

1 **Revision 1**

2 **Provenance Determination of Sapphires and Rubies using Laser-Induced Breakdown**
3 **Spectroscopy and Multivariate Analysis**

4
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11
12 **Abstract**

13 Determination of gem provenance is a topic of research in the gemological community for
14 financial, security, and societal reasons. Laser-Induced Breakdown Spectroscopy (LIBS) and
15 multivariate analysis have the potential to revolutionize the field of gem provenance. This study
16 acquired LIBS spectra from 569 rough sapphire and ruby specimens from 21 localities in 11
17 countries. The spectra were analyzed using the multivariate technique PLSR (Partial Least
18 Squares Regression) in separate algorithms for sapphires and rubies. Each algorithm consists of
19 a series of PLS models. Each model compares the spectra from a locality of interest to the
20 spectra from all other localities in the database. Success rates, as determined by the percent of
21 correct provenance identifications, are 98.9% (sapphire) and 96.0% (ruby) for country of origin
22 and 97.9% (sapphire) and 95.4% (ruby) for deposit of origin. Individual deposits are not
23 recognized by the concentrations of a few elements; rather, the unique geochemical signature of
24 each deposit consists of the ratios of many elements, primarily Ca, Zr, Fe, Ba, Mt, Ti, Sr, Si, Cr,
25 H, C, and Li, some of which may reside in inclusions. This work demonstrates that
26 determination of country or deposit of origin can be related to a quantitative measure with a high
27 level of success.

28 **Keywords:** ruby, sapphire, provenance, laser-induced breakdown spectroscopy, chemometrics

29 **Introduction**

30 The relationship between gem provenance (i.e., country or deposit of origin) and monetary value,
31 combined with the difficulties in provenance determination, have fueled decades of gemological
32 research and limited transparency in the gem industry. In 1990, Gemological Institute of
33 America (GIA) chairman Richard T. Liddicoat explained the technical challenges that exist for
34 determining the source of a gem with any amount of certainty (Liddicoat, 1990). Despite his

35 concerns with the ability and need to accurately determine provenance, demand from both the
36 gem trade and the public for provenance certification has grown (Rossman, 2009; Shor and
37 Weldon, 2009).

38
39 Demand has also risen for gem provenance determination because of socio-political concerns. In
40 2003, the United States banned trade with Myanmar through the Burmese Freedom and
41 Democracy Act, citing concerns of human rights abuses in the country (US Dept. of State,
42 2008a). In a 2008 amendment, the Tom Lantos Block Burmese Jade Act of 2008 closed a
43 loophole in the legislation, specifying that any rubies mined in the country could not be legally
44 imported into the United States for commercial purposes (US Dept. of State, 2008b). In order to
45 enforce sanctions such as these, a reliable method of determining the provenance of gems is
46 required.

47
48 Gemstones from different localities possess different characteristics. Provenance has been
49 determined using a combination of inclusion analysis, trace element chemistry, special
50 characteristics, and internal growth structures (Gübelin, 1953; Gübelin and Koivula, 1986; Ward,
51 1995; Hughes, 1997; Abduriyim and Kitawaki, 2006b; Devouard and Notari, 2009). To gather
52 this information, one must send a gem in question to a laboratory where a series of tests are
53 performed. Despite the amount of information obtained from these tests, it is cautioned that
54 declarations of provenance be regarded only as the professional opinion of the laboratory or
55 gemologist (Ward, 1995; Abduriyim and Kitawaki, 2006b). It is evident that an objective and
56 reliable technique needs to be developed to determine provenance.

57
58 Rubies and sapphires are among the most valuable gemstones. This pilot study uses spectra
59 acquired with Laser-Induced Breakdown Spectroscopy (LIBS) from 569 ruby and sapphire
60 specimens from 21 localities in 11 countries to demonstrate a highly successful method for
61 determining the provenance of corundum samples. An attempt was made to characterize each
62 deposit with analysis of 30 samples; however, sample set size ranged from four to 40 samples
63 per deposit. The method utilizes the multivariate statistical analysis technique PLSR (Partial
64 Least Squares Regression) to build a series of models that sequentially compares spectra from
65 one region to all other regions. This method has proven successful in distinguishing between

66 bacterial pathogens (Multari et al., 2010) and individual limestone beds (McMillan et al., 2012).
67 Success rates, as determined by the percent of correct provenance identifications, are greater
68 than 95% for both country of origin and deposit of origin. LIBS analysis is also minimally
69 destructive (similar to Laser Ablation-Inductively Coupled Plasma-Mass Spectrometry, or LA-
70 ICP-MS), simple to use, and portable. This study demonstrates the potential for LIBS analysis to
71 quantitatively and reliably introduce a new level of transparency to the gem industry.

72

73

Background

74 Geochemical analysis of gemstones enhances techniques for provenance determination by
75 adding to the traditional methods of observations of optical and mineralogic features of the
76 specimen. These observations include index of refraction; UV-visible, infrared, and Raman
77 spectroscopy; fluid and mineral inclusions; and the presence or absence of crystallographic
78 features unique to a specific deposit (Gübelin, 1953; Gübelin and Koivula, 1986; Ward, 1995;
79 Hughes, 1997; Abduriyim and Kitawaki, 2006b; Devouard and Notari, 2009). Because these
80 optical and mineralogic features may not be observed in every specimen from a locality, this
81 method has proven to be useful for some samples but not for all (Muhlmeister et al., 1998).

82

83 Early analytical methods applied to ruby and sapphire provenance were PIXE (Particle-Induced
84 X-ray Emission) and ED-XRF (Energy-Dispersive X-ray Fluorescence). Both techniques are
85 non-destructive and determine the concentrations of several elements in the gemstone. For
86 instance, Calligaro et al. (1999) were able to positively identify the origin of 41 of 64 rubies set
87 on an elaborate necklace using multivariate analysis on PIXE analysis of V, Cr, Fe, Ti, and Ga.
88 A database of 200 analyses of rubies from nine countries was used as a comparative database.
89 Muhlmeister et al. (1998) demonstrated through ED-XRF analysis that chemical characteristics
90 of rubies vary from one source to another. The ternary diagram Fe-V-Ga was used to
91 discriminate rubies from basalt-hosted, metasomatic, and marble-hosted hosts; however, rubies
92 from various localities exhibit significant overlap on the triangular diagram. Similarly, Schwarz
93 and Schmetzer (2001) developed the use of ED-XRF data and the Cr/Ga vs. Fe/Cr diagram to
94 distinguish rubies from Myanmar (Mong Hsu and Mogok), Madagascar (Vatomandry) and
95 Thailand-Cambodia. Rubies from these three areas show good separation on this two-variable
96 diagram.

97

98 The development of the Laser Ablation Inductively Coupled Plasma Mass Spectrometry (LA-
99 ICP-MS) from traditional ICP-MS techniques allowed for minimally destructive trace element
100 analysis (Gray, 1985; Günther and Kane, 1999). Rankin et al. (2003) applied LA-ICP-MS data to
101 the Cr/Ga vs. Fe/Cr diagram of Schwarz and Schmetzer (2001) to discriminate between the east
102 African localities Longido and Chimwanzulu. Saminpanya et al. (2003) proposed the use of the
103 $\text{Cr}_2\text{O}_3/\text{Ga}_2\text{O}_3$ vs. $\text{Fe}_2\text{O}_3/\text{TiO}_2$ diagram to differentiate between rubies and sapphires and between
104 metamorphic and magmatic corundum samples. This discrimination diagram was employed by
105 Abduriyim and Kitawaki (2006b), Sutherland et al. (2009) and Sutherland and Abduriyim (2009)
106 to determine provenance of various suites of gem corundums. Peucat et al. (2007) proposed that
107 the Fe vs. Ga/Mg diagram is useful for discriminating between magmatic and metamorphic blue
108 sapphires in a study with 114 samples from 18 locations. Guillong and Günther (2001) applied
109 multivariate statistics to LA-ICP-MS analysis of seven elements (Mg, Si, Ti, V, Cr, Fe, and Ga)
110 of 25 sapphires from five locations to demonstrate provenance determination. Separation of the
111 groups was fairly good, but some overlap of fields existed. Similarly, Pornwilard et al. (2011)
112 applied multivariate analysis to 10 elements determined by LA-ICP-MS (B, Si, Zn, Ga, Sn, V,
113 Mg, Ti, Cr, and Fe), using 58 samples from six countries. Samples from Kenya and Nigeria
114 were easily distinguished. However, samples from Madagascar and Tanzania were
115 indistinguishable from each other, although together they were distinguished from the other
116 groups. The same was true for samples from Cambodia and Thailand. Although high-precision
117 LA-ICP-MS analysis has proven to be a minimally destructive technique for provenance
118 determination, the fields for many of the countries of origin overlap on these diagrams. All of
119 these diagrams use only a few (three to ten) variables to model a complex chemical system,
120 resulting in insufficient definition of each provenance group. In addition, the difficulty and
121 expense of analysis, combined with the cost of the samples, restricts such studies to relatively
122 few samples (fewer than 15) typically used to characterize each location. This sample size may
123 be insufficient to fully characterize the chemical variability in the deposit, suggesting that the
124 overlap in compositions might be greater if a larger sample set were to be utilized.

125

126 The laser fluorination technique to analyze oxygen isotopes developed by Sharp (1990) made *in*
127 *situ* analysis of a small amount of sample possible; modifications of this technique were made

128 for use with corundum (Yui et al., 2003; Giuliani et al., 2005). Oxygen isotopes have been used
129 to determine the geologic origin of rubies (Giuliani et al., 2005), and have proved useful in
130 determining the source lithology of xenocrystic or placer corundum specimens. Marble-hosted
131 corundum samples have high $\delta^{18}\text{O}$, reported by Giuliani et al. (2005) to range from +16.3 ‰ to
132 +23‰ and by Yui et al. (2008) from +21.6 ‰ to +25.7 ‰. Rubies and sapphires from basalts,
133 igneous rocks, and non-carbonate metamorphic rocks have lower $\delta^{18}\text{O}$, ranging from +1.3 ‰ to
134 +13.9 ‰ (Yui et al., 2003; Giuliani et al., 2005; Yui et al., 2006; Giuliani et al., 2009; Vysotsky
135 et al., 2009). Ruby and sapphire specimens from the same placer deposit have been shown to
136 have distinct $\delta^{18}\text{O}$ values (Yui et al., 2006), suggesting different source locations for the placer.
137 Overall, oxygen isotope analysis of corundum has been able to set some constraints on the source
138 lithology of rubies and sapphires, despite significant overlap in isotopic composition of samples
139 from various igneous and non-carbonate metamorphic lithologies (Giuliani et al., 2005).
140 However, the isotopic compositions of corundum samples are not diagnostic of locality, limiting
141 the use of this technique for provenance determination.

142

143 Traditional techniques for determining ruby and sapphire provenance, including observation of
144 inclusions and other mineralogical features, trace element analysis by XRF, PIXE, and LA-ICP-
145 MS, and oxygen isotope analysis have not yet been able to provide a unique fingerprint for each
146 corundum location. In addition, analytical techniques like LA-ICP-MS require skilled
147 technicians in a laboratory environment. In contrast, Laser-Induced Breakdown Spectroscopy
148 (LIBS) is a rapid and inexpensive technique that is simple to operate, portable, and does not
149 require special laboratory conditions. Thus, provenance of gems using LIBS could be
150 determined at border crossings, ports and airports, gemological laboratories, gem studios, and
151 galleries.

