

1 **REVISION 1**

2
3 **Petalite under Pressure: Elastic Behavior and Phase Stability**

4
5 **Nancy L. Ross,^{1*} Jing Zhao,¹ Carla Slebodnick,² Elinor C. Spencer,¹ and Bryan C.**
6 **Chakoumakos³**

7
8 ^{1,2} Depts. of Geosciences¹ and Chemistry², Virginia Tech, Blacksburg, VA 24061, USA

9 ³ Quantum Condensed Matter Division, Oak Ridge National Laboratory, P.O. Box 2008

10 MS-6393, Oak Ridge, TN 37831-6393, USA

11
12 **Abstract**

13
14 The lithium aluminosilicate mineral petalite (LiAlSi₄O₁₀) has been studied using high-
15 pressure single-crystal X-ray diffraction (HP-XRD) up to 5 GPa. Petalite undergoes two
16 fully reversible pressure-induced first-order phase transitions, not previously reported in
17 the literature, at *ca.* 1.5 and 2.5 GPa. The first of these transforms the low-pressure α -
18 phase of petalite (*P2/c*) to an intermediate β' -phase that then fully converts to the high-
19 pressure β -phase at *ca.* 2.5 GPa. The $\alpha \rightarrow \beta$ transition is isomorphic and is associated
20 with tripling of the unit cell volume. Analysis of the HP-XRD data show that although
21 the fundamental features of the petalite structure are retained through this transition, there
22 are subtle alterations in the internal structure of the silicate double-layers in the β -phase
23 relative to the α -phase. Measurement of the unit cell parameters of petalite as a function
24 of pressure, and fitting of the data with 3rd order Birch-Murnaghan equations of state, has
25 provided revised elastic constants for petalite. The bulk moduli of the α and β -phases are
26 49(1) and 35(3) GPa, respectively. These values indicate that the compressibility of the- α
27 phase of petalite lies between the alkali feldspars and alkali feldspathoids, whereas the β -
28 phase has a compressibility more comparable with layered silicates. Structure analysis

29 has shown that the compression of the α -phase is facilitated by the rigid body movement
30 of the Si_2O_7 units from which the silicate double-layers are constructed.

31
32 **Keywords:** Petalite, high-Pressure, single-crystal X-ray diffraction, equation of state,
33 phase transition

34

35

36

37

Introduction

38

39 The lithium aluminosilicate mineral petalite is one of the three most abundant naturally
40 occurring lithium-rich minerals, and is of fundamental relevance in the evaluation of
41 conditions associated with magmatic pegmatite crystallization processes. The crystal
42 chemistry of the low-pressure α -phase of petalite has been the subject of extensive study
43 (Černý & London, 1983 and references therein).

44 The petalite structure can be described as a 3-dimensional $\text{AlSi}_4\text{O}_{10}$ framework
45 consisting of puckered double-sheets of corner sharing SiO_4 tetrahedra stacked parallel to
46 the (100) plane with corner-sharing AlO_4 tetrahedra that bridge neighboring layers (Fig.
47 1). The neutrality of the structure is ensured by the presence of lithium cations residing
48 within channels that propagate through the structure in the [101] direction. The Li
49 cations are bonded to four oxygen atoms and the resulting LiO_4 polyhedra possess
50 geometries that are intermediate between those of an idealized tetrahedron and a perfect
51 square planar arrangement. Both spectroscopic and diffraction studies have shown that all
52 cation sites within naturally occurring specimens of petalite are fully ordered (Černý &
53 London, 1983; Tagai et al., 1982) and our data concur with this finding.

54 The structure of petalite was originally reported in the non-standard $P2/a$ setting of
55 space group $P2/c$ (Tagai et al., 1982). However, for the high pressure X-ray diffraction

56 (HP XRD) analysis discussed in this contribution we have chosen to represent, for
57 consistency and ease of scrutiny, all petalite phases in a standard $P2/c$ setting. The
58 crystallographic basis of this $P2/c$ setting (\mathbf{a} , \mathbf{b} , and \mathbf{c}) is related to that of the original
59 $P2/a$ setting (\mathbf{a}' , \mathbf{b}' , and \mathbf{c}') by the following expressions: $\mathbf{a} = -\mathbf{a}' - \mathbf{c}'$; $\mathbf{b} = \mathbf{b}'$; and \mathbf{c}
60 $= \mathbf{a}'$. The following description of the α -phase is consistent with the structure in the
61 standard $P2/c$ format. It should be noted, however, that a non-conventional metric unit
62 cell has been chosen to ensure that the structural features align with the unit cell axes.

63 Although there are several reported studies of the relative thermodynamic stability
64 and phase equilibria of the $\text{NaAlSiO}_4\text{-LiAlSiO}_4\text{-SiO}_2\text{-H}_2\text{O}$ system (Fasshauer et al., 1998;
65 London, 1984; Haussühl et. al., 2012), of which petalite is a key member, there is a lack
66 of accurate high pressure structural and elasticity data for petalite. The objective of this
67 study was to rectify this situation, and herein we report an extensive HP-XRD analysis of
68 petalite and describe in detail a previously undiscovered high-pressure phase of this
69 mineral (β -phase). Furthermore, we have collected precise unit cell data as a function of
70 pressure, and these have enabled us to determine accurate elastic constants for both the
71 low and high-pressure phases of petalite.

72 73 **Experimental Details** 74

75 Two HP-XRD experiments were performed with colorless petalite sourced from the
76 Araçuaí pegmatite district, Jequitinhonha Valley, Minas Gerais, Brazil. The first of these
77 conducted with sample 1 allowed for collection of highly accurate and precise unit cell
78 parameters as a function of pressure. These data were employed in the calculation of the
79 elastic constants of α and β -phases. The second petalite crystal (sample 2) was larger than

80 sample 1 and was used for the measurement of diffraction data for structural analysis.

81 The following experimental details apply to both crystals unless stated otherwise.

82 A single crystal of petalite (sample 1: $140 \times 160 \times 25 \mu\text{m}^3$, sample 2:
83 $176 \times 313 \times 30 \mu\text{m}^3$) was loaded in to an ETH diamond anvil cell (DAC) (Miletich et al.,
84 2000) fitted with diamonds with culets $600 \mu\text{m}$ (sample 1) or $650 \mu\text{m}$ (sample 2) in
85 diameter. The sample chamber was a cavity drilled in a stainless-steel gasket that was
86 fitted within the DAC, and had dimensions of $300 \times 90 \mu\text{m}^2$ (sample 1) or $400 \times 90 \mu\text{m}^2$
87 (sample 2). In the case of sample 1 a quartz crystal ($60 \times 80 \times 30 \mu\text{m}^3$) was included in the
88 DAC for pressure calibration measurements (Angel et al., 1997). For the experiment with
89 sample 2, a ruby ball was added to the DAC to act as the pressure calibrant (Mao et al.,
90 1978). After initial unit cell determinations at ambient pressure, a 4:1 MeOH:EtOH
91 solvent mixture was added to the DAC to act as the pressure transmitting medium; this
92 particular alcohol mixture is known to remain hydrostatic up to 9.8 GPa (Angel et al.,
93 2007).

94 Precise unit cell parameters were determined with a Huber diffractometer equipped
95 with an Eulerian cradle and point detector. The instrument was controlled with the
96 SINGLE software (Angel and Finger, 2011). The method employed for the determination
97 of the unit cell parameters was based on the 8-position centering of the sample reflections
98 (King Jr. and Finger, 1979). High-pressure unit cell data for petalite sample 1 were
99 collected over 0–4.5 GPa. When the pressure was raised to *ca.* 5 GPa the crystal
100 disintegrated, possibly due to a phase transition, and the experiment was terminated.

101 HP-XRD data for structure determinations were collected with sample 2 at room
102 temperature on an Oxford Diffraction Xcalibur II (α -phase data collections) or Xcalibur I

103 (β -phase data collection) instrument with monochromated Mo- K_{α} radiation
104 ($\lambda = 0.71073 \text{ \AA}$); these diffractometers are equipped with a point and charge-coupled
105 device (CCD) detectors, respectively. Data were processed with standard instrument
106 software (Agilent Technologies, 2012). Absorption corrections were applied with the
107 ABSORB (Angel, 2005) program, and the data corrected for DAC dips and other
108 statistical anomalies with AVERAGE. All structure solutions and refinements were
109 performed with Olex2 (Dolomanov et al., 2009). The structures of all phases of petalite
110 were solved directly from the high-pressure CCD data by direct methods. Structural
111 refinements were performed on F^2 by full-matrix least-squares refinement techniques.
112 Due to the limited data obtained from the HP-XRD data collections no anisotropic
113 parameters were refined for any of the structural models. Two of the SiO₄ tetrahedra in
114 the structural model of the β -phase were found to be disordered and were modeled
115 accordingly. It was not possible to refine the relative occupancies of the two components
116 of the disorder models so they were fixed to be 50%, and the U_{iso} values of the atoms
117 were fixed to be equal. Where necessary Si–O bond length constraints were applied to the
118 disordered components. Not surprisingly the thermal parameters for the Li⁺ ions did not
119 refine to reasonable values. To overcome this issue the U_{iso} values of the two symmetry
120 independent Li⁺ ions were constrained to be equal. Table 1 summaries the key
121 crystallographic refinement parameters obtained in this study. HP-XRD data in CIF
122 format for the α -phase [at room pressure, and at 0.32(5), 0.56(5), 0.89(5), and
123 1.25(5) GPa] and the β -phase [at 2.71(5) GPa] have been deposited with the American
124 Mineralogist Crystal Structure Database.

