

1 **# 4254R – Revised Version**

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3 **Quadratite, AgCdAsS₃: Chemical composition, crystal structure and**
4 **OD character**

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16 **ABSTRACT**

17 A re-investigation of the crystal structure of quadratite, ideally AgCdAsS₃, was
18 undertaken using a single crystal from the type locality, Lengenbach, Binntal, Switzerland.
19 Average of five electron microprobe analyses led to the empirical formula
20 (Ag_{0.994}Cd_{0.738}Pb_{0.231}Cu_{0.006}Tl_{0.005}Mn_{0.003}Fe_{0.004}Zn_{0.002}Cr_{0.001})_{Σ=1.984}(As_{0.955}Sb_{0.003})_{Σ=0.958}S_{3.058}.
21 Single-crystal structure refinement (*R*1 = 4.84 % for 558 observed reflections) shows that
22 quadratite crystallizes in the space group *P*4₃22 and exhibits an atomic arrangement similar to
23 that of the recently approved new mineral manganoquadratite, AgMnAsS₃. Like
24 manganoquadratite, quadratite adopts a galena-derivative framework, with metal atoms
25 occupying all the available octahedral interstices, although only M1 and M2 cations, occupied
26 mainly by Cd, adopt a fairly regular octahedral coordination; the M3 cation, occupied by Ag,
27 is located outside the centre cavity in a square-pyramidal coordination, whereas Pb at the split
28 position M3' coordinates six S atoms. Arsenic also adopts a 3 + 3 asymmetrical coordination,
29 thus forming the AsS₃ pyramidal groups that typically occur in sulfosalts.

30 The structure can be also described as a stacking of BAB slabs [A: (Cd,Ag)CdS₂ atomic
31 plane; B: (Ag,Pb)AsS₂ atomic plane] along [001]. The rectangular unit cell of these slabs is
32 oriented diagonally to the *a* axes of quadratite and consecutive slabs are related via interlayer
33 two-fold rotation operations parallel either to [100] or to [010]. This ambiguity leads to an OD
34 structure with various possible stacking sequences, from which the tetragonal space group
35 *P4₃22* was observed.

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INTRODUCTION

38 Quadratite, ideally AgCdAsS₃, was first found as minute quadratic crystals within
39 cavities of the well known Lengenbach dolomite, Binntal, Switzerland in 1989 and described
40 as a new mineral species only in 1998 (Graeser et al. 1998), when suitable material was found
41 for physical characterization and diffraction data. On the basis of a single-crystal investigation
42 (Weissenberg and precession methods), Graeser et al. determined that the mineral was
43 tetragonal, with $a = 5.499(5)$, $c = 33.91(4)$ Å, space group *I4₁/amd*. An approximate model of
44 the crystal structure of quadratite was then obtained by Berlepsch et al. (1999), by assuming
45 the apparent *I4₁/amd* crystal symmetry as the result of the superposition of two
46 enantiomorphic structures, having space groups *P4₁2₁2* and *P4₃2₁2*, respectively. According
47 to their model, quadratite can be described as a galena-based derivative framework composed
48 of warped layers parallel to (001) with cations located in distorted octahedral coordinations.
49 Possibly owing to twinning or order-disorder phenomena in quadratite crystals, S atoms are
50 disordered on split positions.

51 Recently, the new mineral manganquatratite (Bonazzi et al. 2012) showing a close
52 similarity of formula (AgMnAsS₃) and unit-cell dimensions [$a_1 = 5.4496(5)$, $c = 32.949(1)$]
53 with quadratite has been found in the Uchucchacua polymetallic deposit, Peru.
54 Manganquatratite crystallizes in the space group *P4₃22* and exhibits a galena-derivative

55 framework, with S atoms arranged in a cubic closest-packing array with metal atoms
56 occupying all available octahedral interstices. Only the Mn^{2+} cations, however, adopt an
57 octahedral coordination whereas Ag^+ and As^{3+} are located outside the centre cavities, forming
58 asymmetrical coordination polyhedra, AgS_5 and AsS_3 , respectively. In order to substantiate
59 the hypothesis drawn by Bonazzi et al. (2012) and to verify whether or not quadratite is
60 isostructural with manganoquadratite or whether it possesses a different symmetry involving
61 an alternative distribution of the metals within the sulfur close packed structure, a re-
62 investigation of the crystal structure of quadratite was undertaken.

