Revision 1

1 Calculation of the energetics of water incorporation in majorite garnet

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Abstract

Interpretation of lateral variations in upper mantle seismic wave speeds requires 8 constraints on the relationship between elasticity and water concentration at high-pressure for all 9 major mantle minerals, including the garnet component. We have calculated the structure and 10 energetics of charge-balanced hydrogen substitution into tetragonal MgSiO₃ majorite up to P =11 12 25 GPa using both classical atomistic simulations and complementary first-principles calculations. At the pressure conditions of Earth's transition zone, hydroxyl groups are predicted 13 to be bound to Si vacancies as the hydrogarnet defect, $[V_{Si} + 4OH_0]^X$, at the Si2 tetrahedral site 14 or as the $[V_{Mg} + 2OH_0]^X$ defect at the octahedral Mg3 site. The hydrogarnet defect is more 15 favorable than the $[V_{Mg} + 2OH_O]^X$ defect by 0.8 – 1.4 eV/H at 20 GPa. The presence of 0.4 wt% 16 Al₂O₃ substituted into the octahedral sites further increases the likelihood of the hydrogarnet 17 defect by 2.2-2.4 eV/H relative to the $[V_{Mg} + 2OH_0]^X$ defect at the Mg3 site. OH defects affect 18 the seismic ratio, $R = d\ln V_s/d\ln V_p$, in MgSiO₃ majorite ($\Delta R = 0.9 - 1.2$ at 20 GPa for 1400 ppm 19 wt H₂O) differently than ringwoodite at high pressure, yet may be indistinguishable from the 20 thermal $d\ln V_s/d\ln V_p$ for ringwoodite. The incorporation of 3.2 wt% Al₂O₃ also decreases $R(H_2O)$ 21 22 by ~0.2-0.4. Therefore, to accurately estimate transition zone compositional and thermal

anomalies, hydrous majorite needs to be considered when interpreting seismic body waveanomalies in the transition zone.

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Keywords

26 Hydrous majorite, Defect mechanisms, Force field, Computer simulation, Density functional27 theory

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Introduction

The amount of water stored in deep crustal and mantle rocks is largely unconstrained, yet 29 may account for a quantity of water comparable to or in excess of the amount contained in the 30 31 present oceans (Hirschmann 2006). Water has a first-order effect on the compressibility and deformation of the crust and mantle (e.g., Smyth et al. 2004; Xu et al. 2013) in addition to 32 melting temperature, electrical and thermal conductivity (e.g., Hirschmann 2006; Panero et al. 33 2013; Thomas et al. 2012). Since water is incorporated into the nominally anhydrous mineral 34 35 phases of Earth's mantle in the form of H defects (e.g., Wright 2006), a clear understanding of the atomic scale behavior and substitution mechanism of hydrogen in high-pressure silicates is 36 critical to our knowledge of mantle processes. 37

38 Majorite, $(Mg,Fe)SiO_3$, is the high-pressure garnet phase stable at transition-zone depths (410 - 660 km) and is the second most abundant phase after the high-pressure olivine 39 polymorphs, accounting for as much as 40 percent of the rock volume (Frost 2008). The defect-40 free, tetragonal Mg-endmember garnet, majorite (space group $I4_1/a$), has a structure consisting of 41 42 3 unique tetrahedral sites (Si1, Si2, and Si3) each linked by corner oxygens to octahedral sites, Mg3 and Si4, and two interstitial distorted dodecahedral sites, Mg1 and Mg2 (Figure 1) (Angel 43 et al. 1989). The 3 tetrahedral sites are distinguished from each other based on the occupancy of 44 the nearest neighbor octahedral sites. The Si1 tetrahedra are linked to Mg3 octahedra, the Si2 45

sites are linked to Si4 octahedra, and Si3 tetrahedra are linked to 2 Mg3 octahedra and 2 Si4 octahedra. The interstitial Mg1 dodecahedral site is more distorted than the Mg2 site. There are 6 unique oxygen sites (Supplemental Data: Table S1). The O1 and O2 sites have the same bonding environment but O1 is bonded to octahedral Mg and O2 is bonded to octahedral silicon. The O3 and O4 sites are both doubly bonded to the Mg1 distorted cubic site. Finally, the O5 and O6 sites are both involved in 2 cubic environments and 1 tetrahedra but O6 is bonded to the Mg octahedra.

The dominant carriers of hydrogen in the transition zone are the high-pressure 53 polymorphs of (Mg,Fe)₂SiO₄ (olivine), wadsleyite and ringwoodite, which can incorporate 54 significant amounts of hydrogen (1-3 wt% H₂O) into their structures (e.g., Kohlstedt et al. 1996; 55 Smyth and Jacobsen 2006). Partitioning experiments in the MgO-SiO₂-H₂O system at transition 56 zone P-T conditions show that the olivine polymorphs (wadsleyite and ringwoodite) dissolve ~ 1 57 58 order of magnitude more than MgSiO₃ (majorite, clinoenstatite, akimotoite) (Bolfan-Casanova et al. 2000) such that $D^{Mg2SiO4/MgSiO3} = \sim 10$. Because the solubility of water in the olivine 59 polymorphs decreases with temperature and the partitioning of water between wadsleyite and 60 ringwoodite may be close to $D^{wad/ring} = 1$ at high temperature (Bolfan-Casanova 2005), majorite 61 solubility and partitioning may play an important role throughout the entire thickness of the 62 transition zone. Water solubility in majorite garnet synthesized at transition zone pressures and 63 temperatures can contain up to ~700 ppm wt H₂O (Bolfan-Casanova et al. 2000; Katayama et al. 64 2003), a quantity sufficient to radically change the deformation characteristics of garnet. For a 65 more complete understanding of the implications of OH defects in garnet in the deep mantle, 66 systematic computational studies of hydrogen incorporation into majorite are required. 67

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At low pressures, H substitution in andradite garnet ($Ca_3Fe_2Si_3O_{12}$) takes place via the 68 69 hydrogarnet defect in which 4 hydrogen atoms charge balance a vacancy ordinarily occupied by a Si atom in the tetrahedral site (Lager et al. 1989). However, the hydrogarnet defect is 70 associated with a volume expansion of the tetrahedral site (e.g., Lager et al. 1989; Purton et al. 71 72 1992) due to the change in Coulomb forces caused by the Si vacancy and also to accommodate the hydrogen bonded network. This volume expansion should be less energetically favorable at 73 high pressure. Infrared absorption spectra indicate that OH is potentially incorporated into 74 majorite by formation of the hydrogarnet defect (Katayama et al. 2003). However, water 75 concentrations in natural garnet samples brought to the surface from the mantle (Bell and 76 Rossmann 1992a, 1992b) and infrared spectroscopy of both natural garnet (Amthauer and 77 Rossman 1998; Beran and Libowitzky 2006) and synthetic majorite (Bolfan-Casanova et al. 78 2000) indicate that hydrogen incorporation in majorite may be complex (Williams and Hemley 79 80 2001). Therefore a systematic investigation of the hydrogen uptake mechanism in majorite is 81 necessary to clarify the situation.

Lateral variations in seismic body wave velocities throughout the mantle are caused by 82 83 temperature and compositional (i.e., water concentration, iron content, partial melting) heterogeneities (Karato 2006). The hydration of transition zone minerals affects the seismic data 84 used to infer high- and low- temperature anomalies and interpretation of mantle plumes and 85 subducted slabs. The seismic ratio, $R=dln V_s/dln V_p$ can be used to differentiate between thermal 86 and compositional effects (Karato and Karki 2001). Indeed variations in seismic velocities, 87 expressed as $dln V_s/dln V_p$, have been used to suggest a strategy to disentangle the effects of 88 89 temperature and water content for ringwoodite and wadsleyite (Panero 2010; Li et al. 2011). The temperature and pressure dependence of majorite sound velocities have been established 90

experimentally (Irifune et al. 2008; Sinogeiken and Bass 2002). Constraining the effect of water
on majorite elasticity is critical to the accurate interpretation of seismic velocities in Earth's
transition zone.

By analogy with other H defects in high-pressure silicates, H is likely incorporated into 94 95 the dodecahedral, octahedral, and tetrahedral sites of the majorite structure. While interstitial hydrogen incorporation is possible in olivine (Balan et al. 2014), it is not likely in the denser 96 garnet structure at high-pressure. Thus, we present a computational investigation of the 97 energetics and associated geophysical properties (P- and S-waves velocities) resulting from 98 hydrogen incorporation in majorite via $[V_{Mg} + 2OH_0]^X$ and $[V_{Si} + 4OH_0]^X$ defects. By comparing 99 the defect energies associated with these different site substitutions of hydrogen, we determine 100 the most favorable hydrogen-defect mechanism. Additionally, we further investigate the 101 102 influence of aluminum on hydrogen incorporation and wave speeds.

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Computational methods

The energies associated with hydrogen and aluminum incorporation in tetragonal majorite garnet (MgSiO₃) were calculated as a function of pressure up to P = 25 GPa using classical atomistic simulations based on the Born model of solids, as implemented in the General Utility Lattice Program (GULP) (Gale and Rohl 2003).

The initial majorite structure was generated according to the experimental single-crystal structure refinement (Angel et al. 1989). Mg and Si are assumed to be ordered over the 2 symmetrically unique octahedral sites based on the low concentration of aluminum (< \sim 8 wt% Al₂O₃) and temperature (*T* = 0 K) (Nakatsuka et al. 1999; Vinograd et al. 2006). Majorite lattice energy minimizations were performed using the full body-centered tetragonal unit cell, which consists of 160 atoms. Interatomic potential functions were used to describe the total lattice energy in terms of the atomic positions. We adopt the fractional charges of Vinograd et al. (2006) where ionic charges are scaled by 0.85 to improve transferability with respect to cation-cation distances. The internal lattice energy is dominated by the Coulomb interactions and evaluated using an Ewald summation. We modeled the short-range interactions between closed shell ionic species using a Buckingham potential of the form;

120
$$U_{sr} = \sum_{ij} A_{ij} exp\left(-\frac{r_{ij}}{\rho_{ij}}\right) - \frac{C_{ij}}{r_{ij}^6}$$
(1)

where A, ρ , and C are empirically derived parameters. The sum is over pairs of ions, i and j ($i \neq j$), with a separation distance, r_{ij} . Cutoffs for the Buckingham potentials are 10.0 Å for hydrogen interactions and 12.0 Å for oxygen-oxygen and cation-oxygen interactions. These potentials are tapered to zero over a range of 2.0 Å to ensure smoothness of the potential energy surface (Mei et al. 1991).

