. The results are compiled in Table 2.

281 **Raman Spectral Results.** Nasikas et al. (2011) reported Raman spectra for of the Ca_1Mg_1 -
282 silicate glasses containing 28, 30 and 33 mol% SiO_2 (CMS28, CM30 and CMS33 glasses). They
283 fit the Raman spectrum of the CaMg orthosilicate glass (CMS33) and reported 50% Q^0 , 35% Q^1 ,
284 13% Q^2 and 2% Q^3 . From these the NBO, BO and O^{2-} mole fractions were determined and X_{O_2} -
285 = 0.084, or 8.4 mol% O^{2-} (for calculations, see Sawyer et al., 2015, their Appendix A). The O
286 species abundances are listed in Table 2. Nasikas et al. (2012) assign an uncertainty of $\pm 3\%$ to
287 their Q species abundances. The uncertainty was added to, and subtracted from, Q^1 (with
288 compensation in Q^0) to obtain 8.8% and 8.0% O^{2-} respectively. The uncertainty then was added
289 to, and subtracted from, Q^2 (with compensation in Q^0) to yield respectively 9.1% and 7.6% O^{2-} .
290 The Raman results for the CMS33 sample therefore yields 8.4 (± 0.8) mol% O^{2-} which, as shown
291 in Fig. 4a, is remarkably close to the 9.5% O^{2-} value obtained by fitting the CMS33 ^{17}O NMR
292 spectrum of Nasikas et al. (2012).

293 **^{17}O NMR and Raman Spectra of Ca_1Mg_1 -Silicate Glasses.** Nasikas et al. (2012) provide ^{29}Si
294 MAS NMR and ^{17}O MAS NMR spectra of the Ca_1Mg_1 -silicate glasses containing 28 and 33
295 mol% SiO_2 (CMS28 and CMS33). They identified the O^{2-} and NBO+BO peaks in their ^{17}O
296 NMR spectra, but they do not fit the spectra and in an attempt at quantification, these spectra
297 were scanned and digitized, imported into and fitted using CASAXPS software. The dots of Fig.
298 4 represent the scanned spectra. After introducing a linear background and two 100% Gaussian
299 peaks to each spectrum, a least squares, entirely free fit was performed (fit parameters given in
300 Table 1). Following Nasikas et al. (2012), the more intense peak was interpreted as the NBO+BO
301 contribution and the weaker peak as O^{2-} . The fits to the CMS33 and CMS28 glasses of Figs 4a
302 and 4b yield respectively ~ 9.5 mol% and ~ 19.3 mol% O^{2-} . Nasikas et al. (2012) quoted ~ 5 mol%
303 O^{2-} for the orthosilicate glass (CMS33) which is somewhat lower than the 8.4 (± 0.8) mol% O^{2-}

304 obtained from their Raman results discussed in the previous paragraph, and from our fit (Fig. 4a).
305 In fitting the ^{17}O NMR spectra, backgrounds were set to minimize the area of the O^{2-} peak (i.e.,
306 background was set at the highest possible intensity on the high ppm side of the spectra) so that
307 mol% O^{2-} values ($\sim 9.5\%$ and $\sim 19.3\%$ O^{2-} for CMS33 and CMS28 respectively) are near
308 minimum values. Other background settings yield greater O^{2-} abundances by 1 to 3 mol%.

309 The NBO and BO contributions cannot be distinguished in the ^{17}O NMR spectra (Figs.
310 4a, 4b) but at the orthosilicate composition the two peaks can be separated using the constraint
311 that $X_{\text{BO}} = X_{\text{O}^{2-}}$ (see Introduction to this section), in a manner analogous to separation of NBO
312 and O^{2-} peaks in Fig. 2a. Three 100% Gaussian peaks, one representing each of BO, NBO and
313 O^{2-} , were introduced to Fig. 4c. The BO and O^{2-} peak intensities were *constrained* to identical
314 values but their peak widths and positions were unconstrained. The NBO peak parameters were
315 unconstrained. The resulting fit to CMS33 glass is illustrated in Fig. 4c and the residuals are
316 shown in Fig. 4e. Fitted peak parameters are provided in Table 1. The fit is somewhat better than
317 the two peak fit of Fig. 4a and it yields 10.3 mol% for O^{2-} and BO, and 79.4 mol% NBO. The fits
318 to Figs. 4a and 4c indicate that the O^{2-} mol% for the CMS33 glass should be ~ 10 mol% O^{2-} . Cast
319 as mole fractions and substituted into Eq. (2) yields $K_1 = 59.4$.

320 **Test for Consistency.** A test is performed to determine if the ^{17}O NMR spectra results for the
321 CMS33 and CMS28 are consistent with each other. Peak area constraints were used to obtain the
322 three peak fit to the Pb77 glass (Fig. 2b) and an identical procedure has been used to evaluate
323 oxygen speciation in the CMS28 glass. Three independent equations were used to solve for the
324 mole fractions of the three oxygen species in the CMS28 glass. The equations are the mass
325 action equation with $K_1 = 59.4$ (derived from the CMS33 glass), the stoichiometry of the
326 polymerization reaction (Eq. 1) and the mass balances constraint where $\sum X_{\text{O-species}} = 1.0$ (see

327 Sawyer et al. 2015 for details). The result is $X_{\text{NBO}} = 0.765$, $X_{\text{BO}} = 0.055$ and $X_{\text{O}^{2-}} = 0.180$ for the
328 CMS28 glass. These were used to calculate $X_{\text{BO}}/X_{\text{NBO}} = 0.0716$ and $X_{\text{O}^{2-}}/X_{\text{NBO}} = 0.235$. These
329 ratios then were used to constrain BO/NBO and O^{2-} /NBO peak areas during fitting of the CMS28
330 ^{17}O NMR spectrum. No other constraints were used. The resulting fit is shown in Fig. 4d,
331 residuals in Fig. 4f, and the fit parameters are given in Table 1. Clearly the BO, NBO and O^{2-}
332 peak areas derived from simultaneous solutions of the above three equations are consistent with
333 the ^{17}O NMR spectrum for CMS28, and with $K_1 = 59.4$ for both glasses. The X_{BO} values for the
334 CMS28 and CMS33 glasses are plotted on Fig. 5a as solid diamonds and the corresponding $X_{\text{O}^{2-}}$
335 values are plotted as crosses (at the same compositions). The ^{17}O NMR spectra of
336 Nasikas et al. (2012) clearly are consistent with each other and with the mass action equation
337 where $K_1 = 59.4$.

338 **Uncertainties.** Different fits to the scanned spectra (Fig. 4) indicate that O^{2-} represents about
339 10 mol% of total oxygen in the orthosilicate glass (Figs. 4a, 4c). Variation in line shapes (i.e.,
340 addition of a Lorentzian component to the peaks) and placement of background indicate ~9.5
341 mole% to ~13 mol% O^{2-} for the CMS33 glass. This variation results solely from fitting the
342 spectra but uncertainty is introduced by scanning the spectra and by assuming that all oxygen
343 peaks contributing to the ^{17}O NMR spectra are symmetric (Gaussian). Considering these, we
344 estimate that the accuracy of our O^{2-} abundances is no better than about ± 4 mol% in O^{2-} . We
345 conclude that O^{2-} represents 10 ± 4 mol% of total oxygen in CMS33 glass and 18 ± 4 mol% in
346 CMS28 (Figs. 4b, 4d).

347 **O^{2-} in Other Ca_1Mg_1 -Silicate Glasses.** Schneider et al. (2000) report Q-species abundances
348 from a ^{29}Si MAS NMR spectrum of $\text{Ca}_{0.5}\text{Mg}_{0.5}\text{SiO}_3$ glass and calculation of oxygen species
349 abundances (Table 2) yielded 0.8 mol% O^{2-} . Taking $K_1 = 59.4$ and considering the stoichiometry

350 of Eq. (1) and $\Sigma X_{\text{O-species}} = 1.0$ (see Sawyer et al. 2015 for details), the percentages of BO, NBO
351 and O^{2-} calculated for this glass are respectively 35.2 mol%, 62.9 mol% and 1.9 mol%; O^{2-} is ~
352 double that obtained from the Q species abundances of Schneider et al. (2000). Their spectrum,
353 however, consisted of one broad, asymmetric peak with no defining shoulders or inflections and
354 the O^{2-} uncertainty associated with the Q species abundances is large. The same calculations
355 were applied to the disilicate glass ($\text{Ca}_{0.5}\text{Mg}_{0.5}\text{Si}_2\text{O}_5$) yielding 60.5%, 39.1% and 0.4%
356 respectively for BO, NBO and O^{2-} . No spectra are available for comparison.

357 **CaO-SiO₂ Glasses**

358 **CaSiO₃ (metasilicate) Glass.** Pedone et al. (2010) presented a theoretical treatment of CaSiO₃
359 glass. They emphasized that fits to ²⁹Si MAS NMR spectra using Gaussian line shapes do not
360 yield accurate Q-species abundances because some Q-species peaks are non-Gaussian. They
361 noted, however, that Gaussian peak shapes may be used to obtain reasonable Q-species
362 abundances from 2D ²⁹Si NMR spectra of CaSiO₃. Zhang et al. (1997) came to a similar
363 conclusion concerning the fitting of ²⁹Si MAS NMR spectra. We therefore focus on the 2D ²⁹Si
364 MAF NMR spectrum of Zhang et al. (1997) which is by far the most comprehensive study of this
365 glass. They list Q-species abundances consistent with their 2D ²⁹Si NMR spectrum (their Table
366 1) and report ~1 mol% O^{2-} in the glass. From their Q species values we calculated BO, NBO and
367 O^{2-} abundances with O^{2-} ~0.9 mol%. Values are listed in Table 2 and are plotted on Fig. 5a (X_{BO}
368 as shaded circles, X_{O_2} as crosses). Zhang et al. (1997) quoted one standard deviation uncertainty
369 (σ) in their Q species abundances and to assess the uncertainty in O^{2-} we applied 2σ to the Q³
370 and Q⁴ abundances, and decreased by 2σ , Q⁰ and Q¹ abundances. Q² was obtained from the
371 constraint that $\Sigma_{\text{Q-species}} = 100$. The maximum and minimum O^{2-} values obtained were 1.3 and 0.6
372 mol%. We conclude that $\text{O}^{2-} = 1.0 (\pm 0.4)$ mol%.