152

153

Materials and Methods

154 **Specimen Acquisition.** A large sample set of rough corundum was acquired from vendors at the
155 Tucson Gem and Mineral Show and mining companies (Table 1). Heat-treated, chemically-
156 treated, and cut gemstones were not used in this study. Because acquisition of samples with
157 known provenance for database development is critical to the study, gems were purchased only
158 from vendors who were able to cite a chain of possession and were knowledgeable about the

159 mines of the region. Every precaution was taken to ensure the reliability of the vendors. For the
160 purposes of this study, corundum with deep pink, fuchsia, maroon, and purple-red colorations
161 were considered rubies, and all other colors were considered sapphires. Countries were
162 characterized by 30 samples, if possible, to capture the chemical variability within the deposits
163 with statistical significance. Five sapphire samples from Sri Lanka and two rubies from
164 Jagdelek, Afghanistan, were originally included; however, there was insufficient information to
165 fully characterize the deposits, and provenance determination failed for these localities.
166 Although several of the data sets have fewer than 30 samples (Psudipada, India; Uмба Valley,
167 Tanzania; Mysore, India; Hunza Valley, Pakistan; and Longido, Tanzania; Table 1), provenance
168 determinations from these localities yielded acceptable accuracies. However, this work suggests
169 that a large number of samples (≥ 30) need to be used to characterize the chemical fingerprint
170 from a gem locality.

171

172 **Sample Analysis.** Samples were analyzed by Laser-Induced Breakdown Spectroscopy (LIBS)
173 (Fig. 1). In LIBS, a laser beam is pulsed on a small area of the sample to create a plasma, a
174 weakly ionized collection of ions, atoms, and free electrons (Cremers and Radziemski, 2006).
175 The plasma contains atoms ablated from the surface of the sample and atoms in the local
176 environment (air or a gas selected for analysis). Due to the high temperature of the plasma ($>$
177 10,000 K), electrons are excited to upper orbitals. As the plasma cools, each electron decays to a
178 lower-energy orbital, and the difference in energy is emitted as a photon with a discrete
179 wavelength that corresponds to the energy difference between orbitals. The photons are
180 collected by a lens into seven optic fibers. A spectrometer, which separates the light into
181 individual wavelengths, is attached to each optic fiber. The spectra from all seven spectrometers
182 are compiled to form a single, continuous spectrum (Fig. 2). The intensities of peaks at specific
183 wavelengths are proportional to the number of photons emitted by a specific orbital transition
184 from a specific element (Cremers and Radziemski, 2006). For example, the 396.1 nm peak for
185 Al is the result of an excited electron in the 4s orbital decaying to the stable 3p orbital. This is
186 statistically the most intense Al peak. Because many electron orbital transitions occur for each
187 element, a LIBS spectrum consists of many peaks for each element. In this work, peaks are
188 identified using the Handbook of Basic Atomic Spectroscopic Data published by NIST
189 (Sansonetti and Martin, 2005).

190

191 The Ocean Optics © 2500+ LIBS instrument was used for this study (Fig. 1). A 1064 nm
192 Nd:Yag laser was pulsed at 120 mJ with a Q-switch delay of 1.5 μ s for each analysis. The Q-
193 switch delay is the interval of time between plasma formation and the collection of light. A
194 delay in collection is necessary because at the instant of plasma formation, a continuum is
195 formed from bremsstrahlung processes and recombination events (Cremers and Raziemski,
196 2006). During these events, photons are emitted as electrons collide in the plasma. Photons
197 emitted from these collisions do not provide elemental data, so it is necessary to delay collection
198 until these events are no longer significant in the signal.

199

200 Analysis protocol was designed to maximize spectral intensity while minimizing damage to the
201 sample. Samples were analyzed inside a sample chamber in an argon atmosphere so that the
202 laser energy is used to excite atoms from the sample instead of atmospheric nitrogen and oxygen.
203 At each analyzed spot, a cleaning shot was taken, followed by an analysis shot. The cleaning
204 shots were at the same energy level as the analysis shots; the data simply were not recorded.
205 Ablation craters were 10-100 μ m in diameter.

206

207 Each specimen was analyzed at 30 spots; these spectra were averaged to create one spectrum per
208 specimen. The Al peaks at 226.9, 236.7, 237.3, 257.5, 281.6, 308.2, 394.4, and 396.1 nm were
209 removed from the spectra to allow multivariate analysis to focus on trace element distributions.
210 All wavelengths > 680 nm except for the 854.2 nm Ca peak for rubies (Fig. 2) were also
211 removed in order to eliminate Ar peaks from the analysis. The 854.2 nm Ca peak was retained in
212 the ruby spectra because it was observed to vary between deposits.

213

214 **Chemometric Analysis.** Chemometric analysis is a method of processing chemical data using
215 multivariate statistics in an attempt to recognize 'hidden phenomena' (Esbensen, 2007). Hidden
216 phenomena are correlations that are not intuitive, or obvious from a simple two-dimensional, or
217 bivariate, graph. In this study, The Unscrambler ® was the multivariate data analysis software
218 used to model LIBS data.

219

220 Partial Least Squares Regression (PLSR) is a multivariate modeling technique that relates two
221 data matrices by multiple linear regressions (Esbensen, 2007). In this study, one matrix (X)
222 contains the LIBS spectra; the other matrix (Y) contains a single integer variable, called the
223 provenance variable, that takes the value of 1 if the specimen came from the locality under
224 scrutiny and 0 if the specimen came from any other locality. PLSR models the X and Y matrices
225 interdependently during calibration, reducing the influence of large variations in X that are
226 irrelevant to Y (Wold et al., 2001). Regression coefficients, the characteristics of X that are
227 relevant to Y, are used to predict Y-values (provenance variables) from X-values (LIBS spectra).
228 This is a powerful technique because it uses all channels of the LIBS spectra, which record
229 emission from nearly all elements from the periodic table.

230

231 In this work, PLSR models are generated and tested in four steps (Fig. 3): 1) training of a model;
232 2) determination of the Value of Apparent Distinction (VAD) that separates two groups of
233 samples; 3) prediction of provenance variables for validation samples; and 4) calculation of
234 success rate by comparing the predicted provenance to known provenance of validation samples.
235 In order to validate a model, it is critical to have spectra from a set of samples of known
236 provenance that can be treated as unknowns. To accomplish this, half of the samples from each
237 locality were used to calibrate the models and the remaining half were used in validation to
238 verify the model and calculate success rates.

239

240 A PLSR model is trained by correlating matrices X (spectra) and Y (provenance variables) using
241 multiple linear regressions. The model relates pertinent aspects of the spectra to provenance
242 variables, 1 or 0, assigned to two groups of samples in the model. The provenance variable "1"
243 is assigned to the spectra from the provenance of interest and the variable "0" is assigned to a
244 group containing all other spectra. The model consists of a set of regression coefficients, one for
245 each variable, which relate the spectral data to the provenance variables. This process is
246 illustrated in Figure 3A, in which the model is represented by a PLSR score plot. The axes of the
247 score plot are PLSR Component 1 (PC1) and PLSR Component 2 (PC2). These components are
248 the axes of linear regressions used in the model and consist of contributions from many of the
249 variables in the model. Each sample plots with a score, or value, along the principal component;
250 samples that plot near each other are spectrally, and thus compositionally, similar. Ideally, the

251 provenance groups would plot in mutually exclusive spaces on this diagram, suggesting that their
252 differences in composition can be completely resolved.

253

254 In detail, modeling was performed using the program The Unscrambler®. The NIPALS
255 algorithm was applied with 9 PCs; no weighting was applied to variables. The model is mean-
256 centered.

257

258 Once a PLSR model has been trained, the model is applied to the training spectra, predicting
259 whether each sample in the training suite is from the location being tested for or from any other
260 location. The predicted value should be close to 1 for stones from the location being examined,
261 and should be close to 0 for stones not from that location (Fig. 3B). While 0.5 is the midpoint
262 between the two target values of the provenance variable, if the distributions of the provenance
263 variable values for the two populations (i.e., being from the location or not) are not symmetric
264 and identical distributions, the midpoint may not provide a good cutoff point, or Value of
265 Apparent Distinction (VAD), for predicting whether the stone is from the location being
266 considered. This second step of setting the VAD is illustrated in Figure 3B, where the calculated
267 provenance predicted values are plotted for samples used to train the Kenya ruby model. Note
268 that the Kenya samples, in closed diamonds, have provenance variables greater than the VAD of
269 0.227 and the samples from all other locations, in open squares, have provenance variables less
270 than the VAD.

271

272 In considering the determination of a good VAD, the sample distributions of the predicted values
273 were often not symmetric and were quite variable (Fig. 4). Hence, a nonparametric kernel
274 density estimator (Silverman, 1986) was chosen to obtain a density estimate of the predicted
275 values for each group (Fig. 4). Kernel densities depend on the selection of a bandwidth
276 parameter; numerous bandwidth selection strategies were investigated by running simulations to
277 determine how well the kernel density estimators using various bandwidth selection methods
278 reproduced the original distribution. The data used for this process simulated a normal
279 distribution, but specifically targeted the sample sizes and variances present in the training data
280 set. Visually, the biased cross-validation method worked the best, giving fewer false multimode
281 densities. At its worst, use of this bandwidth selection method tracked the original distribution

282 similar to other methods, and at its best it tracked it substantially better. Generally, all the
283 methods resulted in similar VADs, even when they resulted in substantially different looking
284 densities.

285

286 For any specified VAD, the small area under the right density curve occurring to the left of the
287 VAD is the estimate of how often misclassification would occur for the population of rubies
288 from the location under consideration (dark shaded area in Fig. 4). Similarly, the area under the
289 left density occurring to the right of the VAD estimates the misclassification rate for the
290 population not from the location (light shaded area in Fig. 4). Once density estimates were
291 obtained, numerical root-finding and numerical integration of the densities were used to solve for
292 the VAD between 0 and 1 that minimized the sum of these two misclassification rates. For the
293 ruby study, VADs ranged from 0.141 to 0.512, and for the sapphire study they ranged from
294 0.359 to 0.604.

295

296 In the validation step, the model uses the regression coefficients calculated in the training step to
297 predict Y-values (provenance variables near 0 and 1) from a new set of validation spectra from
298 samples not used in the training. For instance, in Figure 3C, provenance variables are calculated
299 for five samples, two of which are greater than the VAD of 0.227 and three of which are below
300 the VAD. Samples with predicted provenance variables greater than the VAD are assigned to
301 the location being examined; those with predicted provenance variables less than the VAD are
302 assigned to the group of all other locations.

303

304 The last step is to calculate the success rate of the model (Fig. 3D). This is illustrated for the
305 Kenya ruby model in Figure 5. Spectra from Kenya samples all have predicted provenance
306 variables greater than the VAD of 0.227; they are all correctly identified as Kenyan. All but one
307 of the other spectra, from India, Greenland, Madagascar, Myanmar, Pakistan, Tanzania, and the
308 USA, have predicted provenance variables less than 0.227; they are correctly identified as
309 belonging to this large group. One sample in this group was incorrectly identified as Kenyan.
310 Because 163 of 164 samples were correctly identified, the model has a 99.4 % success rate.

