

Revision 1

Diffusion of Helium in Natural Monazite, and Preliminary Results on He diffusion in Synthetic Light Rare Earth Phosphates

D.J. Cherniak, E.B. Watson
Department of Earth and Environmental Sciences
Rensselaer Polytechnic Institute
Troy, NY 12180 USA

Abstract

Diffusion of helium has been characterized in natural monazite and synthetic LREE phosphates. Polished slabs of natural monazite and flat growth faces of synthetic phosphates were implanted with 100 keV ^3He at a dose of $5 \times 10^{15} \text{ } ^3\text{He}/\text{cm}^2$ and annealed in 1-atm furnaces. ^3He distributions following experiments were measured with Nuclear Reaction Analysis using the reaction $^3\text{He}(d,p)^4\text{He}$. For diffusion in monazite we obtain the following Arrhenius relation for diffusion normal to (100):

$$D = 1.60 \times 10^{-7} \exp(-150 \pm 8 \text{ kJ mol}^{-1}/RT) \text{ m}^2\text{sec}^{-1}.$$

Diffusion in natural monazite exhibits little diffusional anisotropy, as diffusion normal to (001), (100) and (010) appear similar, as do diffusivities of He in natural monazites from two different localities. Over the investigated temperature range, these diffusivities are similar to those of Farley and Stockli (2002), and values obtained for some of the monazite grains analyzed by Boyce et al. (2005), obtained through bulk-release bulk release of He by step heating, and are bracketed by diffusivities obtained by Farley (2007) for monazite-structure synthetic REE phosphates.

He diffusion measured in synthetic REE phosphates (LaPO_4 , NdPO_4 , SmPO_4 and EuPO_4) with the monazite structure appears to behave systematically, with diffusion in the lighter REE phosphates slightly faster than in the heavier REE phosphates. This trend is in broad agreement

33 with the findings of Farley (2007), but the difference in diffusivities among the REE phosphates
34 is smaller than that reported by Farley (2007). Activation energies for He diffusion in the
35 synthetic LREE phosphates are similar to that for natural monazite measured in this study, but
36 He diffusivities in synthetic LaPO_4 are about an order of magnitude faster than in the natural
37 monazites.

38 The differences in He diffusivities among the natural monazites and synthetic REE
39 phosphates may be a consequence of the density and distribution of interstitial apertures in the
40 crystal structure, which may result in differences in He migration rates. The similarities in He
41 diffusivities for natural monazites containing varying mixtures of rare-earth elements, as well as
42 differences in Th contents, however, indicate that the above Arrhenius relation is most relevant
43 for describing He diffusion in monazite in nature.

44 We use this Arrhenius relation to evaluate He retentivity in monazite experiencing thermal
45 events, using both Dodson's (1973) closure temperature formulation and recently developed
46 expressions (Watson and Cherniak, 2013) for prograde thermal events and heating and cooling
47 trajectories. Calculations indicate that monazite is comparatively retentive of He among
48 accessory mineral phases.

49
50

51 Keywords: monazite, xenotime, rare-earth orthophosphates, helium, diffusion, nuclear reaction
52 analysis, thermochronology

53 **1. Introduction**

54
55 The relatively rapid diffusion rates and consequently low closure temperatures of He allow
56 insights into the time-temperature evolution of rocks that would be inaccessible by other means.
57 (U-Th)/He ages for apatite, zircon, titanite, rutile, and monazite, when coupled with a
58 quantitative understanding of the effects of temperature on measured ages due to diffusional loss
59 and conditions for He retention in minerals, can be used to map thermal structure to estimate the
60 timing, rate, and structural details of the process of exhumation and various near-surface tectonic
61 and geomorphic processes (e.g., Wolf et al., 1996; 1998; House et al., 1997;1998; Reiners et al.,
62 2000; Reiners and Farley, 2001; Farley, 2002; Farley and Stockli, 2002; Ehlers and Farley, 2003;
63 Reiners et al., 2005; Stockli, 2005; Shuster and Farley, 2005a). With advancement of analytical
64 techniques, these methods have found greater application (e.g., Farley, 2002; 2000; Reiners et al,
65 2002; 2004; 2005; Wolf et al., 1998; Shuster et al., 2006; Shuster and Farley, 2009). Further
66 understanding of He diffusion kinetics is essential for evaluating conditions under which He is
67 lost or retained in specific minerals and in refining interpretations of time-temperature histories.

68 Much of the present knowledge of the diffusion behavior of monazite and other REE
69 orthophosphates has been obtained through outgassing studies, where samples are heated in a
70 stepwise manner and the He released is measured by mass spectrometry (e.g., Farley, 2007;
71 Boyce et al., 2005; Farley and Stockli, 2002). While the employment of these methods has
72 provided invaluable information about the He diffusion systematics of many mineral phases,
73 several limitations exist. The “bulk release” patterns obtained in these studies do not provide
74 information about initial distributions of helium. Helium may be nonuniformly distributed,
75 depending on the distribution of U and Th in mineral grains, alpha ejection from mineral grains
76 during radioactive decay, and differential He losses due to past thermal histories. In addition,

77 microstructures within mineral grains may create diffusion fast paths, which cannot be readily
78 distinguished from lattice diffusion because profiles are not measured directly in these analyses.
79 Refinements of step-release techniques (e.g., Shuster and Farley, 2004; 2005a,b; Shuster et al.,
80 2004) which involve the generation of a uniform ^3He distribution by proton irradiation, coupled
81 with measurement of the ratio of simultaneously released $^4\text{He}/^3\text{He}$, have helped to surmount
82 some of these difficulties and provide more detailed information about the ^4He distributions
83 within mineral grains. However, non-Arrhenian and other poorly understood diffusion behaviors
84 have been observed for helium in some step-heating studies.

85 Direct profiling to characterize diffusion of implanted ^3He and ^4He in phosphates, oxides
86 and silicates has been undertaken using the techniques of nuclear reaction analysis (NRA) and
87 Elastic Recoil Detection (ERD) (e.g, Ouchani et al., 1998; Miro et al. 2007; 2006; Trocellier et
88 al., 2003a,b; Gosset et al., 2002; Constantini et al., 2002; Cherniak et al., 2009; Cherniak and
89 Watson, 2011; 2012a), and LA-ICPMS (Hodges et al., 2009; van Soest et al., 2011). These
90 studies complement the findings from bulk release experiments and provide additional
91 constraints on He diffusion. In previous work, we have presented results for He diffusion in
92 zircon and apatite (Cherniak et al., 2009), and titanite and rutile (Cherniak and Watson, 2011). In
93 the present study, we continue work on measurements of He diffusion in accessory minerals with
94 a study of natural monazite and synthetic REE phosphates with the monazite structure, taking a
95 similar approach to that in these earlier studies, where ion implantation was used to introduce
96 ^3He , and ^3He concentrations were measured by nuclear reaction analysis.

97 Anisotropy of helium diffusion may be pronounced in some mineral phases, as has been
98 observed recently in measurements of zircon (Cherniak et al., 2009; Hodges et al., 2009) and
99 rutile (Cherniak and Watson, 2011). Since the existence and extent of anisotropy may be difficult

100 to evaluate through bulk-release techniques, direct profiling of He distributions to evaluate
101 diffusion coefficients may provide additional understanding of diffusion behavior and processes.
102 These methods offer a means to directly profile He distributions, permitting direct
103 determinations of diffusional anisotropy. NRA depth profiling measurements, in this case using a
104 deuterium beam to induce nuclear reactions with ^3He introduced into the sample by ion
105 implantation, probe the outer few μm of oriented samples, yielding essentially 1-dimensional
106 geometry in analysis, in contrast to bulk-degassing experiments, where He is released and
107 detected simultaneously from all sides of the sample. NRA also permits direct profiling of much
108 shorter profiles than laser ablation depth profiling (e.g., van Soest et al., 2011), so diffusivities at
109 lower temperatures, which may be closer to those of geological relevance, can be measured. Ion
110 implantation is a means to introduce He in a controlled dose and distribution (determined by the
111 implanted ion energy and the material) in the sample, so there are no analytical artifacts due to
112 initial zoning or other intragrain variations of He concentrations in mineral samples. Such
113 variations may be a significant factor in monazite, where zoning in Th is frequently observed
114 (e.g., Pyle et al., 2001, Kohn and Malloy, 2004; Yang and Pattison, 2006), which could result in
115 nonuniform distributions of ^4He within a mineral grain. Further, studies of He diffusion in
116 natural monazite by Boyce et al. (2005) suggest that intergrain variations in He diffusivities may
117 be due to compositional variations, possibly substitutions of Y and Th for Ce, and/or a
118 consequence of potential influences on He release patterns due to internal zoning of U and Th in
119 individual grains. Among synthetic REE phosphates of the monazite structure, Farley (2007)
120 observed that He diffusivities vary with monazite composition, with faster diffusivities for the
121 lighter REE phosphates than for heavier REE phosphates. To explore some of these potential
122 compositional effects, we performed experiments on natural monazites from two different

123 localities, with differing Th contents, and on four synthetic REE phosphates (SmPO₄, LaPO₄,
124 NdPO₄, and EuPO₄).

125

126 **2. Experimental Procedure**

127

128 **2.1 Sample Preparation**

129

130 The natural monazites used in the experiments were specimens from Brazil and North

131 Carolina. Samples from the latter locality have been used in previous studies of Pb (Cherniak et

132 al., 2004a) and oxygen (Cherniak et al., 2004b) diffusion. These natural monazites were chosen

133 for study because fairly large crystals could be obtained to produce samples with homogeneous

134 regions free of cracks and inclusions of sufficient size for analysis. Compositional information

135 on the monazites is in Table 1. While the monazites have similar REE contents, they differ

136 widely in Th concentration, which has the potential to affect diffusivities both through effects on

137 lattice parameters due to altrivalent substitutions and differences in degree of radiation damage.

138 Specimens of oriented monazite (to measure diffusion normal to (001) and (100), and (100) and

139 (010) faces in the North Carolina and Brazil monazites, respectively) cut into slabs about 0.5 mm

140 thick and polished to 0.3 μm alumina, followed by a chemical polish with colloidal silica. After

141 polishing, monazite samples were cleaned ultrasonically in distilled water and ethanol.

142 Experiments were also run on synthetic REE phosphates produced by a flux growth method

143 using Na₂CO₃-MoO₃ fluxes (Cherniak et al., 2004c). Each synthetic phosphate contained a single

144 REE (Sm, La, Nd, or Eu); information about these materials (electron microprobe analyses and

145 XRD measurements) is presented in Cherniak et al. (2004c). For the synthetic phosphates,

146 samples with large clean growth faces ((100)) were selected; these received no treatment prior to

147 ion implantation other than ultrasonic cleaning in distilled water and ethanol to remove any

148 residual flux clinging to crystal surfaces.

149

150 **2.2 Ion implantation and diffusion experiments**

151 The synthetic and natural monazite samples (typically sections ~2 to 3mm on a side and
152 0.5-1 mm thick) were mounted for ion implantation on an aluminum plate using carbon paint.

153 The samples were implanted at room temperature with 100 keV ^3He ions produced in the Extrion
154 ion implanter at the Ion Beam Laboratory. Doses were $5 \times 10^{15} \text{ } ^3\text{He}/\text{cm}^2$. All of the samples to be
155 implanted were mounted together on the aluminum plate and implanted simultaneously, so they
156 received the same implant dose. For the diffusion experiments, implanted specimens were heated
157 in crimped Pt capsules placed in 1 atmosphere Kanthal-wire wound vertical tube furnaces.

158 Experiments were run in air at temperatures from 300-600°C, for times from 20 minutes to 6
159 weeks (Tables 2 and 3). Temperatures in furnaces were monitored with chromel-alumel (type K)
160 thermocouples, with temperature uncertainties $\sim \pm 2^\circ\text{C}$. Samples were positioned to within 5mm
161 of thermocouple junctions; hotspots in furnaces used for diffusion anneals were typically about 2
162 cm in length.

163

164 **2.3 NRA measurements**

165 ^3He distributions in the samples were measured with Nuclear Reaction Analysis using the
166 $^3\text{He}(d,p)^4\text{He}$ reaction (e.g., Pronko and Pronko, 1974; Dieumegard et al., 1979; Payne et al.,
167 1989; Paszti, 1992). Analyses were performed at the 4 MeV Dynamitron accelerator at the
168 University at Albany. This nuclear reaction has been used to measure ^3He in a variety of
169 minerals and ceramic materials, including apatite (e.g., Miro et al., 2006; Cherniak et al., 2009),
170 zircon (Cherniak et al., 2009), zirconia (Gosset et al., 2002, Costantini et al., 2003; Trocellier et
171 al., 2003a,b), britholite (Gosset and Trocellier, 2005; Gosset et al., 2002, Costantini et al., 2002;
172 Trocellier et al., 2003a; b), titanite (Cherniak and Watson, 2011), rutile (Cherniak and Watson,

173 2011), olivine (Cherniak and Watson, 2012a) and garnet (Roselieb et al., 2006). The protons
174 produced in the reaction, along with backscattered deuterons and products of various (d,p) and
175 (d, α) reactions induced with light elements contained in the sample, were detected with a solid
176 state surface barrier detector with 1500 μm depletion depth and 100 mm^2 area positioned at
177 167.5° with respect to the incident beam. The beamspot incident on sample surfaces was ~ 1 to
178 1.5mm on a side. A 7.5 μm thick Kapton foil was placed in front of the detector to stop some of
179 the backscattered deuterons. Because the protons produced in the $^3\text{He}(d,p)^4\text{He}$ reaction are so
180 energetic, they stand apart from other contributions to the spectrum, with very little background.
181 The cross-section of the reaction has a maximum around 430 keV, but the peak is relatively
182 broad (several hundred keV in width) so it is not possible to obtain high depth resolution for ^3He
183 profiling using typical approaches for resonant or non-resonant NRA. For these analyses, we
184 take the approach used in earlier studies (Cherniak et al., 2009; Cherniak and Watson, 2011;
185 2012a), performing analyses over a range of energies (0.5 to 0.9 MeV in this work) to better
186 define the profile, and comparing the proton yield from the annealed sample (i.e., a sample from
187 a diffusion experiment) to an implanted, unannealed sample at each energy step. It should be
188 emphasized that the sampling depth in the monazites in these analyses is up to several microns,
189 considering the ranges for deuterons of these incident energies in monazite (e.g., Ziegler and
190 Biersack, 2006). Given these depth ranges, and that the implanted He will diffuse both toward
191 and *away from* the sample surface, the depth of material interrogated is well in excess of the few
192 hundred nm depth of the implanted He, in contrast to inaccurate statements made (Ketcham et
193 al., 2013) in reference to an earlier study using this method (Cherniak et al., 2009).

194 These measured ratios were converted into diffusivities by first evaluating the fractional loss
195 of diffusant from an implanted profile as a function of Dt . For a semi-infinite medium with the

196 concentration of diffusant equal to zero at $x = 0$, the distribution of the implanted species can be
 197 described as a function of depth x and time t as (Ryssel and Ruge, 1986):

198
 199

$$N(x,t) = \frac{N_m/2}{\sqrt{\left(1 + \frac{2Dt}{\Delta R^2}\right)}} \left(\exp\left[-\frac{(x-R)^2}{2\Delta R^2 + 4Dt}\right] \times \left[1 + \operatorname{erf}\left(\frac{\frac{R\sqrt{4Dt} + x\sqrt{2\Delta R}}{\sqrt{2\Delta R^2 + 4Dt}}}{\sqrt{4Dt}}\right) \right] + \exp\left[-\frac{(x+R)^2}{2\Delta R^2 + 4Dt}\right] \times \left[1 + \operatorname{erf}\left(\frac{\frac{R\sqrt{4Dt} - x\sqrt{2\Delta R}}{\sqrt{2\Delta R^2 + 4Dt}}}{\sqrt{4Dt}}\right) \right] \right) \quad (1)$$

200 where D is the diffusion coefficient, N_m is the maximum concentration of the implanted species
 201 (in an unannealed sample), R is the range (depth in the material) of implanted species, and ΔR is
 202 the range straggle (full width at half-maximum width of the initial implanted distribution).

