

1 **Revision 3**

2 **Crystal chemistry of synthetic Ti-Mg bearing hibonites: A single crystal X-ray study**

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29 **Abstract:**

30 Hibonite single crystals were synthesized using two different techniques: hot-pressing of
31 polycrystalline hibonite by means of piston-cylinder apparatus and solid state reaction using
32 citrate-based sol-gel precursors. Chemical analyses, UV/Vis spectroscopy and single crystal X-ray
33 characterization were performed on four sets of Ti-Mg bearing hibonites in order to investigate the
34 substitution mechanism of Ti^{3+} , Ti^{4+} and Mg^{2+} , relevant for hibonites found in
35 Calcium-Aluminum-rich inclusions in meteorites. The unit-cell volume of hibonite depends linearly
36 on the concentration of Ti and Mg: $V = 8.21(3) \cdot (\text{Ti}_{\text{tot}} + \text{Mg})_{a.p.f.u.} + 586.06$ (1). Structural
37 refinements, carried out in the space group $P6_3/mmc$, demonstrate that Ti occupies two sites: M2, a
38 trigonal bipyramid, and M4, a distorted octahedron occurring in face-sharing pairs. The Ti
39 occupancy factor was refined at both sites. Due to the repulsion of neighboring Ti cations the bond
40 distance M4-O3 increases with increasing Ti content and the cations are displaced from the central
41 position of the polyhedron. The displacement factors $M2_{U33}$ and the site occupancy factor for Ti in
42 the M2 site positively correlate for the samples which have more than 0.3–0.4 $\text{Ti}_{a.p.f.u.}$, while $M2_{U33}$
43 remains that of pure hibonite for small Ti occupancies at the M2 site. This plateau of displacement
44 factor reflects the local strain fields around the substituted Ti atoms and its magnitude indicates that
45 these strain fields begin to overlap at a Ti-Ti separation of about 1-2 unit cells. For a sample
46 synthesized at low oxygen fugacity we detected Ti^{3+} by means of UV/Vis absorption spectroscopy.
47 The presence of Ti^{3+} has a clear effect on the M4-M4 distance which deviates from the linear trend

48 described by samples containing mainly Ti^{4+} . The average bond length M3-O depends linearly on
49 the Mg content of these synthetic hibonites clearly indicating that Mg occupies this site.

50

51 **Keywords:**

52 hibonite, X-ray diffraction, single crystal, calcium hexaluminates, titanium

53

54 **INTRODUCTION**

55 Hibonite is a mineral rarely occurring on Earth, where it is mostly found in alluvial deposits as a
56 product of high grade metamorphism from upper amphibolite to granulite facies (Maaskant 1980;
57 Ulianov et al. 2005; Nagashima et al. 2010). In terrestrial systems, the composition of hibonite
58 differs significantly from its end-member CaAl_2O_3 composition, showing major REE substitution;
59 the terrestrial mineral has typically black-brownish to black color. Hibonite is also known in the
60 ceramic industry as calcium hexaluminate ($\text{CaO}\cdot 6\text{Al}_2\text{O}_3$ or CA_6), where it is used for various
61 applications, for example, as reinforcement fiber in composite material (Cinibulk 1995; An et al.
62 1996; Dominguez et al. 2001).

63 Besides its rare natural occurrence hibonite is however of great interest because it is a common
64 constituent of Calcium-Aluminum-rich inclusions (CAIs) in carbonaceous chondrites, providing
65 evidence for the formation of the first solid matter in our solar system. Based on observed ^{26}Mg
66 excess (Hinton et al. 1988; Ireland 1990) and on thermodynamic calculations (Grossman and Clark
67 1973), hibonite is considered to be a primary condensate from a hot gas of solar composition. It is
68 the second most Al-rich phase usually found in CAIs after corundum (e.g. Simon et al. 2002;
69 Nakamura et al. 2007). Hibonite has attracted a lot of attention over the years due to the fact that it
70 contains significant amounts of Ti, Mg, Fe, Si and V. The transition metals (Ti, Fe, V) have more
71 than one available oxidation state which may be correlated to the redox conditions of the solar
72 nebula during the condensation process (Ihinger and Stolper 1986; Beckett et al. 1988; Doyle et al.
73 2011; Giannini et al. 2011). However, the structural site at which a cation is accommodated in a
74 material as well as the substitution mechanism in complex systems may often determine the
75 oxidation state independently from the oxygen fugacity. Therefore, determining the Ti site
76 distribution in hibonite and its substitution mechanism is as important as measuring its oxidation
77 state.

78 So far, hibonite has been characterized by means of single crystal X-ray diffraction only on few
79 terrestrial samples from Madagascar (Bermanec et al. 1996; Hofmeister et al. 2004) and on a
80 gem-quality crystal from Myanmar (Nagashima et al. 2010). To our knowledge there are no
81 reported studies on hibonite single crystals from chondrites, mostly because the typical grain sizes
82 of these crystals ($< 30 \mu\text{m}$) are not suitable for conventional X-ray diffractometers, as well as due to
83 technical limitations for sample preparation and extraction.

84 The X-ray structural refinements on the terrestrial samples show that hibonite, $\text{AM}_{12}\text{O}_{19}$, crystallizes
85 in space group $P6_3/mmc$ ($Z = 2$). The structure can be described as a stacking of close-packed
86 oxygen layers parallel to the basal plane of the hexagonal cell, forming spinel-like blocks
87 ($S = [\text{M}_6\text{O}_8]^{2+}$) alternated by hexagonal close-packed blocks ($R = [\text{AM}_6\text{O}_{11}]^{2-}$) in a sequence that can
88 be written as $S'RSR'S'$ where the apex indicates a block rotated with respect to the 2-fold axis
89 parallel to the c axis. This arrangement of layers creates a variety of coordination environments,
90 starting from a large 12-fold coordinated site (A) sitting in the R blocks and, in the case of hibonite,
91 being mainly occupied by Ca. The M ions are distributed over five different sites: three with
92 octahedral (M1, M4, M5), one with tetrahedral (M3) and one with bipyramidal coordination (M2),
93 as illustrated in Fig. 1 (Bermanec et al. 1996). The atomic site M2 is split into two positions
94 according to a dynamic disorder model and also may be suitable for substitutions of Ti (Nagashima
95 et al. 2010).