125
126

Results and Discussion

Elastic Constants

Figure 2 shows the evolution of the petalite unit cell volume with increasing pressure and Table 2 lists the unit cell parameters of petalite as a function of pressure. A graphical representation of these data and an F_E vs. f_E plot are provided in Figures 3 and 4, respectively. The P - V data show the occurrence of two reversible pressure-induced phase transitions, the first at *ca.* 1.5 GPa and the second at *ca.* 2.5 GPa. These transitions are first order in nature, and proceed in the order: α -phase \rightarrow β' -phase \rightarrow β -phase, where the β' -phase is an intermediate phase (see section 3.2.2). The overall consequence of the $\alpha \rightarrow \beta$ transition is a tripling of the unit cell volume; this is most obvious in the CCD images of the two phases (Fig. 5) in which superlattice reflections are present at $\mathbf{q} = \frac{1}{3}\mathbf{c}^*$ in the diffraction pattern of the β -phase.

The P - V data for both the α and β -phases have been fitted, by a least-squares technique, with 3rd order Birch-Murnaghan (BM) equations of state (EoS) (Angel, EOS-FIT). These fits allow for the elucidation of the elastic constants of these two phases, and these are presented in Table 3. However, attention must be given to the estimated standard deviation (esd) values reported with these constants, in particular those for the β -phase, as these are perhaps larger than ideal – this is a consequence of the limited number of available data points to which the EoS functions are fitted. Nonetheless, these constants are notably more accurate and appropriate than those reported by Fasshauer et al. (1998). These authors evaluated the elastic constants for petalite from synchrotron data, yet they did not account for the occurrence of the pressure induced phase transitions and ‘cycled’ the pressure on the sample, thus forcing the

152 crystalline sample to pass through these transitions multiple times. It is therefore not
153 surprising that their reported values for the elastic constants of petalite (Table 3) differ
154 from those determined in this study. However, our experimentally determined value of K_0
155 for the α -phase of petalite is in excellent agreement with value reported by Haussühl et al.
156 (2012), 49(1) GPa, that was derived from density functional theory (DFT) calculations
157 based on elastic stiffness coefficients determined by resonant ultrasound spectroscopy
158 (RUS) measurements conducted under ambient conditions (*i.e.* with α -phase petalite
159 samples). Yet, these authors also reported DFT calculations of the petalite unit cell
160 volume as a function of pressure (up to 30 GPa) that also failed to identify the
161 $\alpha \rightarrow \beta' \rightarrow \beta$ phase transitions.

162 Table 4 lists elastic constants for selected tetrahedral framework minerals and layered
163 silicates for comparison with petalite. It is apparent that the bulk modulus of the α -phase
164 of petalite is slightly more compressible than the alkali feldspars and slightly less
165 compressible than the alkali feldspathoids. In contrast, the bulk modulus of the β -phase of
166 petalite is more akin to those of quartz and the archetypical layered silicate talc in which
167 the SiO_4 layers are not pillared in the third dimension by either AlO_4 or AlO_6 polyhedra,
168 and with pyrophyllite that comprises stacked aluminosilicate layers that are also not
169 covalently linked *via* bridging polyhedra. This would suggest that the presence of the
170 AlO_4 tetrahedra that interconnect the SiO_4 double sheets (Fig. 1) has a minimal impact on
171 the ability of the petalite framework to withstand pressure.

172 It would be constructive to quantify the compressibilities (β_i) of the three
173 crystallographic axes from the unit cell length *vs.* pressure data for petalite (Fig. 3). For
174 an orthogonal unit cell ($\alpha = \beta = \gamma = 90^\circ$) a reasonable approximation of a β_i value can be

175 obtained by fitting the axis length vs. pressure data with an appropriate BM EoS and from
176 the axial bulk modulus (K_i) β_i can be estimated with the equation $\beta_i = (3K_i)^{-1}$. However,
177 this approximation assumes that the strain tensor is restricted, by symmetry, from
178 rotating. Yet, in the case of a monoclinic system one of the three unit cell angles is free to
179 change, thus the requisite symmetry constraints for this approximation are violated.
180 Indeed, to evaluate the axial compressibilities for a non-orthogonal unit cell it is
181 necessary to calculate the full strain tensor, yet due to the limited number of data points
182 available for α and β -phases of petalite such calculations are not feasible.

183

184 **High pressure structural analysis**

185

186 **α -phase compression mechanism.** To aid in the interpretation of the structural

187 changes experienced by the α -phase in response to pressure, it is beneficial to first

188 ascertain the degree of distortion exhibited by the polyhedra comprising the petalite

189 framework. Such distortion of the individual cation tetrahedra can be estimated from the

190 tetrahedral angular variance (σ_{tet}) and quadratic elongation ($\langle\lambda_{tet}\rangle$) parameters (Robinson

191 et al., 1971). These distortion parameters for the AlO_4 , SiO_4 , and LiO_4 polyhedra within

192 the α -phase of petalite are listed in Table 5 as a function of pressure. Also included in this

193 table are the volumes of the polyhedra (V_{poly}) and the center-to-vertex distance (l_0) for a

194 geometrically ideal tetrahedron ($\sigma_{tet} = 0$, $\langle\lambda_{tet}\rangle = 1$) with a volume equal to that of the

195 distorted polyhedron. It is evident that after an initial adjustment to the applied pressure

196 the nearly geometrically ideal SiO_4 tetrahedra remain unaltered with increasing pressure;

197 this finding is also reflected in the lack of statistically significant pressure-induced

198 changes in the bond lengths and angles associated with these tetrahedra (Table 6).

199 Consequently, the SiO_4 tetrahedra can be treated as rigid units, at least over the pressure

200 range investigated (< 5 GPa). Unlike the SiO_4 tetrahedra, the AlO_4 tetrahedra are greatly
201 distorted, but the σ_{tet} values for this unit are suggestive, but not conclusive, of an overall
202 small reduction in the degree of distortion of these polyhedra with increasing pressure.

203 A rigid unit approximation cannot be extended to the LiO_4 units. These polyhedra are
204 best considered as possessing geometries that are intermediate between those of an
205 idealized tetrahedron ($\sigma_{\text{tet}} = 0$) and a perfect square planar arrangement ($\sigma_{\text{tet}} = 47.886$).
206 The variation in the elongation parameter, $\langle \lambda_{\text{tet}} \rangle$, of the LiO_4 polyhedra with pressure is
207 negligible, indicating that there is virtually no change with pressure in the deviation of
208 the Li–O bond lengths from their optimum length (l_0) at that specific pressure. This
209 implies that any pressure-induced distortions of the LiO_4 polyhedra must be facilitated by
210 adjustments in the O–Li–O angles rather than by disproportionate changes in the Li–O
211 bond lengths. This conclusion is further supported by the decrease in the σ_{tet} parameter
212 with increasing pressure that signifies a reduction in angular distortion of the LiO_4 unit as
213 it tends towards a more regular tetrahedral arrangement with increasing pressure.

214 As discussed in section 3.1, the bulk modulus of the α -phase is similar to that of
215 silicate minerals composed of either silicate or aluminosilicate layers that are not
216 covalently linked in the third dimension. This result would suggest that the AlO_4
217 tetrahedra play a minor role in the compression mechanism of this phase. Consequently,
218 one must expect, perhaps counter-intuitively, that compression of the structure is enabled
219 by changes within the silicate double-layers. Further support for this hypothesis is
220 provided by the percentage decreases in the unit cell axes over the 0–1.5 GPa range:
221 $\sim 0.9\%$ (a -axis), $\sim 1.6\%$ (b -axis), and $\sim 1.4\%$ (c -axis). These values indicate that

222 compression within the silicate layers parallel to the (100) plane is favored over
223 compression in the [100] direction that lies $\sim 51^\circ$ from the a^* -axis.

224 To aid in the evaluation of the pressure response of the α -phase, the structure of the
225 silicate double-layers can be simplified by applying the rigid unit approximation to the
226 SiO_4 tetrahedra. Furthermore, as oxygen atom O3 resides on an inversion centre (2*d*) the
227 compressional mechanism must not incorporate any change in the $\text{Si1-O3-Si1}^{\text{viii}}$ bond
228 angle, or rotation of the connected (Si1) O_4 tetrahedra relative to each other. This second
229 symmetry constraint also applies to the connected (Si2) O_4 tetrahedra because the
230 bridging oxygen atom O5 is located on a 2-fold axis (2*f*). Fortuitously, although there are
231 no symmetry restrictions on the $\text{Si2-O5-Si2}^{\text{ix}}$ bond angle, there is no statistically relevant
232 change in this angle with pressure (Table 6). Consequently the Si_2O_7 units, which are
233 shown as light grey and purple in Figure 6, may also be treated as rigid entities. Therefore
234 the compression mechanism must be due primarily to tilting and/or rotation of these
235 Si_2O_7 units relative to each other.

236 The ‘pivot points’ for these possible motions are atoms O1, O2, O4 and O6, thus to
237 evaluate the behavior of the structure it is necessary to assess changes to the bond angles
238 involving these atoms (Table 6). The $\text{O1}\cdots\text{O4}\cdots\text{O2}^{\text{i}}$ and $\text{O4}\cdots\text{O2}^{\text{i}}\cdots\text{O1}^{\text{i}}$ angles represent
239 the hinges for the corner sharing Si_2O_7 units, and they increase and decrease with
240 increasing pressure, respectively (Table 6). Moreover, the $\text{Si1}^{\text{i}}\text{-O2}^{\text{i}}\text{-Si2}$ (symmetry
241 equivalent to the $\text{Si1-O2-Si2}^{\text{vii}}$ angle in Table 6) and Si1-O4-Si2 angles decrease with
242 increasing pressure. It is the concerted changes in these angles with increasing pressure
243 that allows for contraction of the structure along the crystallographic b -axis. The
244 concomitant opening of the Si2-O6-Al1 (symmetry equivalent angle $\text{Si2}^{\text{ix}}\text{-O6}^{\text{ix}}\text{-Al1}^{\text{x}}$

245 shown in Fig. 6) hinge permits compression along the c -axis and an overall reduction in
246 the β -angle.

