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1 **Subsolidus Isothermal Fractional Crystallization**

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9 **ABSTRACT**

10 In theory, multicomponent silicate liquids of minimum or eutectic composition should crystallize  
11 their solidus phases simultaneously and in their invariant proportions. In reality, the  
12 crystallization of those liquids of granitic composition produces sequential assemblages and  
13 normal fractional crystallization of solid solutions when crystallization commences at or along an  
14 isotherm well below the solidus of the system. The sequence of mineral assemblages derives  
15 principally from their relative stabilities, as measured by the Gibbs free energy change for the  
16 reaction of melt to crystals in the metastable region below the liquidus surface, rather than  
17 chemical concentration alone. Whereas crystallization close to the solidus ( $\Delta T \approx 50$  °C) promotes  
18 the simultaneous (eutectic) crystallization of quartz and feldspars that leads to the formation of  
19 granite, large liquidus undercooling ( $\Delta T \approx 200$  °C) produces sequential assemblages from the  
20 margins to centers of melt bodies. The liquidus undercooling that drives subsolidus isothermal  
21 fractional crystallization is the single-most important process for the generation of zoned granitic  
22 pegmatites.

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24 **KEY WORDS:** granite, pegmatite, liquidus undercooling, fractional crystallization, internal  
25 zonation

26

## 27 **LIQUIDUS RELATIONSHIPS IN THE GRANITE SYSTEM**

28 Though liquidus diagrams are utilized to model crystallization of initially crystal-free melts, all  
29 such diagrams are actually derived from thermally prograde partial melting experiments in which  
30 little or nothing crystallizes (Bowen 1928). This is because silicate liquids, and in particular  
31 viscous, high-silica liquids that correspond to the compositions of granites (*s.l.*), tend to persist  
32 metastably well below their liquidus or solidus (Fig. 1a), and hence are of little value in locating  
33 those phase boundaries upon cooling.

34

35 In the case of equilibrium crystallization, a melt of minimum or eutectic composition that cools  
36 to its solidus should crystallize quartz and alkali feldspars simultaneously in their invariant  
37 proportion. That crystallization will not take place precisely at the temperature of the minimum  
38 or eutectic because some degree of supersaturation is necessary to initiate the nucleation and  
39 continued growth of crystals. For igneous systems, the most common cause of supersaturation is  
40 cooling (Fig. 1a); undercooling of up to 50 °C may be necessary to initiate crystallization in  
41 granitic liquids, irrespective of the rate of cooling or time at temperature (Fig. 1a). Within ~ 50-  
42 75 °C of the solidus, however, the driving force to crystallize quartz and feldspar is nearly  
43 equivalent (Fig. 1b), and hence there is a nearly equal probability that both will crystallize  
44 simultaneously, as is the general case for granite. Pegmatites of essentially the same granitic  
45 composition are now known to begin their crystallization at ~ 450 °C, which is 280 °C ( $\Delta T$ )  
46 below the solidus of the hydrous granite system (Ab-Or-Qtz-H<sub>2</sub>O (Chakoumakos and Lumpkin

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47 1992; Morgan and London 1999; Webber et al. 1999; London 2008; London et al. 2012;  
48 Colombo et al. 2012). Equilibrium theory as it has been applied to pegmatites predicts that even  
49 at large undercooling, the crystalline product should be a simultaneous eutectic assemblage  
50 (Burnham and Nekavasil 1986).