96 Few methods have been able to successfully produce synthetic single crystals of hibonite. Mateika
97 and Laudan (1979) reported the synthesis of a hibonite-like compound ($\text{BaAl}_{12}\text{O}_{19}$) using the
98 Czochralski method, and this was followed by the growth of pure hibonite single crystals using the
99 traveling solvent floating zone method (Utsunomiya et al. 1988). More recently, Hofmeister et al.
100 (2004) obtained pure end-member hibonite by laser-heating pellets of $\text{CaO-Al}_2\text{O}_3$ mixtures. Both

101 techniques, however, are not suitable for controlling the oxygen fugacity during crystal growth,
102 moreover laser heating syntheses are often characterized by non-equilibrium conditions.
103 In this study we present single crystal X-ray diffraction (XRD) measurements on four sets of Ti-Mg
104 bearing synthetic hibonites prepared, at variable fO_2 , with two different techniques: hot-pressing of
105 polycrystalline hibonite by means of piston-cylinder apparatus, and solid state reaction using
106 citrate-based sol-gel precursors. These methods allow synthesis of hibonite single crystals which are
107 good proxies for meteoritic hibonites. Our aim is to provide a better understanding of the site
108 occupancy and substitution mechanism for Ti^{3+}/Ti^{4+} - Mg^{2+} -bearing hibonites and to address the
109 question whether it is possible to differentiate between the role of oxygen fugacity and the structural
110 control on the oxidation state of Ti.

111

112

EXPERIMENTAL METHODS

113 **Piston-cylinder**

114 A first attempt to synthesize single crystals of hibonite was done using a piston-cylinder apparatus,
115 as proposed by Geiger et al. (1988). Since these authors used oxide mixtures as starting materials for
116 their experiment, which resulted mostly in unreacted corundum, we have adopted a two-stage
117 synthesis method: polycrystalline hibonite was first synthesized at room pressure and then used as
118 starting material for a high pressure and high temperature experiment employing a piston-cylinder
119 apparatus (Boyd and England 1960) at the Bayerisches Geoinstitut (Table 1). To obtain the
120 polycrystalline starting material, a stoichiometric and homogenized mixture of $CaCO_3$, Al_2O_3 , MgO
121 and TiO_2 was decarboxylated up to 900 °C, pressed into a 1/2" pellet and fired in air at 1430 °C for
122 14 hours. The run product was identified as almost pure hibonite by means of X-ray powder
123 diffraction (XRPD) and it was subsequently sealed inside a Pt capsule, which was inserted into a
124 1/2" MgO-pyrex assembly equipped with graphite heater. The piston-cylinder experiment was run

125 at 15 kbar, the temperature was monitored using a type-D (W - 3 %Re / W - 25 %Re) thermocouple
126 and it was kept constant at 1450 °C for 12 h; then temperature was raised to about 2000 °C for
127 90 min before immediate quench. The Pt capsule partially melted during the experiment. The
128 recovered crystalline material consisted of single crystals of hibonite of up to 200 µm in size and
129 with platy morphology. Due to the graphite heater, the oxygen fugacity for this synthesis can be
130 estimated to have varied between $\log f_{O_2} = -7.6$ and $\log f_{O_2} = -4.9$ during the temperature step from
131 1450 °C to 2000 °C (Jakobsson and Oskarsson 1994; Médard et al. 2008). Compared to the
132 Iron-Wüstite (IW) buffer (Frost 1991), these oxygen fugacity conditions at 15 kbar correspond to
133 IW+1 at 1450 °C and IW at 2000 °C, within uncertainties which are estimated as ± 0.3 log units
134 (Médard et al. 2008).

135

136 **Solid state reaction synthesis**

137 Citrate-based sol-gel precursors were prepared as described by Cinibulk (1998). The initial gel was
138 formed by completely and sequentially dissolving in ethanol, under reflux, the appropriate amounts
139 of aluminum nitrate $Al(NO_3)_3 \cdot 9H_2O$, magnesium nitrate $Mg(NO_3)_2 \cdot 6H_2O$, citric acid
140 $HO_2CCH_2COHCOOHCH_2CO_2H \cdot H_2O$ (2 mole per 1 mole of Al) and calcium acetate
141 $Ca(C_2H_3O_2)_2 \cdot H_2O$. Finally titanium isopropoxide $Ti[OCH(CH_3)_2]_4$ was added together with ethylene
142 glycol $C_2H_6O_2$ (1 mol to every 1 mol of nitrates). The mixture was allowed to reflux (~ 82 °C) for
143 6 h, producing a pale yellow transparent sol, which, in case it turned turbid, could be cleared with
144 the addition of nitric acid HNO_3 (0.2 mol per 1 mol of Ti-isopropoxide, Yoldas 1986). Small
145 aliquots of the sol (~ 10 -20 ml) were then heated up to 150 °C to promote gelification and
146 subsequent polymerization; further heating to ~ 200 °C resulted in the removal of all the solvents,
147 leaving a yellowish resin. Firing the resin up to ~ 600 °C removes all organics, giving an amorphous
148 material, in which the cations are, ideally, uniformly dispersed on an atomistic scale throughout the

149 sample. This material was pressed into 1/2” pellets and heated to temperatures up to 1550 °C either
150 in air ($\log fO_2 = -0.5$) or under reducing conditions at $\log fO_2 = -11.0$ (IW-2.5) using a gas-mixing
151 furnace in which the oxygen fugacity is controlled by a CO/CO₂ flux (Table 1). The run products
152 consisted of hibonite single crystals up to 90 μm in size (Fig. 2), except for gel0 (with composition
153 of pure hibonite, CaAl₁₂O₁₉) whose crystals had sizes smaller than 10 μm and therefore could not be
154 analyzed by means of single crystal XRD, thus X-ray powder diffraction was used instead.

155

156 **SEM-EMPA characterization**

157 The chemical compositions of hibonites were measured with a JEOL JXA-8200 electron
158 microprobe (EMPA), fully-automated with five crystals and five wavelength dispersive
159 spectrometers. The polished samples were coated with about 10 nm of amorphous carbon to avoid
160 charging of the surface and studied at acceleration voltages of 15 kV and probe currents between 15
161 and 20 nA, measuring for 10 sec the pre- and post-peak backgrounds and 20 sec on the peak
162 position. The analytical standards used for the calibration of the energy positions of the analyzed
163 elements were: MgO for Mg, Al₂O₃ for Al, MnTiO₃ for Ti, wollastonite for Ca and enstatite for Si.
164 Also Fe has been probed, however, its signal was below detection limit for all samples. For each
165 specimen 20 to 40 points were measured and averaged (Table 2).