247 The ultimate consequence that can be envisaged as a result of these concerted hinge
248 motions is movement of Si_2O_7 units relative to each other such that there is subtle
249 lessening in the corrugation of the double-layers. This in turn will result in a small
250 decrease in the length of the a -axis in response to pressure, exactly as observed in the
251 experimental data (Fig. 3).

252 Unfortunately, the estimated standard deviation values associated with the bond
253 lengths and angles involving the Li^+ ion are too high to allow for a conclusive
254 determination of the mechanism that causes a reduction in the LiO_4 polyhedral distortion
255 with increasing pressure. However, the data do suggest that the principal driving force for
256 the decrease in distortion is facilitated by the movement of the $(\text{Si}_2)_2\text{O}_7$ units, as
257 evidenced by the decrease in the $\text{Si}_2\text{--O}_6\text{--Li}_1$ angle with increasing pressure and the
258 absence of changes in the $\text{Li}_1\text{--O}_1\text{--Si}_1$ angles.

259
260 **Crystal structure of the β -phase.** At *ca.* 1.5 GPa the compression mechanism for the
261 α -phase reaches a limiting point and the crystal undergoes a first-order phase transition to
262 an immediate phase denoted herein as the β' -phase. The quality of the diffraction data for
263 this phase precluded determination of its crystal structure, but it is likely to be a
264 composite phase comprising structural features associated with both the α and β -phases,
265 but given the unit cell parameters for this phase it is probably most akin to the structure
266 of the β -phase, and may possibly be an incommensurate phase. At *ca.* 2.5 GPa the crystal
267 fully converts to the β -phase.

268 Given that the compression mechanism of the α -phase is enabled by the rigid motion
269 of the Si_2O_7 units, one may reasonably expect that once this mechanism reaches its
270 limiting point that the subsequent phase transition would incorporate an increase in the
271 conformational freedom of these units, perhaps *via* breaking of the inversion and 2-fold
272 symmetries of the $(\text{Si}1)_2\text{O}_7$ and $(\text{Si}2)_2\text{O}_7$ units. Therefore, the expected candidate space
273 groups for the β -phase would be the monoclinic translationengleiche subgroups (*t*
274 subgroups) of $P2/c$, $P2$ and Pc . Yet, the klassengleiche index (*k*-index) for this first-order
275 transition equals three and this precludes the β -phase belonging to a *t* subgroup of $P2/c$.
276 In fact, the $\alpha \rightarrow \beta$ transition is isomorphic with only $\frac{2}{3}$ of the Si_2O_7 units exhibiting a
277 reduction in symmetry *i.e.* tilting/rotation of the SiO_4 units relative to each other (Fig.
278 7a).

279 Unfortunately, because of the disorder exhibited by two of the six symmetry
280 independent SiO_4 tetrahedra, which also impact the geometries of the AlO_4 and LiO_4
281 polyhedra, a comparative analysis of the tetrahedral distortion parameters for the cation
282 polyhedra would be redundant. Furthermore, a detailed discussion of the variations in the
283 construction of the four unique Si_2O_7 units (color coded in Fig. 7) is also of questionable
284 value. However, we can assess the broader structural differences between the two petalite
285 phases. The framework of the β -phase comprises structural features that are essentially
286 analogous to those observed in the crystal structure of the α -phase (Fig. 1), namely
287 silicate double layers pillared by AlO_4 tetrahedra. Yet, there are significant adaptations to
288 the internal structure of the silicate layers in the β -phase caused by the distortion in $\frac{2}{3}$ of
289 the Si_2O_7 units. An overlay of the crystal structures of the α - and β -phases (Fig. 8) shows
290 that the major consequence of this internal rearrangement of the silicate layers is the

291 creation of two types of interlayer channels (denoted A and B in Fig. 8) with dimensions
292 notably different from the channels in the α -phase that are all symmetry related. At
293 1.25(5) GPa the cross-sections of the channels in the α -phase are *ca.* $3.24 \times 4.01 \text{ \AA}^2$; for
294 the β -phase at 2.71(5) GPa the A channels are *ca.* $2.61 \times 4.14 \text{ \AA}^2$ and the cross-sections of
295 the B channels are *ca.* $4.42 \times 2.64 \text{ \AA}^2$. These cross-sectional dimensions are only
296 approximations, but they do show that by converting the dimensions of the channels
297 during the phase transition the petalite structure is able to accommodate contraction along
298 the [001] direction. This transition is also accompanied by a small reduction in the
299 interlayer distance of *ca.* 0.2 \AA . However, there do not appear to be any significant
300 differences in the coordination environments of the Li cations in the two phases.

301

302
303
304

Implications

305 This high-pressure single-crystal XRD study of petalite has revealed, for the first time,
306 that petalite undergoes two first-order phase transitions within the 0–4.5 GPa pressure
307 range. The transformation of the low-pressure α -phase to the high-pressure β -phase
308 proceeds via an intermediate phase, β' -phase, of unknown structure. The α and β -phases
309 are structurally similar although there are small differences in the construction of the
310 silicate double-layers. The compression mechanism of the α -phase has also been
311 elucidated and it has been shown that the rigid body movement of the Si_2O_7 units
312 comprising the silicate double-layers is responsible for the compression of the structure.
313 It is of note that these modifications within the silicate layers lead to a reduction in the
314 distortion of the LiO_4 polyhedra with increasing pressure. This is also one of the first

315 studies that provides details of how Li in 4-fold coordination with oxygen responds to
316 pressure.

317 The bulk moduli of the α - and β -phases are 49(1) and 35(3) GPa, respectively,
318 showing that the high-pressure phase (β) is more compressible than the low-pressure
319 phase (α). The bulk modulus for α is slightly lower than those reported for tetrahedral
320 frameworks such as the alkali feldspars and slightly greater than those reported for alkali
321 feldspathoids. The lower bulk modulus of the β -phase, however, is closer in magnitude to
322 values reported for layered silicates such as talc and pyrophyllite. The results of this
323 study therefore enhance our understanding of the effect of composition and mechanisms
324 that control the compression of tetrahedral framework structures.

325

326

327

328

Acknowledgments

329 N.L.R., E.C.S, and J.Z. gratefully acknowledge support for this work from the National
330 Science Foundation through grant EAR-1118691 and support from the College of
331 Science at Virginia Tech. The XCalibur2 instrument employed in this study was
332 purchased through the NSF grant CHE-0131128. Research conducted at Oak Ridge
333 National Laboratory was sponsored by the Scientific User Facilities Division, Office of
334 Basic Energy Sciences, U.S. Department of Energy.

335

336

337

References

338

339 Agilent Technologies: Data collection and processing software, CrysAlisPro (version

340 171.36), Agilent Technologies (2012).

341 Angel, R. J.: All EoS fits to the data presented herein were performed with EOS-FIT

342 (version 5.2), which is available at www.rossangel.net.

343 Angel R. J. (2005) Absorption corrections for diamond-anvil pressure cells implemented

344 in the software package Absorb6.0. *Journal of Applied Crystallography*, 37, 486-492.

345 Angel R. J., and Finger, L. W. (2011) SINGLE: a program to control single-crystal

346 diffractometers. *Journal of Applied Crystallography*, 44, 247–251.

347 Angel, R. J., Bujak, M., Zhao, J., Gatta, G.D., and Jacobsen, S. D. (2007) Effective

348 hydrostatic limits of pressure media for high-pressure crystallographic studies.

349 *Journal of Applied Crystallography*, 40, 26–32.

350 Angel, R. J., Allan, D. R., Miletich, R., and Finger, L. W. (1997) The use of quartz as an

351 internal pressure standard in high-pressure crystallography. *Journal of Applied*

352 *Crystallography*, 30, 461–466.

353 Benusa, M., Angel, R.J., Ross, N.L. (2005) Compression of albite, $\text{NaAlSi}_3\text{O}_8$.

354 *American Mineralogist*, 90, 1115-1120.

355 Černý, P., London, D. (1983) Crystal chemistry and stability of petalite. *Tschermaks*

356 *Mineralogische und Petrographische Mitteilungen*, 31, 81–96.

357 Dolomanov, O. V., Bourhis, L. J., Gildea, R. J., Howard, J. A. K., and Puschmann, H.

358 (2009) OLEX2: a complete structure solution , refinement and analysis program.

359 *Journal of Applied Crystallography*, 42, 339–341.

- 360 Fasshauer, D.W., Chatterjee, N. D., and Cemic, L. (1998) A thermodynamic analysis of
361 the system $\text{NaAlSiO}_4\text{-LiAlSiO}_4\text{-SiO}_2\text{-H}_2\text{O}$ system based on new heat capacity,
362 thermal expansion, and compressibility data for selected phases. Contributions to
363 Mineralogy and Petrology, 133, 186–198.
- 364 Gatta, G.D., and Angel, R.J. (2007) Elastic behavior and pressure-induced structural
365 evolution of nepheline: Implications for the nature of the modulated superstructure.
366 American Mineralogist, 92, 1446-1455.
- 367 Gatta, G.D., Rotiroti, N., Boffa Ballaran, T., and Pavese, A. (2008) Leucite at high
368 pressure: Elastic behavior, phase stability, and petrological implications. American
369 Mineralogist, 93, 1588-1596.
- 370 Haussühl, E., Schreuer, J., Winkler, B., Haussühl, S., Bayarjargal, L., and Milman,
371 V.(2012) Structure-property relations and thermodynamic properties of monoclinic
372 petalite, $\text{LiAlSi}_4\text{O}_{10}$. Journal of Physics: Condensed Matter, 24, 345402.
- 373 King Jr., H. E., and Finger, L. W. (1979) Diffracted beam crystal centering and its
374 application to high-pressure crystallography. Journal of Applied Crystallography, 12,
375 374–378.
- 376 London, D. (1984) Experimental phase equilibria in the $\text{LiAlSiO}_4\text{-SiO}_2\text{-H}_2\text{O}$: a
377 petrogenetic grid for lithium-rich pegmatites. American Mineralogy, 69, 995–1004.
- 378 Mao, H. K., Bell, P. M., Shaner, J. W., and Steinberg, D. J. (1978) Specific volume
379 measurements of Cu, Mo, Pd, and Ag and calibration of the ruby R_1 fluorescence
380 pressure gauge from 0.06 to 1 Mbar. J. Applied Physics, 49, 3276–3283.