203 Values of R and ΔR for ^3He from the Monte-Carlo simulation program SRIM 2006 (Ziegler and
 204 Biersack, 2006) are 3520 and 860 Å in the natural monazites; values for N_m are ~0.32 at% for
 205 the implanted dose of $5 \times 10^{15}/\text{cm}^2$ for the 100 keV ^3He . For the end-member REE phosphates,
 206 values for R and ΔR , respectively, are 3560 and 860 Å for LaPO_4 , 3550 and 880 Å for NdPO_4 ,
 207 3520 and 880 Å for SmPO_4 , and 3550 and 900 Å for EuPO_4

208 Equation (1) describes the ^3He distribution, but the proton yield measured will be a function
 209 not only of the ^3He concentration but also of the depth in the material over which the incident
 210 deuteron beam can induce the nuclear reaction, the cross-section of the reaction as a function of
 211 energy (and depth in the material), the number of deuterons impinging on the target (N_d), and the
 212 solid angle subtended by the detector (Ω). The number of detected protons for a profile analyzed
 213 with a given beam energy E_0 can be determined from the expression

214
 215

$$N_p(E_0) = N_d(E_0)\Omega \int_{x=0}^{\infty} \frac{d\sigma(E_d(x))}{d\Omega} \rho(x) dx \quad (2)$$

216
 217 where $d\sigma(E_d(x))/d\Omega$ is the differential cross section for the $^3\text{He}(d,p)^4\text{He}$ reaction at energy E_d ,
 218 which describes the probability of the reaction occurring at this deuteron energy. The deuteron

219 energy $E_d(x)$ will be attained at some specific depth x in the material, which is dependent on the
220 incident deuteron energy (E_o) and the rate of energy loss for the deuterons with depth within the
221 material. In the integral above, $\rho(x)$ represents the depth distribution of the diffusant. The above
222 integral is evaluated numerically for each incident deuteron energy by calculating the variation
223 of the reaction cross section with depth in the material. Since the reaction cross section is
224 dependent on deuteron energy, it will vary with depth as energy is lost by incident deuterons
225 traveling through the sample. Values of cross section as a function of energy are derived from
226 the data of Möller and Bensenbacher (1980) and Mayer et al. (2005) corrected for beam-detector
227 angle. These cross-section values are then related to depth in the sample by calculating the
228 energy loss with depth for the incident deuterons for monazite targets using stopping powers
229 obtained from the software SRIM 2006 (Ziegler and Biersack, 2006). The cross-section curves as
230 a function of energy are then used to determine the proton yield from the ^3He concentrations $\rho(x)$
231 across the profile as a function of depth. The values obtained are summed to determine the
232 proton yield for the entire profile for each incident proton energy E_o . The yields for an
233 unannealed implanted reference samples can also be determined in this manner, and a
234 relationship can be determined for each incident beam energy directly relating the ratio of proton
235 yields for an implanted untreated sample and an annealed sample to a specific value of Dt , as
236 outlined in previous work (Cherniak and Watson, 2011; 2012). Uncertainties in diffusivities are
237 determined from counting statistics from the detected proton signals and the variance of
238 calculated diffusivities among incident beam energies used for each sample, which also take into
239 consideration the uncertainties associated with stopping powers in monazite for the incident
240 deuterons and the implanted helium.

241
242 **3. Results**

243
244 ³He diffusion coefficients for natural monazite and the synthetic REE phosphates are
245 presented in **Tables 2 and 3** and plotted in **Figures 1 and 2**. From a least-squares fit to the data
246 for the North Carolina monazite, over the temperature range 317-600°C, we obtain an activation
247 energy of 150 ± 8 kJ/mol and pre-exponential factor (D_0) of 1.60×10^{-7} m²/sec ($\log D_0 = -6.797 \pm$
248 0.603) for diffusion normal to (100). Diffusion normal to (001) appears similar, suggesting little
249 anisotropy for He diffusion in monazite. Diffusion in the Brazil monazite, normal to (100) and
250 (010), does not differ significantly from diffusivities measured for the North Carolina monazite,
251 which suggests that differences in trace and minor element compositions of these natural
252 monazites have little effect on He diffusion. These data also reinforce the observations made for
253 the North Carolina monazite of a lack of significant anisotropy for He diffusion.

254 The time series (**Figure 3**) for the North Carolina monazite shows similar diffusivities for
255 experiments at 450°C for durations differing by about an order of magnitude, suggesting that the
256 dominant process being measured is volume diffusion rather than transient effects that might
257 lead to time-dependence of measured diffusivities, and that diffusion behavior is consistent with
258 the assumptions made in the diffusion model. Uncertainties (2σ values shown) are comparatively
259 large for the shortest anneals because of the relatively small amounts of broadening and He loss
260 for the implanted profile for small values of Dt .

261 Fits to the data for the synthetic REE phosphates (for diffusion normal to (100)), over the
262 temperature range 300-550°C (**Figure 2**) yield activation energies of 155 ± 12 , 128 ± 19 , $132 \pm$
263 17 , and 120 ± 12 kJ/mol, and pre-exponential factors of 8.77×10^{-6} ($\log D_0 = -5.057 \pm 0.946$),
264 3.52×10^{-8} ($\log D_0 = -7.454 \pm 1.533$), 2.25×10^{-8} ($\log D_0 = -7.647 \pm 1.336$), 2.89×10^{-9} m²/sec (\log
265 $D_0 = -8.540 \pm 0.920$) for La, Nd, Sm, and Eu phosphates, respectively. He diffusivities are

266 somewhat faster for the lighter REE phosphates, and decrease for the heavier REE phosphates,
267 although activation energies are higher for He diffusion in the lighter REE phosphates.

268 Helium diffusion also appears faster in the synthetic materials than in the natural monazite.
269 While the results for these synthetic REE phosphates are unquestionably of interest in evaluating
270 He transport in monazite-structure materials from a crystal-chemical perspective, it should be
271 emphasized that, given the similarities in He diffusivities for natural monazites containing
272 varying mixtures of rare-earth elements, as well as differences in other minor elements, the
273 Arrhenius relation determined for natural monazite is most relevant for describing He diffusion
274 in monazite in nature.

275

276 **4. Discussion**

277

278 **4.1 Comparison with other He diffusion data**

279

280 Previous studies have measured He diffusion in both natural monazites and synthetic
281 monazite-structure REE phosphates. These data are summarized in [Figure 4](#). Boyce et al. (2005)
282 measured ^4He diffusion in the standard material Monazite 554, from the Santa Catalina
283 Mountains of Arizona, by stepped heating of selected monazite grains. Some variability among
284 the grains was observed, with diffusion parameters reported for the three monazite grains as
285 follows: $E_a = 248 \pm 11$ kJ/mol, $D_o = 3.89 \times 10^3$ m²/sec ($\ln(D_o/a^2) = 27.4$ sec⁻¹) for grain 3, $E_a =$
286 179.6 ± 1.2 kJ/mol, $D_o = 1.29 \times 10^{-5}$ m²/sec ($\ln(D_o/a^2) = 7.66$ sec⁻¹) for grain 4, $E_a = 216.5 \pm 4.9$
287 kJ/mol, and $D_o = 5.86 \times 10^{-4}$ m²/sec ($\ln(D_o/a^2) = 11.32$ sec⁻¹) for grain 5; D_o values were
288 calculated using grain sizes reported in Boyce et al. (2005), assuming that effective diffusion
289 radii (a) are equivalent to grain radii. These data indicate that He diffusivities in grains 3 and 5
290 differ by more than 4 orders of magnitude, which the authors attribute to compositional
291 variations (possibly substitutions of Y and/or Th for Ce) among monazite grains, and the

292 possible effects on He release patterns of internal zoning of U and Th. These trends roughly
293 bracket the Arrhenius relations we have determined for natural monazites and monazite-structure
294 synthetic rare-earth phosphates. In contrast to the findings of Boyce et al. (2005), Farley and
295 Stockli (2002) analyzed multiple aliquots of the 554 monazite and found little intergrain
296 variability in He diffusivities, obtaining consistent activation energies of ~200 kJ/mol and pre-
297 exponential factors of $5.5 \times 10^{-3} \text{ m}^2/\text{sec}$. Since our data suggest little dependence on He diffusion
298 on natural monazite composition, it seems more likely that the variations in He diffusivities
299 observed by Boyce et al. (2005) may be a consequence of nonuniform distributions of He due to
300 internal zoning of U and Th, or possibly due to the presence of subgrain boundaries or other
301 shortcut diffusion paths that could affect He release patterns in the bulk-release experiments of
302 both Boyce et al. (2005) and Farley and Stockli (2002).

303 Farley (2007) measured He diffusion in a series of synthetic REE and Y orthophosphates
304 (grown via a flux method using a Pb pyrophosphate flux) to explore the dependence of He
305 diffusivity on REE phosphate composition. ^3He was introduced into the samples through
306 spallogenic reactions induced by irradiation with energetic protons. ^3He released during stepped
307 heating was measured to determine He diffusivities. For orthophosphates having the monazite
308 structure, Farley (2007) observed systematic increases in activation energy for He diffusion from
309 LaPO_4 - NdPO_4 , with a slight drop in values of activation energy for SmPO_4 and GdPO_4 . The
310 activation energies and pre-exponential factors obtained for each REE phosphate were as
311 follows: La - $183 \pm 7 \text{ kJ/mol}$, $1.82 \times 10^{-3} \text{ m}^2/\text{sec}$; Ce - $196 \pm 7 \text{ kJ/mol}$, $2.00 \times 10^{-2} \text{ m}^2/\text{sec}$; Pr - 206
312 $\pm 7 \text{ kJ/mol}$, $7.35 \times 10^{-2} \text{ m}^2/\text{sec}$; Nd - $224 \pm 8 \text{ kJ/mol}$, $8.96 \times 10^{-1} \text{ m}^2/\text{sec}$; Sm - $215 \pm 8 \text{ kJ/mol}$,
313 $1.22 \times 10^{-3} \text{ m}^2/\text{sec}$; Gd - $198 \pm 7 \text{ kJ/mol}$, $3.33 \times 10^{-5} \text{ m}^2/\text{sec}$. There are sharp differences among He
314 diffusivities in the monazite-structure REE phosphates, with diffusion in GdPO_4 and SmPO_4

315 much slower than diffusion in NdPO_4 , PrPO_4 , CePO_4 and LaPO_4 . Among the latter group, He
316 diffusivities are faster for the lighter REE phosphates (with larger REE ionic radii and a more
317 open crystal structure). Although we observe broadly similar trends of faster diffusivities for the
318 lighter REE phosphates, and the Arrhenius trends of Farley (2007) bracket our data, the
319 differences in He diffusivities we have measured among the monazite-structure REE
320 orthophosphates are less pronounced than those observed by Farley (2007). In addition, we find
321 smaller activation energies (120-155 kJ/mol) than measured in Farley's (2007) study (183-224
322 kJ/mol). However, if we plot all of the diffusion data from Farley's (2007) investigation, we
323 observe that values for diffusivities determined in his study for both La and Nd phosphates are
324 generally consistent with those measured in the present work. Farley's (2007) data for He
325 diffusion in Gd and Sm phosphates approach our Arrhenius trends for Eu and Sm phosphates at
326 high temperatures ($\sim 600^\circ\text{C}$).

327 The reasons for the quantitative differences among the He diffusivities in synthetic REE
328 phosphates measured in our work and that of Farley (2007) are unclear. As noted in the
329 discussion in section 4.3, there may be some anisotropy of diffusion in the end-member synthetic
330 REE phosphates. Since the data from bulk-release experiments reflect contributions of He from
331 the entire mineral grain, He release patterns will incorporate the effects of anisotropy (e.g.,
332 Cherniak and Watson, 2011), in contrast to data from the present study, which profiles He
333 diffusion in a single crystallographic direction. In addition, the synthetic REE phosphates used in
334 the two studies were grown with different fluxes. The REE phosphates used by Farley (2007)
335 were grown with a Pb pyrophosphate flux, while those used in this work were grown with a
336 Na_2CO_3 - MoO_3 flux. Monazite growth in Pb pyrophosphate fluxes may permit heterogenous
337 incorporation of Pb into the crystal lattice (e.g., Donovan et al., 2003) or produce Pb-rich flux

338 inclusions and crystals with evidence of thermomechanical stress (e.g., Boatner, 2002), which
339 could affect diffusivities.

340

341 **4.2. Potential effects of radiation damage on He diffusion**

342

343 Helium diffusion may be influenced by radiation damage produced through the decay of U,

344 Th and their daughter products. Since monazite incorporates these elements, and often in high

345 concentrations (up to ~30 wt% ThO₂, e.g., Overstreet 1967; Boatner and Sales 1988) it may

346 experience changes in diffusion behavior as a consequence of this damage. Several studies

347 indicate that monazite appears relatively resistant to radiation damage effects (e.g., Meldrum et

348 al., 1996; Ewing and Wang, 2002); for example, monazite cannot be amorphized by

349 bombardment with even very high doses of heavy (800 keV Kr⁺) ions at 175°C (Meldrum et al.,

350 1998). Damage from heavy-ion bombardment at lower temperatures is annealed readily during

351 heating for brief times (20 hours) at relatively modest temperatures (300°C) (Meldrum et al.,

352 1996). This suggests that significant accumulation of radiation damage in monazite may not

353 occur under many geological conditions due to self-annealing of radiation-induced defects, as

354 also evidenced by the rarity of observations of metamict monazite in nature (e.g, Ewing et al,

355 1995, Ewing and Wang, 2002; Boatner and Sales, 1988; Seydoux-Guillaume et al., 2004) .

356 Monazite-structure LREE phosphates bombarded with high dose heavy-ion irradiation are also

357 shown to recover rapidly and achieve complete recrystallization under modest doses of electron

358 irradiation (Meldrum et al., 1997a), indicating a strong thermodynamic driving force for

359 recrystallization. Activation energies for recrystallization under irradiation for REE

360 orthophosphates of monazite structure are also significantly lower than those for ABO₄ type

361 silicates (Meldrum et al., 2000). However, although monazite may self-anneal under many

362 conditions in nature, there is some evidence that it does not always achieve complete

363 recrystallization and repair of damage under low-temperature conditions. For example, studies of
364 monazite fission tracks (e.g., Fayon et al., 2011; Gleadow et al. 2002) indicate that tracks may
365 not fully anneal at surface temperatures over geologic timescales. In addition, Peterman et al.
366 (2012) found different dissolution rates for thermally annealed vs. untreated monazite samples,
367 suggesting the presence of radiation damage which is repaired on thermal annealing (e.g.,
368 Seydoux-Guillaume et al., 2002) .

369 In any discussion of radiation damage, it is important to distinguish between various
370 types of radiation damage, both natural and induced (for example, radiation in nature from alpha
371 recoils, fission fragments, and alpha particles, and damage induced through light or heavy ion
372 implantation or neutron irradiation), which may have significantly different effects on materials.
373 In the present study, in which we have implanted light ions at relatively low energies, radiation
374 damage from the ^3He implants is largely restricted to ionization (over 95% of the energy of the
375 implanted ions is dissipated in ionization effects) rather than significant displacement of lattice
376 atoms, as would occur with implantation of heavy ions, so radiation damage effects that might
377 influence diffusion should be minimal (e.g., Tesmer and Nastasi, 1995; Ziegler and Biersack,
378 2006). In addition, as has been noted by Ewing and Wang (2002), the ionization by which alpha
379 particles dissipate most of their energy causes enhanced annealing of alpha recoil damage; this
380 process can be a dominant means of recrystallization recovery, as has been demonstrated for
381 apatite (e.g., Chaumont et al., 2002), and may be the case for monazite as well.