51

## 52 **DYNAMIC CRYSTALLIZATION EXPERIMENTS**

53 Experiments that were aimed at assessing the crystallization response of felsic and granitic  
54 liquids as functions of undercooling were termed "*dynamic crystallization*" experiments (e.g.,  
55 Swanson 1977; Fenn 1977). London et al. (1989) conducted dynamic crystallization experiments  
56 with obsidian from Macusani, Peru; the composition of that obsidian is virtually identical to the  
57 Tanco rare-element pegmatite, Manitoba (Stilling et al. 2006). Melt containing 4 wt% H<sub>2</sub>O  
58 derived from the Macusani obsidian (saturated at ~ 10 wt% H<sub>2</sub>O) at 200 MPa was taken to its  
59 liquidus of ~ 750 °C, then cooled isobarically to 550°-575 °C ( $\Delta T = 175^\circ\text{-}200^\circ\text{C}$ ) before  
60 crystallization commenced. In all cases, the initial assemblage consists mostly of plagioclase  
61 (An<sub>12</sub>) that is more calcic than the bulk composition (An<sub>3</sub>). That calcic plagioclase (+ quartz ±  
62 zinnwaldite) evolves to albite (An<sub>2</sub>) – K-feldspar pairs (Fig. 2); compositions of the coexisting  
63 feldspars closely match the equilibrium solvus compositions at the P and T of the experiments.  
64 With continued crystallization in the H<sub>2</sub>O-undersaturated system, the melt fractionates toward a  
65 composition that is sodic, alkaline (in relation to measures of A/CNK or ASI), and enriched in  
66 fluxing components (B, P, and F), water (H), and rare alkalis (Li, Rb, Cs). However, that evolved  
67 melt composition first appears as a boundary layer of liquid adjacent to crystallization fronts (see  
68 Fig. 5a of London and Morgan 2012).

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70 Dynamic crystallization involving a 200 MPa minimum haplogranite composition (normative  
71 wt%  $\text{Ab}_{38.23}\text{Or}_{28.72}\text{Qtz}_{33.04}\text{Crn}_{0.01}$ ) with 3 wt%  $\text{B}_2\text{O}_3$  glass and no water added at  $450^\circ\text{C}$  ( $\Delta T \approx$   
72  $300^\circ\text{C}$ ) and 200 MPa (London 1999) produced mineralogical and textural zonation that strongly  
73 resemble the alternations found in pegmatites (London 2008, London et al. 2012). Inward from  
74 the margins to center (Fig. 3), the charge contains four textural - mineralogical zones: (1) graphic  
75 quartz-feldspar intergrowth, (2) crenulate layered aplite, (3) pure feldspar surrounding (4) a  
76 central core of pure quartz. Like pegmatites (London 2008; London et al. 2012), the outer and  
77 zones of that experiment contain less quartz (normative 26 wt%) than the bulk composition; the  
78 commensurate quartz content that brings the bulk composition to the minimum composition of  
79 granite lies in the pure quartz core.

80

81 In the same minimum-melt composition at 200 MPa  $\text{H}_2\text{O}$ , crystallization at  $\Delta T \approx 75^\circ\text{-}100^\circ\text{C}$   
82 produced skeletal K-feldspar crystals only (Evensen 2001). At larger undercooling ( $\Delta T \approx 150^\circ\text{-}$   
83  $200^\circ\text{C}$ ), the same skeletal K-feldspar crystals formed first, and were overgrowth by a graphic  
84 intergrowth of quartz and more sodic feldspar. At  $\Delta T = 250^\circ\text{C}$ , the sequence of crystallization  
85 began with skeletal K-feldspar, followed by spherulitic quartz-plagioclase intergrowths, and  
86 finally monomineralic quartz. A simultaneous assemblage of quartz and alkali feldspar in the  
87 proportions of the minimum was not obtained in any of the undercooled experiments in this  
88 series.

89

## 90 **SUBSOLIDUS ISOTHERMAL FRACTIONAL CRYSTALLIZATION**

91 Parsons (1969) may have been the first to observe that isobaric-isothermal subsolidus  
92 crystallization of solid solutions from undercooled melt produces a sequential evolution of

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93 mineral compositions that closely matches the anticipated fractionation sequence and line of  
94 descent on the liquidus. Parsons noted that the products of isothermal-isobaric crystallization  
95 may be indistinguishable from a normal liquidus fractionation trend. London (2008, p. 278-279)  
96 provided a theory to explain the behavior in the granite system. In the haplogranite system, the  
97 slopes of the liquidus surfaces for quartz and feldspars are not equivalent (Fig. 1b). Hence, their  
98 metastable extensions below the solidus diverge, to different extents, from the projection of the  
99 minimum or eutectic composition to the actual subsolidus temperature of crystallization. Along  
100 the liquidus surface, and at the minimum or eutectic, the free energy ( $\Delta G$ ) of the reactions  $\mu_{i,L}$   
101  $\rightarrow \mu_{i,XL}$ , which correspond to the chemical potentials of components in melt and their equivalent  
102 crystalline phases, is zero for all, and values of  $\Delta G$  become increasingly negative below the  
103 solidus. Relative to the composition and temperature of undercooling, however,  $-\Delta G$  is greater  
104 for some phases than for others, and for the high-temperature ends of solid solutions. For this  
105 reason, the driving force to crystallize phases is not equivalent at a temperature well below the  
106 solidus, and the first phase to crystallize is that whose free energy change ( $-\Delta G$ ) for the  
107 crystallization reaction is greatest. As a result, crystallization is sequential, even for minimum or  
108 eutectic liquid compositions.

