

1 **The sound velocity measurements of Fe₃S**

2 Revision 1

3 Seiji Kamada^{1,2,*}, Eiji Ohtani¹, Hiroshi Fukui^{3,4}, Takeshi Sakai¹, Hidenori Terasaki^{1,5},
4 Suguru Takahashi¹, Yuki Shibasaki¹, Satoshi Tsutsui⁶, Alfred Q. R. Baron^{3,6}, Naohisa
5 Hirao⁶, and Yasuo Ohishi⁶

6 1: Department of Earth and Planetary Materials Science, Graduate School of Science,
7 Tohoku University, Sendai, 980-8578, Japan.

8 2: Department of Geology, University of Illinois at Urbana-Champaign, 1301 West
9 Green street, Urbana, IL, 61801.

10 3: Materials Dynamics Laboratory, RIKEN SPring-8 Center, 1-1-1 Kouto, Sayo
11 679-5148, Japan.

12 4: Graduate School of Material Science, University of Hyogo, 3-2-1, Kamigori, Hyogo
13 678-1279, Japan.

14 5: Department of Earth and Space Science, Graduate School of Science, Osaka
15 University, Osaka 560-0043, Japan.

16 6: Japan Synchrotron Radiation Research Institute, Sayo, Hyogo 679-5198, Japan.

17

18 *: corresponding author

19

20 **Abstract**

21 **We measured the sound velocity of Fe₃S at room temperature up to 85 GPa**
22 **employing inelastic X-ray scattering in order to better constrain the constitution of**
23 **the inner core. The density of Fe₃S was also determined by X-ray diffraction under**
24 **the same conditions. The relation of the P-wave velocity (V_p) and density (ρ) of**

25 **Fe₃S follows Birch's law, $V_P[\text{m/s}] = 1.14(5) \times \rho[\text{kg/m}^3] - 2580(410)$. Based on**
26 **Birch's law determined here for Fe₃S and that for ϵ -Fe reported previously, we**
27 **found that sulfur decreases both density and compressional velocity of hcp-Fe at**
28 **the core pressure and 300 K.**

29

30 **Keyword: Fe₃S, inner core, sound velocity, Birch's law, inelastic X-ray scattering.**

31

32 **Introduction**

33 The Earth's core has been studied seismologically, and seismic wave velocities
34 and the density of the core are important observable properties (e.g., Birch 1964;
35 Dubrovinsky et al. 2000). According to these studies, the inner core is less dense than
36 pure iron, and it has been accepted that the inner core is comprised of iron and light
37 elements (e.g., Poirier 1994). Sound velocity data are more accurate than density in
38 seismology and can provide important constraints on the structure and composition of
39 the inner core (e.g., Badro et al. 2007; Cao et al. 2005; Song and Helmberger 1998). In
40 spite of their importance, the sound velocity data of the core materials at high pressure
41 are still very limited due to technical difficulties although many experiments to
42 constrain the density of the inner core have been carried out using in situ X-ray
43 diffraction (e.g., Chen et al. 2007).

44 Sulfur has been suggested as one of the most plausible light elements in the
45 Earth's core (e.g., Campbell et al. 2007; Seagle et al. 2006). The S content in the core is
46 estimated to be at least a few weight per cent (Hillgren et al. 2000; McDonough 2003).
47 In previous work, phase relationships in the Fe–FeS system under high pressures were
48 investigated (e.g., Fei et al. 2000; Kamada et al. 2010). Kamada et al. (2010) confirmed