382 Radiation damage (both natural and induced) has been proposed to slow diffusion rates in
383 apatite (Shuster et al., 2006; Shuster and Farley, 2009; Flowers et al, 2009). Shuster et al. (2006)
384 suggest that this is the result of trapping of He in defects, and possibly aggregations of He atoms
385 trapped in the manner of gas bubble inclusions. Models have been developed to attempt to

386 quantify and better understand this behavior (Shuster et al., 2006; Flowers et al., 2009),
387 incorporating the effects of accumulation and annealing of radiation damage. Although these
388 models appear to provide an explanation of apatite (U-Th)/He thermochronometric
389 measurements from a range of samples, several outstanding questions remain. While point- or
390 other localized defects may provide traps for atoms that could limit diffusion rates, extended
391 defects typically created through radiation damage (predominantly alpha recoil, which can cause
392 significant displacement of lattice atoms) would seem more likely to enhance, rather than inhibit,
393 diffusion by providing additional pathways for transport. Displacements of lattice atoms due to
394 alpha recoil effects could alter the distribution of interstitial sites by which He migrates, but it
395 seems there would be little barrier to movement of He out of extended defects if there were
396 available interstitial sites around damaged regions for He exchange and transport. It also is likely
397 in the case of apatite, for which these models have been developed and applied, that significant
398 annealing of defects may occur at modest temperatures, including conditions produced through
399 neutron irradiation used to artificially induce damage (e.g., Shuster and Farley, 2009), which
400 would add complexity to interpretations of He release patterns and estimates of diffusivities. In
401 addition, various observations, including the significantly lower helium diffusivities measured by
402 Shuster and Farley (2009) in synthetic apatite (with no radiation damage) compared with those
403 measured for Durango and other natural fluorapatites that may have sustained natural radiation
404 damage, seem difficult to reconcile with a simple conclusion that radiation damage generally
405 tends to decrease diffusivities. It is important as well to emphasize that, along with the differing
406 effects of different types of radiation, there may be differing effects on different materials
407 depending on the types of bonding in a particular mineral structure and other material

408 characteristics. Models developed, for example, to describe radiation damage effects in apatite,
409 such as those outlined above, may not be directly applicable to other mineral phases.

410 The good agreement between the He diffusion results for the natural monazites in the
411 present work argues against significant effects of radiation damage on diffusion in monazite,
412 since these natural monazites differ widely in Th content, and thus in their likely degree of
413 radiation damage. A possible explanation for the differences between He diffusivities for natural
414 monazites and the synthetic REE phosphates may be compositional differences and their effects
415 on directional porosity, as discussed in the next section.

416

417 **4.3 Causes of variations of He diffusion among REE phosphates, natural monazites, and** 418 **other mineral phases: crystals as directional molecular sieves**

419

420 In previous work (Cherniak and Watson, 2011), we presented the concept of directional
421 permeability to develop insight into why helium diffusivity should vary with lattice direction in
422 some crystals but not in others, and to understand differences in He diffusion rates among
423 different minerals. In the present paper, we extend this concept to evaluate REE phosphates of
424 the monazite structure. These materials differ slightly in their lattice parameters due to
425 differences in ionic radii of the REE, permitting exploration of the effects these differences may
426 have on He diffusivities, with the potential as well to shed light on why diffusivities differ
427 between the end-member synthetic REE phosphates and natural monazite which contain a
428 mixture of REEs along with altrivalent elements substituting for the rare earth elements and
429 phosphorus.

430 Cherniak and Watson (2011) noted that all of the minerals that had been studied in their
431 work on He diffusion (zircon, apatite, rutile and titanite) are highly anisotropic in their atomic
432 structure and symmetry, but only zircon and rutile evidence appreciable diffusive anisotropy for

433 helium. They posited that since He — a small, unpolarized noble-gas atom — interacts
434 minimally with the atoms in a crystal, some insight might be obtained simply by considering the
435 size of a He atom relative to the apertures among lattice ions through which diffusive jumps
436 might occur. This builds upon the concept of ionic porosity previously used to rationalize
437 diffusion of noble gases in minerals (e.g., Dahl, 1996; Farley, 2007), but with the idea that ionic
438 porosity can be a function of lattice orientation in some crystals. The specific criterion proposed
439 by Cherniak and Watson (2011) was that He diffusivity in a given crystallographic direction
440 depends upon the minimum (interstitial) aperture in the most densely packed planar section
441 perpendicular to that direction, as well as the number density (i.e., the number per unit area) of
442 those apertures in that plane. In this respect, the relevant concept might be best described as a
443 sort of directional permeability.

444 Using a similar approach to Cherniak and Watson (2011), we entered ion coordinates for the
445 minerals of interest (acquired from CrystalMaker® software, using the parameters of Ni et al.
446 (1995) for La, Nd, Sm and Eu phosphates) into a computer program written for the purpose of
447 creating sections through the structure at specified coordinates of one crystallographic axis. The
448 program was used to slice through the structures of the REE phosphates in step-wise fashion,
449 creating 2-D images of the inter-ionic space at each step. The slices were then evaluated visually
450 to identify the most restrictive plane in the structure for each unique lattice orientation, and
451 aperture sizes determined. These can then be compared with the commonly accepted size of the
452 He atom ($\sim 1\text{Å}$ radius; e.g., Zhang and Xu, 1995; Zhang et al. 2008). Several salient observations
453 can be made from the results for REE phosphate structures.

454 For monazite-structure REE phosphates, aperture sizes are largest in the $\perp c$ plane, followed
455 by planes $\perp a$, with those $\perp b$ the smallest. There is a systematic variation in aperture size across

456 the series of REE phosphates, with apertures largest in the La phosphate, and smallest in the Sm
457 and Eu phosphates, with the Nd phosphate having intermediate values. This is generally
458 consistent with our He diffusion data for these REE phosphates, where $D_{LaPO_4} > D_{NdPO_4} > D_{SmPO_4}$
459 $\approx D_{EuPO_4}$. In addition, the aperture sizes in different planes differ less in the La phosphate than in
460 the other REE phosphates, with a difference of $\sim 0.11 \text{ \AA}$ between aperture sizes in the $\perp c$ plane
461 and the $\perp b$ plane, compared with $\sim 0.35\text{-}0.37 \text{ \AA}$ for the other REE phosphates. The variations in
462 aperture size suggest the possibility of anisotropy of diffusion, and potentially variations in
463 degrees of anisotropy among the REE phosphates. Unfortunately, we were unable to evaluate
464 anisotropy of diffusion for the synthetic REE phosphates because limitations in crystal
465 dimensions precluded obtaining sections in other orientations of sufficient size for analysis.
466 However, it should be noted, as pointed out in Cherniak and Watson (2011), that both the size
467 and density of the apertures may have effects on diffusivities, so that in some cases, as in titanite,
468 there may be a compensating effect between the number and size of apertures that results in little
469 or no difference in He diffusion along different directions.

470 Diffusivities of He in the synthetic REE are faster than in natural monazite, which may be a
471 consequence of the presence of several different REE with slightly differing ionic radii in the
472 natural materials, as well as substituent atoms such as Th, which may be coupled with other
473 elements to attain charge balance (e.g., Ca on the REE site or Si on the P site). These
474 substitutions of both a range of rare earth elements and other species into the mineral lattice
475 would result in greater variation in the size of apertures in the crystallographic planes, potentially
476 slowing diffusivities and decreasing the likelihood of anisotropy of diffusion when compared
477 with synthetic REE phosphates containing a single REE and no other substituent atoms.

478 Diffusivities of He in the synthetic REE phosphates are roughly bracketed by He
479 diffusivities in titanite and zircon normal to c , with diffusion in LaPO_4 closer to He diffusion in
480 titanite, and diffusion in EuPO_4 closer to that in zircon. Interestingly, the aperture sizes
481 determined for titanite in the $\perp c$ plane (0.89 \AA ; Cherniak and Watson, 2011) is similar to that for
482 the $\perp a$ plane in LaPO_4 (0.90 \AA). For EuPO_4 , the aperture size in this plane is somewhat larger
483 (0.76 \AA) than that for the $\perp a$ plane in zircon (0.67 \AA), so the findings for He diffusion in the REE
484 phosphates appear consistent with the concept of directional permeability influencing He
485 diffusivities.

486

487 **5. Geological implications**

488

489 **5.1 He closure temperatures**

490

491 From our diffusion data, we can calculate mean closure temperatures using the formalism of
492 Dodson (1973; 1986). In [Figure 5a](#) we plot mean closure temperatures for monazite and the
493 synthetic REE phosphate as a function of effective diffusion radius for a cooling rate of
494 $10^\circ\text{C}/\text{Myr}$. Since there is little evidence for anisotropy of diffusion in monazite, we plot curves
495 using spherical geometry and Arrhenius parameters for diffusion normal to (100). For
496 comparison with our findings for natural monazite, we plot closure temperature curves using the
497 Arrhenius relations from [Boyce et al. \(2005\)](#), and [Farley and Stockli \(2002\)](#). Because of the
498 higher activation energy for diffusion measured in these studies – which would lead to
499 comparatively slower diffusivities than those derived from the present work if extrapolated to
500 lower temperatures – closure temperatures calculated with our diffusion parameters will be ~ 20 -
501 30°C lower than those determined from the data of Farley and Stockli (2002), and 5 to 90°C
502 lower than those determined from the data of Boyce et al. (2005) for typical grain sizes for
503 monazites. The closure temperatures are also within a few degrees to $\sim 25^\circ\text{C}$ of values recently

504 reported by Peterman et al. (2011). In **Figure 5b**, we plot closure temperature isotherms,
505 calculated with our diffusion parameters for natural monazite, as a function of cooling rate and
506 grain radii. For typical grain sizes and cooling rates, closure temperatures will range from ~170-
507 210°C.

508 509 **5.2. "Opening" temperatures and diffusive responses of He in monazite to heating events**

510
511 While Dodson's closure temperature concept has long been used to assess the retentivity of
512 diffusing species in minerals, its most significant limitation is that it strictly applies to cooling
513 regimes, and was derived specifically with time-temperature paths where $T \propto 1/t$. However,
514 many geological processes involve heating of mineral grains that are diffusively closed at the
515 onset of heating. This is likely to be the case for He diffusion in accessory minerals, as has been
516 noted by Reiners et al. (2005), who point out that Dodson closure temperatures can serve as
517 "useful shorthand" for representing diffusive retentivity but have "little to no significance" for
518 (re)heating events. Thus, in a prograde thermal regime or over a cycle of heating and cooling, it
519 is necessary instead to consider the question of when and to what extent a mineral grain "opens
520 up" diffusively for the diffusant of interest, rather than when closure "sets in."

521 Retentivity of diffusing species on heating has been considered by Cherniak and Watson
522 (2007), who used both mathematical solutions and numerical simulations to evaluate losses of
523 diffusant on heating from ambient conditions to nominal mean closure temperatures along a
524 linear T-t path. Gardes and Montel (2009) derived equations for diffusive opening and for
525 resetting of geochronological systems, but using a time-temperature path with inverse
526 dependence of time on temperature; this is complementary to the path chosen in Dodson's (1973)
527 derivation but may not be realistic for many geological heating scenarios.

528 More recently, Watson and Cherniak have extended their previous work on prograde
529 diffusion paths to consider both linear and parabolic thermal pulses involving a full heating-
530 cooling cycle (Watson and Cherniak, 2013; Cherniak and Watson, 2012b). Through finite-
531 difference modeling of diffusive exchange, complemented by analytical solutions, they obtained
532 simple expressions that relate the fraction of a diffusing species lost during a thermal event to the
533 duration and peak temperatures of the thermal event, grain radii (a), and diffusion parameters
534 (activation energy and pre-exponential factor) for the species of interest. In all of the examples
535 presented below, spherical geometry of grains is considered (a reasonable assumption given
536 typical dimensions of monazite grains, and the lack of significant anisotropy for He diffusion in
537 natural monazite observed in this work), and samples are assumed to have a uniform initial
538 distribution of diffusant, with no in-growth during the thermal events (which is reasonable given
539 the duration of the heating events considered relative to ^4He production).

540 For a simple case of heating at a constant rate ($T \propto t$) Cherniak and Watson (2012b) and
541 Watson and Cherniak (2013) showed that retention of a diffusing species is accurately described
542 by:

$$543 \quad \log \zeta = -0.457 \left[\frac{E_a}{RT} \right] + \log \left[\frac{E_a D_o}{Ra^2 dT/dt} \right] - 2.3 \quad (3)$$

544 with pre-exponential factor D_o in m^2/sec ; activation energy E_a in J/mol ; dT/dt , the heating rate,
545 in deg/sec ; a in meters; R in $\text{J-deg}^{-1}\text{mol}^{-1}$; and T in Kelvin. ζ , equal to the dimensionless
546 parameter Dt/a^2 , can be directly related to the fraction of diffusant lost (F) from a sphere (Crank,
547 1975):

$$549 \quad F = 1 - \frac{6}{\pi^2} \sum_{n=1}^{\infty} \frac{1}{n^2} \exp(-Dn^2\pi^2t/a^2) \quad (4)$$

550

551 In the case of non-isothermal heating, where diffusivities vary with temperature (and thus time),
552 Dt will represent an integral of the diffusivity over the time of the thermal event, i.e.,:

553
$$\zeta = \frac{1}{a^2} \int_{t=0}^{\tau} D(t) dt \quad (5)$$

554
555 Nonetheless, a specific value of ζ will uniquely determine F .

556 We can use eq. 3 above to evaluate conditions under which several (somewhat arbitrary)
557 criteria are met: "opening", constituting 1% loss of diffusant; the "center retention" criterion,
558 where the center of the mineral grain still retains its initial composition of diffusant (which also
559 corresponds to ~50% loss of diffusant from the entire grain); and "resetting", which constitutes
560 90% loss of diffusant. Values of $\log \zeta$ for these conditions are -5.056, -1.515, and -0.738,
561 respectively. In **Figure 6**, we plot temperature conditions as a function of grain radius for each of
562 these criteria, using a heating rate of 10°C/Myr and the diffusion parameters we have obtained
563 for natural monazite. In the case of 50 μ m radius grains, diffusive opening (1% loss) will occur at
564 114°C, grains will still retain initial He in their centers at temperatures up to 190°C, and 90%
565 loss will be experienced on heating to 212°C. Interestingly, the Dodson closure temperature
566 calculated for He in 50 μ m radius monazite for a cooling rate of 10°C/Myr, is 187°C, very close
567 to the maximum temperature for center retention in the monazite grain. The similarity of these
568 values points out that in prograde thermal regimes, significant losses of diffusant can occur at
569 temperatures well below mean closure temperatures calculated with Dodson's (1973) expression.

570 He retentivity for the case of paths involving both heating and cooling (starting at a low
571 initial temperature, heating to peak temperature, and cooling back to the initial temperature) can
572 also be evaluated (Watson and Cherniak, 2013; Cherniak and Watson, 2012b). An extension of
573 the above linear path including both heating and cooling legs can easily be modeled, but a T-t
574 path following a parabolic trajectory may be a more geologically realistic approximation to

575 thermal histories. Taking a finite-difference modeling approach similar to the above case, but
576 with a parabolic time-temperature path, an expression can be derived relating the dimensionless
577 parameter ζ (and therefore fractional loss of diffusant) to the diffusion parameters for the species
578 of interest, the peak temperature (T_{pk} , in degrees K) and duration (τ , in sec) of the thermal event
579 (time from the start of heating from initial temperature to the return to this temperature), and
580 grain radius (a , in m):

$$581 \quad \log \zeta = \log \left[\frac{D_o \tau}{a^2} \right] + \frac{140}{T_{pk}} - \frac{0.437 E_a}{RT_{pk}} - 0.8 \quad (6)$$

582
583 In Figures 7 and 8, we present a few example calculations using eq. 6 and the He diffusion data
584 for monazite measured in this work. In Figure 7, we plot fractional loss of He as a function of
585 peak temperature for 80 μm monazite grains for a thermal event of 20 Myr duration. Monazite
586 grains experiencing a peak temperature of 193°C will lose about 50% of their original He, with
587 5% and 90% losses for peak temperatures of 140 and 216°C, respectively. Also plotted for
588 comparison is a curve for isothermal heating for the same duration (20 Myr) with T constant at
589 T_{pk} rather than T a parabolic trajectory with time; the fractional losses for this case are calculated
590 with the expression

$$591 \quad \zeta = \left[\frac{D_o \tau}{a^2} \right] \exp \left(\frac{-E_a}{RT_{pk}} \right) \quad (7)$$

592
593 For the isothermal T-t history, helium losses will be greater than for the parabolic path with
594 equivalent peak temperature and duration, because the isothermal case will experience greater
595 time at the highest temperature where diffusional losses are greatest.