Due to the partial covalence of the Si-O bond (Pauling 1980), a harmonic angle-bendingterm was also included:

128
$$U_{ijk} = \frac{1}{2}k_{\theta}(\theta - \theta_0)^2$$
 (2)

This was applied for both the Si-O and Al-O tetrahedra and octahedra in order to add an energy penalty when there is a deviation from the coordination-dependent equilibrium bond angle. Three-body terms applied to the majorite Si-O and Al-O polyhedra were defined based on bonding between ions, which was defined to be fixed during relaxation, rather than cutoff distances. The three-body contribution to the optimized total energy was confirmed to ensure that the bonding was correctly defined for each system such that no spurious terms were present. A shell model (Dick and Overhauser 1958) was adopted to account for the polarisability of the This is a preprint, the final version is subject to change, of the American Mineralogist (MSA) Cite as Authors (Year) Title. American Mineralogist, in press. (DOI will not work until issue is live.) DOI: http://dx.doi.org/10.2138/am-2015-5063

136 oxygen anions. The O core-shell interactions are described by spring constants with the137 functional form:

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$$U = \frac{1}{2}k_2r^2 + \frac{1}{24}k_4r^4$$
(3)

The short-range bonded O-H interaction was described using a Coulomb-subtracted Morsepotential (Saul et al. 1985);

141
$$U_r = D_e \left[\left(1 - \exp\left(-a(r - r_0) \right) \right)^2 \right] - \frac{q_i q_j}{r}$$
 (4)

where r_0 is the equilibrium bond length, q is the charge of the species, D_e and a are both fitted parameters physically related to the molecular dissociation energy and vibrational frequency. Here the Coulomb term is expressed in atomic units. The Morse potential is cutoff at 1.3 Å, while the Buckingham potential is excluded for the intramolecular interaction within the hydroxyl group.

Interatomic potential parameters (Table 1) developed for the anhydrous majorite-pyrope 147 solid solution (Vinograd et al. 2006) were augmented with force field parameters derived by 148 149 fitting to experimental structural and elastic properties of brucite, Mg(OH)₂, at both 0 GPa and high pressure (Catti et al. 1995; Jiang et al. 2006). Due to the different fractional charge of the 150 hydroxyl oxygen $(O^{-1.2})$ compared to the non-hydroxyl oxygen $(O^{-1.7})$, we derived the 151 152 Buckingham potential parameter, A, by fitting to data for brucite. The two-body potentials for 153 the interaction between the hydroxyl oxygen and both Al and Si were generated from those for the equivalent interaction for non-hydroxyl oxygen using scaling of coefficients (Schröder et al. 154 155 1992) by 0.709 assuming:

156
$$\frac{A_{Mg-0}^{-1.2}}{A_{Mg-0}^{-1.4}} = \frac{A_{Si-0}^{-1.2}}{A_{Si-0}^{-1.4}} = \frac{A_{Al-0}^{-1.2}}{A_{Al-0}^{-1.4}}$$
(5)

157 Validation of the potential model was accomplished through calculation of the structural

relaxation, including unit-cell parameters, and elasticity of majorite for pressures between 0 and 25 GPa. Additionally, we calculate the structure and elasticity of superhydrous B, Mg₁₀Si₃O₁₄(OH₄), for pressures between 0 and 25 GPa and the zero-pressure structure and bulk modulus of pyrope, corundum, α -quartz, coesite, stishovite, MgO, brucite, kaolinite, and lizardite using the interatomic potentials in Table 1.

A Newton-Raphson optimizer, with Broyden-Fletcher-Goldfarb-Shanno (BFGS) updating of the Hessian matrix, was used for energy minimization. When the gradient norm reached 0.1, we switched to rational function optimization (RFO) to ensure that the final state attained had positive definite curvature. The phonon density of states was also calculated to verify the absence of imaginary modes within the Brillouin zone.

Energy minimizations were performed on the majorite structure with both charged and 168 charge-neutral point defects. Intrinsic vacancies were created by removal of a single atom or 169 170 bound Mg-O pairs where the Mg and O are nearest neighbors. Using the Kröger-Vink defect notation, the intrinsic vacancy defects are expressed as V_{Mg} ", V_{Si} "", and V_{O} ". We calculated 171 172 Schottky defect energies in the form of vacancies where the negatively charged cation vacancy is 173 balanced by a positively charged oxygen vacancy. For mass balance, the atoms that are removed are assumed to form a crystalline solid whose lattice energy also contributes to the Schottky 174 defect energy. The extrinsic defects $OH_0^{,}$, $Al_{Si}^{,}$, $Al_{Mg}^{,}$, $[V_{Mg} + 2OH_0]^X$, $[V_{Si} + 4OH_0]^X$, $[Al_{Si} + 4$ 175 $Al_{Mg} + V_{Mg} + 2OH_0]^X$, and $[Al_{Si} + Al_{Mg} + V_{Si} + 4OH_0]^X$ were introduced by generating 176 vacancies and introducing impurities as appropriate. For the OH₀⁻ defect, the H atom was 177 178 initially placed at three different positions relative to each oxygen site and energy minimization calculations were run to determine the lowest energy configuration. 179 The lowest energy configuration was then used for the high-P calculations and we do not see a change in the 180

relaxed hydrogen configuration up to 25 GPa. The difference in energy between the defective 181 182 and the defect-free majorite lattice was taken to be the defect formation energy. Calculations with a single $[V_{Mg} + 2OH_O]^X$ or $[V_{Si} + 4OH_O]^X$ defect complex per unit cell contain 0.56 - 1.1 183 wt% H₂O and thus additional simulations were performed using 2 x 2 x 2 supercells (1280 184 185 atoms) for a more realistic concentration of hydrogen within the system (700 - 1400 ppm wt)H₂O) and to assess the influence of defect-defect interactions through the periodic boundary 186 The initial atomic positions of impurities were determined visually using GDIS 187 conditions. (Fleming and Rohl 2005) and confirmed after optimization. The lattice parameters for the 188 189 pressure of interest were generated from constant pressure optimizations of the defect-free, bulk cell. Charged defect calculations are performed in the presence of a uniform neutralizing 190 background charge at constant volume. The initial fractional coordinates for the high-pressure 191 192 calculations involving charged defects were taken from the optimization at the previous lower 193 pressure. This ensures that a consistent configuration is being considered as a function of pressure. Calculations involving majorite with charge-neutral defect complexes or any 194 195 calculation involving a defect-free phase were performed at constant pressure.

196 Complementary first-principles simulations were conducted at zero-pressure and P = 20GPa for the most energetically favorable charge-balanced defect complexes as determined by the 197 atomistic simulations. Static, DFT calculations were performed with VASP (Kresse and 198 199 Furthmüller 1996a, 1996b). Ultrasoft pseudopotentials were used and calculations were 200 performed using the Perdew-Wang 1991 (PW91) formalism of the generalized gradient approximation (GGA) for the exchange-correlation functional (Perdew 1991). All first-201 principles calculations were performed using a plane-wave cutoff of 600 eV with an energy 202 203 convergence criterion of 0.001 eV for optimization. The majorite calculations are performed at

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208 The relative stability of the two defect mechanisms, $[V_{Mg} + 2OH_0]^X$ and $[V_{Si} + 4OH_0]^X$

209 was determined by calculating the enthalpy according to the reactions;

at constant volume then subsequently relaxed at constant pressure.

210
$$Mg_{32N-2}Si_{32N}O_{96N}H_4 + 2MgO \leftrightarrow Mg_{32N}Si_{32N-1}O_{96N}H_4 + SiO_2$$
 (6)

211 and

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212
$$Mg_{32N-3}Al_2Si_{32N-1}O_{96N}H_4 + 2MgO \leftrightarrow Mg_{32N-1}Al_2Si_{32N-2}O_{96N}H_4 + SiO_2$$
 (7)

where N is the number of unit cells, with the assumption that the $[V_{Mg} + 2OH_0]^X$ defects are non-213 214 interacting. The enthalpy of SiO₂ was calculated while accounting for the α -215 quartz-coesite-stishovite phase transitions as a function of increasing pressure. The MgO and 216 SiO₂ calculations were performed using the same interatomic potentials (GULP) and pseudopotentials (VASP) as for the majorite calculations, and the initial unrelaxed structures 217 were taken from the American Mineralogist Crystal Structure Database (AMSCD) (Hazen 1976; 218 219 Levien and Prewitt 1981; Levien et al. 1980; Ross et al. 1990). This reaction does not involve 220 free H₂O due to the difficulty of modeling the energetics of supercritical water.

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Results

222 Validation of calculations

The calculated majorite structure (Figure 1) (Supplemental data: Table S2) reproduces the experimentally determined structure (Angel et al. 1989) as we find good quantitative agreement between our calculated results and those previously determined from both theory and experiment (Table 2). The structural parameters are within 0.6% of the experimental values, 227 while the errors are less than 6% for most elastic constants with the exception of C_{12} and C_{16} 228 (Table 3). Our calculated zero-pressure bulk modulus and shear modulus are within the spread 229 of experimental results and at P = 10 GPa deviate from experimental data (Sinogeikin and Bass 230 2002) by less than 3.5% (Table 3; Supplemental data: Figure S1). Results from our static lattice-231 energy calculations (SLEC) and the results from Vinograd et al. (2006) were obtained using essentially the same potential models, except for changes to the truncation of the Buckingham 232 potentials and the inclusion of a fourth-order spring constant in the shell model. Hence, the 233 agreement here is to be expected. For phases other than majorite, we find agreement between our 234 235 calculations and experimentally determined values (Supplemental data: Table S3, Figure S2), with differences of less than ~5% for all structural parameters and ~13% for most bulk moduli. 236 237 The greatest differences in bulk moduli are for MgO and brucite due to the inability of a simple shell-model to capture the well-known Cauchy violation ($C_{12} \neq C_{14}$) in periclase (Catlow et al. 238 239 1976) and the limited transferability of the interatomic potentials to non-silicates. Our first-240 principles calculations reproduce the experimental structure and are consistent with previous 241 DFT-GGA results (Table 2) (Supplemental data: Table S2). The generalized gradient 242 approximation used here tends to lead to a systematic overestimation of structural parameters 243 when compared to experiment, consistent with the observations in the present study. The axial 244 ratio calculated at P = 20 GPa using DFT results is only 0.3% smaller than the force field 245 approach.