109

110 Isothermal subsolidus fractional crystallization is a general consequence for any multi-  
111 component liquid that can persist metastably to temperatures well below its solidus before  
112 crystallization commences, and that can crystallize multiple phases (e.g., the haplogranite ternary  
113 system) or solid solutions (e.g., the plagioclase subsystem). As applied to pegmatites, the first  
114 phases to crystallize along the margin will be those species or solid solutions whose chemical  
115 potentials in the melt are highest at the undercooled state. Consequently, feldspars predominate

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116 over quartz, plagioclase precedes K-feldspar, and the most calcic plagioclase and mafic minerals,  
117 with their higher actual liquidus temperatures, crystallize first -- both in experiments and in  
118 nature.

119

## 120 **THE PEGMATITE PUZZLE**

121 In their landmark summary, Cameron et al. (1949) stated that crystallization in pegmatites is  
122 sequential, from the margins to center, “...as successive layers upon the walls of the chamber  
123 enclosing a body of pegmatitic liquid, and hence are due primarily to fractional crystallization”  
124 (Cameron et al. 1949, p. 105). As evidence, they cited the unidirectional solidification texture of  
125 crystals that expanded inward from margin to core, and the normal fractionation of plagioclase  
126 from An<sub>12</sub> at the margins to ~ An<sub>2</sub> at the center (Cameron et al. 1949, p 100). The salient  
127 features of a body of pegmatite, therefore, were reconciled to an igneous model using the  
128 principles inherent in Bowen’s (1928) concepts of fractional crystallization from silicate melts.

129

130 The problem, which Jahns (Jahns and Tuttle 1963; Jahns and Burnham 1969; Jahns 1982) later  
131 sought to address, was that the compositions of pegmatites are those of the eutectic proportions  
132 of granite, in which plagioclase, K-feldspar, and quartz should crystallize simultaneously in their  
133 invariant proportions. By regarding pegmatites as granitic liquids crystallizing at equilibrium,  
134 Jahns and Burnham (1969; Jahns 1982; Burnham and Nekvasil 1986) implicitly required that the  
135 crystallization of H<sub>2</sub>O-saturated, pegmatite-forming melts at mid-crustal pressures (~ 200-400  
136 MPa) occurs at temperatures close to that of the hydrous granite minimum, which is in the range  
137 of 650°-685 °C over this interval of pressure (Tuttle and Bowen 1958). The principal reason for  
138 the failure of the Jahns-Burnham model (London 2008) was its constraint of equilibrium

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139 crystallization on the liquidus of the hydrous granite system. That constraint has been removed  
140 with recent assessments of the actual conditions at which pegmatites crystallize.

141

142 In pegmatites, sequential (rather than simultaneous) crystallization of minimum or eutectic bulk  
143 compositions, and extended fractional crystallization of feldspars, including major and minor  
144 components, can now be reconciled to the process of subsolidus isothermal fractional  
145 crystallization. Other processes, including chemical diffusion, manifested by local and far-field  
146 chemical gradients (Morgan et al. 2008; London 2009, London et al. 2012; Acosta-Vigil et al.  
147 2012), are important as well. The salient features of pegmatites, however, can now be reproduced  
148 and explained in laboratory simulations that are appropriately scaled in P, T, bulk composition,  
149 and time through the crystallization of hydrous but not H<sub>2</sub>O-saturated, flux-bearing but not  
150 unusual granitic melts at liquidus undercooling of ~ 200°C.

151

152 **ACKNOWLEDGMENTS**

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159 Energy.

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221

222 **FIGURES**

- 223 Fig. 1. (a) Nucleation delay in the granite system for a minimum-melt composition (wt%  
224  $\text{Ab}_{25}\text{Or}_{25}\text{Qtz}_{33}\text{Crn}_{01}$ ) at 200 MPa  $\text{H}_2\text{O}$ . The solid parabolic curve denotes the time (t) –  
225 temperature (T) surface (at constant composition) upon which microscopic crystals appear.  
226 Dashed contours indicate the volume % of crystallization. From Evensen (2001) with  
227 additional data in London (2008). (b) T-X section through the haplogranite liquidus diagram  
228 at 200 MPa  $\text{H}_2\text{O}$ , from Tuttle and Bowen (1958), showing the relative magnitudes of free  
229 energy change for the reaction of melt to crystals ( $-\Delta G$ ) in relation to the magnitude of  
230 liquidus undercooling.