63 CHEMICAL COMPOSITION

64 The crystal fragment of quadratite used for the structural study was analyzed with a
65 JEOL JXA-8200 electron microprobe. Major and minor elements were determined at 15 kV
66 accelerating voltage and 30 nA beam current, with 15s as counting time. For the wavelength-
67 dispersion analyses the following lines were used: $\text{AgL}\alpha$, $\text{CuK}\alpha$, $\text{PbM}\alpha$, $\text{CdK}\alpha$, $\text{TlM}\alpha$, $\text{MnK}\alpha$,
68 $\text{FeK}\alpha$, $\text{ZnK}\alpha$, $\text{CrK}\alpha$, $\text{SbL}\alpha$, $\text{AsL}\alpha$, $\text{SK}\alpha$. The standards employed were: Ag- pure element (Ag),
69 Cu- pure element (Cu), galena (Pb), Cd- pure element (Cd), synthetic TlTe (Tl), synthetic
70 MnS (Mn), pyrite (Fe, S), synthetic ZnS (Zn), Cr- pure element (Cr), synthetic Sb_2S_3 (Sb) and
71 synthetic GaAs (As). The crystal fragment was found to be homogeneous within the
72 analytical error. The average chemical composition (5 analyses), together with the atomic
73 ratios, is shown in Table 1. On the basis of 6 atoms and on the refinement results, the
74 empirical formula is $(\text{Ag}_{0.994}\text{Cd}_{0.738}\text{Pb}_{0.231}\text{Cu}_{0.006}\text{Tl}_{0.005}\text{Mn}_{0.003}\text{Fe}_{0.004}\text{Zn}_{0.002}\text{Cr}_{0.001})$
75 $\Sigma=1.984(\text{As}_{0.955}\text{Sb}_{0.003})\Sigma=0.958\text{S}_{3.058}$.

77 EXPERIMENTAL AND CRYSTAL-STRUCTURE REFINEMENT

78 A small crystal fragment was selected for the X-ray single-crystal diffraction study from
79 a sample of quadratite from the type locality. Unit-cell parameters, determined by centering

80 25 high- θ (13-18°) reflections on an automated diffractometer (Bruker MACH3) are given in
81 Table 2. To check the possible presence of diffuse scattering or weak superlattice peaks, the
82 crystal was also mounted (exposure time of 100 s per frame; 40 mA \times 45 kV) on a CCD-
83 equipped diffractometer (Oxford Xcalibur™ 3), but no additional reflections were detected.
84 Intensity data were collected using MoK α radiation monochromatized by a flat graphite
85 crystal in ω scan mode. Intensities were corrected for Lorentz-polarization effects and,
86 subsequently, for absorption following the semi-empirical method of North et al. (1968). The
87 values of the equivalent reflections were averaged in the Laue group $4/mmm$. The merging R
88 was 9.72% before absorption correction and decreased to 2.25% for the ψ -scan-corrected data
89 set. E-statistics indicated the structure to be centrosymmetric and the systematic absences
90 gave contradictory information. Nevertheless, given the close similarity of quadratite with the
91 recently approved new mineral manganogadratite, AgMnAsS₃, crystallized in the space
92 group $P4_322$ (Bonazzi et al. 2012), we tried to refine the quadratite structure in the same space
93 group starting with the same set of atom coordinates. The full-matrix least-squares program
94 SHELXL-97 (Sheldrick 2008) was used for the refinement of the structure. The site
95 occupancy of all the metal positions was allowed to vary and, surprisingly, we observed a
96 mean electron number for the Ag position (M3) much greater than 47, suggesting
97 incorporation of a heavier element (i.e. Pb) at this site. Accordingly, Ag was refined vs. Pb
98 with the atomic coordinates of these positions left free to vary independently of each other,
99 while the displacement parameters were constrained to be equal. The refined Pb occupancy
100 for the slightly split M3' position [$M3-M3' = 0.27(1) \text{ \AA}$] was found to be 0.213(4), thus
101 indicating that Pb substitutes for Ag in the quadratite structure, and not for Cd as previously
102 supposed (Graeser et al. 1998). To assign the remaining Ag between the two other metal
103 positions (M1 and M2), their occupancy was tentatively left free to vary (Cd vs. vacancy).
104 The M2 site was found to be fully occupied by Cd, whereas M1 exhibited an electron number

105 lower than 48, and was then fixed to $\text{Cd}_{0.58}\text{Ag}_{0.42}$ so as to agree with the chemical formula
106 obtained from the electron microprobe analyses. Finally, the occupancy of the As position
107 was refined versus vacancy but it was found to be fully occupied by arsenic. Neutral
108 scattering curves for Ag, Pb, Cd, As and S were taken from the *International Tables for X-ray*
109 *Crystallography* (Ibers and Hamilton 1974). Inspection of the difference Fourier map revealed
110 three positive peaks of $4 \text{ e}^-/\text{\AA}^3$ approximately located at about 0.6–0.7 \AA from S1, S2 and S3,
111 respectively. However, attempts to introduce these peaks as split sulfur atoms resulted in an
112 unstable refinement and they were disregarded. With anisotropic atomic displacement
113 parameters for all atoms, the R value converged to 4.84% for 558 observed reflections [$F_o >$
114 $4\sigma(F_o)$] and 60 parameters and at 6.08% for all 1485 independent reflections.

115 Experimental details and R indices are given in Table 2. Fractional atomic coordinates
116 and anisotropic-displacement parameters are shown in Table 3. Table 4¹ lists the observed and
117 calculated structure factors for the quadratite structure.

