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4	Pressure-induced phase transitions in coesite
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18	ABSTRACT
19	High-pressure behavior of coesite was studied on single crystals using diamond-anvil cells with
20	neon as the pressure transmitting medium by means of in situ Raman spectroscopy up to

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21 pressures of ~51 GPa. The experimental observations were complemented with theoretical computations of the Raman spectra under similar pressure conditions. We find that coesite 22 undergoes two phase transitions and does not become amorphous at least up to ~51 GPa. The first 23 phase transition (coesite I to coesite II) is reversible and occurs around 23 GPa. The second 24 transition (coesite II to coesite III) at about 35 GPa is also reversible but involves a large 25 26 hysteresis. Samples recovered from the highest pressure achieved, ~51 GPa, show Raman spectra of the initial coesite. The ab initio calculations gave insight into the initiation mechanism of the 27 first phase transition, implying, from the analysis of unstable phonon modes, that it is probably a 28 29 displacive phase transition due to shearing of the four-membered rings of SiO₄ tetrahedra upon compression. The transition to the lowest-symmetry phase, coesite III, is possibly a first order 30 phase transition which leads to a very distinct structure. None of the metastable high-pressure 31 phases of coesite has been previously studied and it was widely accepted that coesite undergoes 32 pressure-induced amorphization at significantly lower pressures (30 GPa). The study of the high-33 pressure behavior of coesite is important to better constrain the metastable phase diagram of 34 silica. Further crystallographic investigations are necessary for characterizing the structures of 35 these metastable coesite forms. Crystalline or amorphous metastable phases derived from coesite 36 37 under high-pressure conditions are of particular interest because they can be used as potential tracers of peak transient pressures (stress) reached in processes such as impacts or faulting. 38

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Keywords: silica, coesite, high-pressure polymorph, metastable, diamond-anvil cell, highpressure Raman spectra

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INTRODUCTION

Silica, SiO₂, exhibits a very rich polymorphism with more than 30 stable or metastable phases, 43 most of which occur at ambient to moderate pressures (< 9 GPa). Some of these phases, such as 44 quartz, trydimite and cristobalite consist of frameworks of SiO₄ tetrahedra and are abundant in 45 nature. Phases of silica stable at higher pressures and temperatures are mostly composed of 46 octahedrally coordinated silicon atoms. Coesite, thermodynamically stable above ca. 2.5 GPa and 47 48 at temperatures in excess of 500 °C, is the densest known polymorph with silicon atom tetrahedrally coordinated to oxygen. This polymorph was first observed experimentally by Coes 49 in 1953 and later discovered in nature by Chao and coworkers, in impact breccia from Meteor 50 Crater (Chao et al. 1960). Nowadays coesite is widely accepted as a high-pressure indicator in 51 rocks related to meteorite impact sites, where it forms due to the high-pressure and high-52 temperature regime of the impact and to the very rapid quenching conditions which prevent a 53 reversion from coesite to quartz (e.g., Xiao et al. 2011). Shock-induced formation of coesite has 54 been also observed in meteorites, where it can be found along with other shock minerals (e.g., 55 Ohtani et al. 2011). Terrestrial occurrence of coesite was reported from deeply (>100 km) 56 subducted crustal rocks (ultra-high pressure metamorphic rocks) or mantle derived rocks 57 (kimberlites), which have been exhumed under conditions that prevent retrograde transition to 58 59 quartz (e.g., Smyth and Hatton 1977; Chopin 1984; Mosenfelder and Bohlen 1997; Parkinson

2000; Korsakov et al. 2007; Ruiz-Cruz et al. 2012). In these rocks coesite commonly occurs as an inclusion within clinopyroxene, olivine, garnet or diamond. Coesite-in-diamond assemblage was 61 62 recently introduced as an important high-pressure barometer (Sobolev et al. 2000).

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Because of the relatively strong Si-O bonding in silica, there are high kinetic barriers associated 63 with the transitions to stable high-pressure phases consisting of SiO₆ octahedra (Haines et al. 64 2001). This results in complicated metastable phenomena at high pressures and ambient 65 temperature such as the persistence of low-pressure phases far out of their stability fields and 66

