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A time-resolved X-ray diffraction study of Cs exchange into hexagonal H-birnessite

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## ABSTRACT

24 To measure the uptake of radioactive Cs in soils that are rich in Mn oxides, we applied  
25 time-resolved synchrotron X-ray diffraction (TR-XRD), inductively coupled plasma-mass  
26 spectrometry (ICP-MS), and analytical scanning electron microscopy (SEM) to determine the  
27 kinetics and mechanisms of aqueous Cs substitution in the phyllomanganate hexagonal H-  
28 birnessite at pH values ranging from 3 to 10. We observed that the rate of Cs cation exchange  
29 into hexagonal H-birnessite exhibited only a weak dependence on pH, but the total amount of Cs  
30 loading in the interlayer region increased dramatically above pH 6.5. The increase in Cs content  
31 at higher pH may be attributed to the increasingly negative charge on the Mn-O octahedral sheets  
32 and perhaps to a structural change towards triclinic symmetry with high pH. Dissolution at low  
33 pH may have inhibited Cs sequestration. Our work supports delamination-reassembly as a  
34 mechanism of cation exchange.

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## INTRODUCTION

37 Cesium-137 is a byproduct of the plutonium production process, and it is a significant  
38 contaminant during nuclear fallout, nuclear plant meltdown, and nuclear waste storage.  
39 Following the nuclear plant disasters at Chernobyl (Ukraine), and most recently, Fukushima  
40 (Japan),  $^{137}\text{Cs}$  was distributed widely through radioactive plumes that contaminated soils and  
41 surface waters. Moreover,  $^{137}\text{Cs}$  is a major component of the nuclear wastes monitored by the  
42 Department of Energy (DOE) at such sites as Hanford, WA, Savannah River, SC, and Oak  
43 Ridge, TN.

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44 At the Hanford site,  $^{137}\text{Cs}$  is responsible for roughly 40% of the radioactivity of the  
45 nuclear waste (McKinley et al. 2001; Gee et al. 2007). Hanford was a plutonium production  
46 factory from 1943 to 1991, and its high-level nuclear waste is stored in 177 underground single-  
47 and double-shell steel tanks. Approximately 3.8 million L of waste have leaked from the single-  
48 shell tanks, partly because the high alkalinity of the waste (pH 13-14) corroded the steel. The  
49 leaking solutions are concentrated in radioactive  $^{137}\text{Cs}$  ( $2 \times 10^{10}$  Bq/L, equivalent to 0.04  
50 mmol/L), and they have contaminated approximately 28,300  $\text{m}^3$  of soil (Gee et al. 2007).  
51 Although the contaminant solutions leaking from the tanks initially are at pH 14, the pH is  
52 neutralized with increasing distance of transport as the solutions are buffered by soil minerals  
53 (Wan et al. 2004). Consequently, in order to model the migration of Cs-rich fluids, it is  
54 necessary to study Cs uptake by soil minerals over a range of pH.

55 Underlying the tank farm at Hanford is the Ringold Formation, which contains  
56 predominantly sand- and cobble-sized gravel with significant amounts of clay, silt, and sand  
57 (Lindsey and Gaylord 1990). These sediments are glacial-fluvial in origin and are coated in  
58 distinct iron and manganese oxides layers (Barnett et al. 2002; Fredrickson et al. 2004). These  
59 manganese oxides make up 0.4-0.93 wt% of the Ringold Formation (Barnett et al. 2002;  
60 Fredrickson et al. 2004). Despite their minor abundances, these phases play a major role in  
61 controlling heavy metal mobility. As coatings on glacial clasts at Hanford, they occur at the  
62 interface between pore solutions and the primary soil minerals. Moreover, the high cation  
63 exchange, redox, and adsorption capacities of Mn oxides are well documented (Fu et al. 1991;  
64 Violante and Pigna 2002; O'Reilly and Hochella 2003; Weaver and Hochella 2003; Negra et al.  
65 2005; Zhao et al. 2009; Lopano et al. 2007, 2009, 2011). Hydrous manganese oxides with layer  
66 and large-tunnel structures are most frequently observed in these soils, such as the

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67 phyllomanganates birnessite and ranciéite, and the tunneled manganite, todorokite (Taylor et al.  
68 1964; Vaniman et al. 2002; Fredrickson et al. 2004). All of these phases occur as submicron  
69 grains with large surface areas, but birnessite is typically the most reactive (Weaver and  
70 Hochella 2003).

71 In this study, we have investigated the interactions of aqueous Cs with a synthetic  
72 hexagonal H-birnessite over a range of pH. Birnessite structures have been shown to exhibit  
73 either triclinic (Lanson et al. 2002; Post et al. 2002) or hexagonal (Silvester et al. 1997; Post et  
74 al. 2008) symmetry. The structure of hexagonal birnessite differs from that of triclinic birnessite  
75 in the near-absence of Mn<sup>3+</sup> and the presence of Mn vacancies (□) in the octahedral sheet,  
76 resulting in the following chemical formula for H-birnessite proposed by Silvester et al. (1997):  
77  $\text{H}_{0.33}\text{Mn}^{3+}_{0.111}\text{Mn}^{2+}_{0.055}(\text{Mn}^{4+}_{0.722}\text{Mn}^{3+}_{0.111}\square_{0.167})\text{O}_2$ . Subsequently, a similar hexagonal structure  
78 was refined for the natural Ca-rich analog of birnessite called ranciéite (Post et al. 2008). The  
79 charge deficits incurred by the vacancies and Mn<sup>3+</sup> in place of octahedral Mn<sup>4+</sup> result in  
80 negatively charged sheets, which are electrostatically balanced by Mn<sup>2+</sup> and possibly hydronium  
81 or various exchanged cations between the sheets.

82 Dyer et al. (2000) determined distribution coefficients for the exchange of <sup>137</sup>Cs into a  
83 highly crystalline synthetic Na-birnessite, and they report that the uptake decreased as the  
84 solution pH increased from 2 to 10. In contrast, Chitrakar et al. (2011) analyzed the uptake of  
85 Cs<sup>+</sup> by a poorly crystalline synthetic Na-birnessite from pH 2.5 to 10.5, and they observed  
86 increasing Cs<sup>+</sup> sequestration between pH 2.5 and 6.0 and little change between pH 6.0 and 10.5.  
87 Chitrakar et al. attribute the disparity in sequestration behavior to the differences in crystallinity,  
88 but neither paper specifies the symmetry of the birnessite starting material. To the best of our  
89 knowledge, when the symmetry is specified, all prior studies of cation exchange in the

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90 phyllomanganate system have focused on triclinic birnessite (e.g., Golden et al. 1986b; Mikhail  
91 and Misak 1988; Al-Attar et al. 2003; Liu et al. 2007; Lopano et al. 2007; Lopano et al. 2009).  
92 However, many scientists have demonstrated that natural soils contain both triclinic and  
93 hexagonal birnessite (Webb et al. 2005; Post et al. 2008; Tan et al. 2010; Santelli et al. 2011). In  
94 light of the high selectivity that birnessite exhibits for dissolved  $\text{Cs}^+$  (Chitrakar et al. 2011), here  
95 we report the effects of pH on Cs cation exchange into a starting material that we know is  
96 hexagonal H-birnessite.

97

98

## EXPERIMENTAL METHODS

### 99 **Birnessite synthesis**

100 Triclinic Na-birnessite was initially synthesized according to the procedure described in  
101 Golden et al. (1986a). At room temperature, oxygen was bubbled (4.2 L/min) through a mixture  
102 of chilled 250 mL 5.5 M NaOH and 200 mL 0.5 M  $\text{MnCl}_2$  for five hours. The precipitate was  
103 divided evenly among 12 centrifuge tubes and centrifuged. The solution was poured off and  
104 replaced with fresh DI water; after five replicate rinsing cycles, the birnessite was stored in fresh  
105 DI water until needed for experiments. For experiments, aliquots of the stored triclinic Na-  
106 birnessite were filtered through a 0.2  $\mu\text{m}$  hydrophilic polypropylene membrane filter (GH  
107 Polypro, Pall) and allowed to air dry. Dry triclinic Na-birnessite (250 mg) was ground under  
108 acetone in an agate mortar to disaggregate clumps. After the acetone had fully evaporated, the  
109 powder was reacted with 250 mL 0.001 M HCl (pH 3) for three hours. The resultant synthetic  
110 hexagonal H-birnessite was filtered and then rinsed with 300 mL DI water, filtered again through  
111 a 0.2  $\mu\text{m}$  filter, and allowed to air dry. The material was initially characterized with a

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112 conventional sealed Mo tube source on a Rigaku II D/MAX-RAPID microdiffractometer  
113 (Materials Characterization Laboratory, Pennsylvania State University).

114

### 115 **Synchrotron X-ray diffraction of cation exchange**

116 Time-resolved X-ray diffraction (TR-XRD) experiments were completed at beam line 13-  
117 BM-C at the Advanced Photon Source (APS) at Argonne National Laboratory (ANL).  
118 Approximately 4 mg of hexagonal H-birnessite were packed between two cotton plugs in a 0.7  
119 mm quartz capillary and attached to a flow-through apparatus based on the design of Wall et al.  
120 (2011). The five Cs-rich cation exchange solutions had the same initial Cs concentration of  
121 0.001 *M*, and pH ranged from 3 to 10 (pH 3, 5, 6.5, 9, 10). The pH was adjusted with CsOH, and  
122 the Cs concentration was controlled with CsCl. Experiments were not completed at pH 13  
123 because increasing the alkalinity using CsOH required a Cs concentration of 0.1 *M*. The solution  
124 flow rate was 1 drop/min (~ 0.05 mL/min). TR-XRD patterns were collected every 60 seconds  
125 for 5 to 9 hours using a MAR165 CCD detector at a wavelength of 0.8335 Å. The sample to  
126 collector distance was 97.6 mm, yielding a 2θ range of 4-50°. Rietveld refinements (Rietveld  
127 1969) were completed for each TR-XRD pattern using the EXPGUI interface (Toby 2001) of the  
128 general structure analysis system (GSAS) (Larson and Von Dreele 1994). Starting structures  
129 were drawn from the model structure of hexagonal H-birnessite proposed by Lanson et al. (2000)  
130 with atom positions determined by Heaney et al. (2003). The background intensities for the TR-  
131 XRD patterns were fit using up to 15 terms of a linear interpolation function. The peak profiles  
132 were modeled by a pseudo-Voigt profile function as parameterized by Thompson et al. (1987),  
133 with asymmetry correction by Finger et al. (1994), and microstrain anisotropic broadening terms  
134 of Stephens (1999).

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135 During initial cycles of refinement only the background, scale, peak profile, and unit-cell  
136 parameters were allowed to vary. The position of the O atom in the Mn-O sheet was then  
137 refined. Following refinements of the interlayer atom positions, occupancy factors and isotropic  
138 atomic displacement factors for the interlayer sites were allowed to vary. Once the interlayer  
139 atoms were settled, the isotropic thermal parameters for the Mn and O in the octahedral sheets  
140 were refined, followed alternately with those for the interlayer atoms. The final  $\chi^2$  values for  
141 end-member hexagonal Cs-birnessite ranged from 2.76-4.82 (Table 1). As is often the case, the  
142 standard deviations calculated by GSAS for the lattice parameters are lower than the true errors,  
143 which are revealed by the scatter in the refined values as a function of temperature (Post and  
144 Bish 1989). The errors calculated by GSAS are presented in the tables and figures of this paper  
145 with the understanding that the actual errors may be more than an order of magnitude higher than  
146 the calculated deviations.

147

148 **Chemical analysis of eluate**

149 The eluate was collected as a function of time; a stepping motor controlled a UR-150  
150 Newport Rotary Stage with an Al tray capable of supporting 15 wide-mouth 15 mL  
151 polypropylene vials. The stepping motor was programmed to rotate to the next vial every 20  
152 min. The eluate was analyzed with an X-Series 2 Thermo Scientific quadrupole inductively  
153 coupled plasma-mass spectrometer (ICP-MS) in conjunction with Thermo Scientific PlasmaLab  
154 software (Materials Characterization Laboratory, Pennsylvania State University) to determine the  
155 change in Cs and Mn elemental concentrations.

156 An FEI Nova NanoSEM 600 analytical scanning electron microscope (ASEM) equipped  
157 with Thermo Fisher Scientific NSS 2.3.89 software (Mineral Sciences Analytical Laboratories,

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158 Smithsonian Institution) was used to determine the distribution of Cs across partially exchanged  
159 hexagonal H-birnessite grains. These partially exchanged products were obtained by flowing  
160 0.001 M CsCl solutions through hexagonal H-birnessite powders in capillaries for 40 min at pH  
161 9. The birnessite was unpacked from the glass capillary, rinsed with 300 mL DI water, and  
162 allowed to air dry at room temperature. Dry samples were mounted on SEM stubs with carbon  
163 tape for elemental mapping analysis.