118

119

DISCUSSION

120 **Cation coordination and layer-like configuration**

121 Like manganoquadratite, quadratite possess a galena-derivative framework, in
122 which a pseudocubic closest-packed array of S atoms has individual (nearly) closest-packed
123 layers stacked along the $[6\bar{6}1]$ direction. Metals occupy all the available octahedral interstices,
124 but only M1 and M2 cations adopt a fairly regular octahedral coordination (Table 5); the M3
125 cation, occupied by Ag, is located outside the centre cavity in a square-pyramidal
126 coordination, whereas Pb at the split position M3' coordinates six sulfur atoms, with a $\langle\text{Pb-S}\rangle$
127 mean distance of 2.867 \AA (Fig. 1). The AgS_5 square pyramids are quite irregular, with three

¹ For a copy of Table 4, document item AMxxxxx, contact the Business Office of the Mineralogical Society of America (see inside front cover of recent issue) for price information. Deposit items may also be available on the American Mineralogist web site at <http://www.minsocam.org>.

128 shorter bond distances at 2.724, 2.747 and 2.78 Å and two longer additional bonds at 2.89 and
129 2.904 Å, thus adjusting to the trapezoidal environment forced by requirements of As.
130 However, in quadratite Ag is not completely ordered at the M3 site which adopts a (3+2)
131 pyramidal coordination, but also occupies the octahedral M1 site together with Cd. The M2
132 site, on the other hand, was found to be occupied by Cd only. Like in manganoquadratite,
133 As^{3+} forms typical AsS_3 groups ($\langle \text{As-S} \rangle = 2.297 \text{ \AA}$).

134 Alternatively, the structure can be described as a stacking along [001] of square-net
135 planes of S atoms each offset from the adjacent one by $\sim \frac{1}{2}a$ with respect to the adjacent one.
136 With this arrangement, cations are located inside the mesh of the S_4 square-nets to form two
137 unique planes, (Cd,Ag) CdS_2 (A) and (Ag,Pb) AsS_2 (B). A-planes are rather regular, whereas
138 the presence of the lone-pair-bearing As^{3+} cation asymmetrically located within the S_4 squared
139 net to bond two sulfur atoms, generates distortion within the square-net plane B. The B-A-B
140 stacking sequence along [001] (Fig. 2) generates slabs of galena-like edge-sharing CdS_6
141 octahedra, and slabs containing two sets of AgS_5 pyramids whose apices alternatively point
142 upwards and downwards [see Bonazzi et al. (2012) for more details]. It is noted here that
143 galena-like MnS slabs in manganoquadratite correspond to structural modules of alabandite,
144 whereas in quadratite the galena-like CdS slabs do not correspond to any existing mineral. In
145 fact, in both the known CdS polymorphs, hawleyite and greenockite, which exhibit sphalerite
146 and wurtzite structure, respectively, Cd is located in the tetrahedral interstices ($\langle \text{Cd-S} \rangle =$
147 2.526 \AA , Skinner 1961; 2.532 \AA , Xu and Ching 1993). In most sulfides, Cd shows a marked
148 preference for tetrahedral coordination. In the spinel-like structure of cadmoindite, CdIn_2S_4 ,
149 Cd was assumed to be ordered at the tetrahedral site (2.543 \AA in the synthetic analogue; Hahn
150 and Klingler 1950); analogously, in the stannite-group minerals čerňnyite, $\text{Cu}_2\text{CdSnS}_4$
151 (Szymański 1978) and barquillite, $\text{Cu}_2\text{CdGeS}_4$, (Murciego et al. 1999) Cd enters the
152 tetrahedral sites. However, for (Cd,Pb)-bearing sulfides and sulfosalts like shadlunite,

153 (Pb,Cd)(Fe,Cu)₈S₈ (Evstigneeva et al. 1973), kudriavite, (Cd,Pb)Bi₂S₄ (Balić-Žunić and
154 Makovicky 2007) and tazieffite, Pb₂₀Cd₂(As,Bi)₂₂S₅₀Cl₁₀ (Zelensky et al. 2009), Cd is hosted
155 in octahedral cavities. In particular, in kudriavite an octahedral site was assumed to be mostly
156 occupied by Cd. Its mean bond distance (2.72 Å) and polyhedral volume (26.46 Å³) are in
157 keeping with the corresponding values in the synthetic CdBi₂S₄ (2.72 Å and 26.31 Å³; Choe
158 et al. 1997) and perfectly match with the geometrical features of the M2 octahedron in
159 quadratite (Table 5). Bond-valence sums calculated from the curves of Brese and O’Keeffe
160 (1991) are reported in Table 6. The valence units obtained are in perfect agreement with the
161 cation populations assumed in the present study.

162

163 **OD character**

164 Berlepsch et al. (1999) suggested that quadratite has a regular tetragonal net of Cd and S
165 atoms, bordered by layers with trapezoidal configuration and eccentrically positioned cations.
166 Disorder (considerable cation overlapping in the averaged structure) prevented resolution of
167 the structure. Therefore, the most obvious explanation for the assumed disorder was that the B
168 layers can surround the more regular tetragonal A layer in various orientations, resulting in an
169 OD structure.

