1 **REVISION 2** 2 3 Cation arrangement in the octahedral and tetrahedral sheets of cis-vacant polymorph of dioctahedral 2:1 phyllosilicates by quantum mechanical calculations 4 E. ESCAMILLA-ROA<sup>a</sup>, A. HERNÁNDEZ-LAGUNA<sup>b</sup>, and C. IGNACIO SAINZ-DÍAZ<sup>b\*</sup> 5 6 7 8 <sup>a</sup> Instituto de Astrofísica de Andalucía (CSIC), Glorieta de la Astronomía s/n, 18008 9 Granada (Spain). 10 <sup>b</sup> Instituto Andaluz de Ciencias de la Tierra (CSIC-UGR), Avda Las Palmeras 4, 18100 11 12 Armilla, Granada (Spain). 13 14 \* Corresponding author: ignacio.sainz@iact.ugr-csic.es 15 16 Abstract 17 18 Density Functional Theory (DFT) calculations were performed to study the 19 crystallographic properties of the cis-vacant form of dioctahedral 2:1 phyllosilicates. 20 Samples with different layer charges are studied; only tetrahedrally charged, only octahedrally charged, or mixed octahedrally/tetrahedrally charged. The isomorphous 21 22 cation substitutions were explored in different relative positions with substitutions of octahedral Al<sup>3+</sup> by Mg<sup>2+</sup> or Fe<sup>3+</sup>, tetrahedral substitution of Si<sup>4+</sup> by Al<sup>3+</sup>, and different 23 interlayer cations (IC) (Na<sup>+</sup>, K<sup>+</sup>, and Ca<sup>2+</sup>). X-Ray diffraction patterns of cis-vacant and 24 25 trans-vacant forms of phyllosilicates were simulated and compared. The experimental observation of clustering tendency of  $Fe^{3+}$  and dispersion tendency of  $Mg^{2+}$  in the 26 octahedral sheet is reproduced and explained with reference to the relative energies of 27 28 the octahedral cation arrangements observing the same tendency that in the trans-vacant 29 forms. These energies are higher than those due to the IC/tetrahedral and IC/octahedral 30 relative arrangements. The tetrahedral and octahedral substitutions that generate charged 31 layers tend also to be dispersed. The energy difference between the cis-vacant and trans-32 vacant polymorphs is smaller than that of cation arrangements. 33

34 Keywords: DFT, clays, cation-ordering, phyllosilicate, polymorph, cis-vacant.

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# 37 Introduction38

39 Phyllosilicates are part of clay minerals, being one the main components of the 40 Earth crust in soils and rocks. These minerals have also several technological uses as 41 materials in catalytic chemistry and green technologies (adsorption of pollutants and 42 treatment of industrial wastewaters). Besides, the adsorption and catalytic properties of 43 these minerals make to consider the clays as support for the origin of the live on Earth 44 and prebiotic reactions under hydrothermal conditions in sea-floors (Bernal, 1949; 45 Swadling et al. 2010). On the other hand, clay minerals have been detected in 46 carbonaceous chondrites of meteorites (Tagish Lake) (Herd et al., 2011), comets, 47 asteroids, Mars (Mustard et al. 2008) and some satellites of the Solar System (Hibbitts 48 and Szanyi, 2007; Lebofsky et al., 1982; Rubin, 1997). The distribution of these 49 minerals in the asteroid belt can provide some clues to explain the conditions in which 50 the solar system was originated.

51 The 2:1 phyllosilicates have a layered structure and consist of an octahedral 52 (Oct) sheet sandwiched between two tetrahedral (T) sheets. The T sheet is formed by 53 tetrahedra of  $SiO_4$  and the Oct sheet is formed by octahedra of Al oxides. The T sheets 54 are always bonded to Oct sheets through oxygen atoms. The Oct sheet has unshared 55 oxygen atoms forming OH groups. On the other hand, in dioctahedral phyllosilicates, 56 one out of three octahedral positions is not occupied by cations, forming a vacant site. 57 The OH groups determine two kinds of crystal forms depending on their disposition in 58 the vacant site of the octahedral sheet, i.e. when the OH groups can be on the same side 59 (cis-vacant, cv) or on opposite sides (trans-vacant, tv) of the vacant site (Fig. 1). These 60 cis-vacant/trans-vacant configurations were first reported by Méring and Oberlin (1971) 61 in montmorrillonite. Drits et al. (1984) were the first to distinguish the reflections of 62 each configuration and to deduce the crystal structure of a cv illite model. However,

63 Drits and Zviagina (2009) noted that in the powder XRD patterns of trans-vacant 3T 64 (3T-tv) and 1M-cv mica polymorphs, the hkl reflections had similar intensities and very 65 close positions being difficult to distinguish them especially for interstratificates of cv 66 and tv layers. Tsipursky and Drits (1984) revealed semi-guantitatively the cv/tv 67 proportions of several dioctahedral 2:1 phyllosilicates, finding a higher cv proportion in 68 montmorillonites than in nontronites and beidellites. The cv polymorph shows a 69 different reactivity to the tv in the dehydroxylation reaction. The cv/tv proportion can be 70 estimated in illites and smectites by X-ray diffraction and thermal analysis (Drits et al. 71 1998). In smectites, the octahedral sheet tends to be cv, whereas illites have mainly a tv 72 configuration (Cuadros, 2002); however, there is no linear relationship between the 73 cv/tv ratio and smectite/illite proportion and some experimental discrepancies have been 74 reported (Drits et al. 2006). For example, Tsipursky and Drits (1984) found that 75 montmorillonite and Al-rich smectites are mainly cv, whereas McCarty and Reynolds 76 (1995) discovered that the proportion of cv layers increased with tetrahedral Al content. 77 Drits (2003) indicated that the cv/ty proportion is related with the formation mechanism 78 of these phyllosilicates. Drits et al. (1998) proposed that illite-smectite interstratificates 79 (I-S) formed from volcanic material contains a significant amount of cv layers, whereas 80 I-S generated from weathered illitic material consists of ty 2:1 layers, according with 81 investigations of smectite illitization of K-bentonites (Cuadros and Altaner, 1998), and 82 hydrothermally altered rhyolitic volcanoclastic materials (Drits et al., 1996).

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The wide diversity of compositions of these minerals is due to their capacity of isomorphous cation substitutions of Al <sup>3+</sup> mainly by Fe <sup>3+</sup> and Mg <sup>2+</sup> in the octahedral sheets, and Si <sup>4+</sup> by mainly Al <sup>3+</sup> in the tetrahedral sheet. These cation substitutions produce compositional heterogeneity and order-disorder phenomena in the crystal 88 structure of these minerals that, along with the stacking ordering of the layers, existence of interstratificates of layers with different crystal-chemistry, and the small particle size 89 90 of clavs, make it difficult to obtain precise structural data by diffraction techniques. 91 These cation substitutions can affect to the cv/tv proportion during the crystallization of 92 these minerals. During the illitization process of montmorillonite, the formation of illite 93 layers should lead to an increase of the proportion of tv layers. However, this process 94 depends on the chemical composition and no proportional relationship between the 95 polymorph ratio and the rate of transformation from smectite to illite has been found 96 (Cuadros and Altaner, 1998; Drits 2003). Drits and Zviagina (2009) suggested that the 97 cv/tv ratio can also depend on the octahedral cation arrangements.

98 On the other hand, the effect of cation substitutions on the tv forms of 99 phyllosilicates has been studied by computational methods (Palin et al. 2004; Sainz-100 Díaz et al. 2001a, 2003a; Hernández-Laguna et al. 2006, Botella et al. 2004) showing 101 that the cation ordering is highly dependent on the chemical composition. For smectite 102 and illite there is not a long-range octahedral cation ordering but a short-range order in small domains (Sainz-Díaz et al. 2003a, 2003b). In tv, the <sup>IV</sup>Al<sup>3+</sup> tends to be dispersed 103 along the tetrahedral sheet. The octahedral  $Mg^{2+}$  and  $Fe^{3+}$  cations tend to be dispersed or 104 105 clustered, respectively, along the octahedral sheet (Ortega-Castro et al. 2010). However, 106 the cv polymorph has received less attention, and fewer studies related with cation 107 substitution on cv forms have been reported (Sainz-Díaz et al. 2001b, 2005). The aim of 108 this work is to study computationally the effect of the cation substitution arrangements 109 (in tetrahedral and octahedral sheet) in the cis-vacant polymorph on the energy and 110 geometrical parameters.

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#### 112 Computational methodology

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113 In order to simulate different compositions of dioctahedral 2:1 phyllosilicates of the cv polymorphs, we used the SIESTA program (Soler et al., 2002) based on the 114 115 Density Functional Theory (DFT), and numerical atomic orbitals (NAO). We used the 116 Generalized Gradient Approximation with the PBE exchange correlation functional 117 (Perdew, et al., 1996), and double- $\zeta$  polarized basis sets, exploring two k points in the 118 Brilloin zone. To describe the core of atoms, we used norm-conserving pseudopotentials 119 (Troullier and Martins, 1991). In each structure, we relax all atomic positions and lattice 120 parameters using a force tolerance of 0.04 eV/Å. In samples with Fe, the minimum spinstate of Fe<sup>3+</sup> cations was considered. The rest of calculation conditions have been 121 122 optimized and described elsewhere (Sainz-Díaz et al. 2005). This methodology has been 123 previously used satisfactorily reproducing the main crystallographic and spectroscopic 124 properties of phyllosilicates (Sainz-Díaz et al. 2002; Botella et al. 2004; Hernández-125 Laguna et al. 2006). Powder X-ray diffraction (PXRD) pattern of the fully optimized cv 126 and tv crystal structures were simulated by means of the Reflex program within the 127 Material Studio package (Accelrys Inc.) for a average crystalline domain of 50 nm with 128 a wavelength of 1.54 Å.