246 Defect energies in the absence of water incorporation

The enthalpy of charged Mg, Si, and O, vacancy formation in MgSiO₃ garnet were calculated up to P = 25 GPa. The ^{VIII}Mg2 and ^{IV}Si2 sites are found to have the lowest energetic cost for forming Mg and Si vacancies (Table 4; Supplemental data: Figure S3). The octahedral 250 site is significantly less favorable for both Mg and Si vacancy defects. The Schottky defect with the lowest energy ($E_{\text{Schottky}} = 4.48 - 7.24 \text{ eV}$) is the $[V_{\text{Mg2}} + V_{\text{O5}}]^X$ defect (Table 4) in which the 251 252 Mg-vacancy and O-vacancy are nearest neighbors with an additional energy cost of 0.07 - 0.26eV when Mg2 and O5 vacancies are not nearest neighbors. Formation of a vacancy at the Mg1 253 254 site, which is bonded to all 6 oxygens, has a greater Schottky defect energy at zero-pressure 255 when the vacancies at the O1 and O2 sites are not nearest neighbors. Conversely at high 256 pressure, lower Schottky defect energies tend to be associated with Mg and O vacancies that are nearest neighbors with the exception of V_{Mg1} " neighboring V_{O1} " or V_{O6} ". When considering the 257 silicon sites, ^{IV}Si2 vacancies have the lowest Schottky defect energies (Table 4). 258

259 **Protonation mechanism**

Protonation of the O1, O4, and O5 sites have energies 0.3 - 0.6 eV lower than O2, O3, and O6 at zero pressure (Figure 2). The protonation energetics can be explained by whether Si (higher energy) or Mg (lower energy) occupies the octahedral site to which the protonated oxygen is bonded. Among the octahedral-Mg oxygen sites, the O5 site is the most favorable site for protonation with a defect formation energy 0.09-0.1 eV lower than O4 and O1. Protonation of the O6 site is 0.20-0.21 eV less favorable compared to the other 2 sites (O2 and O3) involved in Si octahedra.

At all pressures, the O5 site is the most likely to bind a hydrogen atom and the O5 protonation enthalpy increases with pressure at a smaller rate than for the other oxygen sites (Figure 2). Furthermore, protonation of the oxygen sites involved in Si octahedra become less favorable with pressure relative to the sites involved in Mg octahedra.

Based on the energetics associated with creating charged cation and oxygen vacancies,
neutral Schottky defects, and protonating the oxygen sites, we propose four distinct charge-

balanced hydrogen incorporation mechanisms in majorite. These mechanisms are $[V_{Mg2} +$ 273 $2OH_{05}^{X}$, $[V_{Mg3} + 2OH_{05}]^{X}$, $[V_{Si2} + 4OH_{06}]^{X}$, and $[V_{Si4} + 2OH_{02} + 2OH_{03}]^{X}$. The proposed 274 275 mechanisms include the tetrahedral, octahedral, and dodecahedral sites. The defect structures, as optimized at zero-pressure using the force field approach, are shown in Figure 3. We consider 276 hydrogen incorporation into the dodecahedral site as $[V_{Mg2} + 2OH_{O5}]^X$, into the octahedral sites 277 as either $[V_{Mg3} + 2OH_{05}]^X$ or $[V_{Si4} + 2OH_{02} + 2OH_{03}]^X$, and into the tetrahedral site as the 278 hydrogarnet-type defect $[V_{Si2} + 4OH_{O6}]^X$. The optimized hydrogarnet defect consists of the 4 H 279 atoms lying outside of the Si-vacant tetrahedra along the edges and this configuration is 280 confirmed by the DFT calculations. The other three optimized defects show the H atoms 281 pointing inward toward the vacancy and region of negative charge. The DFT calculations also 282 result in the H atoms pointing inward for the $[V_{Mg3} + 2OH_{05}]^X$ defect. However, there is a 283 difference in direction that the H atoms point. The force field calculations yield a configuration 284 285 in which the H atoms lie in the plane formed by the O4 and O5 atoms with the H atoms pointing toward opposite O4 atoms ($\angle O5$ -H-O1 = $\sim 110^{\circ}$). The DFT optimization results in the H atoms 286 pointing toward opposite O1 atoms ($\angle O5$ -H-O1 = $\sim 160^{\circ}$). 287

288	The $[V_{Mg3} + 2OH_{O5}]^{X}$ octahedral-based defect has formation energy 0.07 eV less than the
289	dodecahedral-based $[V_{Mg2} + 2OH_{O5}]^X$ defect at zero-pressure (Supplemental data: Figure S4).
290	The formation enthalpy difference between the two different Mg defects decreases to 0.01 eV at
291	P = 25 GPa. Thus, our interpretation is that H-substitution balanced by Mg vacancies is as likely
292	to occur at octahedral sites as it is to occur at dodecahedral sites. At $P = 0$ GPa, the hydrogarnet
293	defect $[V_{Si2} + 4OH_{O6}]^{X}$ is 3.56 eV more favorable than hydrogen incorporation into the
294	octahedral site that is normally occupied by silicon (Supplemental data: Figure S4). The
295	enthalpy difference between the Si-based hydrogen defects increases with increasing pressure to

3.96 eV at 25 GPa, and therefore the octahedral defect is not expected at any relevant pressure. The enthalpy for reaction 6, which is used to compare the relative stability of the hydrogarnet defect with the $[V_{Mg3} + 2OH_{O5}]^X$ defect, is negative at all pressures (Figure 4) indicating that the hydrogarnet defect should be significantly more stable in majorite at mantle pressures. The stability of the hydrogarnet defect is verified by the DFT calculations (Table 5). The partitioning of hydrogen between the Mg3 sites and Si2 sites can be calculated from the equilibrium constant, *K*, of reaction 6 as;

303
$$D^{Si2/Mg3} = K = \exp\frac{-\Delta G}{RT} \sim \exp\frac{-\Delta H}{RT}$$
 (8)

Because of a greater number of configurations with the Mg site over the Si site, entropic effects will increase ΔG at high temperatures. Therefore, as an upper bound, the partition coefficient at 20 GPa and 1800 K is $D^{Si2/Mg3} \approx 200$.

Al is most likely to be incorporated into the majorite structure at either the Si2 tetrahedral 308 or the octahedral sites: the Al_{Si4}' defect has a formation enthalpy that is only 0.13 eV less than 309 that of the Al_{Si2}' defect at zero-pressure and their enthalpies are equal to each other at 25 GPa. 310 The Al_{Mg3} defect has a formation enthalpy that is at least 1.1 eV less than the enthalpy 311 312 associated with Al substitution for dodecahedral Mg over the entire pressure range. Therefore, we propose that Al is incorporated into majorite via a coupled substitution with octahedral Mg 313 and either octahedral Si4 or tetrahedral Si2. We calculate the formation enthalpy of the $[V_{Mg3} +$ 314 $2OH_{05}^{X}$ defect and the $[V_{Si2} + 4OH_{06}]^{X}$ hydrogarnet defect in the presence of a coupled Al-315 substitution either as $[Al_{Mg3} + Al_{Si2}]^X$ or $[Al_{Mg3} + Al_{Si4}]^X$. Based on the mass-balanced reactions; 316 $Mg_{32N-1}Si_{32N}O_{96N}H_2 + Al_2O_3 \leftrightarrow Mg_{32N-1}Al_2Si_{32N-1}O_{96N}H_2 + MgSiO_3$ (9) 317

318 and

319 $Mg_{32N}Si_{32N-1}O_{96N}H_4 + Al_2O_3 \leftrightarrow Mg_{32N-1}Al_2Si_{32N-2}O_{96N}H_4 + MgSiO_3$ (10)

where Al₂O₃ is corundum and MgSiO₃ is majorite, both the $[V_{Mg3} + 2OH_{O5}]^X$ and the $[V_{Si2} + 2OH_{O5}]^X$ 320 $4OH_{O6}$ ^X are more stable in the presence of a coupled Al-substitution at all pressures (Figure 5). 321 322 Additionally, according to reaction 7 (Figure 4), the presence of Al serves to further stabilize the hydrogarnet defect relative to the $[V_{Mg3} + 2OH_{O5}]^X$. The reaction enthalpy as a function of 323 pressure for reactions 6 and 7 goes through a maximum due to the coesite-stishovite phase 324 transition in SiO₂. The maximum in reaction 6 occurs at 10-15 GPa but in reaction 7 it occurs at 325 7.5-10 GPa. We interpret this as the hydrogarnet defect being more energetically favorable at 326 327 lower pressures in the presence of Al.

328 Influence of defect-defect interactions

Comparison of the defect energies associated with both the single unit cell and 2 x 2 x 2 supercell of Al-free majorite shows that interaction of periodic images of the hydrogen defects is insignificant ($\Delta H_{def} \leq 0.03 \text{ eV}$) (Supplemental data: Figure S4). The defect-defect interactions in aluminous majorite are more significant with the supercell calculations (0.4 wt% Al₂O₃) resulting in hydrous defect formation enthalpies that are up to 0.39 eV greater than the calculations using a single unit-cell (3.2 wt% Al₂O₃).