596 As an example to illustrate the retentivity of He in monazite grains of various sizes
597 experiencing a thermal history with a parabolic trajectory of heating and cooling, we plot

598 fractional loss of He as a function of grain radii for heating events of 2 Myr and two different
599 peak temperatures: 170°C and 200°C (Figure 8). For a peak temperature of 170°C, 30µm
600 diameter grains would preserve more than 50% of their initial He (and retain initial He
601 concentrations in grain centers). If the peak temperature were 200°C, grains would have to be
602 100µm in diameter to retain this information. Also plotted for comparison are calculations for
603 He loss for isothermal heating events of 2 Myr duration at temperatures of 170°C and 200°C. As
604 noted above, the longer times at elevated temperature in the case of isothermal heating will result
605 in greater He losses. Equivalent He losses to that for the 2 Myr parabolic path with 170°C peak
606 temperature would be obtained for isothermal heating at 155°C, and isothermal heating at
607 ~183°C for equivalence with the parabolic path with 200°C peak temperature.

608 In the above examples, we do not treat cases in which diffusant is produced over time by
609 radioactive decay, or for mineral grains in which initial distributions of diffusing He are non-
610 uniform due to alpha ejection. These cases can be readily addressed with numerical simulations,
611 taking into consideration specific details suitable for modeling of a particular sample and its
612 history, but development of generalized relationships is beyond the scope of the present paper.
613 Nonetheless, as an illustration, we offer an example of the effects of alpha ejection profiles on
614 fractional release of helium from monazite grains of different sizes experiencing thermal
615 histories with different peak temperatures. The model considers a parabolic time-temperature
616 path, with duration τ of 20 Myr. Model calculations are done with two monazite grain radii (40
617 and 80µm, assuming spherical grains) and peak temperatures from 125 to 225°C. The alpha
618 ejection zone is modeled as a rim on the grain of 19µm thickness, with an initial linear gradient
619 of He in this rim, with concentrations ranging from a value of C_0 at a depth of 19µm into the
620 grain to a value of $0.45C_0$ at the grain surface. Depths in the grain greater than 19µm will also

621 have an initial concentration of C_0 . The simulations with no alpha ejection have uniform initial
622 concentrations C_0 of He throughout the grain. In **Figure 9**, fractional losses (F) of He are plotted
623 as a function of time elapsed during the heating event, with simulations incorporating alpha
624 ejection compared with those for grains without ejection profiles for peak temperatures of 150°C
625 (**Figure 9a,c**) and 200°C (**Figure 9b,d**). It is evident that the effects of alpha ejection are most
626 significant for cases of small fractional losses across the T-t path; for example, in the case of
627 80µm radius grains, the absolute differences in F at the end of the parabolic path between the
628 simulations with and without alpha ejection are similar for the two peak temperatures, but the
629 relative differences in F are much larger for the simulation with $T_{pk} = 150^\circ\text{C}$, where F is
630 comparatively small. This is further illustrated in **Figure 10**, where ΔF (the difference between
631 fractional loss with ejection, and without ejection) is plotted as a function of F (without ejection)
632 (**Figure 10a**) and peak temperature T_{pk} (**Figure 10b**). While the values for ΔF do not vary greatly
633 across the range of values of F and T_{pk} (ranging from 0 to -0.08), the relative differences will
634 only be large for smaller values of F. Hence, the effects of alpha ejection on He fractional
635 losses will be small for all but the lowest-temperature thermal events in nature, and effects on
636 laboratory-measured He release patterns would be most pronounced for low-temperature heating
637 steps.

638 639 **5.3 He diffusion in accessory minerals**

640
641 **Figure 11** shows a plot of He diffusion data for natural monazite, obtained in the present
642 study, along with titanite and rutile (Cherniak and Watson, 2011) and apatite and zircon
643 (Cherniak et al., 2009). He diffusion in monazite is slightly slower than He diffusion in zircon
644 normal to c, and falls between diffusion along the [100] and [001] directions in rutile. It is
645 considerably slower than diffusion in titanite and zircon parallel to c. He diffusion in apatite is

646 about five orders of magnitude faster than in monazite. Among this group of accessory minerals,
647 activation energies for He diffusion in monazite, titanite and zircon are similar (~150 kJ/mol)
648 while those for apatite and rutile are somewhat lower (~120 kJ/mol).

649

650 **5.4 Relative retentivity of He among accessory minerals**

651

652 Since we have diffusion data from a range of accessory mineral phases, we can assess the
653 relative retentivity of He in rutile, zircon, titanite apatite and monazite. For these calculations, we
654 use diffusion parameters for natural monazite from the present study, values for He diffusion in
655 zircon and apatite from Cherniak et al. (2009) and Arrhenius parameters for titanite and rutile
656 from Cherniak and Watson (2011). In **Figure 12**, we plot the fraction of He retained by each
657 mineral as a function of time for isothermal heating at 250°C. Spherical geometry (with grain
658 radii of 50 µm for monazite and titanite, 200 µm for apatite [because of the comparatively fast
659 diffusion of He in apatite, a larger grain size is used so that timescales for He loss are closer to
660 those for the other minerals]) and the analytical expression for fraction of diffusant lost from a
661 sphere (Crank, 1975) are used for apatite, monazite and titanite since no anisotropy is observed.
662 For rutile and zircon, cylindrical geometry (with grain radii of 50 µm and lengths of 100 µm) and
663 the CYLMOD code for anisotropic diffusion in a cylinder (Watson et al., 2010) are used to
664 calculate fractional He loss given the anisotropy of diffusion in these minerals (two orders of
665 magnitude difference in D for diffusion parallel and normal to c for both zircon and rutile;
666 Cherniak et al., 2009; Cherniak and Watson, 2011). For grains of roughly equivalent size,
667 monazite would be most retentive of He, followed by rutile, zircon and titanite. Apatite is much
668 less retentive of He (e.g., Cherniak et al., 2009; Farley, 2000) than the other accessory mineral
669 phases.

670

671 **Conclusion**

672

673 He diffusion has been measured in natural monazite and synthetic monazite-structure REE

674 phosphates using ion implantation to introduce ^3He and nuclear reaction analysis to measure ^3He

675 in samples following diffusion anneals. For diffusion in natural monazite we obtain the following

676 Arrhenius relation for diffusion normal to (100):

677

678 $D = 1.60 \times 10^{-7} \exp(-150 \pm 8 \text{ kJ mol}^{-1}/RT) \text{ m}^2\text{sec}^{-1}$.

679

680 Diffusion in natural monazite exhibits little diffusional anisotropy, and diffusivities of He in

681 natural monazites from two different localities are similar. The similarities in He diffusivities for

682 these natural monazites containing different proportions of rare-earth elements, as well as

683 differing Th contents, indicate that this Arrhenius relation is most relevant for describing He

684 diffusion in monazite in nature. Over the investigated temperature range, these diffusivities are

685 similar to those of Farley and Stockli (2002), and values obtained for some measurements of

686 natural monazite crystals by Boyce et al. (2005), and are bracketed by diffusivities obtained by

687 Farley (2007) for monazite-structure synthetic REE phosphates.

688 He diffusion in synthetic REE phosphates (LaPO_4 , NdPO_4 , SmPO_4 and EuPO_4) with the

689 monazite structure appears to behave systematically, with diffusion in the lighter REE

690 phosphates slightly faster than in the heavier REE phosphates. This trend is in broad agreement

691 with the findings of Farley (2007), but the difference in diffusivities among the REE phosphates

692 is smaller than that reported in Farley's (2007) work. Activation energies for He diffusion in the

693 synthetic LREE phosphates are similar to that for natural monazite measured in this study, but

694 He diffusivities in synthetic LaPO_4 are about an order of magnitude faster than in the natural

695 monazites. The differences in He diffusivities among the natural monazites and synthetic REE

696 phosphates may be a consequence of "directional porosity" -- the density and distribution of

697 interstitial apertures in the crystal structure, which may result in differences in He migration
698 rates.

699 The Arrhenius relation determined in this work is used to evaluate He retentivity in
700 monazite experiencing thermal events, using both Dodson's (1973) closure temperature
701 formulation and recently developed expressions (Watson and Cherniak, 2013) for prograde
702 thermal events and heating and cooling trajectories, derived from finite difference modeling and
703 mathematical treatments. The finite difference models developed by Watson and Cherniak
704 (2013) can also be modified to incorporate the effects of alpha ejection; these effects are minor
705 for all cases except in instances of very low-temperature heating and concomitant small He
706 losses. These examples, along with calculations using diffusion parameters determined for He
707 diffusion in other accessory minerals, indicate that monazite is comparatively retentive of He.

708
709

710 *Acknowledgements* – Thanks to Richard Ketchum and an anonymous reviewer for their review
711 comments, which aided significantly in improving the final version of the paper, and to Gregory
712 Dumond for editorial handling. We also thank Greg Dumond and Callum Hetherington for their
713 efforts in organizing the GSA special session on monazite and its companion virtual special issue
714 in American Mineralogist. We thank Michihiko Nakamura, Joe Pyle, and Dan Ruscitto for
715 monazite samples and analyses, and Wayne Skala for assistance with ion implantation. This
716 work was supported by grant EAR-0948204 from the National Science Foundation (to
717 E.B.Watson).

718
719

720 **References**

721

722 Boatner, L.A. and Sales, B.C. (1988) Monazite. In W. Lutze and R.C. Ewing, Eds., Radioactive
723 Waste Forms for the Future, p. 495–564. North Holland, Amsterdam.

724

725 Boyce, J. W., Hodges, K.V., Olszewski, W. J., and Jercinovic, M.J. (2005) He diffusion in
726 monazite; implications for (U-Th)/He thermochronometry. *Geochemistry, Geophysics,*
727 *Geosystems*, 6.

728

729 Chaumont, J., Soulet, S., Krupa, J.C., and Carpena, J. (2002) Competition between disorder
730 creation and annealing in fluorapatite nuclear waste forms. *Journal of Nuclear Materials*, 301,
731 122-128.

732

733 Cherniak, D.J. and Watson, E.B. (2007) Ti diffusion in zircon. *Chemical Geology*, 242, 473-483.

734

735 Cherniak, D.J. and Watson, E.B. (2011) Helium diffusion in rutile and titanite, and consideration
736 of the origin and implications of diffusional anisotropy. *Chemical Geology*, 288, 149-161.

737

738 Cherniak, D.J. and Watson E.B. (2012a) Helium diffusion in olivine at 1 atm and 2.7 GPa.
739 *Geochimica et Cosmochimica Acta*, 84, 269–279.

740

741 Cherniak, D.J. and Watson E.B. (2012b) Diffusion in Minerals Relevant to Geochronology. 22nd
742 V.M. Goldschmidt Conference. Geochemical Society.

743

744 Cherniak, D.J., Watson, E.B., and Thomas, J.B. (2009) He diffusion in zircon and apatite.
745 *Chemical Geology*, 268, 155-166.

746

747 Cherniak, D.J., Watson, E.B., Grove, M., and Harrison, T.M. (2004a) Pb diffusion in monazite:
748 a combined RBS/SIMS study. *Geochimica et Cosmochimica Acta*, 68, 829-840.

749

750 Cherniak, D.J., Zhang, X.Y., Nakamura, M., and Watson, E.B. (2004b) Oxygen diffusion in
751 monazite. *Earth and Planetary Science Letters*, 226, 161-174.

752

753 Cherniak, D.J., Pyle, J., and Rakovan, J. (2004c) Synthesis of REE and Y phosphates by Pb-free
754 flux methods, with utilization as standards for electron microprobe analysis, and in design of
755 monazite chemical U-Th-Pb dating protocol. *American Mineralogist*, 89, 1533-1539.

756

757 Costantini, J.-M., Trocellier, P., Haussy, J., and Grob, J.-J. (2002) Nuclear reaction analysis of
758 helium diffusion in britholite. *Nuclear Instruments and Methods*, B195, 400-407.

759

760 Costantini, J.-M., Grob, J.-J., Haussy, J., Trocellier, P., and Trouslard, P. (2003) Nuclear reaction
761 analysis of helium migration in zirconia. *Journal of Nuclear Materials*, 321, 281-287.

762

763 Crank, J. (1975) *The Mathematics of Diffusion*, 2nd edn. Oxford University Press.

764

- 765 Dahl, P.S. (1996) The effects of composition on retentivity of argon and oxygen in hornblende
766 and related amphiboles: a field-tested empirical model. *Geochimica et Cosmochimica Acta*, 60,
767 3687-3700.
- 768 Dieumegard, D., Dubreuil, D., and Amsel, G. (1979) Analysis and depth profiling of deuterium
769 with the $D(^3\text{He,p})^4\text{He}$ reaction by detecting the protons at backward angles. *Nuclear Instruments*
770 *and Methods*, 166, 431-445.
- 771
772 Dodson, M.H. (1973) Closure temperatures in cooling geological and petrological systems.
773 *Contributions to Mineralogy and Petrology*, 40, 259-274.
- 774
775 Dodson, M.H. (1986) Closure profiles in cooling systems. *Materials Science Forum*, 7, 145-154.
- 776
777 Donovan, J.J., Hanchar, J.M., Picolli, P.M., Schrier, M.D., Boatner, L.A. and Jarosewich, E.
778 (2003) A re-examination of the rare-earth-element orthophosphate standards in use for electron-
779 microprobe analysis. *Canadian Mineralogist*, 41, 221-232.
- 780
781 Ehlers, T. A. and Farley, K. A. (2003) Apatite (U-Th)/He thermochronometry; methods and
782 applications to problems in tectonic and surface processes. *Earth and Planetary Science Letters*,
783 206, 1-14.
- 784
785 Ewing, R. C. and Wang, L.-M. (2002) Phosphates as nuclear waste forms. In M.J. Kohn, J.
786 Rakovan, J.M. Hughes, Eds., *Phosphates: geochemical, geobiological, and materials importance*.
787 *Reviews in Mineralogy and Geochemistry*, Vol. 48, pp.673-699. Mineralogical Society of
788 America and Geochemical Society.
- 789
790 Ewing, R.C., Weber, W.J., and Clinard, F.W. Jr. (1995) Radiation effects in nuclear waste forms
791 for high-level radioactive waste. *Progress in Nuclear Energy*, 29, 63-127.
- 792
793 Farley, K.A. (2002) (U-Th)/He dating: Techniques, calibrations and applications. In D. Porcelli,
794 C.J. Ballentine, and R. Wieler, Eds., *Noble Gases in Geochemistry and Cosmochemistry*,
795 *Reviews in Mineralogy and Geochemistry*, Vol. 47, pp. 819-844. Mineralogical Society of
796 America and Geochemical Society.
- 797
798 Farley, K.A. (2000) Helium diffusion from apatite: General behavior as illustrated by Durango
799 fluorapatite. *Journal of Geophysical Research*, 105, 2903-2914.
- 800
801 Farley, K.A. (2007) He diffusion systematics in minerals: Evidence from synthetic monazite and
802 zircon structure phosphates. *Geochimica et Cosmochimica Acta*, 71, 4015-4024.
- 803
804 Farley, K.A. and Stockli, D.F., 2002. (U-Th)/He dating of phosphates: apatite, monazite, and
805 xenotime. In D. Porcelli, C.J. Ballentine, R. Wieler, Eds., *Noble Gases in Geochemistry and*
806 *Cosmochemistry, Reviews in Mineralogy and Geochemistry*, Vol. 47, pp. 559-577.
807 Mineralogical Society of America and Geochemical Society.