49 that Fe₃S is stable with ε-Fe up to 220 GPa, and Fe₃S is therefore one of the candidates
50 of the inner-core materials. The compression behavior of Fe₃S was investigated up to 80
51 GPa (Seagle et al. 2006; Chen et al. 2007). Chen et al. (2007) estimated the S content to
52 be 12.5–20.7 at% (7.9–13.0 wt%) in the outer core and 2.2–6.2 at% (1.4–3.7 wt%) in
53 the inner core. Other studies have investigated the sound velocities, V_P, of iron and
54 iron–light-element alloys (e.g., Antonangeli et al. 2004; Badro et al. 2007; Fiquet et al.
55 2001). Although sound velocities of FeS and FeS₂ have been measured according to
56 inelastic X-ray scattering (IXS), there are very limited data for Fe₃S. FeS and FeS₂ may
57 not be appropriate for the inner core materials because the Fe–S system has several
58 iron-rich intermediates such as Fe₃S₂, Fe₂S, Fe₃S coexisting with Fe and high pressure
59 polymorphs in FeS at high pressure (Fei et al. 1995). Only Fe₃S coexists with ε-Fe
60 under the core conditions as a subsolidus phase (Kamada et al. 2010, 2012). Therefore,
61 it is essential to study V_P of Fe₃S to understand the seismic and chemical properties of
62 the Earth’s core. Lin et al. (2004) studied V_P of Fe₃S up to 57 GPa employing NIS
63 (Nuclear Resonance Inelastic X-ray scattering) and found that it follows Birch’s law,
64 which suggest the linear relationship between density and sound velocity (Birch 1961).
65 They also reported that the sound velocity of Fe₃S changes significantly across the
66 magnetic transition occurred at approximately 21 GPa. However the application of the
67 results to the earth’s core was not made due to a narrow pressure interval of their NIS
68 measurements. In this research, we measured V_P of Fe₃S based on inelastic X-ray
69 scattering method up to 85 GPa.

70

71 **Experimental method**

72 The starting material of Fe₃S was synthesized by a multianvil press from a

73 mixture of powdered Fe (99.9% purity) and FeS (99.9% purity) with the ratio of Fe:S =
74 85:15 (wt%). The synthesis conditions were 21 GPa and temperatures between 1263 K
75 and 1553 K. The sample was first compressed to 21 GPa at room temperature and then
76 heated above the melting temperature at 1533 K for 5 min to homogenize the mixture.
77 The temperature was then lowered to 1413 K and kept at that temperature for 30 min to
78 crystallize Fe₃S from the Fe–S liquid. The temperature was then reduced to 1263 K and
79 kept at that temperature for 1 h for the growth of the Fe₃S crystals. The chemical
80 composition of the recovered sample was determined to be Fe_{73.4(0.1)}S_{26.6(0.1)} (in at%)
81 using a scanning electron microscope with energy dispersive X-ray spectroscopy and its
82 back scattered image is shown in Figure 1. A small fragment of the recovered sample
83 was used for inelastic X-ray scattering (IXS) experiments at high pressures.

84 A symmetric diamond anvil cell was used to generate high pressure. The culet
85 sizes of the diamond anvils were 200, 350, and 400 μm, respectively. A sample was
86 loaded into the hole of a pre-indented rhenium gasket, which was typically about 50 μm
87 thick. The diameter of the sample chamber was 60–100 μm. The sample was
88 sandwiched between NaCl pellets, which served as the pressure-transmitting medium, a
89 thermal insulator, and a pressure scale. A double-sided laser heating method using fiber
90 lasers was used for annealing. The sample was compressed to the target pressure at
91 room temperature, and then annealed at around 1500–2000 K depending on each
92 experimental pressure at BL10XU of SPring-8, Japan (Ohishi et al. 2008). After
93 annealing, XRD patterns were taken at the beamline BL10XU, SPring-8. The diameter
94 of the X-ray beam was collimated to be 15 μm. The typical X-ray wavelength used was
95 0.41348(7) Å. An imaging plate was used as an X-ray detector. The typical exposure
96 time was 10 min. Each integrated X-ray profile along with the 2θ angle was analyzed

97 using the WinPIP software package (Fujihisa 1999, 2005; Fujihisa and Aoki 1998), and
98 the PD Indexer software package (Seto et al. 2010) and the existence of Fe₃S and
99 absence of other impurities were confirmed in all starting samples for the present
100 high-pressure experiments. The density of Fe₃S was measured for the same high
101 pressure cell assembly before or after each IXS measurement using X-ray diffraction
102 (XRD) for the same samples at BL10XU, SPring-8. The pressure was determined from
103 the equation of states (EOS) of NaCl B1/B2 phases (Fei et al. 2007; Matsui et al. 2009).