335 Wave speeds in hydrous majorite

To examine quantities that could provide geophysical evidence of hydrogen incorporation in garnet in the upper mantle and transition zone, the Voigt-Reuss-Hill averages of the bulk and shear moduli were calculated from the elastic constants (Anderson 1963) derived from the force field calculations (Table 3) along with the compressional and shear acoustic velocities, V_p and V_s . There is a negligible effect of water on both V_p and V_s for majorite with 700 – 1400 ppm wt H₂O at 25 GPa (Figure 6). At these concentrations, body wave speeds are reduced by only ~0.2%, 342 unlikely to be detectable by seismological measurements within the limits of radial seismic profile uncertainties (Matas et al. 2007). When normalized to the same water concentration 343 (1400 ppm wt H₂O) over the pressure range of this study, the shear modulus of majorite with the 344 $[V_{\text{Si2}} + 4\text{OH}_{\text{O6}}]^X$ defect is 0.3% greater than with the $[V_{\text{Mg3}} + 2\text{OH}_{\text{O5}}]^X$ defect. There is even less 345 of a difference between the bulk moduli (<0.2%) and no difference between the densities as a 346 function of defect mechanism. Significant effects on body-wave speeds can only be seen at 347 concentrations of >0.5 wt% water with reductions in V_p and V_s of 1-2% at transition zone 348 pressures. However, such concentrations of water in majoritic garnets are unlikely in Earth's 349 350 mantle (Beran and Libowitzky 2006)

351

Discussion

352 **Defect Mechanisms**

Bolfan-Casanova et al. (2000) synthesized tetragonal MgSiO₃ majorite at 17.5 GPa and 353 \sim 1800 K with \sim 680 ppm wt H₂O. They argue against the hydrogarnet substitution based on the 354 IR spectra citing the volume expansion of the Si-O tetrahedra (Lager et al. 1989) and energetic 355 feasibility of the hydrogarnet defect formation only at large water contents (Rossman and Aines 356 357 1991). The OH-absorption band in synthetic majorite (Bolfan-Casanova et al. 2000) is centered 80 cm⁻¹ lower and is 65 cm⁻¹ broader compared to the hydrogarnet OH-absorption band in 358 pyrope synthesized at high-pressure (Withers et al. 1998). The volume expansion of the 359 tetrahedra in andradite garnets (Lager et al. 1989) has been used to explain the apparent abrupt 360 dewatering of pyrope at high-pressure (Withers et al. 1998). However, a more recent study 361 (Mookherjee and Karato 2010) shows that pyrope does not dewater abruptly at P = -7 GPa. 362 Natural grossular garnets with low-OH contents have complex IR spectra and are thus proposed 363 to have substitution of H at the dodecahedral and octahedral site but no evidence for these 364

365 substitutions was presented (Rossman and Aines 1991). Our results show that even at low-water 366 contents, the hydrogarnet defect is likely to form in majorite. Synthesis of majorite in the MORB + H₂O system results in a sharp peak centered at 3580 cm⁻¹ (Katavama et al. 2003) which 367 is only 20 cm⁻¹ lower than the hydrogarnet substitution in synthetic pyrope (Ackermann et al. 368 369 1983). For the hydrogarnet defect in majorite (P = 0 GPa), our calculated bond lengths using force field methods, d(O-O) = 2.83 and 3.24 Å for the shared and unshared edges, are shorter 370 than those in grossular (d(O-O) = 3.08 and 3.29 Å) also calculated using interatomic potentials 371 (Wright et al. 1994). Thus, the incorporation of hydrogen through the hydrogarnet defect causes 372 a greater tetrahedral volume expansion in grossular than in majorite due to a greater lengthening 373 of the 2 shared tetrahedral edges. This greater lengthening of the shared edges in grossular is 374 energetically favorable due to Ca, with its larger ionic radius, occupying the dodecahedral sites. 375 Additionally, our DFT optimizations of the hydrogarnet defect result in d(H...O) = 2.26-2.34 Å, 376 which is shorter than d(H...O) = 2.49-2.62 Å and d(H...O) = -2.23-2.54 Å for katoite and 377 hydropyrope calculated in a previous first principles study (Nobes et al. 2000). The shorter 378 d(H...O) in majorite relative to hydropyrope is related to the O-H...O angle. The longer 379 calculated distances in hydroyrope are associated with O-H...O = 113-120° compared to 146-380 147° in our majorite calculations. Based on shorter O...O and H...O distances, we expect the 381 OH-stretching vibrational frequency to be lower in majorite when compared to other garnets 382 (Libowitzky 1999). Thus it appears that the variation in the vibrational peak positions for the 383 hydrogarnet defect in garnet can be attributed to differences in major and trace element 384 chemistry and possibly the presence of an additional substitution mechanism. 385

386 Our calculated defect binding energies show that isolated hydroxyl groups are unlikely in 387 the majorite structure and hydrogen is associated with cation vacancies. The defect binding This is a preprint, the final version is subject to change, of the American Mineralogist (MSA) Cite as Authors (Year) Title. American Mineralogist, in press. (DOI will not work until issue is live.) DOI: http://dx.doi.org/10.2138/am-2015-5063

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energies for protonation of the ^{VI}Mg site and the formation of the hydrogarnet defect are
calculated according to the reactions;

390
$$V_{Mg3}'' + OH_{O5}' + OH_{O5}' \rightarrow [V_{Mg3} + 2OH_{O5}]^X$$
 (11)

391 and

392
$$V_{\rm Si}^{\prime\prime\prime\prime} + OH_{\rm O5}^{\cdot} + OH_{\rm O5}^{\cdot} + OH_{\rm O5}^{\cdot} + OH_{\rm O5}^{\cdot} \rightarrow [V_{\rm Si} + 4OH_{\rm O}]^X$$
 (12)

The energetics for formation of the hydrogarnet and $[V_{Mg3} + 2OH_{O5}]^{X}$ defects are thus -2.19 eV/H 393 and -1.09 eV/H at zero-pressure. The binding energies become more exothermic with increasing 394 pressure to -2.87 eV/H and -1.64 eV/H at 25 GPa confirming that isolated defects become less 395 favorable at high pressure. The preferential formation of the hydrogarnet defect is consistent 396 397 with atomistic simulations of hydrogen defect formation in ringwoodite (Blanchard et al. 2005). However, Blanchard et al. (2005) show a significantly greater driving force for hydrogen to be 398 bound to cation vacancies in ringwoodite with defect binding energies of -15.80 eV/H and -10.36 399 eV/H. This is consistent with the greater H₂O storage capacity of ringwoodite (e.g., Bolfan-400 401 Casanova 2005).

402 We also compare the relative defect energies of the two defect mechanisms through the 403 reaction of majorite with water as:

404
$$H_2O + Mg_{Mg}^{X} + 2O_O^{X} = [V_{Mg3} + 2OH_{O5}]^{X} + MgO$$
 (13)

405
$$H_2O + Si_{Si}^X + 4O_O^X = [V_{Si2} + 4OH_{O6}]^X + SiO_2$$
 (14)

406 The reaction energies are thus calculated according to;

407
$$E_{12} = E_{Mg-OH} + E_{PT} + U_{MgO}$$
 (15)

408
$$E_{13} = E_{\text{Hydrogarnet}} + 2E_{\text{PT}} + U_{\text{SiO}_2}$$
 (16)

409 where E_{PT} is the proton transfer energy and assumed to be -9.74 eV at zero-pressure. The 410 derivation of E_{PT} and the full Born-Haber thermochemical cycle for hydrolysis reactions can be

found elsewhere (Catlow 1977; Wright et al. 1994). Our zero-pressure calculations show that the 411 hydrogarnet defect is more favorable by 1.44 eV with large negative energies of -6.51 eV/H and 412 -7.95 eV/H for reactions 12 and 13. Thus, it is possible that both types of defects occur in 413 majorite with the hydrogarnet defect likely to be dominant. This is consistent with IR spectra 414 415 that show a deviation from a strict hydrogarnet substitution (Bolfan-Casanova et al. 2000). Atomistic simulations of defect mechanisms in the olivine polymorphs also show that one defect 416 mechanism tends to be favored over the other. In the case of ringwoodite, both mechanisms are 417 energetically favorable with reaction energies of -3.08 eV/H and -6.49 eV/H (Blanchard et al. 418 2005) and as with majorite, the hydrogarnet is more likely to be dominant. The hydrogarnet 419 defect is also likely to occur in olivine with a reaction energy of 0.4 eV/H compared to 1.5 eV/H 420 for the $[V_{Mg} + 2OH_0]^X$ defect (Walker et al. 2006). Conversely, the $[V_{Mg} + 2OH_0]^X$ is 5 eV more 421 favorable than the hydrogarnet defect in wadslevite (Walker et al. 2006). 422

Comparison of our DFT-GGA results at 20 GPa (Table 5) with the work of Panero (2010) confirms that the hydrogarnet defect is more likely to occur in majorite than in ringwoodite. The $[V_{Mg} + 2OH_0]^X$ defect is 0.54 eV/H more favorable in ringwoodite than in majorite, while the hydrogarnet defect formation enthalpy in majorite is 0.12 eV/H less than in ringwoodite. Reaction 3 shows that the hydrogarnet defect is more stable in ringwoodite by 0.17 eV/H (Panero 2010) compared to 0.82 eV/H in majorite.

The stability of the hydrous defects relative to the anhydrous phase in the presence of free H₂O at high-pressure can be accomplished through static calculations using Ice VIII (Panero 2006). The following reactions at 20 GPa are considered;

432
$$Mg_{31}Si_{32}O_{96}H_2 + MgO \rightarrow H_2O (Ice VIII) + Mg_{32}Si_{32}O_{96}$$
 (17)

433 and

19

434 $Mg_{32}Si_{31}O_{96}H_4 + SiO_2 \text{ (stishovite)} \rightarrow 2 H_2O \text{ (Ice VIII)} + Mg_{32}Si_{32}O_{96}$ (18)

resulting in calculated static reaction enthalpies of -1.88 eV and -0.47 eV respectively. 435 Considering the heat of fusion of H₂O at ambient conditions (0.06 eV) and assuming the Dulong-436 Petit limit, the relative enthalpy of reaction 17 increases to 0.09 eV at 20 GPa and 2000 K. 437 438 However, this represents an upper bound because the entropic effects of supercritical water are not considered here. Thus it appears more likely that the hydrogarnet defect will be stable at 439 transition zone conditions and the $[V_{Mg} + 2OH_0]^X$ defect may not occur at high P-T in the 440 presence of water. This supports the interpretation that it is solely the hydrogarnet defect found 441 442 in the IR spectra of Katayama et al. (2003).

It is possible that there are other H-defect mechanisms in majorite besides those considered here. Zhang and Wright (2010) show that coupled substitutions of Al and H into forsterite favors hydrogen substitution at the Si site by 1-2 eV/H. Our calculations show that the presence of Al stabilizes the hydrogarnet defect by 2.2-2.4 eV (Figure 4). However, Mookherjee and Karato (2010) propose that water is incorporated into pyrope at high water contents through the $[(Al+H)_{Si}]^{X}$ defect.