67 transitions to metastable crystalline and amorphous phases. Slow kinetics, enhanced metastability, formation of poorly crystallized or structurally disordered materials usually give 68 rise to weak X-ray diffraction patterns which are difficult to interpret, resulting in contradictory 69 interpretations. Another major complexity in studying the behavior of silica also arises from the 70 fact that the transition mechanisms, the pathways through intermediate metastable phases and the 71 onset of pressure-induced amorphization strongly depend on the starting polymorph, as well as 72 on the hydrostaticity and stress anisotropy present in the sample during experiments. For 73 example, experimental studies on polycrystalline α -quartz in neon pressure medium (Kingma et 74 75 al. 1993) evidenced pressure-induced phase transitions above 21 GPa to a crystalline metastable phase of reduced symmetry, followed by pressure-induced amorphization above 30 GPa. In 76 helium pressure medium, which provides higher hydrostaticity, polycrystalline guartz is found to 77 remain crystalline up to 45 GPa and to transform to a monoclinic phase at such pressure (Haines 78 et al. 2001). A transformation path through several metastable phases has been reported in 79 cristobalite, as well (e.g., Yagi and Yamakata 2000; Prokopenko et al. 2001; Dera et al. 2011). 80 Numerical calculations also stressed the fact that stable polymorphs of SiO₂ may undergo a 81 number of phase transitions to metastable phases with increasing pressure before reaching 82 83 amorphization (Teter and Hemley 1998; Wentzcovitch et al. 1998).

In an experimental study on the high-pressure behavior of coesite, Hemley (1987) observed changes in the Raman spectra of coesite collected at ambient temperature and at the pressures of 22-25 GPa in argon pressure medium, and reported that coesite becomes amorphous above 30 GPa. The authors attributed such changes to a high-pressure phase transformation occurring in coesite; however, no further investigation has been reported to better describe such behavior.

In this study we aim at giving insight into the high-pressure behavior of coesite. We measure in situ Raman spectra at pressures up to 51 GPa and complement them with theoretical

computations of Raman spectra under similar pressure conditions. We find two phase transitions
clearly distinguishable by Raman spectroscopy and explain the mechanism of the first transition
based on the theoretical calculations.

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EXPERIMENTAL METHODS

96 Synthesis

97 The starting material for the coesite synthesis was SiO_2 glass powder with very low trace 98 elements content, as analyzed at the BGI using LA-ICP-MS: Al 20 ppm, Ge 1.3 ppm, Na 1.0 99 ppm, Li 0.8 ppm, and B, Ti, Fe, Ga, Rb and Sn below the detection limits. Coesite single crystals 100 were synthesized by mixing the starting powder with $\sim 5 \text{ wt\%}$ distilled water inside a platinum 101 capsule, which was then welded shut. The capsule was first placed into pyrophyllite sleeves and 102 then in a 0.5" talc-pyrex piston-cylinder assembly containing internal, tapered graphite resistance 103 furnaces (Bromiley and Keppler 2004). The mixture was pressurized to 3.5 GPa and slowly 104 heated up to 1250 °C, kept at this temperature for ~15 hours, then cooled down to 1100 °C in 5 105 hours, and finally quenched. Slow cooling procedure and water-saturated conditions resulted in growth of relatively large (above 100 µm in linear dimensions) crystals. No Raman peaks were 106 observed in the spectra of synthesized coesite in the O-H vibration region (2800-3400 cm⁻¹). This 107 is in agreement with the study on pressure dependence of hydrogen solubility in coesite 108 109 (Mosenfelder 2000; Koch-Müller et al. 2001), according to which no water should be present in 110 coesite synthesized at 3.5 GPa and 1250 °C.

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112 High-pressure Raman spectroscopy

113 Piston-cylinder type diamond anvil cells (DAC) developed at BGI (Kantor et al. 2012) made of high-temperature resistant alloy were used for the high-pressure experiments. Experiments in 114 115 quasi-hydrostatic conditions were carried out using 250 µm culet size diamonds, a cylindrical pressure chamber of 30-40 µm height and ~125 µm diameter drilled in a pre-indented rhenium 116 gasket. We used neon as pressure transmitting medium, loaded using the BGI gas loading system 117 (Kurnosov et al. 2008). Selected crystals were in the form of plates of typical size 15 x 30 x 50 118 μ m³ and they were loaded together with a ~5 μ m in diameter ruby sphere for pressure 119 determination. The pressure was determined using the ruby luminescence line (Mao et al. 1986). 120

Raman spectroscopy measurements were performed using a LabRam system (Horiba Scientific 121 122 Inc.) with a He-Ne-laser (excitation wavelength 632.8 nm, output power 0.15 W, spectral resolution 2 cm⁻¹) as well as Dilor XY Raman spectrometer with Ar+ ion laser (514.5 nm, 123 Coherent Innova 300, spectral resolution 1 cm⁻¹). The output power was varied according to the 124 sample signal between 0.3 and 1.0 W when using the Dilor instrument. The spectrometers were 125 calibrated using either the silicon peak at 520 cm⁻¹ or referencing the value of the absolute 126 wavelength of the ruby R₁ fluorescence line. Raman spectra were collected between 200 and 127 1200 cm⁻¹. This region is optimal because the LabRam spectrometer used in our experiments is 128 equipped with a notch filter which prevents collection of the frequencies lower than 150 cm⁻¹, 129 whereas above 1200 cm⁻¹ low intensity peaks of coesite are suppressed by strong diamond peak 130 at centered near 1300 cm⁻¹. We performed five different DAC experiments at room temperature 131 132 by pressurizing the coesite crystals in steps of several GPa up to a maximum of \sim 51 GPa. In two 133 of these experiments, Raman spectra were also collected during decompression. Peak positions in 134 the Raman spectra were determined by fitting to Lorentzian peak shape using Igor Pro v. 6.22 135 software.