373 **Ca_{0.56}Si_{0.44}O_{1.44} (CS56) Glass.** Thompson et al. (2012) reported a ¹⁷O MAS NMR study of
374 Ca_{0.56}Si_{0.44}O_{1.44} glass (CS56) and used two methods to obtain NBO and BO abundances. The
375 more accurate method (Method#1) yielded 75.4 ±0.6 mol% NBO and 24.6 mol% BO whereas
376 the second (Method#2) yielded 76.9 ±1.2 mol% NBO and 23.1 mol% BO. Had the
377 polymerization reaction (Eq. 1) gone to completion (i.e., K₁ = ∞), two NBO atoms would be
378 present for each Ca atom in the glass so that NBO = 78.6 mol% and BO = 21.4 mol% at this
379 composition. By Method#1 or Method#2, BO is in excess of that expected if the reaction went to
380 completion. From the stoichiometry of Eq. (1), the excess in BO must equal the amount of
381 unreacted O²⁻ remaining in the glass; thus by Method#1 there is 3.2 mol% O²⁻ in the glass (24.6 –
382 21.4 = 3.2 mol% excess BO = 3.2 mol% unreacted O²⁻). By Method#2 the unreacted O²⁻
383 remaining in the glass is 1.7 mol%. Clearly the de-polymerization reaction (Eq. 1) did not go to
384 completion and there is free oxygen in the glass.

385 Thompson et al. (2012) did not observe a separate O²⁻ peak so that it may reside
386 underneath the NBO peak of the ¹⁷O NMR spectrum or elsewhere in the spectrum. If, for
387 example, it resided underneath the BO peak, then the O²⁻ values just calculated represent
388 minimum values. Uncertainty in the composition of the CS56 glass (Thompson et al. 2012) is
389 reflected in the uncertainty of the NBO and BO values (i.e., ±1.4 mol%; Thompson et al. 2012).
390 Considering the uncertainties, O²⁻ is evaluated at 3.2 mol% ±2.0 mol% by the more accurate
391 analytical method and 1.7 mol% ±2.6 mol% by ‘Method#2’. These are listed in Table 2. X_{BO} and
392 X_{O²⁻} were calculated and plotted on Fig. 5a as shaded circles and crosses. The oxygen species
393 abundances are entirely consistent with those of Zhang et al. (1997) and the results conform,
394 within experimental uncertainties, to the mass action equation with K₁ ~ 60 as shown in Fig. 5a
395 (solid curves represent O-species abundances for K₁ = 59.4). The apparent discrepancy between

396 Zhang et al. (1997), who state that O^{2-} is present in $CaSiO_3$ glass, and Thompson et al. (2012),
397 who state there is no evidence for O^{2-} in the 56.6 mol% CaO glass, is resolved by accepting the
398 ^{17}O NMR experimental results for CS56 glass of Thompson et al. (2012). We conclude that there
399 are a few mol% O^{2-} in Ca-silicate glasses ranging in composition from $CaSiO_3$ to Ca_2SiO_4 .

400 **MgO-SiO₂ Glasses**

401 **Mg₂SiO₄ Glass (orthosilicate).** Davis et al. (2011) conducted ^{29}Si 2D MAF NMR studies of
402 Mg_2SiO_4 glass and observed Q^1 species which, at this composition, necessarily indicates the
403 presence of BO and O^{2-} in equal amount. From their Q-species proportions (y_{Qn} values of their
404 Table 2) the mol% of NBO, BO and O^{2-} were calculated (Sawyer et al. 2015) to obtain BO = 4.5
405 ± 1 mol%, NBO = 91 ± 2 mol% and O^{2-} = 4.5 ± 1 mol% (Table 2). Sen et al. (2009) also report Q-
406 species distributions for Mg_2SiO_4 glass from a ^{29}Si MAS NMR study and obtained near-identical
407 results (BO:NBO: O^{2-} = 5:90:5, no uncertainties provided). A ^{29}Si static and MAS NMR study by
408 Sen and Tangeman (2008) report that Q^0 = 49 ± 4 mol% and Q^1 = 51 ± 4 mol% in Mg_2SiO_4 glass
409 from which BO:NBO: O^{2-} = 6.4:87.2:6.4 (Table 2). BO and O^{2-} uncertainties were evaluated at
410 ± 0.5 mol%. The three ^{29}Si NMR studies of Mg_2SiO_4 glass yield remarkably consistent results,
411 indicating between 4 and 7 mol% BO and O^{2-} (Table 2, Fig. 5a).

412 **MgSiO₃ Glass.** The ^{29}Si NMR studies of Davis et al. (2011) and Sen et al. (2009) provide Q-
413 species abundances for $MgSiO_3$ glass from which O-species abundances were calculated, listed
414 in Table 2 and plotted on Fig. 5a (shaded circles). The Davis et al. (2011) experiment yields 1.0
415 mol% O^{2-} whereas the results of Sen et al. (2009) give 2.6 mol% O^{2-} . Mountjoy et al. (2011) also
416 concluded that there was O^{2-} in $MgSiO_3$ glass based on his fit to a ^{17}O NMR spectrum.
417 Apparently, free oxide (O^{2-}) is present in $MgSiO_3$ glass at about the same level as found in the
418 $CaSiO_3$ glass of Zhang et al. (1997). The mass action equation with $K_1 = 59.4$ (Eq. 2) yields O^{2-}

419 ~ 1.9 mol% for metasilicate glass indicating that free oxide is of the same order in both Ca- and
420 Mg-metasilicate glasses.

421 Allwardt and Stebbins (2004) published a well resolved ^{17}O NMR spectrum of MgSiO_3
422 glass. It was left to Mountjoy et al. (2011) to fit the spectrum but they did not include the
423 extremities of the spectrum in their fit and in an attempt to determine details of the relationships
424 among the oxygen species we have scanned and fit the spectrum (Fig. 6). The strongest peak is,
425 according to Allwardt and Stebbins (2004), a NBO peak and like Stebbins and Sen (2013) we
426 use a symmetric Gaussian peak to fit it. Allwardt and Stebbins (2004) note the non-Gaussian
427 (quadrupole) BO lineshape of CaMg and Ca metasilicates and the tail on the right side of Fig. 6
428 suggests a quadrupole lineshape for BO of MgSiO_3 glass. Two Gaussian peaks were employed
429 (Fig. 6, BO#1 and BO#2) solely to fit the low frequency part of the spectrum and to obtain the
430 area of the BO contribution (the peaks have no other significance). The broad contribution
431 extending from ~ 70 to ~ 180 ppm was fit with a Gaussian lineshape and is labelled ‘?’. Its origin
432 is uncertain. Areas (%) of each contribution are provided in Fig. 6 and fit parameters are given in
433 Table 1. An alternative fit to the spectrum would have a linear background extending from -150
434 ppm to about 100 ppm. Such a background would obviate the need to introduce the peak labelled
435 ‘?’. A least squares fit using this background, the NBO, BO#1 and BO#2 peaks yields, however,
436 NBO and BO peak areas similar to the values shown in Fig. 6.

437 The coordination number of free oxygen (O^{2-}) in Mg-silicate melts and glasses cannot yet
438 be determined with certainty and as a result, neither can its position in the ^{17}O NMR spectrum.
439 The NBO and BO contents, however, can be used to estimate of O^{2-} abundance. Normalizing the
440 BO and NBO peak areas listed in Fig. 6 to 100%, then NBO = 63.4% and BO = 36.6%. If the
441 polymerization reaction (Eq. 1) had gone to completion (all O^{2-} consumed) the BO content

442 would be 35.1%, indicating a ~1.5 mol% excess of BO in the glass (i.e., the reaction did not go
443 to completion). By the stoichiometry of the polymerization reaction there is an amount of
444 unreacted O^{2-} in the glass equal to the excess BO (i.e., $O^{2-} \sim 1.5$ mol%). Assuming the 1.5 mol%
445 O^{2-} is under the peak labelled “?” of Fig. 6 (and renormalizing the three O contributions to 100
446 mol%) the proportions of oxygen species (NBO:BO: O^{2-}) $\sim 62.4:36.1:1.5$.

447 The uncertainty associated with the O^{2-} mol% cannot be readily evaluated because the
448 spectrum was scanned. The value of 1.5 mol% O^{2-} in the $MgSiO_3$ glass is, however, consistent
449 with the results of Davis et al. (2011) and Sen et al. (2009), with all three NMR results indicating
450 1.5 (± 1) mol% O^{2-} . Equally important, *all* eight NMR spectral results for Mg_2SiO_4 and $MgSiO_3$
451 glasses, and CMS33 and CMS28 glasses, are consistent with the mass action equation (Eq. 2)
452 where $K_1 \sim 60$ (Nasikas et al. 2012; Davis et al. 2011; Sen et al. 2009; Sen and Tangeman, 2008;
453 Allwardt and Stebbins, 2004).

454 **Other Experimental Studies.** Tangeman et al. (2001) report Q^1 species in the ^{29}Si MAS NMR
455 spectrum of Mg_2SiO_4 glass but do not provide Q-species abundances. Nevertheless, the
456 identification of Q^1 species for this glass composition requires the presence of O^{2-} . Kohara et al.
457 (2004) conducted X-ray and neutron scattering on Mg_2SiO_4 glass which revealed MgO_4 , MgO_5
458 and MgO_6 polyhedra. Some oxygen atoms bridge only the polyhedra making them O^{2-} using our
459 nomenclature. Kohara et al. (2011) used Reverse Monte Carlo fits to diffraction data and density
460 functional theory to model $MgSiO_3$ and Mg_2SiO_4 glasses and again concluded that MgO
461 polyhedra existed in these glasses. The three studies require O^{2-} to be present and indicate that K_1
462 is finite. The conclusions are also consistent with MD simulations as now discussed.

463 **EVIDENCE FOR FREE OXIDE FROM MD SIMULATIONS**

464 Molecular Dynamics (MD) simulations on Ca and Mg silicate systems discussed below

465 indicate mol% levels of O^{2-} in Ca, Mg and CaMg silicate glasses. There are 9 metasilicate, 4
466 orthosilicate MD simulations, and 3 simulations of compositions intermediate between
467 metasilicate and orthosilicate glass, for a total of 16 simulations. All indicate the presence of O^{2-} .
468 In this regard, MD simulations, O 1s XPS, NMR and Raman results are remarkably consistent.
469 The oxygen species abundances derived from these studies are collated and presented in Table 3,
470 and X_{BO} and $X_{O^{2-}}$ values are plotted on Fig. 5b.