Majoritic garnet found in diamond inclusions originating from transition zone depths have been found to contain ~1 wt% Na₂O coupled with ~15-20 wt% Al₂O₃ (Stachl 2001). However, these garnet inclusions are most likely anhydrous with the weight percent of major and minor element oxides summing to >100%. Zhang and Wright (2012) show that the presence of Al³⁺ and the monovalent Li ion may increase the potential of olivine to incorporate water, with the hydrogarnet defect being particularly favorable. Therefore it may be possible that coupled substitution of Na⁺ and Al³⁺ promotes hydrogen uptake in garnet as well. This is a preprint, the final version is subject to change, of the American Mineralogist (MSA) Cite as Authors (Year) Title. American Mineralogist, in press. (DOI will not work until issue is live.) DOI: http://dx.doi.org/10.2138/am-2015-5063

The presence of iron in majorite may also affect the type of defect mechanism present in 456 457 majorite. Atomistic simulations show that in reducing environments, it is favorable for water to be incorporated at vacant oxygen sites formed through reduction of ferric iron to ferrous iron 458 (Wright and Catlow 1994). Indeed, incorporation of water in olivine through Fe redox exchange 459 460 has been observed experimentally (Demouchy and Mackwell 2006). However, IR-spectra of Febearing ringwoodite collected at high-pressure (>20 GPa) and low-temperature (5 K) show that 461 462 water is incorporated at both the octahedral site and through the hydrogarnet defect with multiple defect mechanisms leading to the broad OH-absorption band observed in ringwoodite at 463 higher temperatures (Panero et al. 2013). Therefore, we predict that the hydrogarnet defect is the 464 most stable and dominant defect mechanism in majorite, with the presence of multiple defect 465 mechanisms likely. 466

467

Implications

468 The partitioning of water between mineral phases of the transition zone is dependent upon the type of defect mechanism present in each phase (Keppler and Bolfan-Casanova 2006). 469 If both ringwoodite and majorite incorporate water mainly through the hydrogarnet substitution, 470 471 partitioning between the two phases is independent of water fugacity. Considering that ~1.4 wt% H₂O has been observed in a natural ringwoodite inclusion in a diamond from the transition 472 zone (Pearson et al. 2014), this suggests that majorite in the transition zone may contain 700 ppm 473 water, at least locally in the CH₄-rich environments that are conducive to diamond formation. 474 475 Majorite with water concentrations this large have been shown to be stable in synthesis experiments at lower transition zone pressure-temperature conditions (Bolfan-Casanova et al. 476 2000; Katayama et al. 2003). 477

Lateral heterogeneities in seismic wave speeds in the Earth's upper mantle can be caused by both variations in composition and temperature. The $R(H_2O)$ ratio of $dln(Vs)/d(H_2O)$ and $dln(Vp)/d(H_2O)$ and the R(T) ratio of dln(Vs)/dT and dln(Vp)/dT are useful to elucidate the underlying cause of mantle heterogeneities (Li et al. 2011). We calculate $R(H_2O)$ for Al-free majorite as;

483
$$R(H_2 0) = \frac{\ln V_s(1400 \text{ ppm wt } H_2 0) - \ln V_s(\text{anhydrous})}{\ln V_p(1400 \text{ ppm wt } H_2 0) - \ln V_p(\text{anhydrous})}$$
(19)

484 The R(T) value for majorite was calculated at 16 GPa such that;

485
$$R(T) = \frac{\ln V_s(1473 \text{ K}) - \ln V_s(300 \text{ K})}{\ln V_p(1473 \text{ K}) - \ln V_p(300 \text{ K})}$$
(20)

based on the ultrasonic measurements of Irifune et al. (2008). R(H₂O) for ringwoodite was taken 486 from Panero (2010) and Li et al. (2011). The Li et al. (2011) seismic ratios for olivine, 487 488 wadslyeite, and ringwoodite were determined using experimental and calculated densities, bulk and shear moduli (Inoue et al. 1998; Li et al. 2009; Liu et al. 2009; Mao et al. 2008, 2010; 489 490 Tsuchiya and Tsuchiya 2009; Wang et al. 2003). Even though water at the ~ 1000 ppm level has 491 only a minor effect on the absolute body wave speeds (Figure 6), our calculated $R(H_2O)$ values show that the presence of hydrated majorite is observable (Figure 7) within the typical seismic 492 493 model uncertainty of ± 0.15 (Karato and Karki 2001). The presence of Al has a significant effect on $R(H_2O)$, with our calculations showing that R decreases by ~0.2-0.4 in the presence of 3 wt% 494 Al₂O₃ with the Al substituted into the octahedral sites. Additionally, seismic wave speeds are 495 496 dependent upon the density, bulk modulus, and shear modulus thus the pressure dependence of R is particularly sensitive to the pressure derivatives of these parameters. In addition to pressure 497 498 and temperature, compositional variations, such as variations in Fe content can strongly 499 influence seismic ratios. However, even when considering the presence of Al, $R(H_2O)$ for 500 majorite appears to be significantly different than the same ratio for ringwoodite at high pressures with a difference of 0.5-1.2 at 20 GPa. At the base of the transition zone, $R(H_2O)$ for majorite is indistinguishable from R(T) of ringwoodite calculated by Li et al. (2011) using DFT. R(T) for majorite is ~0.5-1.0 greater than our calculated $R(H_2O)$ for majorite. Our calculated $R(H_2O)$ for Al-free majorite is indistinguishable from that of olivine and wadsleyite up to 15 and 20 GPa but becomes significantly different in the presence of aluminum. Therefore, it appears that the effect of hydrated, aluminous majorite should be visible in the upper mantle and neglecting it may result in an overestimate of temperature anomalies.

508

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References Cited

Ackermann, L., Cemic, L. and Langer, K. (1983) Hydrogarnet substitution in pyrope - a
possible location for "water" in the mantle. Earth and Planetary Science Letters, 62, 208214.

- Amthauer, G. and Rossman, G.R. (1998) The hydrous component in andradite garnet. American
 Mineralogist, 83, 835-840.
- Anderson, O.L. (1963) A simplified method for calculating Debye temperature from elastic
 constants. Journal of Physics and Chemistry of Solids, 24, 909-917.
- Andrault, D., Angel, R.J., Mosenfelder, J.L., and Le Bihan, T. (2003) Equation of state of
- 529 stishovite to lower mantle pressures, American Mineralogist, 88, 301-307.
- 530 Angel, R.J., Finger, L.W., Hazen, R.M., Kanzaki, M., Weidner, D.J., Liebermann, R.C. and
- 531 Veblen, D.R. (1989) Structure and twinning of single-crystal MgSiO₃ garnet synthesized
- at 17 GPa and 1800 °C. American Mineralogist, 74, 509-512.
- Angel. R.J., Allan, D.R., Miletich, R., and Finger, L.W. (1997) The use of quartz as an internal
- pressure standard in high-pressure crystallography. Journal of Applied Crytallography,
 30, 461-466.
- Angel, R.J., Mosenfelder, J.L., and Shaw, C.S.J. (2001) Anomalous compression and equation of
 state of coesite. Physics of the Earth and Planetary Interiors, 124, 71-79.
- Balan, E., Blanchard, M., Lazzeri, M., and Ingrin, J. (2014) Contribution of interstitial OH
- groups to the incorporation of water in forsterite. Physics and Chemistry of Minerals, 41,105-114.
- 541 Bass, J.D., Liebermann, R.C., Weidner, D.J., and Finch, S.J. (1981) Elastic properties from
- acoustic and volume compression experiments. Physics of the Earth and PlanetaryInteriors, 25, 140-158.
- Bell, D.R. and Rossman, G.R. (1992) Water in Earth's mantle the role of nominally
- anhydrous minerals. Science, 251, 1391-1397.
- 546 Bell, D.R. and Rossman, G.R. (1992) The distribution of hydroxyl in garnets from the

This is a preprint, the final version is subject to change, of the American Mineralogist (MSA) Cite as Authors (Year) Title. American Mineralogist, in press. (DOI will not work until issue is live.) DOI: http://dx.doi.org/10.2138/am-2015-5063

- subcontinental mantle of southern Africa. Contributions to Mineralogy and Petrology,
 111, 161-178.
 Beran, A. and Libowitzky, E. (2006) Water in natural mantle minerals II: Olivine, garnet and
 accessory minerals. In H. Keppler and J.R. Smyth, Eds., Water in Nominally Anhydrous
 Minerals, 62, p. 169-191, Reviews in Mineralogy and Geochemistry, Mineralogical
 Society of America, Chantilly, Virginia.
- Bish, D.L. (1993) Rietveld refinement of the kaolinite structure at 1.5 K. Clays and Clay
 Minerals, 41, 738-744.
- Blanchard, M., Wright, K. and Gale, J.D. (2005) A computer simulation study of OH defects in

556 Mg_2SiO_4 and Mg_2GeO_4 spinels. Physics and Chemistry of Minerals, 32, 585-593.

Bolfan-Casanova, N. (2005) Water in the Earth's mantle. Mineralogical Magazine, 69, 229-257.

- 558 Bolfan-Casanova, N., Keppler, H. and Rubie, D.C. (2000) Water partitioning between nominally
- anhydrous minerals in the MgO-SiO₂-H₂O system up to 24 GPa: implications for the
 distribution of water in the Earth's mantle. Earth and Planetary Science Letters, 182, 209221.
- Catlow, C.R.A. (1977) Oxygen incorporation in alkaline-Earth fluorides. Journal of Physics and
 Chemistry of Solids, 38, 1131-1136.
- 564 Catlow, C.R.A., Faux, I.D. and Norgett, M.J. (1976) Shell and breathing shell model
- 565 calculations for defect formation energies and volumes in magnesium oxide. Journal of
 566 Physics C-Solid State Physics, 9, 419-429.
- 567 Catti, M., Ferris, G., Hull, S., and Pavese, A. (1995) Static compression and H disorder in
- brucite, Mg(OH)₂, to 11 GPa: a powder neutron diffraction study. Physics and Chemistry
 of Minerals, 22, 200-206.

- 570 Demouchy, S. and Mackwell, S. (2006) Mechanisms of hydrogen incorporation and diffusion in
- iron-bearing olivine. Physics and Chemistry of Minerals, 294, 347-355.
- 572 Dick, B.G. Jr. and Overhauser, A.W. (1958) Theory of the dielectric constants of alkali halide
 573 crystals. Physical Review, 112, 90-103.
- 574 Finger, L.W. and Hazen, R.M. (1978) Crystal structure and compression of ruby to 46 kbar.
- 575 Journal of Applied Physics, 49, 5823.
- Fleming, S. and Rohl, A. (2005) GDIS: a visualization program for molecular and periodic
 systems. Zeitschrift für Kristallographie, 220, 580–584.
- 578 Frost, D.J. (2008) The upper mantle and transition zone. Elements, 4, 171-176.
- 579 Gale, J.D. and Rohl, A.L. (2003) The general utility lattice program (GULP). Molecular
- 580 Simulation, 29, 291-341.
- 581 Gwamnesia, G.D., Chen, G., and Liebermann, R.C. (1998) Sound velocities in MgSiO₃-garnet to
- 582 8 GPa. Geophysical Research Letters, 25, 4553-4556.
- 583 Hazen, R.M. (1976) Effects of temperature and pressure on cell dimension and x-ray
- temperature factors of periclase. American Mineralogist, 61, 266-271.
- Hirschmann, M.M. (2006) Water, melting, and the deep Earth H₂O cycle. Annual Review of
 Earth and Planetary Sciences, 34, 629-653.
- Inoue, T., Weidner, D.J., Northrup, P.A. and Parise, J.B. (1998) Elastic properties of hydrous
 ringwoodite (gamma-phase) in Mg₂SiO₄. Earth and Planetary Science Letters, 160, 107-
- 589 113
- Irifune, T., Higo, Y., Inoue, T., Kono, Y., Ohfuji, H. and Funakoshi, K. (2008) Sound velocities
 of majorite garnet and the composition of the mantle transition region. Nature, 451, 814817.