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231 Fig. 2. A representative experiment with Macusani glass + 3-4 wt% added H<sub>2</sub>O, preconditioned  
232 at 750 °C, followed by isobaric cooling to 500°-575 °C. Graphic plagioclase + quartz along the  
233 margins radiates inward to patchy crystals of K-feldspar and albite. Isolated albite crystals  
234 occur with Li-mica and abundant quartz in the center of the charge. From London et al.  
235 (1989). (Insert) Ternary feldspar solvi at 750 °C and 500 °C, 200 MPa, calculated from the  
236 program SOLVCALC (Wen and Nekvasil 1994). The red dot corresponds to the normative  
237 feldspar composition of the Macusani glass. From London (2008).

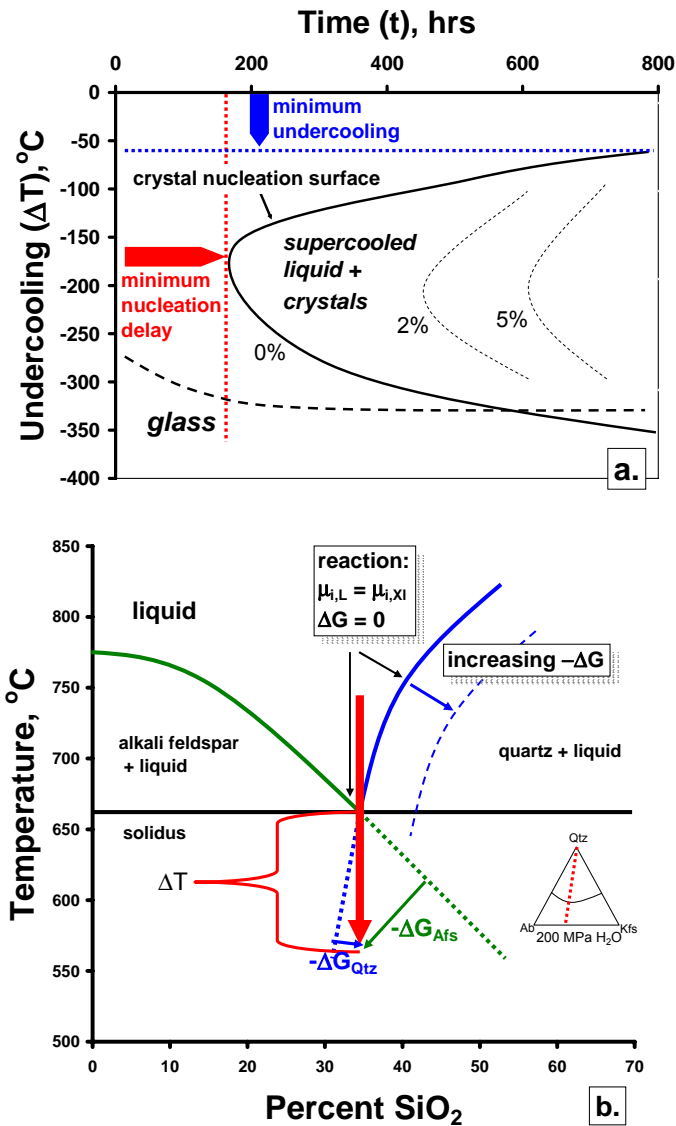
238 Fig. 3. Backscattered electron image of experiment PEG-16, consisting of haplogranite glass  
239 (Ab<sub>38.23</sub>Or<sub>28.72</sub>Qtz<sub>33.04</sub>Crn<sub>00.01</sub>) with 3 wt% B<sub>2</sub>O<sub>3</sub> glass and no water, which was conducted at  
240 450 °C ( $\Delta T \approx 300$  °C) and 200 MPa. Red arrows show the direction of crystallization inward  
241 from margins to center. From London (1999).