- 808 Fayon, A., Gombosi, D. J., and Ruscitto, D. (2011) Fission track dating of monazite; etching
809 efficiencies as a function of U content. Abstracts with Programs - Geological Society of America
810 Annual Meeting, 43, 331.
811
- 812 Flowers, R.M., Ketcham, R.A., Shuster, D.L., and Farley, K.A. (2009) Apatite (U-Th)/He
813 thermochronometry using a radiation damage accumulation and annealing model. *Geochimica et*
814 *Cosmochimica Acta*, 73, 2347-2365.
815
- 816 Gardes, E., and Montel, J.-M. (2009) Opening and resetting temperatures in heating
817 geochronological systems. *Contributions to Mineralogy and Petrology*, 158, 185-195.
818
- 819 Gleadow, A.J.W., Belton, D.X., Kohn, B.P., and Brown, R.W. (2002) Fission track dating of
820 phosphate minerals and the thermochronology of apatite. *Reviews in Mineralogy and*
821 *Geochemistry*, 48: 579-630.
822
- 823 Gosset, D., Trocellier, P., and Serruys, Y. (2002) Determination of the helium diffusion
824 coefficient in nuclear waste, storage ceramics by a nuclear reaction analysis method. *Journal of*
825 *Nuclear Materials*, 303, 115-124.
826
- 827 Gosset, D. and Trocellier, P. (2005) Determination of the helium thermal diffusion coefficient in
828 britholite using a NRA method: new results. *Journal of Nuclear Materials*, 336, 140-144.
829
- 830 Hodges, K., van Soest, M. C., Monteleone, B. D., and Boyce, J. W. (2009) Direct evidence for
831 anisotropic He diffusivity in zircon provided by laser depth profiling. AGU Fall Meeting 2009,
832 abstract #V52C-04
833
- 834 House, M.A., Wernicke, B.P., and Farley, K.A. (1998) Dating topography of the Sierra Nevada,
835 California, using apatite (U-Th)/He ages. *Nature*, 396, 66-69.
836
- 837 House, M. A., Wernicke, B. P., Farley, K. A., and Dumitru, T. A. (1997) Cenozoic thermal
838 evolution of the central Sierra Nevada, California, from (U-Th)/He thermochronometry. *Earth*
839 *and Planetary Science Letters*, 151, 167-179.
840
- 841 Ketcham, R.A., Guenther, W.R., and Reiners, P.W. (2013) Geometric analysis of radiation
842 damage connectivity in zircon, and its implications for helium diffusion. *American Mineralogist*,
843 98, 350-360.
844
- 845 Kohn, M. and Malloy, M. A. (2004) Formation of monazite via prograde metamorphic reactions
846 among common silicates; implications for age determinations. *Geochimica et Cosmochimica*
847 *Acta*, 68, 101-113.
848
- 849 Mayer, M., Alimov, V.K., and Roth, J. (2005) Differential cross-section of the $D(^3\text{He,p})^4\text{He}$
850 nuclear reaction and depth profiling of deuterium up to large depths. *Nuclear Instruments and*
851 *Methods*, B234, 169-175.
852

- 853 Meldrum, A., Wang, L.M., and Ewing, R.C. (1996) Ion beam induced amorphization of
854 monazite. *Nuclear Instruments and Methods*, B116, 220-224.
855
- 856 Meldrum, A., Boatner, L.A., and Ewing, R.C. (1997b) Displacive radiation effects in the
857 monazite- and zircon-structure orthophosphates. *Physical Review*, B56, 13805-13814.
858
- 859 Meldrum, A., Boatner, L.A., and Ewing, R.C. (1997a) Electron-irradiation-induced nucleation
860 and growth in amorphous LaPO₄, ScPO₄, and zircon. *Journal of Materials Science*, 12, 1816-
861 1827.
862
- 863 Meldrum, A., Boatner, L.A., Weber, W.J., and Ewing, R.C. (1998) Radiation damage in zircon
864 and monazite. *Geochimica et Cosmochimica Acta*, 62, 2509-2520.
865
- 866 Meldrum, A., Boatner, L.A., and Ewing, R.C. (2000) A comparison of radiation effects in
867 crystalline ABO₄-type phosphates and silicates. *Mineralogical Magazine*, 64, 185-194.
868
- 869 Miro, S., Studer, F., Costantini, J.-M., Haussy, J., Trouslard, P., and Grob, J.-J. (2006) Effect of
870 composition on helium diffusion in fluoroapatites investigated with nuclear reaction analysis.
871 *Journal of Nuclear Materials*, 355, 1-9.
872
- 873 Miro, S., Studer, F., Costantini, J.-M., Berger, P., Haussy, J., Trouslard, P., and Grob, J.-J.
874 (2007) Effect of gold ion irradiation on helium migration in fluorapatites investigated with
875 nuclear reaction analysis. *Journal of Nuclear Materials*, 362, 445-450.
876
- 877 Möller, W. and Besenbacher, F. (1980) A note on the ³He+D nuclear-reaction cross section.
878 *Nuclear Instruments and Methods*, 168, 111-114.
879
- 880 Ni, Y., Hughes, J.M., and Mariano, A.N. (1995) Crystal chemistry of the monazite and xenotime
881 structures. *American Mineralogist*, 80, 21-26.
882
- 883 Ouchani, S., Dran, J.-C., and Chaumont, J. (1998) Exfoliation and diffusion following helium ion
884 implantation in fluorapatite: implications for radiochronology and radioactive waste disposal.
885 *Applied Geochemistry*, 13, 707-714.
886
- 887 Overstreet, W.C. (1967) The geologic occurrence of monazite. US Geological Survey
888 Professional Paper, 530, 327 p.
889
- 890 Paszti, F. (1992) Microanalysis of He using charged particle accelerators. *Nuclear Instruments*
891 *and Methods*, B66, 83-106.
892
- 893 Payne, R.S., Clough, A.S., Murphy, P., and Mills, P.J. (1989) Use of the D(³He,p)⁴He reaction to
894 study polymer diffusion in polymer melts. *Nuclear Instruments and Methods*, B42, 130-134.
895
- 896 Peterman, E.M., Grove, M., and Hourigan, J. (2011) Development and intercalibration of
897 monazite (U-Th)/ He thermochronology: Catnip Sill, Catalina Core Complex. Paper #130-11,
898 2011 GSA Annual Meeting

- 899
900 Peterman, E.M., Mattinson, J.M., and Hacker, B.R. (2012) Multi-step TIMS and CA-TIMS
901 monazite U–Pb geochronology. *Chemical Geology* 312–313, 58–73
902
903 Pronko, P.P. and Pronko, J.G. (1974) Depth profiling of ^3He and ^2H in solids using the
904 $^3\text{He}(d,p)^4\text{He}$ resonance. *Physical Review*, B9, 2670-2678.
905
906 Pyle, J.M., Spear, F.S., Rudnick, R.L., McDonough, W. F. (2001) Monazite-xenotime-garnet
907 equilibrium in metapelites and a new monazite-garnet thermometer. *Journal of Petrology*, 42,
908 2083-2107.
909
910 Reiners, P.W. and Farley, K.A. (2001) Influence of crystal size on apatite (U-Th)/He
911 thermochronology: an example from the Bighorn Mountains, Wyoming. *Earth and Planetary
912 Science Letters*, 188, 413-420.
913
914 Reiners, P.W., Brady, R., Farley, K. A., Fryxell, J. E., Wernicke, B., and Lux, D. (2000) Helium
915 and argon thermochronometry of the Gold Butte Block, South Virgin Mountains, Nevada. *Earth
916 and Planetary Science Letters*, 178, 315-326.
917
918 Reiners, P.W., Farley, K. A., and Hickey, H. J. (2002) He diffusion and (U-Th)/He
919 thermochronometry of zircon; initial results from Fish Canyon Tuff and Gold Butte.
920 *Tectonophysics*, 349, 297-308.
921
922 Reiners, P.W., Spell, T. L., Nicolescu, S., and Zanetti, K. A. (2004) Zircon (U-Th)/He
923 thermochronometry; He diffusion and comparisons with $^{40}\text{Ar}/^{39}\text{Ar}$ dating. *Geochimica et
924 Cosmochimica Acta*, 68, 1857-1887.
925
926 Reiners, P.W., Ehlers, T.A., and Zeitler, P.K. (2005) Past, present, and future of
927 thermochronology. In: P.W. Reiners, P.W. and T.A. Ehlers, Eds., *Low-temperature
928 Thermochronology: Techniques, Interpretations, and Applications. Reviews in Mineralogy and
929 Geochemistry*, Vol. 58, pp.1-18. Mineralogical Society of America and Geochemical Society,
930 Washington, DC.
931
932 Roselieb, K., Rauch, F., Dersch, O., and Buttner, H. (2006) Diffusivity and solubility of He in
933 garnet: An exploratory study using nuclear reaction analysis. *Nuclear Instruments and Methods*,
934 B244, 412-418.
935
936 Ryssel, H. and Ruge, I. (1986) *Ion Implantation*. John Wiley, New York.
937
938 Seydoux-Guillaume, A.-M., Wirth, R., Deutsch, A., and Schärer, U. (2004) Microstructure of 24-
939 1928 Ma concordant monazites; implications for geochronology and nuclear waste deposits.
940 *Geochimica et Cosmochimica Acta*, 68, 2517-2527.
941
942 Seydoux-Guillaume, A.-M, Wirth, R., Nasdala, L., Gottschalk, M., Montel, J.N, and Heinrich,
943 W. (2002) XRD, TEM and Raman study of experimental annealing of natural monazite.
944 *Physics and Chemistry of Minerals*, 29, 240–253.

- 945
946 Shannon, R.D. (1976) Revised effective ionic radii and systematic studies of interatomic
947 distances in halides and chalcogenides. *Acta Crystallographica*, A32, 751-767.
948
949 Shannon, R.D. and Prewitt, C.T. (1969) Effective ionic radii in oxides and fluorides. *Acta*
950 *Crystallographica*, B 25, 925-946.
951
952 Shuster, D. L. and Farley, K. A. (2009) The influence of artificial radiation damage and thermal
953 annealing on helium diffusion kinetics in apatite. *Geochimica et Cosmochimica Acta*, 73, 183-
954 196.
955
956 Shuster, D. L. and Farley, K. A. (2005a) $^4\text{He}/^3\text{He}$ thermochronometry; theory, practice, and
957 potential complications. In P.W. Reiners, T.A. Ehlers, Eds., *Low-temperature*
958 *Thermochronology: Techniques, Interpretations, and Applications*. Reviews in Mineralogy and
959 *Geochemistry*, Vol. 58, pp.181-203. Mineralogical Society of America and Geochemical
960 Society, Washington, DC.
961
962 Shuster, D.L. and Farley, K.A. (2005b) Diffusion kinetics of proton-induced Ne-21, He-3, and
963 He-4 in quartz. *Geochimica et Cosmochimica Acta*, 69, 2349-2359.
964
965 Shuster, D.L. and Farley, K.A. (2004) $^4\text{He}/^3\text{He}$ thermochronometry, *Earth and Planetary*
966 *Science Letters*, 217, 1-17.
967
968 Shuster, D.L., Farley, K.A., Sistierson, J.M., and Burnett, D.S. (2004) Quantifying the diffusion
969 kinetics and spatial distribution of radiogenic ^4He in minerals containing proton-induced ^3He .
970 *Earth and Planetary Science Letters*, 217, 19-32.
971
972 Shuster, D.L., Flowers, R.M., and Farley, K.A. (2006) The influence of natural radiation damage
973 on helium diffusion kinetics in apatite. *Earth and Planetary Science Letters*, 249, 148-161.
974
975 Stockli, D.F. (2005) Application of low-temperature thermochronometry to extensional tectonic
976 settings. In P.W. Reiners and T.A. Ehlers, Eds., *Low-temperature Thermochronology:*
977 *Techniques, Interpretations, and Applications*. Reviews in Mineralogy and Geochemistry, Vol.
978 58, pp.411-448. Mineralogical Society of America and Geochemical Society, Washington, DC.
979
980 Stockli, D. F., Farley, K. A., Walker, J. D., and Blackburn, T. J. (2005) He diffusion and (U-
981 Th)/He thermochronometry of monazite and rutile. *Geochimica et Cosmochimica Acta*, 69, Issue
982 10, Suppl. 8
983
984 Tesmer, J.R. and Nastasi, M. (1995) *Handbook of Modern Ion Beam Materials Analysis*.
985 Materials Research Society, Pittsburgh, PA.
986
987 Trocellier, P., Gosset, D., Simeone, D., Costantini, J.M., Deschanel, X., Roudil, D., Serruys,
988 Y., Grynszpan, R., Saudé, S., and Beauvy, M. (2003a) Application of nuclear reaction geometry
989 for ^3He depth profiling in nuclear ceramics. *Nuclear Instruments and Methods*, B206, 1077-1082.
990

- 991 Trocellier, P., Gosset, D., Simeone, D., Costantini, J.-M., Deschanel, X., Roudil, D., Serruys,
992 Y., Grynszpan, R., Saudé, S., and Beauvy, M. (2003b) ^3He thermal diffusion coefficient
993 measurement in crystalline ceramics by μNRA depth profiling. Nuclear Instruments and
994 Methods, B210, 507-512.
995
996 van Soest, M., Monteleone, B.D., Hodges, K.V., and Boyce, J.W. (2011) Laser depth profiling
997 studies of helium diffusion in Durango fluorapatite. Geochimica et Cosmochimica Acta, 75,
998 2409-2419.
999
1000 Watson, E.B. and Cherniak D.J. (2013) Simple equations for diffusion in response to heating.
1001 Chemical Geology, 355, 93-104.
1002
1003 Watson, E.B., Wanser, K.H., and Farley, K.A. (2010) Anisotropic diffusion in a finite cylinder,
1004 with geochemical applications. Geochimica et Cosmochimica Acta, 74, 614-633.
1005
1006 Wolf, R.W., Farley, K.A., and Kass, D.M. (1998) Modeling of the temperature sensitivity of the
1007 apatite (U-Th)/He thermochronometer. Chemical Geology, 148, 105-114.
1008
1009 Wolf, R.W., Farley, K.A., and Silver, L.T. (1996) Assessment of (U-Th)-He thermochronometry:
1010 The low-temperature history of the San Jacinto Mountains, California. Geology, 25, 65-68.
1011
1012 Yang, P. and Pattison, D. (2006) Genesis of monazite and Y zoning in garnet from the Black
1013 Hills, South Dakota. Lithos, 88, 233-253.
1014
1015 Zhang, L., Van Orman, J.A., and Lacks, D.J. (2008) Effective radii of noble gas atoms in
1016 silicates from first-principles molecular simulation. American Mineralogist, 94, 600-608.
1017
1018 Zhang, Y. and Xu, Z. (1995) Atomic radii of noble gas elements in condensed phases. American
1019 Mineralogist, 80, 670-675.
1020
1021 Ziegler, J.F. and Biersack, J.P. (2006) The stopping and range of ions in matter. Computer code
1022 SRIM 2006, <http://www.srim.org>.
1023

1024 **Table 1. Compositional analysis of natural monazites used**
1025 **in this study.**

	North Carolina monazite	Brazil monazite
P ₂ O ₅	30.40 (0.34)	27.74 (0.21)
SiO ₂	0.40 (0.17)	1.53 (0.06)
CaO	0.18 (0.17)	0.52 (0.02)
PbO	0.03 (0.02)	0.23 (0.02)
ThO ₂	1.28 (1.24)	7.66 (0.41)
UO ₂	0.10 (0.04)	0.29 (0.07)
Y ₂ O ₃	0.74 (0.16)	0.45 (0.01)
La ₂ O ₃	15.22 (0.96)	14.40 (0.17)
Ce ₂ O ₃	31.12 (1.03)	29.26 (0.44)
Pr ₂ O ₃	4.05 (0.99)	5.05 (0.08)
Nd ₂ O ₃	12.33 (0.79)	10.34 (0.18)
Sm ₂ O ₃	2.19 (0.44)	2.19 (0.05)
Gd ₂ O ₃	1.46 (0.42)	0.89 (0.04)
Tb ₂ O ₃	0.12 (0.04)	0.03 (0.03)
Dy ₂ O ₃	0.36 (0.06)	0.23 (0.02)
Er ₂ O ₃	0.03 (0.02)	0.01 (0.01)
Total	100.01	100.83

1026 Measurements are wt% oxides, by electron microprobe, with
1027 multiple (7-10) point analyses of grains. Standard deviations
1028 are in parentheses.