593	Jacobsen, S.D., Reichmann, HJ., Spetzler, H.A., Mackwell, S.J., Smyth, J.R., Angel, R.J., and
594	McCammon, C.A. (2002) Structure and elasticity of single-crystal (Mg,Fe)O and a new
595	method of generating shear waves for gigahertz ultrasonic interferometry. Journal of
596	Geophysical Research, 107, 2037.
597	Jiang, F., Speziale, S., and Duffy, T.S. (2006) Single-crystal elasticity of brucite, Mg(OH) ₂ , to 15
598	GPa by Brillouin scattering. American Mineralogist, 91, 1893-1900.
599	Karato, S. (2006) Remote sensing of hydrogen in Earth's mantle. In H. Keppler and J.R. Smyth,
600	Eds., Water in Nominally Anhydrous Minerals, 62, p. 343-375, Reviews in Mineralogy
601	and Geochemistry, Mineralogical Society of America, Chantilly, Virginia.
602	Karato, S. and Karki, B.B. (2001) Origin of lateral variation of seismic wave velocities and
603	density in the deep mantle. Journal of Geophysical Research, 106, 21771-21783.
604	Katayama, I., Hirose, K., Yurimoto, H. and Nakashima, S. (2003) Water solubility in majoritic
605	garnet in subducting oceanic crust. Geophysical Research Letters, 30, 2155.
606	Keppler, H. and Bolfan-Casanova, N. (2006) Thermodynamics of water solubility and
607	partitioning. In H. Keppler and J.R. Smyth, Eds., Water in Nominally Anhydrous
608	Minerals, 62, p. 193-230, Reviews in Mineralogy and Geochemistry, Mineralogical
609	Society of America, Chantilly, Virginia.
610	Kohlstedt, D.L., Keppler, H. and Rubie, D.C. (1996) Solubility of water in the alpha, beta and
611	gamma phases of (Mg,Fe) ₂ SiO ₄ . Contributions to Mineralogy and Petrology, 123, 345-
612	357.
613	Kresse, G. and Furthmüller, J. (1996) Efficiency of ab-initio total energy calculations for metals
614	and semiconductors using a plane-wave basis set. Computational Materials Science, 6,
615	15-50.

- 616 Kresse, G. and Furthmüller, J. (1996) Efficient iterative schemes for ab initio total-energy
- calculations using a plane-wave basis set. Physical Review B, 54, 11169-11186.
- Lager, G.A., Armbruster, T., Rotella, F.J. and Rossman, G.R. (1989) OH substitution in garnets:
- k-ray and neutron-diffraction, infrared, and geometric-modeling studies. American
 Mineralogist, 74, 840-851.
- 621 Levien, L. and Prewitt, C.T. (1981) High-pressure crystal structure and compressibility of
- 622 coesite. American Mineralogist, 66, 324-333.
- Levien, L., Prewitt, C.T. and Weidner, D.J. (1980) Structure and elastic properties of quartz at
 pressure. American Mineralogist, 65, 920-930.
- Libowitzky, E. (1999) Correlation of O-H stretching frequencies and O-H...O hydrogen bond
 lengths in minerals. Monatshefte für Chemie, 130, 1047-1059.
- Li, B., Rigden, S.M., and Liebermann, R.C. (1996) Elasticity of stishovite at high pressure.

628 Physics of the Earth and Planetary Interiors, 96, 113-127.

- Li, L., Brodholt, J. and Alfe, D. (2009) Structure and elasticity of hydrous ringwoodite: A first
 principle investigation. Physics of the Earth and Planetary Interiors, 177, 103-115.
- Li, L., Weidner, D.J., Brodholt, J.P. and Alfe, D. (2011) Prospecting for water in the transition
- $zone: d \ln(Vs)/d \ln(Vp)$. Physics of the Earth and Planetary Interiors, 189, 117-120.
- Litasov, K.D., Ohtani, E., Ghosh, S., Nishihara, Y., Suzuki, A., and Funakoshi, K. (2007)
- 634 Thermal equation of state of superhydrous phase B to 27 GPa and 1373 K. Physics of the
 635 Earth and Planetary Interiors, 164, 142-160.
- Liu, J., Chen, G., Gwamnesia, G.D., and Lieberman, R.C. (2000) Elastic wave velocities of
- 637 pyrope-majorite garnets ($Py_{62}Mj_{38}$ and $Py_{50}Mj_{50}$) to 9 GPa. Physics of the Earth and 638 Planetary Interiors, 120, 153-163.

- 639 Liu, L., Du, J., Zhao, J., Liu, H., Gao, H. and Chen, Y. (2009) Elastic properties of hydrous
- 640 forsterites under high pressure: first-principle calculations. Physics of the Earth and641 Planetary Interiors, 176, 89-97.
- Mao, Z., Jacobsen, S.D., Jiang, F., Smyth, J.R., Holl, C.M. and Duffy, T.S. (2008) Elasticity of
- hydrous wadsleyite to 12 GPa: implications for Earth's transition zone. Geophysical
 Research Letters, 35, L21305.
- Mao, Z., Jacobsen, S.D., Jiang, F., Smyth, J.R., Holl, C.M., Frost, D.J. and Duffy, T.S. (2010)
- 646 Velocity crossover between hydrous and anhydrous forsterite at high pressures. Earth and
 647 Planetary Science Letters, 293, 250-258.
- Matas, J., Bass, J., Ricard, Y., Mattern, E. and Bukowinski, M.S.T. (2007) On the bulk
- 649 composition of the lower mantle: predictions and limitations from generalized inversion650 of radial seismic profiles. Geophysical Journal International, 170, 764-780.
- 651 Mei, J., Davenport, J.W. and Fernando, G.W. (1991) Analytic embedded-atom potentials for
- fcc metals: application to liquid and solid copper. Physical Review B, 43, 4653-4658.
- Mellini, M. and Zanazzi, P.F. (1989) Effects of pressure on the structure of lizardite-1T.
- European Journal of Mineralogy, 1, 13-19.
- Mookherjee, M. and Karato, S. (2010) Solubility of water in pyrope-rich garnet at high pressures
 and temperature. Geophysical Research Letters, 37, L03310.
- Nobes, R.H., Akhmatskaya, E.V., Milman, V., White, J.A., Winkler, B., and Pickard, C.J. (2000)
- An ab initio study of hydrogarnets. American Mineralogist, 85, 1706-1715.
- Nakatsuka, A., Yoshiasa, A., Yamanaka, T., Ohtaka, O., Katsura, T. and Ito, E. (1999)
- 660 Symmetry change of majorite solid-solution in the system Mg₃Al₂Si₃O₁₂-MgSiO₃.
 661 American Mineralogist, 84, 1135-1143.

- Pacalo, R.E.G. and Weidner, D.J. (1996) Elasticity of superhydrous B. Physics and Chemistry of
 Minerals, 23, 520-525.
- Pacalo, R.E.G. and Weidner, D.J. (1997) Elasticity of majorite, MgSiO₃ tetragonal garnet.
 Physics of the Earth and Planetary Interiors, 99, 145-154.
- Panero, W.R. (2006) Aluminum incorporation in stishovite. Geophysical Research Letters, 33,
 L20317.
- Panero, W.R. (2010) First principles determination of the structure and elasticity of hydrous
 ringwoodite. Journal of Geophysical Research, 115, B03203.
- Panero, W.R., Smyth, J.R., Pigott, J.S., Liu, Z. and Frost, D.J. (2013) Hydrous ringwoodite to 5
- K and 35 GPa: multiple hydrogen bonding sites resolved with FTIR spectroscopy.
 American Mineralogist, 98, 637-642.
- Pauling, L. (1980) The nature of silicon-oxygen bonds. American Mineralogist, 65, 321-323
- Pearson, D.G., Brenker, F.E., Nestola, F., McNeill, J., Nasdala, L., Hutchison, M.T., Matveev,
- 675 S., Mather, K., Silversmit, G., Schmitz, S., Vekemans, B. and Vincze, L. (2014) Hydrous
- 676 mantle transition zone indicated by ringwoodite included within diamond. Nature, 507,677 221-229.
- 678 Perdew, J.P. (1991) Unified theory of exchange and correlation beyond the local density
- approximation, In P. Ziesche and H. Eschrig, Eds., Electronic Structure of Solids '91, p.
- 680 11-20, Akademie Verlag, Berlin.
- Purton, J., Jones, R., Heggie, M., Öberg, S., and Catlow, C.R.A. (1992) LDF pseudopotential
- calculations of the alpha-quartz structure and hydrogarnet defect, Physics and Chemistryof Minerals, 18, 389-392
- Ross, N.L., Shu, J.-F., Hazen, R.M. and Gasparik, T. (1990) High-pressure crystal chemistry of

- stishovite. American Mineralogist, 75, 739-747.
- 686 Rossman, G.R. and Aines, R.D. (1991) The hydrous components in garnets: grossular-
- 687 hydrogrossular. American Mineralogist, 76, 1153-1164.
- 688 Saul, P., Catlow, C.R.A., and Kendrick, J. (1985) Theoretical studies of protons in sodium
- hydroxide. Philosophical Magazine B, 51, 107-117.
- 690 Schröder, K.-P., Sauer, J., Leslie, M., Catlow, C.R.A. and Thomas, J.M. (1992) Bridging
- hydroxyl-groups in zeolitic catalysts: a computer simulation of their structure,
 vibrational properties and acidity in protonated faujasites (H-Y zeolites). Chemical
 Physics Letters, 88, 320-325.
- 694 Sinogeikin, S.V., Bass, J.D., O'Neill, B., and Gasparik, T. (1997) Elasticity of tetragonal end-
- member majorite and solid solutions in the system Mg₄Si₄O₁₂-Mg₃Al₂Si₃O₁₂. Physics and
 Chemistry of Minerals, 24, 115-121.
- Sinogeikin, S.V., Bass, J.D., Kavner, A., and Jeanloz, R. (1997) Elasticity of natural majorite and
 ringwoodite from the Catherwood meteorite. Geophysical Research Letters, 24, 3265 3268.
- Sinogeiken, S.V., and Bass, J.D. (2000) Single-crystal elasticity of pyrope and MgO to 20 GPa
- by Brillouin scattering in the diamond cell. Physics of the Earth and Planetary Interiors,
 120, 43-62.
- Sinogeikin, S.V. and Bass, J.D. (2002) Elasticity of majorite and a majorite-pyrope solid
- solution to high pressure: implications for the transition zone. Geophysical Research
 Letters, 29, 1017.
- Smyth, J.R. and Jacobsen, S.D. (2006) Nominally Anhydrous Minerals and Earth's Deep Water
 Cycle. In S.D. Jacobsen and S. van der Lee, Eds., Earth's Deep Water Cycle, 168, p. 1-