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243 Fig. 1

244

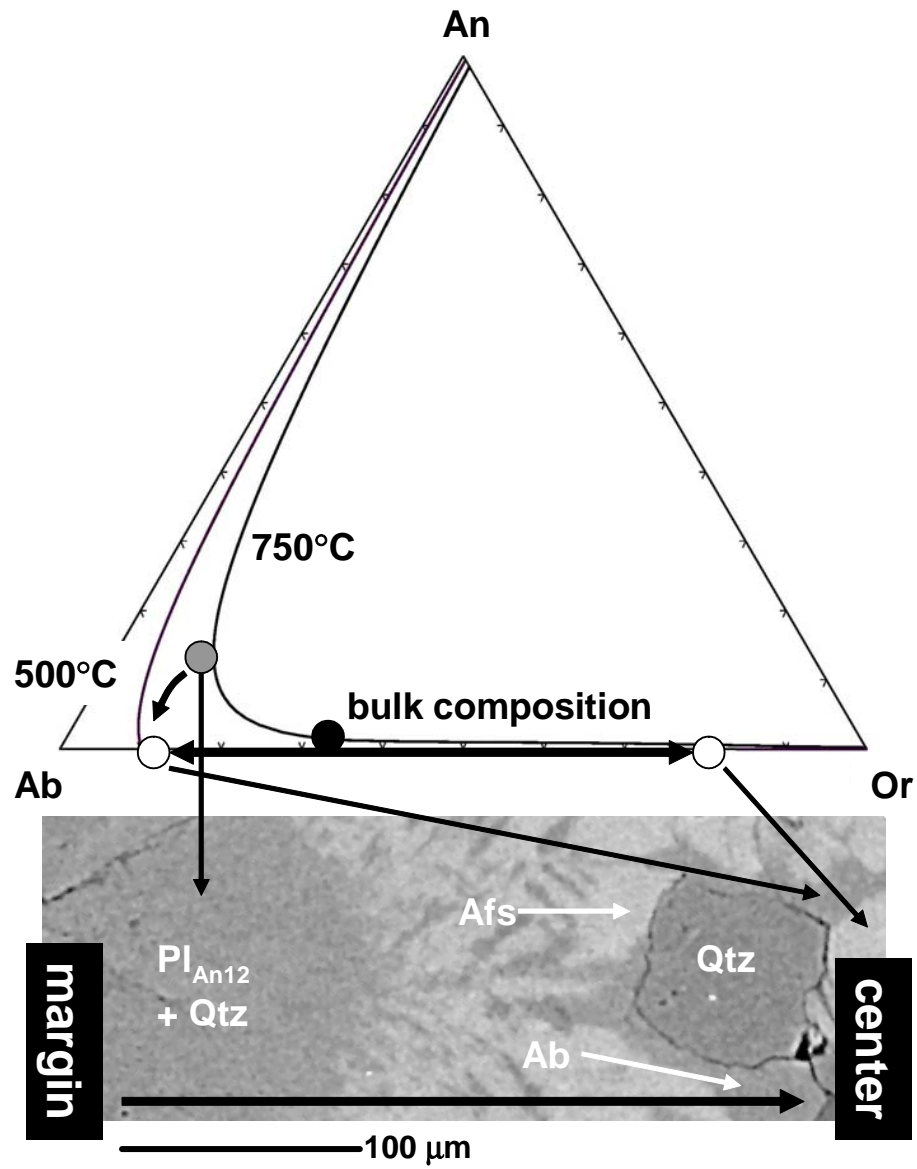