170 The present investigation, obtained on a (nearly) ordered crystal, however, suggests
171 that the order-disorder phenomena are limited to interspaces between immediately adjacent B
172 layers. If the slight puckering of the B layer is neglected, its plane group symmetry is *cm* with
173 a two-dimensional unit mesh having both dimensions equal to a diagonal of the $a_1 \times a_2$ mesh
174 of quadratite. In the sequence of coordination trapezoids, all short As-S bonds and Ag-
175 displacement point in one direction, diagonal to the crystal axes of quadratite. Rather
176 surprisingly, two B layers surrounding one A layer are oriented parallel to each other and
177 point along the same [110] diagonal but displaced by $\frac{1}{2}[1\bar{1}0]$. This creates linear bonded

178 groups S2-M2-S2, S3-M1-S3 and M3-S1...As as the only combinations present in the [001]
179 direction of the three-plane B-A-B slab.

180 This geometrically stable unit is the OD layer of the quadratite structure. If the diagonal
181 in the direction of which the S-As-S configurations point is denoted as the *a* axis of the layer,
182 and the direction perpendicular to the OD layer as the *c* axis (the latter in agreement with the
183 notation of quadratite lattice itself) the layer symmetry symbol will be $C2m(b)$. The glide
184 plane and the two-fold rotation interconnect configurations on the two surfaces of the OD
185 layer. This layer is polar in one intralayer direction and the orientation of the *b*-glide plane
186 perpendicular to the layer-stacking direction is indicated by parentheses.

187 The most interesting portion of the structure is the interface of two B planes from
188 adjacent OD layers. The sulfur atoms form a trapezoidal net, with a zig-zag trend of S-S
189 distances (3.92-3.96 Å) along the **a** direction of the layer and a straight trend with a regular
190 alternation of shorter (3.39 Å) S-S intervals and longer (4.42 Å) S-S intervals along the **b**
191 direction. As mentioned above, As with its short bonds adheres to the 3.39 Å interval whereas
192 Ag is shifted towards the 4.42 Å S-S interval (Fig. 3). The adjacent B plane is placed in such a
193 way that the pyramidal coordinations of M3 and As of the previous layer are completed to
194 (somewhat distorted) octahedral ones. This places the sulfur atoms of the added B layer
195 approximately above the cations of the preceding layer, with the small deviations balanced as
196 well as possible (Fig. 4). Thus, because of the eccentric position of cations in their planar
197 trapezoidal coordinations, the two sulfur nets are shifted against one another and they are
198 related by two fold rotation axes in the interspace, parallel to *only one* diagonal of the
199 quadratite unit cell (Fig. 4). The zig-zag S-S tie-lines, parallel to the **a** vector of each of the
200 two B planes, are *perpendicular* to one another across the interspace, which is an unique case
201 among sulfosalts.

202 Trapezoidal schemes of cation-anion planes with zig-zag and straight lines as those
203 observed here are not unusual in sulfosalts (Makovicky and Mumme 1983; Makovicky and
204 Topa 2011). In all these structures, however, orientations of the two atomic planes facing one
205 another are always parallel, with the straight S-S lines running along the infinite direction of
206 the planar configuration, whereas the zig-zag S-S lines are developed along the direction of its
207 limited extent. The unique behavior of the quadratite structure is apparently connected with,
208 in principle, the infinite character of the observed interface. With the orientation of the third
209 short As-S1 bond into the triple B-A-B slab, away from the interface, the interface of two
210 adjacent B planes has a character close to a *lone electron pair micelle* that extends infinitely
211 in two-dimensions.

212 The interface configuration of atoms described here determines the OD nature of the
213 crystal structure of quadratite (and manganoquadratite, Bonazzi et al. 2012). The two adjacent
214 B planes are either related by a two-fold operation parallel to [100] or, with equal probability,
215 by such an operation parallel to [010] of the quadratite cell, but not both at once. These
216 potential two-fold rotation axes comprise 45° to the **a** and **b** vectors of the layer itself. As the
217 layers are polar, the **a** vector of the generated layer will assume a right-hand or left-hand
218 orientation, always perpendicular to the **a** vector of the initial layer.

219 What is valid for the B planes is also valid for the entire, polar OD layers. As these
220 layers are non-polar in the layer-stacking direction (contain layer-reversing operations of layer
221 symmetry, so called λ - ρ partial symmetry operators, represented by the *intralayer* two-fold
222 rotation and the *b*-glide; the lambda-rho symbol stands for layer-reversing), the layer-
223 reversing *interlayer* operator (two-fold rotation around [100] of quadratite; it is a so called σ - ρ
224 partial symmetry operator) becomes supplemented by an *n* glide plane parallel to (010) of
225 quadratite (i.e., a layer-nonreversing interlayer operator τ) interspersed between the two-fold
226 rotation axes. The alternative interlayer *n*-glide plane, (100), belongs to the other choice of

227 interlayer partial symmetry elements, namely that which includes $2\| [010]$. Thus, $n\| (100)$ and
228 the interlayer rotation $[100]$ mentioned above do not belong to the same choice of symmetry
229 elements and have opposite action, resulting in opposite orientations of the second layer.