708	11, Geophysical Monograph Series, American Geophysical Union, Washingtion, D.C.
709	Smyth, J.R., Holl, C.M., Frost, D.J. and Jacobsen, S.D. (2004) High pressure crystal chemistry of
710	hydrous ringwoodite and water in the Earth's interior. Physics of the Earth and Planetary
711	Interiors, 143-144, 271-278.
712	Stachl, T. (2001) Diamonds from the asthensosphere and the transition zone. European Journal
713	of Mineralogy, 13, 883-892.
714	Thomas, SM., Bina, C.R., Jacobsen, S.D. and Goncharov, A.F. (2012) Radiative heat transfer
715	in a hydrous mantle transition zone. Earth and Planetary Science Letters, 357-358, 130-
716	136.
717	Tsuchiya, J. and Tsuchiya, T. (2009) First principles investigation of the structural and elastic
718	properties of hydrous wadsleyite under pressure. Journal of Geophysical Research, 114,
719	B02206.
720	Vinograd, V.L., Winkler, B., Putnis, A., Kroll, H., Milman, V., Gale, J.D. and Fabrichnaya, O.B.
721	(2006) Thermodynamics of pyrope-majorite, Mg ₃ Al ₂ Si ₃ O ₁₂ -Mg ₄ Si ₄ O ₁₂ , solid solution
722	from atomistic model calculations. Molecular Simulation, 32, 85-99.
723	Walker, A.M., Demouchy, S. and Wright, K. (2006) Computer modelling of the energies and
724	vibrational properties of hydroxyl groups in alpha- and beta-Mg ₂ SiO ₄ . European Journal
725	of Mineralogy, 18, 529-543.
726	Wang, Z., Wang, H., and Cates, M.E. (2001) Effective elastic properties of solid clays.
727	Geophysics, 66, 428-440.
728	Wang, J., Sinogeikin, S.V., Inoue, T. and Bass, J.D. (2003) Elastic properties of hydrous
729	ringwoodite. American Mineralogist, 88, 1608-1611.
730	Weidner, D.J., and Carleton, H.R. (1977) Elasticity of coesite. Journal of Geophysical Research,

- 731 82, 1334-1346.
- Williams, Q. and Hemley, R.J. (2001) Hydrogen in the deep earth. Annual Review of Earth and
 Planetary Sciences, 29, 365-418.
- 734 Withers, A.C., Wood, B.J. and Carroll, M.R. (1998) The OH content of pyrope at high pressure.
- 735 Chemical Geology, 147, 161-171.
- 736 Wright, K. (2006) Atomistic models of OH defects in nominally anhydrous minerals. Water in
- 737 Nominally Anhydrous Minerals, In H. Keppler and J.R. Smyth, Eds., Water in Nominally
- Anhydrous Minerals, 62, p. 67-83, Reviews in Mineralogy and Geochemistry,
- 739 Mineralogical Society of America, Chantilly, Virginia.
- 740 Wright, K. and Catlow, C.R.A. (1994) A computer simulation study of (OH) defects in
- olivine. Physics and Chemistry of Minerals, 20, 515-518.
- 742 Wright, K., Freer, R. and Catlow, C.R.A. (1994) The energetics and structure of the
- hydrogarnet defect in grossular: a computer simulation study. Physics and Chemistry ofMinerals, 20, 500-503.
- Xia, X., Weidner, D.J., and Zhao, H. (1998) Equation of state of brucite: single-crystal Brillouin
 spectroscopy study and polycrystalline pressure-volume-temperature measurement.
 American Mineralogist, 83, 68-74.
- Xu, L., Mei, S., Dixon, N., Jin, Z., Suzuki, A.M. and Kohlstedt, D.L. (2013) Effect of water on
- rheological properties of garnet at high temperatures and pressures. Earth and PlanetaryScience Letters, 379, 158-165.
- 751 Yagi, T., Uchiyama, Y., Akaogi, M., and Ito., E. (1992) Isothermal compression curve of
- 752 MgSiO₃ tetragonal garnet. Physics of the Earth and Planetary Interiors, 74, 1-7.
- Zhang, F. and Wright, K. (2010) Coupled (H^+, M^{3+}) substitutions in forsterite. Geochimica et

754 Cosmochimica Acta, 74, 5958-5965.

- Zhang, F., and Wright, K. (2012) Coupled (Li⁺, Al³⁺) substitutions in hydrous forsterite.
- American Mineralogist, 97, 425-429.
- Zou, Y., Irifune, T., Gréaux, S., Whitaker, M.L., Shinmei, T., Ohfuji, H., Negishi, R., and Higo,
- 758 Y. (2012) Elasticity and sound velocities of polycrystalline $Mg_3Al_2(SiO_4)_3$ garnet up to
- 20 GPa and 1700 K. Journal of Applied Physics, 112, 014910.
- 760

Figure Captions 761

762 **Figure 1.** Crystal structure of defect-free MgSiO₃ tetragonal garnet optimized using force fields. The two octahedral sites are occupied by Si (pink) and Mg (blue). Mg atoms (light 763 blue) occupy two unique interstitial sites. Three unique tetrahedral sites are occupied by Si (red). 764 765 Figure 2. Enthalpy associated with protonating each oxygen site calculated using the force field approach. 766

Figure 3. OH-defect structures in MgSiO₃ majorite optimized using force fields. 767 Hydrogen atoms are light blue and the oxygen atoms are color-coded according to atomic site 768 where O1=red, O2=light green, O3=dark blue, O4=yellow, O5=dark green, O6=purple. (a) 769 $[V_{Mg2} + 2OH_{05}]^{X}$ (b) $[V_{Mg3} + 2OH_{05}]^{X}$ (c) $[V_{Si4} + 2OH_{02} + 2OH_{03}]^{X}$ (d) "Hydrogarnet"-type $[V_{Si2}$ 770 $+40H_{06}]^{X}$. 771

Figure 4. Enthalpies of reactions 6 (Al-free) and 7 ($Al_2O_3 = 0.4$ wt%) calculated as a 772 773 function of pressure using the force field approach. Negative values of the enthalpy correspond to the hydrogarnet defect being favored. 774

Figure 5. Calculated enthalpies (reactions 8 and 9) using force fields for hydrogen 775 776 incorporation via (a) Mg and (b) Si vacancies in the presence of a coupled-substitution of Al for ^{IV}Si or ^{VI}Si and ^{VI}Mg as a function of pressure. Open symbols represent calculations using a 2 x 777 2 x 2 supercell, and the filled symbols represent calculations using the conventional tetragonal 778 779 unit cell.

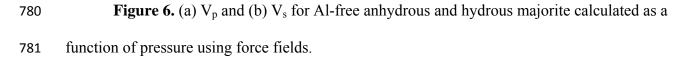


Figure 7. The force field calculated majorite $dln V_s/dln V_p$ due to compositional changes 782 resulting from OH incorporation compared to experimental and computational results for the 783

784	olivine polymorphs (Li et al., 2011). The results from this study are shown by red squares ([V_{Mg3}
785	$([V_{Si2} + 4OH_{O6}]^{X}, C_{water} = 1400 \text{ ppm}), \text{ blue triangles } ([V_{Si2} + 4OH_{O6}]^{X}, C_{water} = 1400 \text{ ppm}), \text{ light blue},$
786	open squares $(V_{\text{Si2}} + 4\text{OH}_{\text{O6}}]^X$, $C_{water} = 1.13 \text{ wt\%}$ and light blue triangles $(V_{\text{Si2}} + 4\text{OH}_{\text{O6}}]^X$, C_{water}
787	= 1.13 wt%, C_{Al2O3} = 3.2 wt%). Experimental results (filled black symbols) for forsterite
788	(square) (Mao et al. 2010), wadsleyite (triangle) (Mao et al. 2008), and ringwoodite (circle)
789	(Inoue et al. 1998; Wang et al. 2003) are shown. Additional computational results (black open
790	symbols and dashed lines) are also shown for forsterite (triangles) (Tsuchiya and Tsuchiya
791	2009), wadsleyite (circles) (Liu et al. 2009), and ringwoodite (squares and dashed line without
792	symbols) (Panero 2010; Li et al. 2009), respectively. For comparison, the thermal $d\ln V_s/d\ln V_p$
793	for ringwoodite (Li et al. 2011) is shown by the orange dotted line.

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Tables

Species	<i>q</i> (e)		
Mg(core)	1.7		
Si(core)	3.4		
Al(core)	2.55		
O(core)	0.746527		
O(shell)	-2.446527		
O _H (core) ^a	-1.2		
H(core)	0.35		
Interaction			
Buckingham	A (eV)	ρ (Å)	$C (\mathrm{eV} \cdot \mathrm{\AA}^6)$
Mg(core) – O (shell)	1432.8544	0.277265	0.0
Si(core) – O (shell)	1073.4668	0.298398	0.0
Al(core) – O (shell)	1262.2081	0.28637	0.0
$Mg(core) - O_H(core)$	1015.8587	0.277265	0.0
$Si(core) - O_H(core)$	761.06168	0.298398	0.0
$Al(core) - O_H(core)$	894.87465	0.28637	0.0
O(shell) – O(shell)	598.8996	0.314947	26.89746
$O(shell) - O_H(core)$	598.8996	0.314947	26.89746
$O_{\rm H}$ (core) – $O_{\rm H}$ (core)	598.8996	0.314947	26.89746
H(core) – O(shell)	191.6667	0.25	0.0
$H(core) - O_H(core)$	191.6667	0.25	0.0
Morse	$D_e ({ m eV})$	a (Å ⁻¹)	r_{0} (Å)
$H(core) - O_H(core)$	7.0525	2.1986	0.94285
Spring	$k_2 (\mathrm{eV/\AA^2})$	$k_4 ({\rm eV}/{\rm \AA}^4)$	
O(core) – O(shell)	56.5598	10000.0	
Three-body	$k_{\theta} (\mathrm{eV/rad}^2)$	θ (degrees)	
$O - {}^{IV}Si - O$	0.77664	109.47	
$O - {}^{VI}Si - O$	2.2955	90.0	
$O - {}^{IV}Al - O$	1.2883	109.47	
O - VIAI - O	1.8807	90.0	

Table 1. Interatomic potential parameters and ionic charges.