1029

1030

1031

1032 Table 2. ^3He Diffusion in Natural Monazite

	$T(^{\circ}\text{C})$	time(sec)	$D(\text{m}^2\text{sec}^{-1})$	log D	+/-
1033	<i>North Carolina Monazite (100):</i>				
	He3EMZ-9	600	1.80×10^3	1.17×10^{-17}	-15.93 0.34
	He3EMZ-3	549	1.80×10^3	2.74×10^{-17}	-16.56 0.36
	He3EMZ-4	500	4.20×10^3	1.69×10^{-17}	-16.77 0.18
	He3EMZ-5	452	1.08×10^4	3.81×10^{-18}	-17.42 0.28
	He3EMZ-6	452	4.50×10^3	4.64×10^{-18}	-17.33 0.44
	He3EMZ-8	454	4.68×10^4	1.91×10^{-18}	-17.72 0.12
	He3EMZ-1	401	7.56×10^4	6.22×10^{-19}	-18.21 0.35
	He3EMZ-7	354	5.08×10^5	5.91×10^{-20}	-19.23 0.31
	He3EMZ-2	317	3.63×10^6	6.01×10^{-21}	-20.22 0.27
1034	<i>North Carolina Monazite (001):</i>				
	He3EMZ-15	550	1.20×10^3	6.90×10^{-17}	-16.16 0.32
	He3EMZ-11	498	4.50×10^3	6.69×10^{-18}	-17.17 0.44
	He3EMZ-10	446	2.52×10^4	1.98×10^{-18}	-17.70 0.35
	He3EMZ-12	402	1.60×10^5	4.68×10^{-19}	-18.33 0.30
	He3EMZ-13	352	1.28×10^6	5.12×10^{-20}	-19.29 0.43
1035	<i>Brazil Monazite (010):</i>				
	He3BrMz-5	550	1.20×10^3	3.42×10^{-17}	-16.47 0.19
	He3BrMz-2	498	4.50×10^3	1.68×10^{-17}	-16.78 0.10
	He3BrMz-1	446	2.52×10^4	2.64×10^{-18}	-17.58 0.15
	He3BrMz-3	402	1.60×10^5	5.37×10^{-19}	-18.27 0.11
	He3BrMz-4	352	1.28×10^6	2.36×10^{-20}	-19.63 0.35
1036	<i>Brazil Monazite (100):</i>				
	He3BrMz-11	550	1.20×10^3	5.95×10^{-17}	-16.23 0.23
	He3BrMz-6	501	5.40×10^3	8.54×10^{-18}	-17.07 0.16
	He3BrMz-7	453	2.64×10^4	1.78×10^{-18}	-17.75 0.08
	He3BrMz-10	395	2.36×10^5	2.87×10^{-19}	-18.54 0.22
	He3BrMz-8	346	1.29×10^6	2.82×10^{-20}	-19.55 0.20

1037

1038

1039

1040 Table 3. ^3He Diffusion in Synthetic REE Phosphates

	$T(^{\circ}\text{C})$	$time(sec)$	$D(m^2sec^{-1})$	$\log D$	+/-
1041	<i>LaPO₄:</i>				
	He3LaPO4-3	501	9.00×10^2	3.38×10^{-16}	-15.51 0.21
	He3LaPO4-4	450	1.50×10^3	7.98×10^{-17}	-16.26 0.26
	He3LaPO4-1	403	1.73×10^5	5.13×10^{-18}	-17.29 0.31
	He3LaPO4-2	357	8.64×10^4	1.48×10^{-18}	-17.83 0.27
	He3LaPO4-5	300	6.91×10^5	5.86×10^{-20}	-19.23 0.22
1042	<i>NdPO₄:</i>				
	He3NdPO4-3	501	9.00×10^2	1.01×10^{-16}	-16.00 0.41
	He3NdPO4-4	450	1.50×10^3	2.65×10^{-17}	-16.58 0.41
	He3NdPO4-1	404	1.73×10^5	2.67×10^{-18}	-17.57 0.25
	He3NdPO4-2	350	6.48×10^4	9.03×10^{-19}	-18.04 0.27
	He3NdPO4-5	299	9.65×10^5	6.19×10^{-20}	-19.21 0.34
1043	<i>SmPO₄:</i>				
	He3SmPO4-3	501	1.20×10^3	3.16×10^{-17}	-16.50 0.35
	He3SmPO4-4	450	5.40×10^3	8.13×10^{-18}	-17.09 0.34
	He3SmPO4-1	403	1.73×10^5	9.46×10^{-19}	-18.02 0.29
	He3SmPO4-2	350	3.46×10^5	2.16×10^{-19}	-18.67 0.28
	He3SmPO4-5	299	9.65×10^5	2.14×10^{-20}	-19.67 0.29
1044	<i>EuPO₄:</i>				
	He3EuPO4-3	501	1.20×10^3	2.58×10^{-17}	-16.59 0.24
	He3EuPO4-4	450	3.30×10^3	6.30×10^{-18}	-17.20 0.22
	He3EuPO4-1	403	1.73×10^5	1.15×10^{-18}	-17.94 0.29
	He3EuPO4-2	357	8.64×10^4	2.88×10^{-19}	-18.54 0.36
	He3EuPO4-5	300	6.91×10^5	3.59×10^{-20}	-19.45 0.19

1045

1046

1047 **Captions for Figures**

1048

1049

1050 **Figure 1.** Arrhenius plot for helium diffusion in natural monazite. From a fit to the data for
1051 diffusion for the North Carolina monazite (diffusion normal to (100)) (black circles) an
1052 activation energy of 150 ± 8 kJ/mol and pre-exponential factor (D_0) of 1.60×10^{-7} m²/sec ($\log D_0$
1053 = -6.797 ± 0.603) are obtained. Diffusion the North Carolina monazite normal to (001) (grey
1054 circles) appears similar, as are data for diffusion in another natural monazite for diffusion normal
1055 to (100) and (010) (white and grey squares, respectively), suggesting little dependence on
1056 crystallographic orientation for He diffusion in monazite.

1057

1058 **Figure 2.** Arrhenius plot for helium diffusion in synthetic REE phosphates. Fits to the data for
1059 the synthetic REE phosphates (for diffusion normal to (100)), over the temperature range 300-
1060 550°C yield activation energies of 155 ± 12 , 128 ± 19 , 132 ± 17 , and 120 ± 12 kJ/mol, and pre-
1061 exponential factors of 8.77×10^{-6} ($\log D_0 = -5.057 \pm 0.946$), 3.52×10^{-8} ($\log D_0 = -7.454 \pm 1.533$),
1062 2.25×10^{-8} ($\log D_0 = -7.647 \pm 1.336$), 2.89×10^{-9} m²/sec ($\log D_0 = -8.540 \pm 0.920$) for La, Nd, Sm,
1063 and Eu phosphates, respectively.

1064

1065 **Figure 3.** Time series for He diffusion in natural monazite. He diffusivities are within
1066 experimental uncertainty for diffusion anneals of durations ranging over an order of magnitude at
1067 450°C, suggesting that volume diffusion of He is the dominant process being measured. Also
1068 evident are the similarities in diffusivities for natural monazites from different localities, and for
1069 different crystallographic orientations.

1070

1071 **Figure 4a.** Summary of measurements of diffusion of He in natural monazite, comparing the
1072 findings from the present study with reported Arrhenius relations from step-heating experiments
1073 of Farley and Stockli (2002) and Boyce et al. (2005) for the 554 Monazite from the Santa
1074 Catalina Mountains of Arizona, by stepped heating of selected monazite grains. Boyce et al.
1075 (2005) observe some variability among the grains they studied (numbered #3, #4 and #5), with
1076 He diffusivities differing by more than 4 orders of magnitude; these trends roughly bracket our
1077 Arrhenius relation for natural monazites. In contrast, Farley and Stockli (2002) analyzed
1078 multiple aliquots of the 554 monazite and found little intergrain variability in He diffusivities;
1079 their diffusivities are faster than those obtained in the present study, but with a higher activation
1080 energy for diffusion.

1081 **Figure 4b.** Summary of measurements for He diffusion in synthetic REE phosphates of monazite
1082 structure, comparing data from the present study with results from the stepped heating studies of
1083 Farley (2007) (lines indicated by (F) in figure). Farley (2007) finds sharp differences among He
1084 diffusivities in the monazite-structure REE phosphates, with diffusion in GdPO_4 and SmPO_4
1085 much slower than diffusion in NdPO_4 and LaPO_4 . Among the latter group, He diffusivities are
1086 faster for the lighter REE phosphates (with larger REE ionic radii and a more open crystal
1087 structure). Although we find broadly similar trends of faster diffusivities for the lighter REE
1088 phosphates, the differences are less pronounced than those observed by Farley (2007).

1089
1090 **Figure 5.** Mean closure temperatures for monazite and synthetic monazite-structure
1091 orthophosphates as a function of effective diffusion radius for a cooling rate of $10^\circ\text{C}/\text{Myr}$, using
1092 the expression of Dodson (1973). In (a), we plot curves using spherical geometry and Arrhenius
1093 parameters obtained in this study for natural monazite normal to (100). For comparison, closure
1094 temperature estimates for monazite from Boyce et al. (2005) (using their Arrhenius relations for

1095 grains #3, #4 and #5, plotted in the previous figure) and Farley and Stockli (2002) are shown. In
1096 (b), we plot closure temperature isotherms, calculated with our diffusion parameters for natural
1097 monazite, as a function of cooling rate and grain radii. For typical grain sizes and cooling rates,
1098 closure temperatures will range from ~170-210°C.

1099

1100 **Figure 6.** Diffusive “opening”, “resetting” and “center retention” criteria for helium in monazite
1101 grains heated at a linear rate of 10°C/Myr, calculated using eq.3. Conditions for “opening” (1%
1102 loss of diffusant); "center retention" criterion (where the center of the mineral grain still retains
1103 its initial concentration of diffusant); and "resetting" (90% loss of diffusant) are plotted as a
1104 function of maximum heating temperature and grain radius. In the case of 50µm radius grains,
1105 diffusive opening will occur at 114°C, grains will still retain initial He in their centers at
1106 temperatures up to 190°C, and resetting will be experienced at 212°C. See text for additional
1107 discussion.

1108

1109 **Figure 7.** Plot of fractional loss of He as a function of peak temperature for 80 µm grains for a
1110 thermal event of 20 Myr duration and parabolic trajectory, calculated using eq. 6. Monazite
1111 grains experiencing a peak temperature of 193°C will lose about 50% of their original He, with
1112 5% and 90% losses for peak temperatures of 140 and 216°C, respectively. Also plotted for
1113 comparison is a curve for isothermal heating for the same duration (20 Myr) with temperature
1114 constant at T_{pk} rather than following a parabolic trajectory with time. Helium losses will be
1115 greater for the isothermal T-t history than for the parabolic path with the same peak temperature
1116 and duration, because the isothermal example will experience a longer time at the highest
1117 temperature where diffusional losses are greatest.

1118 **Figure 8.** Plot of fractional loss of He as a function of grain radii for heating events of 2 Myr and
1119 two different peak temperatures (170°C and 200°C), illustrating the retentivity of He in monazite
1120 grains of various sizes when experiencing a parabolic trajectory of heating and cooling. For a
1121 peak temperature of 170°C, 30µm diameter grains would preserve more than 50% of their initial
1122 He (and retain initial He concentrations in grain centers), while grains of 100µm diameter would
1123 experience equivalent retention for peak temperatures of 200°C. Curves are calculated using eq.
1124 6 and diffusion parameters for He in natural monazite measured in this study. Also plotted for
1125 comparison are calculations for He loss for isothermal heating events of 2 Myr duration at
1126 temperatures of 170°C and 200°C (dashed lines). Because of the longer times at elevated
1127 temperatures for the case of isothermal heating, He losses will be greater.

1128

1129 **Figure 9.** Plots of fractional loss of He for 40µm (a,b) and 80µm (c,d) monazite grains,
1130 comparing He losses for grains modeled with and without the effects of alpha ejection. A
1131 parabolic T-t path of 20 Myr duration is used in the models, with peak temperatures of 150 (a,c)
1132 and 200 (b,d). The effects of alpha ejection are most pronounced for T-t paths with small
1133 fractional losses of He. See text for additional discussion.

1134

1135 **Figure 10.** Plot of ΔF (the difference between fractional loss with ejection, and without ejection)
1136 as a function of F (without ejection) (a) and peak temperature T_{pk} (b). While the values for ΔF
1137 do not vary greatly across the range of values of F and T_{pk} , the relative differences will only be
1138 large for smaller values of F. Hence, the effects of alpha ejection on He fractional losses will
1139 only be significant for very low-temperature thermal events in nature, and effects on laboratory-

1140 measured He release patterns would be most pronounced for low-temperature heating steps. See
1141 text for further discussion.

1142

1143 **Figure 11.** Comparison of He diffusion in natural monazite, apatite, zircon, titanite and rutile.
1144 Sources for data: monazite – this study; apatite and zircon – Cherniak et al. (2009); rutile and
1145 titanite – Cherniak and Watson (2011). He diffusion in monazite is slightly slower than He
1146 diffusion in zircon normal to c, and falls roughly between diffusion along [100] and [001] in
1147 rutile. Helium diffusion in titanite, and rutile along [001] are comparable, while He diffusion in
1148 titanite is intermediate between diffusion in zircon normal and parallel to c. He diffusion in
1149 apatite is about five orders of magnitude faster than in monazite. Among this group of accessory
1150 minerals, activation energies for He diffusion in monazite, titanite and zircon are similar (~150
1151 kJ/mol) while those for apatite and rutile are somewhat lower (~120 kJ/mol).

1152

1153 **Figure 12.** Fraction of He remaining during isothermal heating at 250°C as a function of time
1154 from grains of apatite, titanite, zircon, monazite and rutile. Curves are plotted using the diffusion
1155 parameters from Cherniak et al. (2009) for zircon and apatite, Cherniak and Watson (2011) for
1156 rutile and titanite and this study for monazite. Spherical geometry (with grain radii of 50 μm for
1157 monazite and titanite, 200 μm radii for apatite) and the analytical expression for fraction of
1158 diffusant lost from a sphere (Crank, 1975) are used for apatite, monazite and titanite since no
1159 anisotropy is observed, while cylindrical geometry (with grain radii of 50 μm and lengths of 100
1160 μm) and the CYLMOD code (Watson et al., 2010) are used to calculate fractional He loss for
1161 rutile and zircon given their anisotropy of diffusion. For grains of roughly equivalent size,

1162 monazite should be most retentive of He, followed by rutile, zircon and titanite. Apatite is the
1163 least retentive of He among these accessory mineral phases. See text for additional discussion.