166

167 **Optical spectroscopy**

168 Optical spectra were obtained for gel6-1 and gel6-3 samples using a Bruker IFS20 Fourier
169 Transform (FT) spectrometer with polychromatic beam from a tungsten source modulated using a
170 Michelson interferometer and equipped with a quartz beam splitter for UV/Vis measurements. The
171 measurements were performed in the range from 10000 to 25000 cm⁻¹ accumulating up to 800 scans
172 per spectrum in order to enhance the signal to noise ratio. Double polished thin sections were

173 prepared with chips from gel6-1 and gel6-3 run products and polarized spectra were obtained from
174 crystals oriented with the c axis perpendicular to the direction of propagation of the light beam, i.e.
175 parallel to the glass slide plane, in order to have the c axis parallel to the polarization direction, E .
176 The orientations of hibonite crystals were determined by means of conoscopic methods (Raith et al.,
177 2012) using a petrographic microscope. No signal above the background was visible for gel6-1
178 which was synthesized in air ($\log fO_2 = -0.5$), however a strong absorption was observed for the
179 crystals of sample gel6-3 synthesized at a $\log f(O_2) = -11$ (Fig. 3), indicating that a large portion of
180 Ti in this hibonite is present as Ti^{3+} as discussed below.

181

182 **X-ray powder diffraction data collection and analysis**

183 X-ray powder diffraction was used for all synthetic runs for phase identification (Table 1).
184 Diffraction patterns were collected in the 2θ range between 6 and 110° on a Philips X'Pert Pro
185 diffractometer operating in reflection mode with $Co\ K\alpha_1$ monochromated radiation, using 0.03°
186 step size and $1.8^\circ/\text{min}$ scan speed; Si NIST SRM 640c material was added to the powdered samples
187 as internal standard. Rietveld refinements were carried out using the program suite EXPGUI (Toby
188 2001) based on the refinement algorithm GSAS (Larson and Von Dreele 2004). Refinements of the
189 unit-cell parameters of all phases present in the run product were performed using the structural
190 models from Bermanec et al. (1996), Oetzel and Heger (1999), Sasaki et al. (1987) and Grimes et al.
191 (1983) for hibonite, corundum, Ca-Ti perovskite and spinel, respectively.

192 The unit-cell parameters of the end-member hibonite, gel0, determined by means of XRPD,
193 $a = 5.55822(4)\text{ \AA}$, $c = 21.9048(2)\text{ \AA}$ resulting in a volume cell of $586.060(7)\text{ \AA}^3$, were used as an
194 end-member reference, since we could not obtain any single crystal structural refinement of this
195 sample due to the small size of its crystals.

196

197 **Single crystal X-ray data collection and structure refinements**

198 Hibonite single crystals were chosen for XRD characterization on the basis of their size,
199 morphology and optical properties. A preliminary data set was collected on a 4-circle κ -geometry
200 Xcalibur diffractometer equipped with CCD detector and monochromatic Mo $K\alpha$ radiation. The
201 crystals showing strong diffraction intensities were subsequently measured on a Huber SMC9000
202 4-circle diffractometer equipped with point detector and Mo $K\alpha$. The crystals yielding Bragg
203 reflections with full width at half maximum (FWHM) smaller than 0.12° were further analyzed.
204 Accurate unit-cell parameters were measured on the Huber diffractometer using the 8-position
205 centering procedure (King and Finger 1979; Angel and Finger 2010) on more than ten selected
206 independent reflections. The measurements and the subsequent least square refinement to calculate
207 the symmetry constrained unit-cell parameters were performed with the software SINGLE04 (Angel
208 and Finger 2010) and are reported in Table 3. Complete datasets of diffracted intensities for the
209 selected crystals were measured on the Xcalibur diffractometer at room temperature with optimized
210 number of frames with ω -scan (in one case combined with ϕ -scan) using 0.5° scan width. Data
211 reduction and integration were performed using the CrysAlisPro software (Agilent Technologies
212 2012), which also includes the packages used for analytical absorption correction (Clark and Reid
213 1995) and empirical multi-scan correction (ABSPACK, Agilent Technologies 2012).
214 The structural refinements were carried out on squared structure factors ($F_{o/c}^2$) adopting the
215 scattering curves for neutral atoms published on the International Tables for X-ray Crystallography
216 (Hahn 2005) and using the program suite WinGx (Farrugia 1999) based on the refinement algorithm
217 SHELX (Sheldrick 2008). All the refinements were performed in the space group $P6_3/mmc$ (N° 194)
218 assuming a model for pure hibonite end-member based on the atomic coordinates proposed by
219 Bermanec et al. (1996). Atomic coordinates and anisotropic thermal factors were refined for all
220 samples, as well as an overall scale factor and a 2-term weighing scheme. The Fourier difference

221 maps were evaluated for each dataset in order to estimate the possible location of Ti in the structure
222 of hibonite. Due to the high concentration of Ti in the crystals of gel6-1 and gel6-3, a significant
223 residual electron density was observed at the M4 site, a trigonally distorted octahedron occurring in
224 face-sharing pairs. After refining the Ti occupancy into the M4 site, another peak in the Fourier map
225 appeared at the M2 site, a trigonal bipyramid. After this observation a structural model having Ti in
226 both the M2 and the M4 sites was used to refine the structure of all the other samples, even for those
227 whose Ti concentration was too low to give appreciable peaks in the Fourier difference maps, i.e.
228 HBMT5 and gel4-1. The sum of the occupancies of Ti and Al on the same site has been constrained
229 to be unitary and the coupled atoms were forced to have the same fractional coordinates and thermal
230 factors; however the occupancy of Ti at these two sites has not been constrained. Data collections
231 and refinements details, as well as atomic and displacement parameters are reported in Table 3 and
232 4, respectively.

233 Further structural analyses were performed considering the parameters describing distortions of
234 coordination polyhedra, i.e. octahedral angle variance (OAV), as defined by Robinson et al. (1971)
235 which were calculated using the software XtalDraw (Downs and Hall-Wallace 2003).