311

312 In this study, a series of PLSR models are used to determine provenance. Each model compares
313 spectra from one location of interest (provenance integer variable = 1) to spectra from all other
314 models (provenance integer variable = 0). Separate matching algorithms for rubies and sapphires
315 were developed by constructing a sequential arrangement of models that separate spectra from a
316 single locality from those from all other localities. These are illustrated by flow charts and
317 corresponding score and validation plots (Figs. 6 & 7 for sapphires and Figs. 7 & 8 for rubies).
318 A similar method was developed by Multari et al. (2010) for the identification of bacterial strains
319 using LIBS data and by McMillan et al. (2012) for identification of individual limestone beds.
320 In the algorithms, the first model (India in the sapphire model) uses prediction spectra from all
321 locations. Each spectrum is determined to be similar either to India or to all the other localities
322 in the model. The spectra from this first locality are then removed from all subsequent models.
323 Thus, the second model sapphire (Sapphire Branch) does not include any spectra from India.
324 The number of spectra in each model decreases and the spectra become more chemically similar
325 to each other as one moves through the flow chart. In some cases, it was not possible to separate
326 spectra from a single country, and the algorithm branches, as in the Sapphire Branch model. The
327 algorithms are discussed in detail in the Results section.

328

329 To determine the order of the models, average spectra of each country were visually inspected
330 for unique characteristics. Localities with the most distinct spectra were separated first, allowing
331 the model to focus on small spectral difference between chemically similar samples later in the
332 algorithm. By reducing the number of samples for similar spectra, subtle differences were
333 emphasized in the later models.

334

335 Success rates can be determined for individual models as well as the entire algorithm. Table 2
336 reports the percentage of correct predictions for each model. These success rates reflect only the
337 models that predict provenance and not models that cause branching. Thus, a second method for
338 calculating success rates counts the total number of correct predictions for all models as a
339 percent of the total number of spectra. These overall success rates are shown in Figures 6 & 8.

340

341

Results

342 **Sapphire Provenance Algorithm.** The sapphire provenance algorithm is illustrated in a flow
343 chart in Figure 6; the score and validation plots are presented in Figure 7. Results are shown in
344 Table 2. Score plots show the variation in composition in PC1-PC2 space for the samples used
345 in the model. Ideally, the two groups of samples should not overlap, but in practice, groups with
346 some overlap can still be modeled with high success. Validation plots present the calculated
347 provenance variables for samples used to validate the model. Ideally, all samples in the
348 provenance being modeled should have values greater than or equal to the VAD; samples from
349 all other locations should have values less than the VAD. The success rate of the model is
350 calculated as the percent of samples whose provenance was correctly identified.

351

352 The first locality to be identified in the sapphire algorithm is Psudipada, India. This model is
353 100% successful, correctly identifying the provenance of 118 of 118 samples. The second
354 model, Sapphire Branch, separates samples from Afghanistan and Vietnam from the remaining
355 localities (Tanzania, Australia, Madagascar, and USA). It successfully predicts the origin of 102
356 of 103 samples (99.0% success). The Afghanistan model compares samples from Afghanistan to
357 those from Vietnam. This model is 96.7% successful, correctly identifying 29 of 30 samples.
358 Continuing on the main stem of the algorithm, the Tanzania model identifies samples as being
359 from Tanzania (Songea or Umba Valley) or as being from Australia, Madagascar, or the USA. It
360 has a success rate of 97.3% (72 of 74 samples correctly identified). The Tanzania Deposit model
361 attempts to predict whether samples are from Songea or the Umba Valley in Tanzania. It is not
362 successful, with only 50% success rate. Note that this study only has ten samples from Songea
363 and five from Umba Valley. This is an excellent example of the importance of having a large
364 number of samples when attempting to determine provenance by chemical fingerprinting.

365

366 The Australia model compares sapphires from Australia to those from Madagascar and Montana
367 (USA). The model is 100% successful, with a total of 66 spectra. The Madagascar model
368 compares sapphires from Madagascar and Montana, USA. It, too, is 100% successful; all 45
369 spectra were correctly identified. The final model, Madagascar Deposit, distinguishes between
370 blue and white sapphires from Madagascar. The model correctly identifies 29 of 30 samples
371 (96.7% success).

372

373 **Ruby Provenance Algorithm.** Results for the ruby provenance algorithm are presented in a
374 flow chart (Fig. 8), in score and validation plots (Fig. 9), and in Table 2. The ruby algorithm
375 contains complexity not encountered in the sapphire algorithm, probably because the chemical
376 variation within rubies is less than that within sapphires. The first model distinguishes rubies
377 from Kenya from all other localities. It is 98.2% successful, correctly determining the
378 provenance of 161 of 164 samples. Rubies from Mysore, India, that were obtained free from
379 matrix are separated in the second model, India I. This model correctly predicts the locality of
380 137 of 149 samples (91.9% success). The algorithm bifurcates in the next model, Ruby Branch
381 I. It separates the remaining samples into two groups: 1) USA (Wyoming), Pakistan, and
382 Tanzania; and 2) Greenland, Madagascar, Myanmar, and India (samples in matrix). This model
383 is 99.3% successful, correctly identifying 138 of 139 samples.

384

385 Rubies from Wyoming, Pakistan, and Tanzania comprise the algorithm on the right-hand side of
386 the flow chart (Fig. 8). These sets are chemically similar; however, it is possible to separate
387 them with high success rates by allowing the Wyoming samples to be present in the Ruby
388 Branch II model, but not interpreting their provenance assignments. In the Ruby Branch II
389 model, two groups are determined: 1) Wyoming & Pakistan, and 2) Wyoming & Tanzania. This
390 model is 92.9% successful and correctly identified 26 of 28 samples (the Wyoming samples were
391 not counted). The Pakistan model then discriminates between Wyoming and Pakistan rubies, at
392 a 100% success rate (26 of 26 correct provenance determinations). Similarly, the Wyoming
393 model discriminates between Wyoming and Tanzanian rubies. It also is 100% successful,
394 identifying 42 of 42 samples correctly. Thus, Wyoming rubies can be identified through two
395 routes: the Pakistan model and the Wyoming model. The final model on the right-hand side of
396 the flow chart, the Tanzania Deposit model, discriminates between two Tanzanian regions:
397 Winza and Longido. The model was 86.4% successful and correctly determined the provenance
398 of 19 of 22 samples. This demonstrates that ruby deposits approximately 450 km apart have
399 sufficiently distinct LIBS signatures to be identified with a high success rate.

400

401 The left-hand side of the ruby algorithm flow chart concerns rubies from Greenland,
402 Madagascar, Myanmar, and India (Mysore, samples in matrix). The Greenland model is 98.9%
403 successful, positively identifying 92 of 93 samples. The Madagascar model separates samples

404 from Madagascar at a 97.3% success rate; 73 of 75 samples were positively identified. The
405 Madagascar Deposit model then attempts to discriminate between a set of Madagascar rubies
406 free of matrix and rubies in matrix (amphibolite and biotite gneiss). This model is 100%
407 successful, correctly identifying 32 of 32 samples. The Myanmar model is able to positively
408 identify rubies of Myanmar at a success rate of 86.7% (39 of 45 samples). The final model is the
409 India model, which discriminates Mysore rubies in fuchsite matrix from Mysore rubies in biotite
410 gneiss matrix. This model has a success rate of only 83.3%, correctly identifying 25 of 30
411 rubies.

412

413 Success rates are reported in this work in two ways. First, the success rates for each individual
414 model are shown on Figures 6 & 8 and in Table 2. This calculation simply considers the number
415 of samples involved in the validation model and represents the percentage of samples for which
416 provenance was correctly identified. Success rates for individual models range from 100% to
417 50%. Although the method of expressing success in terms of individual models is
418 straightforward, it does not take into account every model in the algorithm. For instance, the
419 sapphire algorithm branches in a model called Sapphire Branch. The ruby algorithm has two
420 such branches; the success of all models subsequent to the branches depends on the success of
421 the branching model. An alternative method is to calculate the success rate of the total algorithm
422 as the percent of total correct provenance determinations relative to the total number of
423 determinations. Using this method, the overall success rates for sapphire provenance
424 determination are 98.9% for determination of country of origin and 97.9% for determination of
425 deposit of origin. Overall success rates for rubies are similar: 96.0% for country of origin and
426 95.4% for deposit of origin.

427

428 **Necessity of large sample set.** These results demonstrate the need for a large sample set when
429 attempting to determine mineral provenance. Table 2 lists success rates for provenance
430 determination for each locality and the number of samples used in each model. Success rates are
431 > 85%, with two exceptions. One exception is distinguishing between Mysore rubies in fuchsite
432 matrix and Mysore rubies in biotite gneiss matrix. The success rate for this model is only 83.3%
433 success rate, suggesting that the two groups of rubies are similar in composition. In algorithms
434 such as these, materials near the end of the flow chart are chemically similar to each other and

435 thus more difficult to distinguish from each other. The other failure in this study is the ability to
436 distinguish between the Tanzania sapphire localities Songea and Umba Valley. Note, however,
437 that the sample set contains only ten samples from Songea and five from Umba Valley (Table 1).
438 Because half of the samples were used to calibrate the model and half to verify the model, only
439 eight samples were used in the prediction step, and only half of them were correctly identified
440 (Table 2). This suggests that many samples are required to fully capture the chemical variability
441 of a deposit. Clearly, the five samples from Umba Valley were not sufficient. Success rates for
442 localities with at least 30 samples range between 83.3% and 100%.

443

444

Discussion

445 Provenance determination is a difficult issue to solve. Issues such as the large number of
446 samples necessary to conduct rigorous determinations, the cost and complexity of analytical
447 instrumentation, and the skill and experience required to make high-quality gemological
448 observations are obstacles in the attempt to provide quantifiable determinations of country of
449 origin or deposit of origin. This study demonstrates that chemometric analysis of LIBS spectra
450 from a large number of samples makes accurate, rapid provenance determination possible, with
451 success rates generally higher than 95%. In addition, LIBS technology is relatively inexpensive,
452 rugged, portable, and simple to use. The analyst needs no intense training in spectroscopy or
453 gemology.

454

455 The method described here could be fully automated and implemented at critical points in the
456 gem stream, such as border control stations, ports of entry, gem studios, and galleries. Prior to
457 widespread application, several issues need further research. The effect of heat and chemical
458 treatment on provenance analysis with LIBS spectra and multivariate analysis has not been
459 studied; this pilot study used only untreated, uncut samples. Sample library size is critical to the
460 success of any gem provenance project; ultimately, one would like to build a model with at least
461 30 samples from every important corundum deposit. In addition, the number and spatial
462 distribution of LIBS analytical spots on cut gems would be limited to a few spots on the stone's
463 girdle; the model would have to be tested using these analytical protocols. It is possible that
464 more specimens from each locality would be necessary to capture the compositional diversity of
465 each deposit with fewer spectra per sample.