164

### 165 **Kinetic analysis**

166 We applied the approach of Lopano et al. (2011) to determine the kinetics of cation  
167 substitution into the hexagonal H-birnessite structure. This method assumes that cation  
168 exchange in this system obeys Vegard's Law, which posits that the volume of the unit cell varies  
169 linearly with the extent of cation exchange (Denton and Ashcroft 1991). As suggested in Lopano  
170 et al. (2009), this presumption is reasonable, since the large size of Cs<sup>+</sup> will expand the interlayer  
171 of birnessite-like phases. However, the application of Vegard's Law to birnessite is complicated  
172 by the appearance of an intermediate product, in which Cs has fully exchanged for the interlayer  
173 cation but is positionally disordered within the interlayer. The authors treated this issue by  
174 including the disordered state as a distinct phase that contributed to the overall unit-cell volume.  
175 Following Lopano et al. (2011), we propose that the measured volume of the unit cell ( $V_{tot}$ ) at  
176 any point during the exchange of Cs into hexagonal H-birnessite can be represented by a  
177 summation of the three individual phase fractions ( $X_x$ ), each multiplied by their respective unit-  
178 cell volumes,  $q$ ,  $r$ , and  $s$ :

$$179 \quad V_{tot} = qX_A + rX_B + sX_C \quad (1)$$



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180 where  $X_A$  is the phase fraction of initial hexagonal H-birnessite,  $X_B$  is the phase fraction of  
181 disordered hexagonal Cs-birnessite, and  $X_C$  is the phase fraction of ordered hexagonal Cs-  
182 birnessite.

183 As shown in Lopano et al. (2011), the kinetics of  $\text{Cs}^+$  exchange into triclinic Na-  
184 birnessite by extension can be modeled as a two-stage linear reaction. The first stage involves  
185 the complete exchange of cations, and in the second stage cations reorder within the interlayer to  
186 more thermodynamically stable positions (Fig. 1). The rate constant of each reaction stage ( $k_1$   
187 and  $k_2$ , respectively, with units  $\text{min}^{-1}$ ) was determined according to standard kinetic equations for  
188 a first-order compound reaction (Fromherz 1964):



190 
$$X_A = X_A^0 e^{-k_1 t} \quad (3)$$

191 
$$X_B = \frac{X_A^0 k_1}{k_2 - k_1} (e^{-k_1 t} - e^{-k_2 t}) \quad (4)$$

192 
$$X_C = X_A^0 \left\{ 1 - \frac{k_1 k_2}{k_2 - k_1} \left( \frac{e^{-k_1 t}}{k_1} - \frac{e^{-k_2 t}}{k_2} \right) \right\} \quad (5)$$

193 where  $t$  is time and  $X_A^0$  is the initial phase fraction of starting material, A. According to mass  
194 balance:

195 
$$X_{tot} = X_A^0 = X_A + X_B + X_C = 1 \quad (6)$$

196 or

197 
$$X_A^0 = 1 \cdot \quad (7)$$

198 Eqns. 3-7 were substituted into Vegard's Law (Eqn. 1):

199 
$$V_{tot} = q e^{-k_1 t} + \frac{r k_1}{k_2 - k_1} (e^{-k_1 t} - e^{-k_2 t}) + s \left\{ 1 - \frac{k_1 k_2}{k_2 - k_1} \left( \frac{e^{-k_1 t}}{k_1} - \frac{e^{-k_2 t}}{k_2} \right) \right\} \quad (8)$$

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200 The dependence of volume versus time for each pH was fit with Eqn. 8 using Origin 6.1, solving  
201 for  $q$ ,  $r$ ,  $s$ ,  $k_1$ , and  $k_2$ . These five variables were allowed to iterate simultaneously using the  
202 Levenberg-Marquardt algorithm until the reduced  $\chi^2$  was minimized. For this study, we were  
203 most interested in the initial exchange of cations when  $X_A = 1$  and  $t = 0$ , and not the reordering of  
204 cations; therefore, the initial rate of the cation exchange was determined using the first-stage rate  
205 constant ( $k_1$ ) and phase fractions  $X_A$  and  $X_B$ . The initial rate in terms of  $X_A$ ,  $X_B$ , and  $k_1$  can be  
206 defined with standard first-order reversible kinetics as (Lasaga 1981)

$$207 \quad \frac{dX_A}{dt} = -k_1 X_A^n \quad (9)$$

$$208 \quad \frac{dX_B}{dt} = k_1 X_A^n \quad (10)$$

209 where  $n$  is the reaction order. Taking the derivative of Vegard's Law (Eqn. 1) with respect to  
210 time,

$$211 \quad \frac{dV}{dt} = q \frac{dX_A}{dt} + r \frac{dX_B}{dt}, \quad (11)$$

212 and substituting Eqn. 9 and 10 into Eqn. 11, the initial rate  $dV/dt$  in  $\text{\AA}^3/\text{min}$  is

$$213 \quad \lim_{t \rightarrow 0, X_A \rightarrow 1} \left( \frac{dV}{dt} \right) = -k_1 q + k_1 r \quad (12)$$

214 or

$$215 \quad \frac{dV}{dt} = k_1 (r - q) \quad (13)$$

216 When we plotted the log of the initial rate as a function of pH, we could calculate a linear  
217 regression for which the negative slope was the reaction order,  $n$ , and the y-intercept was the log  
218 of the initial rate constant,  $w$ , with units  $\text{\AA}^3/(\text{min} \cdot \text{mol})$ :

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219 
$$\log\left(\frac{dV}{dt}\right) = -n(\text{pH}) + \log w \quad (14)$$

220 which simplifies to

221 
$$\frac{dV}{dt} = w[H^+]^n \quad (15)$$

222 Thus, Eqn. 15 allows us to determine the effect of solution pH on the rate of Cs cation exchange  
223 as measured from volume changes of the hexagonal birnessite unit cell.

224

## 225 RESULTS

226 The substitution of Cs<sup>+</sup> into hexagonal H-birnessite is evident from X-ray diffraction  
227 patterns through a marked decrease in the ratio of the 001 to 002 diffraction peaks (Fig. 2). Cs  
228 has a considerably larger scattering factor than the exchangeable proton/water complex in the  
229 interlayer of hexagonal H-birnessite, causing a reduction in the peak intensity ratio between the  
230 (001) and (002) peaks from roughly 4:1 to 2:1 (Lopano et al. 2009). Rietveld refinement results  
231 for the exchange of Cs into hexagonal H-birnessite at pH 3, 5, 6.5, 9, and 10 are compiled in  
232 Table 1. Atom positions are listed in Table 2, and selected bond distances are listed in Table 3.  
233 A typical Rietveld refinement is shown in Figure 3 for Cs exchange into hexagonal H-birnessite.

234 All unit-cell parameters increased with extent of reaction, resulting in an increase of unit-  
235 cell volume with time. In order to determine the rate constant associated with the first stage of  
236 exchange ( $k_1$ ), we fit the unit-cell volume as a function of time using Eqn. 8 (Fig. 4). To  
237 determine the initial rate of cation exchange for a given pH, we applied Eqn. 13, and the results  
238 of this analysis are presented in Table 4.

239 The dependence of the initial reaction rate on pH (Eqn. 14, Fig. 5) refined as

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240 
$$\log\left(\frac{dV}{dt}\right) = -0.0791(pH) - 0.9885 \quad R^2 = 0.894, \quad (16)$$

241 which can be simplified to an exponential form where the initial rate constant,  $w$ , is the  
242 coefficient and the reaction order,  $n$ , is the exponent:

243 
$$\frac{dV}{dt} = 0.103[H^+]^{0.079} \quad (17)$$

244 As can be seen in Figure 5, the exchange rate of  $Cs^+$  into the interlayer of hexagonal H-birnessite  
245 decreased only slightly as the pH increased. By extension, the reaction order of the cation  
246 exchange was also extremely small (0.079), indicating a weak dependence of exchange rate on  
247 pH.

248 The change in final unit-cell volume increased as pH increased (Fig. 6), particularly as  
249 pH exceeded 6. To the extent that unit-cell volume is a proxy for  $Cs^+$  exchange, we can infer  
250 that more  $Cs^+$  is exchanged into the interlayer of hexagonal H-birnessite with increasing  
251 alkalinity, consistent with the results of Chitrakar et al. (2011). The occupancy factor of the  
252 interlayer cation also increased as pH increased from 3 to 10, which is direct evidence that more  
253 Cs exchanged into the interlayer (Table 2). We tested this conclusion by ICP-MS analysis of Cs  
254 and Mn in the eluate, which was collected as a function of time after it interacted with the  
255 hexagonal H-birnessite. When pH was 6.5 or higher, all of the Cs was sequestered by the  
256 birnessite powder in the first reaction stages. In Figure 7, we present the percentage of Cs  
257 removed from or released to the flow-through solution as a function of time. Positive data points  
258 indicate sequestration by the solid, whereas negative data points represent release of Cs by the  
259 solid. For example, if an eluted aliquot collected at a given time was measured as 0.5 mM Cs,  
260 then that represents +50 wt% sequestration (removal of Cs from the solution), since the flow-  
261 through solution enters the capillary with a concentration of 1.0 mM Cs. As can be seen in this

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262 figure, a maximum of only 25 wt% of the Cs in the influent was adsorbed within the first 20  
263 minutes at pH 3, whereas 100 wt% of the Cs was sequestered by the birnessite over the first 100  
264 min at pH 10. For all pH values, the sequestration of Cs eventually was followed by the release  
265 of Cs to the solution.

266

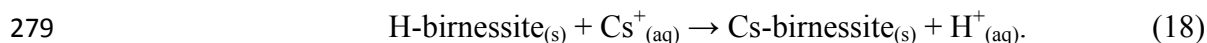
267

## DISCUSSION

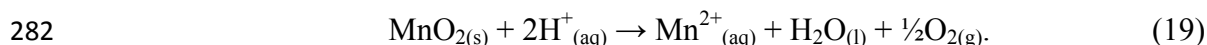
### 268 Controls of Cs uptake

269 We postulate that the rate and amount of Cs<sup>+</sup> uptake as a function of pH are controlled by  
270 two factors: 1) the charge on the octahedral sheets; and 2) the presence of competing cations  
271 (including H<sup>+</sup>) in solution. The point-of-zero charge (PZC) of birnessite is approximately 3.0  
272 (Tan et al. 2008), and the octahedral MnO<sub>6</sub> sheets thus become more negatively charged as pH  
273 increases beyond 3 (Murray 1974; McKenzie 1981). In order to maintain neutrality of the  
274 surface charge at high pH, more Cs must adsorb to surface sites. Thus, the change in surface  
275 charge as a function of pH may explain the increased uptake of Cs in more alkaline solutions.

276 Secondly, Cs exchange at low pH is not chemically favorable because, by Le Châtelier's  
277 principle, the excess number of protons in the starting solution drives the reaction in the reverse  
278 direction and prevents Cs cation exchange:



280 Finally, acidic dissolution occurs at a pH as low as 3 (Murray 1974; Eary and Ral 1987),  
281 and that may inhibit Cs from entering the interlayer due to Mn<sup>2+</sup><sub>(aq)</sub> production, where



283 Measurements of the dissolved Mn in the leachate solutions from our experiments suggest that  
284 some dissolution did occur in the earliest stages of reaction (Fig. 8). At each pH, a small amount

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285 of Mn desorbed or dissolved from the hexagonal H-birnessite, with the greatest measured value  
286 (5 ppm after 20 min) occurring at pH 6.5. At pH 3 (Fig. 8A), the initial release of Mn reached  
287 only 1 ppm, but unlike reactions at higher pH, the concentration of Mn in the leachate achieved a  
288 non-zero steady state concentration of approximately 200 ppb for the remainder of the reaction,  
289 indicating a constant loss of  $\text{Mn}^{2+}$  from the solid. This observation supports our inference that  
290 reductive dissolution of hexagonal H-birnessite occurs at low pH as Cs is exchanged into the  
291 interlayer, or perhaps a small amount of interlayer  $\text{Mn}^{2+}$  is forced into solution due to the large  
292 size of the incoming  $\text{Cs}^+$ .

293

#### 294 **Transformation from hexagonal to triclinic symmetry**

295 Although we successfully refined all of the exchanged Cs-birnessite structures within the  
296 hexagonal  $P-3$  space group, we nevertheless speculate that the higher loading of Cs within  
297 birnessite at higher pH was promoted by a transformation towards triclinic symmetry. At pH 9  
298 and 10, the occupancy of octahedral Mn increased from approximately 0.7 to 1.0 (Fig. 9),  
299 indicating that the concentration of octahedral vacancies dropped to zero with higher pH. As  
300 described in Silvester et al. (1997) and Post et al. (2008), vacancies in the octahedral sheet are a  
301 defining feature of hexagonal birnessite, whereas the absence of these vacancies is more  
302 representative of triclinic birnessite (Post et al. 2002). At the same time, there is a slight  
303 decrease in interlayer  $\text{Mn}^{2+}$  site occupancy from 0.17 to 0. It is possible that interlayer Mn is  
304 migrating from the interlayer into the octahedral sheet and it may be that Cs exchange into the  
305 interlayer promotes the transfer of Mn into the octahedral sheet due to the size and charge of Cs,  
306 which leads to the expansion of the interlayer.