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The crystal structure and atomic positions were taken from the experimental data of models proposed by Tsipursky and Drits (1984) based on electron diffraction for the cv forms of dry samples of smectites and illites. The H atom coordinates were included manually and optimised previously by Sainz-Díaz et al. (2002). All samples are also completely dry in our simulations. The presence of additional water molecules would demand a higher computational effort and time, owing to the higher number of atoms and the appearance of several minima in a quite flat potential energy surface. This could

<sup>130</sup> Models

also produce a noise effect in our energy calculations between the cation arrangementsof cv forms and between the cv and tv polymorphs.

We use one unit cell (40–43 atoms) with periodic boundary conditions. Hence, only formal cation substitutions can be included, that is, the minimum substitution degree is one cation per unit cell and no partial substitution was possible. This limitation generates models with cation contents that can be slightly different that in natural samples.

145 To study the effect of the cation substitutions in different layers we propose 16 models, based on the general formula  $IC_{x+y}(Al_{4-x-z}Mg_xFe^{3+z})(Si_{8-y}Al_y)O_{20}(OH)_4$ , shown 146 in Table 1, in which the tetrahedral sheet  $Si^{4+}$  substitution by  $Al^{3+}$  and  $Al^{3+}$  by  $Mg^{2+}$  or 147  $Fe^{3+}$  in the octahedral sheet are considered. Several interlayer cations (IC) neutralize the 148 149 layer charge coming from the isomorphic substitution:  $Na^+$  (samples cis1, cis3, cis5, cis7, cis10, cis13, and cis15),  $K^+$  (cis2, cis4, cis6, cis8, cis11, cis14, and cis16), and 150  $Ca^{2+}$  (cis9 and cis12) are included. In this series, there are samples without tetrahedral 151 152 charge (cis3, cis4, and cis10-cis14), samples with a certain tetrahedral charge, samples 153 without octahedral charge (end member of beidellite, samples cis1 and cis2), and 154 samples with high octahedral charge (cis10-cis12). Samples with a high Fe content in 155 the octahedral sheet are also included (cis15 and cis16).

Samples **cis1** and **cis2** have only one tetrahedral sheet with substitution of one  ${}^{IV}AI^{3+}$  per unit cell that is surrounded by other Si cations in the neighbour unit cell taking into account the periodical boundary conditions. Samples **cis3** and **cis4** have no tetrahedral substitution and one Mg<sup>2+</sup> per unit cell in the octahedral sheet with only one interlayer cation per unit cell. Samples **cis5** and **cis6** have one  ${}^{IV}AI^{3+}$  cation substitution per unit cell in only one tetrahedral sheet and the other tetrahedral sheet has no substitution. This sample has one Fe<sup>3+</sup> cation per unit cell in the octahedral sheet and one interlayer cation

per unit cell. Samples cis7 and cis8 show one octahedral Mg<sup>2+</sup> substitution and one 163 tetrahedral <sup>IV</sup>Al<sup>3+</sup> substitution with two ICs per unit cell and all tetrahedral cavities are 164 occupied by IC's. Cis9 is similar to this last one, with the same tetrahedral and 165 166 octahedral composition but with one  $Ca^{2+}$  as IC per unit cell, where only half of the 167 tetrahedral cavities are occupied with IC's. Cis10 and cis11 have no tetrahedral substitution and two Mg<sup>2+</sup> cations per unit cell in the octahedral sheet with two 168 interlayer cations per unit cell. Cis12 is like this last one but with one  $Ca^{2+}$  as IC per 169 unit cell. Cis13 and cis14 have no tetrahedral substitution and one  $Mg^{2+}$  and one  $Fe^{3+}$ 170 171 cation per unit cell in the octahedral sheet with one IC per unit cell. Cis15 and cis16 show a high concentration of  $Fe^{3+}$  with two octahedral cations per unit cell and only one 172 tetrahedral substitution, <sup>IV</sup>Al<sup>3+</sup>, in only one tetrahedral sheet, and one interlayer IC per 173 174 unit cell (Table 1).

175 Charged samples have integer values of the charge per unit cell. Then these 176 cation substitutions decrease the symmetry of the crystal structure, and different cation 177 arrangements can exist for a certain cation composition. A specific crystallographic 178 definition of the cation substitution sites should be established for the comparison of 179 different cation arrangements. Considering a projection of these lattice structures on the plane (001), the tetrahedral  $Al^{3+}$  cation can be close to the (100) plane (T1) or close to 180 181 the (200) plane (T2) (Fig. 1). Analogously the octahedral cation substitution can be 182 close to the (100) plane (O1) or close to the (200) plane (O2) (Fig. 2). All our samples 183 are in the T2 arrangement. We explore several cation substitution arrangements in order 184 to determine the energy and geometrical differences. Similar arrangements have been 185 studied previously by DFT methodology in trans-vacant polymorphs (Hernández-186 Laguna et al., 2006).

- 187
- 188 **Results**

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189 In Table 2, the main crystal lattice parameters of the calculated structures with 190 different cation arrangements for the monosubstituted (per unit cell in the tetrahedral or 191 octahedral sheet) cv samples are compiled. The energy difference between cation-192 arrangements (relative energy from the minimum,  $\Delta E = 0.0$  eV) for each sample and the 193 energy difference between the cv and tv forms are also included in Table 2. The same 194 features are collected in Table 3 for the cv samples bisubstituted (per unit cell) in the 195 octahedral sheet. The corresponding values of these features for the tv forms have been 196 included in Tables 4 and 5 for comparisons (Hernández-Laguna et al. 2006).

197 Although the experimental studies of crystal lattice parameters were based on 198 mixtures of tv and cv forms (Tsipursky and Drits, 1984), the calculated values of cell 199 parameters are similar to the experimental values for clay minerals with similar 200 compositions to our models in the cv (Tables 2 and 3) and tv samples (Tables 4 and 5). 201 Nevertheless, the calculated values of the parameters a and b of cv and tv forms are 202 slightly larger than the experimental values. No significant differences (< 2%) are 203 observed in the calculated values of a within the series of cv samples. In general, 204 samples with Mg have a slightly greater value of a (5.28-5.30 Å in cis10-cis12), and 205 those with Fe has slightly smaller value of a (5.23 Å in cis5 and cis15). Similar 206 differences are observed in tv forms. The parameters c and  $\beta$  of the cv forms are 207 smaller than in the tv forms (Tables 4 and 5), but these differences of c and  $\beta$  are 208 balanced and the d(001) spacing  $(c.\sin\beta)$  is maintained at similar values for both forms, 209 as it was expected from experimental values.

A linear relationship is found between the d(001) spacing  $(c.\sin\beta)$  and the ionic potential (IP = q/ir; q = formal charge, ir = ionic radius, Shannon 1976) of the interlayer cation (IC) for a series with the same composition and different IC. This linear regression is observed for samples with tetrahedral and octahedral charges,

214  $(Si_7Al)(Al_3Mg)(IC^{x+})_{2/x}$  (cis7-cis9) (Fig. 3a), and with only high octahedral charge, 215  $(Si_8)(Al_2Mg_2)(IC^{x+})_{2/x}$  (cis10-cis12) (Fig. 3b). This relationship indicates that with a 216 higher IP the IC will be smaller or with higher charge and it will interact more with the 217 tetrahedral cavity decreasing the d(001) spacing. For example, in samples with only one 218 tetrahedral substitution of  $Al^{3+}$  (<sup>IV</sup>Al) per unit cell, cis1 (IC = Na<sup>+</sup>) shows a smaller 219 d(001) spacing ( $c.\sin\beta$ ) than cis2 (IC = K<sup>+</sup>).