236

237

RESULTS AND DISCUSSION

238 **The crystal chemistry of hibonite**

239 The synthetic methods and conditions for the single crystals analyzed in this study are reported in
240 Table 1; the expected nominal compositions are indicated together with the main phases detected by
241 XRPD and the color of synthetic hibonite crystals. The average chemical compositions measured by
242 EMPA on several crystals are listed in Table 2, where the total amount of Ti is calculated as TiO₂.
243 The corresponding chemical formulae are calculated normalizing the cation numbers to 19 O.
244 Tables 1 and 2 also include the sample gel0, corresponding to polycrystalline pure end-member

245 hibonite. The run products obtained from the sol-gel precursors have a homogeneous composition,
246 as revealed by the small deviations between EMPA analyses performed on several spots for each
247 sample. The absence of zoning is also confirmed by SEM back scattered electron (BSE) imaging of
248 all polished samples, see Fig. 2 as an example. Microprobe analyses of the sample prepared from
249 oxide mixture (HBMT5) yield compositions with standard deviations similar to those of samples
250 prepared by the sol-gel method. The unit-cell parameters obtained for each single crystal and those
251 obtained from XRPD on the corresponding bulk sample agree very well, e.g. the volume cell for the
252 sample gel6-3 obtained from XRPD is $604.10(4) \text{ \AA}^3$ (compare with Table 3). The grain size of
253 hibonite seems to be related to the concentration of doping elements (i.e. Ti and Mg, Table 3): larger
254 crystals are produced at higher concentrations of Ti and Mg.

255 The composition of synthesized hibonite crystals is clearly different from the nominal composition
256 of the starting materials (compare Table 1 and 2). The measured chemical formulae are closer to the
257 nominal values for samples with low Ti-Mg content (HBMT5 and gel4-1). The samples with high
258 Ti-Mg content have compositions that deviate from the nominal ones because Ti and Mg are also
259 accommodated in the spinel and Ca-Ti-perovskite phases, also present in the run products (Table 1).

260 Most of the samples have a Ti:Mg ratio that is close to 1:1, suggesting that the coupled substitution
261 $2\text{Al}^{3+} = \text{Ti}^{4+} + \text{Mg}^{2+}$ is the major incorporation mechanism for Ti and Mg in hibonite. At low
262 oxygen fugacity (gel6-3), the hibonite structure takes up more Ti, resulting in a small excess of Ti
263 with respect to Mg, most likely because more reducing conditions favor the substitution of Ti^{3+}
264 according to an $\text{Al}^{3+} = \text{Ti}^{3+}$ substitution. The presence of Ti^{3+} in gel6-3 is confirmed by the strong
265 absorption band observed in the UV/Vis spectrum for this sample (Fig. 3). As demonstrated by
266 Ihinger and Stolper (1986), this absorption band at 715 nm is uniquely attributed to the presence of
267 Ti^{3+} and results in the blue color of hibonite. It was not possible to collect absorption spectra for

268 sample HBMT5, however these hibonite crystals are also blue in color (Table 1), suggesting the
269 presence of trivalent Ti.

270

271 **Effect of Ti-Mg incorporation on the unit-cell parameters**

272 The unit-cell volume of the studied hibonites varies linearly with the concentration of $Ti_{tot} + Mg$
273 (Fig. 4, Table 3); the solid line drawn on Fig. 4 is a linear fit through our data, which gives the
274 following empirical relationship: $V = 8.21(3) \cdot (Ti_{tot} + Mg)_{a.p.f.u.} + 586.06(1)$. An increase of the
275 unit-cell volume is consistent with an expansion of the oxygen framework as a consequence of the
276 substitution of Al^{3+} (0.535 Å) with larger cations such as Mg^{2+} (0.720 Å), Ti^{4+} (0.605 Å) and Ti^{3+}
277 (0.67 Å). The data reported in the literature generally lie above our trend; for pure end-member
278 hibonite the unit-cell volumes reported by Hofmeister et al. (2004) and Utsunomiya et al. (1988) are
279 0.35 % and 0.70 % greater than the unit-cell volume obtained for the end-member hibonite
280 synthesized in this study (gel0). This discrepancy may be due to the different synthesis procedures,
281 which can give rise to varying degrees of non-stoichiometry affecting the unit-cell parameters, as
282 well as to the accuracy in the centering of Bragg reflections, which can result in systematic errors.
283 In the case of our samples, we have observed that the unit-cell parameters measured by means of
284 XRPD are in good agreement with those obtained from the 8-positions centering method. The most
285 outlying data point is that from Bermanec et al. (1996), reporting a cell volume 1.5 % larger than
286 that described by our regression line, likely due to the presence of REE in this natural hibonite. In
287 fact, the sample studied by Nagashima et al. (2010), being an unusually REE-free terrestrial
288 hibonite, is in good agreement with our regression.

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290

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292 **Effect of Ti-Mg incorporation on the hibonite structure**

293 The occupancy of Ti has been refined both at the M2 and the M4 sites; the overall Ti concentration
294 that can be calculated from the refined occupancies is in very good agreement with the EMPA
295 measurements (Table 2 and 4). The variation of the M4-O bond distances as a function of Ti content
296 is shown in Fig. 5. In contrast to what is reported by Nagashima et al. (2010), the distance M4-O5
297 does not seem to be influenced by the Ti substitution. The difference between M4-O5 and M4-O3
298 bond lengths increases as reported by Nagashima et al. (2010) simply because the M4-O3 bond
299 length increases, as shown in Fig. 5. The change in M4-O3 bond length is due to the repulsion of the
300 highly charged Ti atoms (mostly present as Ti^{4+}) and their consequent displacement from the central
301 position of the polyhedron along the *c* axis. This displacement can be visualized by plotting the
302 variation of the M4-M4 distance with respect to the Ti content (Fig. 6). For our synthetic samples,
303 we observe that with increasing amount of Ti the M4-M4 distance increases. Note, however, that
304 this distance is clearly smaller for gel6-3. This is likely due to the fact that this sample contains a
305 larger amount of Ti^{3+} with respect to the other samples and as a consequence the repulsion between
306 the M4 cations is weaker. The hibonites from Madagascar (Bermanec et al. 1996; Hofmeister et al.
307 2004) show a larger M4-M4 distance with respect to the trend represented by our samples; however
308 this is not surprising given their complex chemistry. More puzzling are the differences between our
309 samples and the hibonite studied by Nagashima et al. (2010), which has a much simpler chemical
310 formula. However, this is possibly only an apparent discrepancy because the Ti content
311 ($\text{Ti}_{a.p.f.u.} = 0.52$) reported as EMPA analysis in Nagashima et al. (2010) is smaller than that
312 calculated from the M2 and M4 site occupancies ($\text{Ti}_{a.p.f.u.} = 0.61$), listed in their XRD data. This
313 would correspond to about 1 wt% more of TiO_2 in the formula of hibonite by Nagashima et al.
314 (2010). Considering this larger amount of Ti, their data point is in better agreement with our results.