466

467 One goal of provenance determination is to gain an understanding of the chemical differences
468 between samples from various locations. In chemometric analysis, loading vectors are used to
469 determine which chemical elements are important in discriminating between two groups of
470 samples. Loading vectors are the contribution of each variable (wavelength) to the linear
471 regression. If a linear regression trends in the direction of increasing value for a certain
472 wavelength variable, for instance increasing intensity of a Ca wavelength, that wavelength, and
473 thus the concentration of the emitting element, will have a strong positive influence on the linear
474 regression and a large positive loading vector. In contrast, if the regression trends in a direction
475 of decreasing value for a wavelength, that wavelength (and element) will have a negative loading
476 vector. Loading vectors for the models were qualitatively inspected to discern which elements
477 have high positive loading vectors for the deposit being considered in the model (Table 2).
478 Elements with very high loading vectors were considered to have strong influence; those with
479 high loading vectors were considered to have lesser but significant influence. Elements with
480 moderate and lower loading vectors are not listed in Table 2; they exert lesser influence on the
481 model and are thus less significant for discrimination purposes. These elements are important in
482 discriminating between corundum deposits, in approximate order of decreasing importance: Ca,
483 Zr, Fe, Ba, Mg, Ti, Sr, Na, V, Si, Cr, H, C, and Li. Some of these elements may reside in
484 inclusions in the analyzed samples; however, the inclusions must have been sufficiently
485 abundant for them to contribute significantly to the loading vectors. The chemical differences
486 between corundum deposits are not simple (Table 2); it is the ratios of many elements that
487 comprise the unique chemical signature of each deposit. The signature is too complex to be
488 discerned by traditional geochemical techniques (Abduriyim and Kitawaki, 2006a, 2006b;
489 Calligaro et al., 1999; Muhlmeister et al., 1998; Peucat et al, 2007; Pornwilard et al., 2011;
490 Rankin et al., 2003; Saminpanya et al., 2003) because it is inherited from subtle compositional
491 differences in the host rock during metamorphism.

492

493 It is interesting that most of the elements listed in Table 2 are not chromophores. This study
494 indicates that provenance determination using chemometric analysis of LIBS spectra is
495 independent of the color of the stones. Some of the sample sets analyzed in this paper have
496 consistent colors; however, three of the sapphire sets have a wide variety of colors (Table 1).

497 The Australian, Umba Valley, and Montana sample sets all exhibit multiple colors. However,
498 the Australian and Montana (USA) models are 100% successful, indicating that the models are
499 independent of color.

500

501 The ideal method for provenance determination would compare spectra of unknown samples to a
502 database that contains spectra from every known ruby or sapphire deposit. Obviously, such a
503 sample collection is prohibited by time and funding. The finite size of our database opens the
504 question of how samples from localities other than those present in the calibration are handled in
505 the algorithms. There are two possibilities. First, a sample may be sufficiently similar to
506 samples from one of the localities in the database that it is classified incorrectly. In some cases,
507 such samples can be recognized by using chemometrics to compare the LIBS spectrum of the
508 unknown sample to those of the known samples. If the unknown sample is an outlier, it is most
509 likely from a different location. However, the possibility exists that the unknown deposit may
510 actually be similar in composition to one of the localities in the calibration. In this case, the
511 sample will be mis-identified; the best method to avoid this is to build a sample base that
512 contains as many deposits as possible.

513

514 Alternatively, an unknown sample may be unlike any samples from any of the localities in the
515 calibration. In this case, the sample will consistently be classified as a "0" and will be identified
516 as one of the localities at the end of the flow charts (Montana for sapphires; Mysore or Tanzania
517 for rubies; Figures 6 & 8). In this case, chemometrics (i.e., Principal Component Analysis) can
518 be used to compare all of the spectra that are classified in the final localities; if the sample is an
519 outlier, its provenance is most likely one not found in the calibration sample base.

520

521 If this method were to be used commercially, building the sample base would be a high priority.
522 As new localities are added, the algorithms would need to be revised. The order in which the
523 samples are considered is of primary concern, although there is more than one order that
524 produces satisfactory results. The addition of any new locality requires development of an
525 entirely new algorithm, because the most chemically unique samples are separated out first,
526 leaving the more chemically similar samples at the end of the process. While the process of
527 determining the order of the algorithm is time-consuming, it is not intrinsically difficult.

528

529

Implications

530 Provenance determination is an important aspect of gem values as well as a political and national
531 security issue. Traditional methods for determining country of origin or deposit of origin include
532 comparing gemological observations and/or trace concentrations using XRF, PIXE, and ICP-MS
533 data, of unknown samples to those from known localities. Results have been promising but no
534 unique solution has emerged for several reasons. First, the variety of color, inclusions, and
535 unique mineralogical features is fairly large in each deposit and not all specimens from a deposit
536 contain all of the identifying features. Second, trace element studies have used a relatively small
537 number of variables (the number of elements analyzed), and in some cases, a relatively small
538 number of samples.

539

540 Chemometric treatment of Laser-Induced Breakdown Spectroscopy (LIBS) spectra from
541 sapphires and rubies is a new and successful method for provenance determination. The main
542 advantages of LIBS are 1) ease of analysis; 2) rapidity of analysis; and 3) little or no required
543 sample preparation. Because of this, it is possible to analyze many (i.e., hundreds) samples
544 rapidly, creating a data base that closely represents the chemical variation in each locality.
545 LIBS instruments could be operated at strategic points such as border crossings, international
546 port facilities, and even military outposts to determine the provenance of gems and conflict
547 minerals in real time. Instruments could also be used in gem galleries and studios to insure that
548 the gem provenance is accurately reported.

549

550 The ability to obtain spectra from large sample sets and to analyze the large resulting data set
551 provides a new direction for mineral analysis and research. For instance, the process described
552 in this paper could be applied to correlation of strata using mineral compositions. Examples
553 include correlating ash-flow tuffs by LIBS analysis of phenocryst minerals, or correlating clastic
554 sedimentary rocks through LIBS analysis of the heavy minerals zircon, tourmaline, and rutile. In
555 this case, one would expect to see several populations of each phase; however, analysis of
556 hundreds or thousands of grains would provide an adequate statistical base for estimation of the
557 population distribution of each group. Such a project is daunting in scale using traditional
558 technology.

559

560 This study demonstrates that quantifiable, high-precision provenance determination is possible
561 using technology that is durable, portable, relatively inexpensive, and operable by a range of
562 end-users. Overall, the sapphire algorithm correctly identified the provenance in 432 of 437
563 cases (98.9%) for country of origin and in 465 of 475 cases for deposit of origin (97.9%).
564 Success rates for rubies are similar. Overall, 759 of 791 ruby spectra in the algorithm were
565 correctly identified (96.0%) at the country of origin level; the overall deposit of origin success
566 rate is 95.4% (835 of 875). The application of chemometric analysis of LIBS spectra could bring
567 new transparency to the gem industry.

568

569

Acknowledgements

570 The authors gratefully acknowledge Tristan Likes and Karly Baughn for logistical support and
571 Materialytics, LLC, for funding. We also thank M. Darby Dyar and an anonymous reviewer for
572 insightful comments that improved the quality of this contribution to mineral science.

573

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References Cited

576 Abduriyim, A., and Kitawaki, H. (2006a) Applications of laser ablation-inductively coupled
577 plasma-mass spectrometry (LA-ICP-MS) to gemology. *Gems & Gemology*, 42, 98-118.

578

579 Abduriyim, A., and Kitawaki, H. (2006b) Determination of the origin of blue sapphire using
580 laser ablation inductively coupled plasma mass spectrometry (LA-ICP-MS). *Journal of*
581 *Gemmology*, 30, 23-36.

582

583 Calligaro, T. Piorot, J.-P., and Querré, G. (1999) Trace element fingerprinting of jewelry rubies
584 by external beam PIXE. *Nuclear Instruments and Methods in Physics Research B*, 150, 628-634.

585

586 Esbensen, K.H. (2004) *Multivariate Data Analysis-in practice: An introduction to multivariate*
587 *data analysis and experimental design*, 598 p. CAMO process AS, Oslo.

588

589 Cremers, D.A., and Radziemski, L.J. (2006) *Handbook of Laser-Induced Breakdown*
590 *Spectroscopy*, 283 p. John Wiley & Sons. Ltd., Chichester.

591

592 Devouard, B., and Notari, F. (2009) The identification of faceted gemstones; from the naked eye
593 to laboratory. *Elements*, 5, 163-168.

594

- 595 Giuliani, G., Fallick, A.E., Garnier, V., France-Lanord, C., Ohnenstetter, D., and Schwarz, D.
596 (2005) Oxygen isotope composition as a tracer for the origins of rubies and sapphires. *Geology*,
597 33, 249-252.
- 598
599 Giuliani, G., Fallick, A., Ohnenstetter, D., and Pegere, G. (2009) Oxygen isotopes composition
600 of sapphires from the French Massif Central: implications for the origin of gem corundum in
601 basaltic fields. *Miner Deposita*, 44, 221-231.
- 602
603 Gray, A.L. (1985) Solid sample introduction by laser ablation for inductively coupled plasma
604 source mass spectrometry. *Analyst*, 110, 551-556.
- 605
606 Gübelin, E.J. (1953) *Inclusion as a Means of Gemstone Identification*, 220 p. Gemological
607 Institute of America, Los Angeles.
- 608
609 Gübelin, E.J., and Koivula, J.I. (1986) *Photoatlas of Inclusions in Gemstones*, 531 p. ABC
610 Edition, Zurich, Switzerland.
- 611
612 Guillong, M., and Günther, D. (2001) Quasi 'non-destructive' laser ablation-inductively coupled
613 plasma-mass spectrometry fingerprinting of sapphires. *Spectrochimica Acta Part B*, 56, 1219-
614 1231.
- 615
616 Günther, D., and Kane, R.E. (1999) Laser ablation-inductively coupled plasma-mass
617 spectrometry: A new way of analyzing gemstones. *Gems & Gemology*, 35, 160-161.
- 618
619 Hughes, R.W. (1997) *Ruby & Sapphire*, 511 p. RWH Publishing, Boulder, CO.
- 620
621 Liddicoat, R.T. (1990) The country of origin question. *Gems & Gemmology*, 26, 247.
- 622
623 McMillan, N.J., Montoya, C., and Chesner, W.H. (2012) Correlation of limestone beds using
624 laser-induced breakdown spectroscopy and chemometric analysis. *Applied Optics*, 51, B213-
625 B222.
- 626
627 Muhlmeister, S., Fritsch, E., Shigley, J.E., Devouard, B., and Laurs, B.M. (1998) Separating
628 natural and synthetic rubies on the basis of trace-element chemistry. *Gems and Gemology*, 43,
629 80-101.
- 630
631 Multari, R.A., Cremers, D.A., Dupre, J.M., and Gustafson, J.E. (2010) The use of laser-induced
632 breakdown spectroscopy (LIBS) for distinguishing between bacterial pathogen species and
633 strains. *Applied Spectroscopy*, 64, 750-759.
- 634