220 Small geometrical differences are observed between the cation arrangements. In samples with only one octahedral substitution of  $Mg^{2+}$  per unit cell (cis3 and cis4), three 221 possible relative positions of  $Mg^{2+}$  with respect to the IC can be considered: O1, where 222 223 the IC and  $Mg^{2+}$  are in the same (100) plane and in the same tetrahedral cavity (Fig. 2a); O2a, where the IC is in the (100) plane and  $Mg^{2+}$  is in the (200) plane and both cations 224 are in the same (020) plane (Fig. 2b); and O2b, where the IC is in the (100) and (020) 225 planes and  $Mg^{2+}$  is in the (200) and (010) planes (Fig. 2c). In both samples, cis3 and 226 **cis4**, the most stable distribution is the O1, owing to the proximity of IC and  $Mg^{2+}$  that 227 228 increases the electrostatic interactions between IC and the MgOHAl and apical MgOSi oxygens that are highly charged due to the presence of  $Mg^{2+}$ . In cis3 the least stable 229 cation arrangement is the O2a. In this case the IC and Mg<sup>2+</sup> are also close and the 230 electrostatic interactions between IC and the O atoms joined to Mg<sup>2+</sup> are also strong. 231 However the IC are between two  $Mg^{2+}$  cations in the same (020) plane with an IC...Mg 232 distance of 5.23 Å. This arrangement produces a higher distortion due to the higher size 233 of  $Mg^{2+}$  with respect to the  $Al^{3+}$  in octahedral coordination (Shannon 1976), increasing 234 235 slightly the value of the lattice parameter a. In cis4 this O2a configuration is not so 236 unstable because this distortion is relaxed with a IC...Mg distance (6.00 Å) larger and a 237 higher lattice volume than in cis3. In the tv forms the relative energy of the cation 238 arrangements is the opposite, O2b is more stable than O1 (Table 4), although the energy 239 difference is very small. In general, the energy difference between these cation 240 arrangements is greater in the cv form than in tv (Sainz-Díaz et al., 2005). In the most 241 stable structure of **cis4**, the cv form is more stable than tv, probably due to that the 242 IC...Mg and HO...IC distances are slightly shorter in cv (5.16 and 3.81 Å) than in tv 243 (5.27 and 3.83 Å). In these samples, **cis3** and **cis4**, the configuration O1 has a higher value of b because both IC and  $Mg^{2+}$  cations are in the same plane along the b axis 244 245 producing a slight distortion. The configuration O2b shows a high value of d(001)246 spacing  $(c.\sin\beta)$  with respect to the rest. On the other hand, these samples (cis3 and cis4) 247 show smaller values of d(001) spacing than those with only tetrahedral charge, **cis1** and 248 cis2 or cis5 and cis6. This could possibly be caused by the octahedral source of negative charges created by the isomorphic substitution of Mg<sup>2+</sup>. This charge is more distributed 249 250 in the inner apical tetrahedral oxygens and attracts to the IC from both sides of the 251 interlayer space, whereas in cis1 and cis2 the charge defect comes from the external 252 basal tetrahedral sheet of only one side of the interlayer space. Similar effect was 253 detected in our calculated tv forms (Table 4). Sato et al. (1992) detected also 254 experimentally this effect in montmorillonite and beidellite with Na<sup>+</sup> and K<sup>+</sup> as IC.

In addition to the tetrahedral substitution, the octahedral substitution can be  $Fe^{3+}$ 255 instead of  $Mg^{2+}$  without generating octahedral charge (cis5 and cis6). Keeping the 256  $^{IV}Al^{3+}$  substitution in the site T2 and the IC along the (100) plane, we can consider two 257 possible cation arrangements of  $Fe^{3+}$  with respect to the IC: O1, where the  $Fe^{3+}$  are 258 along the (100) plane; and O2 with the  $Fe^{3+}$  in (200) plane. No significant differences in 259 260 the lattice parameters values are observed between both cation arrangements (Table 2). 261 In both samples, O1 is slightly more stable than O2, like in **cis3** and **cis4**, but with 262 smaller energy differences. In these samples the tetrahedral Al substitution is only on 263 one part of the interlayer space producing an asymmetry in this space and the tetrahedral charge makes that the IC are slightly displaced 0.1 Å from the center of interlayer to the
tetrahedral sheet which support the Al substitution as in cis1 and cis2. In the tv forms

trans5 and trans6, the O1 is also the most stable cation arrangement (Table 4).

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267 Cation isomorphous substitutions can produce octahedral and tetrahedral charge simultaneously, with one  $Mg^{2+}$  cation in the octahedral sheet and one  ${}^{IV}Al^{3+}$  in the 268 tetrahedral sheet per unit cell. In this work we study this kind of substitution with 269 different IC's, such as Na<sup>+</sup>, K<sup>+</sup>, and Ca<sup>2+</sup>, in cis7, cis8, and cis9, respectively. 270 Considering supercells of this series, all cation substitutions, <sup>IV</sup>Al<sup>3+</sup> and Mg<sup>2+</sup>, are 271 272 disperse following the Lowenstein rule (Lowenstein, 1954) in the tetrahedral sheet and avoiding also Mg<sup>2+</sup>OMg<sup>2+</sup> pairs in octahedral sheet. Taking into account the relative 273 positions of <sup>IV</sup>Al<sup>3+</sup> and Mg<sup>2+</sup> each other and with respect to the IC, several possible 274 cation arrangements can be considered. With divalent IC (cis9), only half of the 275 tetrahedral cavities are occupied by IC. Considering that the <sup>IV</sup>Al<sup>3+</sup> cations are in T2 276 277 position, the possible octahedral cation arrangements can be: O1, where the IC and  $Mg^{2+}$  are along the (100) plane (Fig. 2a); O2a, where the IC are along the (100) plane 278 and the Mg<sup>2+</sup> cations are in the planes (200) and (020) (Fig. 2b); and O2b, like the 279 previous one but with the  $Mg^{2+}$  along the planes (200) and (010) (Fig. 2c). With 280 281 monovalent IC (cis7 and cis8) all tetrahedral cavities are occupied by IC. In all cases the O2b configuration is the most stable (Table 2), because both substitutions, <sup>IV</sup>Al<sup>3+</sup> and 282  $Mg^{2+}$ , sources of the tetrahedral and octahedral charges, are more separate from each 283 284 other than in the other configurations. In this series the energy differences between 285 cation arrangements are much higher than in the above previous samples. Similar 286 behaviour is observed in the tv forms of this series, **trans7-trans9**, where the O2b is the 287 most stable cation arrangement (Table 4). 288

## 289 Bisubstitutions in the octahedral sheet

Instead of tetrahedral cation substitution, isomorphous substitutions of two Mg<sup>2+</sup> 290 cations per unit cell can be produced. These substitutions generate octahedral charge 291 292 that is compensated by different IC's,  $Na^+$  (cis10),  $K^+$  (cis11), or  $Ca^{2+}$  (cis12). In 293 addition to the relative positions of the octahedral substitutions with respect to the IC, 294 we have to consider the specific cation arrangements among the octahedral cations. As 295 explained elsewhere (Sainz-Díaz et al., 2002; Hernández-Laguna et al., 2006), three 296 kinds of arrangements can be considered: *ortho*, where the cation substitution sites are 297 the nearest neighbors to a distance of 2.9-3.1 Å; meta, where these substituted sites are separated by one  $Al^{3+}$  with an inter-site distance about 5 Å; and *para*, when these sites 298 are separated by two  $Al^{3+}$  (with an inter-site distance close to 6 Å) in the same unit cell, 299 300 respectively. Taking into account the translational crystal lattice periodicity and the 301 neighbor unit-cells, these cation arrangements considered in one unit cell will be related 302 with more arrangements. Then, two ortho arrangements can exist, one forming a chain of  $Mg^{2+}$  along the *a* axis direction (Fig. 4a), and another one that is the same of the *para* 303 304 distribution where all patterns, ortho, meta and para, co-exist (Fig. 4b). Besides, the *meta* distribution has also two more  $Mg^{2+}$  cations as second neighbors within a *meta* 305 306 ordering pattern with the vicinal cells (Fig. 4c and 4d).

In all cases the *meta* arrangement is the most stable and the *ortho* is the least stable with higher energy differences than in the above previous arrangements (Table 3). In the samples with monovalent IC, **cis10** and **cis11**, two possible *meta* distributions can exist: *meta*-1, where IC and  $Mg^{2+}$  are in the same (020) plane (Fig. 4d), and *meta*-2 (Fig. 4c). This last one is slightly more stable than the *meta*-1. In all cases, no significant difference in the crystal lattice parameters is found within the cation arrangements. This is consistent with previous results on tv forms (Table 5) indicating

the tendency of  $Mg^{2+}$  to be dispersed along the octahedral sheet of phyllosilicates 314 315 (Cuadros et al. 1999, Sainz-Diaz et al. 2000, Hernández-Laguna et al. 2006). The 316 energy differences derived of the cation distribution along of the octahedral sheet are 317 greater than those derived from IC/tetrahedral and IC/octahedral cation arrangements in 318 previous samples. The ortho configuration has the highest polyhedron distortions and 319 the highest repulsive interactions of the negative charge generated by the presence of two <sup>VI</sup>Mg<sup>2+</sup> cations as first neighbors separated by 2.98 Å, which forms a chain of Mg<sup>2+</sup> 320 321 cations along the *a* axis direction. This arrangement produces a high concentration of 322 charge along this direction and a high distortion in the coupling of polyhedra due to the higher ionic radius of Mg<sup>2+</sup> than Al<sup>3+</sup>. Therefore, the probability to find a MgMg pair 323 324 will be very low in these samples. In the para configuration this distortion is partial and 325 this configuration has lower energy than ortho and higher energy than meta.

326 A semiquantitative approach to analyze the energetic of the cation arrangement 327 in this  $Al_2Mg_2$  system is to consider the interaction energies between both cations as 328 first, and second neighbours in the ortho, meta and para arrangements in one unit cell. 329 These interactions can be defined as cation exchange potential terms  $(J_{AA})^{i}$  in the 330 octahedral sheet described elsewhere (Sainz-Díaz et al. 2003a): Specific formulae 331 neglecting third and fourth neighbour interactions were applied to the ty forms previously (Hernández-Laguna et al. 2006). Then, the  $J_{AA}^{1}$  and  $J_{AA}^{2}$  were determined 332 from the energy differences of *ortho*, *meta* and *para* arrangements in the unit cell.  $J_{AA}^{1}$ 333 and  $J_{AA}^{2}$  mean the energy change for forming two homocationic pairs  $(Al^{3+}..Al^{3+})$  and 334 Mg<sup>2+</sup>..Mg) from two heterocationic pairs (2 Al<sup>3+</sup>..Mg<sup>2+</sup>) at first and second 335 neighbourhood ( $J_{AA}^{i} = E_{AA}^{i} + E_{BB}^{i} - 2E_{AB}^{i}$ ), respectively (Table 6). Exchange potentials 336 at first neighbours,  $J_{AA}^{1}$ , are approximately seven times larger than the second 337 338 neighbour terms owing to the shorter distances between cations in the octahedral sheet.