315 There also is some evidence of Ti occupying the M2 site. The axial (M2-O1) and equatorial
316 (M2-O3) bond distances are not clearly dependent on the Ti concentration; however we observe a
317 correlation between the displacement factor along the *c* axes, $M2_{U33}$ (Table 4), and the site
318 occupancy factor (*s.o.f.*) for Ti at the M2 site (Fig. 7). This displacement factor can be interpreted as
319 a measure of the cationic disorder in the trigonal bipyramid due to the different charge of
320 substituting cations. An increasing amount of Ti substituting for Al into the M2 site corresponds to
321 an enlargement of the displacement factor $M2_{U33}$. It appears, however, that $M2_{U33}$ remains that of
322 pure hibonite for small Ti occupancies at the M2 site. This plateau of displacement factor is similar
323 to the plateau of transition temperature or transition pressure (Salje et al. 1991; Hayward and Salje,
324 1996; Carpenter et al. 1999, 2009; Boffa Ballaran et al. 2000) that can be observed when a second
325 component of a solid solution is added into the structure of the other end-member. Change in the
326 transition point, or, in this case, in the displacement parameter occurs only once the microscopic
327 strain fields around the impurity atoms start to overlap. The magnitude of the plateau is therefore a
328 reflection of the magnitude of the local strain fields around the substituted Ti atoms. Since a visible
329 change in $M2_{U33}$ can be observed only for samples which have more than 0.3 – 0.4 $Ti_{a,p.f.u.}$ (Table 2
330 and 4), we can estimate that the strain fields around each Ti atom begins to overlap at a Ti-Ti
331 separation of about 1-2 unit cells. The significant difference of $M2_{U33}$ between our sample gel6-3
332 containing Ti^{3+} and the terrestrial hibonite from Nagashima et al. (2010), supposedly containing
333 only Ti^{4+} (Fig. 7) may therefore be due to smaller microscopic strain fields around the Ti^{3+} atoms as
334 well as to a weaker repulsion because of its smaller charge.

335 Due to the very low difference in the scattering factors of Al^{3+} and Mg^{2+} (the two cations are
336 isoelectronic), it was not possible to directly locate the position of Mg and thus the refinements were
337 carried out without considering this cation. However, there is a clear correlation between the
338 concentration of Mg in hibonite obtained from the EMPA and the M3-O tetragonal bond distance

339 (Fig. 8). We observe an elongation of the M3-O bond distance as a function of Mg content and we,
340 therefore, can confirm that indeed divalent cations occupy the M3 site as suggested by Bermanec et
341 al. (1996) and Nagashima et al. (2010). The variation of the average M3-O bond length with Mg
342 content fits the following regression through our data: $d_{\text{M3-O}} = 0.065(3) \cdot \text{Mg}_{a.p.f.u.} + 1.800(2)$, where
343 1.800(2) is the extrapolated tetrahedral bond distance of pure hibonite. This value is in good
344 agreement with the tetrahedral distances reported by Hofmeister et al. (2004) and Utsunomiya et al.
345 (1988).

346 Substitution of Ti and Mg also affects the polyhedra which are occupied only by Al. In particular
347 the site M1 becomes more irregular as a function of Mg content because of the expansion of the
348 tetrahedron M3 which is connected to M1 through the bridging oxygen O4. This is clearly seen in
349 the increase of the octahedral angle variance (OAV, Table 4), which is a measure of the distortion of
350 the 6-fold coordination environment; i.e. the closer the OAV is to zero, the more regular the
351 octahedron is. The M5 site instead is sandwiched between the layers where Ti and Mg are
352 substituting (Fig. 1). As a result of the individual M5-O bond variations driven by the substitution in
353 the adjacent sites, the M5 octahedron tends to become more regular as the substitution of Ti and Mg
354 occurs into the structure of hibonite (Table 4).

355

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IMPLICATIONS

357 The simple chemistry of the samples synthesized in this study allows us to exclusively determine
358 the effect of Mg and Ti substitution on the hibonite structure. Ti clearly occupies both M4 and M2
359 sites (Figs. 6 and 7). At low oxygen fugacities we observe a detectable amount of Ti^{3+} , with a clear
360 effect on the M4-M4 distance which deviates from the linear trend described by samples containing
361 mainly Ti^{4+} (Fig. 6). The presence of a plateau effect in the change of the M2 displacement
362 parameter with Ti substitution (Fig. 7) gives an idea of the magnitude of the microscopic strain

363 fields around the Ti atoms which appear to be similar to the strain fields inferred when Fe²⁺ atoms
364 are substituted by Mg into the grunerite structure (Boffa Ballaran et al. 2000) or for dopant atoms in
365 oxide perovskites (Carpenter et al. 2009).

366 The hibonites synthesized in this study have chemical compositions comparable to that of meteoritic
367 samples. Knowing the exact coordination of the Ti atoms is fundamental for quantifying the Ti³⁺
368 /Ti⁴⁺ ratio in hibonite, as has been attempted in several studies aimed to give better insights on the
369 oxygen fugacity conditions in the solar nebula during formation and evolution of CAIs. These
370 studies have used UV/visible (Ihinger and Stolper 1986), ESR (Becket et al. 1988), EELS (Giannini
371 et al. 2011) and Xanes spectroscopy (Doyle et al. 2011) and have so far given only qualitative
372 results due to the fact that the coordination of Ti was based on simple assumptions. Chemical and
373 structural information as reported in this study provide strong constraints on the Ti distribution and
374 therefore can be used to quantify the spectroscopic result.

375

376

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FIGURES CAPTIONS

495 **Figure 1.** Crystal structure of hibonite showing the coordination polyhedra and the repetitive
496 blocks. The figure was generated using the software VESTA (Momma and Izumi, 2011).

497 **Figure 2.** SEM-BSE image of gel6-1 sample. Light grey =hibonite (hib), dark grey = spinel (sp),
498 white = Ca-Ti-perovskite (pv) , black = voids.