1164

1165

1166

Figure 1

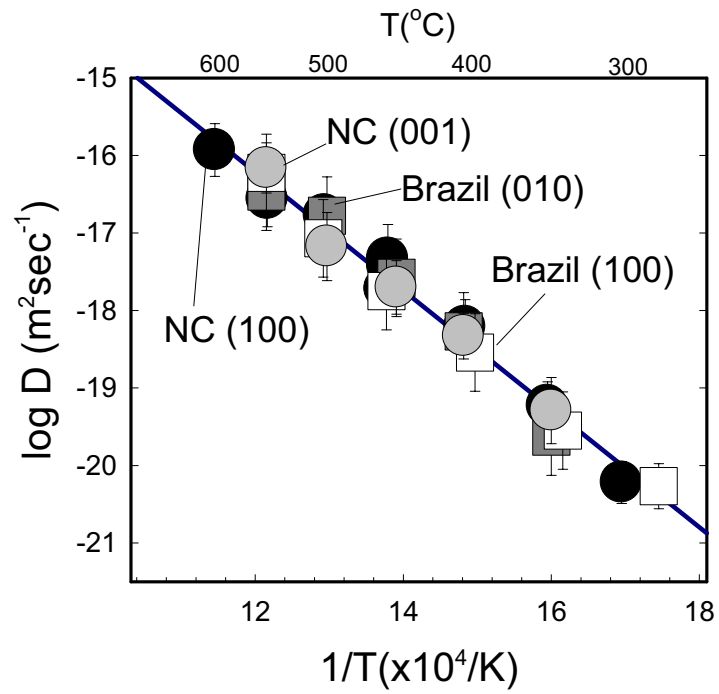


Figure 2

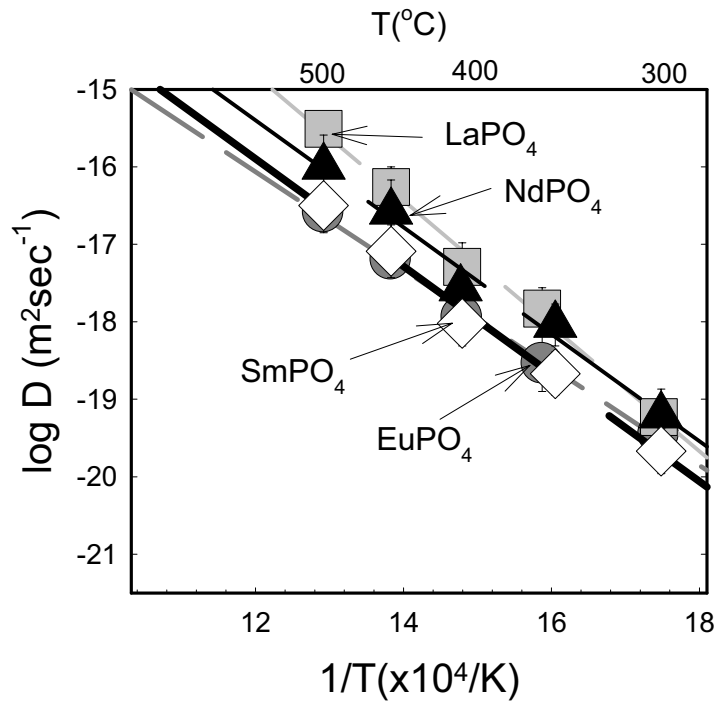


Figure 3

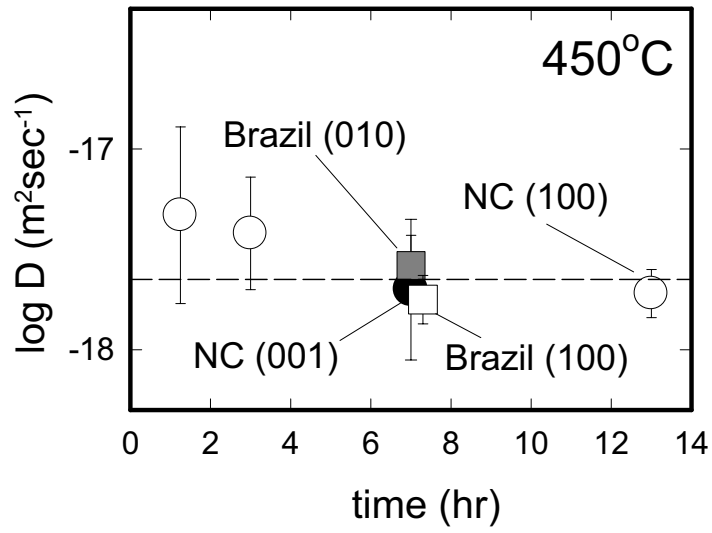


Figure 4a

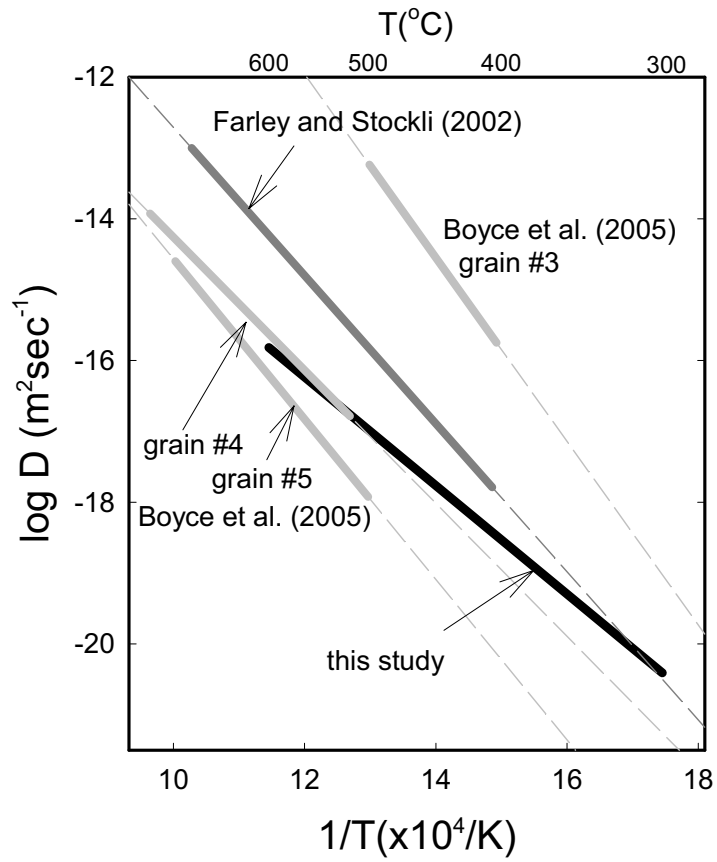


Figure 4b

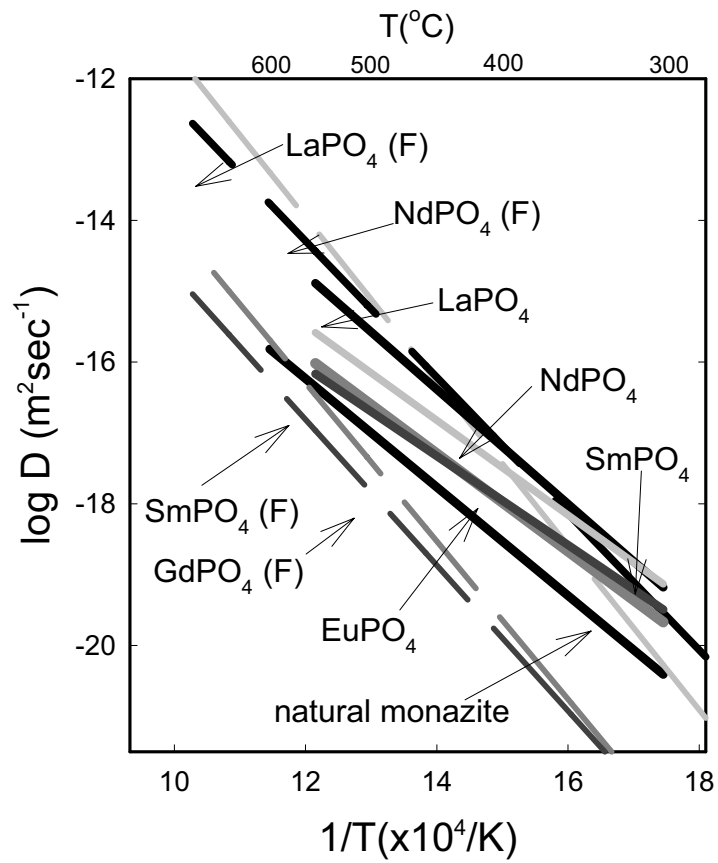


Figure 5a

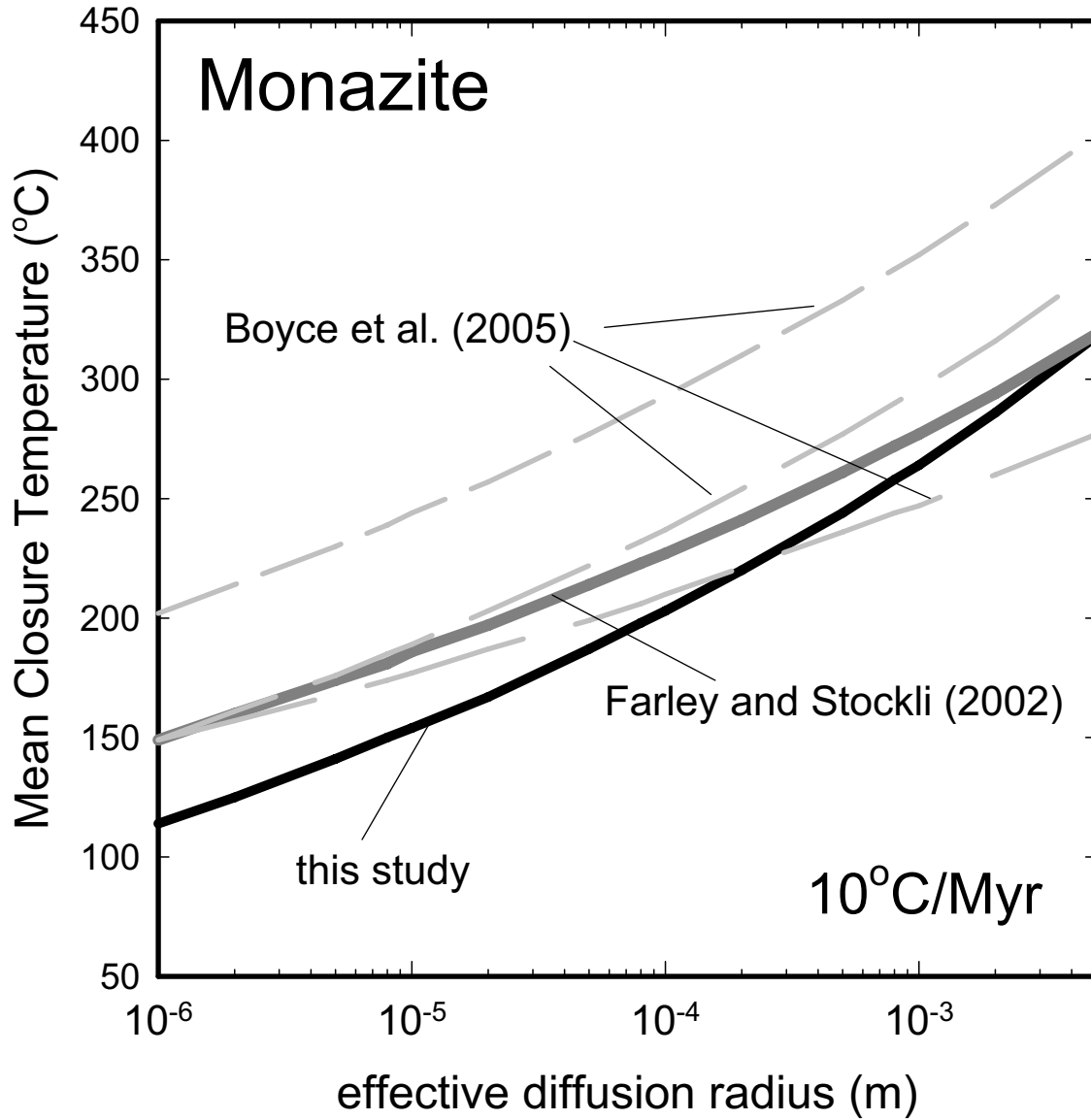


Figure 5b

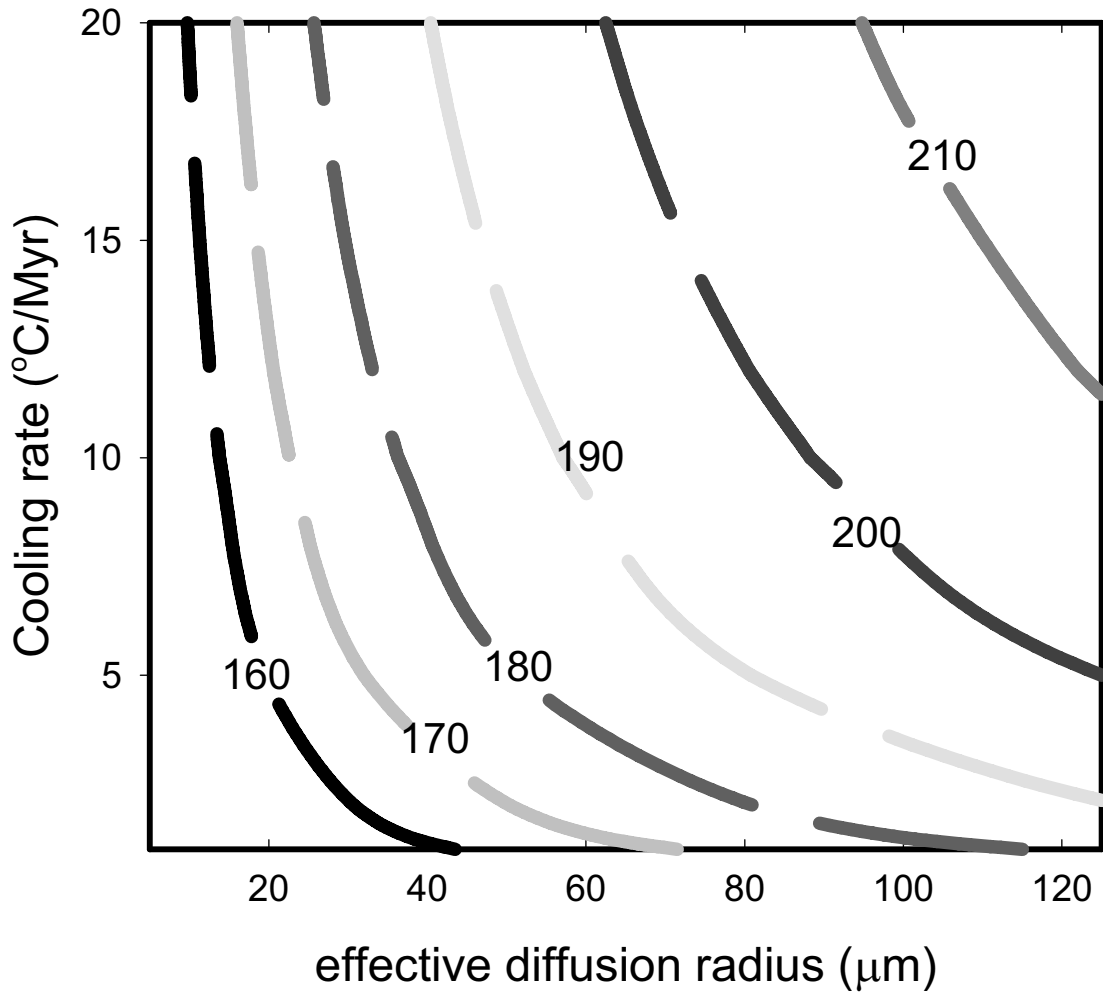


Figure 6

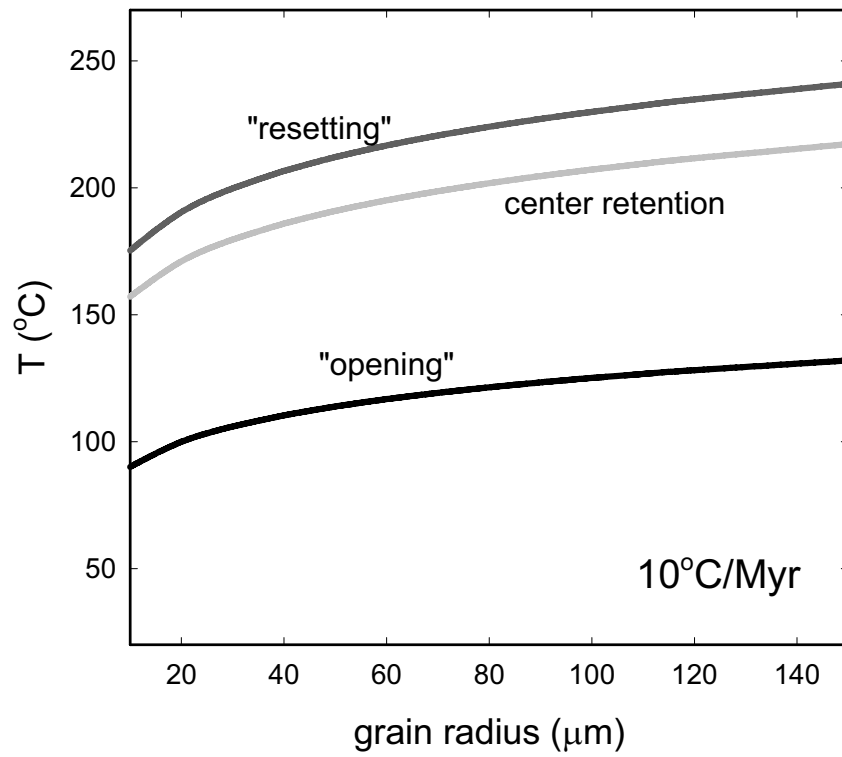


Figure 7.