The  $J_{AA}^{1}$  values in the cv polymorphs are 1.5 and 1.75 times larger than in tv for Na<sup>+</sup> 339 and K<sup>+</sup> samples, respectively, whereas  $J_{AA}^2$  values in cv are 2.8, and 12.9 times larger 340 than in tv for Na<sup>+</sup> and K<sup>+</sup> samples, respectively. This could indicate qualitatively that 341 342 the octahedral  $Mg^{2+}$  cations in cv forms tend to be more dispersed than in tv forms. On the other hand, in  $Ca^{2+}$  samples both exchange potentials in cv are similar that those in 343 344 tv (Hernandez-Laguna et al 2006). Plotting both exchange potentials for cv forms as a 345 function of the formal charge/ionic radius of the IC (Fig. 5) a non-linear decreasing is 346 observed, showing an opposite trend with respect to the tv samples (Hernandez-Laguna 347 et al, 2006). The interaction of the IC with the octahedral cation exchange dynamics is 348 clearly observed in both cv and tv polymorph, but the opposite trend is surprising. The 349 position of the OH's around the vacant is quantitatively different for the cation 350 exchange in the octahedral sheet and the effect of the IC on this cation exchange is 351 different in both cv and tv polymorphs. Nevertheless, this study is based only in 352 exchange potentials for first and second neighbours, however our results highlight the 353 necessity of further work on cation ordering in cv forms with larger models.

The double substitution in the octahedral sheet can be also by one  $Mg^{2+}$  and  $Fe^{3+}$ 354 355 per unit cell without tetrahedral substitution, generating less interlayer charge, cis13 (IC =  $Na^+$ ) and **cis14** (IC = K<sup>+</sup>). In all cases the *meta* configurations are the most stable, 356 whereas the ortho and para have similar energy each other (Table 3). In this series 357  $(Mg^{2+}/Fe^{3+})$  the energy difference between *meta* and *ortho* configurations is smaller 358 than in the previous cis10-cis12 series. The  $Fe^{3+}$  cation does not generate a negative 359 360 charge in the layer, then the repulsive interactions are smaller and the charge distribution is more dispersed than in the series with two Mg<sup>2+</sup> cations. No significant 361 362 difference in the crystal lattice parameters are observed between the cation 363 arrangements. In the tv forms trans13 and trans14 (Table 5) the meta configuration is

also the most stable cation arrangement and the *ortho* one is the least stable one.
However, in tv forms the *para* one has similar energy to *meta* one (Hernández-Laguna
et al. 2006).

367

The double octahedral substitution can be with two Fe<sup>3+</sup> cations and one 368 tetrahedral <sup>IV</sup>Al<sup>3+</sup> substitution within one unit cell, cis15 (IC = Na<sup>+</sup>) and cis16 (IC = K<sup>+</sup>). 369 In this series there is no octahedral charge and the interlayer charge comes from the 370 tetrahedral sheet. Considering the <sup>IV</sup>Al<sup>3+</sup> site in T2 and the IC in the (100) plane, we 371 calculate the *ortho*, *meta*, and *para* arrangements of  $Fe^{3+}$  cations. In all cases of this 372 373 series, the ortho configuration is the most stable and the meta one is the least stable 374 (Table 3). This is consistent with previous experimental and theoretical results on tv forms indicating the tendency of  $Fe^{3+}$  to be clustered along the octahedral sheet of 375 376 phyllosilicates (Cuadros et al. 1999; Sainz-Diaz et al. 2000; Hernández-Laguna et al. 377 2006). However, in the cv forms, the energy differences between these configurations 378 are greater than in tv forms (Table 5).

379

#### 380 *Cis-vacant / trans-vacant configurations*

381 The cv/tv proportion in these phyllosilicates can be determined with the 382 parameter  $\varepsilon$  ( $\varepsilon = |c.\cos\beta|/a$ ) (Drits and McCarty 1996). This can be calculated from the 383 d values obtained from the indexing of the reflection lines in powder XRD. In the 384 quantitative determination of cv/tv proportions, values of  $\varepsilon$  for pure cv and pure tv385 structures must be determined previously. However, different experimental values have been reported for similar samples, such as  $\varepsilon_{cis} = 0.308$  and  $\varepsilon_{trans} = 0.383$  (McCarty and 386 Reynolds 1995), and  $\varepsilon_{cis} = 0.300-0.302$  and  $\varepsilon_{trans} = 0.400$  (Drits and McCarty 1996), 387 388 being a handicap to apply it to other samples. We can calculate this parameter from a

389 theoretical crystal structure with one specific cation content, a cation distribution for 390 only cv or tv forms and for different cation compositions and cation arrangements 391 (Tables 2-5). In our samples, we observe a significant variation of this parameter with 392 the nature of cation substitution and also with the relative arrangements of these 393 substituted cations, being in the range of 0.23 - 0.35 for cv forms. Nevertheless, the 394 average value for all cv samples is 0.294 that is consistent with the experimental value 395 (0.300-0.302) obtained by Drits and McCarty (1996) with natural samples, where a 396 mixture of all situations, local cation compositions and cation arrangements, can exist. 397 Excluding the less probable cation arrangements (structures with high energy, relative 398 energy > 0.5 eV) the average value of  $\varepsilon$  is 0.297, closer to the experimentally estimated 399 value. There is no clear relationship between the nature of cation substitution and the variation of  $\varepsilon$ . Nevertheless, samples with Ca<sup>2+</sup> as IC (cis9 and cis12) show higher 400 values of  $\varepsilon$  than those with K<sup>+</sup> or Na<sup>+</sup>. Samples with high content of Fe<sup>3+</sup> (cis15 and 401 402 **cis16**) show also high values of  $\varepsilon$ . The variation of  $\varepsilon$  due to the cation arrangement some 403 times is greater than that due to the nature of cation substitution.

We can observe clearly the different values of  $\varepsilon$  in tv forms that appears in the range of 0.38-0.43. In general, the calculated *c* values are slightly greater than those estimated experimentally. In the tv forms, like in cv, no clear relationship between  $\Delta\varepsilon$ and nature of cation substitution and cation arrangement was found. In general, samples with Mg<sup>2+</sup> show lower  $\varepsilon$ .

In general the energy difference between cv and tv forms ( $\Delta E_{cv-tv}$ ) is smaller than that between the cation arrangements (Tables 2 and 3). The  $\Delta E_{cv-tv}$  can vary with the cation arrangement according to experimental results (Drits et al. 2006). The pattern of the relative cation distribution can be different in cv and tv forms. In some cases we compare the energy differences between those cv and tv configurations with similar 414 relative cation arrangement. When the cation arrangements have similar energy, we compare average energy values of each polymorph. In cases where the energy 415 416 differences between cation arrangements are important (> 0.2-0.25 eV), we used the 417 most stable configuration for each polymorph for energy comparisons. Values 418 calculated with different criteria are shown when the cv/tv energy difference changes 419 with the comparison criterion (Tables 2 and 3). In samples with only a tetrahedral 420 substitution (cis1 and cis2) the energy difference between polymorphs are negligible. 421 With the additional presence of Fe in octahedral sheet (cis5, cis6, cis15, and cis16), the 422 cv forms are more stable than tv. Samples with one octahedral Mg cation per unit cell 423 (cis3, cis4, cis7-cis9, and cis13-cis14) show that the tv are slightly more stable than cv. 424 The energy difference depends on the criterion for the cation arrangement comparison 425 and average values were considered when the energy difference between cation 426 arrangements are lower than 0.1 eV and only the most stable ones were considered for 427 the rest of cases (for example, the O1 arrangements of cis7 and cis8 were not considered 428 due to their high energy and consequently low probability to appear). In samples with 429 two octahedral  $Mg^{2+}$  cation substitutions and no tetrahedral charge (cis10-cis12) the 430 configuration cv is slightly more stable than tv.

431

We simulated the PXRD patterns of our models based on their crystal lattice structures and atomic positions. This simulation can be useful to experimental work in order to predict or identify reflections observed in the laboratory or to introduce this information in the simulated annealing programs used for identifying different crystal phases in a clay mineral. In all cv and tv forms of our series, the 060 reflection appears at 1.51-1.52 Å (1.53 Å in **cis11**) (61.1-60.7  $2\theta$  units) that is characteristic of dioctahedral phyllosilicates (beidellite and illite, Brindley and Brown 1980) and it can 439 be used for distinguishing the trioctahedral phyllosilicates where this 060 reflection 440 appears at 1.53 - 1.55 Å (60.5-59.5 2 $\theta$  units).