104 IXS experiments were performed at BL35XU, SPring-8, Japan (Baron et al.
105 2000). The sample was placed in the diamond anvil cell which was set, in a helium gas
106 atmosphere, on the Eulerian cradle of the IXS spectrometer. Focusing with a pair of
107 Kirkpatrick–Baez mirrors reduced the beam size to about 15 μm vertically by 17 μm
108 horizontally (full width at half maximum). The energy resolution was 3.0 meV FWHM
109 at 17.795 keV using the Si (999) reflection. A 3 × 4 array of spherical analyzer crystals
110 was set at the end of the 10-m horizontal arm to analyze the scattered X-rays with 12
111 different scattering vectors. Energy scans at constant momentum transfer were carried
112 out by varying the energy of the X-rays incident on the sample. The momentum
113 resolution was set by slits in front of the analyzers to about 0.38–0.41 nm⁻¹, full width.
114 Each set of spectra was collected for 8–10 h. The Stokes scattering contributed by LA
115 phonons was fitted with a Lorentzian function to obtain the energy position at each
116 momentum transfer, Q . Using the 12-crystal analyzers, we can obtain the relationship
117 between momentum transfer and energy of acoustic phonons across the first Brillouin
118 zone. Because polycrystalline Fe₃S was used as a sample, the V_p measured was
119 orientation-averaged.

120

121 **Results and discussion**

122 The IXS from Fe₃S was measured in the pressure ranging from 23.8 to 84.5
123 GPa. The experimental conditions and results are summarized in Table 1. Examples of
124 IXS spectra at different pressures and their fitting results are shown in Figure 2. The
125 peak observed at zero energy in each spectrum relates to elastic scattering from the
126 sample. Open diamonds represent peak positions of transverse acoustic (TA) phonons
127 from a diamond anvil. Because diamond has high sound velocities, TA phonon peaks
128 were observed at higher energy and only low Q conditions. Solid diamond symbols
129 represent peak positions of LA phonons of Fe₃S. Each peak energy position was
130 obtained by fitting a Lorentzian function to the peak.

131 Each dispersion relationship between energy and momentum transfers was
132 fitted using eq. (1), and the dispersion curves obtained are shown in Figure 3.

133
$$E[\text{meV}] = 4.192 \times 10^{-4} V_P [\text{m} \cdot \text{s}^{-1}] \times Q_{MAX} [\text{nm}^{-1}] \times \sin \left[\frac{\pi}{2} \frac{Q[\text{ns}^{-1}]}{Q_{MAX}[\text{ns}^{-1}]} \right], \quad (1)$$

134 where E and Q are the energy and momentum transfers to the phonon and V_P is the
135 sound velocity of the sample. V_P and Q_{MAX} are free parameters. The results are
136 summarized in Table 1. The energy of the Fe₃S LA phonon at the same Q increases with
137 increasing pressure, indicating that V_P increases with increasing pressure.

138 The results of this study are plotted as a function of density in Figure 4 together
139 with results from previous studies. The compressional velocity and density of the inner
140 core for the preliminary reference Earth model (PREM) (Dziewonski and Anderson
141 1981) are also plotted in this figure. The present data are plotted in the figure together
142 with previous studies. The slopes of Birch's law decrease with decreasing the amount of
143 sulfur in iron sulfides. The slope of Fe₃S is similar to that of Fe. The present velocities

144 are consistent with those of Lin et al. (2004) and follow Birch's law (Birch 1961) as
145 shown in Figure 4. The linear relationship between density and sound velocity was
146 obtained by combining the data from the present study with those from Lin et al. (2004),

$$147 \quad V_p[\text{m/s}] = 1.14(5) \times \rho[\text{kg/m}^3] - 2580(410) \quad (R^2 = 0.983), \quad (2)$$

148 where ρ is the density of Fe_3S .