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307 Another indication that a symmetry transition was initiated at higher pH can be seen in  
308 the sharp increase in the change of unit-cell volume above pH 6 (Fig. 6). The unit-cell volume of  
309 triclinic M-birnessite is greater than that of hexagonal M-birnessite, and thus a hexagonal-  
310 triclinic structure transition would be accompanied by a step increase in unit-cell volume.  
311 Indeed, when the unit-cell volume behaviors are considered for each pH (Fig. 4), the low pH  
312 reactions exhibited a different character than those at high pH. For pH 6.5 and lower, one can  
313 clearly detect the two stages of reaction as modeled by Lopano et al. (2009) as two distinct  
314 regions with different slopes for  $dV/dt$ . Like Lopano et al. (2009), we interpret the abrupt  
315 increase in unit-cell volume in the first stage as representing the full exchange of  $\text{Cs}^+$  for  $\text{H}^+$ ; the  
316 comparatively lengthy second stage of minor volume increase reflects a positional ordering of  
317  $\text{Cs}^+$  within the interlayer. At pH 9 and 10, however, the dependence of the volume change is less  
318 easily demarcated into two regimes, perhaps because the exchange of  $\text{Cs}^+$  continued long after  
319 the time that exchange had ceased in the experiments at low pH. Our analyses of the eluate  
320 strongly support this conclusion (Fig. 7). Consequently, the two-stages observed at low pH were  
321 blurred at high pH by the expansion of the interlayer and increased  $\text{Cs}^+$  uptake. We attempted to  
322 refine the higher pH powders with a triclinic structure but the goodness of fit parameters became  
323 much worse than with a hexagonal structure.

324

### 325 **Back reaction**

326 The release of Cs following its uptake was observed at each pH, and that phenomenon  
327 requires some explanation. If Cs leached out of the interlayer, we would expect to see the unit-  
328 cell volume decrease towards the initial volume of hexagonal H-birnessite. However, in all  
329 instances the unit-cell volume remained constant once cation exchange was complete, indicating

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330 that Cs remained in the interlayer. Rather, we speculate that Cs was released from edge or  
331 surface sites on the birnessite platelets, or as a result of the reordering of interlayer cations during  
332 stage two of the reaction. We recognize that some percentage of Cs is adsorbed rather than  
333 exchanged; indeed, studies such as that by Peacock and Sherman (2007) have demonstrated that  
334 the sorption of dissolved  $\text{Ni}^{2+}$  on the birnessite surface increases markedly from pH 1 to 7.  
335 However, our XRD data did not allow us to distinguish between exchanged and sorbed  
336 populations of Cs.

337

### 338 **Mechanism of exchange**

339 Cation exchange in layered structures conventionally has been explained through simple  
340 diffusion of solvated ions into the solid accompanied by counter-diffusion of cations from the  
341 solid to the solution (Helffferich 1962). If this mechanism is operative when  $\text{Cs}^+$  exchanges into  
342 hexagonal H-birnessite, then a Cs-rich reaction rim would form around the edges of each  
343 partially-exchanged birnessite grain as the Cs migrated from the edges of the grain towards the  
344 core until exchange was complete. Alternatively, Putnis (2002) has demonstrated that cation  
345 exchange commonly involves dissolution of the starting structure followed by reprecipitation of  
346 the final structure. This model also may create reaction rims, if the reprecipitation is  
347 pseudomorphic (Labotka et al. 2004), or it may be marked by the transient co-existence of  
348 endmember phases. In the present experiment, this mechanism would generate the growth of  
349 hexagonal Cs-birnessite particles at the expense of hexagonal H-birnessite.

350 The octahedral sheets in birnessite have the capacity to separate into monolayers when  
351 intercalated with organic ions and washed, and the monolayers then reconstruct as stacked  
352 crystals upon drying (Liu et al. 2000; Yang et al. 2004). By extension, Lopano et al. (2009)



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353 proposed a “delamination-reassembly” mechanism for the substitution of Cs into triclinic Na-  
354 birnessite, and this exchange model represents a hybrid between simple diffusion and  
355 dissolution-precipitation. If this model is applied to the present system, adjacent octahedral  
356 sheets delaminated, allowing Cs cations to exchange with all of the protons within a single  
357 interlayer. Cation exchange then proceeded through a layer-by-layer substitution until all  
358 protons swapped out for Cs.

359 If this mechanism occurred during our experiments, then elemental maps of individual  
360 platelets of partially exchanged H-birnessite crystals would not exhibit a reaction rim. Instead,  
361 they would display a homogeneous distribution of Cs across a given grain. As can be seen in our  
362 ASEM elemental maps of partially exchanged hexagonal H-birnessite at pH 9 (Fig. 10), no Cs-  
363 rich reaction rims enveloped individual grains of birnessite. Consequently, we rule out diffusion  
364 as the exchange mechanism. Likewise, we do not believe that dissolution-precipitation was the  
365 exchange mechanism because there were no Cs-rich grains interspersed with Cs-depleted grains.  
366 Rather, the homogeneous distribution of Cs supports delamination-reassembly as the driving  
367 mechanism for exchange.

368

369

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375

Revision 2.

## REFERENCES

- 376
- 377 Al-Attar, L., Dyer, A., Paajanen, A., and Harjula, R. (2003) Purification of nuclear wastes by  
378 novel inorganic ion exchangers. *Journal of Materials Chemistry*, 13(12), 2969-2974.
- 379 Barnett, M.O., Jardine, P.M., and Brooks, S.C. (2002) U(VI) adsorption to heterogeneous  
380 subsurface media: Application of a surface complexation model. *Environmental Science*  
381 *& Technology*, 36(5), 937-942.
- 382 Chitrakar, R., Makita, Y., and Sonoda, A. (2011) Cesium ion exchange on synthetic birnessite  
383 ( $\text{Na}_{0.35}\text{MnO}_2 \cdot 0.6\text{H}_2\text{O}$ ). *Chemistry Letters*, 40, 1118-1120.
- 384 Denton, A.R., and Ashcroft, N.W. (1991) Vegard's law. *Physical Review A*, 43(6), 3161.
- 385 Dyer, A., Pillinger, M., Harjula, R., and Amin, S. (2000) Sorption characteristics of  
386 radionuclides on synthetic birnessite-type layered manganese oxides. *Journal of Materials*  
387 *Chemistry*, 10(8), 1867-1874.
- 388 Eary, L.E., and Ral, D. (1987) Kinetics of chromium (III) oxidation to chromium (VI) by  
389 reaction with manganese dioxide. *Environmental Science & Technology*, 21, 1187-1193.
- 390 Finger, L.W., Cox, D.E., and Jephcoat, A.P. (1994) A Correction for Powder Diffraction Peak  
391 Asymmetry Due to Axial Divergence. *Journal of Applied Crystallography*, 27, 892-900.
- 392 Fredrickson, J.K., Zachara, J.M., Kennedy, D.W., Kukkadapu, R.K., McKinley, J.P., Heald,  
393 S.M., Liu, C., and Plymale, A.E. (2004) Reduction of  $\text{TcO}_4^-$  by sediment-associated  
394 biogenic Fe(II). *Geochimica et Cosmochimica Acta*, 68(15), 3171-3187.
- 395 Fromherz, H. (1964) *Physico-chemical calculations in science and industry*. Butterworth & Co.,  
396 London.
- 397 Fu, G., Allen, H.E., and Cowan, C.E. (1991) Adsorption of cadmium and copper by manganese  
398 oxide. *Soil Science*, 152(2), 72-81.

Revision 2.

- 399 Gee, G.W., Oostrom, M., Freshley, M.D., Rockhold, M.L., and Zachara, J.M. (2007) Hanford  
400 site vadose zone studies: An overview. *Vadose Zone Journal*, 6(4), 899-905.
- 401 Golden, D.C., Chen, C.C., and Dixon, J.B. (1986a) Synthesis of Todorokite. *Science*, 231(4739),  
402 717-719.
- 403 Golden, D.C., Dixon, J.B., and Chen, C.C. (1986b) Ion exchange, thermal transformations, and  
404 oxidizing properties of birnessite. *Clays and Clay Minerals*, 34(5), 511-520.
- 405 Heaney, P.J., Post, J.E., Lopano, C.L., and Hanson, J.C. (2003) Hydrogen exchange in Na-  
406 birnessite: A time-resolved synchrotron X-ray diffraction analysis. *Geological Society of*  
407 *America Abstracts with Programs*, 35, 620.
- 408 Helfferich, F. (1962) *Ion Exchange*. 624 p. McGraw-Hill, New York.
- 409 Labotka, T.C., Cole, D.R., Fayek, M., Riciputi, L.R., and Stadermann, F.J. (2004) Coupled  
410 cation and oxygen-isotope exchange between alkali feldspar and aqueous chloride  
411 solution. *American Mineralogist*, 89(11-12), 1822-1825.
- 412 Lanson, B., Drits, V.A., Feng, Q., and Manceau, A. (2002) Structure of synthetic Na-birnessite:  
413 Evidence for a triclinic one-layer unit cell. *American Mineralogist*, 87(11-12), 1662-  
414 1671.
- 415 Lanson, B., Drits, V.A., Silvester, E., and Manceau, A. (2000) Structure of H-exchanged  
416 hexagonal birnessite and its mechanism of formation from Na-rich monoclinic busserite at  
417 low pH. *American Mineralogist*, 85(5-6), 826-838.
- 418 Larson, A.C., and Von Dreele, R.B., 1994. GSAS-General Structure Analysis System. Los  
419 Alamos National Laboratory,

Revision 2.

- 420 Lasaga, A.C. (1981) Rate Laws of Chemical Reactions. In A.C. Lasaga, and R.J. Kirkpatrick,  
421 Eds. Kinetics of Geochemical Processes, 8, p. 1-68. Mineralogical Society of America,  
422 Chelsea, MI.
- 423 Lindsey, K.A., and Gaylord, D.R. (1990) Lithofacies and sedimentology of the Miocene-  
424 Pliocene Ringold Formation, Hanford Site, South-Central Washington. Northwest  
425 Science, 64(3), 165-180.
- 426 Liu, Z., Ooi, K., Kanoh, H., Tang, W., and Tomida, T. (2000) Swelling and delamination  
427 behaviors of birnessite-type manganese oxide by intercalation of tetraalkylammonium  
428 ions. Langmuir, 16(9), 4154-4164.
- 429 Liu, Z.H., Kang, L.P., Zhao, M.Z., and Ooi, K. (2007) Preparation, ion-exchange, and  
430 electrochemical behavior of Cs-type manganese oxides with a novel hexagonal-like  
431 morphology. Journal of Materials Research, 22(9), 2437-2447.
- 432 Lopano, C.L., Heaney, P.J., Bandstra, J.Z., Post, J.E., and Brantley, S.L. (2011) Kinetic analysis  
433 of cation exchange in birnessite using time-resolved synchrotron X-ray diffraction.  
434 Geochimica Et Cosmochimica Acta, 75(14), 3973-3981.
- 435 Lopano, C.L., Heaney, P.J., and Post, J.E. (2009) Cs-exchange in birnessite: Reaction  
436 mechanisms inferred from time-resolved X-ray diffraction and transmission electron  
437 microscopy. American Mineralogist, 94(5-6), 816-826.
- 438 Lopano, C.L., Heaney, P.J., Post, J.E., Hanson, J., and Komarneni, S. (2007) Time-resolved  
439 structural analysis of K- and Ba-exchange reactions with synthetic Na-birnessite using  
440 synchrotron X-ray diffraction. American Mineralogist, 92(2-3), 380-387.
- 441 McKenzie, R.M. (1981) The surface charge on manganese dioxides. Australian Journal of Soil  
442 Research, 19, 41-50.

Revision 2.