230 Tentatively, we can insert the observed elements of OD symmetry into a tetragonal-
231 structured symbol, in agreement with the resulting symmetry of the observed quadratite
232 polytype, with a sequence $a_1 a_2 (c) d_1 d_2$ in terms of the quadratite lattice [d are the diagonals
233 of tetragonal lattice in the (001) plane]. In this *groupoid symbol* (Dornberger-Schiff 1956), a
234 line with intralayer operators is followed by that with interlayer operators arranged in the
235 same sequence.

$$\begin{array}{c} 236 \qquad \qquad \qquad 1 \ 1 \ (n) \ 2 \ m \\ 237 \qquad \qquad \qquad \{2 \ n \ (1) \ 1 \ 1\} \end{array}$$

238
239 There are two structures with the simplest, maximally-ordered stacking sequences, for
240 which all layer pairs are equal (the principal property of OD structures with one kind of layers,
241 as in the present case, distinguishing them from other, less determinate layer-stacking
242 sequences) including layer triples, quadruples, etc.

243 When the same interlayer symmetry element is used (only $2\| [100]$ or only $2\| [010]$), a
244 polar two-layer sequence results with an n glide plane as the universal element. When the
245 active interlayer twofold operations are systematically permuted (e.g., the two fold rotation
246 about $a_1, a_2, -a_1, -a_2, a_1, \dots$, connected with the appropriate permutation of symbols in the above
247 two-line *groupoid* symbol), a four-layer structure results, which corresponds to the observed
248 structure $P4_322$ or to its enantiomorph $P4_122$, for which an opposite sequence of axes is used.
249 The λ partial symmetry operations m and b do not convert into the operations of the space
250 group, only the two-fold intra and interlayer operations do, becoming elements of $P4_322$. Any
251 mistake in this application will result in a non-periodic sequence shift, or in the opposite

252 enantiomorph or even in non-periodic layer sequences. Mistakes like these were present in the
253 original quadratite material, in which mixing of the $P4_322$ and $P4_122$ structure portions
254 resulted in the *apparent* space group $I4_1/amd$ of a superposition structure, as previously noted
255 by Berlepsch et al. (1999).

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ACKNOWLEDGEMENTS

258 We thank Luca De Battisti who provided us with the quadratite sample from the type
259 locality. This work was funded by “Progetto d’Ateneo 2009” to P. Bonazzi and the research
260 grant no. 09-065749/FNU to E. Makovicky. The manuscript benefited from the revision of S.
261 Mills, R. Peterson, D. Topa, and the Associate Editor D. Gatta.

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REFERENCES

- 264 Balić-Žunić, T. and Makovicky, E. (2007) The crystal structure of kudriavite, $(Cd,Pb)Bi_2S_4$.
265 Canadian Mineralogist, 45, 437-443.
- 266 Berlepsch P., Balić-Žunić, T. and Makovicky, E. (1999) The superposition structure of
267 quadratite $Ag(Cd,Pb)AsS_3$. 1s. Det 30. Danske Krystallografmøde, Forskningscenter
268 Risø, 1999. Abstract 30.
- 269 Bonazzi, P., Keutsch, F.N. and Bindi, L. (2012) Manganquadratite, $AgMnAsS_3$, a new
270 manganese bearing sulfosalt from the Uchucchacua polymetallic deposit, Lima
271 Department, Peru: Description and crystal structure. American Mineralogist, 97, 1199-
272 1205.
- 273 Brese, N.E. and O’Keeffe, M. (1991) Bond-valence parameters for solids. Acta
274 Crystallographica, B47, 192-197.

- 275 Choe, W., Lee, S., O'Connell, P. and Covey, A. (1997) Synthesis and structure of new Cd-Bi-
276 S homologous series: a study in intergrowth and the control of twinning patterns.
277 Chemistry of Materials, 9, 2025-2030.
- 278 Dornberger-Schiff, K. (1956) On the order-disorder structures (OD-structures). Acta
279 Crystallographica, 9, 593-601.
- 280 Evstigneeva, T.L., A.D. Genkin, N.V. Troneva, A.A. Filimonova and Tsepina, A.I. (1973)
281 Shadlunite, a new sulfide of copper, iron, lead, manganese and cadmium from copper-
282 nickel ores. Zapiski Vsesoyuznogo Mineralogicheskogo Obshchestva, 102, 63-74 (in
283 Russian).
- 284 Graeser, S., Lustenhouwer, W. and Berlepsch, P. (1998) Quadratite, $\text{Ag}(\text{Cd,Pb})(\text{As,Sb})\text{S}_3$ – a
285 new sulfide mineral from Lengnau, Binntal (Switzerland). Schweizer
286 Mineralogische und Petrographische Mitteilungen, 78, 489-494.
- 287 Hahn, H. and Klingler, W. (1950) Untersuchungen über ternäre Chalkogenide. I. Über die
288 Kristallstruktur einiger ternärer Sulfide, die sich vom In_2S_3 ableiten. Zeitschrift für
289 Anorganische und Allgemeine Chemie, 263, 177-190.
- 290 Ibers, J.A. and Hamilton, W.C. Eds. (1974) International Tables for X-ray Crystallography,
291 vol. IV, 366p. Kynock, Dordrecht, The Netherlands.
- 292 Makovicky, E. and Mumme, W.G. (1983) The crystal structure of ramdohrite, $\text{Pb}_6\text{Sb}_{11}\text{Ag}_3\text{S}_{24}$,
293 and its implications for the andorite group and zinckenite. Neues Jahrbuch für
294 Mineralogie Abhandlungen, 147, 58-79.
- 295 Makovicky, E. and Topa, D. (2011) The crystal structure of gustavite, $\text{PbAgBi}_3\text{S}_6$. Analysis of
296 twinning and polytypism using the OD approach. European Journal of Mineralogy, 23,
297 537-550.