499 **Figure 3.** Absorption spectra of samples gel6-1 synthesized in air (dotted line) and gel6-3
500 synthesized at an oxygen fugacity of $\log f\text{O}_2 = -11$ (solid line). The strong absorption band at
501 715 nm of gel6-3 indicates that part of Ti in hibonite is present as Ti^{3+} .

502 **Figure 4.** Unit-cell volume of hibonites as a function of the sums of the transition metal cations
503 substituting for Al. Vertical diamonds = single crystals from this study; horizontal diamond = gel0;
504 open symbols = literature data. The solid line indicates a fit through the data points of this study (R^2
505 = 1.00) according to the expression $V = 8.21(3) \cdot (Ti_{tot} + Mg)_{a.p.f.u.} + 586.06(1)$.

506 **Figure 5.** Bond distances M4-O5 and M4-O3 as a function of the sum of trivalent and tetravalent
507 cations, in the case of this study exclusively Ti, substituting for Al. Symbols as in Figure 4. The
508 solid line indicates a fit through the data points for this study ($R^2 = 0.96$) according to the expression
509 $d_{M4-O3} = 0.42(2) \cdot (Ti_{tot})_{a.p.f.u.} + 1.961(2)$ while the horizontal dashed line is a guide to the eyes drawn
510 through the average of our data in order to show that the M4-O5 distance is independent of cation
511 substitution.

512 **Figure 6.** Inter-atomic distance M4-M4 as a function of the sum of trivalent and tetravalent cations,
513 in the case of this study exclusively Ti, substituting for Al. Symbols as in Figure 4. The solid line
514 indicates a fit through the data points for this study, excluding gel6-3 which deviates from the linear
515 trend due to the presence of Ti^{3+} : $d_{M4-M4} = 0.117(3) \cdot (Ti_{tot})_{a.p.f.u.} + 2.584(2)$, ($R^2 = 1.00$).

516 **Figure 7.** Displacement factor U_{33} for the M2 site as a function of the corresponding refined site
517 occupancy factor, *s.o.f.*, of Ti. Solid diamonds = this study, open symbols = literature data. The
518 solid line indicates a fit through the data points for this study ($R^2 = 0.95$), excluding gel6-3:
519 $M2_{U33} = 0.17(5) \cdot (Ti_{s.o.f.})_{a.p.f.u.}$. The dotted line indicates a possible plateau at $0.008(3) \text{ \AA}^2$ which
520 represents the displacement factor for pure hibonite.

521 **Figure 8.** Bond distances M3-O as a function of the sum of divalent cations substituting for Al, in
522 the case of this study exclusively Mg. Symbols as in Figure 4. The solid line indicates a fit through
523 the data points for this study ($R^2 = 0.99$) according to the expression d_{M3-O}
524 $= 0.065(3) \cdot Mg_{a.p.f.u.} + 1.800(2)$.

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526

TABLES

527 **Table 1.** Synthetic methods, conditions and run products for hibonite samples.

Sample	Method [§]	Temp. [°C]	log <i>f</i> O ₂	time [h]	Nominal composition of hibonite	Main products*	Color of hibonite [#]
HBMT5	PC	1450	-7.6	12	CaAl _{11.25} Ti _{0.42} Mg _{0.33} O ₁₉	hib	blue
		2000	-4.9	1.5			
gel4-1	SG	1550	-0.5	15	CaAl _{11.4} Ti _{0.40} Mg _{0.20} O ₁₉	hib	white
gel6-1	SG	1550	-0.5	15	CaAl _{8.00} Ti _{2.00} Mg _{2.00} O ₁₉	hib + sp + pv	white
gel6-3	SG	1550	-11	15	CaAl _{8.00} Ti _{2.00} Mg _{2.00} O ₁₉	hib + sp + pv	blue
gel0	SG	1550	-0.5	15	CaAl _{12.00} O ₁₉	hib	white

[§]PC = piston cylinder, SG = sol-gel; * detected as > 5 %_{wt} from XRPD: hib = hibonite,

pv = Ca-Ti-perovskite, sp = spinel; [#]color of the recovered pellets after firing at high temperature: while the bulk color of samples synthesized in air appears white, the individual single crystals are colorless.

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 531 **Table 2.** Chemical composition of hibonite crystals determined by EMPA; one-sigma standard
 532 deviations are given in brackets. For each sample 20 to 40 points were measured and averaged.

	HBMT5	gel4-1	gel6-1	gel6-3	gel0
Oxides wt%					
CaO	8.51(7)	8.40(6)	8.21(7)	8.19(8)	8.64(6)
Al₂O₃	86.3(4)	86.7(2)	75.4(2)	72.4(5)	91.1(5)
MgO	1.9(1)	1.28(2)	5.27(7)	5.7(1)	==
TiO₂	4.3(3)	3.4(1)	11.0(1)	13.8(2)	==
Tot.	101.0(2)	99.7(2)	99.9(3)	100.2(4)	99.8(5)
Cations per formula unit, normalized to 19 oxygen atoms					
Ca	1.01(2)	1.01(2)	1.00(2)	1.00(2)	1.03(2)
Al	11.30(4)	11.47(2)	10.14(2)	9.75(4)	11.98(2)
Mg	0.31(3)	0.21(2)	0.90(2)	0.97(3)	==
Ti*	0.36(4)	0.28(2)	0.94(2)	1.18(3)	==
*Total amount of Ti calculated as Ti ⁴⁺ .					

533

534 **Table 3.** Details for data collection and refinements from single crystal XRD measurements
 535 performed on hibonite.