441 Comparing different cation arrangements for the same chemical composition, 442 the reflections positions are almost the same, changing only the relative intensities of 443 some reflections. For example in bisubstituted series in octahedral sheet, the PXRD 444 patterns of *ortho* and *para* arrangements are very similar (for **cis13**, Fig. 6a and 6b), 445 whereas the *meta* form shows more differences in the relative intensities, especially the 446 020 reflection that is more intense in *meta* (Fig. 6c) than in *ortho* and *para*, probably 447 due to the differences in the cell lattice parameter b (Table 3) that produces a 448 superposition of the 020,  $1\overline{10}$ , and 110 reflections increasing the intensity of this peak. This effect is more clear in **cis10** (with 2  $Mg^{2+}$  per unit cell), where the 020, or (020 + 449  $1\overline{10} + 110$ ) reflections are more intense than the 001 one (Fig. 7a). This variation of 450 451 relative intensities of XRD reflections with the octahedral cation distribution was 452 previously detected experimentally by Drits and Zviagina (2009). In general the high 453 intensity of the peak at 19.4-19.8° is mainly due to the 110 reflection in the cv forms or to the 020 reflection in the tv forms. In **cis10** the 110,  $02\overline{2}$ , 111, and  $11\overline{3}$  reflections are 454 455 more intense (Fig. 7a) than in tv where the 020,  $1\overline{1}1$ ,  $11\overline{2}$ , and 112 reflections (Fig. 7b) 456 are significantly more intense than in cv. With respect to the peak positions, the main 457 differences are observed in the  $11\overline{2}$ , 112,  $11\overline{3}$ , and 202 reflections that appear at 25.2°, 458 28.2°, 31.8°, and 41.1° in cis10 (Fig.7a) and at 24.4°, 29.3, 31.0°, and 43.0° in trans10, 459 respectively (Fig. 7b).

In **cis15** the most intense reflection is the 001 one (Fig. 8a), being the relative intensities of the other reflections much lower than in the previous samples. Nevertheless, the relative intensities of the rest of peaks are similar, except the 002, 113, and 060 reflections that are much less intense than in **cis10**. Similar differences 464 were found in the tv forms (Fig. 8b). In this sample, the  $01\overline{1}$  reflection appears at 13.3°, 465 like in cis13, but it is not detected in cis10. In trans15 the ortho, meta and para 466 arrangements show similar positions of reflections with slight differences in relative 467 intensities in some reflections. However, some differences in the relative intensities and 468 reflection positions can be observed between the cv and tv forms of the most stable 469 cation arrangement, like in cis10/trans10 samples described above. These differences 470 between cv and tv forms are similar for all samples and are consistent with that found 471 experimentally by Drits (2003), and Zviagina et al. (2007).

472

#### 473 Discussion

474 In general the cv forms can present similar cation arrangements that the tv 475 forms. Within a certain chemical composition, the most stable cation arrangements are 476 similar for both polymorphs observing some differences in the relative energies between 477 arrangements. Nevertheless, the energy differences related with cation arrangements are 478 greater than those between cv and tv polymorphs. These energy differences between cv 479 and tv forms are too small to explain the probability to crystallize a cv or tv form with 480 relation to the chemical composition. Hence other factors can affect the cv and tv 481 formation in clay minerals and no prediction can be performed about the direct effect of 482 cation substitution on the cv/tv proportion. Though the temperature effect has not been 483 taken into account in our calculations, we can infer that the formation of these 484 polymorphs in the nucleation is not controlled thermodynamically. The different 485 proportion of these polymorphs in natural samples and conditions will be controlled by 486 kinetic conditions during the nucleation of these minerals. This fact can explain the non-487 linear relationship between illite/smectite and tv/cv proportions found experimentally in 488 natural samples (Drits, 2003; Drits and Zviagina, 2009).

The presence of water in the interlayer space in our models would generate more realistic models, but it would require a high computational cost. Besides, these more complex models would introduce another variable in our research moving over of our main aim, which is focused in the relative energy between the cation arrangements of cv forms and between the cv/tv forms. Within a systematic research, the scope of this work is to observe this behavior in dry samples. This work opens a window to explore more variables, such as, the water effect on these energy differences, in further researches.

496 Nevertheless, the presence of water will be in the interlayer space and interacting 497 with the IC and water could alter only slightly the relative proportion of these 498 polymorphs, because the energy differences are very small and lower than that from 499 cation arrangements. However, the water effect will be very important during the 500 nucleation process and formation of these polymorphs, where higher amount of water 501 can be present in hydrothermal or quasi-amorphous-phases scenarios that are out of the 502 scope of this work. From our relative energy results with ideal samples, layers with high 503 Mg content and no tetrahedral Al tend to be in a cv form, however during a illitization 504 process the tetrahedral Al content increases and the Mg content can decrease and the tv 505 form will be more stable and the system will tend to nucleate a tv form.

506 A remarkable consideration should be explained in order to understand the cv/tv 507 formation and the discrepancies found. We suggest that the crucial moment is the 508 nucleation step of each layer. The probability of formation of cv or tv polymorphs will 509 depend on the chemical composition of the local environment of this crystal-nucleus 510 and the nucleation kinetics. However, one layer cannot support cv and tv forms 511 simultaneously. This means that the crystal growth of the nucleated layer will maintain 512 the initial structure of the polymorph nucleated (cv or tv). The attachment of the 513 aggregation units during this crystal growth will depend more on the chemical 514 composition of the local environment than on the type of polymorph, due to the low 515 energy differences between cv and tv forms. This can explain that natural samples with 516 the same chemical composition can appear with different cv/tv polymorphism.

517 Besides, the cation arrangement is also important thermodynamically, even more 518 than the cv/tv proportion because of the higher energy differences between cation 519 arrangements. Hence both phenomena, local cation arrangement and cv/tv 520 polymorphism, can be established during the nucleation step. However, it is more 521 probable that the cv/tv forms are nucleated initially and after the cation arrangements 522 are established during the crystal growth, depending on the local chemical environment.

523 Another possibility is the possible formation of amorphous pre-nuclei phases 524 where the cv/tv polymorphs can be pre-established. The atoms in these amorphous 525 phases will have a higher mobility and some cation arrangements could be formed 526 during the equilibration time just before the nucleation looking for a low energy state. 527 This hypothesis would be within the recent concept of polyamorphism that have been 528 found in carbonates (Cartwright et al. 2012), where different amorphous phases can 529 exist and induce the nucleation of the corresponding crystal polymorph. In our minerals, 530 two different amorphous phases could be related with cv and tv crystal forms. However, 531 this subject is out of the scope of the present work and further investigations will be 532 necessary to understand the nucleation process of phyllosilicates.

533

The cation exchange potentials indicate a greater dispersion tendency of octahedral Mg cations in the cv forms than in tv. Nevertheless, in our calculations no temperature effect has been included. Hence our energy calculations cannot predict the possible preferences for cation arrangements that can occur during the cv/tv transformation in the dehydroxylation of cv forms where migrations of octahedral cations are produced at high temperatures for generating tv forms and the cation arrangements could be alteredin the short-range ordering of octahedral cations.

There are differences in intensities and positions in some reflections of the PXRD patterns between cv and tv forms, however these differences can change with the chemical composition and the cation arrangement. This fact is observed in our ideal theoretical models, but it should be taken into account in the experimental patterns with mixture of layers with different cation arrangements. Hence our calculated models can be useful for the experimental work in crystal structure determinations in phyllosilicates.

548

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#### 559 **REFERENCES CITED**

Bernal, J.D. (1949) The Physical Basis of live. Proceedings of the Physical Society A,
62, 537-558.

562

563 Botella, V., Timón, V., Escamilla-Roa, E., Hernández-Languna, A., and Sainz-Díaz,

564 C.I. (2004) Hydrogen bonding and vibrational properties of hydroxy groups in the

565 crystal lattice of dioctahedral clay minerals by means of first principles calculations.

- 566 Physics and Chemistry of Minerals, 31, 475-486.
- 567

568 Cartwright, J.H.E., Checa, A.G., Gale, J.D., Gebauer, D., and Sainz-Díaz, C.I. (2012) 569 Calcium Carbonate Polyamorphism and Its Role in Biomineralisation: How many ACCs are there?. Angewandte Chemie International Edition (in press). 570 571 Cuadros J. (2002) Structural insights from the study of Cs-exchanged smectites 572 573 submitted to wetting-and-drying cycles. Clay Minerals, 37, 473-486. 574 575 Cuadros, J., and Altaner, S.P. (1998) Characterization of mixed-layer illite-smectite 576 from bentonites using microscopic, chemical, and X-ray methods; constraints on the 577 smectite-to-illite transformation mechanism. American Mineralogist, 83, 762-774. 578 579 Cuadros, J., Sainz-Díaz, C.I., Ramírez, R., and Hernández-Laguna, A. (1999) Analysis 580 of Fe segregation in the octahedral sheet of bentonitic illite-smectite by means of FTIR, 581 27 Al MAS NMR and reverse Monte Carlo simulations. American Journal of Science, 582 299, 289-308. 583 584 Drits, V.A. (2003) Structural and chemical heterogeneity of layer silicates and clay 585 minerals. Clay Minerals, 38, 403-432. 586 587 Drits, V.A., Salyn, A.L. and Sucha, V. (1996) Structural transformations of 588 interstratified illite-smectites from Dolna Ves hydrothermal deposits: dynamics and 589 mechanisms. Clays and Clay Minerals, 44, 181-190. 590 591 Drits, V.A., Lindgreen, H., Salyn, A.L., Ylagan, R., and McCarty, D.K. (1998) 592 Semiquantitative determination of trans-vacant and cis-vacant 2:1 layers in illites and 593 illite-smectites by thermal analysis and X-ray diffraction. American Mineralogist, 83, 594 1188-1198. 595 596 Drits, V.A., and McCarty, D.K. (1996) The nature of diffraction effects from illite and 597 illite-smectite consisting of interstratified trans-vacant and cis-vacant 2:1 layers; a 598 semiquantitative technique for determination of layer-type content. American 599 Mineralogist, 81, 852-863. 600 601 Drits, V.A., McCarty, D.K., and Zviagina, B.B. (2006) Crystal-chemical factors 602 responsible for the distribution of octahedral cations over trans- and cis-sites in 603 dioctahedral 2:1 layer silicates. Clays and Clay Minerals, 54, 131-152. 604 605 Drits, V.A., and Zviagina, B.B. (2009) Trans-vacant and cis-vacant 2:1 layer silicates: 606 structural features, identification, and occurrence. Clays and Clay Minerals, 57, 405-607 415. 608 Drits, V.A., Plançon A., Sakharov, B.A., Besson, G., Tsipursky, S.I., and Tchoubar, C. 609 610 (1984) Diffraction effects calculated for structural models of K-saturated montmorillonite containing different types of defects. Clay Minerals, 19, 541-562. 611 612 613 Herd, C.D.K., Blinova, A., Simkus, D.N., Huang, Y., Tarozo, R., Alexander, C.M.O.D., 614 Gyngard, F., Nittler, L.R., Cody, G.D., Fogel, M.L., Kebukawa, Y., Kilcoyne, A.L.D., 615 Hilts, R.W., Slater, G.F., Glavin, D.P., Dworkin, J.P., Callahan, M.P., Elsila, J.E., De 616 Gregorio, B.T., and Stroud, R.M. (2011) Origin and Evolution of Prebiotic Organic Matter As Inferred from the Tagish Lake Meteorite. Science, 332, 1304-1307. 617