471 **CaMg-Silicate Glasses**

472 Al-Hasni and Mountjoy (2014) reported MD simulations of glasses ranging in
473 composition from $MgSiO_3$ (metasilicate) to Mg_2SiO_4 (orthosilicate). They report Q-species
474 abundances and from these the O-species abundances were calculated, tabulated (Table 3) and
475 plotted on Fig. 5b. All plot above the curve where $K_1 = \infty$ indicating that free oxygen is present
476 at all compositions although in somewhat greater concentrations than obtained from the ^{17}O
477 NMR results (Fig. 5a, diamonds). Mead and Mountjoy (2006), Mountjoy et al. (2011) and Al-
478 Hasni and Mountjoy (2014) emphasize that simulated quench rates are much greater than
479 experimental rates ($\sim 10^{10}$ times). If the structure has not completely adjusted to the quenched
480 temperatures, the distribution of species (e.g., Q species and O species) may retain residual
481 distributions reflective of a greater temperature. To summarize, the MD studies may apply to
482 temperature conditions different from those of the ^{17}O NMR study (Nasikas et al. 2012). If this
483 situation holds one must conclude that O^{2-} is present in the glasses and that it is more abundant in
484 melts (high temperature) than in glasses at ambient temperature.

485 MD simulations on Ca-Mg metasilicate glasses by Cormier and Cuello (2013) include
486 four glasses containing ~ 50 mol% SiO_2 , but they have differing proportions of CaO and MgO.
487 They list BO, NBO and O^{2-} mol% in their Fig. 9 and these have been extracted, tabulated (Table

488 3) and plotted on Fig. 5b. All contain free oxide and are consistent with the results of Al-Hasni
489 and Mountjoy (2014). MD simulations indicate that O^{2-} is present at mol% levels in invert
490 MgCa-silicate glasses. Secondly, K_1 is finite in this ternary system so that the three oxygen
491 species must exist at all compositions within the system. We emphasize, however, that O^{2-}
492 should be very low in all highly siliceous glasses, and perhaps beyond the detectability.

493 **Mg-Silicate Glasses**

494 Ghosh et al. (2014) conducted MD simulations on $MgSiO_3$ glass from which they list Q
495 species abundances. The Q species distribution of their lowest pressure simulation yields O^{2-} of
496 ~ 3.4 mol% (Table 3). Mountjoy et al. (2011) conducted an MD simulation of $MgSiO_3$ and
497 reported that it contained ~ 4.5 mol% O^{2-} in the glass, which compares favourably with the result
498 of Ghosh et al. (2014). They did not, however, report BO and NBO abundances nor Q species
499 abundances so that BO and NBO abundances are not recorded in Table 3.

500 Spiekermann et al. (2013) conducted MD simulations of Mg_2SiO_4 , $MgSiO_3$ and $MgSi_2O_5$
501 glasses. They quoted Q-species abundances and from these the oxygen species concentrations
502 were determined and listed in Table 3. O^{2-} was present at 7.8 mol% in Mg_2SiO_4 glass, at 4.8
503 mol% in $MgSiO_3$ glass and 0.8 mol% O^{2-} was present in $MgSi_2O_5$ glass. These free oxygen
504 abundances are commensurate with O^{2-} concentrations in the CaMg-silicate glasses of Al-Hasni
505 and Mountjoy (2014).

506 Sen and Tangeman (2008) and de Koker et al. (2009) report MD simulations of Mg_2SiO_4
507 glass and melt, and they provide Q-species abundances. The Sen and Tangeman (2008) result
508 gives 5 mol% O^{2-} for Mg_2SiO_4 glass and de Koker et al. (2009) yields 15 mol% for the same
509 glass composition (Table 3). These results straddle X_{BO} curve for $K_1 = 59.4$ on Fig. 5b. The de
510 Koker et al. (2009) result (Table 3) is almost identical to the Mg_2SiO_4 result of Al-Hasani and

511 Mountjoy (2014) and the Sen and Tangeman (2008) result is similar to the Mg_2SiO_4 of
512 Spiekermann et al. (2013). These MD simulations are remarkably consistent with respect to O^{2-}
513 abundances in glasses ranging in composition from the disilicate (MgSi_2O_5) to Mg_2SiO_4 .

514 **Ca-silicate Glasses**

515 Mead and Mountjoy (2006) and Cormier and Cuello (2013) provide MD simulations of
516 Ca-metasilicate glass. The former study reports Q-species abundances where $\text{Q}^0:\text{Q}^1\text{Q}^2:\text{Q}^3:\text{Q}^4 =$
517 $6:23:40:25:8$. From these values the O species abundances were calculated and are listed in
518 Table 3. Cormier and Cuello (2013) plot Q species abundances and from the plot $\text{Q}^0:\text{Q}^1\text{Q}^2:\text{Q}^3:\text{Q}^4$
519 $\sim 5:24:36:28:7$. They also plot oxygen species abundances in their Fig. 9 and these have been
520 extracted and included in Table 3, and plotted on Fig. 5b. The Mead and Mountjoy (2006) result
521 indicates 1.0 mol% O^{2-} in the glass whereas the Cormier and Cuello (2013) result yields 1.3
522 mol% O^{2-} . These results agree with the 2D ^{29}Si MAF NMR experimental result (Zhang et al.
523 1997) which gives 1.0 (± 0.4) mol% O^{2-} . Wu et al. (2015) conducted MD simulations on the
524 CaO-SiO₂ system. They plotted their oxygen species on diagrams and these have been extracted
525 and included in Table 3 and plotted on Fig. 5b. The O^{2-} values are similar to those of Al-hasni
526 and Mountjoy (2014) for the Mg-silicate system. Pedone et al. (2010) determine Q species
527 abundances for CaSiO₃ glass using approaches different from the above two MD studies. One
528 model indicates minor O^{2-} with $\text{Q}^0:\text{Q}^1\text{Q}^2:\text{Q}^3:\text{Q}^4 \sim 0:23:53:17:7$ and the second yields
529 $\text{Q}^0:\text{Q}^1\text{Q}^2:\text{Q}^3:\text{Q}^4 \sim 0:27:50:20:3$ but these give a physically impossible BO value (Fig. 6) and a
530 negative O^{2-} value.

531 A ^{29}Si MAS NMR spectrum for CaSiO₃ glass redrawn after Zhang et al. (1997) is
532 reproduced in Fig. 7a along with their free fit to the spectrum. Zhang et al. (1997) emphasize that
533 the fit to Fig. 7a is incorrect in that Q^2 is too abundant and Q^0 , Q^1 and Q^4 are absent. They

534 obtained more accurate Q species values by projecting their 2D ^{29}Si MAF NMR spectrum onto
535 the MAS dimension and fitting Q species signals to the projected spectrum using constraints
536 derived from the 2D ^{29}Si MAF NMR spectrum. The projected spectrum and fit are illustrated in
537 Fig. 7b. The Q species distributions of Mead and Mountjoy (2006), Cormier and Cuello (2013)
538 and Pendone et al. (2010) agree better with the Q species distribution of Fig 7b than with that of
539 Fig. 7a. Accepting the fit in Fig. 7b, we conclude that Q species distributions derived from the
540 simulations are as accurate as Q species abundances derived from a *free fit* to the ^{29}Si MAS
541 NMR spectrum of CaSiO_3 glass. The Q^2 peak, for example (Fig. 7a) is very broad, primarily
542 because there is no spectral feature to constrain its width. Poor spectral resolution (i.e., no strong
543 shoulders or minima) precludes extraction of accurate Q species abundances from Fig. 7a or
544 from any similarly resolved spectrum.

545 **Implications**

546 The high resolution of the new generation of XPS instrument has been used to detect, and
547 for the first time to accurately quantify the amount, of O^{2-} (free oxygen) in binary silicate Pb
548 glasses. The advance results primarily from a technical development whereby surface charging
549 of insulators (e.g., silicate glasses) is effectively eliminated. This, coupled with detailed
550 knowledge of O 1s XPS lineshapes and linewidths, allows for accurate measurement of oxygen
551 species in binary glasses (e.g., Sawyer et al., 2015; 2012; Nesbitt et al., 2011). Once measured at
552 one composition, the equilibrium constant for Eq. 2 allows calculation of oxygen species
553 abundances in more siliceous glasses. The mass action equation relating the three oxygen species
554 (Eq. 2) necessarily holds across the *entire* binary silicate system, requiring all three species to be
555 present in all binary melts where equilibrium is established. Most emphatically, O^{2-} is an
556 essential, thermodynamically important constituent of binary Pb, Ca and Mg silicate melts and

557 glasses. Clearly, O^{2-} obtained in MD simulations is *not* just an ‘accidental product’ associated
558 with (rapid) cooling rates employed in the simulations (Cormier and Cuello, 2013).

559 Determination of O species abundances in silicate melts has exceedingly important
560 implications concerning the reactivity of glasses. Of the three oxygen species O^{2-} is by far the
561 most basic and will be much more reactive toward H_2O , CO_2 and sulfur gases than will be BO or
562 NBO (Sawyer et al., 2015). There is also a large supply of O^{2-} in melts. Any O^{2-} consumed by
563 reaction will be replenished via reaction (1) according to the principle of Le Chatelier. Reaction
564 (1) acts like a classic buffer maintaining near-constant O^{2-} abundances in melts during reaction.
565 The buffer capacity of the reaction may be exceedingly large and is dependent primarily on the
566 NBO content of the melt or glass. As a result, even low concentrations of O^{2-} may control
567 reaction rates due to its continual replenishment.

568 Accurate quantification of O 1s XPS, 2D ^{17}O NMR spectra and 2D ^{29}Si NMR spectra
569 now can be achieved (e.g., Fig. 1; Davis et al., 2010; Florian et al., 1996; Farnan et al., 1992).
570 Interpretation and quantification of many published spectra, however, are very difficult because
571 spectra are poorly resolved, or lineshapes and linewidths are uncertain with spectral properties
572 varying according to experimental conditions and glass compositions. As a result of these
573 problems, many ^{17}O NMR, ^{29}Si MAS NMR and XPS O 1s spectra have been published with no
574 fits (or only partial fits) yet species abundances have been quoted based on the spectra.
575 Unfortunately, without complete fits, quoted abundances of species cannot be tested or verified
576 and must be questioned. Here, we have attempted to show how detailed, complete fitting of
577 spectra, combined with the use of mass and charge balances, can be used to extract species
578 abundances from complex spectra, and to assign realistic uncertainties to the abundances.

