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Revision 1

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5 **Direct observation of Ca-Na ordering and structure polarity in Ca-rich intermediate**
6 **plagioclase feldspar with incommensurate modulated structure**

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19 **Abstract**

20 Ca-Na ordering and structural polarity of subcells in an intermediate plagioclase with modulated
21 structure have been observed using Z-contrast imaging methodology with an aberration-
22 corrected scanning transmission electron microscope. Neighboring lamellar domains with $I1$
23 symmetry are related by inversion twin operation, instead of anti-phase domain boundaries (or,
24 APBs) as in all previously reported structure models. The boundaries between lamellar domains
25 have $I\bar{1}$ symmetry instead of $C\bar{1}$ symmetry. Modulated plagioclase has unique Ca-Na and Al-Si
26 ordering structure that is different from those in end-member structures of anorthite and low
27 albite. The modulated structures of intermediate plagioclase are not metastable structures formed
28 during phase transition, but rather thermodynamically stable structures at low temperature due to
29 Ca-Na ordering within the subcells with $I1$ symmetry.

30

31

32 **Introduction**

33 Although plagioclase feldspars are the most abundant mineral in the earth's crust, their crystal
34 structures and the formation mechanism of modulated structure in intermediate plagioclase have
35 been an enigma for decades beginning with the first discovery of modulated structure in 1940
36 (Chao and Taylor, 1940; Kirkpatrick et al., 1987; McConnell, 2008; Smith and Brown, 1988).
37 Low temperature intermediate plagioclase feldspars (An 25 – An75) display major *a*-reflections
38 ($l=2n$, $h+k=2n$) and extra satellite reflections (*e*- and *f*- reflections) that characterize
39 incommensurate modulated structures, or *e*-plagioclase (Ribbe, 1983; Smith and Brown, 1988).
40 The *e*-reflections are pairs of satellite diffraction spots neighboring *b* reflections ($l=2n+l$,
41 $h+k+l=2n$), although the *b*-reflections do not appear. The *f*-reflections are pairs of weak satellite
42 diffraction spots neighboring *a*-reflections (Ribbe, 1983). Crystal structure models for
43 modulated plagioclase still remain controversial. For example, multiple structure models have
44 been proposed based on the exact same set of experimental data (Horst et al., 1981; Yamamoto,
45 1984). Modulated structure and its formation mechanism affect subsolidus phase relations in
46 intermediate plagioclase feldspars (Carpenter, 1994; Grove et al., 1983; Smith and Brown,
47 1988). It is important to understand crystal structure of modulated structures in intermediate
48 plagioclase. All proposed structure models based on X-ray diffraction and transmission electron
49 microscopic studies can be categorized into two groups:

50 Periodic alternating lamellae with anorthite ($I\bar{1}$) structure in anti-phase
51 relationship with a stacking vector of $\frac{1}{2}c$, or $\frac{1}{2}[\mathbf{a}+\mathbf{b}]$: An...An*...An.... (McConnell,
52 1963; Horst et al., 1981; Wenk and Nakajima, 1980). The symbols An and An* represent
53 plagioclase lamellar domains with anorthite-like structure in anti-phase relationship. The
54 boundaries (APBs) will have $C\bar{1}$ symmetry.

55 Periodic alternating lamellae with anorthite ($I\bar{1}$) and albite ($C\bar{1}$) structures.
56 Anorthite-like lamellae are in anti-phase relationship with albite-like domains at the
57 boundary (i.e., anti-phase domain boundary or, APB) positions:
58 An...Ab...An*...Ab...An... (Grove, 1977; Kumao et al., 1981; Nakajima et al., 1977;
59 Smith and Ribbe, 1969; Yamamoto et al., 1982, 1984). This group of models displays
60 density modulation (or compositional variation along the modulation direction) in
61 addition to the anti-phase relationship.

62 All proposed models are based on anorthite and albite-like subunits. However, Al-Si ordering
63 (like Al occupancy in T10 site) and electron density mapping of Ca-Na atoms indicate that the
64 incommensurate modulated structure is not a mixture of low albite and anorthite subunits based
65 on the average structure of modulated plagioclase feldspars studied to date (Kitamura et al.,
66 1984; Ribbe, 1983; Smith and Brown, 1988; Wenk et al., 1980)..