- 635 Peucat, J.J., Ruffault, P., Fritsch, E., Bouhnik-Le Coz, M., Simonet, C., and Lasnier, B. (2007)
636 Ga/Mg ratio as a new geochemical tool to differentiate magmatic from metamorphic blue
637 sapphires. *Lithos*, 98, 261-274.
638
- 639 Pornwilard, M.-M., Hansawek, R., Shiowatana, J., and Siripinyanond, A. (2011) Geographical
640 origin classification of gem corundum using elemental fingerprint analysis by laser ablation
641 inductively coupled plasma mass spectrometry. *International Journal of Mass Spectrometry*,
642 306, 57-62.
643
- 644 Rankin, A.H., Greenwood, J., and Hargreaves, D. (2003) Chemical fingerprinting of some East
645 African gem rubies by laser ablation ICP-MS. *Journal of Gemmology*, 28, 473-482.
646
- 647 Rossman, G.R. (2009) The geochemistry of gems and its relevance to gemology: Different
648 traces, different prices. *Elements*, 5, 159-162.
649
- 650 Saminpanya, S., Manning, D.A.C., Droop, G.T.R., and Henderson, C.M.B. (2003) Trace
651 elements in Thai gem corundums. *Journal of Gemmology*, 28, 399-415.
652
- 653 Sansonetti, J.E., Martin, W.C., and Young, S.L., (2005), *Handbook of Basic Atomic*
654 *Spectroscopic Data (version 1.1.2) (Online) Available: <http://physics.nist.gov/Handbook>*
655 *(accessed March 23, 2003). National Institute of Standards and Technology, Gaithersburg,*
656 *Maryland.*
657
- 658 Schwarz, D., and Schmetzer, K (2001) Rubies from the Vatomandry area, eastern Madagascar.
659 *Journal of Gemmology*, 27, 409-146.
660
- 661 Sharp, Z.D. (1990) A laser-based microanalytical method for the in situ determination of oxygen
662 isotope ratios of silicate and oxides. *Geochimica et Cosmochimica Acta*, 54, 1353-1357.
663
- 664 Shor, R., and Weldon, R. (2009) Ruby and sapphire production and distribution: A quarter
665 century of change. *Gems & Gemology*, 45, 236-259.
666
- 667 Silverman, B. W. (1986) *Density Estimation for Statistics and Data Analysis*, 175 p. Chapman &
668 *Hall/CRC Monographs on Statistics & Applied Probability.*
669
- 670 Sutherland F.L., and Abduriyim A. (2009) Geographic typing of gem corundum: a test case from
671 Australia. *Journal of Gemmology*, 31, 203-210.
672

- 673 Sutherland, F.L., Zaw, K., Mefre, S., Giuliani, G., Fallick, A.E., Graham, I.T., and Webb, G.B.
674 (2009) Gem-corundum megacrysts from east Australian basalt fields: trace elements, oxygen
675 isotopes, and origins. *Australian Journal of Earth Sciences*, 56, 1003-1022.
676
- 677 U.S. Department of State (2008a) 2008 Human Rights Report: Burma. (accessed January 2015)
678 <http://www.state.gov/g/drl/rls/hrrpt/2008/eap/119035.htm>.
- 679 U.S. Department of State (2008b) H.R. 3890 (110th): Tom Lantos Block Burmese JADE
680 (Junta's Anti-Democratic Efforts) Act of 2008. (accessed January 2015)
681 <http://www.govtrack.us/congress/bills/110/hr3890>.
- 682
- 683 Vysotsky, S.V., Yakovenko, V.V., Ignat'ev, A.V., and Karabstov, A.A. (2009) The oxygen
684 isotopic composition as an indicator of the genesis of "basaltic" corundum. *Russian Journal of*
685 *Pacific Geology*, 3, 64-48.
- 686
- 687 Ward, F. (1995) *Rubies and Sapphires*, 64 p. Gem Book Publishers, Bethesda, Maryland.
688
- 689 Wold, S., Sjöström, M., and Eriksson, L. (2001) PLS-regression: a basic tool of chemometrics.
690 *Chemometrics and Intelligent Laboratory Systems*, 58, 109-130.
- 691
- 692 Yui, T-F., Zaw, K., and Limtrakun, P. (2003) Oxygen isotope composition of the Denchai
693 sapphire, Thailand: a clue to its enigmatic origin. *Lithos*, 67, 153-161.
694
- 695 Yui, T-F., Wu, C-M., Limtrakun, P., Sricharn, W., and Boonsoong, A. (2006) Oxygen isotope
696 studies on placer sapphire and ruby in the Chanthaburi-Trat alkali basaltic gemfield, Thailand.
697 *Lithos*, 86, 197-211.
- 698
- 699 Yui, T-F., Zaw, K., and Wu, C-M. (2008) A preliminary stable isotope study on Mogok Ruby,
700 Myanmar. *Ore Geology Reviews*, 34, 192-199.
701

Figure Captions

702

703

704 Figure 1. LIBS analysis starts with a pulsed laser (B, with control box A), in this case a Nd-
705 YAG laser. A digital camera (C) allows one to target and photograph specific areas on samples.
706 A burst of laser light is focused in the sample by lens D, causing atoms to ablate and burn in a
707 short-lived plasma, or burning gas. Electrons in this high-temperature plasma are excited into
708 higher-energy orbitals, and give off energy in the form of light as they decay into lower-energy
709 orbitals during plasma cooling. This spectrum of light (different wavelengths for each element)
710 is collected by optic fiber and diffracted by a spectrometer (E) and recorded by a computer (F).

711

712 Figure 2. Representative ruby and sapphire LIBS spectra (averages of 30 spectra). Major
713 elemental emission lines are identified.

714

715 Figure 3. Partial Least Squares Regression model process. Half of the spectra from every
716 locality are used for calibration; the other half are used for validation. The spectra are divided
717 into two groups. One group contains spectra from the locality of interest; the other group
718 contains spectra from all other localities. A. Calibration. In calibration, the spectra are
719 regressed against the integers "1" (locality of interest) or "0" (all other localities) B.
720 Determination of the VAD (Value of Apparent Distinction), the value of the provenance variable
721 used to distinguish between the two groups, using provenance variables for each sample
722 calculated during the calibration stage. C. Prediction of provenance variables for the validation
723 samples. D. Calculation of success rate.

724

725 Figure 4. Kernel density estimates of the population of predicted values for rubies from Kenya
726 (on the right) and of the population of predicted values for rubies from other mines (on the left).
727 The sample predicted values are indicated by the vertical lines below the density curves – dashed
728 vertical lines are for predicted values for rubies from the Kenya mine; solid lines are for rubies
729 from other mines. The VAD (Value of Apparent Distinction) that minimizes the total crossover
730 areas of the two densities is indicated by the dashed vertical line.

731

732 Figure 5. The results of the validation step are shown for the Kenya ruby model. The predicted
733 provenance value (Y-axis) is shown for each sample in the model. Rubies from Kenya have
734 provenance variables greater than the Value of Apparent Distinction (0.29 for this model) and
735 thus are classified as Kenyan. The other samples, from India, Greenland, Madagascar,
736 Myanmar, Pakistan, Tanzania, and USA, yield provenance variables less than 0.29, and are
737 classified as belonging to this group of countries. One sample is incorrectly classified, yielding a
738 success rate of 99.4%.

739

740 Figure 6. The matching algorithm for sapphires consists of 8 models. The model correctly
741 predicts the country of origin for 98.9% of the validation spectra and the deposit of origin for
742 97.9% of the validation spectra.

743

744 Figure 7. Score plots and validation plots for PLSR (Partial Least Squares Regression) models in
745 the sapphire matching algorithm.

746

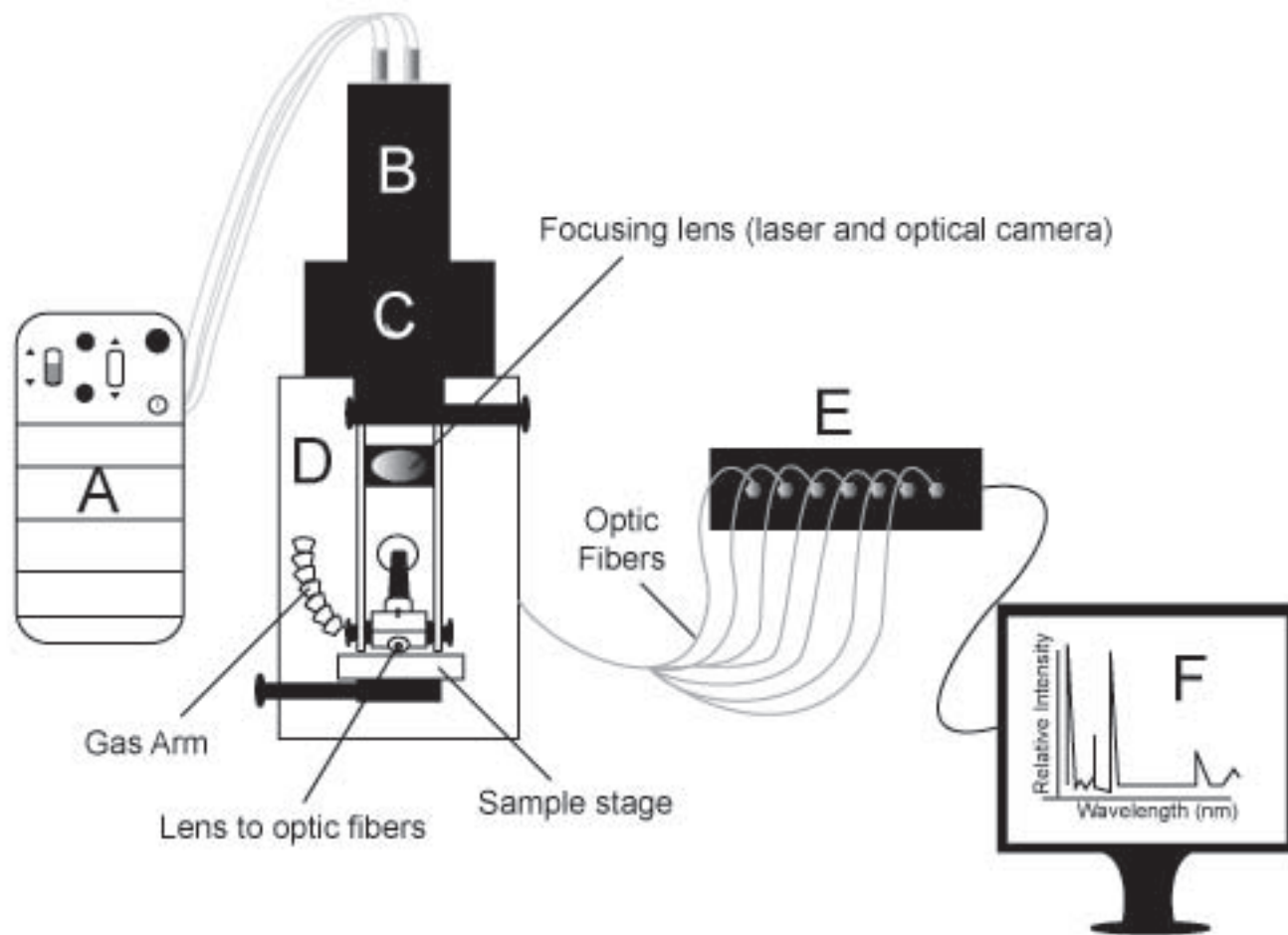
747 Figure 8. The matching algorithm for rubies consists of 12 models. The model correctly
748 predicts the country of origin for 96.0% of the validation spectra and the deposit of origin for
749 95.4% of the validation spectra.