579

CONCLUSIONS

580 There is direct O 1s XPS experimental evidence for ~35 mol% O²⁻ in the Pb-silicate glass
581 containing 76.6 mol% PbO. This amount is consistent with the ²⁹Si MAS NMR and O 1s XPS
582 results for the binary, and with the mass action equation where K₁ ~12. There is also direct ¹⁷O
583 NMR experimental evidence for ~ 10 mol% O²⁻ in CaMg-orthosilicate glass (Nasikas et al.
584 2012). 2D ²⁹Si MAF NMR spectral evidence demonstrates ~ 1 mol% O²⁻ in Ca-metasilicate glass
585 (Zhang et al. 1997) and the ¹⁷O NMR result a glass containing 56.6 mol% CaO yields ~3 mol%
586 O²⁻ (Thompson et al. 2012). Eight separate NMR results for Mg-silicate glasses indicate ~1
587 mol% O²⁻ in MgSiO₃ glass and ~5 mol% or more in Mg₂SiO₄ glass (Table 2). Importantly the
588 CaMg silicate, Ca silicate and Mg-silicate glasses are thermodynamically consistent indicating
589 that K₁ ~ 60 with uncertainties considered. Many MD calculations pertaining to Mg-silicate
590 glasses CaMg-silicate glasses have indicated O²⁻ at the 0.5 to 15 mol% range (Table 3). From
591 these results we conclude that free oxide is present in the binary CaO-SiO₂, MgO-SiO₂ and likely
592 is present in ternary CaO-MgO-SiO₂ glasses and melts. The most reliable ²⁹Si NMR studies are
593 the 2-D ²⁹Si NMR type (e.g., Davis et al. 2011; 2010; Zhang et al. 1997; 1996).

594 ACKNOWLEDGEMENTS

595 Financial support for this research was provided by Discover Grants from the National
596 Science and Engineering Council of Canada (NSERC) to H.W. Nesbitt, Henderson, and R.A.
597 Secco. We thank Surface Science Western for providing access to the XPS instrument and thank
598 Dr. M. Biesinger who oversaw its use.

599

600 References

601 Al-Hasni, B.M., and Mountjoy G. (2014) A molecular dynamics study of the atomic structure of
602 $x(\text{MgO})_{100-x}(\text{SiO}_2)$. Journal Non-Crystalline Solids, 389, 33–44.

- 603 Allwardt, J.R., and Stebbins, J.F. (2004) Ca-Mg and K-Mg mixing around non-bridging O atoms
604 in silicate glasses: An investigation using ^{17}O MAS and 3QMAS NMR. American
605 Mineralogist, 89, 777-784.
- 606 Bancroft G.M., Nesbitt H.W., Ho R., Shaw D.M., Tse J.S., and Biesinger M.C. (2009) Toward a
607 comprehensive understanding of solid state core-level XPS linewidths: experimental and
608 theoretical studies on the Si 2p and O 1s linewidths in silicates. Physical Review B
609 80,075405.
- 610 Cormier, L., and Cuello, G.J. (2013) Ca and Na environments in $\text{Na}_2\text{O}-\text{CaO}-\text{Al}_2\text{O}_3-\text{SiO}_2$
611 glasses: influence of cation mixing and cation-network interactions. Geochimica et
612 Cosmochimica Acta, 122, 498-510. doi.org/10.1016/j.gca.2013.04.026.
- 613 Dalby, K.N., Nesbitt, H.W., Zakaznova-Herzog, V.P., and King, P.L. (2007) Resolution of
614 bridging oxygen signals from O 1s spectra of silicate glasses using XPS: Implications for
615 O and Si speciation. Geochimica et Cosmochimica Acta, 71, 4297-4313.
- 616 Davis, M.C., Kaseman, D.C., Parvani, S.M., Sanders, K.J., Grandinetti, P.J., Massiot, D., and
617 Florian, P. (2010) $Q^{(n)}$ Species Distribution in $\text{K}_2\text{O}\cdot 2\text{SiO}_2$ Glass by ^{29}Si Magic Angle
618 Flipping NMR. Journal of Physical Chemistry A, 114, 5503-5508.
- 619 Davis, M.C., Sanders, K.J., Grandinetti, P.J., Gaudio, S.J., and Sabyasachi, S. (2011) Structural
620 investigations of magnesium silicate glasses by ^{29}Si 2D Magic-Angle Flipping NMR.
621 Journal of Non-Crystalline Solids, 357, 2787-2795.
- 622 de Koker, N.P., Stixrude, L., and Karki, B.B. (2009) Thermodynamics, structure, dynamics, and
623 freezing of Mg_2SiO_4 liquid at high pressure. Geochimica et Cosmochimica Acta, 72,
624 1427-1441.
- 625 Du, J., and Cormack, A.N. (2004) The medium range structure of sodium silicate glasses: a

- 626 molecular dynamics simulation. *Journal of Non-Crystalline Solids*, 349, 66–79.
- 627 Farnan, I., Grandinetti, P.J., Baltisberger, J.H., Stebbins, J.F., Werner, U., Eastman, M.A., and
628 Pines, A. (1992) Quantification of the disorder in Network-modified silicate glasses.
629 *Nature*, 38, 31-35.
- 630 Fayon, F., Bessada, C., Massiot, D., Farnan, I., and Coutures, J.P. (1998) ^{29}Si and ^{207}Pb NMR
631 study of local order in lead silicate glasses. *Journal of Non-Crystalline Solids*, 232-234,
632 403-408.
- 633 Fincham, C.F.B., and Richardson, F.D. (1954) The Behaviour of Sulphur in Silicate and
634 Aluminate Melts. *Proceedings of the Royal Society of London*, A223, 40-62.
- 635 Florian, P., Vermillion, K.E., Grandinetti, P.J., Farnan, I., and Stebbins, J.F. (1996) Cation
636 Distribution in Mixed Alkali Disilicate Glasses. *Journal of American Chemical Society*,
637 118, 3493-3497.
- 638 Furukawa, T., Brawer, S.A., and White, W.B. (1978) The structure of lead silicate glasses
639 determined by vibrational spectroscopy. *Journal of Materials Science*, 13, 268-282.
- 640 Ghosh, D.P., Karki, B.B., and Stixrude, L. (2014) First-principles molecular dynamics
641 simulations of MgSiO_3 glass: Structure, density, and elasticity at high pressure. *American*
642 *Mineralogist*, 99, 1304-1314.
- 643 Henderson, G.S. (2005) The structure of silicate melts: a glass perspective. *Canadian*
644 *Mineralogist*, 43, 1921-1958.
- 645 Henderson, G.S., Calas, G., and Stebbins J.F. (2006) The structure of silicate glasses and melts.
646 *Elements*, 2, 269-273.
- 647 Iwamoto, N., Tsunawaki, Y., and Miyago, M. (1979) Structural Study of PbO-SiO_2 Slags by
648 Raman Spectroscopy. *Journal of Japanese Institute of Metals*, 43, 1138-1144.

- 649 Kohara, S., Suzuya, K., Takeuchi, K., Loong, C.-K., Grimstitch, M., Weber, J.K.R., Tangeman,
650 A., and Key, S. (2004) Glass Formation at the Limit of Insufficient Network Formers.
651 Science, 303, 1649- 1652.
- 652 Kohara, S., Akola, J., Morita, H., Suzuya, K., Weber, J.K.R., Wilding, M.C., and Benmore, C.J.
653 (2011) Relationship between topological order and glass forming ability in densely
654 packed enstatite and forsterite composition glasses. Proceedings of the National Academy
655 of Sciences, 108, 14780-14785.
- 656 Lee, S.K., and Kim, E.J. (2015) Probing metal-bridging oxygen and configurational disorder in
657 amorphous lead silicate: insights from ^{17}O solid-state nuclear magnetic resonance.
658 Physical Chemistry C, 119, 748-756.
- 659 Mead, R.N., and Mountjoy, G. (2006) A Molecular Dynamics Study of the Atomic Structure of
660 $(\text{CaO})_x(\text{SiO}_2)_{1-x}$ Glasses. Journal of Physical Chemistry B, 110, 14273-14278.
- 661 Mountjoy, G. (2007) The local atomic environment of oxygen in silicate glasses from molecular
662 dynamics. Journal of Non-Crystalline Solids. 353, 1849–1853.
- 663 Mountjoy, G., Al-Hasni, B.M., and Storey, C. (2011) Structural organisation in oxide glasses
664 from molecular dynamics modelling. Journal of Non-Crystalline Solids. 357, 2522–2529.
- 665 Mysen, B.O. (2003) Physics and Chemistry of silicate glasses and melts. European Journal of
666 Mineralogy, **15**, 781-802.
- 667 Nasikas, N.K., Chrissanthopoulos, A., Bouropoulos, N., Sen, S., and Papatheodorou (2011)
668 Silicate Glasses at the Ionic Limit: Alkaline-Earth Sub-Orthosilicates. Chemistry of
669 Materials, 23, 3692–3697.

- 670 Nasikas, N.K., Edwards, T.G., Sen, S., and Papatheodorou, G.N. (2012) Structural
671 Characteristics of Novel Ca–Mg Orthosilicate and Suborthosilicate Glasses: Results from
672 ^{29}Si and ^{17}O NMR Spectroscopy. *Journal of Physical Chemistry B*, 116, 2696-2702.
- 673 Nesbitt, H.W., Bancroft, G.M., Davidson, R., McIntyre, N.S., and Pratt, A.R. (2004) Minimum
674 XPS core-level line widths of insulators, including silicate minerals. *American*
675 *Mineralogist*, 89, 878-882.
- 676 Nesbitt, H.W., Bancroft, G.M., Henderson, G.S., Ho, R., Dalby, K.N., Huang, Y., and Yan, Z.
677 (2011) Bridging, non-bridging and free (O^{2-}) oxygen in $\text{Na}_2\text{O-SiO}_2$ glasses: An X-ray
678 Photoelectron Spectroscopic (XPS) and Nuclear Magnetic Resonance (NMR) study,
679 *Journal of Non-Crystalline Solids*, 357, 170-180.
- 680 Nesbitt, H.W., and Bancroft, G.M. (2014) High Resolution Core- and Valence-Level XPS
681 Studies of the Properties (Structural, Chemical and Bonding) of Silicate Minerals and
682 Glasses. *Reviews in Mineralogy and Geochemistry*, Geological Society of America, 78,
683 271-329.
- 684 Nesbitt, H.W., Bancroft, G.M., Thibault, Y., Sawyer, R., and Secco, R.A. (2015a) Aspects
685 concerning spectroscopic studies of oxygen speciation in potassium silicate glasses and
686 melts. *Canadian Journal of Chemistry*, in press.
- 687 Nesbitt, H.W., Henderson, G.S., Bancroft, G.M., and Ho, R. (2015b) Experimental evidence for
688 Na coordination to bridging oxygen in Na-silicate glasses: Implications for spectroscopic
689 studies and for the modified random network model. *Journal of Non-Crystalline Solids*,
690 409, 139–148.
- 691 Park, J.H., and Rhee, P.C-H. (2001) Ionic properties of oxygen in slag. *Journal of Non-*
692 *Crystalline Solids*, 282, 7-14.