149 Theoretical calculations using the *ab initio* method (Sha and Cohen 2010;
150 Vočadlo et al. 2009) revealed a large temperature effect on Birch's law above 2,000 K.
151 Recent IXS measurement of ϵ -Fe (Antonangeli et al. 2012; Mao et al. 2012) revealed
152 that the density- V_p relation significantly deviates from the shock compression data
153 suggesting a large temperature dependency of Birch's law, although the effect of
154 temperature is negligible in the lower temperature range. V_p and density of hcp-Fe
155 measured at 300 K (Antonangeli et al. 2012; Mao et al. 2012) and calculated
156 theoretically (Sha and Cohen 2010; Vočadlo et al. 2009) at 0 K provide Birch's law for
157 hcp-Fe as follows:

$$158 \quad V_p[\text{m/s}] = 1.18(4) \times \rho[\text{kg/m}^3] - 3660(430) \quad (R^2 = 0.986). \quad (3)$$

159 Comparing with equations (2) and (3), we can evaluate the effect of sulfur in
160 Birch's law for hcp-Fe at 300 K. Figure 4 shows the density and compressional velocity
161 of Fe_3S and hcp-Fe at the core pressures of 136 GPa and 330 GPa at 300 K. This figure
162 clearly indicates that both density and compressional velocity of Fe_3S at 300 K and the
163 same pressure are smaller than those of hcp-Fe, indicating a light element, S, reduces
164 both density and compressional velocity of the iron inner core.

165 The compressional velocity and density relations for Fe_3S and hcp-Fe given in
166 equations (2) and (3) indicate that both curves of Birch's law locate above those of the

167 PREM inner core. Birch's law of Fe₃S and hcp-Fe at 300 K indicates that the PREM
168 compressional velocity of the inner core can be explained by two ways, i.e., hcp-Fe and
169 Fe₃S have large temperature effects on Birch's law or the inner core contains heavy
170 elements with a negligible temperature effect on Birch's law. We calculated V_S based
171 on the equation of state of Fe₃S reported by Seagle et al. (2006) and Chen et al. (2007).
172 The calculated V_S at the inner core is much faster than that of the PREM inner core at
173 the inner core boundary assuming no temperature dependency in Birch's law.

174 Although there are some controversies in the experimental results on existence
175 of temperature dependence on Birch's law (Antonangeli et al. 2012; Lin et al. 2005;
176 Mao et al. 2012), recent theoretical calculations and shock wave experiments (Brown
177 and McQueen 1981) indicate existence of large temperature dependence in Birch's law
178 at temperatures above 2000 K. We need to determine experimentally the sound velocity
179 at temperature above 2000 K, and the temperature dependence on Birch's law to the
180 core conditions in order to estimate the amount of sulfur in the inner core.

181

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195 **References**

- 196 Antonangeli, D., Occelli, F., Requardt, H., Badro, J., Fiquet, G., and Krisch, M. (2004)
197 Elastic anisotropy in textured hcp-iron to 112 GPa from sound wave propagation
198 measurements. *Earth and Planetary Science Letters*, 225, 243–251.
- 199 Antonangeli, D., Komabayashi, T., Occelli, F., Borissenko, E., Walters, A.C., Fiquet, G.,
200 and Fei, Y. (2012) Simultaneous sound velocity and density measurements of hcp
201 iron up to 93 GPa and 1110 K: An experimental test of the Birch’s law at high
202 temperature. *Earth and Planetary Science Letters*, 331–332, 210–214.
- 203 Badro, J., Fiquet, G., Guyot, F., Gregoryanz, E., Occelli, F., Antonangeli, D., and
204 d’Astuto, M. (2007). Effect of light elements on the sound velocities in solid iron:
205 Implications for the composition of Earth’s core. *Earth and Planetary Science*
206 *Letters*, 254, 233–238.
- 207 Baron, A. Q. R., Tanaka, Y., Goto, S., Takeshita, K., Matsushita, T., and Ishikawa, T.
208 (2000) An X-ray scattering beamline for studying dynamics. *Journal of Physics*
209 *Chemistry of Solids*, 61, 461–465.
- 210 Birch, F. (1961) Composition of the Earth’s mantle. *Geophysical Journal of the Royal*
211 *Astronomical Society*, 4, 295–311.
- 212 Birch, F., 1964. Density and composition of mantle and core. *Journal of Geophysical*
213 *Research*, 69(20), 4377–4388.
- 214 Brown, J. M. and McQueen, R. G. (1986) Phase transitions, Grüneisen parameter, and