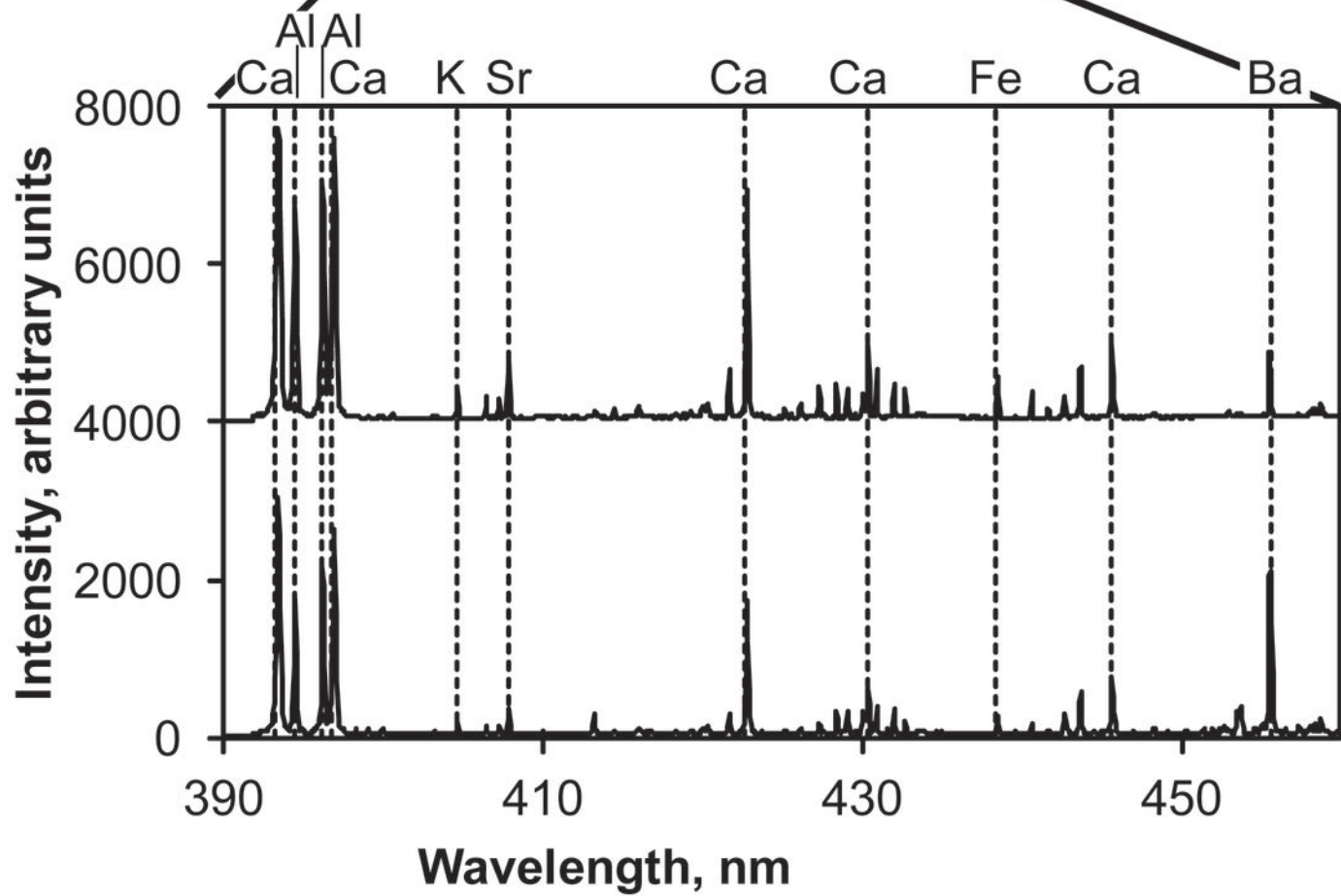
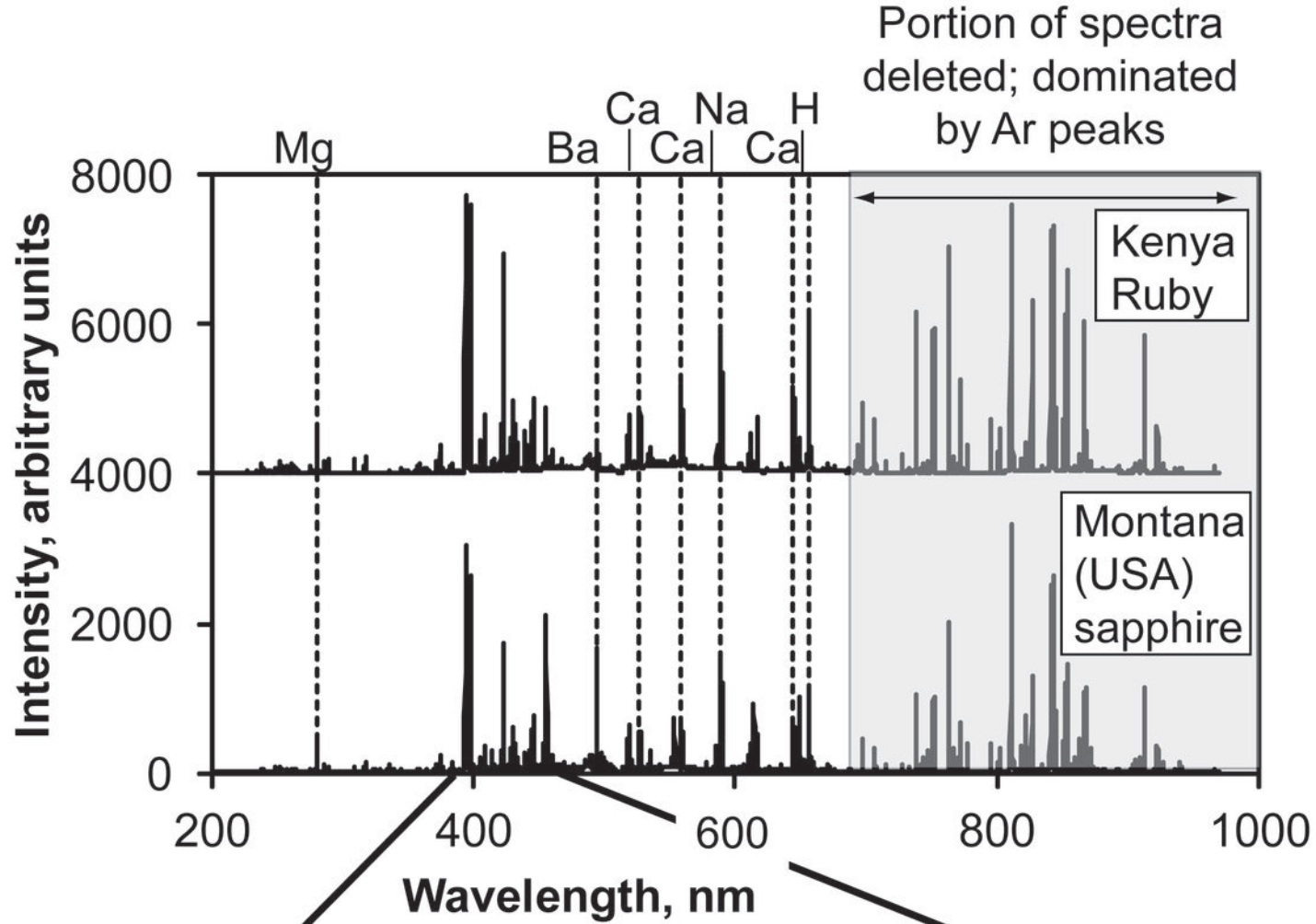
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751 Figure 9. Score plots and validation plots for PLSR (Partial Least Squares Regression) models in
752 the ruby matching algorithm.

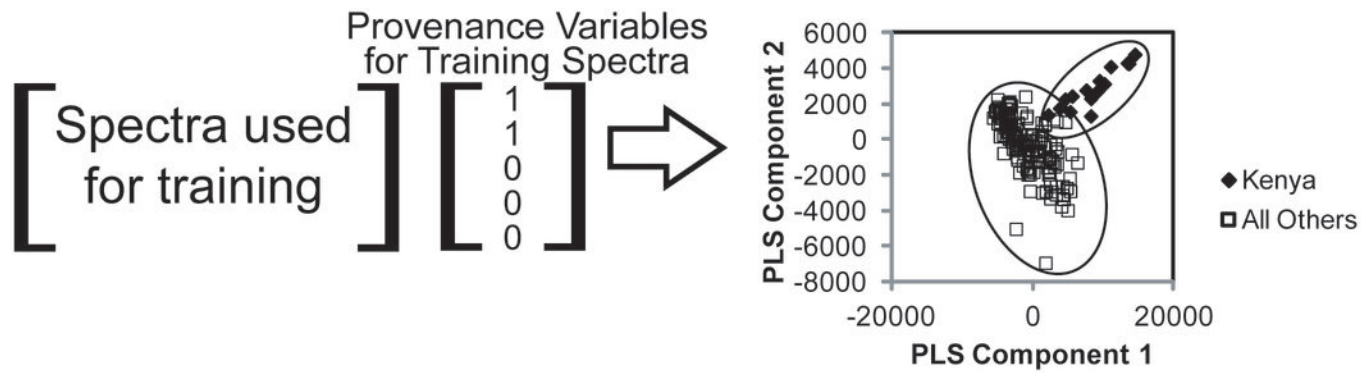
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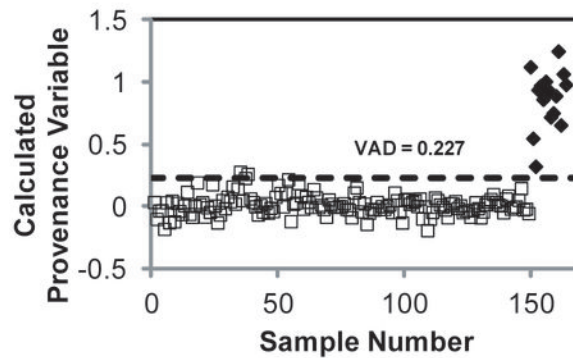




A. Step One: Training the PLSR model



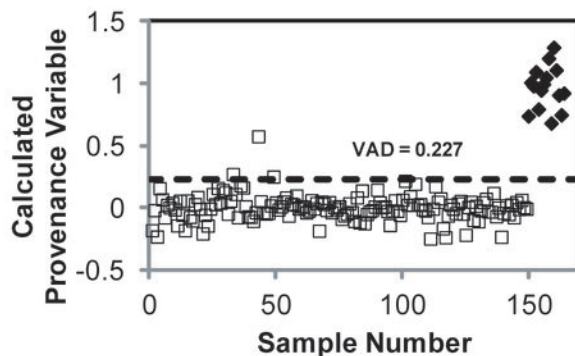
B. Step Two: Determine the Value of Apparent Distinction