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245 Fig. 2

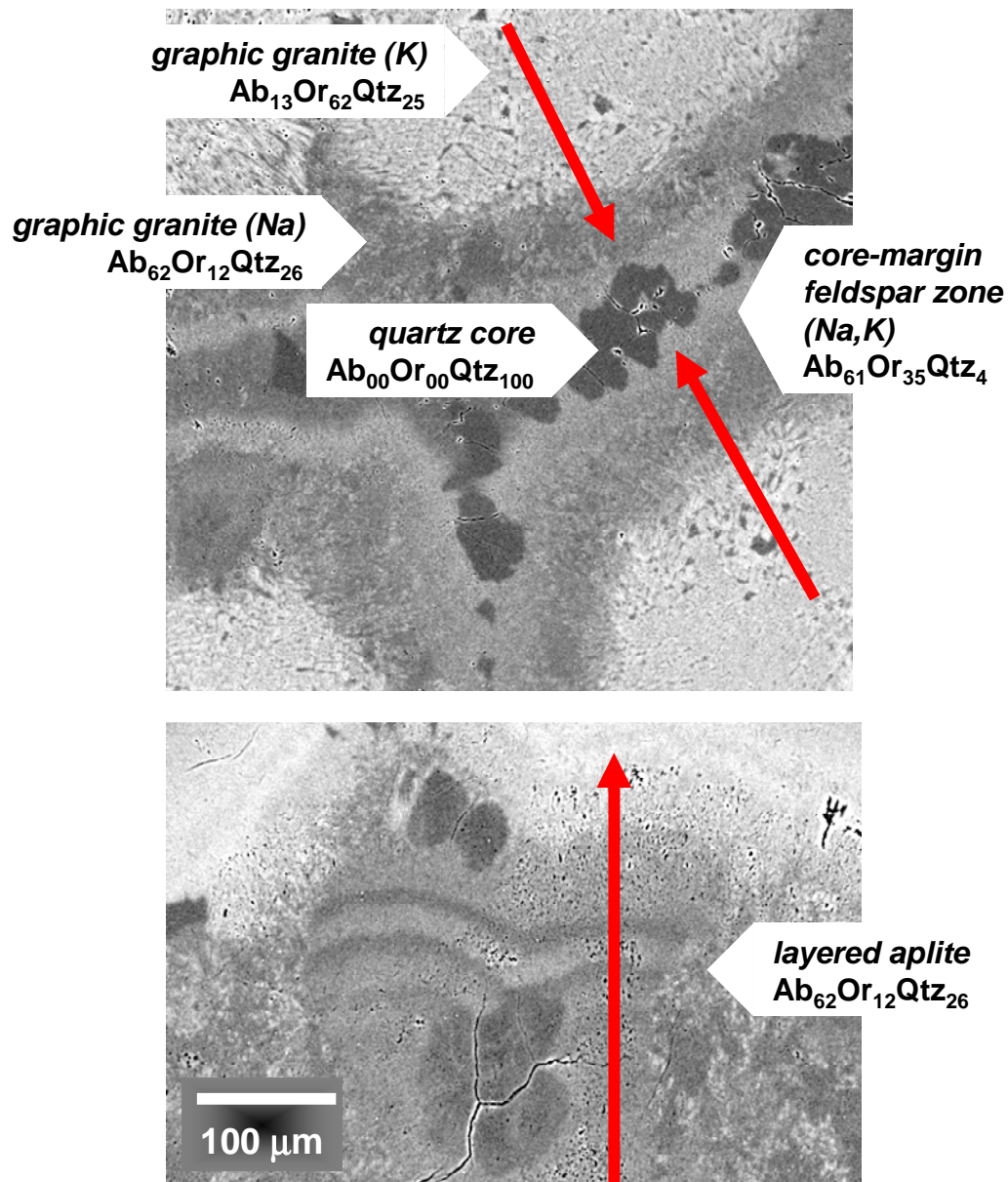
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