- 443 McKinley, J.P., Zeissler, C.J., Zachara, J.M., Serne, R.J., Lindstrom, R.M., Schaefer, H.T., and  
444 Orr, R.D. (2001) Distribution and retention of Cs-137 in sediments at the Hanford Site,  
445 Washington. *Environmental Science & Technology*, 35(17), 3433-3441.
- 446 Mikhail, E.M., and Misak, N.Z. (1988) Sorption of Cesium and Cobalt Radionuclides on a New  
447 Manganese Oxide. *Applied Radiation and Isotopes*, 39(11), 1121-1124.
- 448 Murray, J.W. (1974) The surface chemistry of hydrous manganese dioxide. *Journal of Colloid  
449 and Interface Science*, 46(3), 357-371.
- 450 Negra, C., Ross, D.S., and Lanzirotti, A. (2005) Soil manganese oxides and trace metals:  
451 Competitive sorption and microfocused synchrotron X-ray fluorescence mapping. *Soil  
452 Science Society of America Journal*, 69(2), 353-361.
- 453 O'Reilly, S.E., and Hochella, M.F. (2003) Lead sorption efficiencies of natural and synthetic Mn  
454 and Fe-oxides. *Geochimica Et Cosmochimica Acta*, 67(23), 4471-4487.
- 455 Peacock, C.L. and Sherman, D.M. (2007) Sorption of Ni by birnessite: Equilibrium controls on  
456 Ni in seawater. *Chemical Geology*, 238, 94-106.
- 457 Post, J.E. and Bish, D.L. (1989) Rietveld refinement of crystal structures using powder X-ray  
458 diffraction data. *Reviews in Mineralogy*, 20, 277-308.
- 459 Post, J.E., Heaney, P.J., and Ertl, A. (2008) Rietveld refinement of the rancieite structure using  
460 synchrotron powder diffraction data. *Powder Diffraction*, 23(1), 10-14.
- 461 Post, J.E., Heaney, P.J., and Hanson, J. (2002) Rietveld refinement of a triclinic structure for  
462 synthetic Na-birnessite using synchrotron powder diffraction data. *Powder Diffraction*,  
463 17(3), 218-221.
- 464 Putnis, A. (2002) Mineral replacement reactions: from macroscopic observations to microscopic  
465 mechanisms. *Mineralogical Magazine*, 66(5), 689-708.

Revision 2.

- 466 Rietveld, H.M. (1969) A Profile Refinement Method for Nuclear and Magnetic Structures.  
467 Journal of Applied Crystallography, 2, 65-71.
- 468 Santelli, C.M., Webb, S.M., Dohnalkova, A.C., and Hansel, C.M. (2011) Diversity of Mn oxides  
469 produced by Mn(II)-oxidizing fungi. Geochimica Et Cosmochimica Acta, 75(10), 2762-  
470 2776.
- 471 Silvester, E., Manceau, A., and Drits, V.A. (1997) Structure of synthetic monoclinic Na-rich  
472 birnessite and hexagonal birnessite. 2. Results from chemical studies and EXAFS  
473 spectroscopy. American Mineralogist, 82(9-10), 962-978.
- 474 Stephens, P.W. (1999) Phenomenological model of anisotropic peak broadening in powder  
475 diffraction. Journal of Applied Crystallography, 32, 281-289.
- 476 Tan, H., Zhang, G.X., Heaney, P.J., Webb, S.M., and Burgos, W.D. (2010) Characterization of  
477 manganese oxide precipitates from Appalachian coal mine drainage treatment systems.  
478 Applied Geochemistry, 25(3), 389-399.
- 479 Tan, W.F., Lu, S.J., Liu, F., Feng, X.H., He, J.Z., and Koopall, L.K. (2008) Determination of the  
480 point-of-zero, charge of manganese oxides with different methods including an improved  
481 salt titration method. Soil Science, 173(4), 277-286.
- 482 Taylor, R.M., McKenzie, R.M., and Norrish, K. (1964) The mineralogy and chemistry of  
483 manganese in some Australian soils. Australian Journal of Soil Research, 2, 235-248.
- 484 Thompson, P., Cox, D.E., and Hastings, J.B. (1987) Rietveld Refinement of Debye-Scherrer  
485 Synchrotron X-Ray Data from Al<sub>2</sub>O<sub>3</sub>. Journal of Applied Crystallography, 20, 79-83.
- 486 Toby, B.H. (2001) EXPGUI, a graphical user interface for GSAS. Journal of Applied  
487 Crystallography, 34, 210-213.

Revision 2.

- 488 Vaniman, D.T., Chipera, S.J., Bish, D.L., Duff, M.C., and Hunter, D.B. (2002) Crystal chemistry  
489 of clay-Mn oxide associations in soils, fractures, and matrix of the Bandelier Tuff,  
490 Pajarito Mesa, New Mexico. *Geochimica Et Cosmochimica Acta*, 66(8), 1349-1374.
- 491 Violante, A., and Pigna, M. (2002) Competitive sorption of arsenate and phosphate on different  
492 clay minerals and soils. *Soil Science Society of America Journal*, 66(6), 1788-1796.
- 493 Wall, A.J., Heaney, P.J., Mathur, R., Post, J.E., Hanson, J.C., and Eng, P.J. (2011) A flow-  
494 through reaction cell that couples time-resolved X-ray diffraction with stable isotope  
495 analysis. *Journal of Applied Crystallography*, 44, 429-432.
- 496 Wan, J.M., Larsen, J.T., Tokunaga, T.K., and Zheng, Z.P. (2004) pH neutralization and zonation  
497 in alkaline-saline tank waste plumes. *Environmental Science & Technology*, 38(5), 1321-  
498 1329.
- 499 Weaver, R.M., and Hochella, M.F. (2003) The reactivity of seven Mn-oxides with Cr-aq(3+): A  
500 comparative analysis of a complex, aq environmentally important redox reaction.  
501 *American Mineralogist*, 88(11-12), 2016-2027.
- 502 Webb, S.M., Tebo, B.M., and Bargar, J.R. (2005) Structural characterization of biogenic Mn  
503 oxides produced in seawater by the marine bacillus sp strain SG-1. *American*  
504 *Mineralogist*, 90(8-9), 1342-1357.
- 505 Yang, X.J., Makita, Y., Liu, Z.H., Sakane, K., and Ooi, K. (2004) Structural characterization of  
506 self-assembled MnO<sub>2</sub> nanosheets from birnessite manganese oxide single crystals.  
507 *Chemistry of Materials*, 16(26), 5581-5588.
- 508 Zhao, W., Feng, X., Tan, W., Liu, F., and Ding, S. (2009) Relation of lead adsorption on  
509 birnessites with different average oxidation states of manganese and release of  
510 Mn<sup>2+</sup>/H<sup>+</sup>/K<sup>+</sup>. *Journal of Environmental Sciences*, 21, 520-526.

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## FIGURE CAPTIONS

512

513

514 Figure 1. A schematic of the two stage cation exchange reaction: stage one is the complete  
515 exchange of cations while stage two is the reordering of cations within the interlayer. The  
516 structures represent projections along the  $a$ -axis. Atomic color assignments: O (yellow),  $\text{Mn}^{4+}$   
517 ( $\text{Mn}^{2+}$  (pink, interlayer),  $\text{H}_3\text{O}^+$  (green), and Cs/ $\text{H}_2\text{O}$  (blue).

518

519 Figure 2. Stacked TR-XRD patterns of hexagonal H-birnessite exchanged with 0.001 M  $\text{Cs}^+$  at  
520 pH 10, with  $2\theta$  ( $^\circ$ ) along the  $x$ -axis, intensity along the  $y$ -axis, and time (min) along the  $z$ -axis  
521 where each pattern represents 5 min in time.

522

523 Figure 3. A typical Rietveld refinement of Cs exchange into hexagonal H-birnessite at pH 6.5.  
524 The black symbols represent the collected data, the green line represents the background, and the  
525 red line represents the modeled XRD pattern. Finally, the purple line represents the difference  
526 between the background and modeled pattern in comparison to the collected data.

527

528 Figure 4. Volume,  $V$ , ( $\text{\AA}^3$ ) plotted versus time (min) fit with Vegard's Law (Eqn. 8) with  $k_1$  ( $\text{min}^{-1}$ )  
529  $^1$ ) as the rate constant of reaction stage one and  $k_2$  ( $\text{min}^{-1}$ ) as the rate constant of reaction stage  
530 two at (a) pH 3, (b) pH 5, (c) pH 6.5, (d) pH 9, and (e) pH 10.

531

532 Figure 5. The log of the initial rate plotted as a function of pH. The change in initial cation  
533 exchange rate is weakly dependent on pH.

534

535 Figure 6. The change in volume ( $\text{\AA}^3$ ) versus time (min) versus pH. The unit-cell volume  
536 increases as pH increases.

537

538 Figure 7. Plots of Cs uptake (wt%) from the flow-through solution as a function of time.  
539 Positive percentages represent Cs uptake while negative percentages represent Cs release from  
540 the hexagonal birnessite. More Cs is sequestered by the hexagonal H-birnessite as the pH  
541 increases. Each plot represents a cation exchange reaction completed at a different pH: (a) pH 3,  
542 (b) pH 5, (c) pH 6.5, (d) pH 9, and (e) pH 10.

543

544 Figure 8. Plots of the Mn concentration (ppm) in the leachate as a function of time (min). Each  
545 plot represents a cation exchange reaction completed at a different pH: (a) pH 3, (b) pH 5, (c) pH  
546 6.5, (d), pH 9, and (e) pH 10.

547

548 Figure 9.  $\text{Mn}_{(\text{oct})}$  site occupancy increases to 1.0 as pH increases, indicating the vacancies within  
549 the octahedral Mn-O sheet are filled with oxidized  $\text{Mn}^{2/3+}$  from the interlayer.

550

551 Figure 10. ASEM elemental maps showing the distribution of Mn, O, and Cs on partially  
552 exchanged hexagonal H-birnessite at pH 9 (40 min).

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559**TABLES**Table 1. Final Rietveld refinement parameters for end-member hexagonal H-birnessite exchanged with 0.001 M Cs<sup>+</sup> at various pHs.

	pH 3	pH 5	pH 6.5	pH 9	pH 10
Space group	$P\bar{3}$	$P\bar{3}$	$P\bar{3}$	$P\bar{3}$	$P\bar{3}$
Unit cell					
a = b (Å)	2.85090(4)	2.85054(3)	2.85844(3)	2.86977(1)	2.87725(3)
c (Å)	7.37897(9)	7.36808(2)	7.35841(9)	7.37082(7)	7.37601(6)
V (Å <sup>3</sup> )	51.938(8)	51.848(9)	52.068(4)	52.570(4)	52.882(1)
Refinement					
No. of diffraction poin	1676	1676	1676	1676	1676
No. of reflections	27	29	29	27	21
Diffraction range (2θ)	3.9-37.303	3.9-37.303	3.9-37.303	3.9-37.303	3.9-37.303
No. of variables	32	31	32	31	30
R(F <sup>2</sup> )	0.0193	0.017	0.0175	0.017	0.018
R <sub>wp</sub>	0.0147	0.0105	0.0144	0.0195	0.0195
χ <sup>2</sup>	4.823	3.788	3.941	3.473	2.756

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562  
563 Table 2. Atomic coordinates and isotropic displacement factors for Cs-exchanged hexagonal H-  
564 birnessite across a wide pH range.  
565

pH	Atom	x	y	z	Site occupancy factor	$U_{\text{iso}} \times 10^2$ ( $\text{\AA}^2$ ) <sup>**</sup>
3	Mn <sub>oct</sub>	0	0	0	0.738(4)	1.500
	O <sub>oct</sub>	0.3333	0.6667	0.12145(1)	1.000	2.477
	O <sub>int</sub> <sup>*</sup>	0.6667	0.3333	0.46085(9)	0.667(2)	8.000
	Mn <sub>int</sub>	0	0	0.72346(9)	0.167(7)	1.500
5	Mn <sub>oct</sub>	0	0	0	0.709(2)	1.500
	O <sub>oct</sub>	0.3333	0.6667	0.11788(9)	1.000	2.477
	O <sub>int</sub> <sup>*</sup>	0.6667	0.3333	0.46895(2)	0.682(0)	8.000
	Mn <sub>int</sub>	0	0	0.72635(5)	0.179(0)	1.500
6.5	Mn <sub>oct</sub>	0	0	0	0.816(5)	1.500
	O <sub>oct</sub>	0.3333	0.6667	0.12060(1)	1.000	2.477
	O <sub>int</sub> <sup>*</sup>	0.6667	0.3333	0.46532(5)	0.727(7)	8.000
	Mn <sub>int</sub>	0	0	0.71783(1)	0.160(7)	1.500
9	Mn <sub>oct</sub>	0	0	0	1.000(0)	1.500
	O <sub>oct</sub>	0.3333	0.6667	0.10760(3)	1.000	2.477
	O <sub>int</sub> <sup>*</sup>	0.6667	0.3333	0.45128(2)	0.879(1)	8.000
	Mn <sub>int</sub>	0	0	0.69510(1)	0.000	1.500
10	Mn <sub>oct</sub>	0	0	0	1.000(0)	1.500
	O <sub>oct</sub>	0.3333	0.6667	0.10019(2)	1.000	2.477
	O <sub>int</sub> <sup>*</sup>	0.6667	0.3333	0.44941(9)	0.892(8)	8.000
	Mn <sub>int</sub>	0	0	0.68417(5)	0.000	1.500

566  
567 <sup>\*</sup>O<sub>int</sub> designates a combined O (water) and Cs site.