67

68 **Sample and Experimental Methods**

69 The studied bytownite sample is from an anorthosite in Roosevelt, Kiowa County, Oklahoma.
70 The composition of plagioclase ranges from ~An65 to ~An75 (Powell and Fischer, 1976). A
71 plagioclase crystal with ~An70 was selected for Z-contrast imaging analyses. Composition of
72 the crystal grain was analyzed using X-ray energy-dispersive spectroscopy (EDS) methodology
73 after acquiring Z-contrast images. The k-factors for Na, Ca, and Al, which are required for
74 quantitative EDS analyses of the plagioclase were determined using standards of albite and a
75 synthetic anorthite. The crystal displays homogeneous modulated structure without any
76 exsolution lamellae.

77 Scanning transmission electron microscopy (STEM) analyses were carried out using a FEI Titan
78 80-200 aberration-corrected STEM operated at 200 kV. The microscope is equipped with a
79 CEOS probe aberration corrector, an EDAX high-resolution X-ray energy-dispersive (EDS)
80 detector, and a Gatan image filtering system. All Z-contrast images were acquired using camera
81 length of 160 mm in order to maximize differences among different atoms (Xu et al., 2014). The
82 high-angle annular dark-field (HAADF) STEM imaging (or Z-contrast imaging) is capable of a
83 spatial resolution <0.1 nm using aberration-corrected STEM. Signal intensity is proportional to
84 atomic number ($\sim Z^2$) and number of atoms along the beam direction for the imaging acquisition
85 condition (Kirkland, 1998; Pennycook, 2002). The TEM samples were prepared by crushing the
86 selected bytownite grain between two glass slides with ethanol. A drop of the suspension was
87 placed on a lacey-carbon Cu grid and air dried. The specimen was lightly plasma cleaned before
88 insertion into the STEM column on a double-tilt specimen holder. Interesting areas and crystal
89 grains with needed zone-axis orientations were located using TEM mode, due to the ease with
90 which appropriate zone-axis orientation can be identified under TEM mode. The probe
91 aberration correction was carried out first using a standard sample of nano-gold particles on a
92 single-tilt specimen holder. The double-tilt specimen holder containing the bytownite specimen
93 was again inserted into the STEM column for Z-contrast imaging under STEM mode. Switching
94 from STEM mode to TEM mode will lose aberration-corrected conditions.

95

96 **Results and Discussions**

97 The selected area electron diffraction pattern from the bytownite ($\sim An_{72}$) investigated here,
98 displays strong *a*-reflections, weak *e*-reflections, and very weak *f*-reflections (Fig. 1A). No

99 exsolution lamellae were observed in the studied sample, although it is within the Huttenlocher
100 intergrowth region. Micro-exsolution lamellae in some bytownite samples occur only in rock that
101 cooled extremely slow (Grove, 1976; Smith and Brown, 1988). A plagioclase grain with An72
102 was chosen for Z-contrast imaging because the modulation direction for ~An70 plagioclase is
103 very close to $(0\bar{1}1)^*$ direction, i.e., about normal to $(0\bar{1}1)$ (Ribbe, 1983; Smith and Brown,
104 1988). The modulation direction will be approximately perpendicular to the a -axis, a main
105 direction of feldspar. Z-contrast images along the a -axis will reveal structure variation along the
106 modulation direction clearly.

107

108 The obtained Z-contrast image along the a -axis clearly shows ordering of Ca atoms (indicated by
109 arrows) along $\sim (0\bar{1}1)$ planes (Fig. 2B). Signal intensity in Z-contrast images is directly related to
110 atomic number (Z) and occupancy of the atoms (Pennycook, 2002). Z-contrast images are very
111 sensitive to compositional change or variation. Z-contrast imaging that uses non-coherent
112 electrons scattered at high angle can avoid multiple diffraction that occurs in high-resolution
113 TEM imaging (Kirkland, 1998; Pennycook, 2002). No compositional or density modulation is
114 observed in Z-contrast images collected during this study. Fast Fourier transform (FFT) patterns
115 from Z-contrast images do not show satellite reflections around the 000 spot (Fig. 1C). If
116 composition or density modulation occurs in the crystal, satellite reflections will occur around
117 the 000 spot (Smith and Brown, 1988). The Ca-Na ordering phenomenon is obvious in a noise-
118 filtered Z-contrast image (Fig. 3). Arrows indicate Ca ordering at the boundaries ($\sim // (0\bar{1}1)$)
119 between the lamellar domains (Fig. 3). Outlines of unit cells (based on body-centered setting of
120 plagioclase) for the subcells are also inserted in the image. Yellow outlines are for subcells in the
121 lamellar domains. Red outlines are for subcells at the boundaries between the neighboring