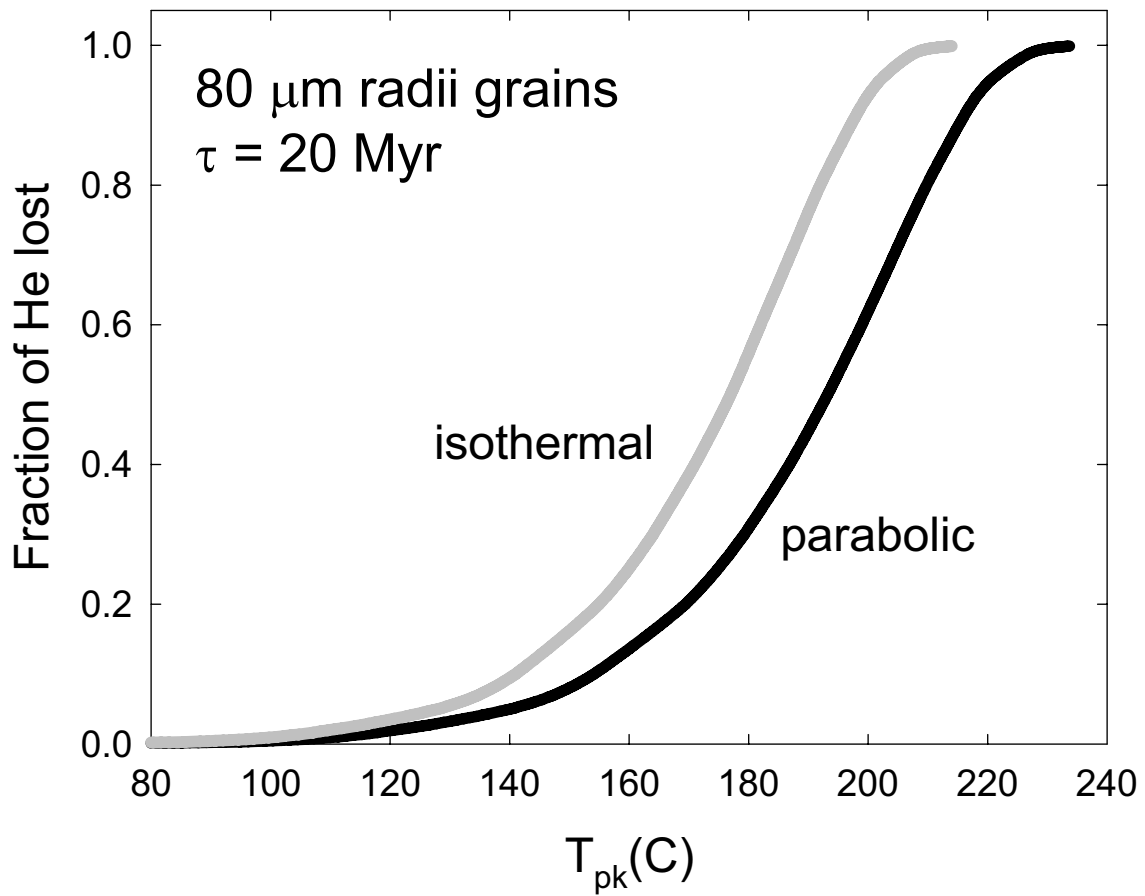


Figure 8

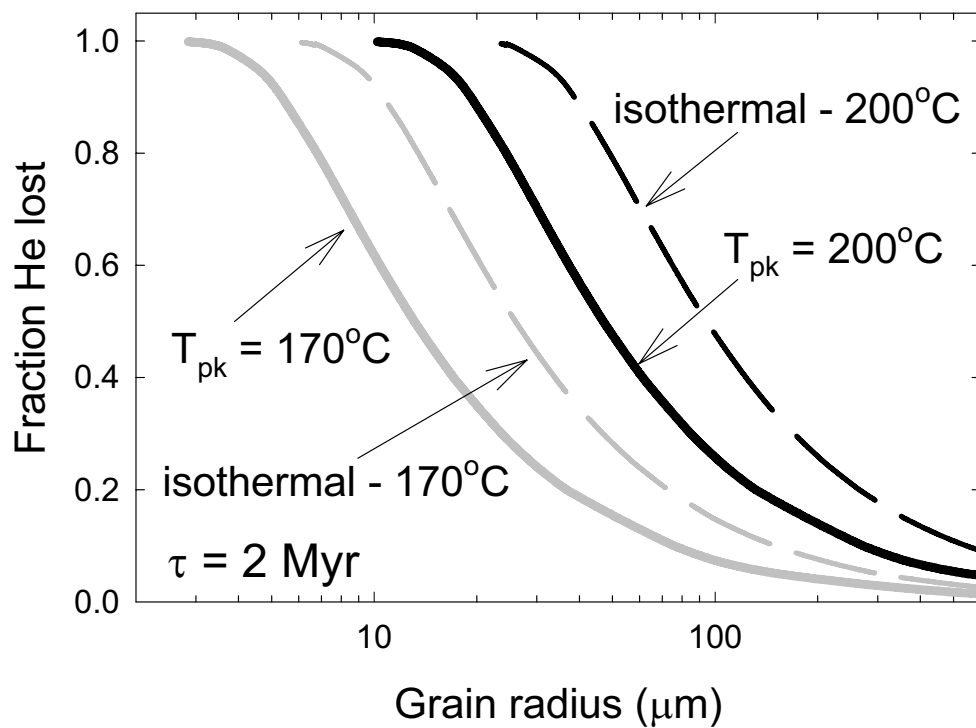


Figure 9

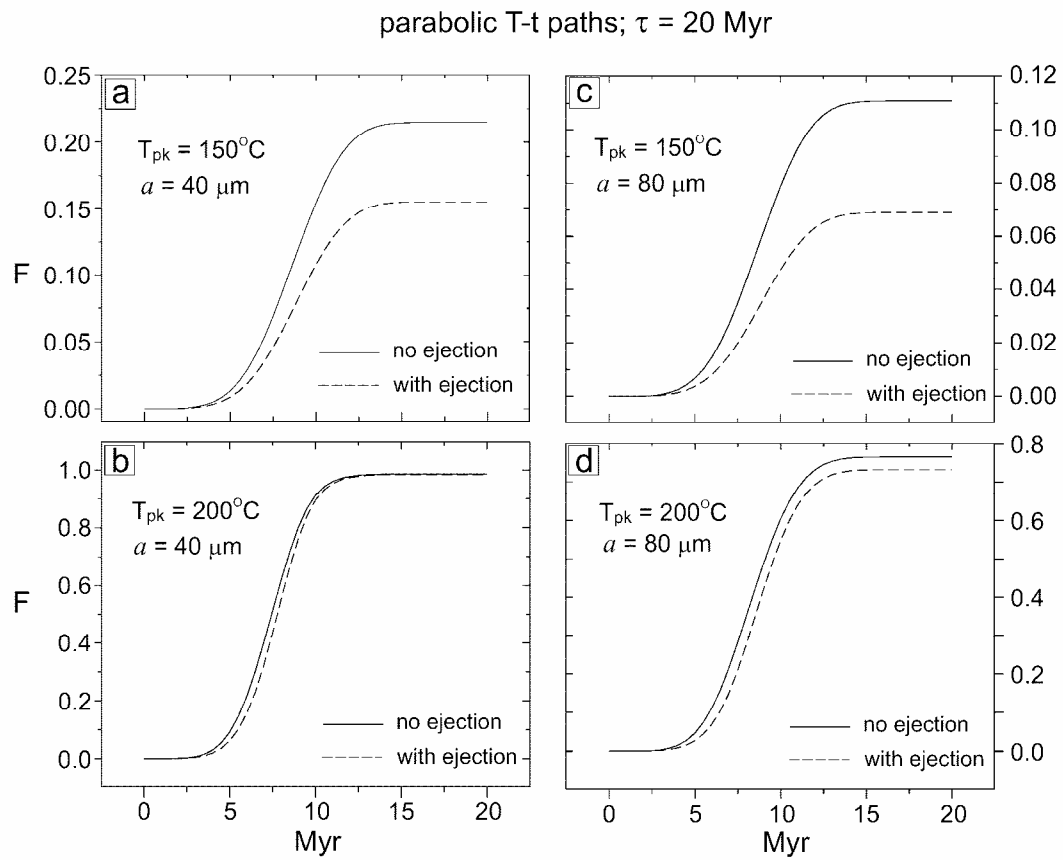


Figure 10

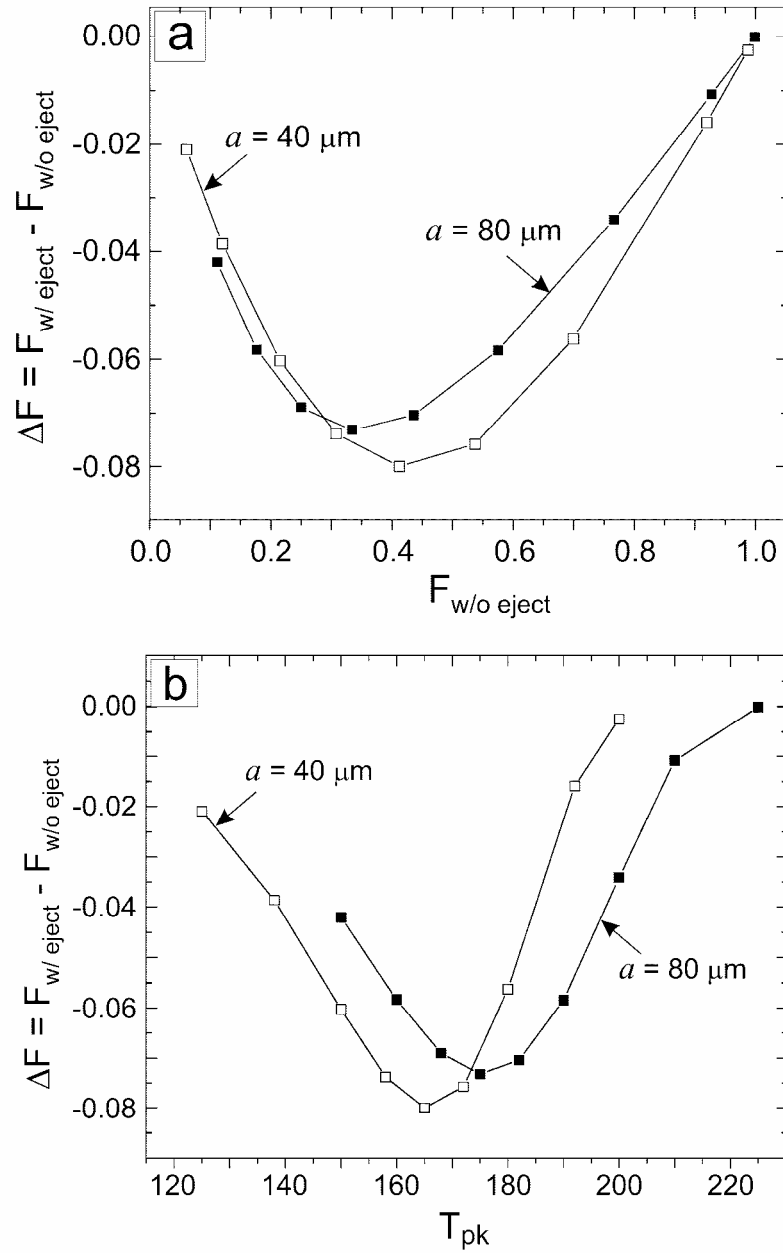


Figure 11

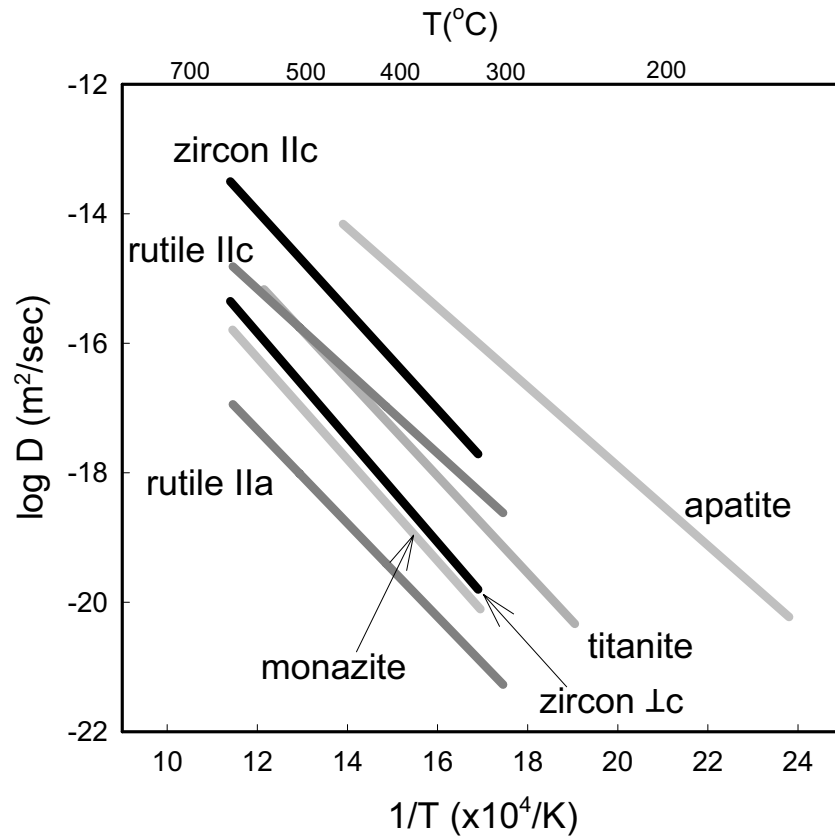


Figure 12