136 External electrical heating in DAC

Heating experiments up to ~400 °C were performed using platinum-wire resistive whole-cell 137 heater. The heater has an external diameter of 50 mm, it is made of fired pyrophyllite and 0.5 mm 138 139 in diameter platinum wire is folded over the inner surface of the heater. For the purpose of protecting the Raman spectrometer from heating over several hours, we used a thermal insulator 140 that is made of a square-shaped double-layered stainless steel box. Stainless steel of "type 141 142 1.4571" is oxidation-resistant at elevated temperatures and shows no oxidation effect to at least 600 °C (Fig. 1). The DAC and the whole-cell heater were fixed on a stainless steel holder, which 143 144 was then placed inside the steel box with openings at the bottom and the top, to allow optical access. Temperature was measured using a Pt Pt/Rh S-type thermocouple placed in the vicinity of 145 146 the gasket.

In the first experiment, the coesite sample was pressurized at room temperature up to 29 GPa and then slowly heated up to 400 °C. During heating up to 200 °C the pressure dropped down to 27 GPa and was readjusted before further heating. In a second experiment, the coesite sample was pressurized from room pressure up to 34 GPa and then slowly heated up to 200 °C. At this temperature, however, the Raman spectrum was very poor and therefore the experiment was interrupted. Pressure was monitored from a position of the ruby fluorescence peaks corrected for temperature after Rekhi et al. (1999).

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155 Transmission Electron Microscopy

156 Conventional TEM characterizations in bright-field and dark-field imaging and selected electron 157 diffraction techniques were carried out with a Philips CM20FEG equipped with an energy 158 dispersive X-ray (EDX) analyzer, operated at 200 kV. Analyses were performed on several chips

of a crystal which was subjected to a maximum pressure of 35 GPa. The recovered material was first characterized by Raman spectroscopy and then further crushed between two tungsten carbide plates. The ethanol dispersion was placed on a lacey carbon film on Cu-grid (300 mesh). Selected area electron diffraction (SAED) patterns from different chips were obtained to distinguish between crystalline and amorphous domains or particles. The chemistry of the grains was also cross-checked using EDX spectroscopy.

165 X-ray diffraction

We selected coesite single crystals at BGI using a rotating anode high-brilliance Rigaku
diffractometer with Mo Kα radiation, equipped with Osmic focusing X-ray optics and Bruker
Apex CCD detector.

The crystal recovered after a repeated experiment at 34 GPa and ~300 °C was analyzed by means 169 of single-crystal X-ray diffraction at the beamline 13IDD of the GSECARS at the Advanced 170 Photon Source, Argonne National Laboratory, USA. An incident monochromatic beam with 171 wavelength of 0.3344 Å was focused to a spot of 4x8 μ m². Diffraction images were collected 172 173 using a MAR165 CCD detector with sample-to-detector distance of approximately 250 mm. The sample was also analyzed by X-ray diffraction mapping along a 5 x 5 points, covering an area of 174 $12 \times 12 \mu m^2$ (step size 3 μm), with exposure time of 10 s at each point. Diffraction images were 175 176 integrated using the Fit2d software (Hammersley 1996).

177 Ab initio calculations

We analyze the pressure dependence of the phonon spectra also from the first-principles calculations. We determine the ground-state properties using standard density-functional theory (Kohn and Sham 1965; Payne et al. 1992; Martin 2003) in the ABINIT implementation, based on 181 planewaves and pseudopotentials (Gonze et al. 2002, 2009). Starting from the crystal structure refined by Angel et al. (2003) we determine the theoretical structure of coesite up to 40 GPa in 10 182 GPa steps. Then we compute the energy derivatives to build the dynamical matrices and the 183 Raman tensors in the framework of the density-functional perturbation theory (Baroni et al. 2001; 184 Gonze et al. 2005; Veithen et al. 2005). We employ a 4x4x4 grid of special k points (Monkhorst 185 186 and Pack) to sample the electron density in the reciprocal space and a kinetic energy cutoff of 38 Hartrees (1 Hartree = 27.2116 eV). With these parameters the precision of the calculation is 187 typical on the order of 0.001 Hartree in energy and better than 1 GPa in pressure. We store all the 188 189 Raman spectra computed under pressure on the WURM website (http://www.wurm.info). More details of the Raman calculations can be found in the original WURM paper (Caracas and 190 191 Bobocioiu, 2011).