122 domains (Fig. 3). Based on the intensities of Ca-Na (or, M) sites in the lamellar domains,
123 subcells do not have a symmetry center (or inversion center). Possible symmetry for the subcells
124 in the lamellar domains is $I1$, instead of $I\bar{1}$. Neighboring lamellar domains with $I1$ symmetry are
125 in an inversion twinning relationship. Structure models for the subcell domains and an inversion
126 twin boundary between neighboring lamellar domains are proposed in Figure 4. Al-Si ordering
127 structure in subcells with $I1$ symmetry is different from analogous ordering in low albite and
128 anorthite. Structures of albite and anorthite along a -axis are also illustrated in Fig. 5 (Angel,
129 1988; Harlow and Brown, 1980; Wainwright and Starkey, 1971). The subcell has an anorthite
130 sub unit with anorthite-like Al-Si ordering (Fig. 4C, 4D). However, in the albite-like subunit,
131 only one of the two T1o sites can be filled by Al. This follows the Al avoidance rule due to Al in
132 the anorthite region. Remaining Al will be distributed in T1m, T2m, and T2o sites in the albite-
133 like region (Fig. 4C, 4D). Al occupancy in the T1o site for the $I1$ structure (Figs. 4C, 4D) will be
134 0.5 using an average structure with $C\bar{1}$ symmetry. Al occupancies in T1o sites of the average $C\bar{1}$
135 symmetry structure will not be compatible with a mixture of low albite and anorthite subunits.
136 This is consistent with the observed Al-Si ordering in average structure of modulated plagioclase
137 feldspars (Figure 16 of Ribbe, 1972; Figure 3.8 of Smith and Brown, 1988). Proposed structure
138 types with Ca-Na polarity in the modulated structure may explain unique electron density of M
139 (Ca-Na) sites in average $C\bar{1}$ symmetry structures compared to a simple mixture of anorthite and
140 low albite domains. The structure at the inversion boundary will have $I\bar{1}$ symmetry with Ca-Na
141 ordering in 0 and z sites, respectively (Fig. 4B). Modulation in e -plagioclase is not a
142 compositional or density modulation, but a positional modulation involving shifts and ordering
143 of Ca-Na and Al-Si atoms within the subcells (Fig. 6).

144

145 Satellite reflections characterizing the modulated structure can also be observed in a $[\bar{1}\bar{1}\bar{1}]$ -zone-
146 axis diffraction pattern (Fig. 7A). A Z-contrast image and its noise-filtered image along the
147 $[\bar{1}\bar{1}\bar{1}]$ -zone-axis shows structural modulation along $\sim (0\bar{1}1)^*$ direction (Fig. 8A, 8B). The
148 observed image also indicates that the subcells in the lamellar domains do not have an inversion
149 center (Fig. 7D). Projection of the proposed $I1$ symmetry structure along $[\bar{1}\bar{1}\bar{1}]$ direction (Fig.
150 8C) matches evidence presented in the image (Fig. 8D). Periodic big dark (labeled “D”) and
151 small less dark (labeled “LD”) areas along c -axis result from Ca-Na ordering in the subcells of a
152 lamellar domain (Fig. 8D). If the subcells have inversion operation, the features of dark areas
153 should be the same because they are related by an inversion center.

154

155 Toman and Frueh (1976) proposed periodic APBs for modulated structure if subcells are centric.
156 They also proposed the possibility of a periodic inversion boundary for modulated structure if
157 subcells are non-centric (Toman and Frueh, 1976). However, X-ray diffraction alone cannot tell
158 the difference between the two possibilities (Toman and Frueh, 1976). As an alternative,
159 McConnell (2008) proposed a Ca-Na ordered structure for subcells with a primitive Bravais
160 lattice in the modulated structure. In this case the proposed periodic anti-phase lamellae domains
161 are related by a translational vector of $\frac{1}{2} [\mathbf{a}+\mathbf{b}+\mathbf{c}]$ (McConnell, 2008). This is not consistent with
162 the observed Z-contrast images presented here.