- 298 Murciego, A., Pascua, M.I., Babkine, J., Dusausoy, Y, Medembach, O. and Bernhardt, H-J.
299 (1999) Barquillite, $\text{Cu}_2(\text{Cd,Fe})\text{GeS}_4$, a new mineral from Barquilla deposit, Salamanca,
300 Spain. *European Journal of Mineralogy*, 11, 111-117.
- 301 North, A.C.T., Phillips, D.C. and Mathews, F.S. (1968) A semiempirical method of
302 absorption correction. *Acta Crystallographica*, A24, 351-359.
- 303 Robinson, K., Gibbs, G.V. and Ribbe, P.H. (1971) Quadratic elongation; a quantitative
304 measure of distortion in coordination polyhedra. *Science*, 172, 567-570.
- 305 Sheldrick, G.M. (2008) A short history of SHELX. *Acta Crystallographica*, A64, 112-122.
- 306 Skinner, B.J. (1961) Unit-cell edges of natural and synthetic sphalerites. *American*
307 *Mineralogist*, 46, 1399-1411.
- 308 Szymański, J.T. (1978) The crystal structure of černyite, $\text{Cu}_2\text{CdSnS}_4$, a cadmium analogue of
309 stannite. *Canadian Mineralogist*, 16, 147-151.
- 310 Xu, Y.N. and Ching, W.Y. (1993) Electronic, optical, and structural properties of some
311 wurtzite crystals. *Physical Review*, B48, 4335-4351.
- 312 Zelenski, M., Garavelli, A., Pinto, D., Vurro, F., Moëlo, Y., Bindi, L., Makovicky, E. and
313 Bonaccorsi, E. (2009) Tazieffite $\text{Pb}_{20}\text{Cd}_2(\text{As,Bi})_{22}\text{S}_{50}\text{Cl}_{10}$, a new chloro-sulfosalt from
314 Mutnovsky volcano, Kamchatka Peninsula, Russian Federation. *American Mineralogist*,
315 94, 1312-1324.
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323 FIGURE CAPTIONS

324 FIGURE 1- M3 (white) and M3' (black) sites within the octahedral cavity. Ag at M3 links five
325 sulfur atoms in a square-pyramidal coordination; Pb at M3' assumes an octahedral
326 coordination. Sulfur atoms are depicted as small gray circles.

327

328 FIGURE 2- Succession of (Cd,Ag)CdS₂ (A) and (Ag,Pb)AsS₂ (B) layers stacked along [001].

329 The B-A-B stacking generates slabs of galena-like edge-sharing CdS₆ and
330 (Cd,Ag)S₆ octahedra (depicted in white), and slabs containing two sets of AgS₅
331 pyramids (in gray). Arsenic atoms are depicted as black circles.

332

333 FIGURE 3- Trapezoidal net of sulfur atoms (B plane) with a zig-zag trend of S-S distances

334 (3.92-3.96 Å) along the **a**_{layer} direction and straight trend with a regular alternation
335 of shorter (3.39 Å) S-S intervals and longer (4.42 Å) S-S intervals along the **b**_{layer}
336 direction. White, black and gray circles represent Ag at M3, As and S respectively.
337 M3' site is omitted for clarity. S-S tie-lines are depicted in gray. Long As-S bonds
338 are dashed.

339

340 FIGURE 4- Two adjacent B planes shifted against one another and related by two fold rotation

341 axes in the interspace. White, black and gray circles represent Ag at M3, As and S
342 respectively. M3' site is omitted for clarity. S-S contacts are depicted in gray. Long
343 As-S bonds are dashed. The zig-zag S-S tie-lines, parallel to the **a** vector of each of
344 the two B planes, are perpendicular to one another across the interspace, a case so
345 far unique among sulfosalts.