	HBMT5	gel4-1	gel6-1	gel6-3
Crystal size [mm]	0.175x0.115x0.045	0.06x0.04x0.01	0.19x0.17x0.09	0.135x0.095x0.03
<i>a</i> [Å]	5.5778(6)	5.5711(7)	5.6071(4)	5.6192(4)
<i>c</i> [Å]	21.9523(7)	21.9448(8)	22.0653(4)	22.0944(5)
<i>V</i> [Å³]	591.5(1)	589.9(1)	600.80(8)	604.18(8)
Scan type	φ-ω scan	ω scan	ω scan	ω scan
θ_{max} [°]	63.66	64.2	72.79	72.67
Reflections	12489	10949	16667	2997
Unique reflections	441	442	615	596
<i>R</i>_{int} [%]	3.63	9.47	4.50	3.17
<i>R</i>_s [%]	3.29	5.37	4.14	5.15
<i>R</i>₁ [%]	2.78	3.82	4.05	3.99
<i>wR</i>₂ [%]	7.71	9.66	9.88	9.99
Number of parameters	44	44	44	44

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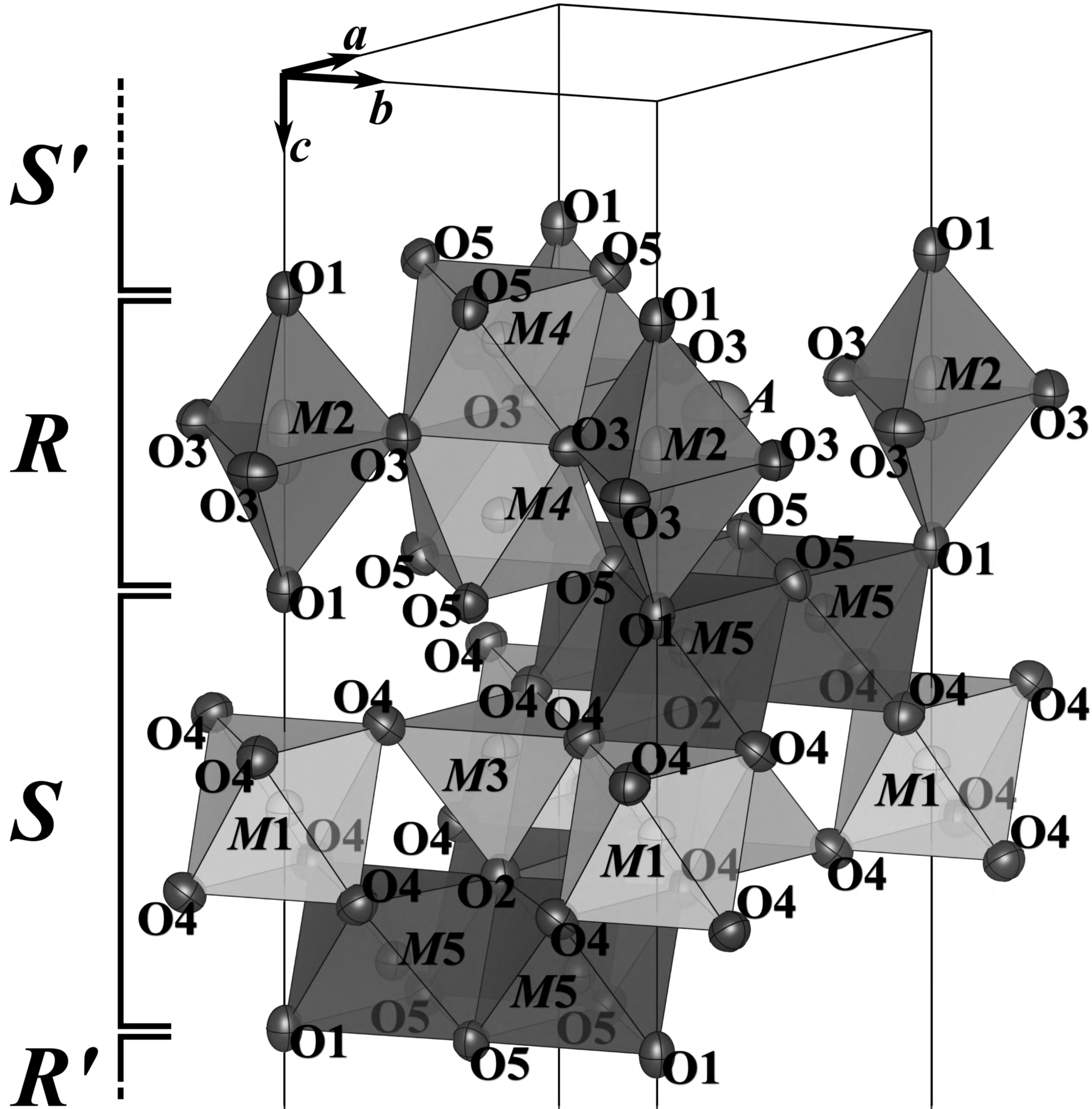
538 **Table 4.** Refined atomic coordinates, displacement parameters and angle variations for the analyzed
 539 hibonites.