568 <sup>\*\*</sup>Values of  $U_{\text{iso}}$  were fixed.

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Table 3. Selected bond distance values for Cs-exchanged hexagonal H-birnessite as a function of pH.

Bond	pH 3	pH 5	pH 6.5	pH 9	pH 10
Mn <sub>oct</sub> -Mn <sub>oct</sub>	2.85090(29) x 6	2.85054(32) x 6	2.85844(35) x 6	2.86977(32) x 6	2.87725(31) x 6
Mn <sub>oct</sub> -O <sub>oct</sub>	1.874(4) x 6	1.861(4) x 6	1.874(5) x 6	1.837(4) x 6	1.8182(34) x 6
O <sub>oct</sub> -O <sub>int</sub>	3.045(19) x 3	3.066(18) x 3	3.026(16) x 3	3.027(17) x 3	3.062(11) x 3
O <sub>oct</sub> -O <sub>int</sub>	3.074(18)	3.044(19)	3.047(23)	3.251(21)	3.317(19)
Mn <sub>int</sub> -O <sub>oct</sub>	2.005(5) x 3	2.006(4) x 3	2.034(6) x 3	2.205(10) x 3	2.300(12) x 3
Mn <sub>int</sub> -O <sub>int</sub>	2.542(16) x 3	2.511(15) x 3	2.485(19) x 3	2.444(18) x 3	2.400(17) x 3
Mn <sub>int</sub> -O <sub>int</sub>	2.135(13) x 3	2.186(14) x 3	2.131(13) x 3	1.977(12) x 3	1.931(12) x 3

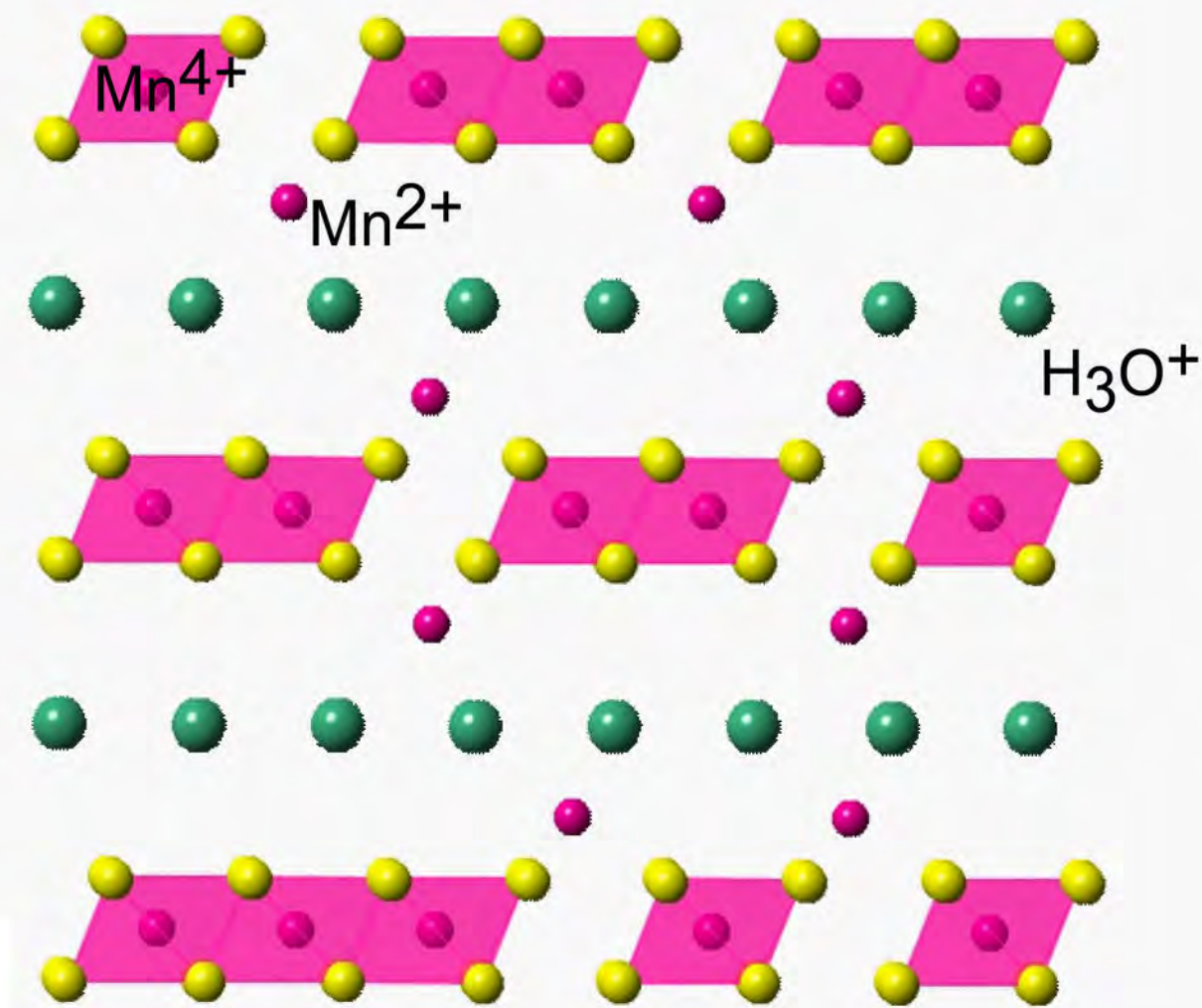
573  
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575  
576 Table 4. The first stage rate constant,  $k_I$ , and initial rate,  $dV/dt$ , of  $\text{Cs}^+$  exchange into hexagonal  
577 H-birnessite as a function of pH.  
578

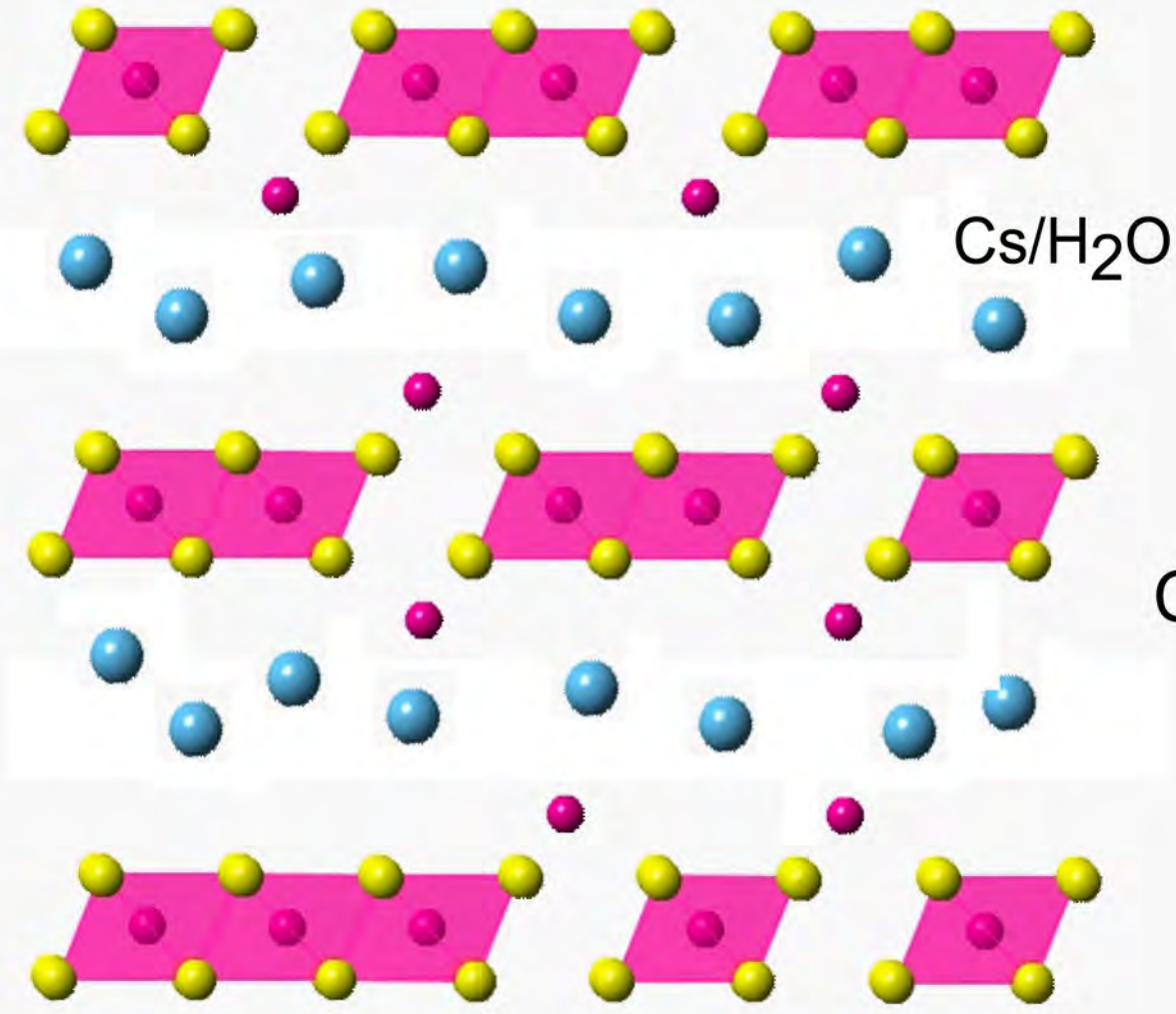
<b>pH</b>	<b><math>k_I</math> (<math>\text{min}^{-1}</math>)</b>	<b><math>dV/dt</math> (<math>\text{\AA}^3/\text{min}</math>)</b>
3	$0.195 \pm 0.0132$	$0.064 \pm 0.0045$
5	$0.101 \pm 0.0156$	$0.037 \pm 0.0070$
6.5	$0.122 \pm 0.0325$	$0.033 \pm 0.0110$
9	$0.122 \pm 0.2265$	$0.016 \pm 0.0853$
10	$0.066 \pm 0.0962$	$0.021 \pm 0.1106$

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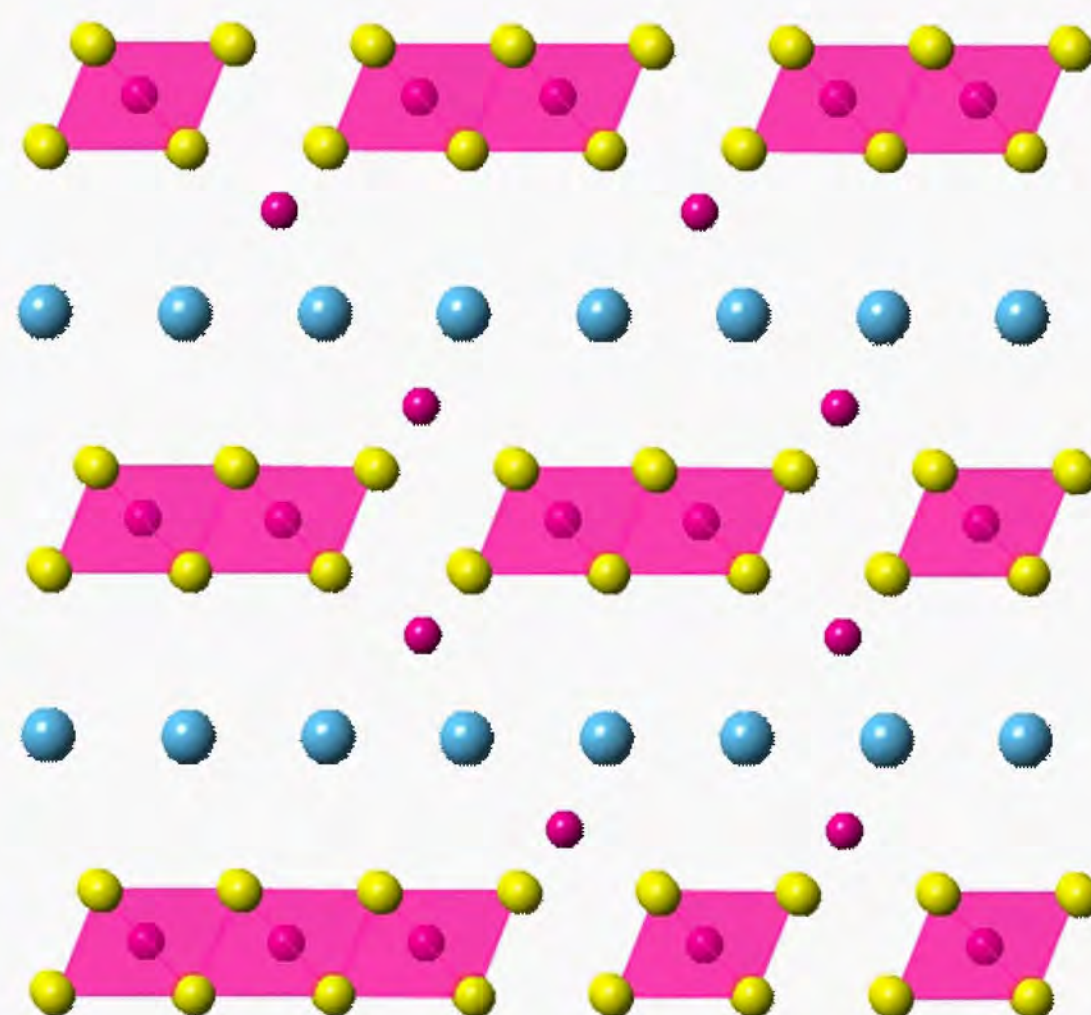
hexagonal H-birnessite