618 619 Hernández-Laguna, A., Escamilla-Roa, E., Timón, V., Dove, M.T., and Sainz-Díaz, C.I. 620 (2006) DFT study of the cation arrangements in the octahedral and tetrahedral sheets of 621 dioctahedral 2:1 phyllosilicates. Physics and Chemistry of Minerals, 33, 655-666. 622 623 Hibbitts, C.A., and Szanyi, J. (2007) Physisorption of CO<sub>2</sub> on non-ice materials relevant 624 to icy satellites. Icarus, 191, 371-380. 625 626 Lebofsky, L.A., Feierberg, M.A., and Tokunaga, A.T. (1982) Infrared observations of 627 the dark side of Iapetus. Icarus, 49, 382-386. 628 629 Lowenstein, W. (1954) The distribution of aluminium in the tetrahedra of silicates and 630 aluminates. American Mineralogist 39, 92-96. 631 632 McCarty, D.K., and Reynolds, R.C. (1995) Rotationally disordered illite/smectite in 633 Paleozoic K-bentonites. Clays and Clay Minerals, 43, 271-284. 634 635 Méring, J., and Oberlin, A. (1971). Smectites. In: The Electron-Optical Investigation of 636 Clays (J.A.Card, ed.). 193-229. Mineralogical Society, London, UK. 637 638 Mustard, J.F., Murchie, S.L., Pelkey, S.M., Ehlmann, B.L., Milliken, R.E., Grant, J.A., 639 Bibring, J.P., Poulet, F., Bishop, J., Dobrea, E.N., Roach, L., Seelos, F., Arvidson, R.E., 640 Wiseman, S., Green, R., Hash, C., Humm, D., Malaret, E., McGovern, J.A., Seelos, K., 641 Clancy, T., Clark, R., Marais, D.D., Izenberg, N., Knudson, A., Langevin, Y., Martin, 642 T., McGuire, P., Morris, R., Robinson, M., Roush, T., Smith, M., Swayze, G., Taylor, 643 H., Titus, T., and Wolff, M. (2008) Hydrated silicate minerals on Mars observed by the 644 Mars Reconnaissance Orbiter CRISM instrument. Nature, 454, 305-309. 645 646 Ortega-Castro, J., Hernandez-Haro, N., Dove, M.T., Hernández-Laguna, A., and Sainz-647 Díaz, C.I. (2010) Density functional theory and Monte Carlo study of octahedral cation 648 ordering of Al/Fe/Mg cations in dioctahedral 2:1 phyllosilicates. American 649 Mineralogist, 95, 209-220. 650 651 Palin, E.J., Dove, M.T., Hernández-Laguna, A., and Sainz-Díaz, C.I. (2004) A 652 computational investigation of the Al/Fe/Mg order-disorder behavior in the dioctahedral 653 sheet of phyllosilicates. American Mineralogist, 89, 164-175. 654 655 Perdew, J.P., Burke, K., and Ernzerhof, M. (1996) Generalized Gradient Approximation 656 Made Simple. Physical Review Letters, 77, 3865-3868. 657 658 Rubin, A.E. (1997) Mineralogy of meteorite groups. Meteoritics and Planetary Science, 659 32, 231-247. 660 661 Sainz-Díaz, C.I., Hernández-Laguna, A., and Dove, M.T. (2001a) Modelling of 662 dioctahedral 2:1 phyllosilicates by means of transferable empirical potentials. Physics 663 and Chemistry of Minerals, 28, 130-141. 664 665 Sainz-Díaz, C.I., Hernández-Laguna, A., and Dove, M.T. (2001b) Theoretical 666 modelling of cis-vacant and trans-vacant configurations in the octahedral sheet of illites

and smectites. Physics and Chemistry of Minerals, 28, 322-331.

| 668 |   |
|-----|---|
| 669 | Sainz-Díaz, C.I., Palin, E.J., Hernández-Laguna, A., and Dove, M.T. (2003a)               |
| 670 | Octahedral cation ordering of illite and smectite. Theoretical exchange potential         |
| 671 | determination and Monte Carlo simulations. Physics and Chemistry of Minerals, 30,         |
| 672 | 382-392.  |
| 673 |   |
| 674 | Sainz-Díaz, C.I., Palin, E.J., Hernández-Laguna, A., and Dove, M.T. (2003b) Monte         |
| 675 | Carlo simulations of ordering of Al Fe and Mg cations in the octahedral sheet of          |
| 676 | smectites and illites American Mineralogist 88 1033-1045                                  |
| 677 |   |
| 678 | Sainz-Díaz C I Timón V Botella V Artacho E and Hernández-Laguna A (2002)                  |
| 670 | Ouantum mechanical calculations of diactahadral 2:1 nhvllosilisates: Effect of            |
| 690 | Qualitum mechanical calculations of diocialicular 2.1 physiosincates. Effect of           |
| 000 | Ministruction distributions in pyrophymie, mile, and smectile. American                   |
| 681 | Mineralogist, 87, 958-965.  |
| 682 |   |
| 683 | Sainz-Díaz, C.I., Escamilla-Roa, E., and Hernández-Laguna, A. (2005) Quantum              |
| 684 | mechanical calculations of trans-vacant and cis-vacant polymorphism in dioctahedral       |
| 685 | 2:1 phyllosilicates. American Mineralogist, 90, 1827-1834.                                |
| 686 |   |
| 687 | Sato, T., Watanabe, T., and Otsuka, R. (1992) Effects of layer charge, charge location,   |
| 688 | and energy change on expansion properties of dioctahedral smectites. Clays and Clay       |
| 689 | Minerals, 40, 103-113.  |
| 690 |   |
| 691 | Shannon, R.D. (1976) Revised effective ionic radii and systematic studies of              |
| 692 | interatomic distances in halides and chalcogenides. Acta Crystallographica A32, 751-      |
| 693 | 767   |
| 694 |   |
| 695 | Soler I M Artacho E Gale I D García A Junquera I Ordeión P and Sánchez-                   |
| 696 | Portal D (2002) The SIESTA method for ab-initio order-N materials simulation              |
| 607 | Journal of Physics: Condensed Matter 1/ 27/5 2770   |
| 608 | Journal of Thysics. Condensed Matter, $14, 2743-2779$ .                                   |
| 600 | Swedling I. P. Coveney P. V. and Greenwall H. C. (2010) Clay minorals mediate             |
| 700 | Swauning, J. D., Coveney, F. V., and Oreenweit, H. C. (2010) Clay initialian ineutate     |
| 700 | Tolding and regiosefective interactions of KNA. A large-scale atomistic simulation        |
| /01 | study. Journal of the American Chemical Society, 132, 13/50–13/64.                        |
| /02 |   |
| 703 | Troullier, N., and Martins, J.L. (1991) Efficient pseudopotentials for plane-wave         |
| 704 | calculations. Physical Review B, 43, 1993-2006.   |
| 705 |   |
| 706 | Tsipursky, S.I., and Drits, V.A. (1984) The distribution of octahedral cations in the 2:1 |
| 707 | layers of dioctahedral smectites studied by oblique-texture electron diffraction. Clay    |
| 708 | Minerals, 19, 177-193.  |
| 709 |   |
| 710 | Zviagina, B.B., Sakharov, B.A., and Drits, V.A. (2007) X-ray diffraction criteria for the |
| 711 | identification of trans- and cis-vacant varieties of dioctahedral micas. Clays and Clay   |
| 712 | Minerals, 55, 467–480.  |
| 713 | , ,   |
| 714 |   |

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Figure 1.- Crystal structure of cis-vacant (a) and trans-vacant (b) forms of dioctahedral 2:1 phyllosilicates. The unit cell used in the calculations is marked with a square. The octahedral sheet is represented by polyhedra in pink colour, and the H, IC, O and Si atoms are described in black, grey, red, and yellow colours, respectively. The hexagons that are formed by tetrahedral and octahedral cations are marked by dashed and plain lines, respectively. Vertical dashed lines represent the (100) and (200) planes.

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Figure 2.- Cation arrangements for simultaneous monosubstitutions in tetrahedral and octahedral sheet: O1 (a), O2a (b), O2b (c). The H, IC, octahedral substitution, and tetrahedral substituted atoms are represented as balls. The octahedral substitutions are in green colour. The H, IC, O, Al and Si atoms are in black, grey, red, pink, and yellow colours, respectively.