C. Step Three: Prediction of Provenance Variables for Validation Samples

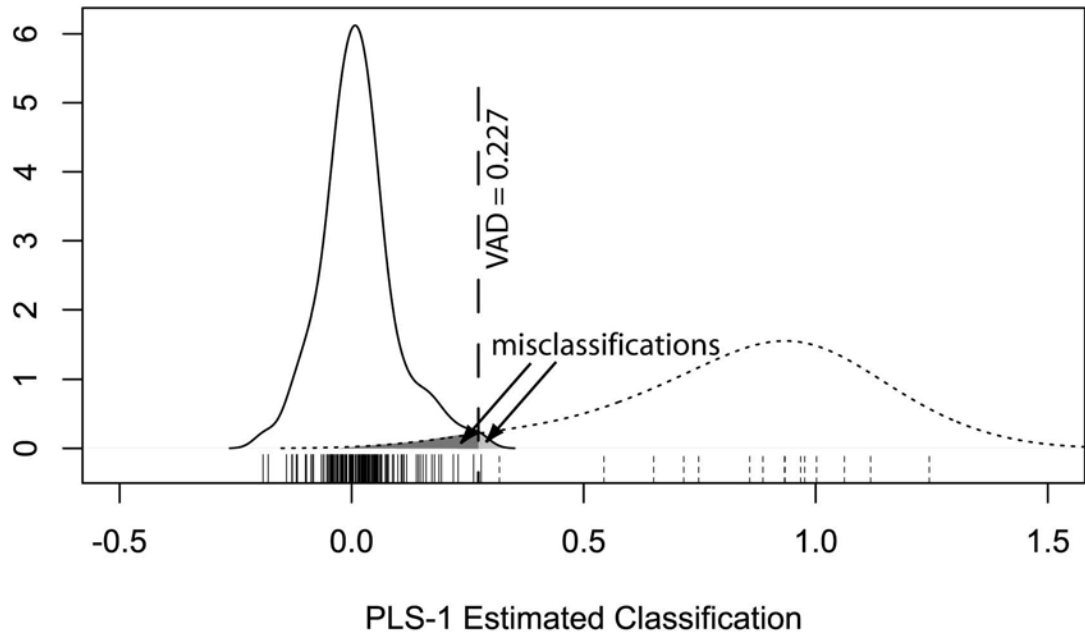


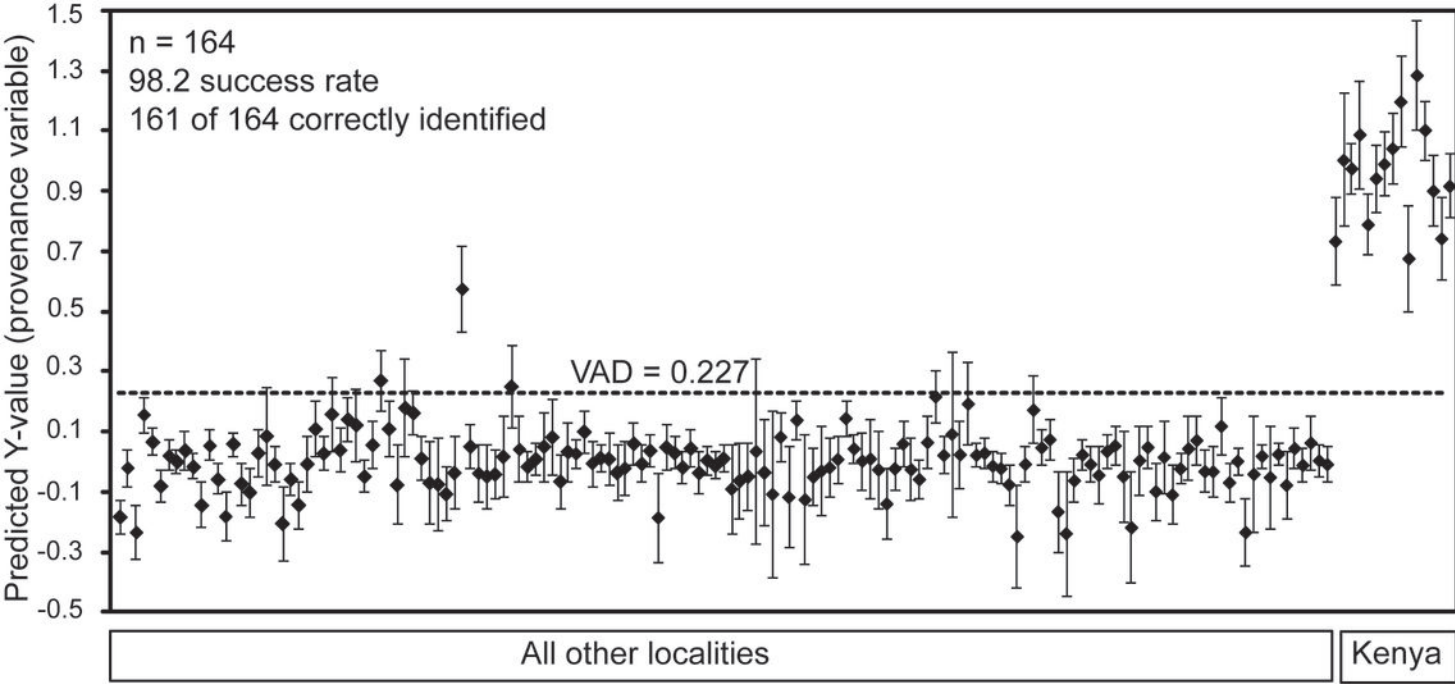
D. Step Four: Calculation of Success Rate



Correct Prediction
161 of 164 samples
98.2% success rate

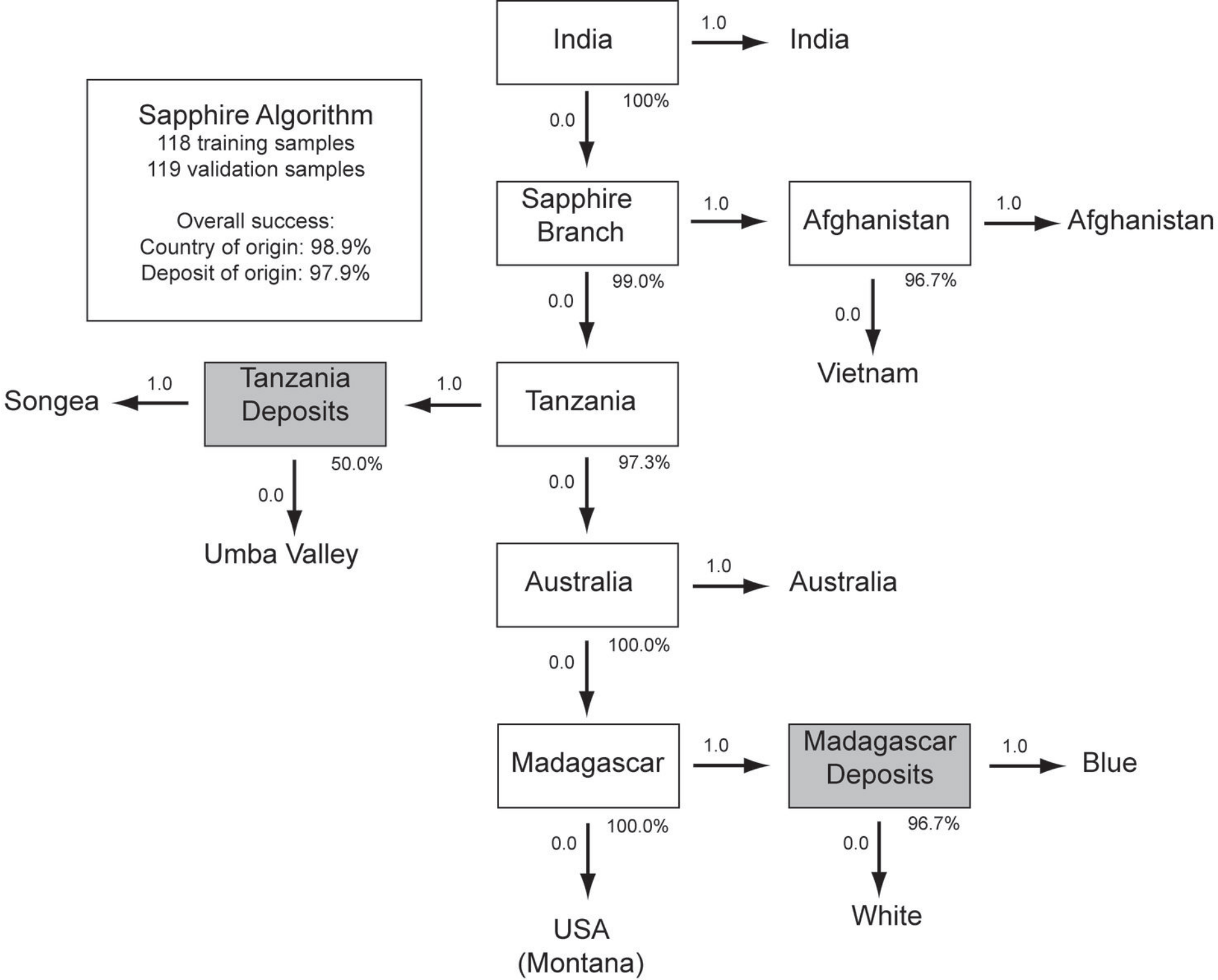
Density



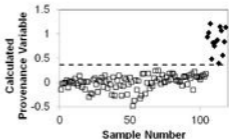
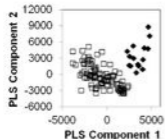


Sapphire Algorithm
118 training samples
119 validation samples

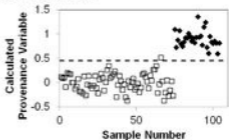
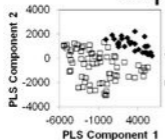
Overall success:
Country of origin: 98.9%
Deposit of origin: 97.9%



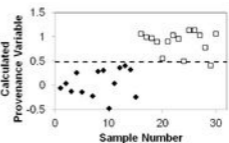
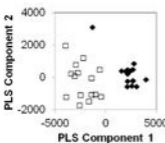
India



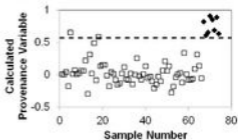
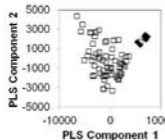
Sapphire Branch



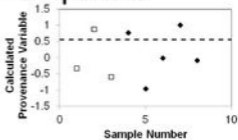
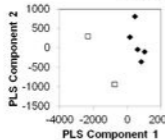
Afghanistan



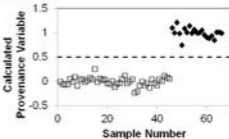
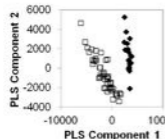
Tanzania



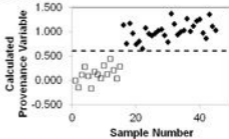
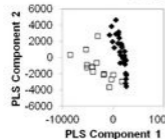
Tanzanian Deposits



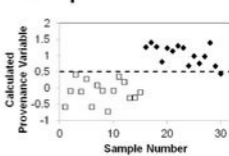
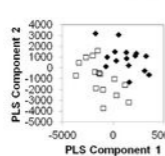
Australia