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RESULTS

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194 High-pressure, room temperature Raman spectroscopy

195 Selected Raman spectra collected during compression are shown in Figure 2. At ambient pressure coesite shows prominent peaks at 202, 261, 322, 352, 371, 425, 469 and 519 cm^{-1} , with the last 196 peak being the most intense. The intensities and positions of these peaks are in good agreement 197 198 with previous studies (Sharma et al. 1981; Boyer et al. 1985; Hemley 1987). The peaks that are expected to be centered around 665 cm⁻¹ and 785 cm⁻¹ at ambient pressure have only been 199 observed at elevated pressures and not in all experiments. A peak located at 815 cm⁻¹ was 200 observed starting from ambient conditions, but was not detected in all experiments. Another 201 peak, not previously reported in high-pressure Raman spectroscopy studies of coesite, was 202 203 observed in two experiments. It appeared at and above 4.5 GPa, and, according to its pressure

shift, it can be expected to occur around 860 cm⁻¹ at ambient conditions. Raman bands at 1036 and 1164 cm⁻¹ were observed at ambient conditions outside the DACs, but not under compression due to their very low intensities. All the vibration bands are significantly weaker than the main 519 cm⁻¹ band, they all show continuous positive pressure shift during compression and can be followed up to ~28 GPa (Fig. 2a). The bands located at 519, 665, 785 and 815 cm⁻¹ have the largest pressure shifts, in good agreement with the previous study by Hemley (1987).

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The most intense 519 cm⁻¹ band was described as v_s (Si-O-Si) symmetric stretching mode with A_g 211 symmetry (Sharma et al. 1985, and references therein). It shows continuous positive pressure 212 213 increase up to 23 GPa. Above 23 GPa a new strong vibrational band appears at a frequency of about 20 cm⁻¹ lower than the main Raman peak, which at this pressure has a frequency of 593 cm⁻¹ 214 ¹, as was also observed by Hemley (1987). Several other new modes become visible at lower 215 frequencies, confirming the results reported by Hemley (1987) and their interpretation of a 216 217 possible phase transition to a phase with reduced symmetry or enlarged unit cell. This postcoesite phase, hereafter referred as coesite II, can be followed upon compression up to ~35 GPa 218 (Fig. 2b). The A_g mode persists up to ~35 GPa, although its intensity decreases significantly. 219 Above ~35 GPa, the two high-frequency peaks disappear; only one new peak centered around 220 ~600 cm⁻¹ can be observed (Fig. 2b). This sudden change in the Raman spectrum indicates a 221 222 possible discontinuous transition to a new phase, hereinafter referred as to coesite III. On further compression up to ~51 GPa, the peak centered around ~600 cm⁻¹ decreases in intensity and 223 exhibits a very small pressure increase (Fig. 2b). Above ~35 GPa, in addition to the peak centered 224 around ~600 cm⁻¹, new bands appear as two triplets of equally spaced peaks between ~250-300 225 cm^{-1} and between ~620-720 cm^{-1} . Appearance of a large number of new vibrational modes may 226

227	indicate that coesite III has either an enlarged unit cell or lower symmetry with respect to coesite
228	I and II structures. At ~51 GPa no vibrational modes can be observed. The pressure dependence
229	of the main 519 cm ⁻¹ Raman mode (dv/dP), where v is the ambient-pressure phonon frequency
230	and P is the pressure) was derived from a series of experiments and it is, on average, 3.0 ± 0.4
231	cm ⁻¹ /GPa (Fig. 3). Based on the zero-pressure bulk modulus K_{T0} = 100.8 ± 0.5 GPa reported by
232	Angel et al. (2001) and using the formulation of the mode-Grüneisen parameter as γ_{ν} =
233	$(K_{T0}/v)(dv/dP)$, we obtain a value of 0.58 ± 0.08 for the A _g mode, only slightly higher than the
234	values reported in Hemley (1987).