- 381 McCarthy, A. C., Downs, R. T., and Thompson, R. M. (2008) Compressibility trends of
382 the clinopyroxenes, and in-situ high-pressure single-crystal X-ray diffraction study of
383 jadite. *American Mineralogy*, 93, 198–209.
- 384 Miletich, R., Allan, D. R., and Kuhs, W. F. (2000) High-Temperature and High-Pressure
385 Crystal Chemistry, Mineralogical Society of America Geochemical Society (Vol.41),
386 R. M. Hazen and R. T. Downs (Eds.), pg. 445–519.
- 387 Pawley, A. R., Clark, S. M., and Chinnery, N. J. (2002) Equation of state measurements
388 of chlorite, pyrophyllite, and talc. *American Mineralogy*, 87, 1172–1182.
- 389 Robinson, K., Gibbs, G. V., and Ribbe, P. H. (1971) Quadratic elongation: a quantitative
390 measure of distortion in coordination polyhedra. *Science*, 172, 567–570.
- 391 Tagai, T., Reid, H., Joswig, W., and Korekawa, M. (1981) Kristallographische
392 untersuchungen eines petalits mittels neutronenbeugung und
393 transmissionselektronenmikroskopie. *Zeitschrift für Kristallographie*, 160, 159–170.
394

395

Figure Captions

396

397 **Figure 1.** The crystal structure of the low-pressure α -phase of petalite in the $P2/c$ setting:
398 (a) view along the [010] direction; (b) view along the [001] direction. Light and dark
399 purple tetrahedra represent symmetry independent SiO_4 units, blue tetrahedra are
400 associated with AlO_4 units, and the orange spheres represent Li^+ ions that reside within
401 the cavities of the anionic $\text{AlSi}_4\text{O}_{10}$ framework.

402

403 **Figure 2.** V - P data for petalite: data collected with two different petalite samples are
404 shown as solid (sample 1) and open circles (sample 2). Error bars have been included but
405 are smaller than the symbols. Solid black curves represent 3rd order BM-EoS fits to the
406 V - P data [$w\chi^2 = 0.8215$, α -phase, 0–1.5 GPa; $w\chi^2 = 2.4719$, β -phase, 2.5–4.5 GPa]. The
407 β -phase volume has been divided by three to normalize it with respect to the volume of
408 the α -phase.

409

410 **Figure 3.** Petalite unit cell parameters as a function of pressure: (A) axes lengths [circles:
411 a -axis; squares: b -axis; diamonds: c -axis]; (B) β -angle. The β -phase c -axis length has
412 been divided by three to normalize it with respect to the length of the α -phase c -axis.

413

414 **Figure 4.** F_e vs. f_e plot for petalite calculated from accurate and precise unit cell data
415 determined from eight-position centering of selected sample reflections (see section 3.1
416 in the manuscript).

417

418 **Figure 5.** $0kl$ projections of the HP-XRD data recorded with a CCD detector: (left)
419 α -phase (ambient pressure); (right) β -phase at 2.71(5) GPa.

420

421 **Figure 6.** Section of the silicate double-layer within the structure of the α -phase of
422 petalite showing atom labels. Symmetry codes: (i) $x, 1 + y, z$; (viii) $1 - x, -y, 2 - z$; (ix)
423 $1 - x, y, 3/2 - z$; (x) $x, y, 1 + z$.

424

425 **Figure 7.** The crystal structure of the high-pressure β -phase of petalite in the $P2/c$ setting:
426 (a) view along the [010] direction; (b) view along the [001] direction. Light and dark
427 purple and brown polyhedra represent symmetry independent Si_2O_7 units. Dark blue
428 tetrahedra are AlO_4 units, and orange spheres represent Li^+ cations. For clarity, in the
429 case of disordered SiO_4 units only a single component is shown.

430

431 **Figure 8.** Overlay of the α -phase (light grey) and β -phase (multicoloured) of petalite. The
432 letters A and B denote the two symmetry independent cavities observed in the β -phase;
433 only symmetry equivalent cavities are present in the crystal structure of the α -phase; Li^+
434 cations of this phase have been omitted for clarity. Note: these are exact overlays; no
435 corrections for variations in the unit cell parameters of the two phases have been made.
436 Dotted lines represent outlines of the unit cells. The red and green lines represent the x
437 and y dimensions, respectively, used to measure the cross-sections of the channels.

438

439

440

441

442 **Table 1.** Refinement details for petalite as a function of pressure.

	Pressure (GPa)					
	Ambient	0.32(5)	0.56(5)	0.89(5)	1.25(5)	2.71(5)
Phase	α -phase	α -phase	α -phase	α -phase	α -phase	β -phase
Crystal system	Monoclinic	Monoclinic	Monoclinic	Monoclinic	Monoclinic	Monoclinic
Space group	<i>P2/c</i>	<i>P2/c</i>	<i>P2/c</i>	<i>P2/c</i>	<i>P2/c</i>	<i>P2/c</i>
<i>Z</i>	2	2	2	2	2	6
<i>a</i> (Å)	11.2296(1)	11.2067(4)	11.1895(4)	11.1705(4)	11.1425(4)	10.830(1)
<i>b</i> (Å)	5.1396(3)	5.1228(4)	5.1100(4)	5.0963(4)	5.0723(4)	5.0530(3)
<i>c</i> (Å)	11.7514(5)	11.7160(7)	11.6872(7)	11.6569(7)	11.6092(7)	33.59(2)
β angle (°)	141.312(1)	141.243(2)	141.190(2)	141.134(2)	141.074(2)	140.6648(2)
<i>V</i> (Å ³)	423.95(3)	421.07(4)	418.83(4)	416.41(4)	412.26(4)	1165.2(7)
ρ_{cal} (g cm ⁻³)	2.399	2.416	2.429	2.443	2.467	2.619
Unique reflns. (<i>I</i> > 2 σ <i>I</i>)	398	283	449	451	429	885
R(int)	0.037	0.098	0.043	0.040	0.045	0.111
N ^o parameters	32	32	32	32	32	106
N ^o restraints	0	0	0	0	0	0
GoF	1.193	1.203	1.125	1.171	1.154	1.586
<i>R</i> 1 (<i>I</i> > 2 σ <i>I</i>)	0.0484	0.0456	0.0494	0.0513	0.0593	0.0955
<i>wR</i> 2 (<i>I</i> > 2 σ <i>I</i>)	0.1056	0.0999	0.1133	0.1181	0.1288	0.1748

443

444

445
446
447
448
449
450

Table 2. Unit cell parameters for petalite as a function of pressure. Data are listed in the order in which they were measured. The β -phase c -axis length has been divided by three to normalize it with respect to the length of the α -phase c -axis.

Pressure (GPa)	a -axis (Å)	b -axis (Å)	c -axis (Å)	β angle	Volume (Å ³)
Sample 1					
0.000(7)	11.22860(3)	5.1385(1)	11.7486(2)	141.311(3)	423.74(4)
0.343(6)	11.20328(9)	5.1194(2)	11.7096(5)	141.239(3)	420.47(5)
0.355(7)	11.20553(4)	5.11908(9)	11.7091(2)	141.240(3)	420.50(4)
0.670(7)	11.18278(7)	5.1023(1)	11.6730(3)	141.171(4)	417.60(5)
1.041(7)	11.1547(1)	5.0822(9)	11.6290(2)	141.094(3)	414.06(4)
1.472(7)	11.12857(9)	5.0556(1)	11.5803(3)	141.076(4)	409.35(5)
2.038(8)	10.9432(2)	5.0512(2)	11.3745(3)	140.836(4)	397.08(5)
2.639(8)	10.8334(6)	5.0444(2)	11.1830(3)	140.738(4)	386.77(6)
3.33(1)	10.7221(4)	5.0348(2)	11.0256(4)	140.512(6)	378.49(4)
3.782(9)	10.6409(2)	5.0346(2)	10.9077(4)	140.302(5)	373.25(6)
4.35(1)	10.5284(2)	5.0346(2)	10.7402(4)	139.992(6)	366.00(7)
Sample 2					
0.00	11.2296(1)	5.1396(3)	11.7514(5)	141.312(1)	423.96(5)
0.32(5)	11.2067(2)	5.1228(4)	11.7160(7)	141.243(3)	421.07(7)
0.56(5)	11.1895(2)	5.1100(5)	11.6872(7)	141.190(3)	418.83(7)
0.89(5)	11.1705(3)	5.0963(4)	11.6569(8)	141.134(3)	416.41(8)
1.25(5)	11.1425(2)	5.0723(5)	11.6092(9)	141.074(3)	412.26(9)
2.07(5)	10.9342(1)	5.0507(4)	11.3647(7)	140.816(3)	396.54(7)
2.21(5)	10.9301(2)	5.0504(4)	11.3588(6)	140.809(3)	396.22(7)
2.59(5)	10.9028(3)	5.0472(4)	11.3240(7)	140.772(3)	394.082(7)
1.39(5)	11.1379(1)	5.0661(3)	11.5978(5)	141.076(1)	411.16(5)
1.69(5)	10.98981(7)	5.0571(2)	11.4321(4)	140.897(1)	400.73(4)
1.91(5)	10.93681(7)	5.0511(3)	11.3659(6)	140.826(1)	396.62(5)
2.09(5)	10.9332(2)	5.0510(6)	11.361(1)	140.825(3)	396.3(1)

451
452

453 **Table 3.** Experimentally Determined Elastic Constants for the α and β -phases of petalite.
 454