10/29

798 Table 2. Calculated structural parameters for tetragonal MgSiO₃ majorite compared to

Cell parameters	XRD ^a	<i>SLEC</i> This Study	% difference	$SLEC^{b}$	DFT-GGA This Study	DFT-GGA ^b
		P = 0	GPa			
<i>a</i> (Å)	11.501(1)	11.506	0.04	11.494	11.638	11.670
<i>c</i> (Å)	11.480(2)	11.416	-0.56	11.392	11.528	11.561
c/a	0.9982(2)	0.9922	-0.60	0.9912	0.9905	0.9907
$V(\text{\AA}^3)$	1518.6(4)	1511.27	-0.48	1505.04	1561.34	1574.47
		P = 10	GPa			
a (Å)	11.315	11.307	-0.07	_	_	_
<i>c</i> (Å)	11.214	11.211	-0.03	_	_	_
c/a	0.9911	0.9915	0.04	_	_	_
$V(\text{\AA}^3)$	1435.7	1433.33	-0.17	_	_	_
		P = 20	GPa			
<i>a</i> (Å)	_	11.144	_	_	11.251	_
<i>c</i> (Å)	_	11.048	_	_	11.115	_
c/a	_	0.9913	_	_	0.9879	_
$V(\text{\AA}^3)$	_	1372.05	_	_	1407.06	_

799	published	experimental	and com	putational data.
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^aAmbient condition (Angel et al. 1989) and P = 9.72 GPa experiments (Yagi et al. 1992) and ; ^bCASTEP (Vinograd et al. 2006)

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801 Table 3. Elastic constants, bulk (K_s) and shear (μ) moduli of tetragonal majorite garnet

802 (MgSiO₃).

Elastic	Experimental	SLEC This study	<i>SLEC</i> ^b
constants	(GPa)	(GPa)	(GPa)
	P = 0 GPa		
C_{11}	^a 286.4(13)	296.52	295.10
C_{33}	^a 280.1(18)	296.14	-
C_{44}	^a 85.0(7)	86.05	85.23
C_{66}	^a 93.2(11)	94.14	93.66
C_{12}	^a 83.0(29)	112.5	112.7
C_{23}	^a 104.9(24)	102.42	-
C_{16}	^a 1.4(13)	14.30	14.72
	P = 10 GPa		
C_{11}	_	347.04	-
C_{33}	-	350.51	-
C_{44}	_	92.99	_
C_{66}	-	103.66	-
C_{12}	-	141.27	-
C_{23}	-	132.47	-
C_{16}	-	21.55	-
	P = 20 GPa		
C_{11}	-	392.16	-
C_{33}	-	398.69	-
C_{44}	-	97.96	-
C_{66}	_	109.86	-
C_{12}	_	170.97	-
C_{23}	-	164.06	-
C_{16}	-	26.36	-
tropic properties			
	P = 0 GPa		
$K_{ m s}$	^a 159.8(44), ^c 167.3(33) ^d 164.4(5),	169.3	170.14
	^e 170(5), ^f 166(3) ^g 166(5), ^h 164(4)		
μ	^a 89.7(6), ^c 88.3(18), ^d 94.9(2)	90.8	-
	^e 89(1), ^f 85(2), ^g 88(2), ^h 87(2)		
	P = 10 GPa		
$K_{ m s}$	^b 210(4)	206.3	-
μ	^b 103(2)	99.4	-
	P = 20 GPa		
$K_{ m s}$	-	242.4	-
μ	_	105.3	-

^aAmbient condition experiments, Mj_{100} (Pacalo and Weidner 1997); ^bVinograd et al. (2006); ^c Mj_{100} (Gwamnesia et al. 1998); ^dpyrolite minus olivine composition (Irifune et al. 2008); ^e Mj_{50} Py₅₀ (Liu et al. 2000); ^f Mj_{100} (Sinogeikin

and Bass 2002); ${}^{g}Mj_{100}$ (Sinogeikin et al. 1997a); ^hnatural Catherwood meteorite sample (Sinogeikin et al. 1997b)

Table 4. Calculated vacancy formation energy and crystalline lattice energies from force fields

807 implemented in GULP.

Defect	Formation Enthalpy (eV)		
Unbound vacancies	0 GPa	25 GPa	
$V_{\rm Mg1}$ "	18.89	19.50	
V_{Mg2}	18.77	19.38	
V _{Mg3} "	19.43	20.26	
V _{Si1} ""	76.61	78.89	
V _{Si2} ""	70.07	71.95	
V _{Si3} ""	73.39	75.84	
V _{Si4} ""	72.56	74.36	
V _{O1}	17.06	16.78	
V ₀₂	16.69	16.92	
V_{O3}	15.93	15.56	
V_{O4}	15.96	15.54	
V ₀₅	15.95	15.56	
$V_{\rm O6}$	17.08	17.31	
Bound vacancies	- ,		
$[V_{\rm Mg1} + V_{\rm O1}]^{\rm x}$	35.86	36.34	
$[V_{\rm Mg1} + V_{\rm O2}]^{\rm x}$	35.44	36.32	
$[V_{\rm Mg1} + V_{\rm O3}]^{\rm x}$	34.97	34.99	
$[V_{\rm Mg1} + V_{\rm O4}]^{\rm x}$	35.87	35.03	
$\left[V_{\rm Mg1} + V_{\rm O5}\right]^{\rm x}$	34.90	35.01	
$[V_{\rm Mg1} + V_{\rm O6}]^{\rm x}$	36.15	37.07	
$[V_{Mg2} + V_{O1}]^{x}$	35.20	35.24	
$\left[V_{\rm Mg2} + V_{\rm O2}\right]^{\rm x}$	35.04	35.24	
$[V_{Mg2} + V_{O5}]^{x}$	34.66	34.68	
$[V_{Mg2} + V_{O6}]^{x}$	35.47	36.59	
$[V_{Mg3} + V_{O1}]^{x}$	35.69	35.88	
$[V_{Mg3} + V_{O4}]^{x}$	36.40	34.81	
$[V_{Mg3} + V_{O5}]^{x}$	34.67	35.04	
Phase	2	55.01	
MgO	-30.18	-27.44	
α-Quartz	-95.35	-	
Stishovite	-	-91.06	

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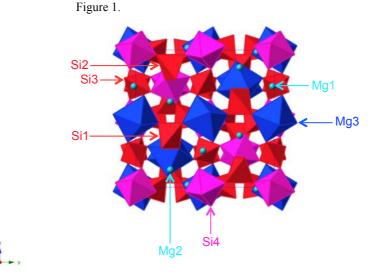
Table 5. Enthalpies calculated from first principles at the DFT-GGA level of theory.

	0 GPa	20 GPa
	Enthalpy (eV)	
MgO ^a	-12.01	-9.71
SiO ₂ , α-quart z^a	-23.98	_
SiO ₂ , stishovite ^a	_	-20.55
Majorite ^b	-1147.67	-963.27
Defe	ect Formation Enthalpy (eV/	H)
M_{Mg3} + 2(OH _{O5})	-0.51	-0.62
$V_{\rm Si2}^{\rm H} + 4(\rm OH_{\rm O6})$	-1.37	-1.16
	Reaction enthalpy (eV/H)	
Reaction 6	-0.85	-0.82
1		

810 ^a1 formula unit; ^bFull unit cell (8 formula units)

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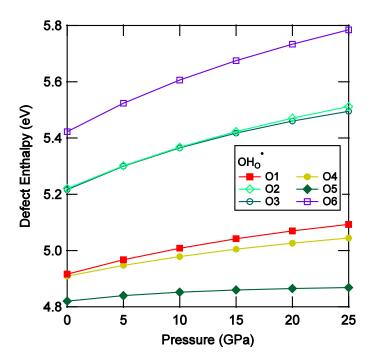
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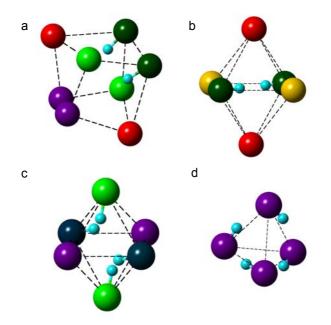
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Figure 2.



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Figure 3.



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Figure 4.

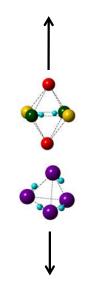


Figure 5a.

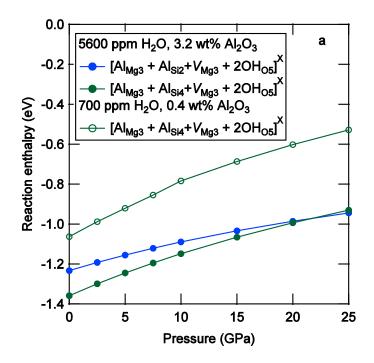


Figure 5b

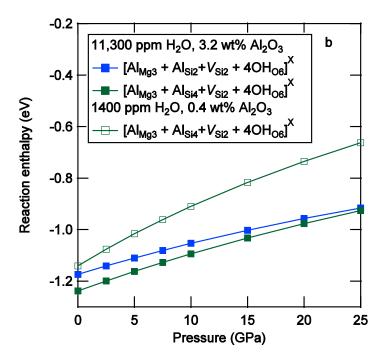


Figure 6a.

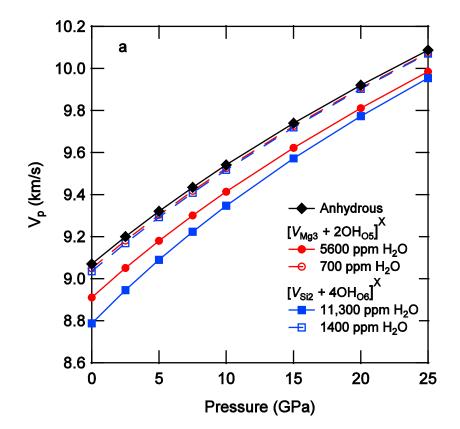


Figure 6b.