163

164 **Implications**

165 The transition of An-rich plagioclase from $I\bar{1}$ to $I1$ symmetry involves slight changes in Al-Si
166 ordering structure, i.e., movement of residual Al in some Si sites (blue) to neighboring Al sites

167 (Fig. 4B). Ca-Na ordering will result in Al ordering around Ca atom pairs (Figs. 4C, 4D). Phase
168 transition from $I\bar{1}$ to the modulated structure is a Na-Ca ordering process accompanied by Al-Si
169 ordering within the subcells with $I1$ symmetry. The neighboring lamellar domains of $I1$
170 symmetry are related by inversion twin operation. The newly discovered structure for the
171 intermediate plagioclase helps to understand Al-Si ordering and the subsolidus phase diagram of
172 plagioclase. Ca-Na ordering in intermediate plagioclase may lower the total energy and stabilize
173 the modulated structure (McConnell, 2008). The observed enthalpy difference between ordered
174 and disordered labradorite may support Ca-Na ordering in addition to the Al-Si ordering
175 (Carpenter et al., 1985).

176

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183

184

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251 Section B 40, 228-237.
- 252

253 **Figures captions**

254 Figure 1: SAED pattern along a -axis (A), Fast Fourier transform (FFT) patterns of annular
255 bright-field (ABF) image (B), and Z-contrast image (C) of modulated bytownite. Satellite
256 reflections do not occur around the 000 spot of FFT pattern (C).

257

258 Figure 2: ABF STEM image (A) image and Z-contrast image (B) along a -axis. Arrows indicate
259 ordering of Ca atoms (bright spots) at the boundary positions between the lamellae domains.

260

261 Figure 3: Noise-filtered Z-contrast image clearly showing Ca-Na ordering in lamellae domains
262 and at the inversion boundary positions. Neighboring lamellae domains with $I1$ symmetry are in
263 inversion twin relationship. A unit cell structure model showing polarity of Na-Ca atoms is also
264 overlaid on the image.

265

266 Figure 4: (A) Structure model for plagioclase with $C\bar{1}$ symmetry, i.e., average subcell structure
267 of plagioclase. (B) Structure model ($I\bar{1}$) for the boundary between lamellae domains. (C)
268 Structure model for the subcell ($I1$) of lamellae domain. (D) Structure model for the subcell that
269 is in inversion twin relationship with (C). Neighboring lamellae domains are in enantiomorphic
270 pairs, i.e., left-handed and right-handed structures. Oxygen atoms are omitted to enhance the
271 structural differences.

272 Big yellow spheres: Ca; small yellow spheres: Na; blue spheres: Si; turquoise spheres: Al.

273

274 Figure 5: Projections of low-albite ($C\bar{1}$), anorthite ($I\bar{1}$), and anorthite ($P\bar{1}$) structures along their
275 a -axes showing positions of Na and Ca atoms in the structures. Oxygen atoms are omitted to
276 enhance the structural differences.

277 Big yellow spheres: Ca; small yellow spheres: Na; Blue spheres: Si; turquoise spheres: Al.

278

279

280 Figure 6: Proposed model for modulated structure showing inversion boundaries // $(0\bar{1}1)$.

281 Arrows indicate the boundaries. The boundary between neighboring lamellae domains has $I\bar{1}$

282 symmetry instead of $C\bar{1}$ symmetry. The periodicity in this figure is shorter than the periodicity in

283 the actual crystal. This simplification is necessary in order to save page space.

284 Big yellow spheres: Ca; small yellow spheres: Na; blue spheres: Si; turquoise spheres: Al, or Al-

285 dominated sites.

286

287 Figure 7: SAED pattern (A) and FFT pattern (B) along $[\bar{1}\bar{1}\bar{1}]$ -zone-axis showing satellite

288 reflections along $\sim (01\bar{1})^*$ direction.

289

290 Figure 8: Z-contrast image (A) and noise-filtered image (B) along $[\bar{1}\bar{1}\bar{1}]$ -zone-axis showing

291 modulation along $\sim (\bar{1}\bar{1}\bar{1})^*$ direction. Boundaries between neighboring lamellae domains are

292 illustrated by yellow lines. A structural projection of *I1* intermediate plagioclase (C) and a

293 zoomed-in image (D) of sub-figure (B) show structural polarity with periodic big dark (D) and

294 small less dark (LD) areas along *c*-axis in the subcells of a lamellar domain. The polarity is a

295 result of Ca-Na ordering (C).