Parameter	α-phase	β-phase	Fasshauer et al.[†]
K_0 (GPa)	49(1)	35(3)	33
K'	-6(1)	0.0(6)	0.1
K'' (GPa ⁻¹)	-2.07	-0.45	-

455 [†]Fasshauer et al. (1998). No esd values were reported for these values.
 456

457 **Table 4.** Equation of state parameters of other minerals for comparison with petalite.
 458

Mineral	Formula	K_0 (GPa)	K' / K'' (GPa ⁻¹)	Reference
Albite	NaAl ₃ SiO ₈	52.3(9)	8.8(6)/-2.8(2)	Benusa et al. (2005)
Microcline	KAlSi ₃ O ₈	58.7(7)	3.8(5)/-0.95(17)	Ross (personal comm.)
Leucite (tetragonal)	KAlSi ₂ O ₆	41.9(6)	4 (fixed)	Gatta et al. (2008)
Leucite (triclinic)		33.2(5)	4 (fixed)	
Nepheline	NaAlSiO ₄	47.32(26)	2.77(24)/0.758(79)	Gatta and Angel (2007)
Pyrophyllite	Al ₂ Si ₄ O ₁₀ (OH) ₂	37(3)	10(1)	McCarthy et al. (2008)
Talc	Mg ₃ Si ₄ O ₁₀ (OH) ₂	41(4)	6(2)	Pawley et al. (2002)
Quartz	SiO ₂	37.12(4)	5.99(4)	Angel et al. (1997)

459
 460
 461

462
463

Table 5. Distortion parameters for polyhedra in the α -phase of petalite.

Parameter	Pressure (GPa)					
	Ambient	0.32(5)	0.56(5)	0.89(5)	1.25(5)	
Si1	σ_{tet} ($^{\circ}$)	1.336	1.589	1.499	1.491	1.381
	V_{poly} (\AA^3)	2.139	2.142	2.145	2.126	2.123
	l_0 (\AA)	1.609	1.610	1.611	1.606	1.605
	$\langle \lambda_{tet} \rangle$	1.001	1.000	1.001	1.001	1.001
Si2	σ_{tet} ($^{\circ}$)	1.344	1.726	1.540	1.556	1.667
	V_{poly} (\AA^3)	2.115	2.114	2.116	2.112	2.097
	l_0 (\AA)	1.603	1.603	1.604	1.603	1.599
	$\langle \lambda_{tet} \rangle$	1.001	1.001	1.000	1.000	1.001
Al1	σ_{tet} ($^{\circ}$)	9.134	9.457	9.424	9.342	9.211
	V_{poly} (\AA^3)	2.553	2.546	2.525	2.552	2.538
	l_0 (\AA)	1.707	1.706	1.701	1.707	1.704
	$\langle \lambda_{tet} \rangle$	1.021	1.022	1.022	1.022	1.021
Li1	σ_{tet} ($^{\circ}$)	20.235	19.982	19.961	19.535	19.273
	V_{poly} (\AA^3)	3.251	3.195	3.173	3.184	3.159
	l_0 (\AA)	1.851	1.840	1.835	1.838	1.833
	$\langle \lambda_{tet} \rangle$	1.100	1.097	1.098	1.093	1.091

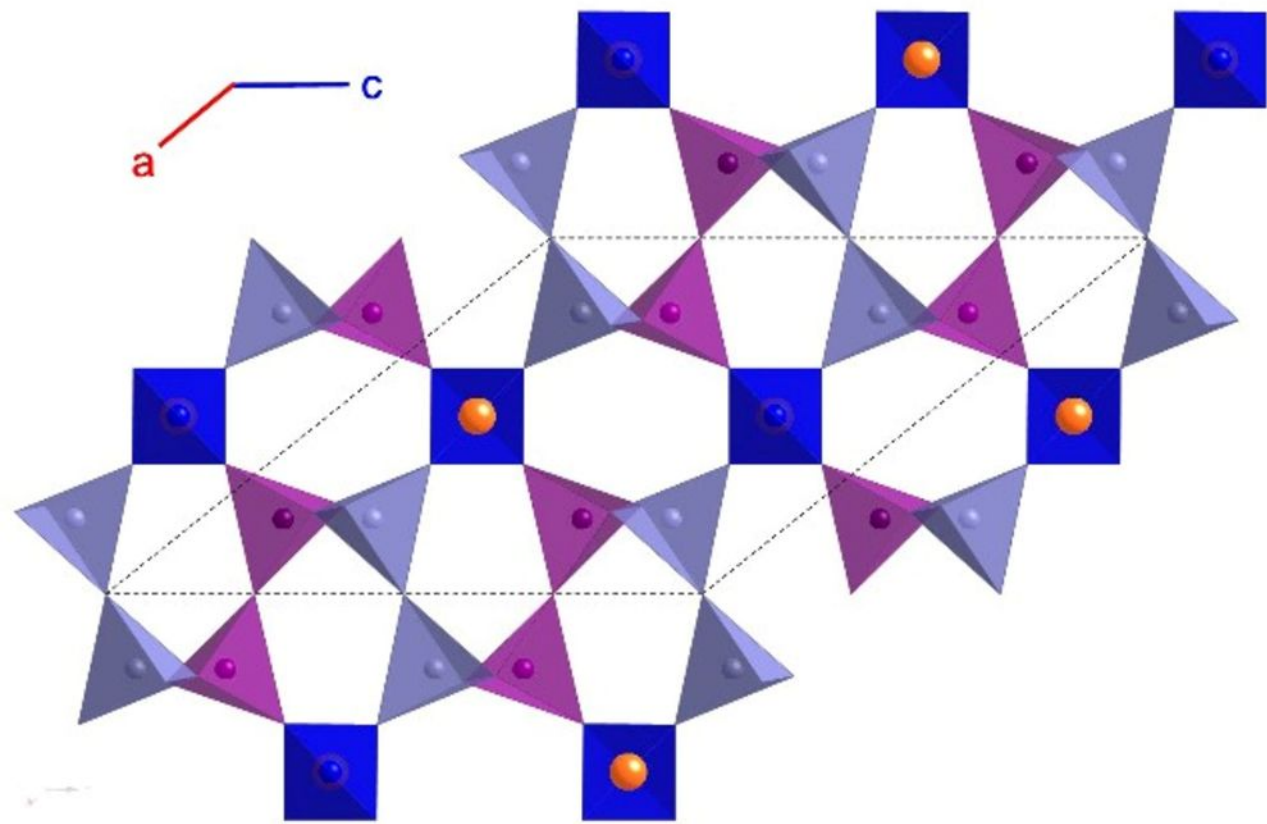
464
465
466
467
468
469
470
471
472
473
474
475
476
477
478
479
480
481
482
483
484
485
486
487
488
489

490 **Table 6.** Selected bond lengths (Å) and angles (°) for the α -phase of petalite as a function
 491 of pressure. Parameters that exhibit statistically significant changes with pressure are
 492 highlighted in grey.