At the highest pressure reached in these experiments, about 51 GPa, the Raman spectrum of 235 coesite almost vanishes. Under decompression the vibrational modes of coesite III regain 236 intensity, with the most prominent peaks visible at ~250, ~540 and ~580 cm⁻¹. Their frequencies 237 decrease continuously down to ~24 GPa without any abrupt change, suggesting that the structure 238 of coesite III is preserved down to 24 GPa and that the transition to the coesite II phase is not 239 reversible or has a very large hysteresis. A strong single band centered around 600 cm⁻¹ appears 240 at ~24 GPa and its intensity increases with further decompression, until it dominates the Raman 241 spectra below ~20 GPa, suggesting that the structure of coesite has been retrieved. Indeed, the 242 Raman spectrum of the recovered crystal at room pressure is identical to that of the starting 243 material (Fig. 4). The fact that the pressure-quenched material is crystalline coesite strongly 244 suggests that the high-pressure phase coesite III was also crystalline at 51 GPa even if the Raman 245 vibrations could not be observed. 246

247 Raman active modes from ab initio calculations

We compute the phonons in the Brillouin zone-center, with both frequencies and atomic displacement patterns, for coesite I up to 40 GPa. We equally determine the Raman tensors and

compute the Raman intensities for the Raman-active modes. All the spectra are reported on the WURM website (http://www.wurm.info), but for sake of clarity only the spectrum at ambient pressure is represented here, in Figure 5a. Figure 5b shows pressure dependence of selected most dominant modes. The Raman spectra are dominated by the A_g mode situated at ~510 cm⁻¹ at ambient pressure. A series of low intensity peaks are observed at frequencies higher than 600 cm⁻¹ , in excellent agreement with the experimental data.

The strongest A_g mode, located at ~510 cm⁻¹ at ambient pressure (at 541 cm⁻¹at 10 GPa) is a 256 257 breathing mode of the four-membered rings comprised of SiO₄ tetrahedra (Fig. 6a) and it arises from bending of four different Si-O-Si bonds that vibrate in phase, namely Si-O2-Si, Si-O3-Si, 258 259 Si-O4-Si and Si-O5-Si (nomenclature after Angel et al. 2003, see Figures 2 and 4 in the cited reference). Except for the Si-O4-Si bond angle, which changes by only a few degrees throughout 260 261 the pressure range examined by Angel et al. (2003), other three bond angles show strong pressure 262 dependence. In contrast to these four angles, Si-O1-Si is rigid due to symmetry constrains and remains 180° throughout the investigated range. Atomic movements of this breathing Ag mode 263 are illustrated in a representative four-membered ring in Figure 6a seen during contraction. The 264 largest displacement is seen in O3 and O4 atoms, which are moving symmetrically inward, and in 265 O5 atoms, that are moving parallel to each other along a-axes, but in the opposite direction. 266

A B_g mode that appears at 77 cm⁻¹ at ambient conditions (also 77 cm⁻¹ at 10 GPa and 56 cm⁻¹ at 20GPa) is dominant in the lower frequency region and shows softening with increasing pressure (Fig. 5b), similar to previous experimental studies (Hemley 1987). This mode corresponds to shearing of the tetrahedra rings (Fig. 6b and c) and may have a significant influence on the structural distortion at elevated pressures. Shearing of the four-membered rings is illustrated by the two adjacent four-membered rings shown in Figure 6b. Within the same ring O3 atoms are

273 displaced in the same direction, but this displacement direction is opposite between the two adjacent rings. O2 atoms vibrate opposite to the O3 displacement direction. Within the ring, one 274 of the O4 atoms moves downwards and the other upwards from the plane of the ring. All O5 275 atoms of the structure move in the same direction, in the plane of the SiO₄ rings. Similar intensity 276 variation is observed in an A_{μ} mode that appears at 115 cm⁻¹ at ambient pressure (Fig. 5b). Above 277 20 GPa this infrared active mode becomes even more unstable than the Raman active 77 cm⁻¹ 278 279 mode; this enhances the displacement of the O1 atom from the rigid 180° Si-O1-Si bond (Fig. 6d). Then this displacement could initiate the structural changes that we observe above 24 GPa. 280 281 However, an IR study is required in order to confirm this prediction. For a better visualization of the atomic motions, please visit http://www.wurm.info. 282

Other two modes in the 400-500 cm⁻¹ region (Fig. 5a) are correlated with the motion of the SiO₄ tetrahedra rings, although they have low intensity. One is a complex B_g mode at 430 cm⁻¹, corresponding to both breathing and shearing of the SiO₄ tetrahedra rings, and the other one is an A_g mode at 455 cm⁻¹, which arises from stretching of the rings. The 430 cm⁻¹ mode has not been observed experimentally, but the 455 cm⁻¹ mode, albeit very weak, was present in some of our spectra.