Fig. 1

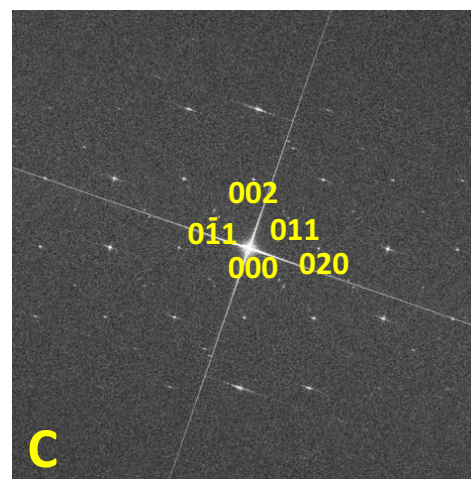
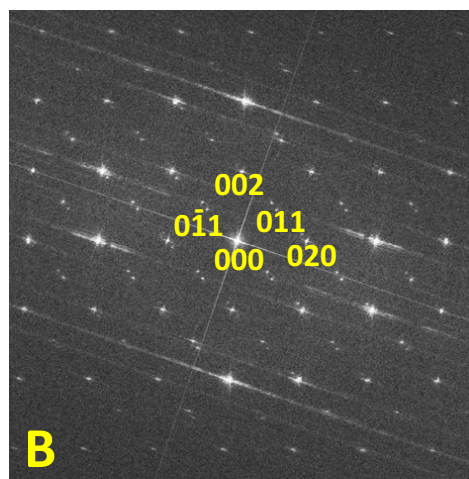
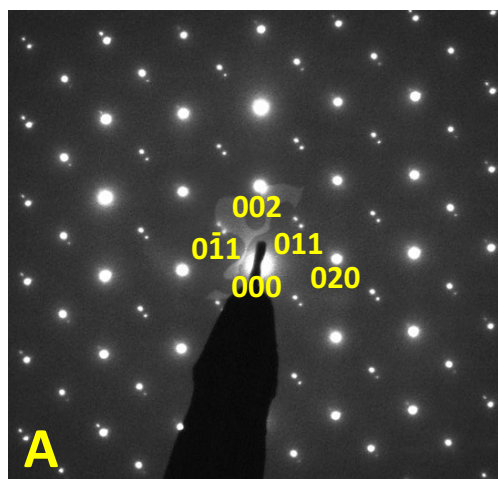