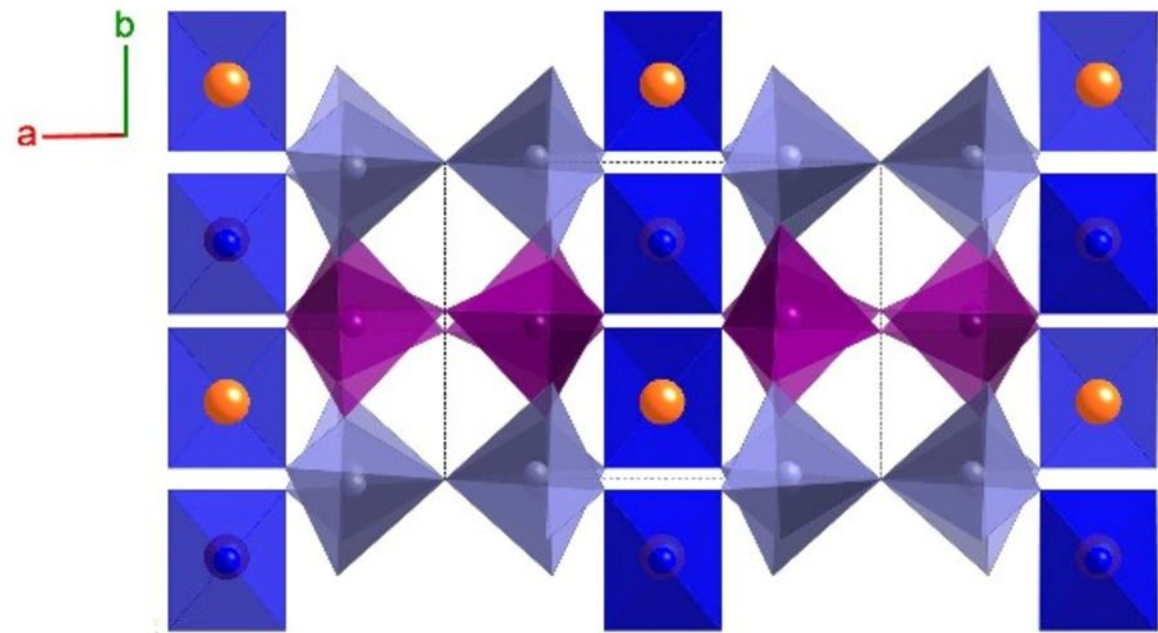
	Pressure (GPa)				
	Ambient	0.32(5)	0.56(5)	0.89(5)	1.25(5)
Si1–O1	1.607(10)	1.605(12)	1.618(11)	1.600(11)	1.599(14)
Si1–O2	1.608(6)	1.619(5)	1.615(5)	1.613(5)	1.614(7)
Si1–O3	1.602(2)	1.601(3)	1.596(2)	1.596(2)	1.591(3)
Si1–O4	1.622(4)	1.616(4)	1.617(4)	1.617(4)	1.619(6)
Si2–O2 ⁱ	1.615(5)	1.607(4)	1.612(4)	1.611(4)	1.611(6)
Si2–O4	1.600(7)	1.608(7)	1.610(7)	1.605(7)	1.596(9)
Si2–O5	1.599(4)	1.594(4)	1.594(4)	1.598(4)	1.597(5)
Si2–O6	1.600(4)	1.606(5)	1.599(4)	1.599(4)	1.594(5)
Al1–O1 ⁱⁱ	1.716(8)	1.717(9)	1.709(8)	1.723(9)	1.718(11)
Al1–O1 ⁱⁱⁱ	1.716(8)	1.717(9)	1.709(8)	1.723(9)	1.718(11)
Al1–O6	1.733(4)	1.732(4)	1.730(4)	1.728(4)	1.725(5)
Al1–O6 ^{iv}	1.733(4)	1.732(4)	1.730(4)	1.728(4)	1.725(5)
Li1–O1 ^v	1.931(12)	1.905(15)	1.913(13)	1.933(14)	1.910(17)
Li1–O1 ^{vi}	1.931(12)	1.905(15)	1.913(13)	1.933(14)	1.910(17)
Li1–O6	1.952(11)	1.949(12)	1.933(11)	1.910(12)	1.919(14)
Li1–O6 ^v	1.952(11)	1.949(12)	1.933(11)	1.910(12)	1.919(14)
Al1…Li1	2.578(14)	2.592(17)	2.559(14)	2.529(16)	2.541(19)
Al1…Li1 ^{vii}	2.562(14)	2.531(17)	2.551(14)	2.568(16)	2.532(19)
O1–Si1–O2	110.9(4)	111.7(4)	111.2(3)	111.3(4)	111.3(4)
O1–Si1–O3	110.97(17)	110.89(19)	110.83(17)	110.75(18)	110.7(2)
O1–Si1–O4	107.7(4)	107.5(4)	107.0(4)	107.1(4)	107.4(5)
O2–Si1–O3	109.2(3)	108.7(3)	109.1(3)	109.1(3)	109.0(4)
O2–Si1–O4	109.7(3)	109.6(3)	109.6(3)	109.7(3)	109.3(4)
O3–Si1–O4	108.3(3)	108.4(3)	109.1(2)	108.9(3)	109.1(3)
O2 ⁱ –Si2–O4	109.9(4)	110.3(4)	109.9(4)	110.3(4)	110.4(5)
O2 ⁱ –Si2–O5	110.6(4)	110.6(4)	110.7(4)	110.4(4)	110.5(5)
O2 ⁱ –Si2–O6	107.6(2)	106.9(2)	107.0(2)	107.2(2)	106.9(3)
O4–Si2–O5	108.0(3)	107.7(3)	108.2(3)	107.9(3)	107.8(4)
O4–Si2–O6	110.7(4)	110.2(4)	110.1(3)	111.1(4)	110.7(5)
O5–Si2–O6	110.1(4)	111.1(5)	110.9(4)	110.0(4)	110.5(6)
O1 ⁱⁱ –Al1–O1 ⁱⁱⁱ	97.8(5)	97.6(5)	97.2(5)	97.7(5)	97.9(6)
O1 ⁱⁱ –Al1–O6	117.3(3)	116.9(3)	117.2(3)	117.6(3)	117.2(4)
O1 ⁱⁱ –Al1–O6 ^{iv}	113.7(3)	114.6(4)	114.2(3)	113.6(4)	113.9(4)
O1 ⁱⁱⁱ –Al1–O6	113.7(3)	114.6(4)	114.2(3)	113.6(4)	113.9(4)
O1 ⁱⁱⁱ –Al1–O6 ^{iv}	117.3(3)	116.9(3)	117.2(3)	117.6(3)	117.2(4)
O6–Al1–O6 ^{iv}	98.4(3)	97.5(3)	98.1(2)	98.0(3)	98.0(3)
O1 ^v –Li1–O1 ^{vi}	84.1(7)	85.4(8)	84.2(7)	84.3(8)	85.4(9)
O1 ^v –Li1–O6	124.9(3)	124.2(3)	124.4(3)	124.6(3)	124.1(3)
O1 ^v –Li1–O6 ^{iv}	121.8(3)	122.2(4)	121.9(3)	121.1(3)	121.2(4)
O1 ^{vi} –Li1–O6	121.8(3)	122.2(4)	121.9(3)	121.1(3)	121.2(4)
O1 ^{vi} –Li1–O6 ^{iv}	124.9(3)	124.2(3)	124.4(3)	124.6(3)	124.1(3)
O6–Li1–O6 ^{iv}	84.5(6)	83.8(7)	85.0(6)	86.1(7)	85.5(8)
Si1–O1–Al1 ⁱⁱ	147.8(4)	148.0(4)	148.1(4)	148.6(4)	149.2(5)
Si1–O2–Si2 ^{viii}	152.1(3)	150.2(3)	149.0(3)	147.8(3)	146.0(4)
Si1–O3–Si1 ^{viii}	180	180	180	180	180
Si1–O4–Si2	148.9(6)	147.8(6)	146.2(6)	145.8(6)	144.9(8)
Si2–O5–Si2 ^{ix}	163.1(5)	162.1(4)	162.1(4)	162.3(5)	161.8(6)
Si2–O6–Al1	145.1(2)	145.3(2)	146.1(2)	146.4(2)	147.1(3)
Si2–O6–Li1	126.0(3)	125.3(4)	125.3(3)	125.4(4)	124.5(5)
Al1–O1 ⁱⁱ –Li1 ^v	89.1(5)	88.5(6)	89.3(5)	89.0(6)	88.4(7)
Al1–O6–Li1	88.6(3)	89.3(4)	88.5(3)	87.9(4)	88.2(4)
Al1–O6 ^v –Li1	88.6(3)	89.3(4)	88.5(3)	87.9(4)	88.2(4)
Li1–O1 ^v –Si1 ^v	123.0(4)	123.4(4)	122.5(4)	122.3(4)	122.3(5)
Li1–O1 ^{vi} –Si1 ^{vi}	123.0(4)	123.4(4)	122.5(4)	122.3(4)	122.3(5)
Li1–O6 ^{vi} –Si2 ^{iv}	126.0(3)	125.3(4)	125.3(3)	125.4(4)	124.5(5)
O1…O4…O2 ⁱ	144.1(4)	145.6(4)	146.5(4)	147.3(5)	148.3(6)
O4…O2 ⁱ …O1 ⁱ	95.7(3)	94.0(3)	93.0(3)	92.3(3)	90.9(4)

Symmetry codes: (i) $x, 1 + y, z$; (ii) $-x, -y, 1 - z$; (iii) $x, -y, z - 1/2$; (iv) $-x, y, 1/2 - z$; (v) $-x, 1 - y, 1 - z$; (vi) $x, 1 - y, z - 1/2$;
 (vii) $x, y - 1, z$; (viii) $1 - x, -y, 2 - z$; (ix) $1 - x, y, 3/2 - z$; (x) $x, y, 1 + z$