289 High-temperature, high-pressure Raman spectra

The Raman spectra collected at 27-29 GPa up to 400 °C and at 34 GPa up to 200 °C are shown in Figure 7a and b, respectively. The first heating experiment was carried out in the pressure range where coesite II phase (Figs. 2a and 2b) was observed, and, as expected, the main feature in the Raman spectra is the peak doublet located ~600 cm⁻¹ (Fig. 7a). The intensity of the vibrational modes decreases with increasing temperature, and at 27 GPa, as expected, they shift to lower frequency. However, at 29 GPa the higher frequency peak shifted 4 cm⁻¹ towards higher

frequency between room temperature and 425 °C, whereas the lower frequency band softened of $\sim 1 \text{ cm}^{-1}$, increasing in this way the total spread of the doublet. At this temperature an intermediate peak appears in the spectra but due to the very poor quality of the spectra it is hard to tell if it is a signal from the sample or a spike. At higher temperatures the intensity of the doublet decreased significantly and the doublet peak was not observable.

At 34 GPa and 100 °C, the peak doublet of coesite II is still present and decreases both in intensity and in frequency with increasing temperature. No signal was observed at 200 °C (Fig. 7b). Raman spectra were collected during decompression at elevated temperature, but no Raman spectra of coesite were observed. At room pressure and after cooling down to room temperature, a broad peak close in position to the main vibration mode of coesite was observed (Fig. 7b). The recovered crystal was also analyzed by single-crystal X-ray diffraction (see further).

307 TEM observations

One of the recovered samples was investigated by transmission electron microscopy. This sample 308 309 was selected for the TEM analysis because the central, thickest part of the crystal was bridged between diamond anvils at ~35 GPa during compression, whereas the thinner edges of the crystal 310 remained largely undisturbed by the diamond culets. Raman spectra collected on the material 311 recovered from the thin edge of the sample show a weak peak around 425 and 514 cm⁻¹, and the 312 313 TEM analysis of the same material revealed that very thin grain domains are indexed with coesite in the SAED pattern (Fig. 8). On the other hand, the material recovered from the bridged part of 314 315 the crystal does not show any Raman active modes and appears entirely amorphous at the TEM. 316 Our observations agree qualitatively with the previous studies on high-pressure silica behavior: in 317 experiments with stiff pressure media where amorphization is initiated at lower pressures with 318 respect to experiments in quasi-hydrostatic conditions (e.g., Hemley 1987; Haines et al. 2001).

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320 X-ray diffraction

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X-ray mapping along 25 spots of the sample quenched from ~300 °C and 34 GPa indicates that the material is well-crystallized. All observed diffraction peaks belong to coesite (Fig. 9). Phase identification was carried out using the Match! Software v 1.11 (with Crystallography Open Database), considering only the region of d-spacing between 4.5 and 1.0 Å (2theta $5 - 19^{\circ}$). The suggested possible phases by the program are coesite, diamond and quartz, however all of the peaks assigned to quartz have d-spacing which can also be assigned to coesite, and no peak belonging solely to quartz has been observed (Fig. 9).

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DISCUSSION

329 Coesite appears to undergo at least two distinct transitions to metastable phases upon compression, as shown in DAC experiments with quasi-hydrostatic medium (Ne) up to ~51 GPa. 330 A similar high-pressure behavior, i.e., complex path of transformations to metastable phases 331 332 before amorphization, have been reported for quartz (Kingma et al. 1993; Haines et al. 2001) and 333 it is in agreement with predictions from numerical models, which suggest that a number of 334 metastable phases can appear on compression of SiO₂ materials before amorphization 335 (Wentzcovitch et al. 1998; Dubrovinsky et al. 2004). Most certainly these phases appear as a 336 consequence of the lack of energy at room temperature to overcome the considerable potential 337 barrier needed to increase the silicon coordination by oxygen from 4 to 6.

The transition from coesite I to coesite II at around 23 GPa was initially reported by Hemley (1987). The study focused on the phase transition, showing its relation to phonon softening, but did not go further into clarifying the eventual splitting of the most intense Raman doublet above

~23 GPa. The author also reports one single broad peak above 30 GPa centered around 600 cm⁻¹, 341 interpreted as a feature similar to that reported for silica glass, and therefore concludes that above 342 343 such pressure coesite becomes amorphous. Hemley (1987) also reported that the splitting at 23 GPa was obscured in all experiments except in those with argon, which was providing the best 344 quasi-hydrostatic conditions in their experiments at higher pressures. Neon is shown to be a softer 345 346 pressure-transmitting medium and to give quasi-hydrostatic conditions at higher pressures than argon (Klotz et al. 2009). In our experiments, therefore, we are able not only to clearly follow the 347 evolution of the splitting of the main Raman mode above 23 GPa, but also to observe another 348 phase transition at \sim 35 GPa. Non-hydrostatic compression, as we observed on the example of 349 350 partially bridged coesite crystal as well as reported in the experiments with Ar or stiffer pressure media (Hemley 1987), leads to amorphization of coesite at lower pressures at room temperature. 351

Our experimental and theoretical results are in very good agreement, with a discrepancy in frequencies of about 10 cm⁻¹ between the calculated and the measured spectra. The main Raman mode is at 519 cm⁻¹ in the experimental spectra and at 510 cm⁻¹ in the calculated; another intense A_g mode which is observed at 426 cm⁻¹ is calculated at 415 cm⁻¹. Moreover, the calculated frequency shifts with pressure are very similar to those observed experimentally, at least for the strongest Raman modes.