- 693 Pedone, A., Charpentier, T., and Menziani, M.C. (2010) Multinuclear NMR of CaSiO₃ glass:
694 simulation from first-principles. *Physical Chemistry and Chemical Physics*, 12, 6054–
695 6066.
- 696 Retsinas, A., Kalampounias, A.G., and Papatheodorou, G.N. (2014) Reaching the ionic limit in
697 the (1-X)[Ca_{0.5}-Mg_{0.5}]O–XSiO₂ pseudo binary glass system with 0.5 < X < 0.27: Glass
698 formation and structure. *Journal of Non-Crystalline Solids*. 383, 38-43.
- 699 Rybicki, J., Rybicka, A., Witkowska, A., Bergmanski, G., Di Cicco, A., Minicucci, M., and
700 Mancini, G. (2001) The structure of lead-silicate glasses: molecular dynamics and
701 EXAFS studies. *Journal of Physics of Condensed Matter*, 13, 9781-9797.
- 702 Sawyer, R., Nesbitt, H.W., and Secco, R.A. (2012) Three types of oxygen in K₂O-SiO₂ glasses:
703 an X-ray photoelectron spectroscopy (XPS) study. *Journal of Non-Crystalline Solids* 358,
704 290-302.
- 705 Sawyer, R., Nesbitt, H.W., Bancroft, G.M., Thibault, Y., and Secco, R.A. (2015) Spectroscopic
706 Studies of Oxygen Speciation in K-silicate Glasses and Melts. *Canadian Journal of*
707 *Chemistry*, 93, 60-73.
- 708 Schneider, J., Mastelaro, V.R., Panepucci, H., and Zanutto, E.D. (2000) ²⁹Si MAS-NMR studies
709 of Qⁿ structural units in metasilicate glasses and their nucleating ability. *Journal of Non-*
710 *Crystalline Solids*, 273, 8-18.
- 711 Sen, S., and Tangeman, J. (2008) Evidence for anomalously large degree of polymerization in
712 Mg₂SiO₄ glass and melt. *American Mineralogist*, 93, 946-949.
- 713 Sen, S., Maekawa, H., and Papatheodorou, G.N. (2009) Short-range structure of invert glasses
714 along the pseudo-binary join MgSiO₃-Mg₂SiO₄: results from ²⁹Si and ²⁵Mg NMR
715 spectroscopy. *Journal of Physical Chemistry*, 113, 15243-15248.

- 716 Shirley D.A. (1972) High resolution x-ray photoemission spectrum of the valence bands of Au.
717 Physical Review B 5, 4709-4714.
- 718 Smets, B.M.J., and Lommen, T.P.A. (1982) The structure of glasses and crystalline compounds
719 in the system PbO-SiO₂, studied by x-ray photoelectron spectroscopy. Journal of Non-
720 Crystalline Solids, 48, 423-430.
- 721 Spiekermann, G., Steele-MacInnis, M., Kowalski, P.M., Schmidt, C., and Jahn, S. (2013)
722 Vibrational properties of silica species in MgO-SiO₂ glasses obtained from ab initio
723 molecular dynamics. Chemical Geology, 346, 22-33.
- 724 Stebbins, J.F. (1995) Dynamics and structure of silicate and oxide melts: nuclear magnetic
725 resonance studies. In Structure, Dynamics, and Properties of Silicate Melts (J.F. Stebbins,
726 P.F. McMillan & D.B. Dingwell, eds.). *Reviews in Mineralogy*, **32**, 141-245.
- 727 Stebbins, J.F., and Sen, S. (2013) Oxide ion speciation in potassium silicate glasses: New limits
728 from ¹⁷O NMR. Journal of Non-Crystalline Solids, 368, 17-22
- 729 Takaishi, T., Takahashi, M., Jin, J., Uchino, T., and Yoko, T. (2005) Structural Study on PbO-
730 SiO₂ Glasses by X-Ray and Neutron Diffraction and ²⁹Si MAS NMR Measurements.
731 Journal of American Ceramics Society, 88, 1591-1596.
- 732 Tangeman, J.A., Phillips, B.L., Navrotsky, A., Weber, J.K.R., Hixson, A.D., and Key, T.S.
733 (2001) Vitreous forsterite (Mg₂SiO₄): Synthesis, structure, and thermochemistry.
734 Geophysical Research Letters, 28, 2517-2520.
- 735 Thompson, L.M., McCarty, R.J., and Stebbins, J.F. (2012) Estimating accuracy of ¹⁷O NMR
736 measurements in oxide glasses: Constraints and evidence from crystalline and glassy
737 calcium and barium silicates. Journal of Non-Crystalline Solids, 358, 2999-3006.
- 738 Toop, G.W., and Samis, C.S. (1962) Activities of ions in silicate melts. Transactions of the

- 739 Metallurgical Society of AIME, 224, 878-887.
- 740 Wu, T., He, S., Liang, Y., and Wang, Q. (2015) Molecular dynamics simulation of the structure
741 and properties for the CaO–SiO₂ and CaO–Al₂O₃ systems. *Journal of Non-Crystalline*
742 *Solids*, 411, 145–151
- 743 Zakaznova-Herzog, V.P., Nesbitt, H.W., Bancroft, G.M., Tse, J.S., Gao, X., and Skinner, W.
744 (2005) High-resolution valence-band XPS spectra of the nonconductors quartz and
745 olivine. *Physical Review B* 72, 205113-1 – 205113-13.
- 746 Zakaznova-Herzog, V.P., Nesbitt, H.W., Bancroft, G.M., and Tse, J.S. (2006) High resolution
747 core and valence band XPS spectra of non-conductor pyroxenes. *Surface Science*, 600,
748 3175-3186.
- 749 Zakaznova-Herzog, V.P., Nesbitt, H.W., Bancroft, G.M., and Tse, J.S. (2008) Characterization
750 of leached layers on olivine and pyroxenes using high-resolution XPS and density
751 functional calculations. *Geochimica et Cosmochimica Acta*, 72, 69–86
- 752 Zhang, P., Dunlap, C., Florian, P., Grandinetti, P.J., Farnan, I., and Stebbins, J.F. (1996) Silicon
753 site distributions in alkali silicate glass derived by two-dimensional ²⁹Si nuclear magnetic
754 resonance. *Journal of Non-crystalline Solids*, 204, 294-300.
- 755 Zhang, P., Grandinetti, P.J., and Stebbins, J.F. (1997) Anionic Species Determination in CaSiO₃
756 Glass Using Two-Dimensional ²⁹Si NMR, *Journal of Physical Chemistry B*, 101, 4004-
757 4008

758

759 **Figure Captions**

760 Fig. 1: O 1s XPS spectra of Pb-silicate glass containing 50 mol% PbO (Fig. 1a), 67 mol% PbO

761 (Fig. 1b) and 77 mol% PbO (Fig. 1c). The shaded dots represent the experimental data,
762 the thin curves represent the fitted peaks and the background, and the thicker curve
763 represents the fit to the data. The data of Figs. 1a and 1b are taken from Dalby et. al.
764 (2007).

765 Fig. 2: Illustrates two 3-peak fits to the O 1s XPS spectrum of Pb77 glass (76.6 mol% PbO)
766 using different constraints to fit an O^{2-} peak to the spectrum. (a) represents a fit where the
767 FWHM of the BO and NBO peaks were constrained to 1.22 eV and the third peak was
768 unconstrained. (b) represents a fit where the FWHM of the BO peak was constrained to
769 1.22 eV and the proportions of the BO, NBO and O^{2-} peaks were constrained to
770 10.8:54.2:35.0 which are the ratios derived from the fit to Fig. 1c (see text for explanation
771 and Sawyer et al. 2014 for the calculation of O-species abundances).

772 Fig. 3: Illustrates the BO and O^{2-} abundances from experimental results. BO and O^{2-} mole
773 fractions (large and small shaded squares respectively) were calculated from the Q-
774 species abundances obtained from the ^{29}Si MAS NMR results of Fayon et al. (1998). The
775 The large and small shaded circles represent respectively BO and O^{2-} mole fractions
776 calculated from the O 1s XPS results (Dalby et al. 2007). The large and small dots
777 represent respectively the BO and O^{2-} mole fractions obtained by fitting the spectrum of
778 the Pb77 glass (Fig. 1c) and the error bars illustrate the compositional uncertainty. The
779 uncertainty in X_{BO} and $X_{\text{O}^{2-}}$ is ± 0.02 . The thick solid curve illustrates X_{BO} calculated
780 from Eq. (2) with $K_1 = 12.0$. The dotted, dashed and dash-dot curves represent
781 respectively X_{BO} , X_{NBO} and $X_{\text{O}^{2-}}$ calculated for $K_1 = \text{infinity}$ (i.e., the polymerization
782 reaction goes to completion).

783 Fig. 4: Fits to the ^{17}O NMR spectra for the Ca_1Mg_1 -silicate glasses containing 28 and 33 mol%

784 SiO₂ (respectively CMS28 and CMS33 glasses) of Nasikas et al. (2012). (a) and (b)
785 represent two-peak fits to the CMS33 and CMS28 glasses. (c) and (d) represent three
786 peak fits to the same glasses using the same method employed to fit the Pb77 glass of
787 Fig. 2b. (e) and (f) represent the residuals to (c) and (d). The dotted curves represent the
788 spectra published by Nasikas et al. (2012). They were scanned and fitted to quantify these
789 important spectra because no fits were provided in the original publication.