- 215 elasticity for shocked iron between 77 GPa and 400 GPa. *Journal of Geophysical*
216 *Research*, 91(B7), 7485–7494.
- 217 Campbell, A. J., Seagle, C. T., Heinz, D. L., Shen, G., and Prakapenka, V. B. (2007)
218 Partial melting in the iron–sulfur system at high pressure: A synchrotron X-ray
219 diffraction study. *Physics of Earth and Planetary Interiors*, 162, 119–128.
- 220 Cao, A., Romanowicz, B., Takeuchi, N. (2005) An observation of PKJKP: Inferences
221 on inner core shear properties. *Science*, 308, 1453–1455.
- 222 Chen, B., Gao, L., Funakoshi, K., and Li, J. (2007) Thermal expansion of iron-rich
223 alloys and implications for the Earth’s core. *Proceedings of the National Academy*
224 *of Sciences*, 104(22), 9162–9167.
- 225 Dubrovinsky, L. S., Saxena, S. K., Tutti, F., Rekh, S., LeBehan, T., 2000. *In situ* X-ray
226 study of thermal expansion and phase transition of iron at multimegabar Pressure.
227 *Physical Review Letters*, 84(8), 1720–1723.
- 228 Dziewonski, A. M. and Anderson, D. L. (1981) Preliminary reference Earth model.
229 *Physics of Earth and Planetary Interiors*, 25, 297–356.
- 230 Fei, Y., Prewitt, C. T., Mao, H.-K., and Bertka, C. M. (1995) Structure and density of
231 FeS at high pressure and high temperature and the internal structure of Mars.
232 *Science*, 268, 1892–1894.
- 233 Fei, Y., Li, J., Bertka, C. M., and Prewitt, C. T. (2000) Structure type and bulk modulus
234 of Fe₃S, a new iron–sulfur compound. *American Mineralogist*, 85, 1830–1833.
- 235 Fei, Y., Ricolleau, A., Frank, M., Mibe, K., Shen, G., and Prakapenka, V. (2007)
236 Toward an internally consistent pressure scale. *Proceedings of the National*
237 *Academy of Sciences*, 104(22), 9182–9186.
- 238 Fiquet, G., Badro, J., Guyot, F., Requardt, H., and Krisch, M. (2001) Sound velocities in

- 239 iron to 110 gigapascals. *Science*, 291, 468–471.
- 240 Fujihisa, H. (1999) An X-ray powder pattern analysis program for imaging plate. *The*
241 *Review of high pressure science and technology*, 9(1), 65–70 (in Japanese).
- 242 Fujihisa, H. (2005) Recent progress in the powder X-ray diffraction image analysis
243 program PIP. *The Review of high pressure science and technology*, 15(1), 29–35
244 (in Japanese).
- 245 Fujihisa, H., and Aoki, K. (1998) High pressure X-ray powder diffraction experiments
246 and intensity analysis. *The Review of high pressure science and technology*, 8(1),
247 4–9 (in Japanese).
- 248 Hillgren V., Gessmann, C. K., and Li, J. (2000) An experimental perspective on the
249 light element in Earth's core. In Canup, R. M., Righter, K., Eds., *Origin of the*
250 *Earth and Moon*, p. 245–263. The University of Arizona, Arizona.
- 251 Kamada, S., Terasaki, H., Ohtani, E., Sakai, T., Kikegawa, T., Ohishi, Y., Hirao, N.,
252 Sata, N., Kondo, T. (2010) Phase relationships of the Fe–FeS system in conditions
253 up to the Earth's outer core. *Earth and Planetary Science Letters*, 294, 94–100.
- 254 Kamada, S., Ohtani, E., Terasaki, H., Sakai, T., Miyahara, M., Ohishi, Y., and Hirao, N.
255 (2012) Melting relationships in the Fe–Fe₃S system up to the outer core conditions.
256 *Earth and Planetary Science Letters*, 359–360, 33–40.
- 257 Lin, J.-F., Fei, Y., Sturhahn, W., Zhao, J., Mao, H. K., and Hemley, R. J. (2004)
258 Magnetic transition and sound velocities of Fe₃S at high pressure: Implications for
259 Earth and planetary cores. *Earth and Planetary Science Letters*, 226, 33–40.
- 260 Lin, J.-F., Sturhahn, W., Zhao, J., Shen, G., Mao, H.-K., and Hemley, R.J. (2005) Sound
261 velocities of hot dense iron: Birch's law revisited. *Science*, 308, 1892–1894.
- 262 Mao, Z., Lin, J.-F., Liu, J., Alatas, A., Gao, L., Zhao, J., and Mao, H.-K. (2012) Sound