$k_1$   
Cation exchange



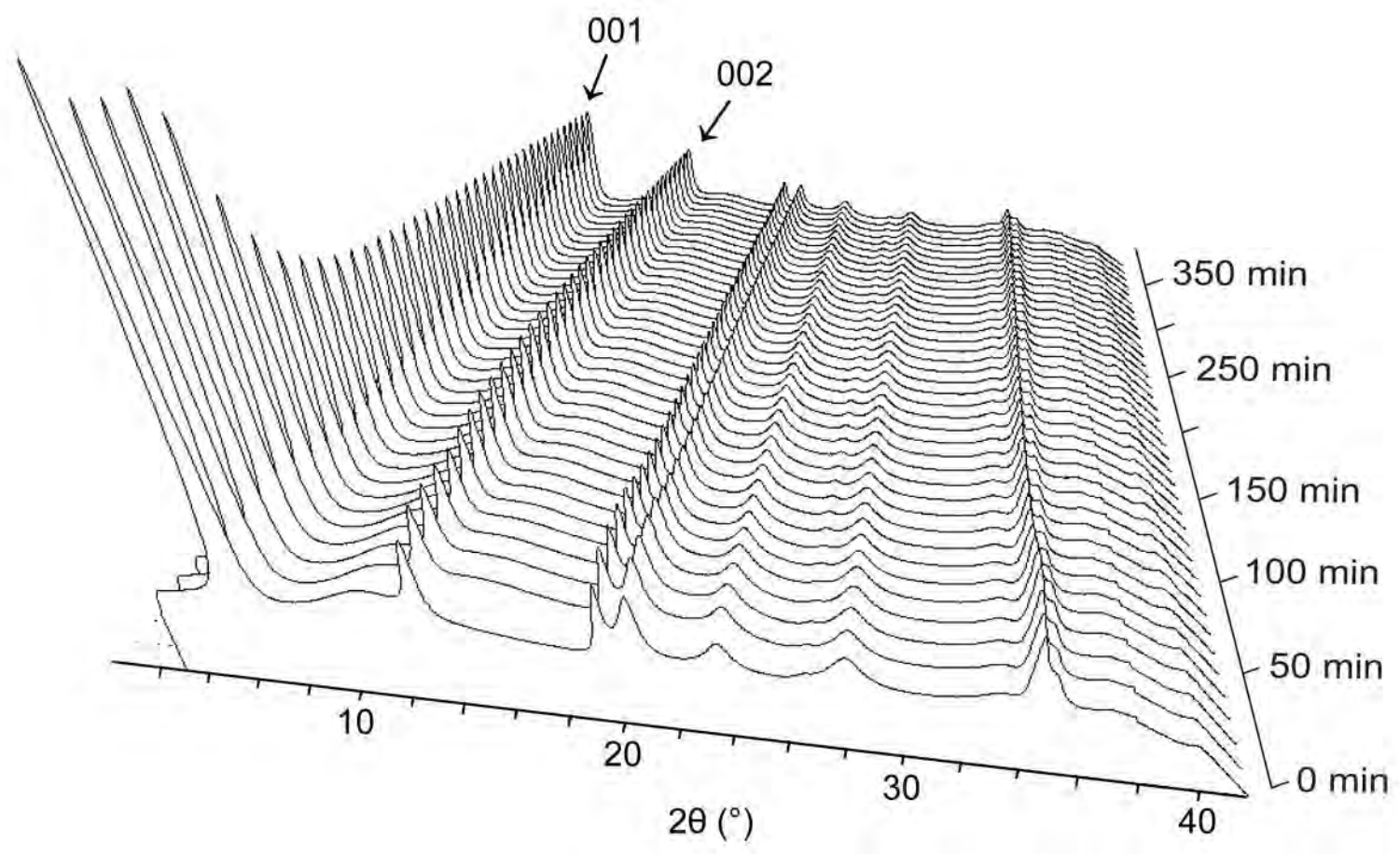
hexagonal Cs-birnessite (disordered)

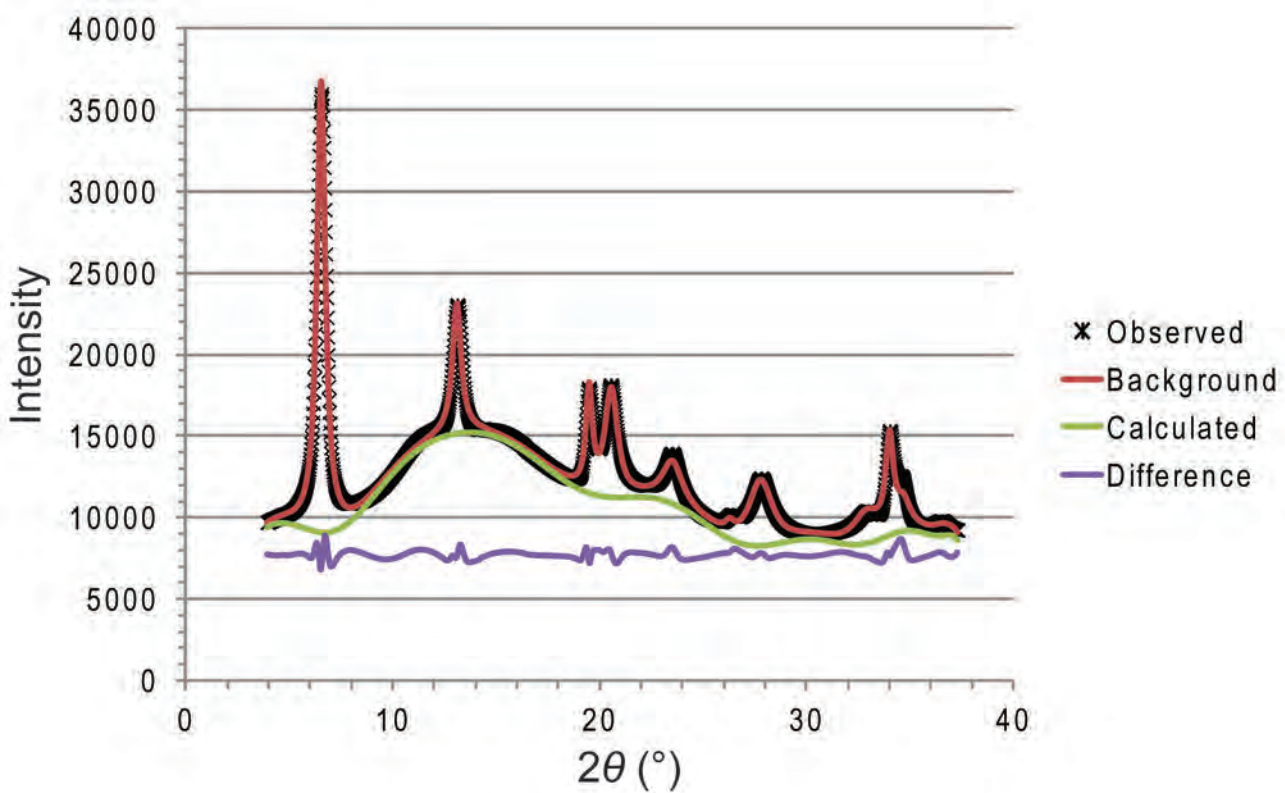
$k_2$   
Cation ordering

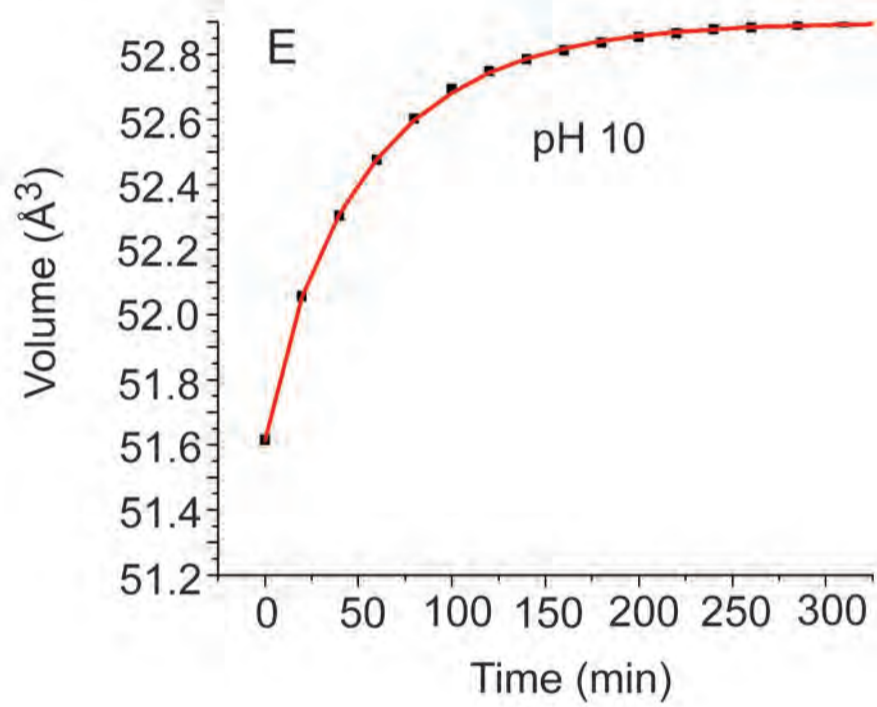
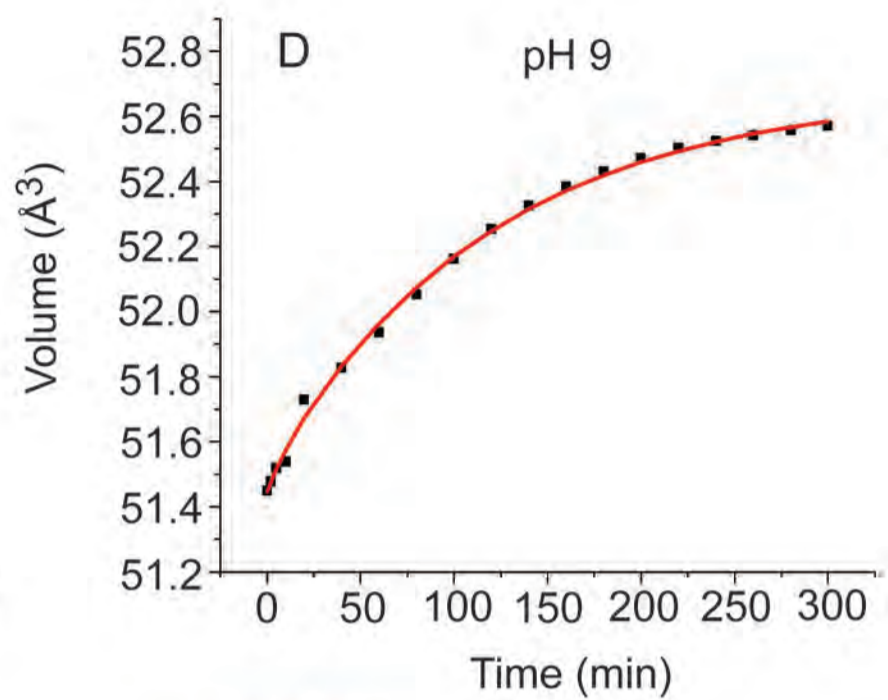
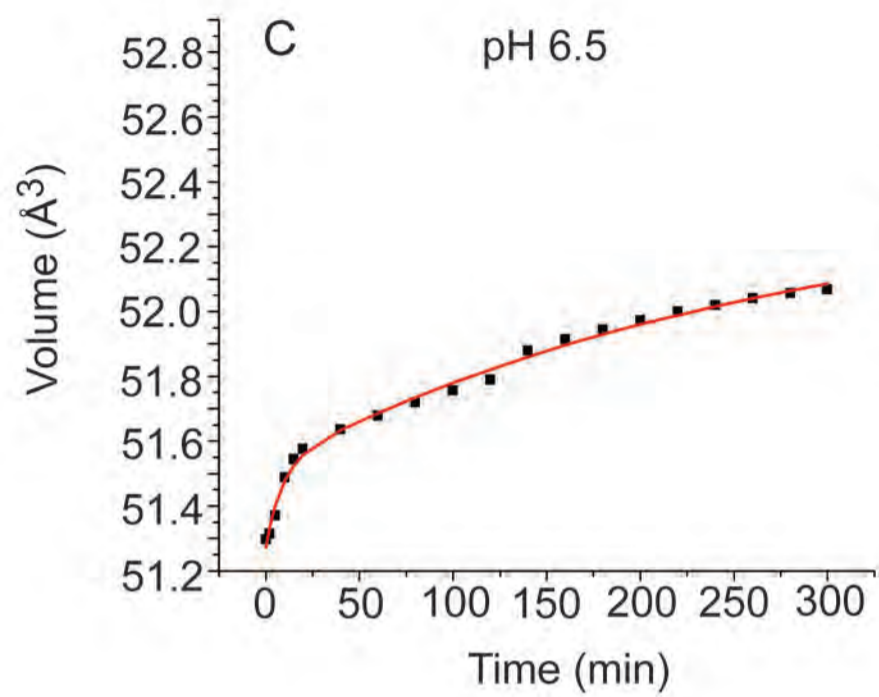
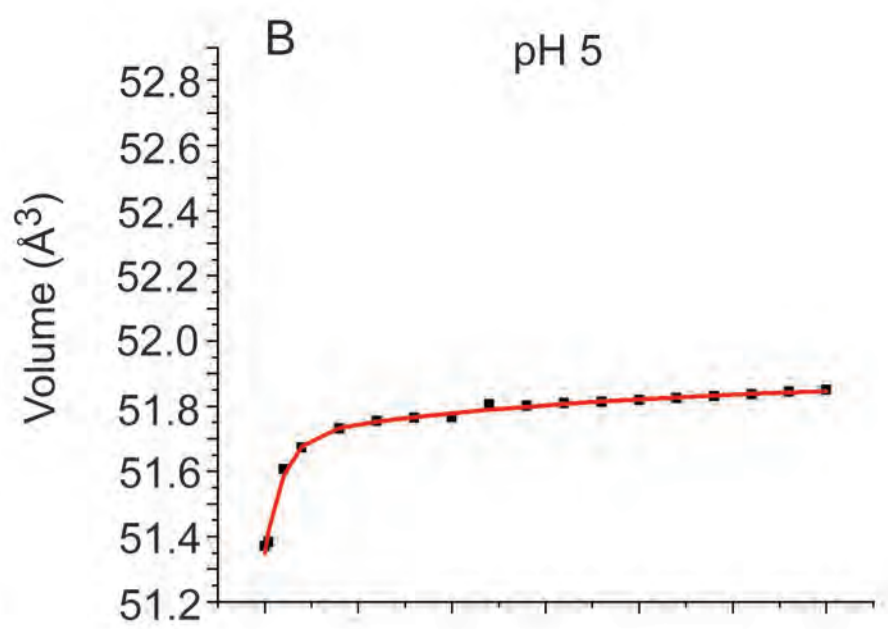
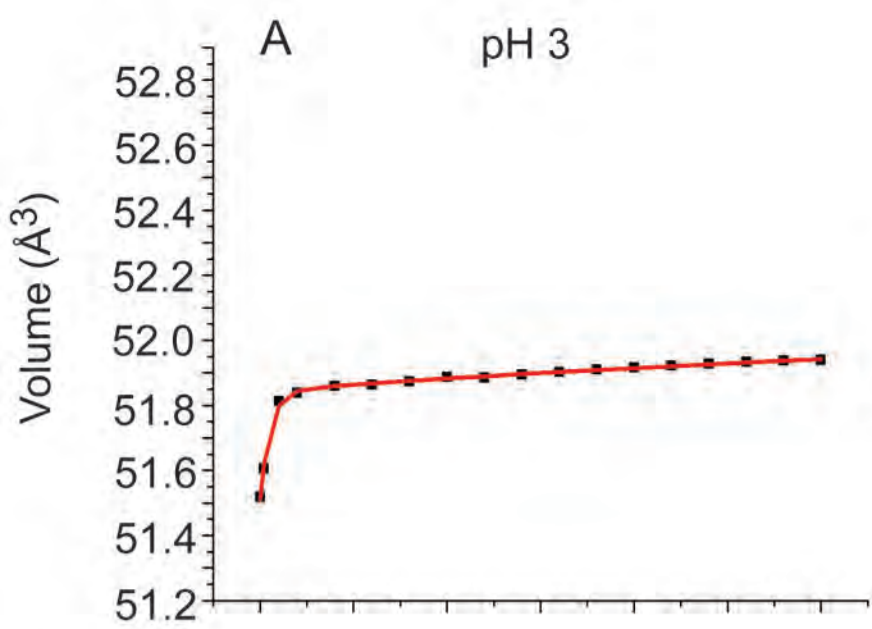