790 Fig. 5: Illustrates oxygen species abundances as a function of composition (mole fraction of MO
791 where MO = MgO, CaO, or CaO+MgO). (a) All data were obtained from experimental
792 studies (see text for sources). All data plot above the dashed curve labelled $K_1 = \infty$. (b) all
793 data were obtained from MD calculations (see text for sources). The solid curves
794 represent the mole fractions of BO, NBO and O²⁻ calculated for $K_1 = 59.4$ (see Eq. 2).
795 The dashed curves represent the mole fractions of the same species calculated for $K_1 =$
796 infinity. The shaded areas represent physically impossible values for X_{BO} .

797 Fig. 6: Fit to the ¹⁷O NMR spectrum of MgSiO₃ glass. The dots represent the scanned spectrum
798 (after Allwardt and Stebbins, 2004) and the curve intersecting the dots is the overall fit to
799 the spectrum. The origin of the peak labelled ‘?’ is uncertain but likely represents a
800 spinning sideband and perhaps O²⁻. The total BO contribution (solid curve) is asymmetric
801 and is the sum of peaks BO#1 and BO#2. These two BO peaks have no significance other
802 than to allow an estimate of the total BO contribution to the spectrum.

803 Fig. 7: (a) ²⁹Si MAS NMR spectrum of CaSiO₃ glass (solid thick curve) and free fit to the
804 spectrum (redrawn after Zhang et al. 1997, their Fig. 5). The dashed curves represent the
805 freely fit curve for each Q species. (b) Projection of the total intensity onto the isotropic
806 dimension and fit after Zhang et al. (1997; their Fig. 4). The solid thick curve represents

807 the MAS spectrum shown in Fig. 7a and the dashed curves represent the Q species with
808 each lineshape determined from the 2D ^{29}Si MAF NMR spectrum (Zhang et al. 1997,
809 Fig. 3).