Fig. 2

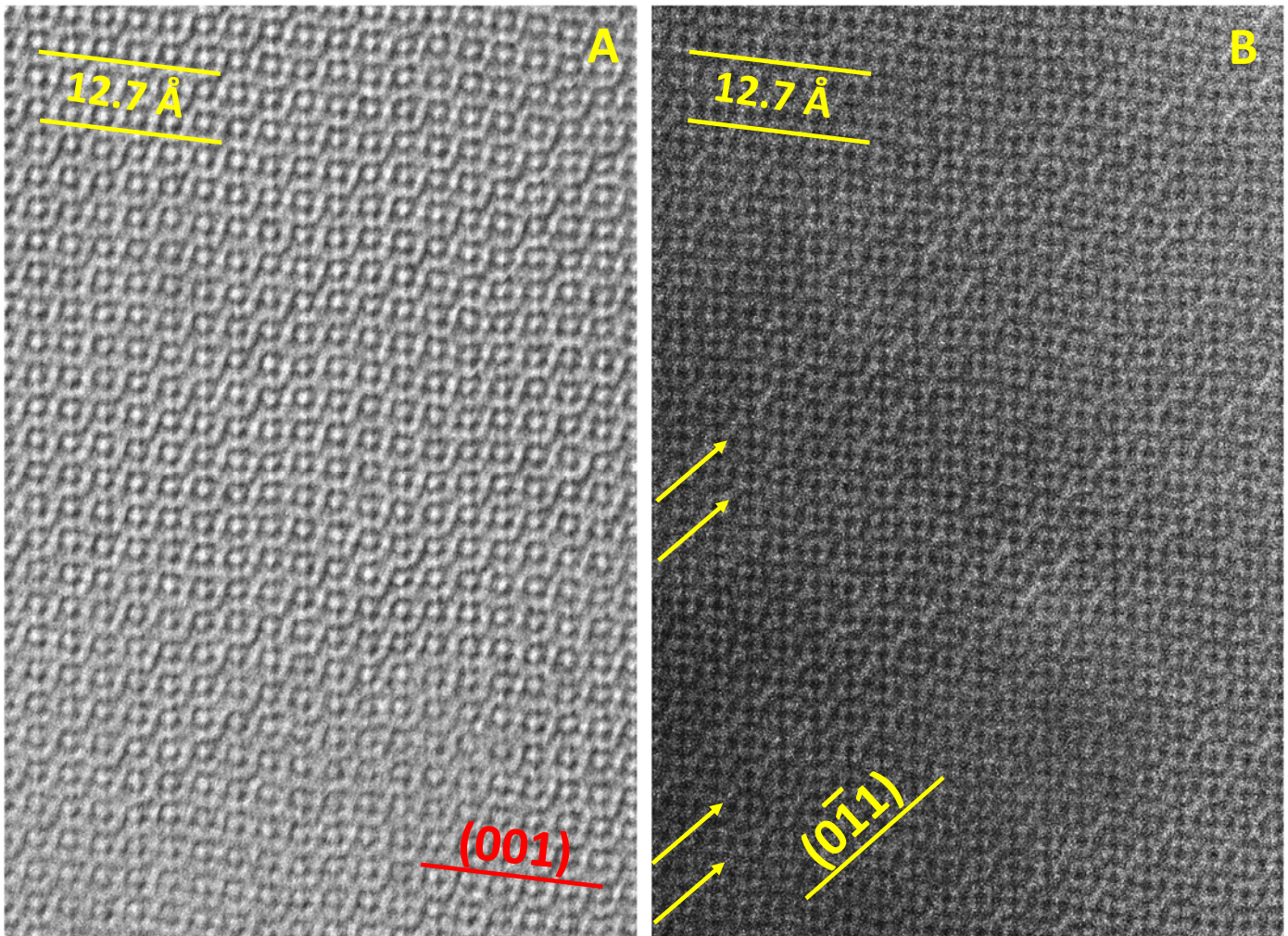


Fig. 3:

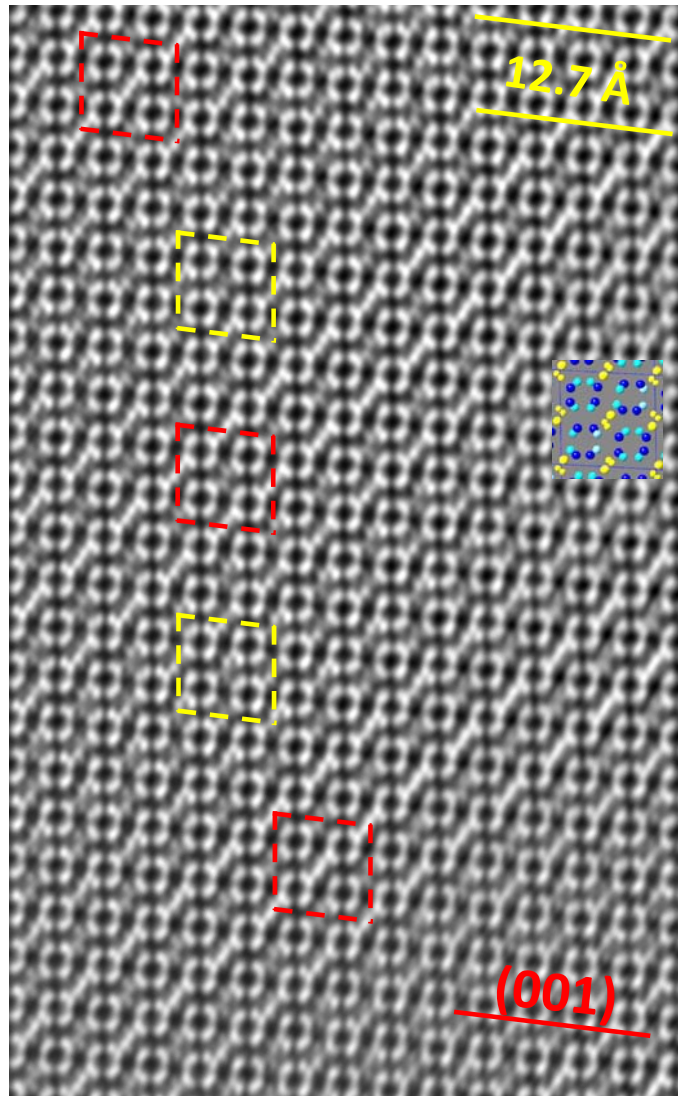


Fig. 4

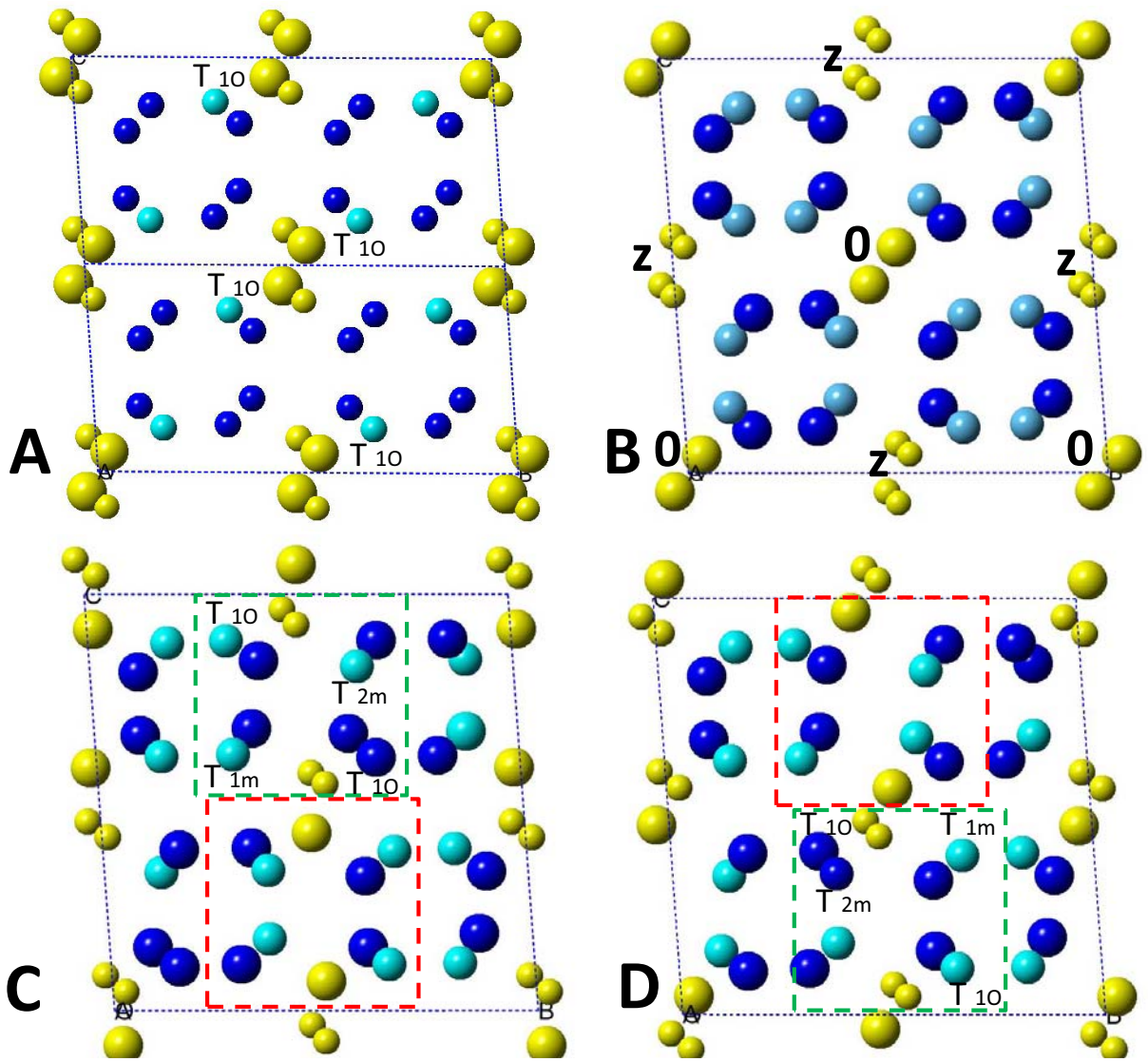


Fig. 5