hexagonal Cs-birnessite (ordered)

a

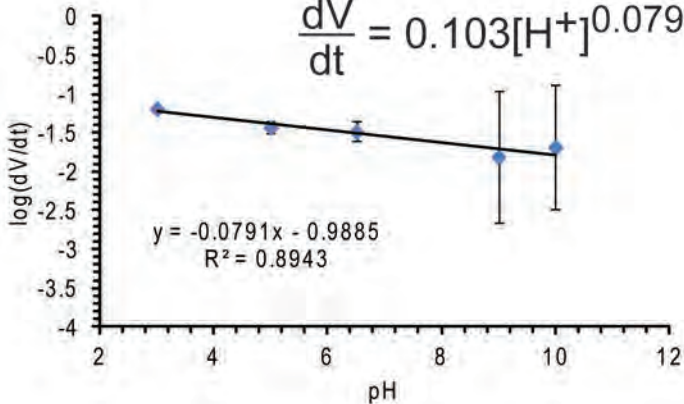


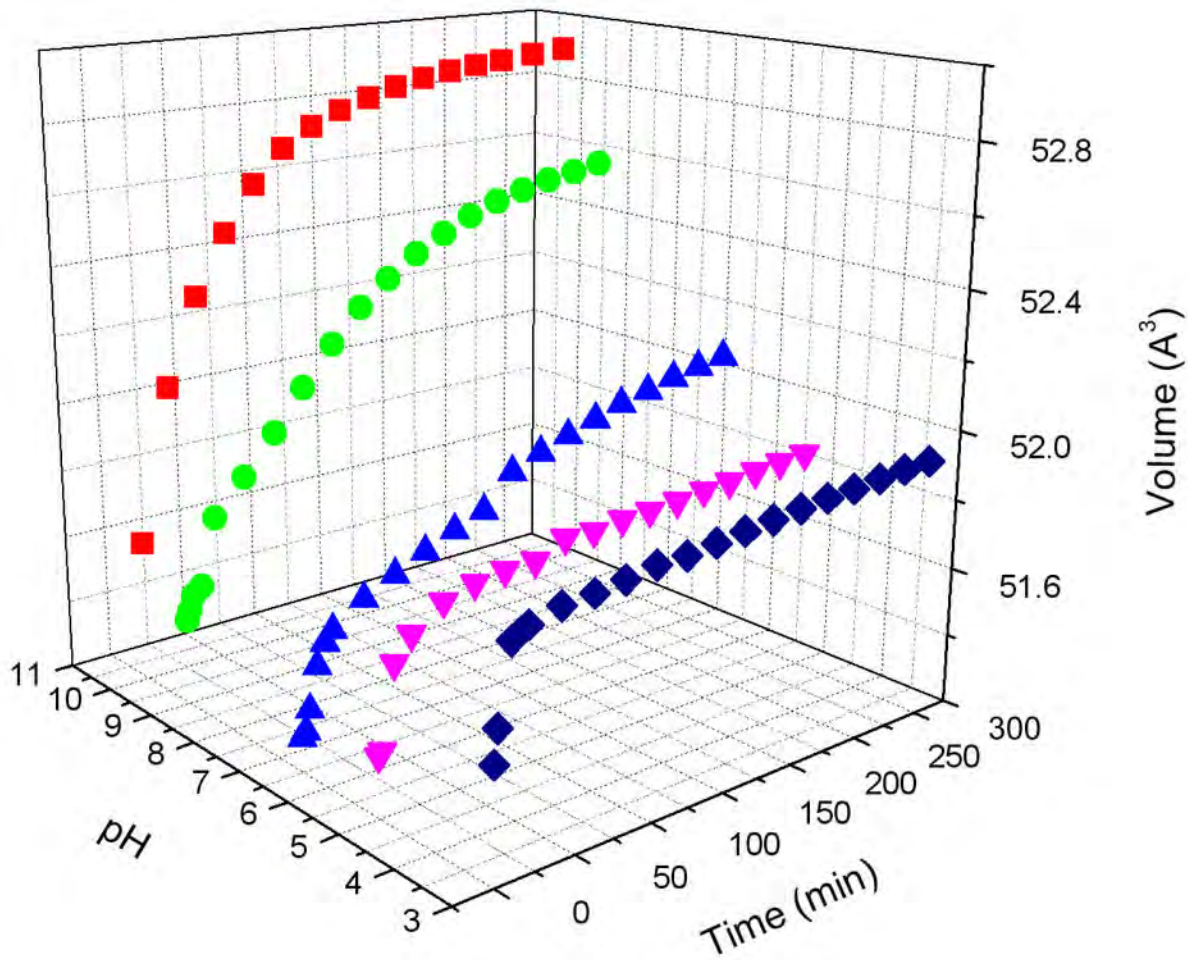


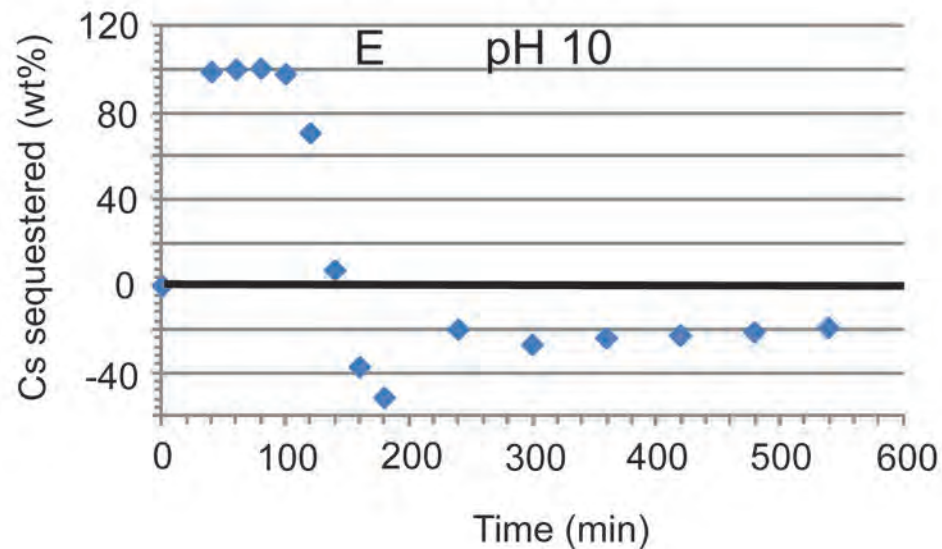
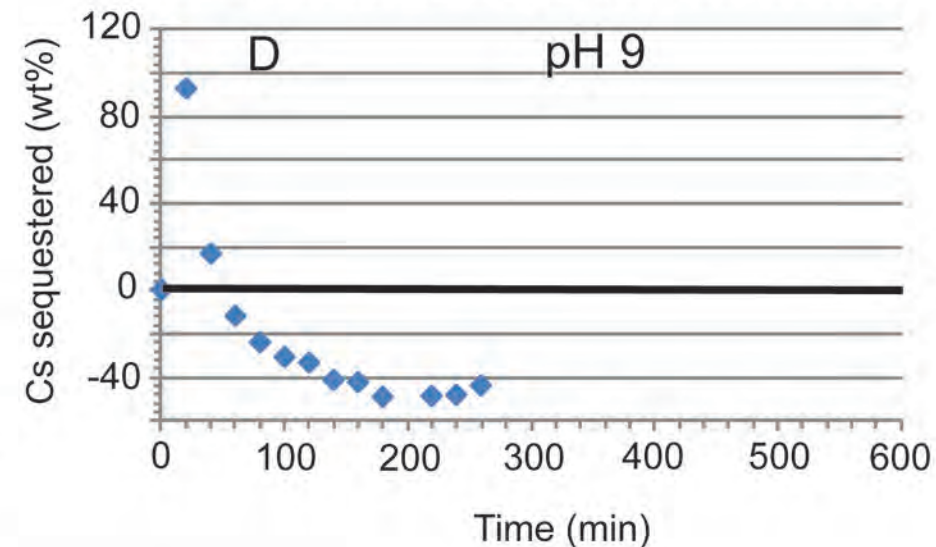
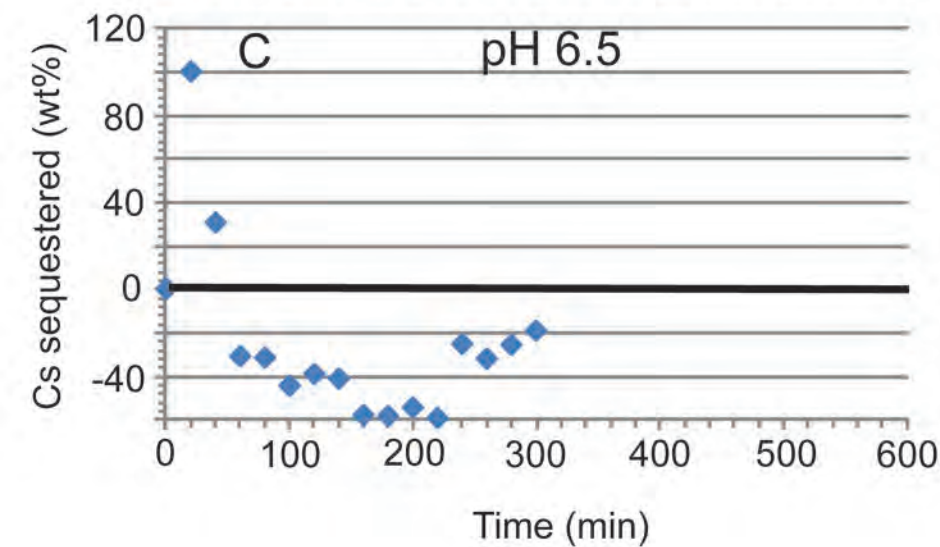
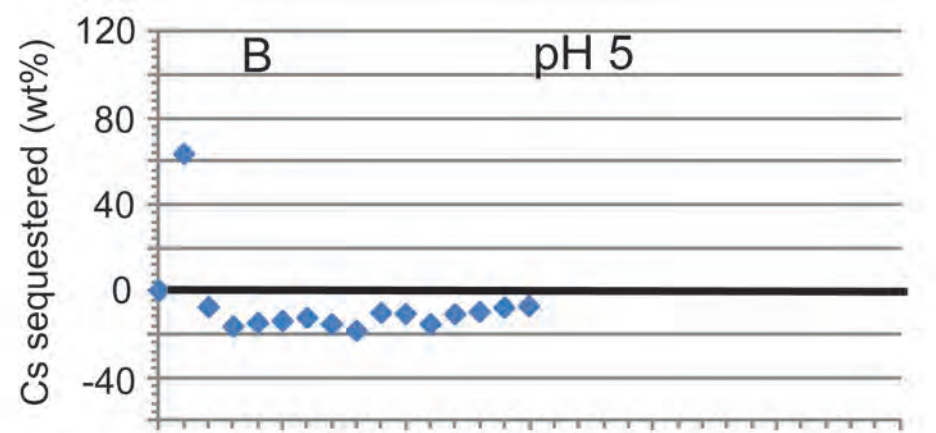
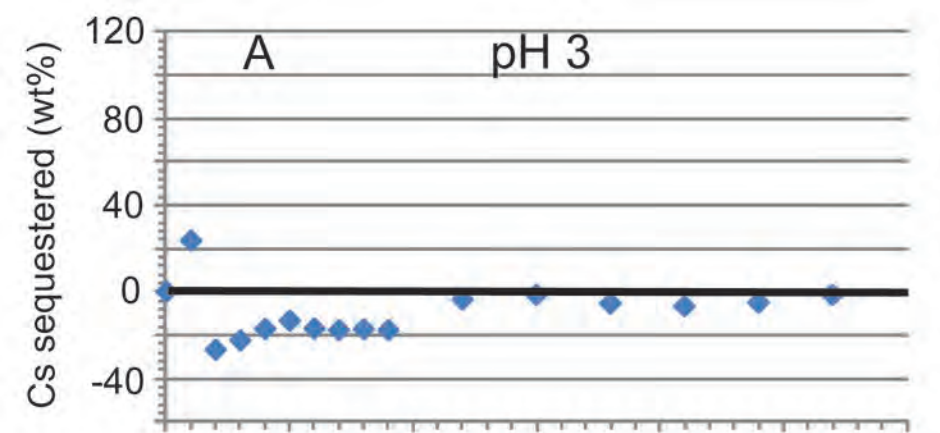