- 730
- Figure 3.- Relationship between ionic potential of IC and averaged  $c\sin\beta$  values for the most stable cation arrangements of samples with substitution of <sup>IV</sup>Al<sup>3+</sup> and Mg<sup>2+</sup> (a), and samples with bisubstitution of Mg<sup>2+</sup> (b).
- 734

Figure 4.- The *ortho* (a), *para* (b), *meta2* (c), and *meta1* (d) cation arrangements of the samples bisubstituted in the octahedral sheet. The H, IC, and octahedral substitution are highlighted as balls. The octahedral substitutions are in blue colour. The H, IC, O, Al and Si atoms are in black, grey, red, pink, and yellow colours, respectively. In part d, the black line represents the [020] plane.

740

Figure 5.- Cation exchange potentials (in eV) at first and second neighbours as a function of the formal charge/ ionic radius (in formal-charge/Å).

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Figure 6.- Powder X-ray diffraction (PXRD) patterns simulated for the fully optimized crystal structures of cv sample **cis13** in the *ortho* (a), *para* (b), and *meta* (c) octahedral cation arrangements.

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Figure 7.- PXRD patterns simulated for *meta* arrangement of cis10 (a) and trans10 (b)forms.

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Figure 8.- PXRD patterns of **cis15** (a) and **trans15** (b) forms of in the most stable cation arrangement.

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756 Table 1.-Chemical composition of the samples studied in the cis-vacant form. Structural formulae on the basis  $O_{20}$  (OH)<sub>4</sub> (T = tetrahedral, Oc = octahedral) 757

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| Sample | ${\rm Si}^{4+}({\rm T})$ | $Al^{3+}(T)$ | $\mathrm{Al}^{3+}(\mathrm{Oc})$ | $Mg^{2+}(Oc)$ | $\mathrm{Fe}^{3+}(\mathrm{Oc})$ | Interlayer cation |
|--------|--------------------------|--------------|---------------------------------|---------------|---------------------------------|-------------------|
| cis1   | 7                        | 1            | 4                               |               |                                 | Na <sup>+</sup>   |
| cis2   | 7                        | 1            | 4                               |               |                                 | $K^+$             |
| cis3   | 8                        |              | 3                               | 1             |                                 | $Na^+$            |
| cis4   | 8                        |              | 3                               | 1             |                                 | $\mathbf{K}^+$    |
| cis5   | 7                        | 1            | 3                               |               | 1                               | $Na^+$            |
| cis6   | 7                        | 1            | 3                               |               | 1                               | $\mathbf{K}^+$    |
| cis7   | 7                        | 1            | 3                               | 1             |                                 | $2Na^+$           |
| cis8   | 7                        | 1            | 3                               | 1             |                                 | $2K^+$            |
| cis9   | 7                        | 1            | 3                               | 1             |                                 | $Ca^{2+}$         |
| cis10  | 8                        |              | 2                               | 2             |                                 | $2Na^+$           |
| cis11  | 8                        |              | 2                               | 2             |                                 | $2K^+$            |
| cis12  | 8                        |              | 2                               | 2             |                                 | $Ca^{2+}$         |
| cis13  | 8                        |              | 2                               | 1             | 1                               | $Na^+$            |
| cis14  | 8                        |              | 2                               | 1             | 1                               | $\mathbf{K}^+$    |
| cis15  | 7                        | 1            | 2                               |               | 2                               | $Na^+$            |
| cis16  | 7                        | 1            | 2                               |               | 2                               | $K^+$             |

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| 762 | Table 2 Relative energy (in eV) and main crystal lattice parameters (distances in Å, |
|-----|--|
| 763 | angles in degrees) of the cation arrangements calculated and experimental values     |
| 764 | (Tsipursky and Drits, 1984) of monosubstituted samples for cv polymorphs.            |

| sample   | $\Delta E^*$ | а    | b    | С         | β     | $c\sin\beta$ | 8           | $\Delta E_{\text{cis-trans}}$ † |
|----------|--------------|------|------|-----------|-------|--------------|-------------|---------------------------------|
| Exp      |              | 5.20 | 9.01 | 10.0-10.2 | 99.5  | 9.85-9.91    | 0.300-0.302 |                                 |
| Cis1     |              | 5.25 | 9.08 | 9.99      | 98.9  | 9.87         | 0.294       | -0.002                          |
| Cis2     |              | 5.26 | 9.11 | 10.10     | 98.7  | 9.98         | 0.290       | -0.008                          |
| Cis3 O1  | 0.0          | 5.26 | 9.15 | 9.86      | 97.1  | 9.78         | 0.232       | 0.025‡                          |
| Cis3 O2a | 0.063        | 5.28 | 9.09 | 9.88      | 99.0  | 9.76         | 0.293       | 0.064§                          |
| Cis3 O2b | 0.042        | 5.27 | 9.11 | 9.92      | 97.7  | 9.83         | 0.252       | 0.075‡                          |
| Cis4 O1  | 0.0          | 5.28 | 9.17 | 9.92      | 98.3  | 9.82         | 0.271       | -0.024‡                         |
| Cis4 O2a | 0.010        | 5.30 | 9.13 | 9.95      | 99.2  | 9.82         | 0.300       | 0.016§                          |
| Cis4 O2b | 0.072        | 5.28 | 9.14 | 10.01     | 97.9  | 9.91         | 0.261       | 0.073‡                          |
| Cis5 O1  | 0.0          | 5.23 | 9.08 | 9.93      | 98.9  | 9.81         | 0.294       | -0.011§#                        |
| Cis5 O2  | 0.010        | 5.23 | 9.08 | 9.95      | 99.5  | 9.82         | 0.314       |                                 |
| Cis6 O1  | 0.0          | 5.25 | 9.11 | 10.06     | 98.8  | 9.94         | 0.293       | -0.015‡                         |
| Cis6 O2  | 0.010        | 5.25 | 9.11 | 10.10     | 99.1  | 9.97         | 0.304       |                                 |
| Cis7 O2b | 0.0          | 5.25 | 9.10 | 10.04     | 97.9  | 9.95         | 0.263       | 0.025#                          |
| Cis7 O2a | 0.272        | 5.27 | 9.09 | 10.00     | 99.0  | 9.88         | 0.297       |                                 |
| cis7 O1  | 0.505        | 5.25 | 9.11 | 10.02     | 99.1  | 9.89         | 0.302       | 0.204‡                          |
| Cis8 O2b | 0.0          | 5.28 | 9.16 | 10.14     | 97.8  | 10.05        | 0.261       | 0.024#                          |
| Cis8 O2a | 0.295        | 5.30 | 9.15 | 10.14     | 99.0  | 10.02        | 0.299       |                                 |
| Cis8 O1  | 0.533        | 5.27 | 9.18 | 10.16     | 98.1  | 10.02        | 0.272       | 0.222‡                          |
| Cis9 O2b | 0.0          | 5.29 | 9.08 | 9.95      | 100.4 | 9.79         | 0.340       | 0.097#                          |
| Cis9 O2a | 0.294        | 5.32 | 9.06 | 9.93      | 101.7 | 9.72         | 0.379       |                                 |
| Cis9 O1  | 0.335        | 5.28 | 9.13 | 9.92      | 100.6 | 9.75         | 0.346       | 0.041‡                          |

<sup>765</sup> 

\* Relative energy of the cation arrangements for each sample (relative energy from the minimum,  $\Delta E =$ 766 0.0 eV). The standard deviations are lower than  $2 \times 10^{-4}$  eV. † Energy difference between the cv and tv polymorphs,  $\Delta E = E_{cis} - E_{trans}$ . The energy values are negative, then negative values of  $\Delta E$  mean that the cv form is more stable than tv. ‡ Forms with similar relative positions of cations. § Energy difference 767 768 taken from average energy values of each polymorph. # Difference between the most stable cation-769 770 arrangement of each polymorph.

**Table 3.-** Relative energy (in eV) and main lattice parameters (distances in Å, angles in
degrees) of the cation arrangements of cv polymorphs calculated for octahedrally
bisubstituted samples (o, m, and p, mean *ortho*, *meta* and *para*, respectively) and
experimental crystallographic values (Tsipursky and Drits 1984).

sample  $\Delta E^*$  $\Delta E_{\text{cis-trans}}$ † а b С  $c \sin\beta$ ε 5.20 Exp 9.01 10.0-10.2 99.5 0.300-0.302 9.85 Cis10m2 5.25 9.11 9.97 99.2 0.304 -0.063<sup>±</sup> 0.0 9.84 9.05 9.98 99.5 Cis10m1 0.045 5.28 9.84 0.312 9.98 Cis10p 0.232 5.27 9.09 98.5 9.87 0.280 0.741 5.27 9.08 9.97 98.2 Cis10o 9.87 0.270 5.28 97.4 0.244 Cis11m2 0.0 9.19 10.01 9.93 -0.033‡ Cis11m1 0.053 5.30 9.12 10.03 99.9 9.88 0.325 Cis11p 0.218 5.29 9.15 10.04 98.6 9.93 0.284 5.29 Cis110 0.779 9.13 10.0 98.2 9.90 0.270 0.0 5.31 9.06 9.91 9.73 0.350 -0.004Cis12m 100.8 5.30 99.5 9.74 Cis12p 0.185 9.10 9.88 0.308 Cis120 0.644 5.29 9.10 9.81 98.0 9.72 0.258 Cis13m 0.0 5.26 9.11 9.86 97.9 9.77 0.233 0.059‡ Cis130 0.146 5.27 9.09 9.87 99.0 9.75 0.293 5.27 9.09 9.85 99.1 Cis13p 0.186 9.73 0.296 5.28 9.92 99.1 Cis14m 0.0 9.14 9.80 0.285 0.032‡ 99.9 Cis14p 5.29 9.13 9.92 9.78 0.176 0.322 Cis14o 0.190 5.28 9.14 9.92 99.9 9.77 0.323 Cis150 0.0 5.23 9.09 9.92 99.4 9.79 0.310 -0.193Cis15p 5.22 9.04 9.91 99.1 9.79 0.300 0.308 0.390 5.23 9.93 99.3 Cis15m 9.05 9.80 0.307 99.4 Cis160 0.0 5.25 9.16 10.00 9.87 0.311 -0.223 0.347 5.25 9.10 10.01 99.2 0.305 Cis16p 9.88 Cis16m 0.438 5.25 9.09 10.00 99.1 9.87 0.301