Madagascar

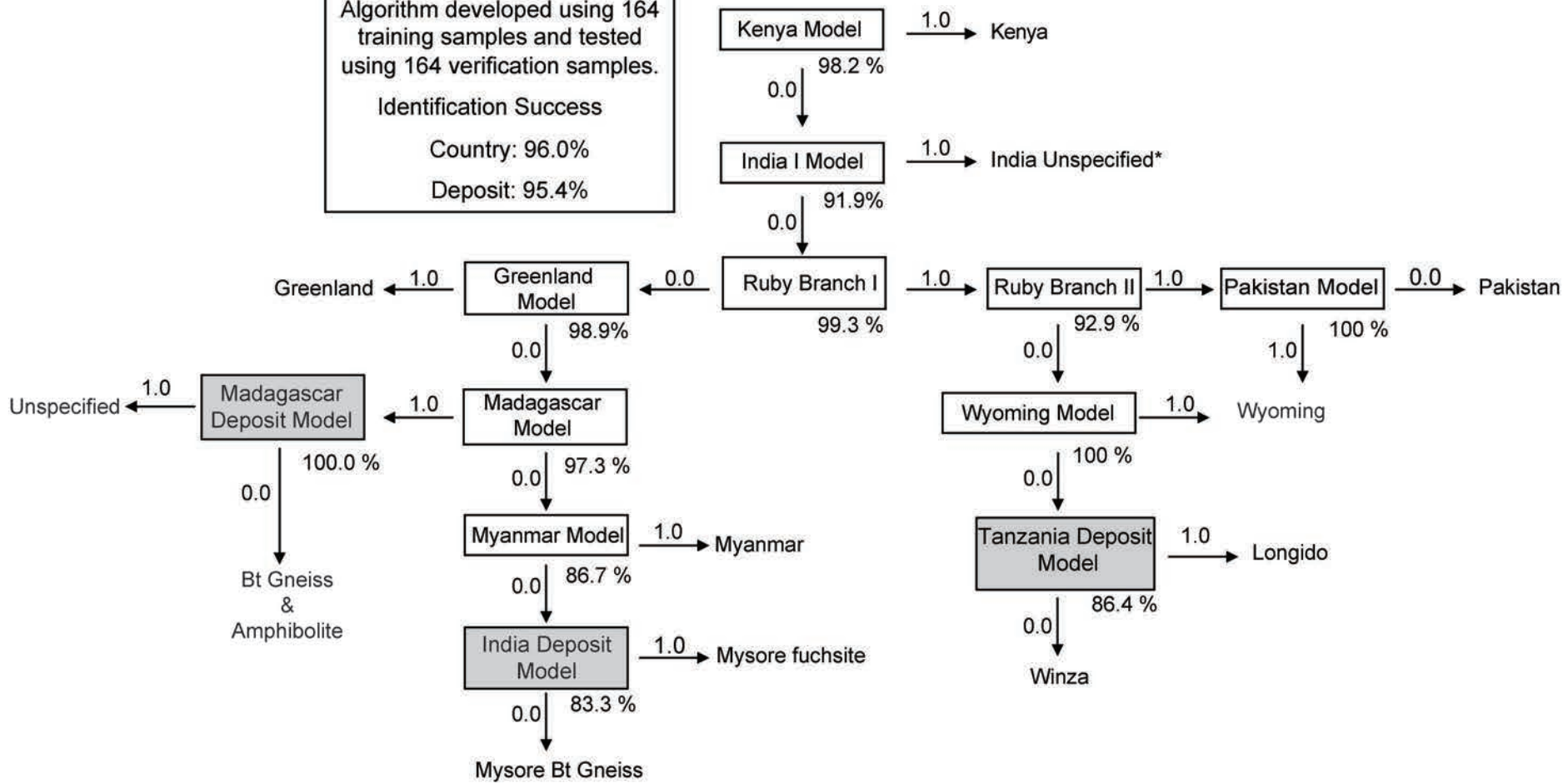


Madagascar Deposits

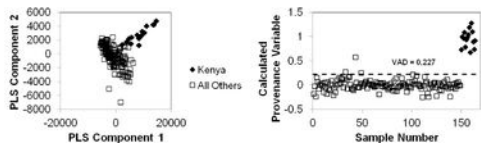


Ruby Provenance Algorithm

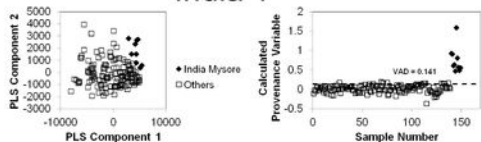
Algorithm developed using 164 training samples and tested using 164 verification samples.
Identification Success
 Country: 96.0%
 Deposit: 95.4%



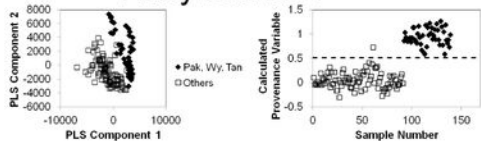
Kenya



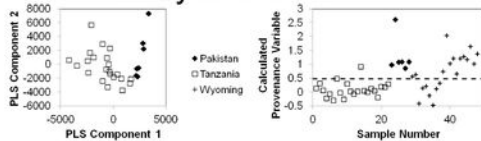
India 1



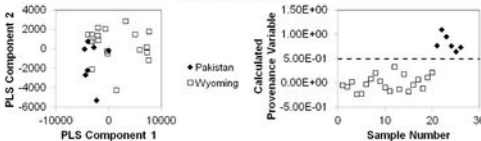
Ruby Branch I



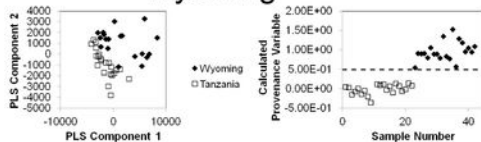
Ruby Branch II



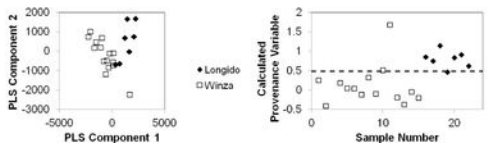
Pakistan



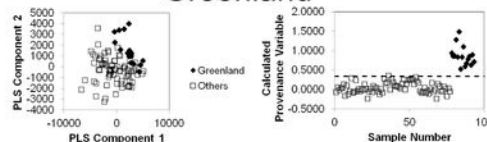
Wyoming



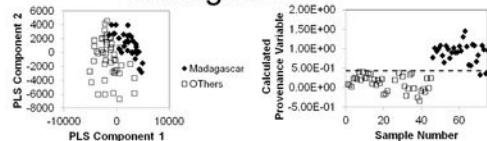
Tanzania Deposits



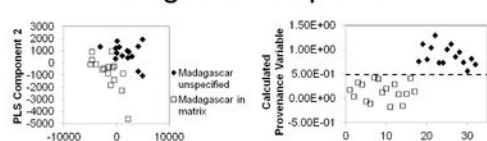
Greenland



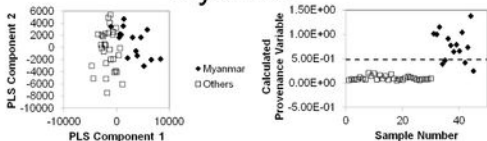
Madagascar



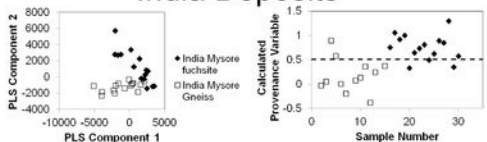
Madagascar Deposits



Myanmar



India Deposits



Sapphire Samples				
Country	Deposit	Host Lithology	Color(s)	No. of Sapphires
Afghanistan	Badakashan	Phologpite Schist	blue	30
Australia	Queensland	Unknown	yellow, dark blue	43
India	Mysore	Unknown	black	29
Madagascar	Southern	Unknown	white, beige	30
Madagascar	Southern	Unknown	bluish purple	30
Tanzania	Songea	Pegmatite	grey and black	10
Tanzania	Umba Valley	Unknown	brown & tan with blue tint	5
USA	Rock Creek, MT	Unknown	blue, green, yellow	30
Vietnam	Unknown	Unknown	black	30

Ruby ^a Samples				
Country	Deposit	Host Lithology		No. of Rubies
India	Mysore	Unknown	maroon	19
India	Mysore	Fuchsite	fuchsia	30; 8 samples
India	Mysore	Biotite Gneiss	fuchsia	30; 9 samples
Greenland	Fiskenaesset	Amphibolite	maroon	32
Kenya	Rift Valley	Unknown	fuchsia	30
Madagascar	Southern	Unknown	fuchsia	30
Madagascar	Southern	Amphibolite & Biotite Schist	fuchsia	35; 18 samples
Myanmar	Unknown	Unknown	maroon	30
Pakistan	Hunza Valley	Marble	magenta	13; 11 samples
Tanzania	Winza	Unknown	maroon	30
Tanzania	Longido	Fuchsite/Zoisite	fuchsia	14; 6 samples
USA	Wyoming	Fuchsite	purple	39

^a All pink to purple-red samples were classified as rubies in this study.

Country	Deposit of Origin	Success Rate, %	Correct Predictions	Elements Enriched in Deposit being Modeled¹
India	Psudipada	100	118 of 118	Ca (Zr, V, Na, H)
Afghanistan	Badakashan	96.7	29 of 30	Ba (Mg)
Vietnam	Unknown	96.7	29 of 30	Sr, Na
Australia	Queensland	100	66 of 66	Zr (Ba, Mg, Na)
USA	Rock Creek, MT	100	45 of 45	Zr (Mg)
Madagascar ²	country of origin	100	45 of 45	Li (Si, Sr)
Madagascar ³	Southern (White)	96.7	29 of 30	Mg
Madagascar ³	Southern (Blue)	96.7	29 of 30	Ba (Li)
Tanzania ²	Country of origin	97.3	72 of 74	(Fe, Ba)
Tanzania ³	Songea	50	4 of 8	Ba (Na, Li)
Tanzania ³	Umba Valley	50	4 of 8	Ca, Zr

Ruby Algorithm, listed in model order

Country	Deposit	Success I	Correct Predictions	
Kenya	Rift Valley	98.2	161 of 164	Zr (Ti, Ba, Ca)
India	Mysore, unspecified	91.9	137 of 149	Zr, Fe (Ti, Na, Ca, C)
Pakistan	Hunza Valley	100	26 of 26	Ca, Na
USA	Wyoming	100	42 of 42	(Ba, Sr, Na, Li)
Tanzania ²	country of origin	100	42 of 42	Mg
Tanzania ³	Winza	86.4	19 of 22	Ca (Na, Mg, Fe, Li)
Tanzania ³	Longido	86.4	19 of 22	Zr (Mg, Ti)
Greenland	Fiskenaasset	98.9	92 of 93	Ca, Mg (Fe, Ba, Zr, Cr, Na)
Madagascar ²	country of origin	97.3	73 of 75	Mg, Ca, Sr, Zr, Ba (Na, H)
Madagascar ³	Southern, unspecified	100	32 of 32	Zr (Mg, Sr, Ba)
Madagascar ³	Southern, gneiss and amphibolite	100	32 of 32	Ca, Na (Fe)
Myanmar	Unknown	86.7	39 of 45	(Mg, Ti, Cr, Ba, C)
India ²	country of origin	86.7	39 of 45	Si, Sr, H, Hf
India ³	Mysore, fuschite	83.3	25 of 30	Ba (Ca, Cr, H)

India ³	Mysore, gniess	83.3	25 of 30	(Mg, Na)
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¹Elements with strong influence; those with lesser but significant influence listed in parentheses.

²Model identifies country of origin only.

³Model identifies deposit of origin.