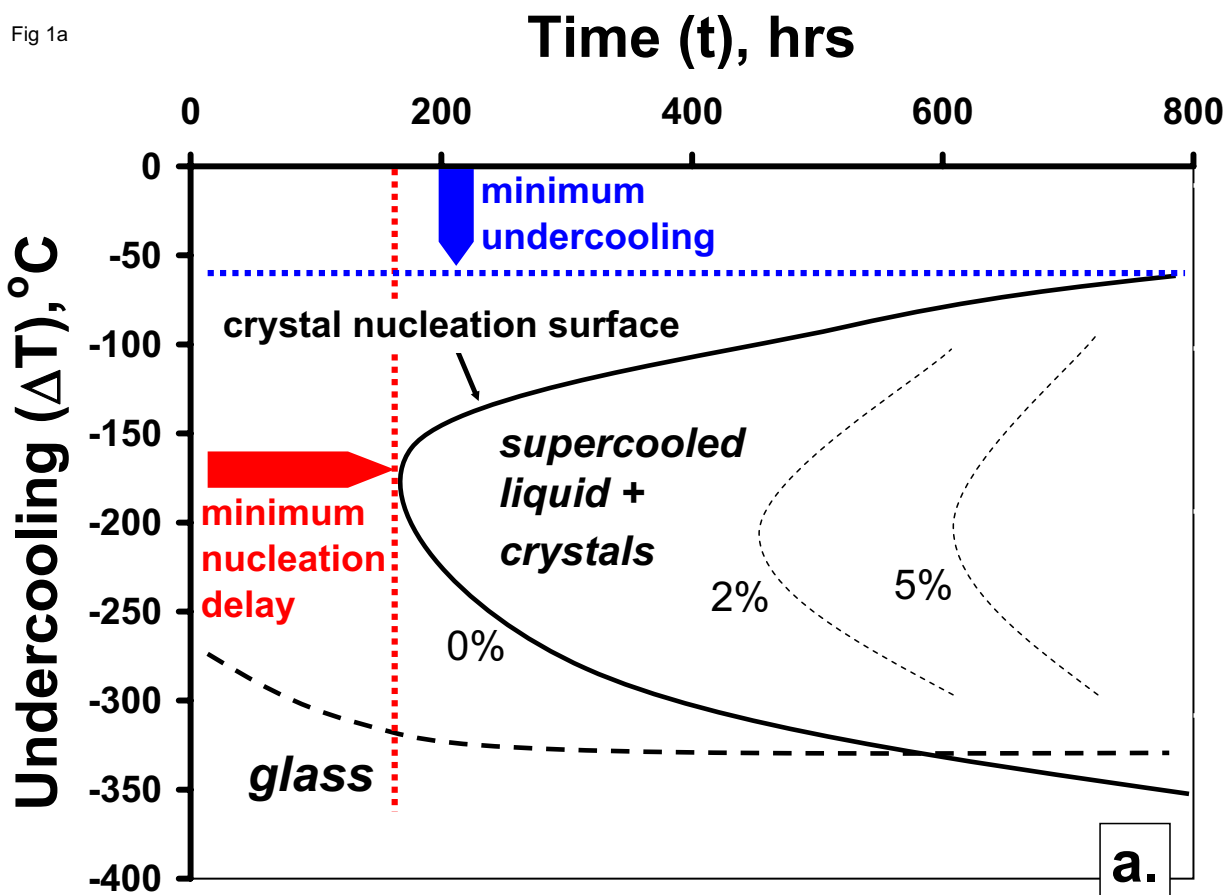
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248 Fig. 3