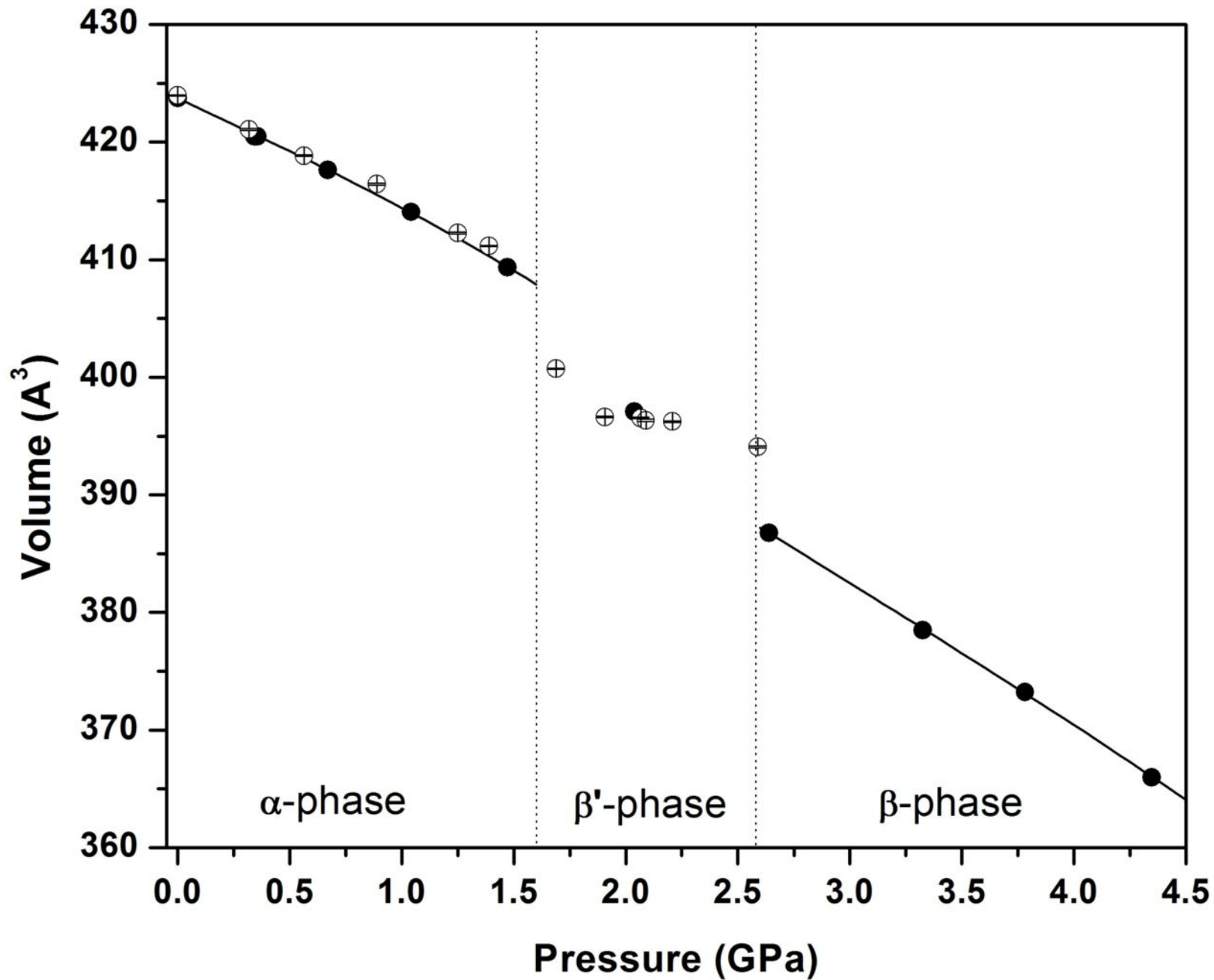
493
494

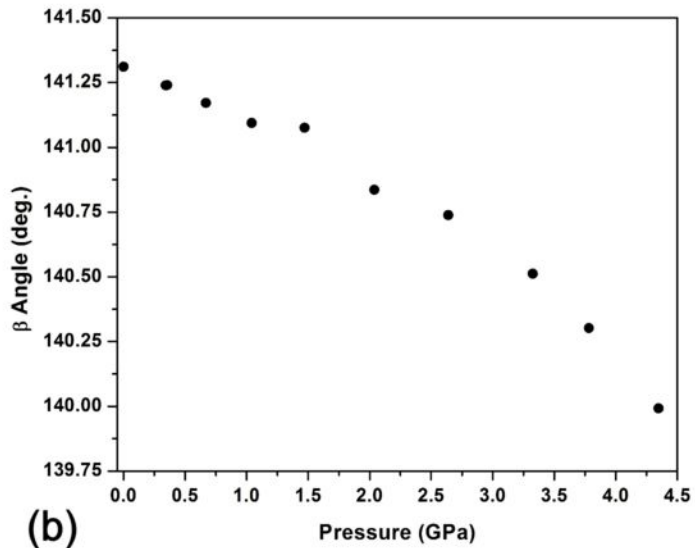
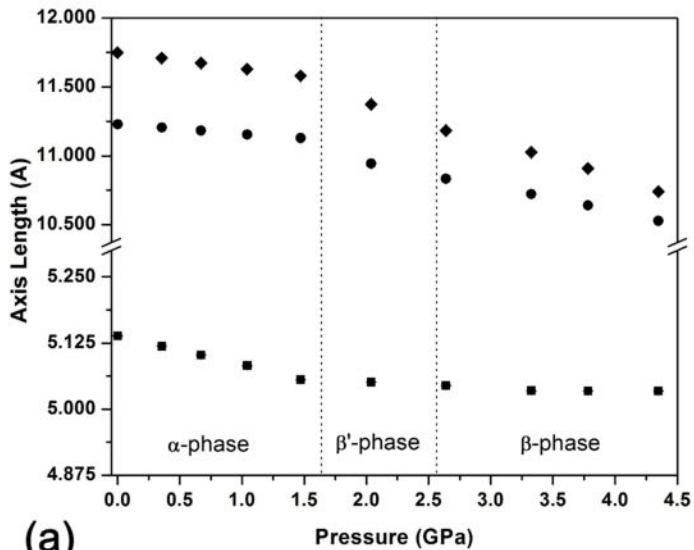


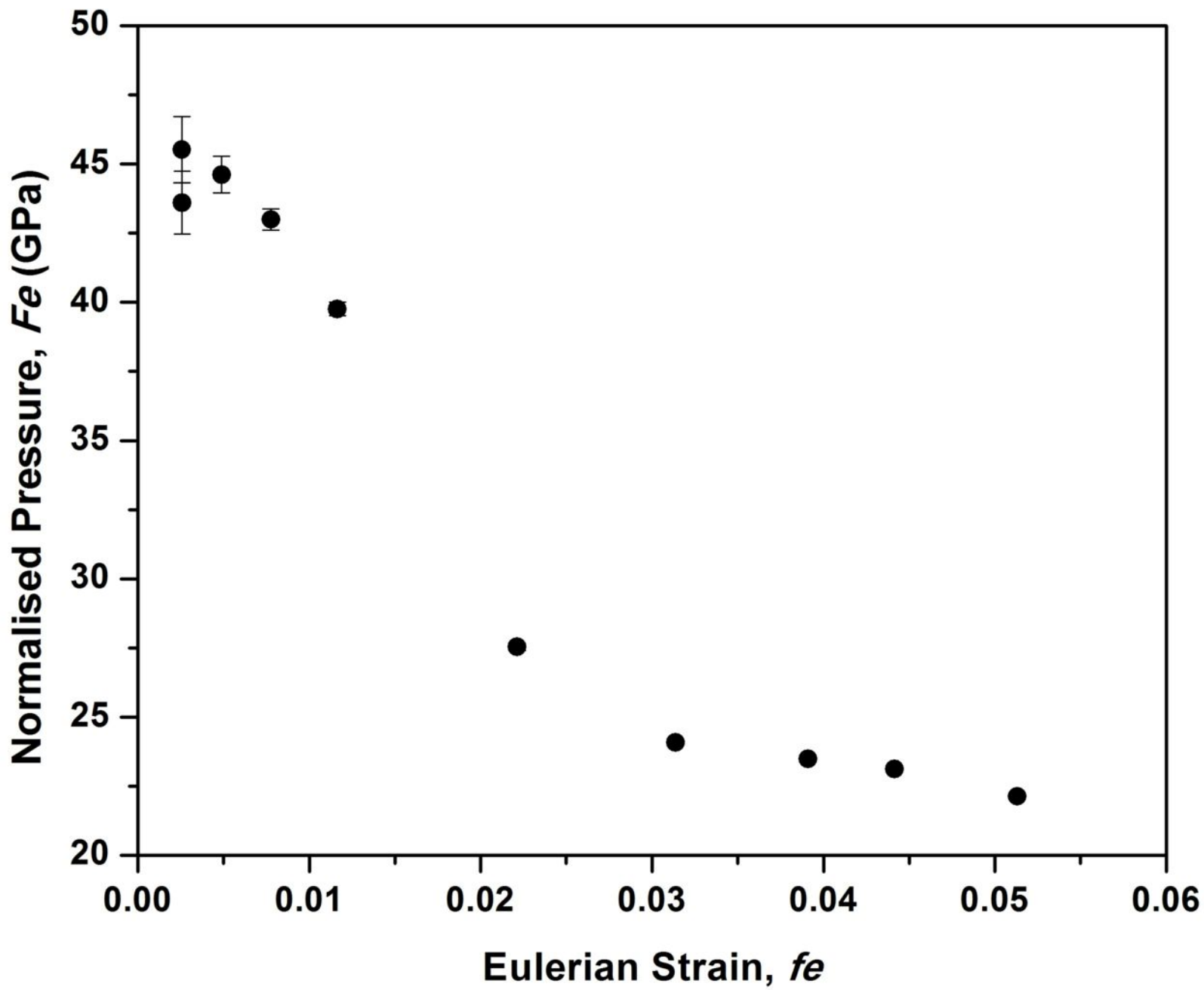
(a)

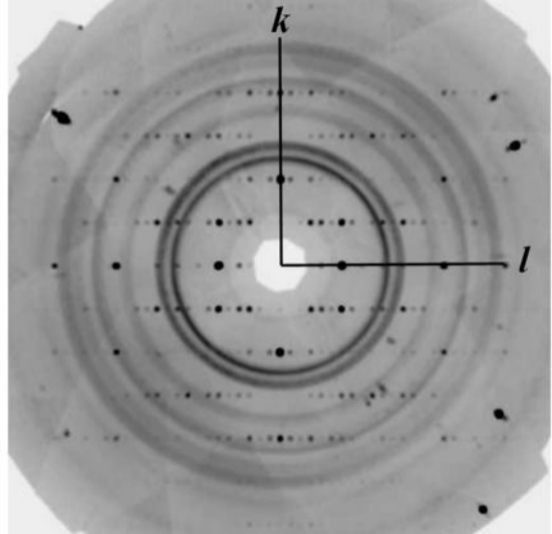
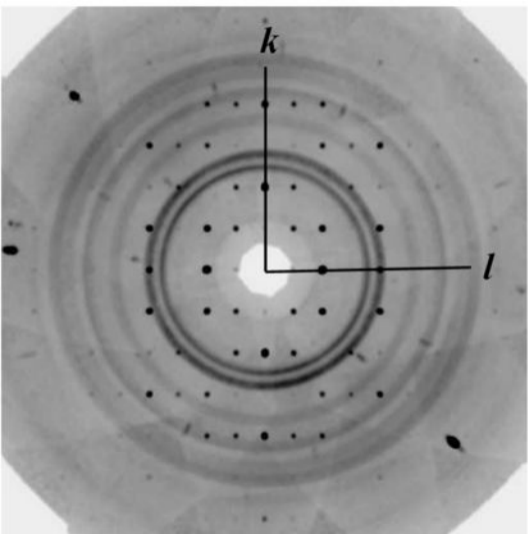