- 263 velocities of Fe and Fe-Si alloy in the Earth's core. Proceedings of the National
264 Academy of Sciences, 109, 10239–10244.
- 265 Matsui, M. (2009) Temperature–pressure–volume equation of state of the B1 phase of
266 sodium chloride. Physics of Earth and Planetary Interiors, 174, 93–97.
- 267 McDonough, W. F. (2003) Compositional model for the Earth's core, In R.W. Carlson
268 Ed., Treatise on Geochemistry, p. 547–568. Elsevier, Oxford.
- 269 Ohishi, Y., Hirao, N., Sata, N., Hirose, K., and Takata, M. (2008) Highly intense
270 monochromatic X-ray diffraction facility for high-pressure research at SPring-8.
271 High Pressure Research, 28(3), 163–173.
- 272 Poirier J. P., 1994. Light elements in the Earth's outer core: A critical review. Physics of
273 Earth and Planetary Interiors, 85, 319–337.
- 274 Seagle, C. T., Campbell, A. J., Heinz, D. L., Shen, G., and Prakapenka, V. B. (2006)
275 Thermal equation of state of Fe₃S and implications for sulfur in Earth's core.
276 Journal Geophysical Research, 111, B06209.
- 277 Seto, Y., Hamane, D., Nagai, T., and Sata, N. (2010) Development of a software suite
278 on X-ray diffraction experiments. The Review of high pressure science and
279 technology, 20(3), 269–276 (in Japanese).
- 280 Sha, X. and Cohen, R. E. (2010) Elastic isotropy of ϵ -Fe under Earth's core conditions.
281 Geophysical Research Letters, 37, L10302.
- 282 Song X., Helmberger, D. V., 1998. Seismic evidence for an inner core transition zone.
283 Science, 282, 924–927.
- 284 Vočadlo, L. (2007) Ab initio calculations of the elasticity of iron and iron alloys at inner
285 core conditions: Evidence for a partially molten inner core? Earth and Planetary
286 Science Letters, 254, 227–232.

287 Vočadlo, L., Dobson, D. P., and Wood, I. G. (2009) Ab initio calculations of the
288 elasticity of hcp-Fe as a function of temperature. Earth and Planetary Science
289 Letters, 288, 534–538.

290

291 **Figure captions**

292

293 Figure 1. Back scattered electron image of the synthesized Fe₃S. We can see only Fe₃S
294 in this figure and the chemical analysis using EDS showed the composition of
295 Fe_{73.4(0.1)}S_{26.6(0.1)}.

296

297 Figure 2. Examples of IXS spectra taken in this study at 23.8 and 84.5 GPa. Open
298 diamond symbols represent peak positions of TA phonons of diamond. Solid diamond
299 symbols show peak positions of LA phonons of Fe₃S. The grey curve, grey dotted curve,
300 grey dashed curve, and dot-dashed curve represent fitting results for Fe₃S (LA), elastic,
301 diamond (TA) peaks, and diamond (LA) peak respectively.

302

303 Figure 3. Dispersion curves of the longitudinal acoustic phonon branch of Fe₃S at
304 pressures from 23.8 to 84.5 GPa and room temperature.

305

306 Figure 4. V_p plotted against density. Open and solid squares represent the data of Fe₃S
307 from this study and those from Lin et al. (2004), respectively. Solid and open upward
308 triangles represent results of ε-Fe from Mao et al. (2012) and Antonangeli et al. (2012),
309 respectively. Solid and open downward triangles are data of FeS reported by Vočadlo
310 (2007) based on ab initio calculation and Badro et al. (2007) based on IXS, respectively.