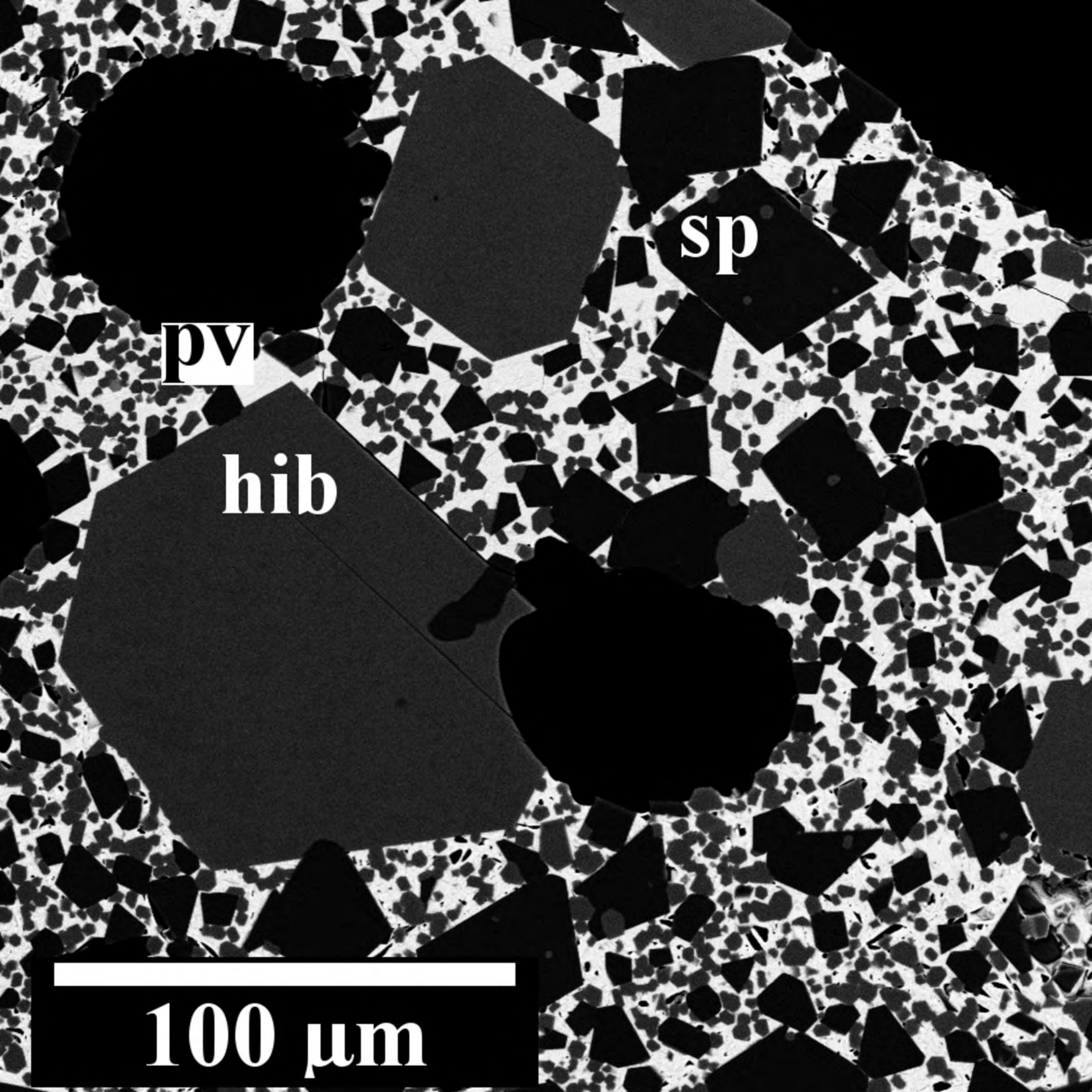
Site	Wyck. [†]	Sym. [#]	Ref. [*]	HBMT5	gel4-1	gel6-1	gel6-3
A	<i>2d</i>	$\bar{6}m2$	<i>x</i>	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
			<i>y</i>	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
			<i>z</i>	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{4}$
			<i>U_{eq}</i>	0.0213(2)	0.0212(4)	0.0272(3)	0.0288(4)
M1	<i>2a</i>	$\bar{3}m$	<i>x</i>	0	0	0	0
			<i>y</i>	0	0	0	0
			<i>z</i>	0	0	0	0
			<i>U_{eq}</i>	0.0066(3)	0.0070(4)	0.0058(3)	0.0062(3)
			OAV	14.22	11.93	22.69	24.23
M2	<i>4e</i>	<i>3m.</i>	<i>x</i>	0	0	0	0
			<i>y</i>	0	0	0	0
			<i>z</i>	0.2414(2)	0.2407(2)	0.2414(2)	0.2411(2)
			<i>U₃₃</i>	0.017(3)	0.006(4)	0.022(3)	0.023(2)
			<i>U_{eq}</i>	0.0097(9)	0.006(1)	0.010(1)	0.013(1)
			<i>s.o.f.</i>	0.10(1)	0.04(1)	0.13(2)	0.18(2)
M3	<i>4f</i>	<i>3m.</i>	<i>x</i>	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
			<i>y</i>	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
			<i>z</i>	0.02785(4)	0.02783(6)	0.02731(5)	0.02727(5)
			<i>U_{eq}</i>	0.0069(2)	0.0074(3)	0.0081(2)	0.0091(3)
M4	<i>4f</i>	<i>3m.</i>	<i>x</i>	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
			<i>y</i>	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
			<i>z</i>	0.19019(3)	0.19036(6)	0.18895(4)	0.18912(3)
			<i>U_{eq}</i>	0.0063(3)	0.0060(4)	0.0060(3)	0.0065(2)
			<i>s.o.f.</i>	0.115(6)	0.07(1)	0.32(1)	0.413(8)
M5	<i>12k</i>	<i>.m.</i>	<i>x</i>	0.16823(5)	0.16835(8)	0.16748(6)	0.16751(7)
			<i>y</i>	0.33646(9)	0.3367(2)	0.3350(1)	0.3350(1)
			<i>z</i>	0.89148(2)	0.89138(4)	0.89247(3)	0.89273(3)

			U_{eq}	0.0064(2)	0.0068(3)	0.0063(2)	0.0065(2)
			OAV	32.49	33.58	29.02	29.19
O1	4e	3m.	x	0	0	0	0
			y	0	0	0	0
			z	0.14956(9)	0.1493(2)	0.1503(1)	0.1504(1)
			U_{eq}	0.0076(4)	0.0071(7)	0.0078(4)	0.0081(5)
O2	4f	3m.	x	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$
			y	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
			z	0.94399(9)	0.9444(2)	0.9421(1)	0.9420(1)
			U_{eq}	0.0082(4)	0.0094(7)	0.0083(4)	0.0091(5)
O3	6h	mm2	x	0.1808(2)	0.1808(3)	0.1808(2)	0.1802(2)
			y	0.3616(3)	0.3616(5)	0.3617(4)	0.3603(4)
			z	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$
			U_{eq}	0.0091(4)	0.0090(5)	0.0093(4)	0.0106(4)
O4	12k	.m.	x	0.1542(1)	0.1545(2)	0.1524(2)	0.1518(2)
			y	0.3083(2)	0.3090(4)	0.3048(3)	0.3036(3)
			z	0.05254(6)	0.05222(9)	0.05323(6)	0.05325(6)
			U_{eq}	0.0083(3)	0.0085(4)	0.0092(3)	0.0094(3)
O5	12k	.m.	x	0.50359(9)	0.5036(2)	0.5041(1)	0.5048(1)
			y	0.0072(2)	0.0072(4)	0.0082(3)	0.0096(3)
			z	0.14956(6)	0.14941(9)	0.14983(6)	0.14986(6)
			U_{eq}	0.0076(3)	0.0077(4)	0.0070(3)	0.0080(3)
(Ti_{tot})_{a.p.f.u.}**				0.33(2)	0.18 (3)	0.78(3)	1.01(2)

[†]Wyckoff symbol; [#]Site symmetry; ^{*} Refined values: U_{33} [\AA^2], U_{eq} [\AA^2] and *s.o.f.* = site occupancy factor; the OAV=octahedral angle variance is expressed in deg; ^{**}Ti content per formula unit calculated from Ti *s.o.f.* for M2 and M4 sites.

540
541





pv

sp

hib

100 μm