At 8 GPa, a small shoulder at 228 cm⁻¹(Fig. 2a) can be observed overlying the 220 cm⁻¹ peak (202 cm⁻¹ at ambient pressure). From a previous study (Hemley 1987) it appears that the mode at 176 cm⁻¹ intersects the 202 cm⁻¹ mode at ~8 GPa, and therefore it could be the cause of the shoulder in the spectra we recorded at this pressure. However, it should be noted that the results of our ab initio calculations are in contrast with such an interpretation since these two calculated

modes do not cross at any pressure (calculated up to 40 GPa), although their separation decreases
with increasing pressure.

365 In light of our experiments and ab initio calculation we can give an insight on the mechanism of 366 transformation from the coesite I to coesite II phase in terms of a complex phonon softening. The crystal structure of coesite II has a lower symmetry than coesite I, as it appears from the 367 increasing number of the vibrational modes observed in this study. The calculations show that 368 369 three phonon modes, one Ag, one Au and one Bu soften under compression (Fig. 4b), the former 370 two becoming imaginary around 27 GPa. They all correspond to some form of shear of the SiO₄ 371 tertrahedra rings, but the A_u and B_u modes are only infrared active. Freezing of any or all of these 372 modes could enhance a displacive transition and may be associated with a breaking of the symmetry of the four-membered rings. This can also give rise to two slightly different breathing 373 374 modes for two differently sheared rings, a consequence of which is the splitting of the main A_g mode (at 510 cm⁻¹ at room pressure) associated with the breathing of the four-membered rings. 375

An alternative explanation is that the second Raman peak at 560 cm⁻¹ in the coesite II structure 376 arises from the coupling between the soft B_g mode, situated at 77 cm⁻¹ at ambient conditions and 377 imaginary at the transition, with either the Bg mode at 430 cm⁻¹ (at ambient conditions, 450 cm⁻¹ 378 at 20 GPa) or the A_g mode at 455 cm⁻¹ (at ambient conditions, 468 cm⁻¹ at 20 GPa). In particular 379 the coupling and further energy transfer between the two Bg modes is very likely due to their 380 381 identical symmetry. This transfer can also enhance the Raman intensity of the higher-energy 382 mode. Coupling of the unstable B_g and the stable A_g modes is possible because of similarities between their eigendisplacements. The coupling could also enhance the polarizability of the 383 384 higher-energy mode and hence its Raman signature.

The transition from coesite I to coesite II is likely to be second order in character because of the phonon softening, continuous behavior of the main Raman peak, and because of the absence of hysteresis. Decrease in intensity and softening of the main peak doublet during heating, support

hysteresis. Decrease in intensity and softening of the main peak doublet during heating, support 387 the observation that coesite II is a metastable phase, which exists only at room temperatures far 388 outside the pressure stability field of coesite. The heating which is insufficient to transform 389 390 coesite to the thermodynamically stable phase – stishovite – enhances the thermal motion of the 391 metastable structure and causes instability but, most probably, does not lead to amorphization. 392 Hence, the pressure- and temperature-quenched sample retransforms to coesite. The anomalous 393 spreading of the doublet and shifting to the higher frequency at 29 GPa and 400 °C requires further understanding and structural analysis of coesite II. 394

The transition of coesite II to coesite III is possibly first order in character, as it appears from the abrupt change in Raman spectra above \sim 35 GPa (Fig. 2b). As expected in a first order transition, the frequency of the main mode, situated at \sim 600 cm⁻¹, does not vary significantly with pressure (Fig. 4) and a hysteresis is probably hindering reversible transformation from coesite III to coesite II.

The mechanisms of this transition cannot be revealed from ab initio calculation, since the structure of the two polymorphs is still unknown. If we assume that the major peak observed in the Raman spectra is still correlated to the O-Si-O motions as the A_g mode, the major decrease in frequency may suggest a softer Si-O bond and, hence an increase in coordination number of the Si. Coesite III would therefore have at least some of Si in octahedral coordination. However, to confirm such hypothesis, a structural study is required.

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IMPLICATIONS

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The study of the high-pressure behavior of coesite reveals two high-pressure polymorphs that remain crystalline far above the previously reported amorphization pressure. This significant discrepancy between previous and our current results implies that the metastable phase diagram of silica phases requires a substantial revision. Crystalline or amorphous metastable phases derived from coesite under high-pressure conditions can be of interest in geological application as potential tracers of peak transient pressure conditions reached in processes such as impacts or faulting.