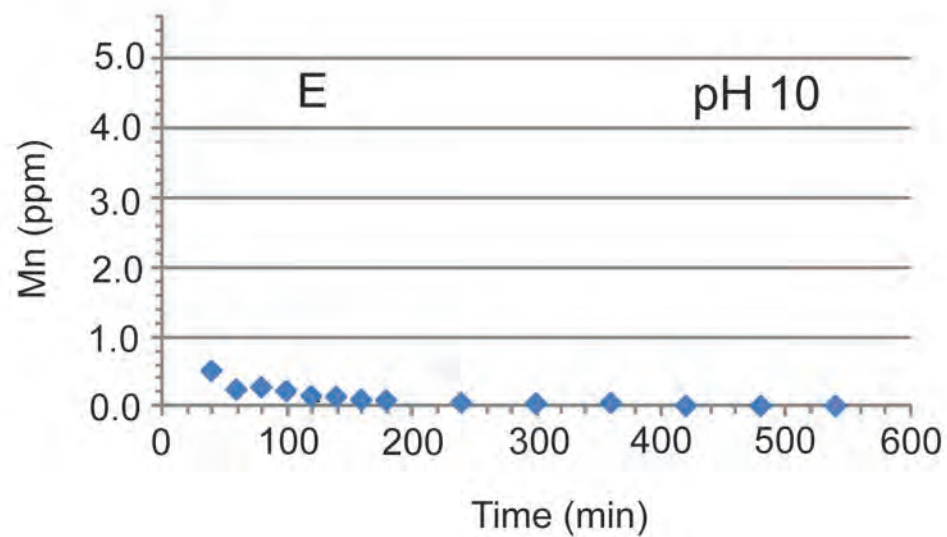
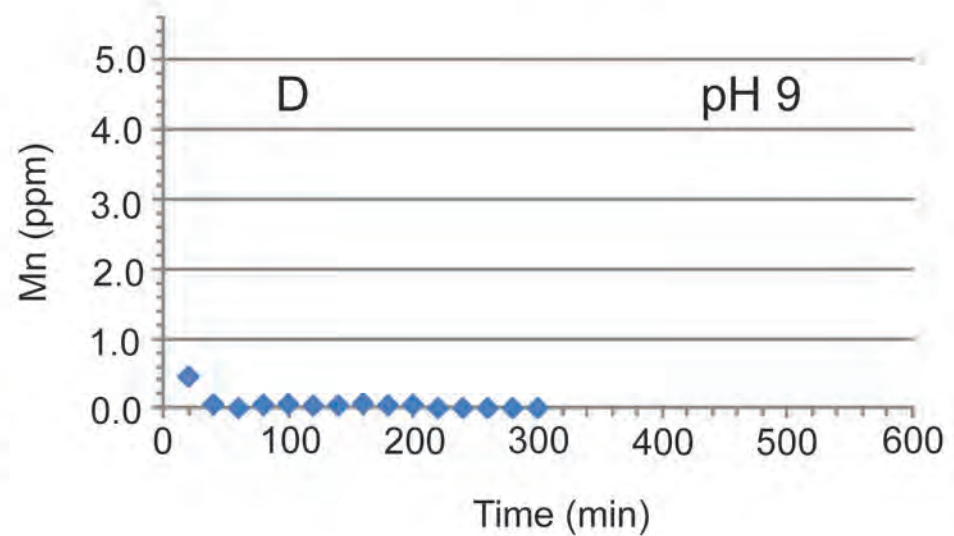
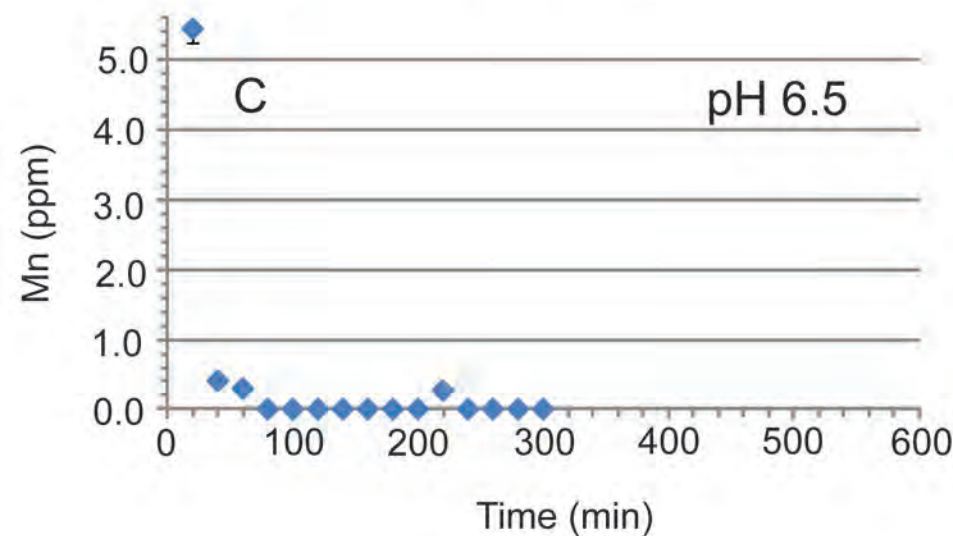
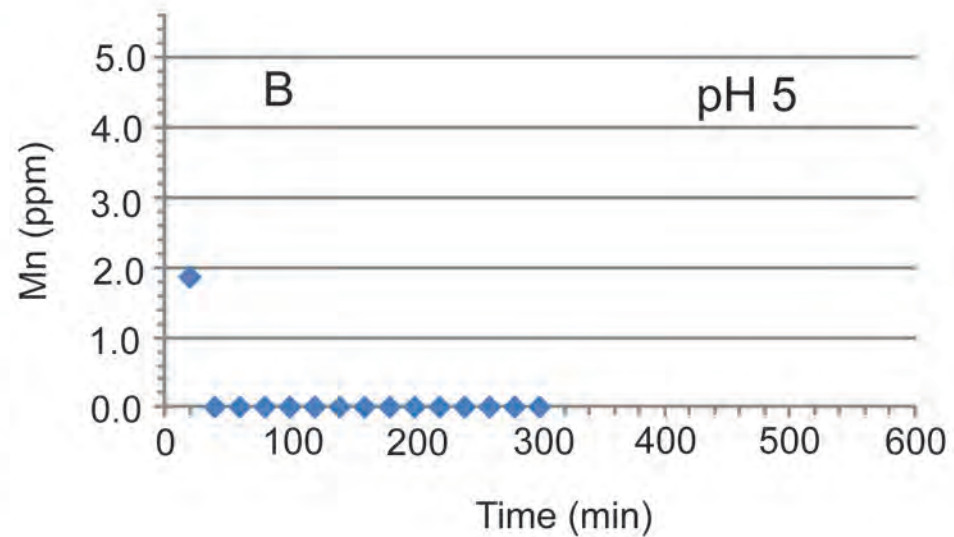
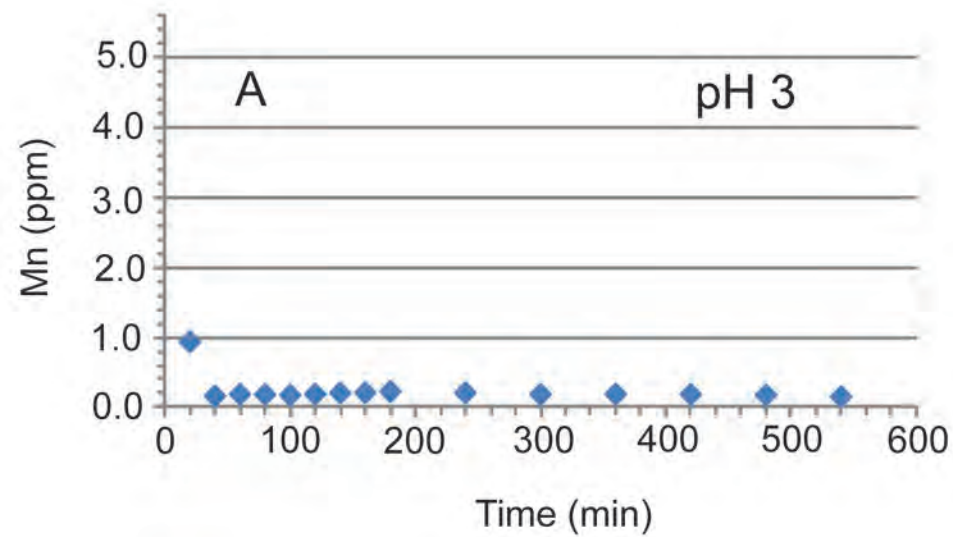


$$\frac{dV}{dt} = 0.103[\text{H}^+]^{0.079}$$









$Mn_{(oct)}$  site occupancy