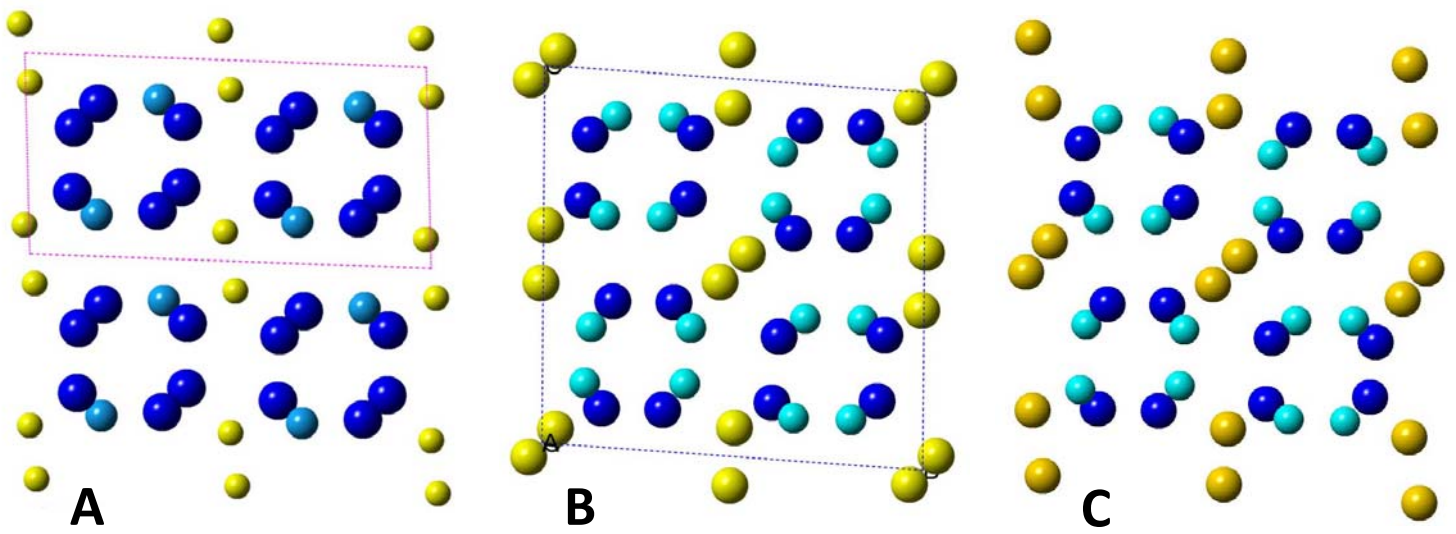


Fig. 6

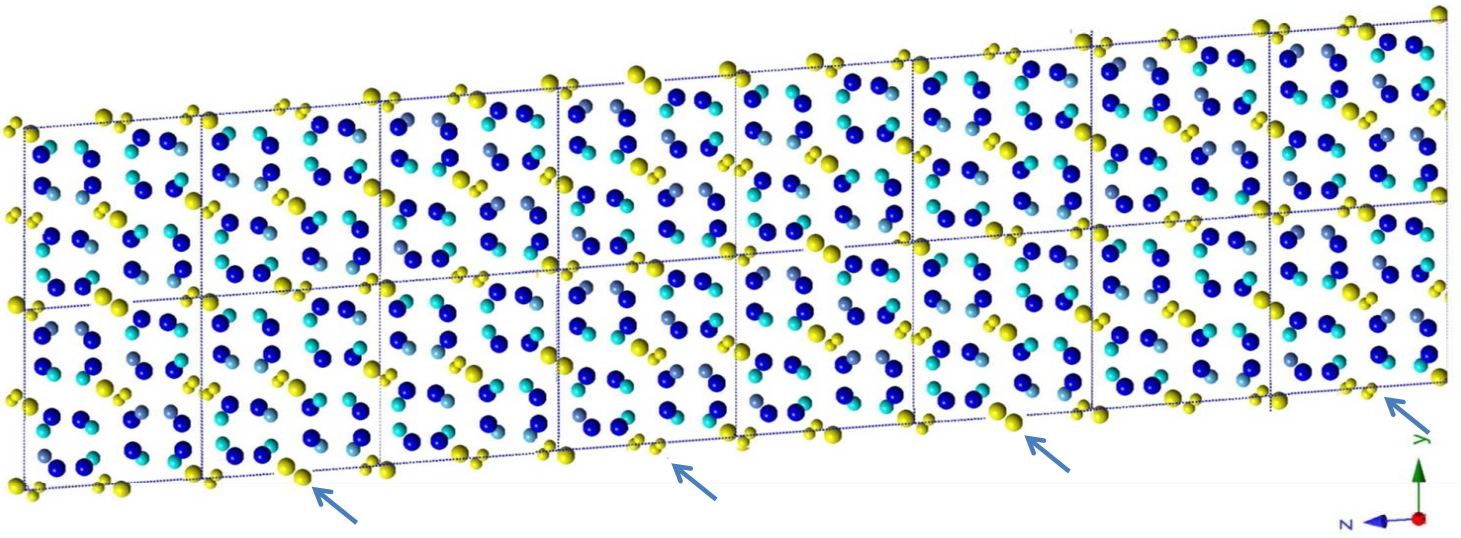


Fig. 7