311 Open diamonds represent data of FeS₂ reported by Badro et al. (2007). Solid diamonds
312 are the data calculated theoretically (Vočadlo et al., 2009; Sha and Cohen, 2010). The
313 crosses are V_P values of the PREM inner core (Dziewonsk and Anderson, 1981). The
314 dashed line represents Birch's law for Fe₃S, and expressed by equation (2) in the text,
315 whereas the solid line represents that for ε-Fe expressed by equation (3). Open circles
316 are V_P of ε-Fe and Fe₃S under the core conditions with error bars. The dotted dashed
317 line and long dash line are Birch's law for FeS₂ (Badro et al., 2007) and FeS (Badro et
318 al., 2007; Vočadlo, 2007), respectively.

319

320 **Table 1.** Experimental conditions and results.

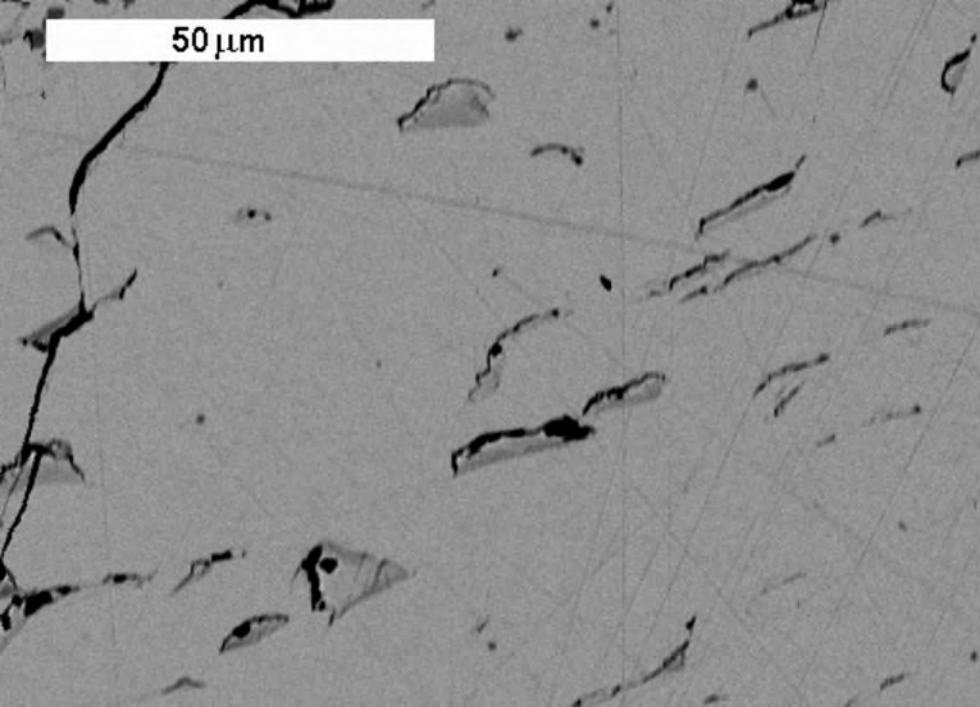
Run number	P ^c [GPa]	T [K]	ρ ^d [kg/m ³]	V _P ^e [m/s]
IXSFE3S03 ^a	23.8(10)	300	8060(20)	6660(80)
IXSFE3S02_01 ^b	35.2(35)	300	8340(20)	6950(190)
IXSFE3S04 ^a	52.9(38)	300	8870(30)	7460(170)
IXSFE3S02_02 ^b	55.1(16)	300	8960(10)	7650(60)
IXSFE3S07 ^a	56.5(9)	300	9030(30)	7640(200)
IXSFE3S08 ^a	67.4(5)	300	9200(20)	8090(270)
IXSFE3S10 ^c	84.5(17)	300	9610(30)	8310(50)

The numbers in parentheses show errors. a: λ=0.41348(7) Å, b: λ=0.41495(10) Å, b: λ=0.41300(9) Å
c: The pressure was the average of multiple measurements of a sample using the equation of state of NaCl(B1) or NaCl(B2) at 300 K after annealing. The pressure error is the standard deviation of multiple measurements.

d: The density of Fe₃S was the average of multiple measurements based on XRD patterns. The density error is the standard deviation of multiple measurements. e: V_P was obtained with free *Q_{MAX}*

321

50 μm



Intensity (a.u.)