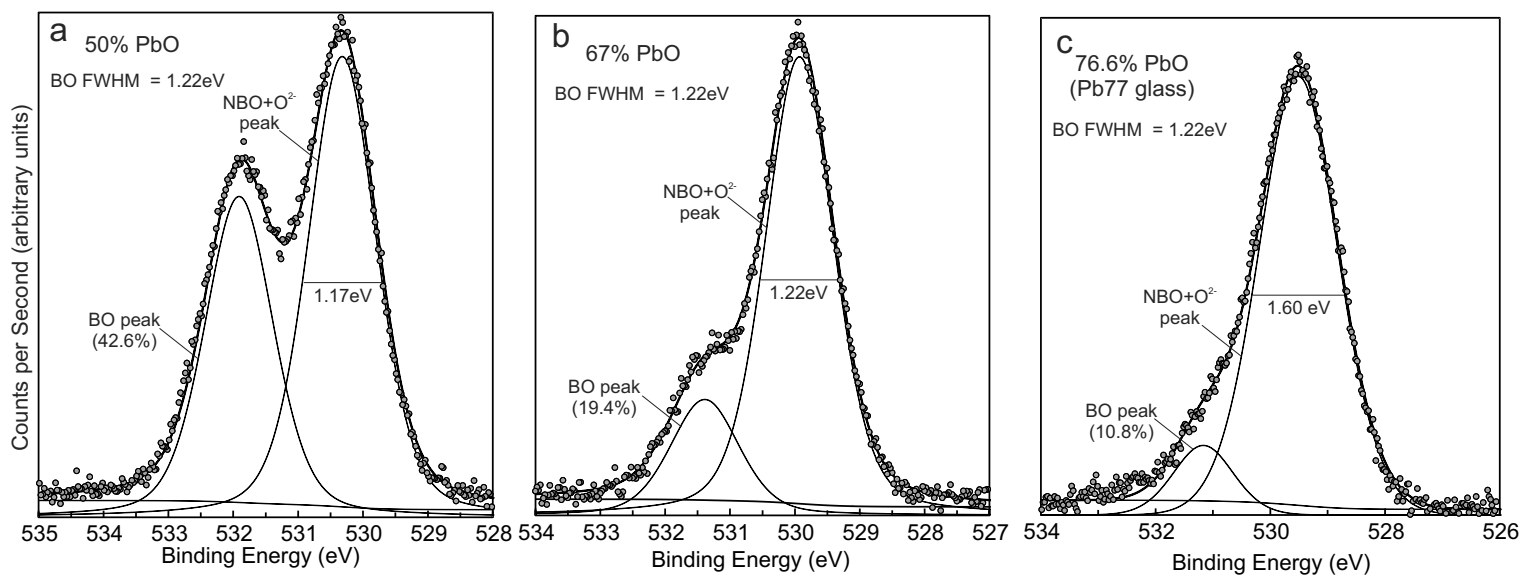


Fig. 1 - hwn

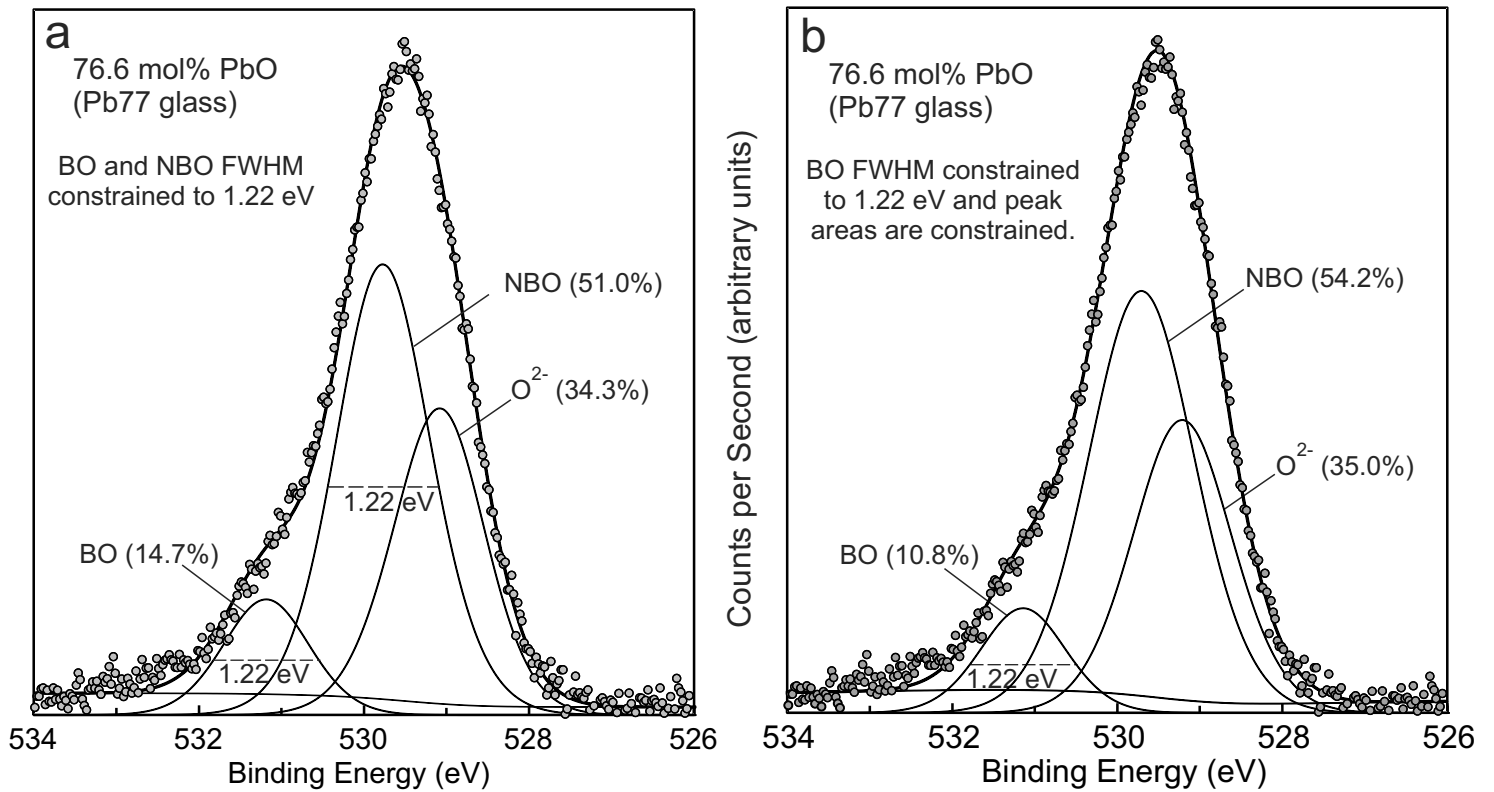


Fig. 2

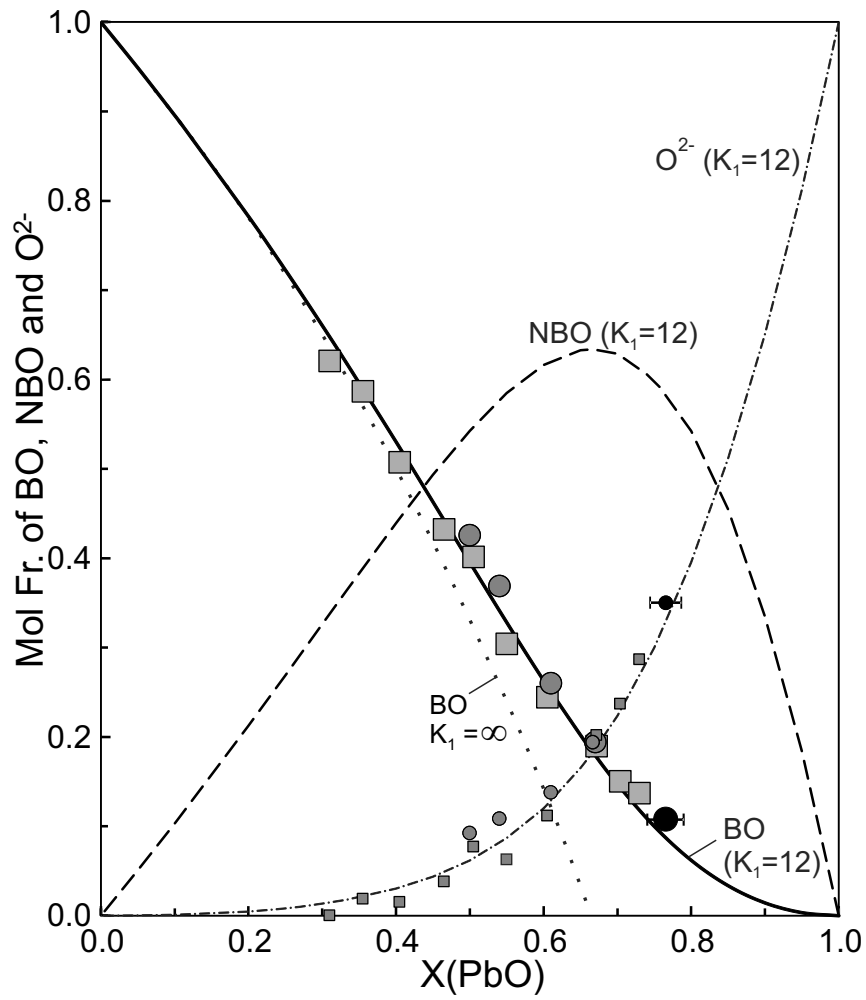


Fig. 3 - hwn

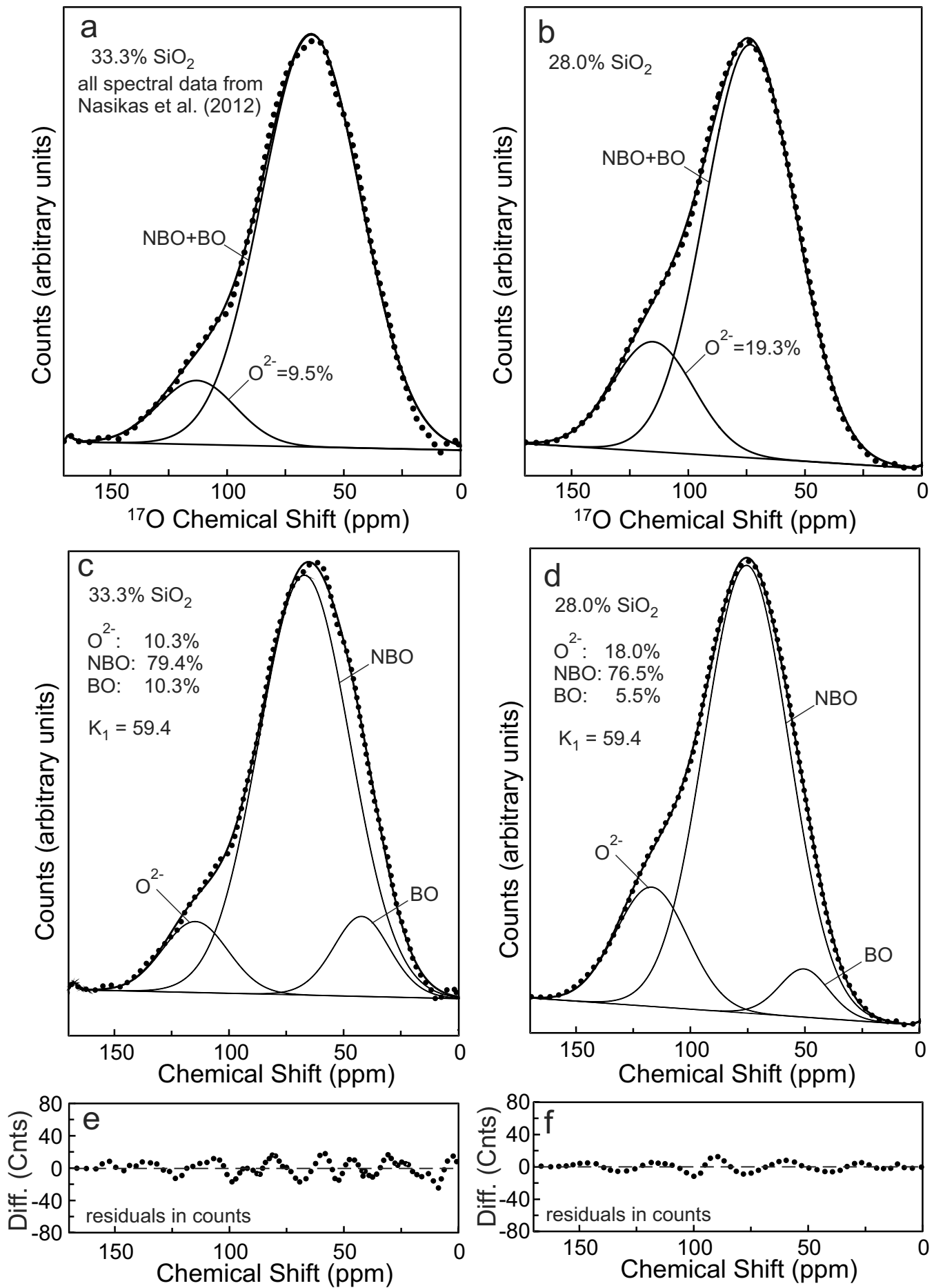


Fig. 4 - hwn

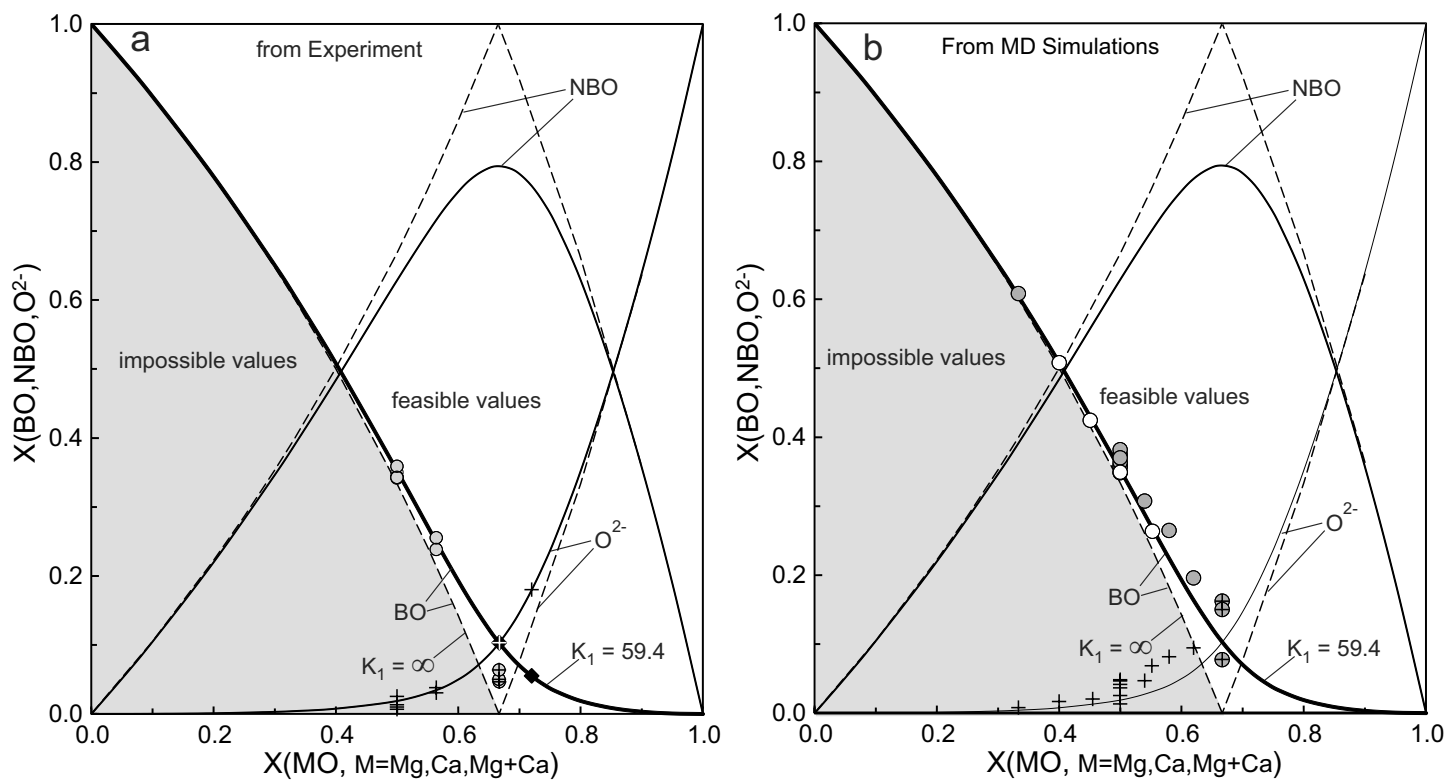


Fig. 5 - hwn

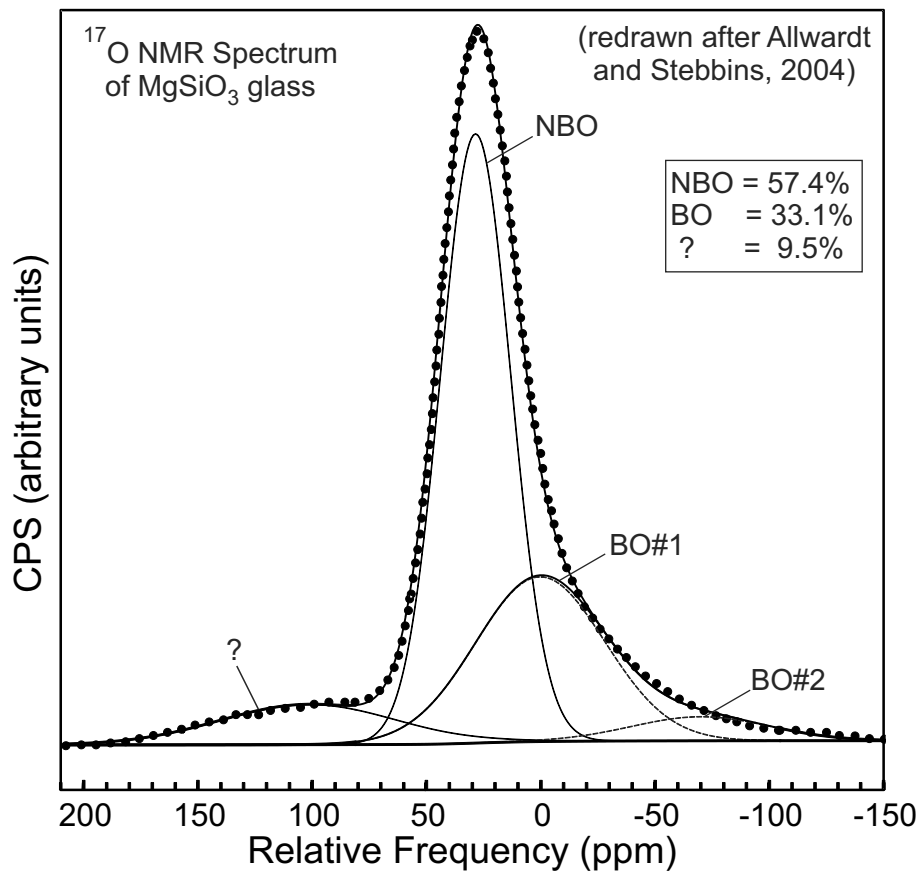


Fig 6 - hwn

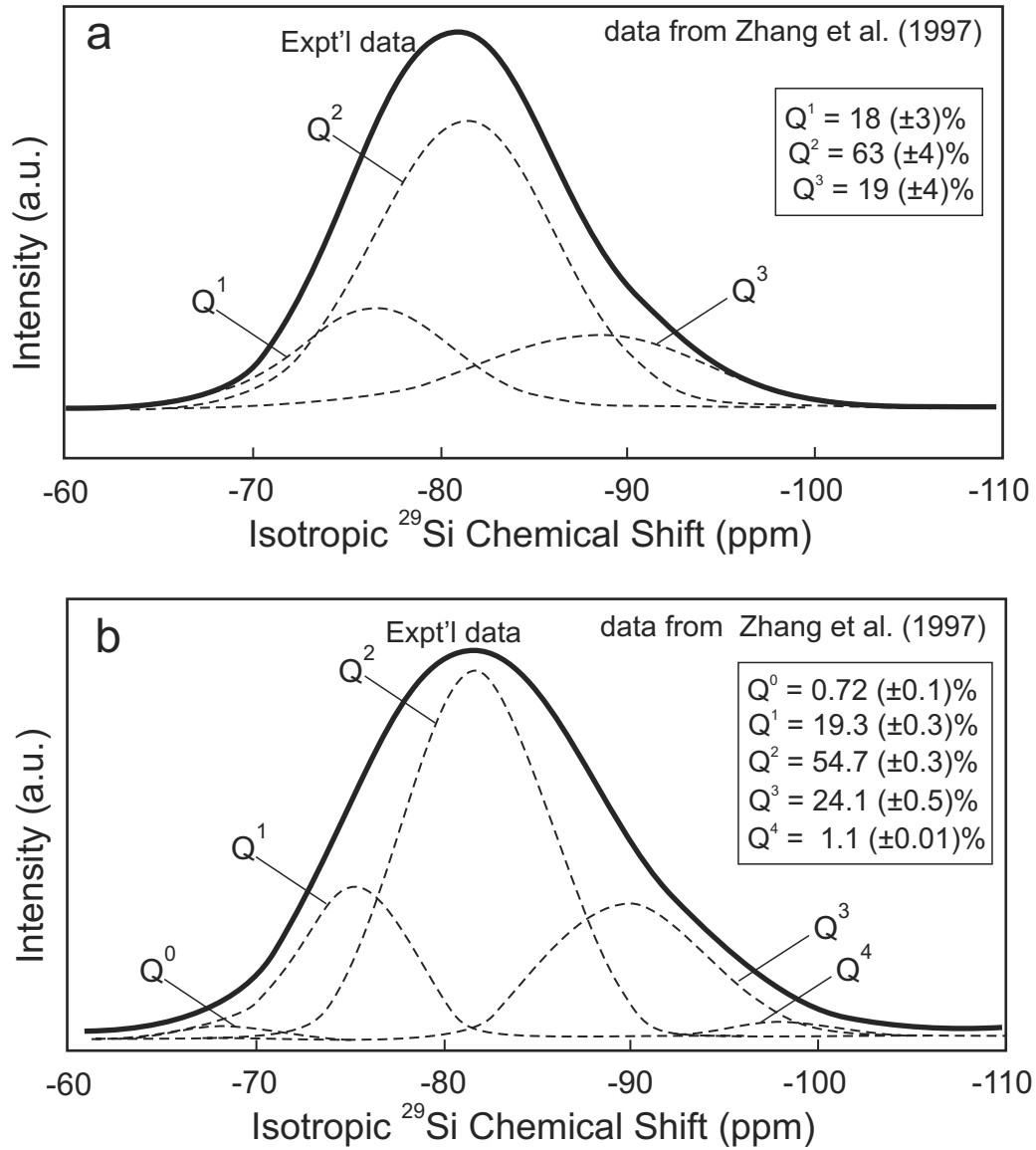


Fig. 7 - hwn

Table 1: BO, NBO and O²⁻ Peak Parameters from Fits to Spectra of Figs. 1, 2, 4 and 6

	Peak	Position	FWHM	Intensity
Figs. 1 and 2: O 1s XPS Spectral Results				
		(eV)	(eV)	(mol%)
Fig. 1c: BO FWHM constrained	BO	531.14	1.22	10.8
	NBO+O ²⁻	529.51	1.6	89.2
Fig. 2a: BO and NBO FWHM constrained	BO	531.01	1.22	14.7
	NBO	529.76	1.22	51.0
	O ²⁻	529.04	1.21	34.3
Fig. 2b: BO FWHM and peak areas constrained	BO	531.15	1.22	10.8
	NBO	529.71	1.52	54.2
	O ²⁻	529.22	1.41	35.0
Figs. 4 and 6: ¹⁷O NMR Spectral Results				
	Peak	Position	FWHM	Intensity
		(ppm)	(ppm)	(mol%)
Fig. 4a: Unconstrained 2 peak fit to CM33 spectrum	BO+NBO	64.2	50.6	90.5
	O ²⁻	114.5	34.5	9.5
Fig. 4b: Unconstrained 2 peak fit to CM28 spectrum	BO+NBO	73.4	45.4	80.7
	O ²⁻	115.1	40.8	19.3
Fig. 4c: Three peak fit to the CM33 spectrum	BO	41.9	29.5	10.3
	NBO	67.1	46	79.4
	O ²⁻	113.8	33.6	10.3
Fig. 4d: Three peak fit to the CM28 spectrum	BO	51.9	26.6	5.5
	NBO	75.4	43.5	76.5
	O ²⁻	116.5	37.7	18.0
Fig. 6: Three peak fit to Mg-metasilicate glass ^{1,2}	BO#1	0.38	66.6	28.6
	BO#2	-70.0	71.1	4.5
	NBO	28.6	36.1	57.4
	"?"	101.7	91.0	9.5
	O ²⁻	--	--	1.5

1 - The asymmetric quadrupole peakshape of BO was fit using two Gaussian peaks
 2 - The O²⁻ mol% was calculated from total BO and NBO abundances (see text).

Table 2: O-species abundances derived from experimental studies and plotted on Fig. 5a¹

Literature Source	X _{MgO}	X _{CaO}	X _{SiO₂}	X _{BO}	X _{NBO}	X _{O₂⁻}
Nasikas et al. (2012) NMR - from our fit (Table 1)	0.334	0.334	0.333	0.103	0.794	0.103
	0.360	0.360	0.280	0.055	0.765	0.180
Nasikas et al. (2011) Raman CaMg-silicate glasses	0.334	0.334	0.333	0.084	0.832	0.084
Davis et. al. (2011) NMR - Mg-silicate glasses	0.667		0.333	0.046	0.907	0.046
	0.500		0.500	0.343	0.646	0.010