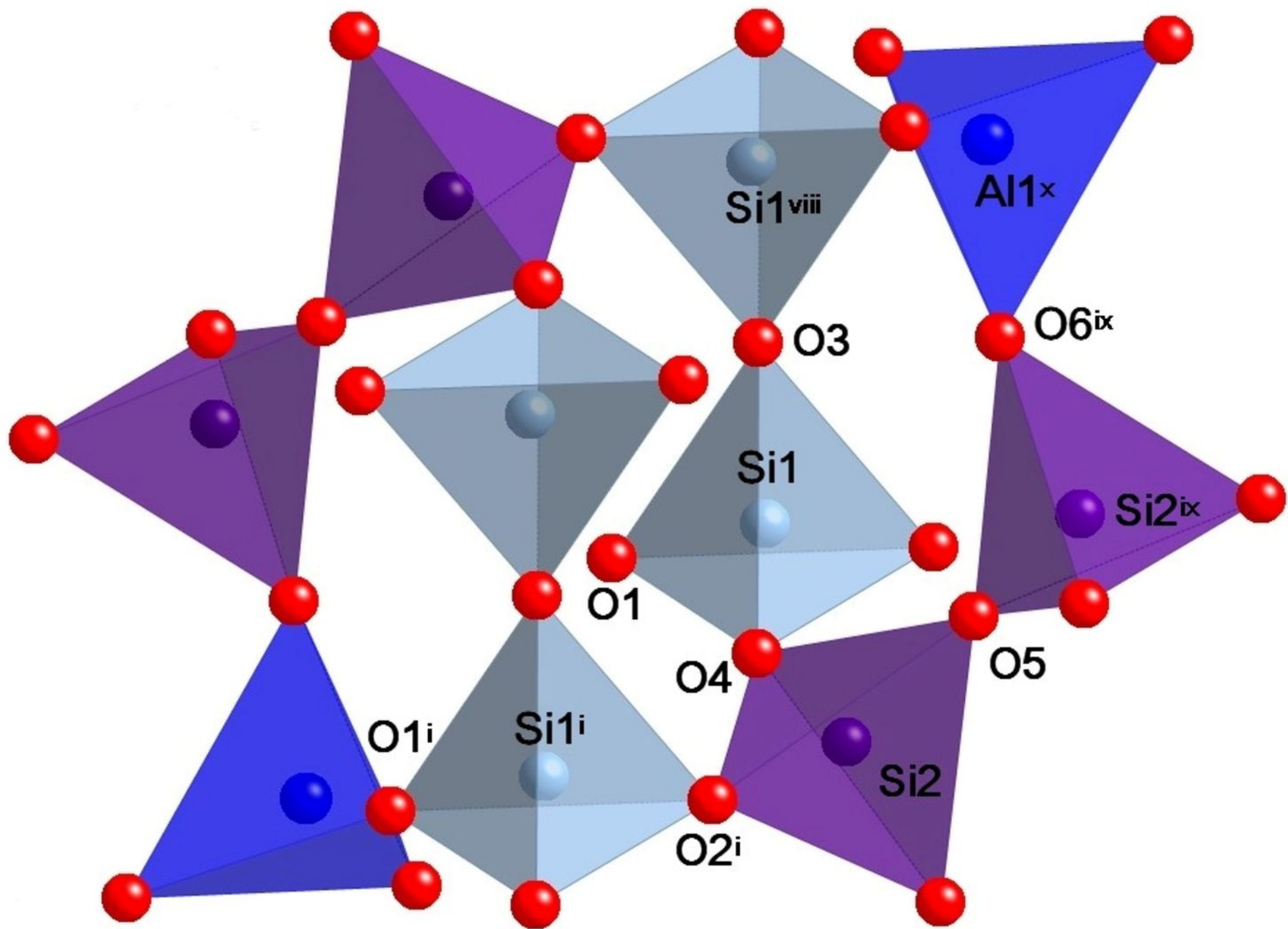
(b)

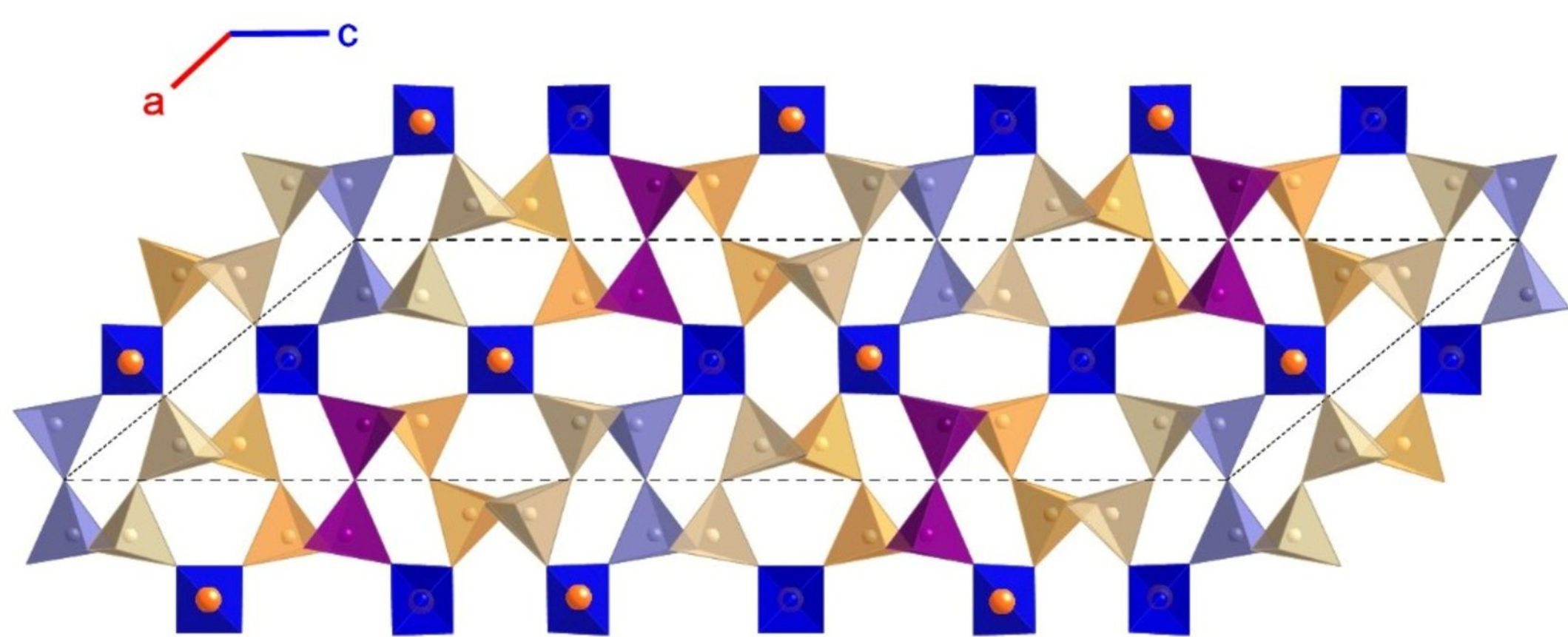




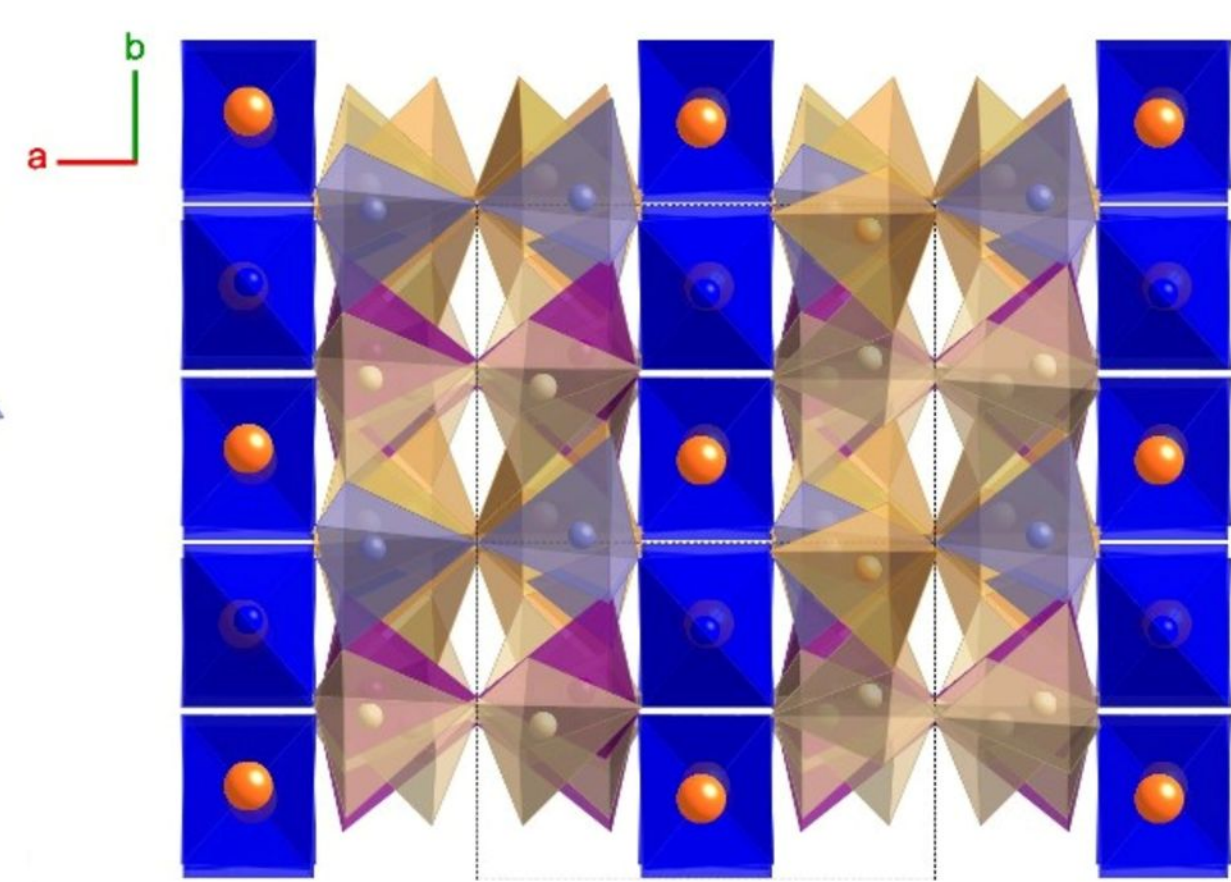








(a)



(b)