346

TABLE 1 – Electron microprobe analyses (means, ranges and standard deviations in wt % of elements) and atomic ratios (on the basis of 6 atoms) for quadratite.

	wt %	range	σ	atomic ratios
Tl	0.23	0.04 – 0.37	0.05	0.005
Ag	26.30	25.42 – 26.63	0.32	0.994
Cu	0.10	0.00 – 0.12	0.03	0.006
Pb	11.72	11.02 – 11.87	0.15	0.231
Cd	20.35	19.79 – 20.68	0.28	0.738
Zn	0.04	0.00 – 0.09	0.01	0.002
Fe	0.06	0.03 – 0.09	0.02	0.004
Mn	0.03	0.01 – 0.06	0.02	0.003
Sb	0.05	0.00 – 0.12	0.02	0.003
As	17.55	16.94 – 18.33	0.23	0.955
Cr	0.01	0.00 – 0.02	0.01	0.001
S	24.04	23.78 – 24.57	0.21	3.058
total	100.48	98.49 – 101.35		6.000

TABLE 2 – Crystallographic data and refinement parameters for quadratite

Crystal data	
Ideal formula	(Ag,Pb)(Cd,Ag)AsS ₃
Crystal system	tetragonal
Space group	<i>P</i> 4 ₃ 22
Unit-cell parameters <i>a</i> , <i>c</i> (Å)	5.5229(4), 33.399(5)
Unit-cell volume (Å ³)	1018.8(2)
<i>Z</i>	8
Crystal size (mm)	0.070×0.090×0.095
Data collection	
Diffractometer	Bruker MACH3
Temperature (K)	298(3)
Radiation, wavelength (Å)	MoK α , 0.71073
θ_{\max} for data collection (°)	30.00
<i>h</i> , <i>k</i> , <i>l</i> ranges	0 – 7, 0 – 7, 0 – 46
scan mode, scan width (°), scan speed (°/min)	ω , 2.00, 2.75
Total reflections collected	2324
Unique reflections (<i>R</i> _{int})	1485 (2.25%)
Unique reflections <i>F</i> > 4 σ (<i>F</i>)	558
Absorption correction method	ψ -scan (North et al. 1968)
Structure refinement	
Refinement method	Full-matrix least-squares on <i>F</i> ²
Weighting scheme	1/ σ^2 (<i>F</i>)
Data/restraints/parameters	2324/0/61
<i>R</i> ₁ [<i>F</i> > 4 σ (<i>F</i>)]	4.84%
<i>R</i> ₁ all	6.08%
Largest diff. peak and hole (e ⁻ /Å ³)	4.45, -5.00

TABLE 3 – Atoms, site occupancy, fractional atom coordinates (\AA), and atomic displacement parameters (\AA^2) for quadratite.

atom	site occupancy	<i>x</i>	<i>y</i>	<i>z</i>	U_{iso}	U_{11}	U_{22}	U_{33}	U_{23}	U_{13}	U_{12}
M1	4 <i>c</i> Cd _{0.58} Ag _{0.42}	0.2429(3)	0.2429(3)	1/8	0.0237(3)	0.0246(4)	0.0246(4)	0.0220(5)	0.0001(4)	-0.0001(4)	0.001(2)
M2	4 <i>c</i> Cd _{1.00}	0.7382(3)	0.7382(3)	1/8	0.0235(3)	0.0227(4)	0.0227(4)	0.0249(5)	0.0003(4)	-0.0003(4)	-0.001(2)
M3	8 <i>d</i> Ag _{0.787(4)}	0.748(2)	0.236(2)	0.0337(1)	0.0240(6)	0.0247(8)	0.0286(7)	0.019(1)	0.003(2)	-0.001(2)	-0.0012(9)
M3'	8 <i>d</i> Pb _{0.213(4)}	0.740(3)	0.242(4)	0.0417(2)	0.0240(6)	0.0247(8)	0.0286(7)	0.019(1)	0.003(2)	-0.001(2)	-0.0012(9)
As	8 <i>d</i> As _{1.00}	0.2559(3)	0.7443(3)	0.04947(3)	0.0208(2)	0.0206(6)	0.0212(6)	0.0205(4)	0.0001(7)	-0.0007(7)	-0.001(1)
S1	8 <i>d</i> S _{1.00}	0.2220(7)	0.7364(8)	0.11861(7)	0.0201(6)	0.024(2)	0.018(1)	0.019(1)	0.002(1)	0.003(1)	0.002(2)
S2	8 <i>d</i> S _{1.00}	0.6646(6)	0.7249(8)	0.0474(1)	0.0254(9)	0.028(2)	0.022(2)	0.026(2)	-0.001(2)	0.004(1)	0.002(2)
S3	8 <i>d</i> S _{1.00}	0.2334(7)	0.1620(6)	0.04691(8)	0.0208(8)	0.016(2)	0.033(2)	0.014(1)	0.001(1)	0.003(2)	0.002(2)