414

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550 FIGURE CAPTIONS

FIGURE 1. External heating assembly, consisting of a pyrophillite whole cell heater surrounding
DAC placed on a stainless steel holder and double-layered stainless-steel insulation box. The coin
is used as a scale marker.

FIGURE 2. (a) Raman spectra collected up to 30 GPa during compression. The star located above the doublet peak at 24.2 GPa indicates appearance of coesite II phase. (b) Raman spectra collected between 30 and 51 GPa during compression. The star above the spectrum at 38.3 GPa indicates disappearance of the main doublet peak and the transition to coesite III.

FIGURE 3. Pressure dependence of the main Raman active mode obtained from several different
experiments at ambient temperature. Phase transitions at ~23 and ~35 GPa are indicated by solid
lines, and the thermodynamic stability field of coesite is indicated by dotted lines.

FIGURE 4. Raman spectra collected during decompression from ~51 GPa to ambient pressure.
Note that the power of the incident laser beam was decreased below 20 GPa from 1.0 to 0.3 W.

FIGURE 5. (a) Theoretical Raman spectrum at ambient conditions. The spectrum is dominated by 563 the strong A_g mode at 510 cm⁻¹. Several peaks are visible at low frequencies and the most intense 564 is the Bg mode at 77 cm⁻¹, while all peaks above 600 cm⁻¹ are very weak. A few peaks are 565 symmetry-labeled. The inset shows the peaks occurring in the 400-500 cm⁻¹ range, with intensity 566 magnified, with the B_g mode at 430 and the A_g mode at 455 cm⁻¹. (b) Pressure variation of 567 selected modes in coesite. Note that the lowest frequency modes become unstable with increasing 568 569 pressure. The A modes bear symbols; the g modes are represented with solid line; the dashed line 570 represent modes that are only infrared active. Three modes become unstable between 20 and 30

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GPa, including a B_g Raman active mode at 77cm⁻¹ and an A_u infrared active at 111 cm⁻¹ (ambient conditions). These two modes are displayed in Figure 6c and d at elevated pressure.

573 FIGURE 6. Atomic displacement pattern of some of the most representative Raman modes of 574 coesite at 10 GPa. They dominate the Raman spectra and their behavior is likely responsible for 575 the structural changes exhibited under pressures. White corresponds to silicon atom, grey is 576 oxygen; atomic nomenclature is after Angel et al. (2003). Ellipses are surrounding representative 577 SiO₄ rings and grey arrows placed on oxygen atoms are indicating displacement directions. (a) The strongest A_g mode at 541 cm⁻¹ (located at 510 cm⁻¹ at ambient pressure) is a breathing mode 578 of the four-membered tetrahedral rings. (b) The B_g mode at 77 cm⁻¹ (also 77 cm⁻¹ at 10 GPa) 579 dominates the spectra at low frequencies and it corresponds to shearing of the four-membered 580 silica rings. The sketch in the upper left corner on the figure is for simplifying the structure of one 581 ring. (c) The same B_g mode at 20 GPa (56 cm⁻¹) in different crystallographic orientation. (d) 582 Infrared active Au mode at 20 GPa (78 cm⁻¹) showing significant displacement of the O1 atom 583 from the rigid 180 °Si-O1-Si bond. 584

FIGURE 7. (a) Raman spectra collected at 27-29 GPa during heating up to 400 °C. At both pressures one can notice a decrease in intensity and an increase in the splitting of the doublet. (b) Raman spectra collected at 34 GPa during heating up to 200 °C and after quenching to ambient conditions. Only a decrease in intensity can be observed at this pressure, without an increase in the splitting of the doublet.

FIGURE 8. TEM analysis of one of the grains recovered from the thin edge of the crystal bridged
at 35 GPa, showing diffraction profiles that can be attributed to coesite. The material from which
this grain was selected shows a weak Raman peak around 520 cm⁻¹.

- 593 FIGURE 9. Representative X-ray diffraction data showing that the crystalline phase quenched
- from ~34 GPa and ~300 °C is coesite. Reference phases are taken from Crystallography Open
- 595 Database: coesite Araki and Zoltai (1969), synthehic sample at ambient conditions; quartz -
- Hazen et al. (1989), synthetic sample at pressure of 1bar; and diamond Wyckoff (1963).

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Heater contacts

Thermocouple

Stainless steel box with insulation material

Pyrophillite whole - cell heater

Figure 1.



Figure 2a



Figure 2b.



Figure 3.



Figure 4.



Figure 5.



Figure 6.



Figure 7a.



Figure 7b.



Figure 8.