<sup>777</sup> \* Relative energy of the cation arrangements for each sample (relative energy from the <sup>778</sup> minimum,  $\Delta E = 0.0 \text{ eV}$ ). The standard deviations are lower than  $2 \times 10^{-4} \text{ eV}$ . †Energy <sup>779</sup> difference between the most stable cation arrangements for cv and tv polymorphs,  $\Delta E =$ <sup>780</sup>  $E_{\text{cis}} - E_{\text{trans}}$ . The energy values are negative, then negative values of  $\Delta E$  mean that the cv <sup>781</sup> form is more stable than tv. The errors are lower than  $2 \times 10^{-4} \text{ eV}$ . ‡Difference between <sup>782</sup> polymorphs with similar arrangements of cations.

**Table 4.-** Lattice parameters (distances in Å, angles in degrees) of the tv polymorphs of the monosubstituted samples and relative energy of the cation arrangements calculated

and experimental values (Tsipursky and Drits 1984).

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| sample     | $\Delta E^*$ | а    | b    | С          | β     | $c \sin \beta$ | ε              |
|------------|--------------|------|------|------------|-------|----------------|----------------|
| exp        |              | 5.18 | 9.01 | 10.05-10.2 | 101.4 | 9.8-9.99       | 0.383†, 0.400‡ |
| trans1     |              | 5.26 | 9.00 | 10.05      | 101.9 | 9.83           | 0.394          |
| Trans2     |              | 5.29 | 9.12 | 10.12      | 102.1 | 9.90           | 0.401          |
| Trans3 O2  | 0.0          | 5.27 | 9.12 | 10.07      | 103.0 | 9.81           | 0.430          |
| Trans3 O1  | 0.008        | 5.28 | 9.13 | 10.16      | 105.3 | 9.80           | 0.508          |
| Trans4 O2  | 0.0          | 5.29 | 9.16 | 10.08      | 102.5 | 9.84           | 0.412          |
| Trans4 O1  | 0.026        | 5.30 | 9.16 | 10.06      | 102.3 | 9.83           | 0.404          |
| Trans5 O1  | 0.0          | 5.25 | 9.05 | 10.07      | 102.9 | 9.82           | 0.428          |
| Trans5 O2  | 0.061        | 5.25 | 9.05 | 10.05      | 102.5 | 9.81           | 0.414          |
| Trans6 O1  | 0.0          | 5.27 | 9.07 | 10.19      | 102.8 | 9.94           | 0.428          |
| Trans6 O2  | 0.045        | 5.27 | 9.08 | 10.18      | 102.7 | 9.93           | 0.425          |
| Trans7 O2b | 0.0          | 5.26 | 9.12 | 10.10      | 101.8 | 9.89           | 0.393          |
| Trans7 O1  | 0.325        | 5.27 | 9.13 | 10.11      | 102.0 | 9.89           | 0.399          |
| trans7 O2a | 0.342        | 5.25 | 9.13 | 10.10      | 101.8 | 9.89           | 0.393          |
| Trans8 O2b | 0.0          | 5.29 | 9.17 | 10.23      | 102.1 | 10.00          | 0.405          |
| Trans8 O1  | 0.336        | 5.29 | 9.17 | 10.21      | 102.1 | 9.98           | 0.405          |
| Trans8 O2a | 0.352        | 5.29 | 9.17 | 10.21      | 102.1 | 9.98           | 0.405          |
| Trans9 O2b | 0.0          | 5.29 | 9.10 | 10.02      | 102.6 | 9.78           | 0.413          |
| Trans9 O2  | 0.356        | 5.29 | 9.10 | 10.03      | 102.7 | 9.78           | 0.417          |
| Trans9 O1  | 0.391        | 5.30 | 9.09 | 10.07      | 103.8 | 9.78           | 0.453          |

\* Relative energy of the cation arrangements for each sample (relative energy from the minimum,  $\Delta E = 0.0$  eV). The standard deviations are lower than  $2 \times 10^{-4}$  eV. † Experimental values from McCarty and Reynolds (1995). ‡ From Drits and McCarty (1996).

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Table 5.- Lattice parameters (distances in Å, angles in degrees) and relative energy (eV)
of the cation arrangements calculated for tv samples octahedrally bisubstituted (o, m,
and p, mean *ortho*, *meta* and *para*, respectively) and experimental values (Tsipursky
and Drits 1984).

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| sample   | $\Delta E^*$ | а    | b    | С          | β     | $c \sin \beta$ | 3              |
|----------|--------------|------|------|------------|-------|----------------|----------------|
| exp      |              | 5.18 | 9.01 | 10.05-10.2 | 101.4 | 9.8-9.99       | 0.383†, 0.400‡ |
| Trans10m | 0.0          | 5.26 | 9.10 | 9.99       | 101.6 | 9.79           | 0.382          |
| Trans10p | 0.230        | 5.25 | 9.12 | 10.06      | 101.9 | 9.84           | 0.395          |
| Trans10o | 0.568        | 5.26 | 9.10 | 9.98       | 101.6 | 9.78           | 0.382          |
| Trans11m | 0.0          | 5.28 | 9.15 | 10.07      | 101.8 | 9.86           | 0.390          |
| Trans11p | 0.291        | 5.30 | 9.15 | 10.08      | 101.5 | 9.88           | 0.379          |
| Trans110 | 0.610        | 5.27 | 9.15 | 10.08      | 101.6 | 9.87           | 0.385          |
| Trans12m | 0.0          | 5.29 | 9.11 | 9.95       | 103.1 | 9.69           | 0.426          |
| Trans12p | 0.142        | 5.28 | 9.09 | 10.02      | 104.2 | 9.71           | 0.466          |
| Trans12o | 0.618        | 5.27 | 9.11 | 9.96       | 102.4 | 9.73           | 0.406          |
| Trans13m | 0.0          | 5.26 | 9.08 | 10.01      | 102.6 | 9.77           | 0.415          |
| Trans13p | 0.008        | 5.27 | 9.08 | 10.05      | 103.3 | 9.78           | 0.439          |
| Trans13o | 0.365        | 5.26 | 9.09 | 10.0       | 102.9 | 9.75           | 0.424          |
| Trans14m | 0.0          | 5.29 | 9.14 | 10.05      | 102.7 | 9.80           | 0.418          |
| Trans14p | 0.036        | 5.29 | 9.12 | 10.08      | 103.0 | 9.82           | 0.429          |
| Trans14o | 0.311        | 5.28 | 9.15 | 10.03      | 102.5 | 9.79           | 0.411          |
| Trans150 | 0.0          | 5.25 | 9.01 | 10.06      | 103.5 | 9.78           | 0.447          |
| Trans15p | 0.119        | 5.25 | 9.03 | 10.03      | 102.3 | 9.80           | 0.407          |
| Trans15m | 0.220        | 5.24 | 9.02 | 10.02      | 102.2 | 9.79           | 0.404          |
| Trans160 | 0.0          | 5.27 | 9.08 | 10.11      | 102.6 | 9.87           | 0.418          |
| Trans16p | 0.110        | 5.27 | 9.07 | 10.16      | 102.1 | 9.93           | 0.404          |
| Trans16m | 0.232        | 5.27 | 9.06 | 10.13      | 102.5 | 9.89           | 0.416          |

805 \* Relative energy of the cation arrangements for each sample (relative energy from the 806 minimum,  $\Delta E = 0.0$  eV). The standard deviations are lower than  $2 \times 10^{-4}$  eV. 807 †Experimental values from McCarty and Reynolds (1995). ‡ From Drits and McCarty 808 (1996).

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| 812 | Table 6 Exchange | potentials (eV) | of octahedral | cations for | cv Si <sub>8</sub> Al <sub>2</sub> Mg <sub>2</sub> | samples at |
|-----|------------------|-----------------|---------------|-------------|--|------------|
|-----|------------------|-----------------|---------------|-------------|--|------------|

813 first and second neighbours.

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|     | Sample                             | $J_{\mathrm{AA}}{}^1$ | $J_{\mathrm{AA}}{}^2$ |
|-----|------------------------------------|-----------------------|-----------------------|
|     | <b>Cis10</b> (IC=Na <sup>+</sup> ) | 0.509                 | 0.075                 |
|     | Cis11 $(IC=K^+)$                   | 0.561                 | 0.092                 |
|     | <b>Cis12</b> ( $IC=Ca^{2+}$ )      | 0.459                 | 0.068                 |
| 815 |                                    |                       |                       |



Figures

