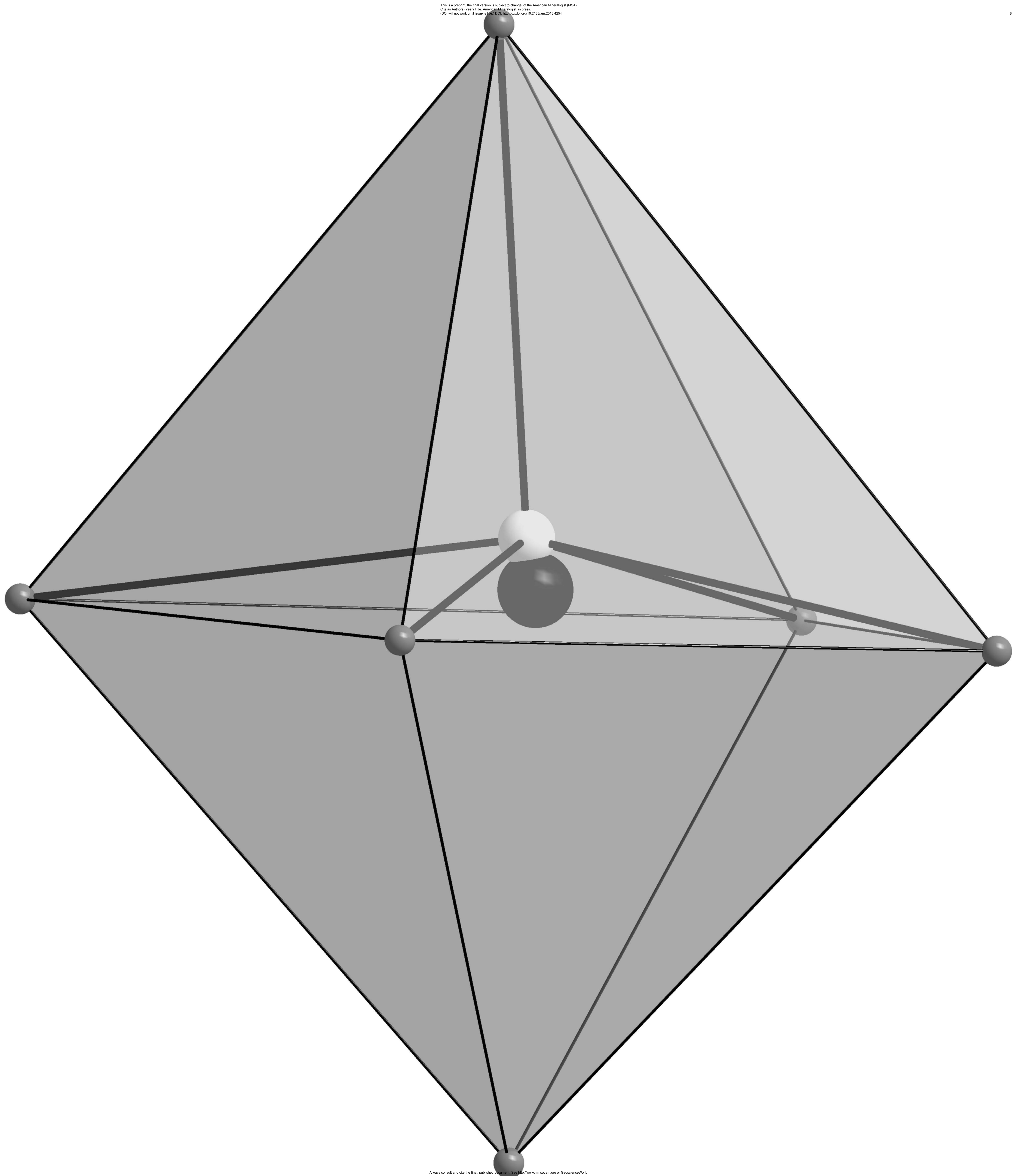
TABLE 5 – Selected bond distances (Å) for quadratite.

M1 - S3 (x2)	2.647(3)	M2 - S2 (x2)	2.624(3)
- S1 (x2)	2.736(5)	- S1 (x2)	2.681(4)
- S1 (x2)	2.808(5)	- S1 (x2)	2.859(4)
mean	2.730	mean	2.721
V_p	26.52	V_p	26.35
σ_{oct}^2	51.5	σ_{oct}^2	43.1
λ_{oct}	1.0161	λ_{oct}	1.0144
M3 - S3	2.724(4)	M3' - S2	2.71(2)
- S3	2.747(9)	- S3	2.77(2)
- S2	2.78(1)	- S3	2.84(2)
- S2	2.89(1)	- S2	2.89(2)
- S3	2.904(9)	- S3	2.994(9)
mean	2.810	- S1	2.999(8)
		mean	2.867
As - S3	2.261(4)		
- S2	2.312(4)		
- S1	2.317(3)		
mean	2.297		

Note: the octahedral angle variance (σ^2) and the octahedral quadratic elongation (λ) were calculated according to Robinson et al. (1971); M3-S longer than 3.2 Å are neglected.

TABLE 6 - Bond-valence (*v.u.*) arrangement for quadratite.

	M3	M1	M2	As	Σ S
	$\text{Ag}_{0.787}\text{Pb}_{0.213}$	$\text{Cd}_{0.58}\text{Ag}_{0.42}$	Cd	As	
S1		$0.26^{x2\downarrow x1\rightarrow}$, $0.20^{x2\downarrow x1\rightarrow}$	$0.36^{x2\downarrow x1\rightarrow}$, $0.22^{x2\downarrow x1\rightarrow}$	0.89	1.93
S2	0.23, 0.18		$0.42^{x2\downarrow x1\rightarrow}$	0.90	1.73
S3	0.29, 0.26, 0.16	$0.31^{x2\downarrow x1\rightarrow}$		1.03	2.05
	1.12	1.54	2.00	2.81	



B —
A —
B —