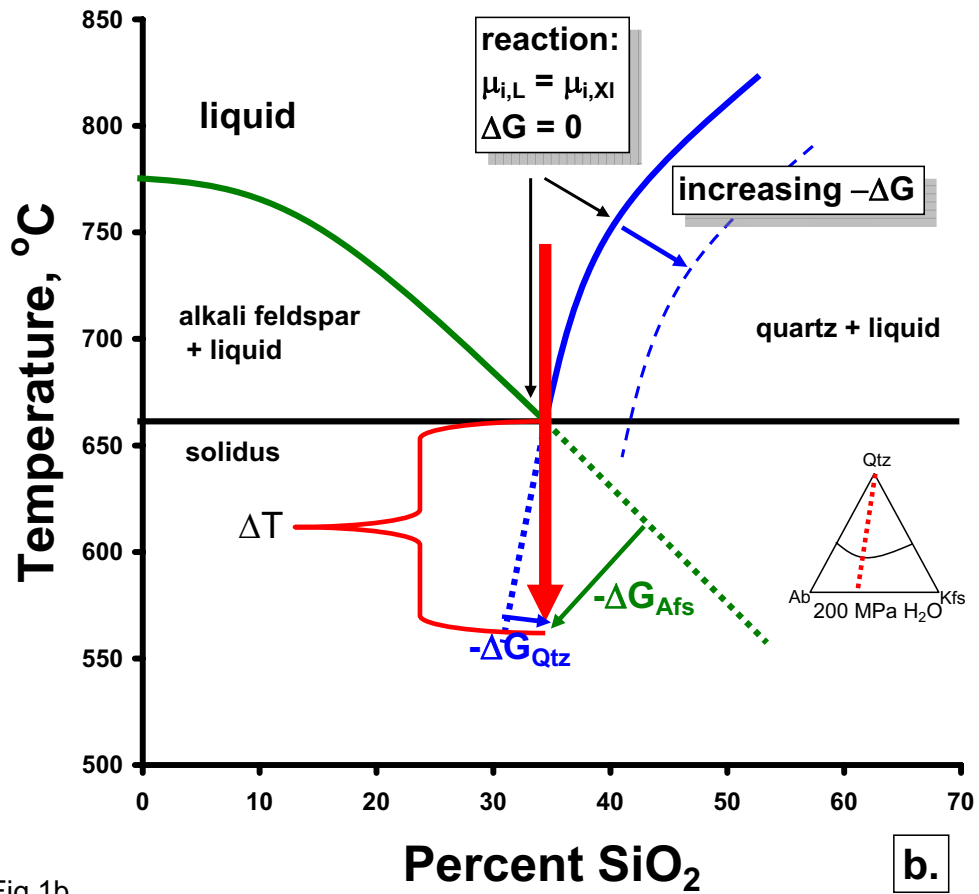


Fig 1b



Fig. 2

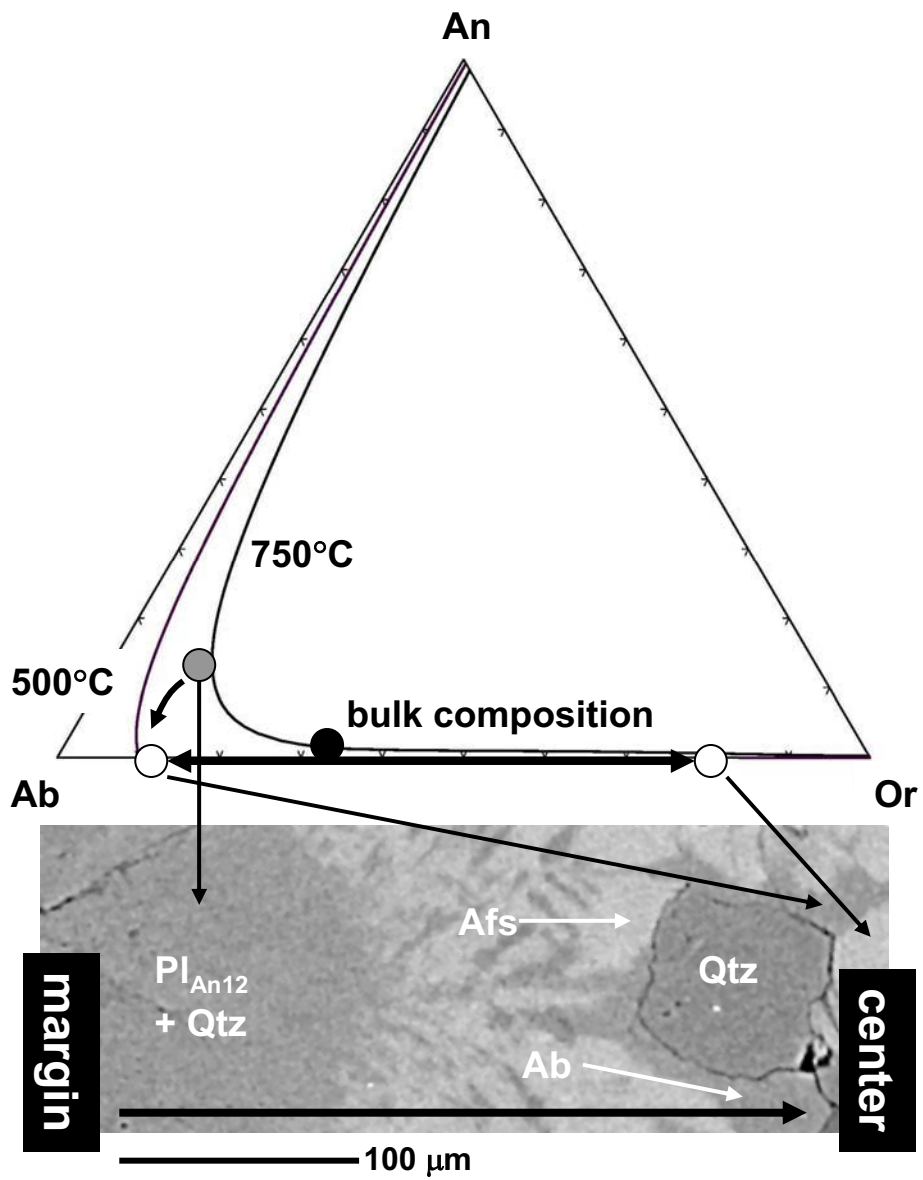


Fig 3