Sen et al. (2009) NMR - Mg-silicate glasses	0.667		0.333	0.050	0.900	0.050
	0.500		0.500	0.359	0.616	0.026
Sen and Tangeman (2008) NMR Mg-silicate glass	0.667		0.333	0.064	0.872	0.064
Allwardt and Stebbins (2004) NMR - MgSiO ₃ glass	0.500		0.500	0.360	0.625	0.015 ²
Sneider et al. (2000) NMR - CaMg-silicate glass	0.250	0.250	0.500	0.342	0.650	0.008
Thompson et al. (2012) NMR - from Sidebands		0.564	0.436	0.230	0.738	0.032
Thompson et al. (2012) NMR from peak areas		0.564	0.436	0.223	0.746	0.017
Zhang et al. (1997) NMR - Ca-metasilicate glass		0.500	0.500	0.343	0.648	0.009
Retsinas et al. (2013) Raman - CaMg-silicate glasses:	0.250	0.250	0.500	0.422	0.578	0.062
	0.270	0.270	0.460	0.320	0.680	0.052
	0.290	0.290	0.420	0.264	0.736	0.064
	0.310	0.310	0.380	0.200	0.800	0.082
	0.320	0.320	0.360	0.153	0.847	0.074
	0.335	0.335	0.330	0.110	0.890	0.106
	0.340	0.340	0.320	0.074	0.926	0.097
	0.350	0.350	0.300	0.013	0.987	0.102
	0.360	0.360	0.280	0.013	0.987	0.136

1 - All results where X_{O₂⁻} has a negative value are excluded (i.e., impossible results).

2 - This value was calculated assuming O²⁻ was under then NBO peak (see text).

Table 3: O-species abundances derived from MD simulations and plotted on Fig. 5b¹

Literature Source	X _{MgO}	X _{CaO}	X _{SiO₂}	X _{BO}	X _{NBO}	X _{O₂-}
Al-Hasni & Mountjoy (2014) Mg-silicate glasses	0.667		0.333	0.162	0.676	0.162
	0.620		0.380	0.196	0.710	0.094
	0.580		0.420	0.265	0.654	0.082
	0.540		0.460	0.307	0.646	0.047
	0.500		0.500	0.375	0.583	0.042
Mountjoy et al. (2011) Mg-metasilicate glass	0.500		0.500			0.045
Spiekermann et al. (2013) Mg-silicate glasses	0.667		0.333	0.077	0.845	0.078
	0.500		0.500	0.382	0.570	0.048
	0.333		0.667	0.608	0.384	0.008
Sen et al. (2009) Mg-silicate glasses ¹	0.667		0.333	0.050	0.900	0.050
	0.500		0.500	0.359	0.616	0.026
Mead and Mountjoy (2006) Ca-metasilicate glass		0.500	0.500	0.343	0.647	0.010
Cormier and Cuello (2013) Ca-Mg-silicate glasses		0.500	0.500	0.347	0.640	0.013
	0.120	0.380	0.500	0.357	0.617	0.027
	0.380	0.120	0.500	0.363	0.600	0.037
	0.500		0.500	0.370	0.580	0.047
de Koker et al. (2009) Mg ₂ SiO ₄ glass	0.667		0.333	0.150	0.700	0.150

1 - All results where X_{O₂-} has a negative value are excluded.